

OUTCOMES-BASED EDUCATION (OBE) COURSE SYLLABUS

Stat 121 Mathematical Statistics I

Quality Goals of the Faculty of Natural and Mathematical Sciences

- 1. Provide quality instruction, research, extension, and innovation for global competitiveness;
- 2. Develop knowledgeable, skilled, and innovative individuals who value and pursue the advancement of scientific knowledge for the betterment of society; and
- 3. Produce future-proof graduates and workforce in biology, biotechnology, chemistry, mathematics, meteorology, physics, and statistics.

Quality Objectives of the Department Statistics

- 1. Produce highly trained graduates in Statistics;
- 2. Undertake quality instruction, research, and extension activities in statistics and allied fields;
- 3. Actively promote the appropriate utilization of statistics among scientists, technologists, and development workers; and
- 4. Maintain productive linkages and cooperation with statistical units and agencies locally and internationally.

I. PROGRAM INFORMATION

1.	Name of the Program	Bachelor of Science in Statistics
2.	CHED CMO Reference	CMO No. 42 s2017
3.	BOR Approval	BOR Resolution No. 61 s2018

4. Program Educational Objectives and Relationship to Institution Mission

Program Educational Objectives	N	Mission*			
Program Educational Objectives	а	b	С		
A number of graduates hold key statistical positions in government line agencies.	√	<	✓		
2. Some of the graduates become regular instructors in High School.	✓	✓	✓		
3. The top-ranking graduates are teaching in HEIs with at least an MS degree.	√	✓	√		
4. A fraction of the graduates are employed as statisticians and/or researchers in research centers and private companies with research units.	√	✓	>		
5. Some of the graduates are engaged in consultancy services in market research and project monitoring, and evaluation work.	✓	✓	√		

^{*}a - produce graduates equipped with advanced knowledge and lifelong learning skills, b - ethical standards through high-quality instruction and innovative research, c – impactful community engagements



III. COURSE INFORMATION

1. Course Code	STAT 121					
2. Course Title	Mathematical Statistics I					
3. Pre-requisite	Math 112s (Set Theory/Logic)					
	Math 114s (Calculus 1)					
4. Co-requisite	None					
5. Credit	4 units					
6. Semester Offered	1st semester					
7. Number of hours	4 hrs. lecture per week					
8. Course Description	Elements of probability; random variables; discrete and					
	continuous random variables; probability distributions; special					
	distributions; mathematical expectations; multivariate probability					
	distributions					
9. Sustainable	SDG 4 - Ensure Inclusive and Equitable Quality Education and					
Development Goals	Promote Lifelong Learning Opportunities for All					
10. 4th Industrial	Artificial Intelligence (AI) Gemini					
Revolution (4IR)	- , ,					
11. Education 5.0	Collaborative Learning, Technology at its Core, and Lifelong					
	Learning.					

12. Program Outcomes and Relationship to Program Educational Objectives									
	Program Outcomes (POs)				Program Educational Objectives				
		1	2	3	4	5			
Commor	n to All Baccalaureate Programs	1	1	1					
а	Articulate and discuss the latest developments in the practice of Statistics (PQF Level 6 descriptor)			✓	✓	✓			
b	Effectively communicate orally and in writing using both the English and Filipino languages.	√		✓	^	✓			
С	Work effectively and independently in multi-disciplinary and multi-cultural teams (PQF Level 6 descriptor)	✓		✓	✓	✓			
d	Demonstrate professional, social, and ethical responsibility, especially in practicing intellectual property rights and sustainable development.	✓		√	✓	✓			
е	Preserve and promote "Filipino historical and cultural heritage" (based on RA 7722)								
Commor	n to the Science and Mathematics Programs								
f	Demonstrate broad and coherent knowledge and understanding in the core areas of the physical and natural sciences and mathematics								
g	Apply critical and problem solving skills using the scientific method	✓		√	√	√			
h	Interpret scientific data and make judgments that include reflection on relevant scientific and ethical issues	✓		√	^	✓			
i	Carry out basic mathematical and statistical computations and use appropriate technologies in the analysis of data	✓		√	✓	√			
j	Communicate information, ideas, problems, and solutions, both orally and in writing, to other scientists, decision-makers, and the public	✓		>	√	>			
k	Relate science and mathematics to the other disciplines			√	√	✓			

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I	Design and perform safe and responsible techniques and procedures in laboratory or field practices	✓		✓	✓	✓
m	Critically evaluate inputs from others	✓		✓	√	✓
n	Appreciate the limitations and implications of science in everyday life	√		√	✓	✓
0	Commit to the integrity of data	✓		✓	✓	√
Specific	to the BS Statistics Program	•	•	•		
р	Demonstrate broad and coherent knowledge and understanding in the core areas of statistics, computing, and mathematics	√	√	✓	~	\
q	Generate information involving the conceptualization of a strategy for generating timely and accurate/reliable data, organizing a process for putting together or compiling the needed data, and transforming available data into relevant and useful forms	✓		✓	√	✓
r	Translate real-life problems into statistical problems	√		√	√	✓
S	Identify appropriate statistical tests and methods and use these properly for the given problems, select optimal solutions to problems, and make decisions in the face of uncertainty	√		✓	✓	✓

13. Course Outcomes (COs) and Relationship to Program Outcomes (POs)																			
Program Outcomes										Out									
Addressed by the Course Outcomes																			
By the end of the course, the students must be able to:	а	b	С	d	е	f	g	h	i	j	k	I	m	n	0	р	q	r	S
CO 1: Compute the probability of events	L	P				L	L	P	L	0	0			L		L	P	P	L
CO 2: Evaluate the distributional properties of discrete random variables	L	P				L	L	P	L	0	0			L		L	P	P	L
CO 3: Evaluate the distributional properties of continuous random variables	L	P				L	L	P	L	0	0			L		L	P	P	L
CO 4: Derive properties of multivariable distributions	L	P				L	L	P	L	0	0			L		L	P	P	L

L: facilitates learning of competency Level:

P: allows student to practice competency (no input, but competency is evaluated)
O: opportunity for development (no input or evaluation, but competency is practiced)

14. OB	TL Course Content and P	lan	\	
Week	Topics	Learning Outcomes	Teaching and Learning Activities	

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			Teaching Activities	Learning Activities	Assess- ment Tasks
1	 Class Orientation VSU Vision Mission, and Quality Policy Statement OBE Course Syllabus (Course Content, Class Policies, Requirements, Grading System, etc.) Values Integration: Open-mindedness and proper netiquette 	 State the VSU Vision, Mission and Quality Policy. Describe and explain the important features of the course Apply proper netiquette during virtual classes 	Conduct virtual classes/ meetings Solicit question, and feedback from students	Asking question s about the course Sharing of expectati ons	Quiz No. 0 (warm up essay- type quiz)
CO 1 :	Compute probability of ever Module 1.		1	T	Problem
	Introduction to Probability Lesson 1.1 Properties of Probability Lesson 1.2 Counting Methods Lesson 1.3 Conditional Probability Lesson 1.4 Independent Events Lesson 1.5 Law of Total Probability and Bayes Theorem	 Explain what is probability, Differentiate the ways of assigning probabilities to events, Explain the difference between permutation and combination, Apply permutation and combination in assigning probabilities to events, Explain the idea and compute of conditional probability, Apply the multiplication rule of probability, Determine if two or more events are independent, Compute the probability of the intersection of two or more independent events, and Articulate and apply Bayes' Theorem to find the conditional probability. 	 Lectures Demonst rations Proving and deriving statistical results Classroo m exercises and assessm ent tasks 	 Solving Learning Tasks Solving Assessm ent Tasks Asking questions and clarificati ons on solutions to class exercises and problem sets 	Set 1 Problem Set 2 Quiz No. 1 Quiz No. 2 First Long Exam
	Evaluate the distributional p	roperties of discrete			
6-10	Module 2. Discrete Random Variables and	Explain the intuitive and formal definition	LecturesDemonst rations	Solving Learning Tasks	ProblemSet 3Problem

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				T		
	Their Probability		of a random variable,	Proving	Solving	Set 4
	Distribution	2.	Construct the	and	Assessm	• Quiz No. 3
	Lesson 2.1		probability mass	deriving	ent Tasks	Qu 1101 0
	Random Variables		function and	statistical	Asking	• Quiz No. 4
	and Their Probability		cumulative distribution	results	questions	0 1
	Distribution		function of a	• Classroo	and	Second Long
	Lesson 2.2		discrete random	m	clarificati	Long Exam
	Mathematical	_	variable	exercises and	ons on	Exam
	Expectation	3.	Articulate the meaning and	assessm	solutions	
	Lesson 2.3		properties of	ent tasks	to class	
	Moment Generating		mathematical	CIII lasks	exercises	
	Functions	١,	expectation,		and	
	Lesson 2.4	4.	Determine expected value of		problem sets	
	The Binomial		a discrete random		Seis	
	Distribution		variable,			
		5.	Determine the			
	Lesson 2.5		moment generating			
	The Geometric and		function (mgf) of			
	Negative Binomial		a discrete random			
	Distributions	6	variable,			
	Lesson 2.6	6.	Apply the mgf in finding the mean			
	The Hypergeometric		and variance of a			
	Distribution		discrete random			
	Lesson 2.7	7.	variable, Familiarize with			
	The Poisson	١٠.	common discrete			
	Distribution		probability			
			distributions,			
		8.	Derive the mean and variance of			
			discrete			
			probability			
			distributions, and			
		9.	Solve problems associated with			
			discrete			
			probability			
			distributions.			
	Evaluate the distributional	pro	perties of continu	ous random v	ariables	
11-15	Module 3	1.	Explain the	 Lectures 	 Solving 	Problem
	Continuous Random		definition of probability density	 Demonst 	Learning	Set 5
	Variables and Their		function (pdf) and	rations	Tasks	Problem
	Probability Distribution		cumulative	 Proving 	Solving	Set 6
	Lesson 3.1		distribution	and	Assessm	_
	Probability Density		function (CDF) of continuous	deriving	ent Tasks	• Quiz No. 5
	Function and		random variables,	statistical	Asking	• Quiz No. 6
	Cumulative	2.	Derive the pdf	results	questions	- QUIZ 140. 0
	Distribution Function		from the CDF and	Classroo	and	Third Long
	of Continuous	3.	vice versa, Compute	m	clarificati	Exam
	Random Variables	٥.	probabilities	exercises	ons on	
	Lesson 3.2		associated with a	and	solutions	
	Mathematical		continuous	assessm ent tasks	to class	
	Expectation for		random variable using either its	GIII IASKS	exercises	
	Continuous Random		pdf or CDF,		and	
	Variables	4.	Determine		problem sets	
	vailables		expected value of		3513	
		1				

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Lesson 3.3 The Uniform Distribution Lesson 3.4 The Normal Distribution Lesson 3.5 The Gamma Distribution Lesson 3.6 The Exponential Distribution Lesson 3.7 The Chi-Square Distribution Lesson 3.8 The Beta Distribution	a discrete random variable, 5. Determine the moment generating function (mgf) of a continuous random variable 6. Familiarize with common discrete probability distributions, 7. Derive the mean and variance of discrete probability distributions, and 8. Solve problems associated with discrete probability distributions.	
16-18 Module 4. Multivariate Distributions Lesson 4.1 Joint Probability Distribution Lesson 4.2 Marginal Probability Distribution Lesson 4.3 Conditional Probability Distribution Lesson 4.4 Independent Random Variables	 Describe joint and marginal distributions of discrete and continuous random variables; Derive joint and marginal distributions of discrete and continuous random variables, and conditional distributions of discrete and continuous random variables; and continuous random variables; and Derive conditional distributions of discrete and continuous random variables; and Explain the concept of independent random variables. Lectures Demonst rations Proving and deriving statistical results Classroo mexercises and clarificati ons on solutions to class exercises and problem sets 	Quiz No. 8 Fourth Long Exam

15. Life-long Learning Opportunities

Students will be encouraged to practice solving additional probability problems in other textbooks so that they will become more proficient and prepared when they enrol in Mathematical Statistics II.

16. Contribution of Course to Meeting the Professional Component

General Education: 0 %
Mathematical Component: 40%
Statistical Component: 60%

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17. References and Other Learning Resources

A. Textbooks

- 1. Mendenhall, W., Scheaffer, R. L., and Wackerly, D. D. (2008). *Mathematical Statistics with Applications*, 7th ed. Brooks/Cole, Cenage Learning.
- 2. Hogg, R. V., Tanis, E. A., and Zimmerman, D. L. (2015). *Probability and Statistical Inference*, 9th ed. Pearson Education, Inc.
- 3. Hogg, R.V. and Craig, A. T. (2004). *Introduction to Mathematical Statistics*, Fifth Edition, Macmillan Publishing Co., Inc., N.Y.
- 4. Ramachandran, K. M. and Tsokos, C. P. (2009). *Mathematical Statistics with Applications*. Elsevier Inc.
- 5. Miller, I. and Miller, M. (1999). John E. Freund's *Mathematical Statistics*. 6th ed. Prentice-Hall Int'I., Inc. New Jersey.
- 6. Mood, Graybill, and Boes. 1974. *Introduction to the Theory of Statistics*. Third Edition. International Student Edition. McGraw-Hill Kogakusha, Ltd.

B. Learning Guide

- Milla, N. E. (2021). Student Learning Guide in Stat 121 (Mathematical Statistics
 1)
- **C. Other Learning Resources** (Journals, Videos, Websites, Webinars, Open Educational Resources, etc.)
 - 1. https://online.stat.psu.edu/stat414/

18. Course Assessment and Evaluation

The performance of students will be assessed and evaluated based on the following:

Item No,	Assessment Tasks	Percentage Contribution (1)	No. of Times in the Semester (2)	Individual Task % Contribution (1/2)
1	Quizzes (Q)	15	8	1.875/Q
2	Problem Sets (PS)	25	8	3.125/PS
3	Long Examinations (LE)	60	4	15/LE

Grading System (60% Passing)

Grading System (60%	o Passing)		
Range	Grade	Range	Grade
98-100	1.00	53-59	3.25
95-97	1.25	46-52	3.50
90-94	1.50	39-45	3.75
85-89	1.75	32-38	4.00
80-84	2.00	25-21	4.25
75-79	2.25	18-24	4.50
70-74	2.50	11-17	4.75
65-69	2.75	0-10	5.0
60-64	3.00		

19. Course Policies

A. Instructional materials such as lecture guides and assessment tasks are made available to all students via GitHub (https://github.com/bertmilla76/Stat-121-Mathematical-Statistics-I). Students are encouraged to read the lecture guides before coming to class.

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- B. Classes are conducted **face-to-face**, but under rare circumstances, class sessions may be delivered virtually using either ZOOM or Google Meet. The FB Messenger Chat Group will be used for easy and faster communication and consultations.
- C. **Submission of Course Requirements**. Quizzes, problem sets, and long examinations are administered during face-to-face class sessions. Instructions on how to submit the answers to quizzes, problem sets, and long examinations are provided in each course requirement.
- D. Queries and Clarifications. For queries, clarifications, or urgent questions, a student may contact the course instructor during the official class schedule, Monday to Friday only, using the contact information given at the last part of this document or via the FB Messenger Group Chat.
- E. All students are reminded to observe all policies, regulations, and rules of the university (particularly on attendance and cheating) and other related laws of the land and are advised to read, understand, and practice the provisions of the VSU Student Manual.
- F. **NO REMOVAL EXAMINATION!** INC mark shall be given to students per BOR-Approved Policies.

These class policies shall serve as our written agreement for the whole semester. The students will be informed immediately of any changes to these policies that may arise for reasons of improving the delivery of the quality of instruction for the betterment of the Teaching and Learning process.

20. Course Materials and Facilities Available

Student Learning Guide (online via GitHub)
Facebook Messenger Group Chat
Statistics Computing Laboratory

21. Revision History				
Revision	Date of	Date of	Highlights of	Revised by
number	Revision	implementation	Revision	
7	August 7,	1st Sem., AY 2025-	•	Norberto E. Milla, Jr.
	2025	2026	vision and mission, the course content, the references, and adjusted the class policies to suit flexible learning Revised the	
			grading scheme	
			 Updated to 	
			conform with form	
			TP-IMD-08 v04 01-	
			23-2025	

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6	August 8, 2023	1 st Sem., AY 2023- 2024	Revised the teaching and learning activities and the classroom assessment (including grading requirements) to fit face-to-face classes. Norberto E. Milla, Jr.
5	July 2021	1 st Sem., SY 2020- 2021	 Revised and simplified the course policies particularly on the submission of student output. Norberto E. Milla, Jr.
4	January 2021	1 st Sem., SY 2020- 2021	 Revised to conform with form TP-IMD- 08 v3 Norberto E. Milla, Jr.
3	July 2020	1 st Sem., SY 2020- 2021	 Revised based on the self-learning modules prepared for flexible learning due to COVID-19 pandemic Norberto E. Milla, Jr.
2	July 2019	1 st Sem., SY 2019- 2020	Updating the course content and course outcomes. Norberto E. Milla, Jr.
1	July 2018	1 st Sem., SY 2018- 2019	Updating of the VSU's vision and mission, the references, and course policies. Norberto E. Milla, Jr.
0	July 2017		Original OBEdized syllabus in Mathematical Statistics I incorporating the topics indicated in the CMO for BS Statistics. Norberto E. Milla, Jr.

22. Preparation			
Dropared by	Name	Signature	Date Signed
Prepared by	NORBERTO E. MILLA, JR.		

INSTRUCTOR/PROFESSOR INFORMATION IV.

Name of Instructor/Professor	NORBERTO E. MILLA, JR.
2. Office and Department	Faculty Room No.1 (Annex), Department of Statistics
3. Telephone/Mobile Numbers	+63 9473941899
4. Email Address	bertmilla@vsu.edu.ph
5. Consultation Time	

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23. Department Instructional Materials Review Committee:

Committee	Name	Signature	Date Signed
Member:	VIRGELIO M. ALAO		
Member:	NORBERTO E. MILLA, JR.		
Chairperson:	DONNA C. CUYNO		

	Name	Signature	Date Signed
Noted by:	REV RHIZZA L. AURE		
	Dean, FNMS		
Verified by:	MARK GIL A. VEGA Head, IMDO		
Validated by:	MA. RACHEL KIM L. AURE Director, IEO		