

# HW1-Programming

● Graded

## Student

Brian Bertness

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## Total Points

25 / 25 pts

## Autograder Score

18.0 / 18.0

## Passed Tests

test\_C1Fit (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_C1Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_C2Fit (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_C2Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_C3Fit (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_C3Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_computeCov (test\_MyDiscriminant.TestMyDiscriminant) (2/2)  
test\_computeMean (test\_MyDiscriminant.TestMyDiscriminant) (1/1)  
test\_computePrecision (test\_MyDiscriminant.TestMyDiscriminant) (1/1)  
test\_computePrior (test\_MyDiscriminant.TestMyDiscriminant) (1/1)  
test\_computeRecall (test\_MyDiscriminant.TestMyDiscriminant) (1/1)

## Question 2

[Code Sanity](#)

7 / 7 pts

✓ - 0 pts Correct

## Autograder Results



This test the fit function of classifier C1

Your S for both classes are:

```
[[[ 1.43781459  1.24407538  1.4050195  1.25014251  0.44606905
    0.21774186  1.12986533  2.42769858]
 [ 1.24407538  3.84355238  4.36296535  1.22208113  1.48580304
    0.51661422  0.50935232  6.4949891 ]
 [ 1.4050195  4.36296535  8.23386906  2.11785909  2.73801346
    1.56375799 -0.84281537  7.80134805]
 [ 1.25014251  1.22208113  2.11785909  3.99903851 -0.21275367
    1.08232519  1.01143298  3.2204665 ]
 [ 0.44606905  1.48580304  2.73801346 -0.21275367  2.81247403
   -0.12402908  0.86774363  2.13936869]
 [ 0.21774186  0.51661422  1.56375799  1.08232519 -0.12402908
    0.95087368 -0.46473474  1.86517572]
 [ 1.12986533  0.50935232 -0.84281537  1.01143298  0.86774363
   -0.46473474  3.96668692  1.63874881]
 [ 2.42769858  6.4949891  7.80134805  3.2204665  2.13936869
    1.86517572  1.63874881 14.54667084]]]
```

```
[[ 1.30424291  1.17675824  0.18340592  0.87089916  1.15054609
    0.7423137  1.07919291  1.84996001]
 [ 1.17675824  3.13097865 -0.16135333  0.43245499  1.20970531
    0.72685675  0.27247502  2.92221783]
 [ 0.18340592 -0.16135333  6.72650694  2.59256962  1.84112898
    1.50964579  2.03543038  6.93512008]
 [ 0.87089916  0.43245499  2.59256962  3.93849718  1.01394707
    1.98598543  2.27406539  4.73865443]
 [ 1.15054609  1.20970531  1.84112898  1.01394707  2.87137815
    0.83385036  2.25316578  3.38395507]
 [ 0.7423137  0.72685675  1.50964579  1.98598543  0.83385036
    2.37610777  1.18698751  2.33902631]
 [ 1.07919291  0.27247502  2.03543038  2.27406539  2.25316578
    1.18698751  6.44746773  2.55969108]
 [ 1.84996001  2.92221783  6.93512008  4.73865443  3.38395507
    2.33902631  2.55969108 19.39182337]]]
```

GT shared\_S are:

```
[[[ 1.43781459  1.24407538  1.4050195  1.25014251  0.44606905
    0.21774186  1.12986533  2.42769858]
 [ 1.24407538  3.84355238  4.36296535  1.22208113  1.48580304
    0.51661422  0.50935232  6.4949891 ]
 [ 1.4050195  4.36296535  8.23386906  2.11785909  2.73801346
    1.56375799 -0.84281537  7.80134805]
 [ 1.25014251  1.22208113  2.11785909  3.99903851 -0.21275367
    1.08232519  1.01143298  3.2204665 ]
 [ 0.44606905  1.48580304  2.73801346 -0.21275367  2.81247403
   -0.12402908  0.86774363  2.13936869]
 [ 0.21774186  0.51661422  1.56375799  1.08232519 -0.12402908
    0.95087368 -0.46473474  1.86517572]
 [ 1.12986533  0.50935232 -0.84281537  1.01143298  0.86774363
   -0.46473474  3.96668692  1.63874881]
 [ 2.42769858  6.4949891  7.80134805  3.2204665  2.13936869
    1.86517572  1.63874881 14.54667084]]]
```

```
[[ 1.30424291  1.17675824  0.18340592  0.87089916  1.15054609
   0.7423137  1.07919291  1.84996001]
 [ 1.17675824  3.13097865 -0.16135333  0.43245499  1.20970531
   0.72685675  0.27247502  2.92221783]
 [ 0.18340592 -0.16135333  6.72650694  2.59256962  1.84112898
   1.50964579  2.03543038  6.93512008]
 [ 0.87089916  0.43245499  2.59256962  3.93849718  1.01394707
   1.98598543  2.27406539  4.73865443]
 [ 1.15054609  1.20970531  1.84112898  1.01394707  2.87137815
   0.83385036  2.25316578  3.38395507]
 [ 0.7423137  0.72685675  1.50964579  1.98598543  0.83385036
   2.37610777  1.18698751  2.33902631]
 [ 1.07919291  0.27247502  2.03543038  2.27406539  2.25316578
   1.18698751  6.44746773  2.55969108]
 [ 1.84996001  2.92221783  6.93512008  4.73865443  3.38395507
   2.33902631  2.55969108 19.39182337]]]
```

### test\_C1Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)

This test the predictions of C1.

Your prediction are:

```
[2. 2. 2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 1.
 2. 2. 2. 2. 1. 1. 1. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.
 1. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 1. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2.
 2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2.
 2. 2. 2. 2.]
```

GT is:

```
[2. 2. 2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 1.
 2. 2. 2. 2. 1. 1. 1. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.
 1. 2. 2. 2. 2. 2. 1. 2. 2. 2. 2. 1. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2.
 2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2.
 2. 2. 2. 2.]
```

## test\_C2Fit (test\_MyDiscriminant.TestMyDiscriminant) (2/2)

This test the fit function of classifier C2

Your shared\_S are:

```
[[ 2.71394249 2.8980981 2.03005823 2.32788275 2.44556456 1.94408372
 2.11467397 3.87525675]
 [ 2.8980981 5.4016963 2.98814342 2.33615901 3.1401789 2.33936364
 1.62228674 6.22657007]
 [ 2.03005823 2.98814342 8.63209716 3.8712958 3.69177331 2.96198898
 2.29155721 9.07916957]
 [ 2.32788275 2.33615901 3.8712958 5.21078844 2.1280328 3.02302387
 2.8862445 6.06305947]
 [ 2.44556456 3.1401789 3.69177331 2.1280328 4.44793178 2.02884713
 2.94510795 5.02238615]
 [ 1.94408372 2.33936364 2.96198898 3.02302387 2.02884713 3.25654972
 1.71047814 4.01132185]
 [ 2.11467397 1.62228674 2.29155721 2.8862445 2.94510795 1.71047814
 6.38519461 3.66022826]
 [ 3.87525675 6.22657007 9.07916957 6.06305947 5.02238615 4.01132185
 3.66022826 20.18824015]]
```

GT shared\_S are:

```
[[ 2.71394249 2.8980981 2.03005823 2.32788275 2.44556456 1.94408372
 2.11467397 3.87525675]
 [ 2.8980981 5.4016963 2.98814342 2.33615901 3.1401789 2.33936364
 1.62228674 6.22657007]
 [ 2.03005823 2.98814342 8.63209716 3.8712958 3.69177331 2.96198898
 2.29155721 9.07916957]
 [ 2.32788275 2.33615901 3.8712958 5.21078844 2.1280328 3.02302387
 2.8862445 6.06305947]
 [ 2.44556456 3.1401789 3.69177331 2.1280328 4.44793178 2.02884713
 2.94510795 5.02238615]
 [ 1.94408372 2.33936364 2.96198898 3.02302387 2.02884713 3.25654972
 1.71047814 4.01132185]
 [ 2.11467397 1.62228674 2.29155721 2.8862445 2.94510795 1.71047814
 6.38519461 3.66022826]
 [ 3.87525675 6.22657007 9.07916957 6.06305947 5.02238615 4.01132185
 3.66022826 20.18824015]]
```

## test\_C2Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)

This test the predictions of C2.

Your prediction are:

[2. 2. 2. 1. 2. 1. 1. 2. 1. 1. 2. 1. 2. 1. 2. 2. 1. 2. 2. 2. 2. 1. 2. 1.  
2. 2. 2. 2. 1. 1. 1. 2. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.  
1. 2. 2. 2. 2. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 2. 2.  
2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 1. 2. 2. 1. 2. 2. 2. 2.  
2. 2. 2. 2.]

GT is:

[2. 2. 2. 1. 2. 1. 1. 2. 1. 1. 2. 1. 2. 1. 2. 2. 1. 2. 2. 2. 2. 1. 2. 1.  
2. 2. 2. 2. 1. 1. 1. 2. 2. 2. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.  
1. 2. 2. 2. 2. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 2. 2.  
2. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 2. 2. 2. 1. 2. 2. 1. 2. 2. 2. 2.  
2. 2. 2. 2.]

## test\_C3Fit (test\_MyDiscriminant.TestMyDiscriminant) (2/2)

This test the fit function of classifier C3, you need to cast the non-diagonal entries to 0  
also don't forget to weighted combine S1/S2 to get the shared\_S

Your shared\_S are:

```
[[ 2.71394249 0.      0.      0.      0.      0.
   0.      0.    ]
 [ 0.      5.4016963 0.      0.      0.      0.
   0.      0.    ]
 [ 0.      0.      8.63209716 0.      0.      0.
   0.      0.    ]
 [ 0.      0.      0.      5.21078844 0.      0.
   0.      0.    ]
 [ 0.      0.      0.      0.      4.44793178 0.
   0.      0.    ]
 [ 0.      0.      0.      0.      0.      3.25654972
   0.      0.    ]
 [ 0.      0.      0.      0.      0.      0.
   6.38519461 0.    ]
 [ 0.      0.      0.      0.      0.      0.
   0.      20.18824015]]
```

GT shared\_S are:

```
[[ 2.71394249 0.      0.      0.      0.      0.
   0.      0.    ]
 [ 0.      5.4016963 0.      0.      0.      0.
   0.      0.    ]
 [ 0.      0.      8.63209716 0.      0.      0.
   0.      0.    ]
 [ 0.      0.      0.      5.21078844 0.      0.
   0.      0.    ]
 [ 0.      0.      0.      0.      4.44793178 0.
   0.      0.    ]
 [ 0.      0.      0.      0.      0.      3.25654972
   0.      0.    ]
 [ 0.      0.      0.      0.      0.      0.
   6.38519461 0.    ]
 [ 0.      0.      0.      0.      0.      0.
   0.      20.18824015]]
```

## test\_C3Predict (test\_MyDiscriminant.TestMyDiscriminant) (2/2)

This test the predictions of C3.

Your prediction are:

[1. 2. 1. 1. 2. 1. 1. 2. 1. 1. 2. 1. 2. 1. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1.  
2. 2. 2. 2. 1. 1. 1. 2. 2. 1. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.  
1. 2. 2. 2. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 1. 1. 1. 1. 2. 1. 2. 2. 2.  
2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 1. 2. 2. 1. 1. 2. 2. 2.  
2. 2. 2. 2.]

GT is:

[1. 2. 1. 1. 2. 1. 1. 2. 1. 1. 2. 1. 2. 1. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1.  
2. 2. 2. 2. 1. 1. 1. 2. 2. 1. 1. 1. 2. 2. 1. 2. 2. 2. 2. 2. 1. 2. 2. 2.  
1. 2. 2. 2. 1. 2. 1. 2. 2. 2. 1. 1. 2. 1. 2. 1. 1. 1. 1. 2. 1. 2. 2. 2.  
2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 1. 1. 2. 2. 1. 1. 2. 2. 2.  
2. 2. 2. 2.]





This test the computeCov() helper functions.

We randomly generate 5 sets with 10\*8 shape to find the COV

-----

Your solution at Test 0 is:

```
[[ 0.0889507 -0.01647154 -0.02153902 -0.011146  0.01614989 0.04350251
   0.02469651 0.0287701 ]
 [-0.01647154 0.06973672 0.0388712 -0.01590982 0.00395175 -0.05082096
  -0.01641289 0.0018101 ]
 [-0.02153902 0.0388712 0.06625452 -0.01803218 0.01763471 0.00027809
  -0.01957927 0.00916325]
 [-0.011146 -0.01590982 -0.01803218 0.02375462 -0.00240452 -0.00639558
   0.00577777 -0.01034688]
 [ 0.01614989 0.00395175 0.01763471 -0.00240452 0.07941694 -0.0106533
   0.07544718 0.05285736]
 [ 0.04350251 -0.05082096 0.00027809 -0.00639558 -0.0106533 0.10160804
  -0.02614318 0.00096413]
 [ 0.02469651 -0.01641289 -0.01957927 0.00577777 0.07544718 -0.02614318
   0.11150464 0.06342069]
 [ 0.0287701 0.0018101 0.00916325 -0.01034688 0.05285736 0.00096413
   0.06342069 0.06656478]]
```

GT is:

```
[[ 0.0889507 -0.01647154 -0.02153902 -0.011146  0.01614989 0.04350251
   0.02469651 0.0287701 ]
 [-0.01647154 0.06973672 0.0388712 -0.01590982 0.00395175 -0.05082096
  -0.01641289 0.0018101 ]
 [-0.02153902 0.0388712 0.06625452 -0.01803218 0.01763471 0.00027809
  -0.01957927 0.00916325]
 [-0.011146 -0.01590982 -0.01803218 0.02375462 -0.00240452 -0.00639558
   0.00577777 -0.01034688]
 [ 0.01614989 0.00395175 0.01763471 -0.00240452 0.07941694 -0.0106533
   0.07544718 0.05285736]
 [ 0.04350251 -0.05082096 0.00027809 -0.00639558 -0.0106533 0.10160804
  -0.02614318 0.00096413]
 [ 0.02469651 -0.01641289 -0.01957927 0.00577777 0.07544718 -0.02614318
   0.11150464 0.06342069]
 [ 0.0287701 0.0018101 0.00916325 -0.01034688 0.05285736 0.00096413
   0.06342069 0.06656478]]
```

-----

Your solution at Test 1 is:

```
[[ 0.05479457 0.00776728 0.02819913 0.04859511 0.0486294 0.01835938
  -0.01093299 0.04941813]
 [ 0.00776728 0.07361011 0.00340686 0.04364852 0.00536263 0.02299631
   0.01113939 0.03204267]
 [ 0.02819913 0.00340686 0.08482313 0.06943254 0.01998049 0.08094043
  -0.01020302 0.03810356]
 [ 0.04859511 0.04364852 0.06943254 0.10562777 0.04529594 0.0845132
  -0.0202048 0.07262209]
 [ 0.0486294 0.00536263 0.01998049 0.04529594 0.05543721 0.01407108
  -0.02652481 0.04746691]
 [ 0.01835938 0.02299631 0.08094043 0.0845132 0.01407108 0.10330048
  -0.0115905 0.05731749]
 [-0.01093299 0.01113939 -0.01020302 -0.0202048 -0.02652481 -0.0115905
```

0.09447296 -0.04330112]  
[ 0.04941813 0.03204267 0.03810356 0.07262209 0.04746691 0.05731749  
-0.04330112 0.1105482 ]]

GT is:

[[ 0.05479457 0.00776728 0.02819913 0.04859511 0.0486294 0.01835938  
-0.01093299 0.04941813]  
[ 0.00776728 0.07361011 0.00340686 0.04364852 0.00536263 0.02299631  
0.01113939 0.03204267]  
[ 0.02819913 0.00340686 0.08482313 0.06943254 0.01998049 0.08094043  
-0.01020302 0.03810356]  
[ 0.04859511 0.04364852 0.06943254 0.10562777 0.04529594 0.0845132  
-0.0202048 0.07262209]  
[ 0.0486294 0.00536263 0.01998049 0.04529594 0.05543721 0.01407108  
-0.02652481 0.04746691]  
[ 0.01835938 0.02299631 0.08094043 0.0845132 0.01407108 0.10330048  
-0.0115905 0.05731749]  
[-0.01093299 0.01113939 -0.01020302 -0.0202048 -0.02652481 -0.0115905  
0.09447296 -0.04330112]  
[ 0.04941813 0.03204267 0.03810356 0.07262209 0.04746691 0.05731749  
-0.04330112 0.1105482 ]]

-----

Your solution at Test 2 is:

[[ 0.08505974 0.03450228 -0.01193273 -0.00524796 0.01120509 -0.01875967  
0.00673483 0.01588703]  
[ 0.03450228 0.10518799 0.01518292 -0.04231919 0.04174065 -0.02661213  
0.010678 0.01386302]  
[-0.01193273 0.01518292 0.08547138 -0.04860232 -0.00703112 0.00141279  
0.0332502 0.03646121]  
[-0.00524796 -0.04231919 -0.04860232 0.08071985 -0.0218343 0.04525702  
-0.03339081 -0.03566894]  
[ 0.01120509 0.04174065 -0.00703112 -0.0218343 0.06660513 -0.02430969  
0.02139677 -0.01292649]  
[-0.01875967 -0.02661213 0.00141279 0.04525702 -0.02430969 0.04555685  
-0.01760783 -0.01280827]  
[ 0.00673483 0.010678 0.0332502 -0.03339081 0.02139677 -0.01760783  
0.05182447 0.03130241]  
[ 0.01588703 0.01386302 0.03646121 -0.03566894 -0.01292649 -0.01280827  
0.03130241 0.0574954 ]]

GT is:

[[ 0.08505974 0.03450228 -0.01193273 -0.00524796 0.01120509 -0.01875967  
0.00673483 0.01588703]  
[ 0.03450228 0.10518799 0.01518292 -0.04231919 0.04174065 -0.02661213  
0.010678 0.01386302]  
[-0.01193273 0.01518292 0.08547138 -0.04860232 -0.00703112 0.00141279  
0.0332502 0.03646121]  
[-0.00524796 -0.04231919 -0.04860232 0.08071985 -0.0218343 0.04525702  
-0.03339081 -0.03566894]  
[ 0.01120509 0.04174065 -0.00703112 -0.0218343 0.06660513 -0.02430969  
0.02139677 -0.01292649]  
[-0.01875967 -0.02661213 0.00141279 0.04525702 -0.02430969 0.04555685  
-0.01760783 -0.01280827]  
[ 0.00673483 0.010678 0.0332502 -0.03339081 0.02139677 -0.01760783

0.05182447 0.03130241]  
[ 0.01588703 0.01386302 0.03646121 -0.03566894 -0.01292649 -0.01280827  
0.03130241 0.0574954 ]]

-----

Your solution at Test 3 is:

[[ 0.09163497 0.01249203 -0.03393975 0.04103219 -0.01706239 0.00742286  
0.01981043 0.00538194]  
[ 0.01249203 0.04492758 0.00270599 0.0366516 0.01555546 0.00406492  
0.03895344 0.00778529]  
[-0.03393975 0.00270599 0.06417279 0.01686394 0.00415029 0.01892078  
0.0253209 -0.00051454]  
[ 0.04103219 0.0366516 0.01686394 0.0814071 -0.01178271 0.04871216  
0.05183951 0.00425153]  
[-0.01706239 0.01555546 0.00415029 -0.01178271 0.0371799 -0.01403554  
0.02177715 -0.00679106]  
[ 0.00742286 0.00406492 0.01892078 0.04871216 -0.01403554 0.05654842  
0.01760016 -0.03119823]  
[ 0.01981043 0.03895344 0.0253209 0.05183951 0.02177715 0.01760016  
0.08528434 0.00604487]  
[ 0.00538194 0.00778529 -0.00051454 0.00425153 -0.00679106 -0.03119823  
0.00604487 0.11629381]]

GT is:

[[ 0.09163497 0.01249203 -0.03393975 0.04103219 -0.01706239 0.00742286  
0.01981043 0.00538194]  
[ 0.01249203 0.04492758 0.00270599 0.0366516 0.01555546 0.00406492  
0.03895344 0.00778529]  
[-0.03393975 0.00270599 0.06417279 0.01686394 0.00415029 0.01892078  
0.0253209 -0.00051454]  
[ 0.04103219 0.0366516 0.01686394 0.0814071 -0.01178271 0.04871216  
0.05183951 0.00425153]  
[-0.01706239 0.01555546 0.00415029 -0.01178271 0.0371799 -0.01403554  
0.02177715 -0.00679106]  
[ 0.00742286 0.00406492 0.01892078 0.04871216 -0.01403554 0.05654842  
0.01760016 -0.03119823]  
[ 0.01981043 0.03895344 0.0253209 0.05183951 0.02177715 0.01760016  
0.08528434 0.00604487]  
[ 0.00538194 0.00778529 -0.00051454 0.00425153 -0.00679106 -0.03119823  
0.00604487 0.11629381]]

-----

Your solution at Test 4 is:

[[ 0.12369371 0.07515975 0.03984408 0.03115606 0.00595641 -0.00662781  
-0.00615451 -0.03015835]  
[ 0.07515975 0.09499617 0.0115346 0.02843702 0.0120597 0.02199165  
0.01655307 -0.02350239]  
[ 0.03984408 0.0115346 0.09885199 -0.01907784 0.02493639 -0.00816587  
-0.01845778 -0.01257176]  
[ 0.03115606 0.02843702 -0.01907784 0.04881931 -0.02619879 0.00927612  
0.01999505 0.01941759]  
[ 0.00595641 0.0120597 0.02493639 -0.02619879 0.04557326 0.00662006  
-0.02384613 -0.00081745]  
[-0.00662781 0.02199165 -0.00816587 0.00927612 0.00662006 0.04495194  
-0.00035861 -0.00062773]

[-0.00615451 0.01655307 -0.01845778 0.01999505 -0.02384613 -0.00035861  
0.05843185 0.02168865]  
[-0.03015835 -0.02350239 -0.01257176 0.01941759 -0.00081745 -0.00062773  
0.02168865 0.07056546]]

GT is:

[[ 0.12369371 0.07515975 0.03984408 0.03115606 0.00595641 -0.00662781  
-0.00615451 -0.03015835]  
[ 0.07515975 0.09499617 0.0115346 0.02843702 0.0120597 0.02199165  
0.01655307 -0.02350239]  
[ 0.03984408 0.0115346 0.09885199 -0.01907784 0.02493639 -0.00816587  
-0.01845778 -0.01257176]  
[ 0.03115606 0.02843702 -0.01907784 0.04881931 -0.02619879 0.00927612  
0.01999505 0.01941759]  
[ 0.00595641 0.0120597 0.02493639 -0.02619879 0.04557326 0.00662006  
-0.02384613 -0.00081745]  
[-0.00662781 0.02199165 -0.00816587 0.00927612 0.00662006 0.04495194  
-0.00035861 -0.00062773]  
[-0.00615451 0.01655307 -0.01845778 0.01999505 -0.02384613 -0.00035861  
0.05843185 0.02168865]  
[-0.03015835 -0.02350239 -0.01257176 0.01941759 -0.00081745 -0.00062773  
0.02168865 0.07056546]]

### test\_computeMean (test\_MyDiscriminant.TestMyDiscriminant) (1/1)

This test the computeMean() helper functions.

We randomly generate 5 sets with 10\*8 shape to find the mean

-----

Your solution at Test 0 is:

[0.48620993 0.60142359 0.42328614 0.5208569 0.62093252 0.48997793  
0.47616414 0.48229321]

GT is:

[0.48620993 0.60142359 0.42328614 0.5208569 0.62093252 0.48997793  
0.47616414 0.48229321]

-----

Your solution at Test 1 is:

[0.47078338 0.65417328 0.61337443 0.42501799 0.50691927 0.36362749  
0.40788188 0.5367783 ]

GT is:

[0.47078338 0.65417328 0.61337443 0.42501799 0.50691927 0.36362749  
0.40788188 0.5367783 ]

-----

Your solution at Test 2 is:

[0.50027491 0.58800114 0.29322758 0.51637001 0.54116711 0.4892752  
0.41076239 0.50394513]

GT is:

[0.50027491 0.58800114 0.29322758 0.51637001 0.54116711 0.4892752  
0.41076239 0.50394513]

-----

Your solution at Test 3 is:

[0.53886073 0.60022392 0.63459956 0.50831958 0.63470775 0.33840958  
0.56117373 0.43171471]

GT is:

[0.53886073 0.60022392 0.63459956 0.50831958 0.63470775 0.33840958  
0.56117373 0.43171471]

-----

Your solution at Test 4 is:

[0.38529714 0.50343767 0.37877246 0.41150032 0.2833117 0.54969377  
0.5030993 0.50614784]

GT is:

[0.38529714 0.50343767 0.37877246 0.41150032 0.2833117 0.54969377  
0.5030993 0.50614784]

### test\_computePrecision (test\_MyDiscriminant.TestMyDiscriminant) (1/1)

this test the compute\_precision() helper function

we randomly generate 5 sets with 100\*1 shape predictions and ytest to find the precision

GT Precision: 0.7014925373134329; Your Precision: 0.7014925373134329

GT Precision: 0.6307692307692307; Your Precision: 0.6307692307692307

GT Precision: 0.8309859154929577; Your Precision: 0.8309859154929577

GT Precision: 0.625; Your Precision: 0.625

GT Precision: 0.7671232876712328; Your Precision: 0.7671232876712328

### test\_computePrior (test\_MyDiscriminant.TestMyDiscriminant) (1/1)

This test the computePrior() helper functions.

We randomly generate 5 sets with 10\*1 shape to find the prior

-----

The labels are:

[2. 2. 2. 2. 2. 2. 2. 2. 1. 2.]

Your solution at Test 0 is:

[0.1 0.9]

GT is:

[0.1 0.9]

-----

The labels are:

[1. 2. 2. 2. 1. 1. 2. 1. 2. 2.]

Your solution at Test 1 is:

[0.4 0.6]

GT is:

[0.4 0.6]

-----

The labels are:

[1. 2. 2. 2. 2. 1. 1. 2. 2. 1.]

Your solution at Test 2 is:

[0.4 0.6]

GT is:

[0.4 0.6]

-----

The labels are:

[2. 2. 1. 2. 1. 2. 2. 2. 2. 2.]

Your solution at Test 3 is:

[0.2 0.8]

GT is:

[0.2 0.8]

-----

The labels are:

[2. 2. 2. 2. 1. 2. 1. 2. 2. 1.]

Your solution at Test 4 is:

[0.3 0.7]

GT is:

[0.3 0.7]

### test\_computeRecall (test\_MyDiscriminant.TestMyDiscriminant) (1/1)

this test the compute\_recall() helper function

we randomly generate 5 sets with 100\*1 shape predictions and ytest to find the recall

GT Recall: 0.6575342465753424; Your Recall: 0.6575342465753424

GT Recall: 0.7088607594936709; Your Recall: 0.7088607594936709

GT Recall: 0.640625; Your Recall: 0.640625

GT Recall: 0.6764705882352942; Your Recall: 0.6764705882352942

GT Recall: 0.726027397260274; Your Recall: 0.726027397260274





```

1  import numpy as np
2  # some tips
3  # |S| is the determinant of S in the discriminant functions, try np.linalg.det()
4  # you can also directly get the inverse of a matrix by np.linalg.inv()
5
6
7  # ----- You are going to implement 3 classifiers and corresponding helper
  functions -----
8  # ----- Three classifiers start from here -----
  -----
9  class GaussianDiscriminantBase:
10     def __init__(self) -> None:
11         pass
12
13     def calculate_metrics(self, ytest, predictions):
14         precision = compute_precision(ytest, predictions)
15         recall = compute_recall(ytest, predictions)
16         return precision, recall
17
18  class GaussianDiscriminant_C1(GaussianDiscriminantBase):
19     # classifier initialization
20     # input:
21     # k: number of classes (2 for this assignment)
22     # d: number of features; feature dimensions (8 for this assignment)
23     def __init__(self, k=2, d=8):
24         self.m = np.zeros((k,d)) # m1 and m2, store in 2*8 matrices
25         self.S = np.zeros((k,d,d)) # S1 and S2, store in 2*(8*8) matrices
26         self.p = np.zeros(2) # p1 and p2, store in dimension 2 vectors
27
28     # compute the parameters for both classes based on the training data
29     def fit(self, Xtrain, ytrain):
30         # Step 1: Split the data into two parts based on the labels
31         Xtrain1, Xtrain2 = splitData(Xtrain, ytrain)
32
33         # Step 2: Compute the parameters for each class
34         # m1, S1 for class1
35         self.m[0,:] = computeMean(Xtrain1)
36         self.S[0] = computeCov( Xtrain1 )
37
38         # m2, S2 for class2
39         self.m[1,:] = computeMean(Xtrain2)
40         self.S[1] = computeCov( Xtrain2 )
41
42         # priors for both class
43         self.p = computePrior(ytrain)
44
45
46
47

```

```

48 # predict the labels for test data
49 # Input:
50 # Xtest: n*d
51 # Output:
52 # Predictions: n (all entries will be either number 1 or 2 to denote the labels)
53 def predict(self, Xtest):
54     # placeholders to store the predictions
55     # can be ignored, removed or replaced with any following implementations
56     predictions = np.zeros(Xtest.shape[0])
57
58     # for indexing predictions in the loop
59     i = 0
60
61     # must convert the means to 2d matrices and transpose to a column vector
62     # at that point I can use formula 5.20 in the book
63     mean0 = np.zeros((1, 8))
64     mean0[0] = self.m[0]
65     mean0 = mean0.transpose()
66     mean1 = np.zeros((1, 8))
67     mean1[0] = self.m[1]
68     mean1 = mean1.transpose()
69
70     for x_observation in Xtest:
71         # change the vector to a column vector so it will work with the book's formula
72         observation = np.zeros( (1, 8) )
73         observation[0] = x_observation
74         observation = observation.transpose() # we pass in a column vectors!
75
76         probClassC1 = computeDisc(observation, mean0, self.S[0], self.p[0])
77         probClassC2 = computeDisc(observation, mean1, self.S[1], self.p[1])
78
79         if probClassC1[0][0] > probClassC2[0][0]:
80             predictions[i] = 1
81         else:
82             predictions[i] = 2
83         i += 1
84
85     return np.array(predictions)
86
87
88
89
90 class GaussianDiscriminant_C2(GaussianDiscriminantBase):
91     # classifier initialization
92     # input:
93     # k: number of classes (2 for this assignment)
94     # d: number of features; feature dimensions (8 for this assignment)
95     def __init__(self, k=2, d=8):
96         self.m = np.zeros((k,d)) # m1 and m2, store in 2*8 matrices
97         self.shared_S = np.zeros((d,d)) # the shared covariance S that will be used for both classes
98         self.p = np.zeros(2) # p1 and p2, store in dimension 2 vectors
99

```

```

100 # compute the parameters for both classes based on the training data
101 def fit(self, Xtrain, ytrain):
102     # Step 1: Split the data into two parts based on the labels
103     Xtrain1, Xtrain2 = splitData(Xtrain, ytrain)
104
105     # Step 2: Compute the parameters for each class
106     # m1
107     self.m[0, :] = computeMean(Xtrain1)
108
109     # m2
110     self.m[1, :] = computeMean(Xtrain2)
111
112     # compute the shared covariance
113     self.shared_S = computeCov(Xtrain) # compute the covariance on the whole data set!
114
115     # priors for both class
116     self.p = computePrior(ytrain)
117
118     # Fill in your code here !!!!!!!!!!!!!!!!!!!!!!!
119     # Step 3: Compute the shared covariance matrix that is used for both class
120     # shared_S is computed by finding a covariance matrix of all the data
121
122 # predict the labels for test data
123 # Input:
124 # Xtest: n*d
125 # Output:
126 # Predictions: n (all entries will be either number 1 or 2 to denote the labels)
127 def predict(self, Xtest):
128     # placeholders to store the predictions
129     # can be ignored, removed or replaced with any following implementations
130     predictions = np.zeros(Xtest.shape[0])
131
132     # for indexing predictions in the loop
133     i = 0
134
135     # must convert the means to 2d matrices and transpose to a column vector
136     # at that point I can use formula 5.20 in the book
137     mean0 = np.zeros((1, 8))
138     mean0[0] = self.m[0]
139     mean0 = mean0.transpose()
140     mean1 = np.zeros((1, 8))
141     mean1[0] = self.m[1]
142     mean1 = mean1.transpose()
143
144     for x_observation in Xtest:
145         # change the vector to a column vector so it will work with the book's formula
146         observation = np.zeros((1, 8))
147         observation[0] = x_observation
148         observation = observation.transpose() # we pass in a column vectors!
149
150         probClassC1 = computeDisc(observation, mean0, self.shared_S, self.p[0])
151         probClassC2 = computeDisc(observation, mean1, self.shared_S, self.p[1])

```

```

152
153     if probClassC1[0][0] > probClassC2[0][0]:
154         predictions[i] = 1
155     else:
156         predictions[i] = 2
157     i += 1
158
159     return np.array(predictions)
160
161
162 class GaussianDiscriminant_C3(GaussianDiscriminantBase):
163     # classifier initialization
164     # input:
165     # k: number of classes (2 for this assignment)
166     # d: number of features; feature dimensions (8 for this assignment)
167     def __init__(self, k=2, d=8):
168         self.m = np.zeros((k,d)) # m1 and m2, store in 2*8 matrices
169         self.shared_S = np.zeros((d,d)) # the shared covariance S that will be used for both classes
170         self.p = np.zeros(2) # p1 and p2, store in dimension 2 vectors
171
172     # compute the parameters for both classes based on the training data
173     def fit(self, Xtrain, ytrain):
174         # Step 1: Split the data into two parts based on the labels
175         Xtrain1, Xtrain2 = splitData(Xtrain, ytrain)
176
177         # Step 2: Compute the parameters for each class
178         # m1
179         self.m[0, :] = computeMean(Xtrain1)
180
181         # m2
182         self.m[1, :] = computeMean(Xtrain2)
183
184         # compute the shared covariance
185         self.shared_S = np.diag(np.diag(computeCov(Xtrain)))
186
187         # priors for both class
188         self.p = computePrior(ytrain)
189
190     # predict the labels for test data
191     # Input:
192     # Xtest: n*d
193     # Output:
194     # Predictions: n (all entries will be either number 1 or 2 to denote the labels)
195     def predict(self, Xtest):
196         # placeholders to store the predictions
197         # can be ignored, removed or replaced with any following implementations
198         predictions = np.zeros(Xtest.shape[0])
199
200         # for indexing predictions in the loop
201         i = 0
202
203         # must convert the means to 2d matrices and transpose to a column vector

```

```

204 # at that point I can use formula 5.20 in the book
205 mean0 = np.zeros((1, 8))
206 mean0[0] = self.m[0]
207 mean0 = mean0.transpose()
208 mean1 = np.zeros((1, 8))
209 mean1[0] = self.m[1]
210 mean1 = mean1.transpose()
211
212 for x_observation in Xtest:
213     # change the vector to a column vector so it will work with the book's formula
214     observation = np.zeros( (1, 8) )
215     observation[0] = x_observation
216     observation = observation.transpose() # we pass in a column vectors!
217
218     probClassC1 = computeDisc(observation, mean0, self.shared_S, self.p[0])
219     probClassC2 = computeDisc(observation, mean1, self.shared_S, self.p[1])
220
221     if probClassC1[0][0] > probClassC2[0][0]:
222         predictions[i] = 1
223     else:
224         predictions[i] = 2
225     i += 1
226
227 return np.array(predictions)
228
229
230 # ----- Helper Functions start from here -----
231
232 # Input:
233 # features: n*d matrix (n is the number of samples, d is the number of dimensions of the feature)
234 # labels: n vector
235 # Output:
236 # features1: n1*d
237 # features2: n2*d
238 # n1+n2 = n, n1 is the number of class1, n2 is the number of samples from class 2
239 def splitData(features, labels):
240     # defensive programming: make sure features and labels are of the same size.
241     if (np.size(features, 0) != np.size(labels)):
242         raise IndexError( "The number of rows of features and labels do not match.")
243
244     # placeholders to store the separated features (feature1, feature2),
245     # can be ignored, removed or replaced with any following implementations
246     features1 = np.zeros([np.sum(labels == 1), features.shape[1]]) # array[ num of class y=1 values,
number of features
247     features2 = np.zeros([np.sum(labels == 2), features.shape[1]]) # array[ num of class y=2 values,
number of features
248
249     # need to know what index each feature array is at so I can copy from main feature array.
250     # I could rely on the fact that the data has all of class 1 first and then all of class 2 but that seems
a wonky
251     # and bug-ridden way to program.

```

```

252 featuresIndex = np.array( [0,0] )
253
254 # separate the features according to the corresponding labels, for example
255 # if features = [[1,1],[2,2],[3,3],[4,4]] and labels = [1,1,1,2], the resulting feature1 and feature2
will be
256 # feature1 = [[1,1],[2,2],[3,3]], feature2 = [[4,4]]
257 for i in range(0, len(labels)):
258     if labels[i] == 1:
259         features1[ featuresIndex[0] ] = features[i]
260         featuresIndex[0] += 1
261     elif labels[i] == 2:
262         features2[ featuresIndex[1] ] = features[i]
263         featuresIndex[1] += 1
264     else:
265         raise ValueError("Class in data not in {1,2}.")
266
267     return features1, features2
268
269
270 # compute the mean of input features
271 # input:
272 # features: n*d
273 # output: d
274 def computeMean(features):
275
276     # placeholders to store the mean for one class
277     # can be ignored, removed or replaced with any following implementations
278     m = np.zeros(features.shape[1])
279
280     # fill in the code here !!!!!!!!!!!!!!!!!!!!!!!
281     # try to explore np.mean() for convenience
282     # decided to go a different route so I could practice with routines I will probably use for
calculating variance
283     # and covariance
284
285     m = (np.sum(features, axis = 0))
286
287     # the number of columns is features[0] while the number of rows is len(features)
288     m = np.divide( m, float( len(features) ) )
289
290     return m
291
292
293
294 # wrapper function that calls np.cov() and computes the covariance
295 # input:
296 # features: n*d
297 # output: d*d
298 def computeCov(features):
299     # placeholders to store the covariance matrix for one class
300     # can be ignored, removed or replaced with any following implementations
301     covMatrix = np.eye(features.shape[1])

```

```

302
303     # try to explore np.cov() for convenience
304     covMatrix = np.cov(features, rowvar = False)
305
306     return covMatrix
307
308
309 # compute the priors of input features
310 # input:
311 # labels: n*1
312 # output: 2
313 def computePrior(labels):
314     # placeholders to store the priors for both class
315     # can be ignored, removed or replaced with any following implementations
316     p = np.array([0.5,0.5])
317
318     # p[0] contains prior for class 1
319     # p[1] contains prior for class 2
320     p[0] = np.count_nonzero(labels == 1.0) / float( len(labels) )
321     p[1] = np.count_nonzero(labels == 2.0) / float( len(labels) )
322
323     return p
324
325 # compute the discriminant function
326 # input:
327 # observation: d * 1
328 # means: d * 1
329 # covMatrix: d*d
330 # prior: scaler
331 def computeDisc(observation, means, covMatrix, prior):
332
333     return (-.5) * np.log( np.linalg.det( covMatrix ) ) - 0.5 * ( observation.T @ np.linalg.inv(covMatrix )
334     @ observation - 2 * observation.T @ np.linalg.inv( covMatrix ) @ means + means.T @ np.linalg.inv(
335     covMatrix) @ means ) + np.log( prior )
336
337
338 # compute the precision
339 # input:
340 # ytest: the ground truth labels of the test data, n*1
341 # predictions: the predicted labels of the test data, n*1
342 # output:
343 # precision: a float with size 1
344
345 def compute_precision(ytest, predictions):
346     precision = 0.0 # a place holder can be neglected
347
348     # precision = countOf[true positive predictions] / countOf[positive predictions]
349     # here we assume label==2 is the positive label
350     truePositives = 0
351     countOfPositives = 0
352     for i in range( len (predictions) ):
353
354         if ( predictions[i] == 2 ):

```

```
352         countOfPositives += 1
353
354         if ( ytest[i] == 2 ):
355             truePositives += 1
356
357     precision = truePositives / countOfPositives
358     return precision
359
360 # compute the recall
361 # input:
362 # ytest: the ground truth labels of the test data, n*1
363 # predictions: the predicted labels of the test data, n*1
364 # output:
365 # recall: a float with size 1
366 def compute_recall(ytest, predictions):
367     recall = 0.0 # a place holder can be neglected
368
369     # recall = countOf[true positive predictions] / countOf[positive labels in ytest]
370     # here we assume label==2 is the positive label
371     truePositives = 0
372     positiveLabelsInTest = 0
373     for i in range( len (predictions) ):
374
375         if ytest[i] == 2:
376             positiveLabelsInTest += 1
377
378         if ( predictions[i] == 2):
379             truePositives += 1
380
381     recall = truePositives / positiveLabelsInTest
382     return recall
```