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Binary Images Morphological Processing



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Binary Images

- Binary images
- Thresholding
- Mathematic Morphology
 - (also for non binary images)
- Connected components extraction

- In some cases it is necessary/useful to acquire/produce and/or process images whose pixels can only have 0/1 logical values
 - PBM or XBM image formats

```
00010010001000
00011110001000
00010010001000
```



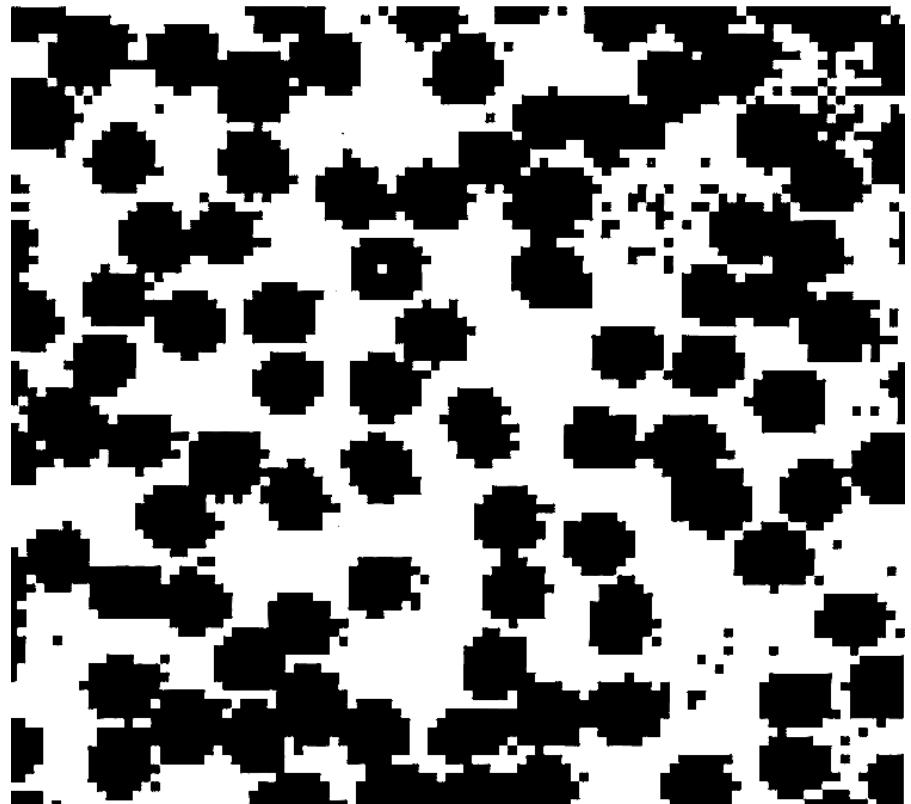
- 1 actually can be considered as !=0
- 255 is often used for simplicity

0	0	0	255	0	0	255	0	0	0	255	0	0	0
0	0	0	255	255	255	255	0	0	0	255	0	0	0
0	0	0	255	0	0	255	0	0	0	255	0	0	0

Example



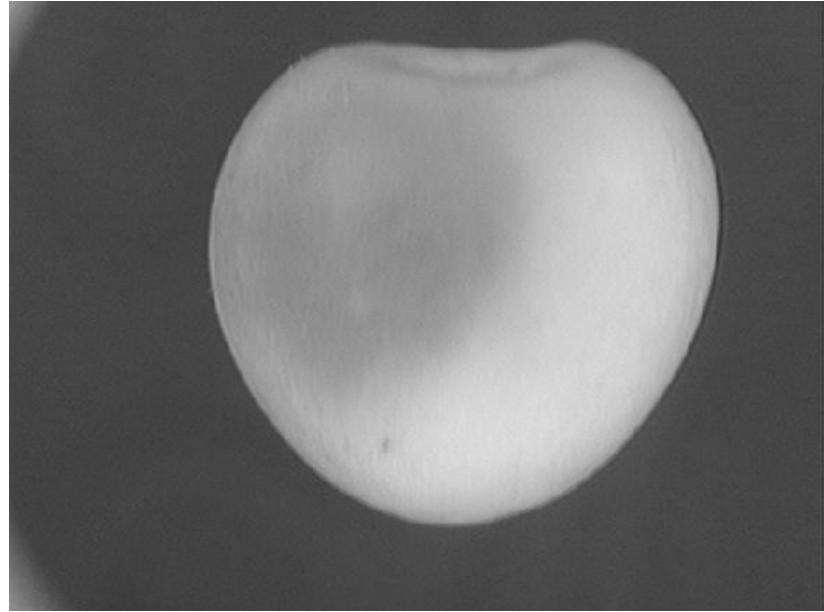
- Why binary images?
 - They are simpler to process
 - Example: Image of blood cells
 - We would like to estimate red blood cells
 - Anyway they are not isolated (<50%)
 - How we can separate them?
 - Often output of other processing techniques
 - i.e. edge detection



How to obtain binary images?

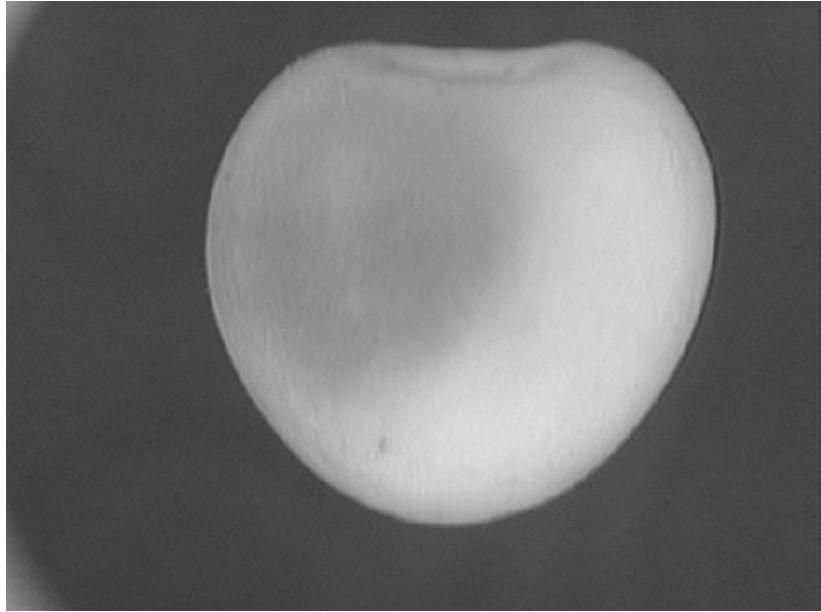
- Basically no B/W cameras
- Besides specific processing → thresholding
 - Pixel above a specific value → 1
 - Pixel below a specific value → 0

- We would like to discard a bruised apple
- How we can select the bruised part?
 - Extract “dark” pixels
- We can only use pixel brightness
- Thresholding:



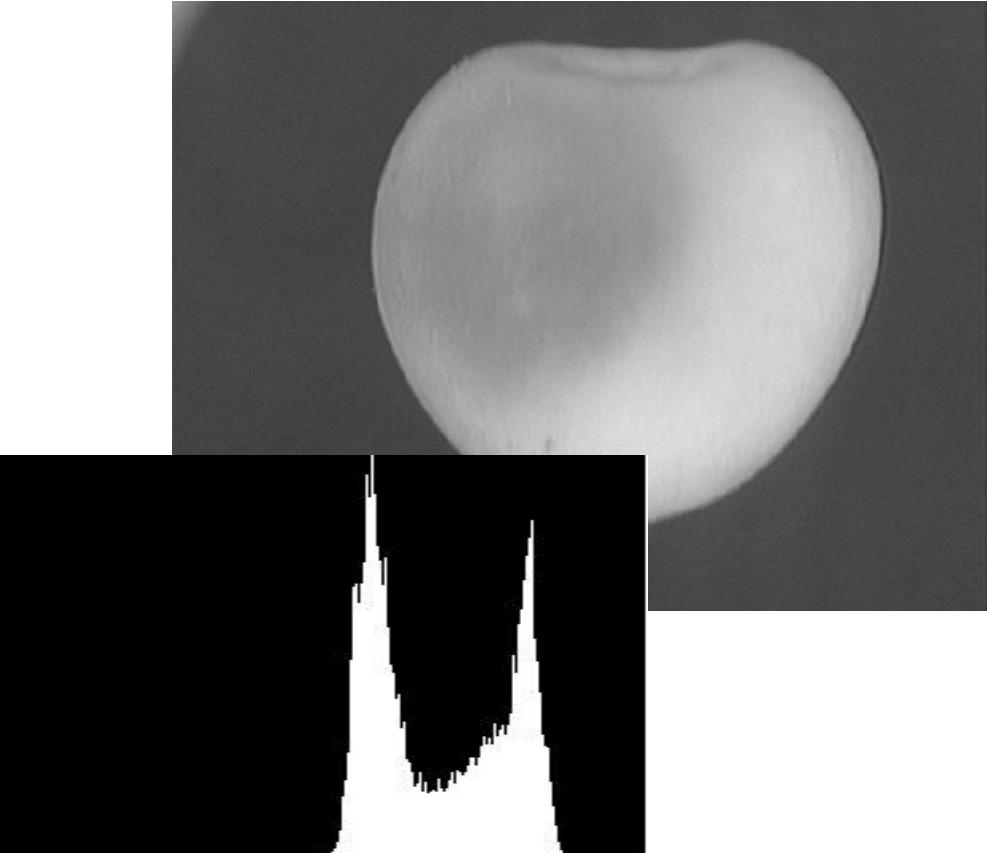
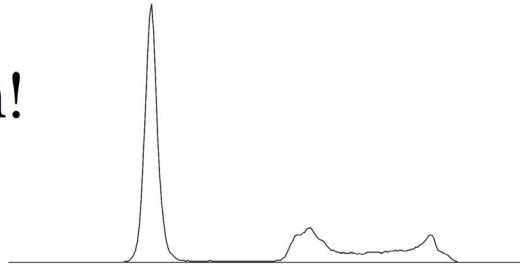
$$out(r,c) = \begin{cases} 0 & \text{where } in(r,c) < th \\ 1 & \text{where } in(r,c) \geq th \end{cases}$$

- Anyway we have:
 - “Good” apple part
 - Bruised apple part
 - Background
- How we decide about the threshold?



$$out(r,c) = \begin{cases} 0 & \text{where } in(r,c) < th \\ 1 & \text{where } in(r,c) \geq th \end{cases}$$

- Anyway we have:
 - “Good” apple part
 - Bruised apple part
 - Background
- How we decide about the threshold?
- Histogram!

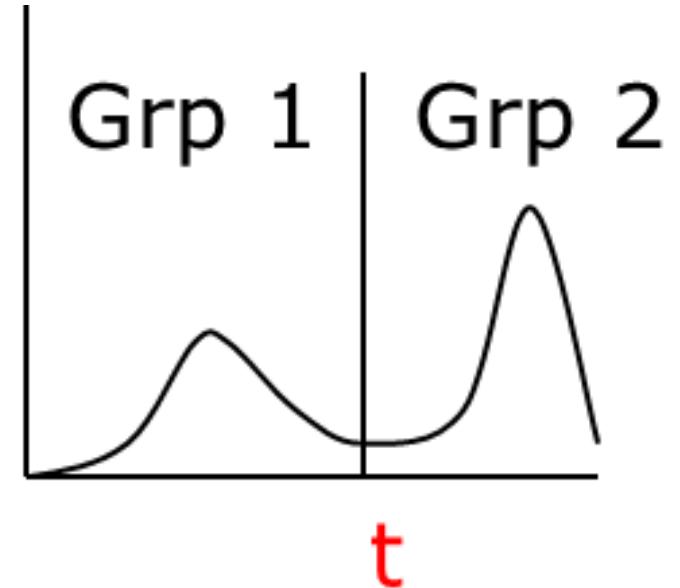


Otsu's Method



- Best threshold computation
- Problem: find a th that minimize weighted sum of each group variance

$$\sigma^2(th) = \sigma_1^2(th) \cdot w_1(th) + \sigma_2^2(th) \cdot w_2(th)$$



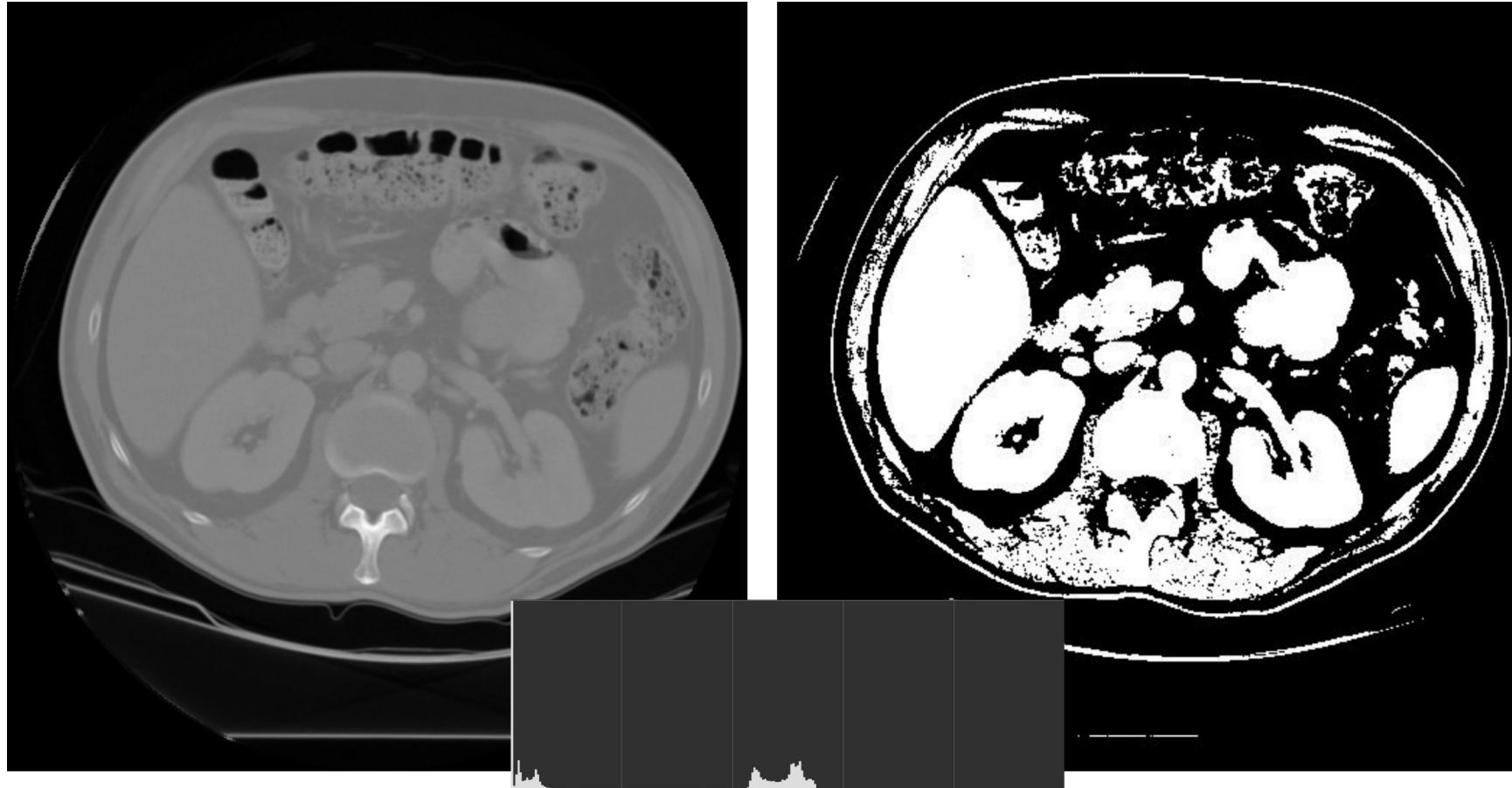
- $w_1(th)$ & $w_2(th)$ are the probability of belonging to group 1 or 2

$$w_1(th) = \sum_{i=0}^{th-1} h(i)$$

$$w_2(th) = \sum_{i=th}^L h(i)$$

Otsu's Method

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Otsu's Method





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Morphological Processing

- Used to extract image components that are useful in the representation and description of region shape, such as
 - boundaries extraction
 - skeletons
 - convex hull
 - morphological filtering
 - thinning
 - pruning



- Main operations
 - Erosion $\rightarrow \ominus$
 - Dilation $\rightarrow \oplus$
 - Opening $\rightarrow \circ$
 - Closing $\rightarrow \bullet$
 - Hit or Miss $\rightarrow \otimes$

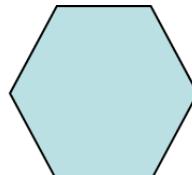
Structuring Element



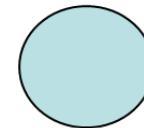
- Small “mask” to probe the image under study
 - Convolution like approach
- Structuring Element features an origin
- Shape and size must be adapted to geometric properties we would like to mask/obtain



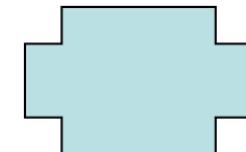
box



hexagon



disk

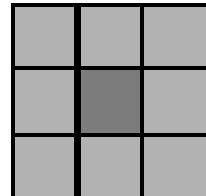
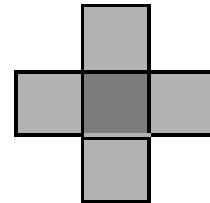
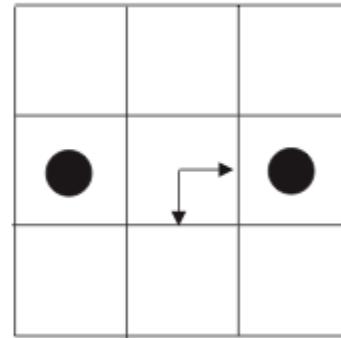
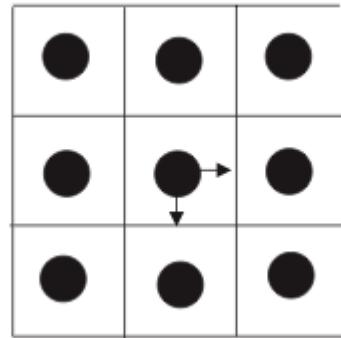
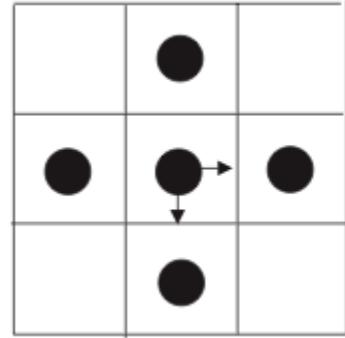


something

box(length, width)

disk(diameter)

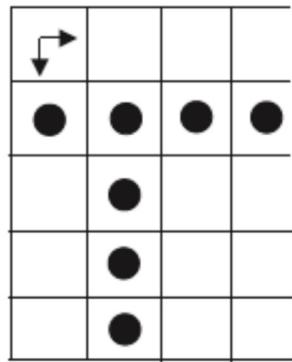
Structuring Element



- The structuring element B is “moved” (B_z) on the image A for a set of values z belonging to an Euclidean Space E
- The result is the set of z values for which B_z is in A

$$A \ominus B = \{ z \in E^2 : B_z \subseteq A \}$$

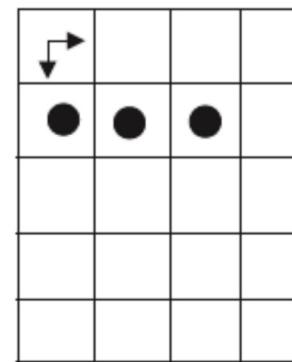
- Practically the structuring element is superimposed on all the pixel of the image.
 - When it completely fits the binary image the result is 1, otherwise 0
 - Logical AND
 - It shrinks image elements



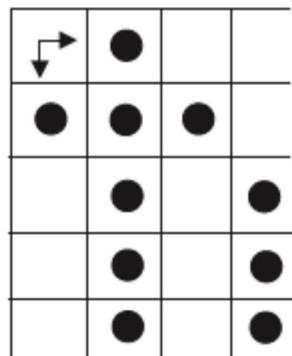
A



B



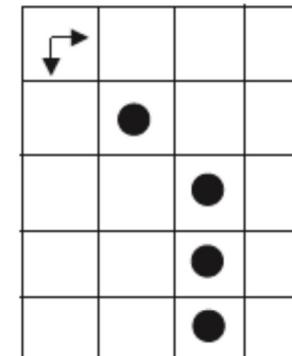
A ⊖ B



A



B



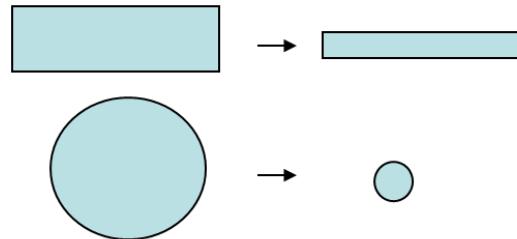
A ⊖ B



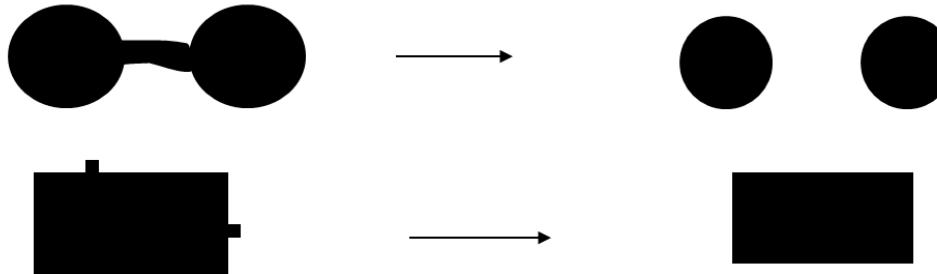
Erosion **shrinks** the connected sets of 1s of a binary image.

It can be used for

1. shrinking features

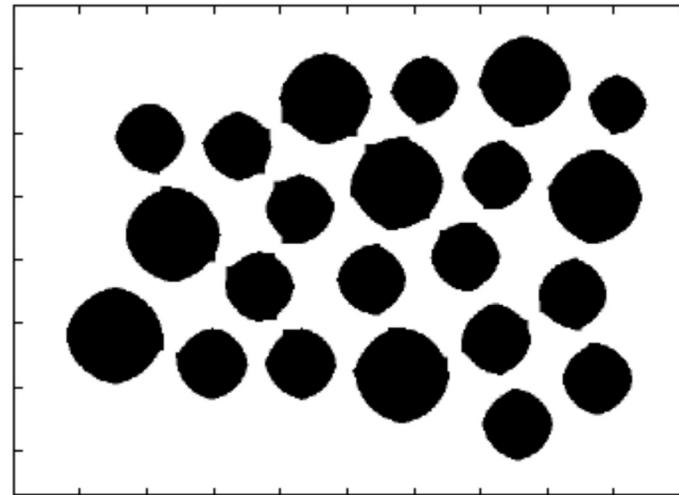


2. Removing bridges, branches and small protrusions





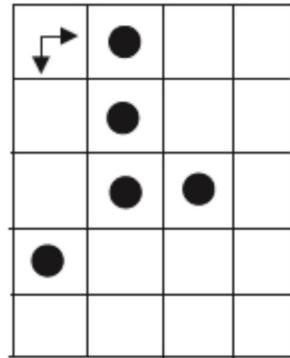
- Consider the following image



- We can use erosion to separate elements

- Again the structuring element is superimposed on all the pixel of the image.
 - When it hits the binary image the result is 1, otherwise 0
 - Logical OR
- It “dilates” image elements

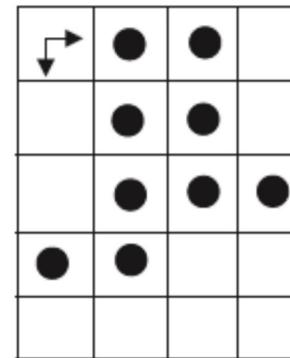
Dilation \oplus



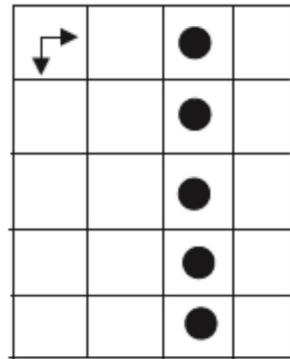
A



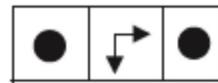
B



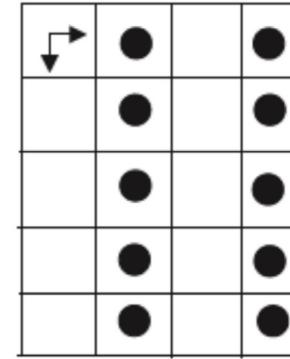
$A \oplus B$



A



B



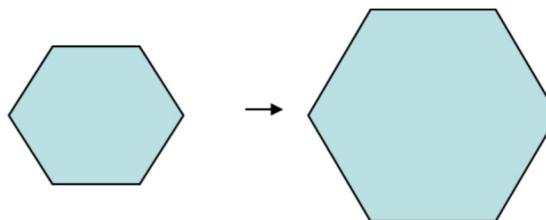
$A \oplus B$



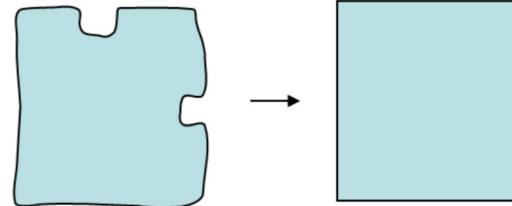
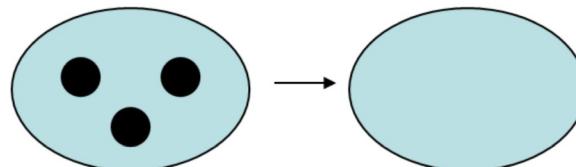
Dilation **expands** the connected sets of 1s of a binary image.

It can be used for

1. growing features



2. filling holes and gaps



- We can use erosion and dilation to remove small details or to fill some gaps
- But they also affect other part of the image...
- Solution
 - Combine them!

Opening/Closing

- Opening
 - Erosion followed by dilation

$$A \circ B = (A \ominus B) \oplus B$$

- Closing
 - Dilation followed by erosion

$$A \cdot B = (A \oplus B) \ominus B$$

- The same structuring element is used

Examples

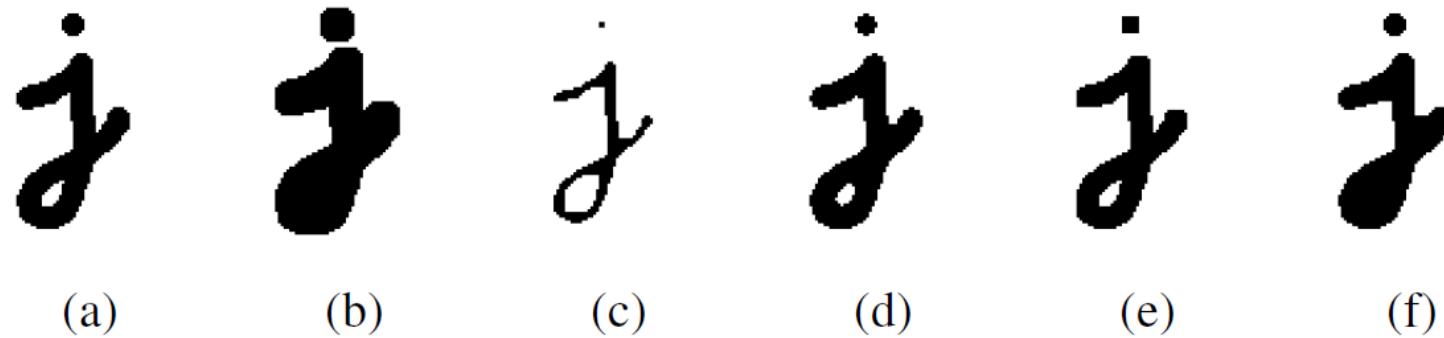


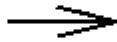
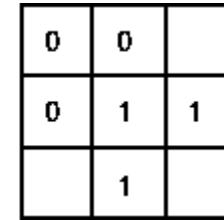
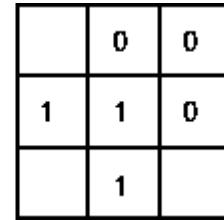
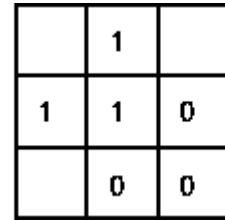
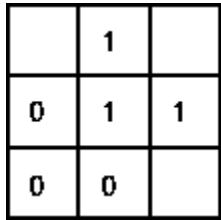
Figure 3.21 Binary image morphology: (a) original image; (b) dilation; (c) erosion; (d) majority; (e) opening; (f) closing. The structuring element for all examples is a 5×5 square. The effects of majority are a subtle rounding of sharp corners. Opening fails to eliminate the dot, since it is not wide enough.

Source: Szeliski

- Two “disjoint” structuring elements are used: A e B
 - $A \cap B = \emptyset$
- Two erosion are used and joined
 - $I \otimes X = (I \ominus A) \cap (I^c \ominus B)$
 - Where I^c is the complement for I and $X = (A, B)$
- The idea is that A should match shapes and B background
 - It can be seen as an “extended” SE

	1	
0	1	1
0	0	

Hit or Miss \otimes

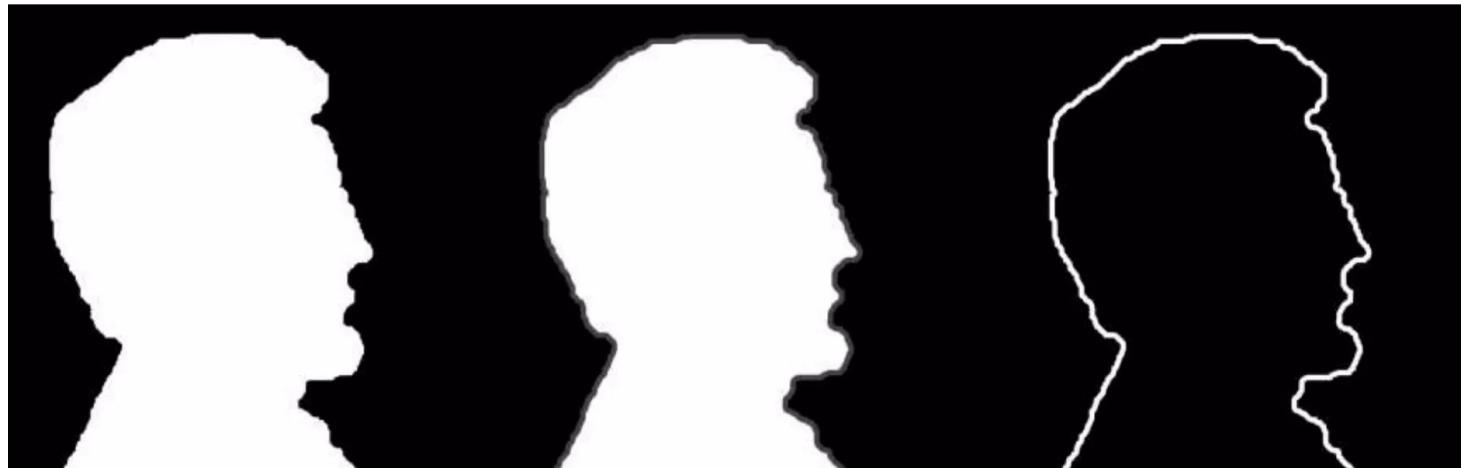


A 10x10 binary matrix where most elements are 0s. Several 1s are highlighted in yellow. The highlighted 1s form a pattern that includes the first row, the second column, the third row, the fourth column, the fifth row, the sixth column, the seventh row, the eighth column, the ninth row, and the tenth column. This results in a 10x10 grid of 1s with a yellow border around the entire grid.

Border Extraction

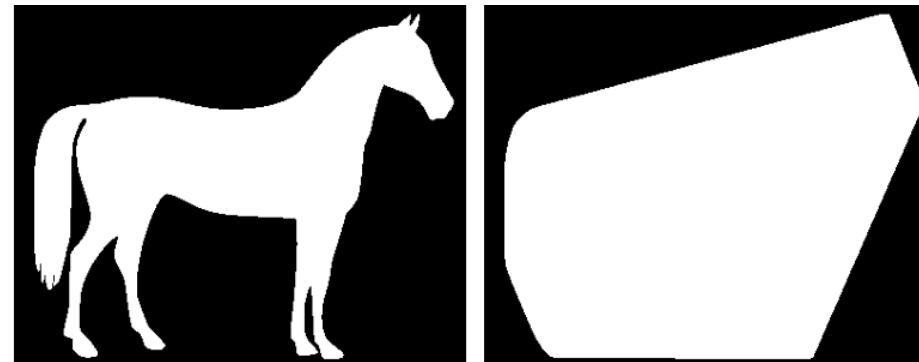


- Erode image using a given SE
- The difference between original image and eroded one is the “border”
- The thickness of the contour depends on the SE size



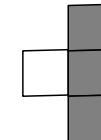
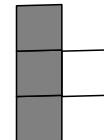
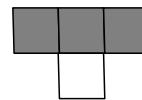
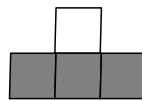


- A set of points X is defined as **convex set** if any straight line segment between two X points completely lies inside X
- The **convex hull** H of a S set is the smallest convex set that contains S
- **Convex deficiency** is $H-S$



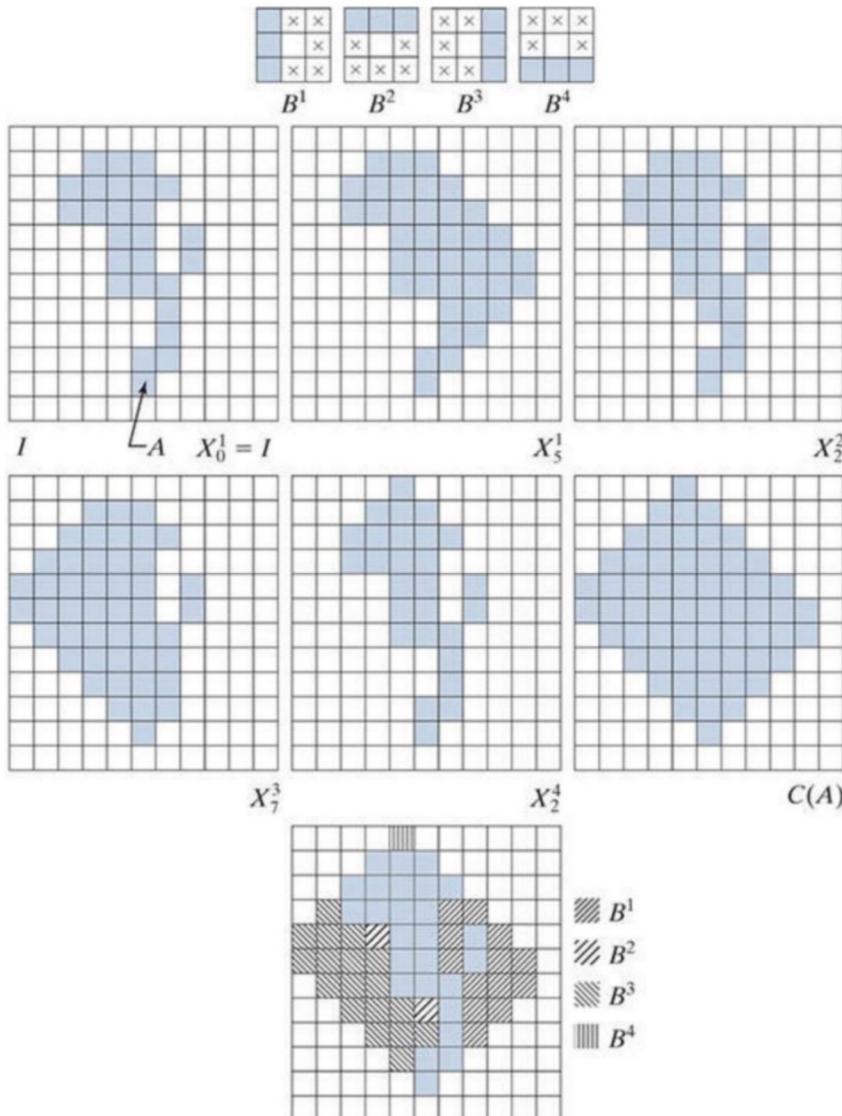


- Convex Hull can be computed using a set of hit and miss transform
 - Apply each SE to the original shape until the result is different
 - The union of the 4 resulting shapes is a convex hull



Convex Hull

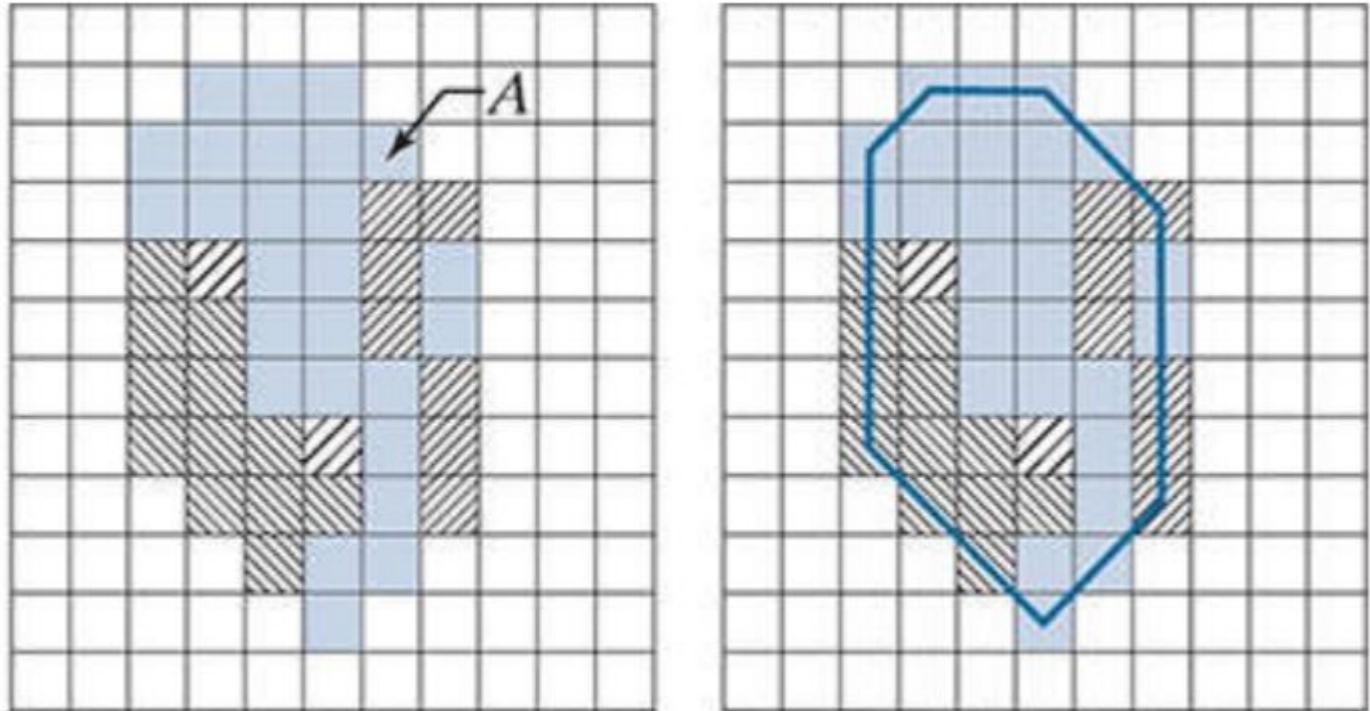
Not optimized!



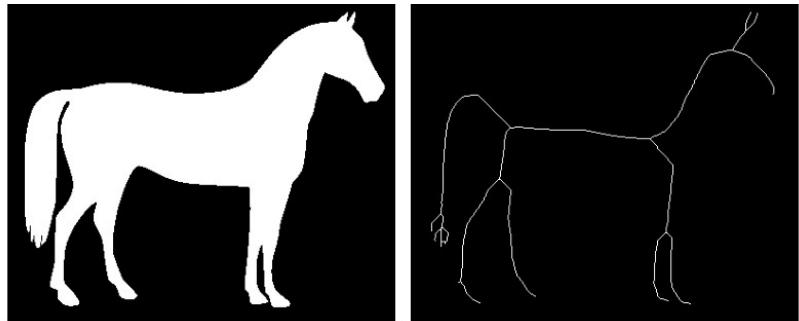
Convex Hull



Edge pixels can be used to “trim” the result
Namely, limiting the convergence in the horizontal or vertical directions



- Skeleton is a thin version of a shape
 - Single pixel thickness
 - Equidistant to shape borders
 - Topological equivalence
- Again a hit and miss approach
 - Up to 8 SEs





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Morphological Processing for Grey Level Images



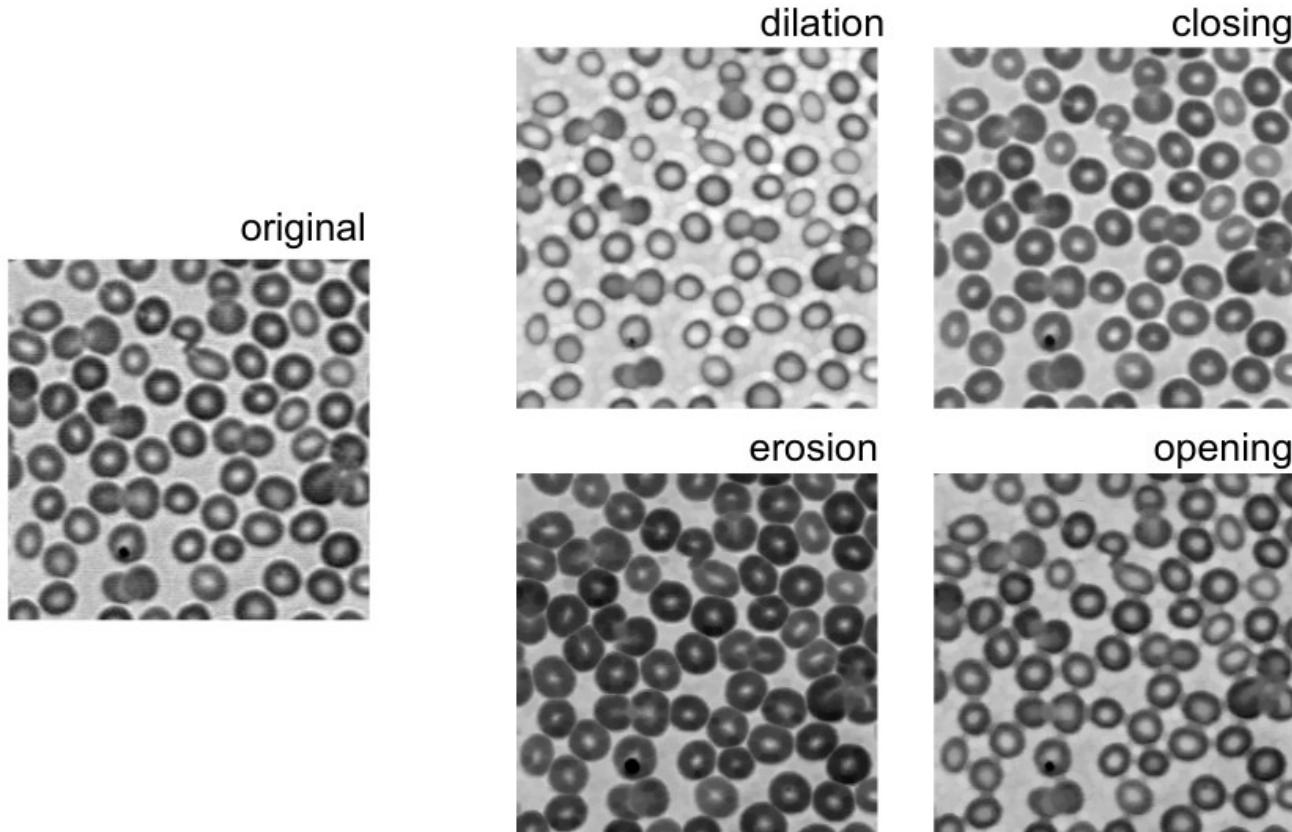
- Mathematical morphology can be extended to grayscale images
- Applications
 - Contrast enhancement
 - Texture description
 - Edge detection
 - Thresholding

Grayscale Morphology



- In a grayscale image there is no “object” and “background”
- Structuring element is still a mask
- Min and Max operators are used
 - Dilation → max element under the mask wins
 - Erosion → min element under the mask wins
- Opening & Closing as before

Grayscale Morphology





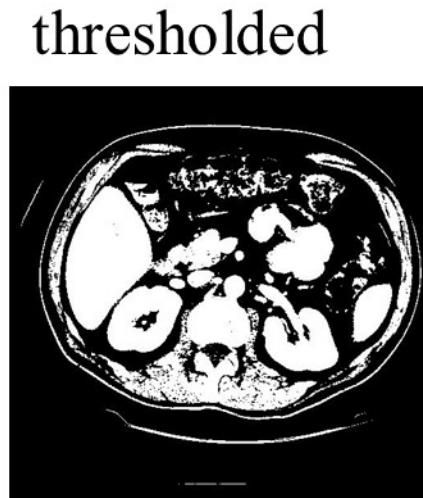
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Connected Components

Connected Components



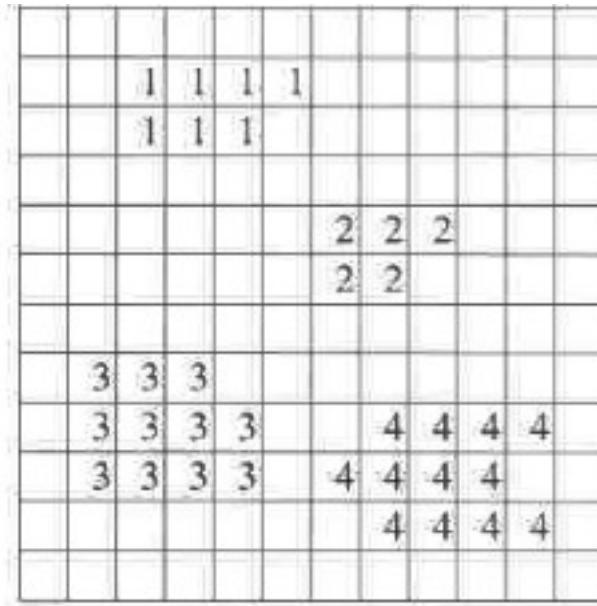
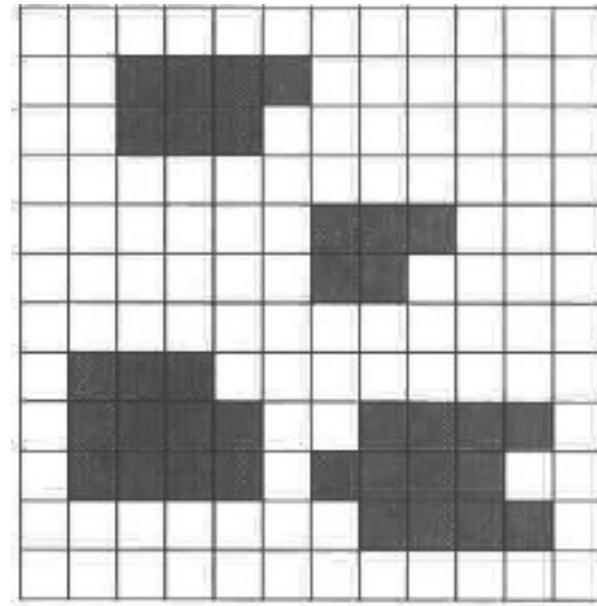
- A connected component is a **contiguous** group of pixels that have the **same value**
 - Actually not only for binary images



Labelling algorithms for CC



- We assign a unique label to each component

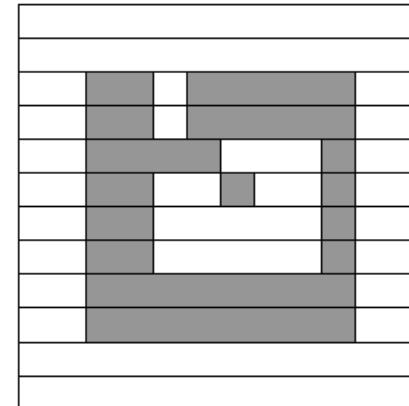


Source: R. Jain

Labelling algorithms for CC

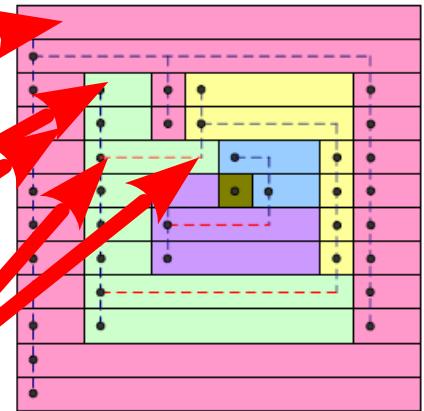


- Different approaches can be used:
 - Recursive Tracking
 - Parallel Growing
 - Row-by-Row (widely used)



Row by Row Labelling algorithm

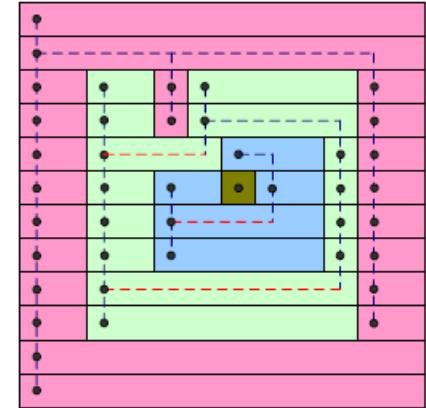
- 1st pass:
 - First row:
 - Check left neighbour, do it have the same value?
 - Yes → same label
 - No → new label
 - Other rows
 - Check left and upper neighbour
 - They have same value and same label → same label
 - Current pixel have same value of only one of them → same label of that one
 - They have same value but different label (!) → set lowest label and track the equivalence
 - Otherwise → new label



Row by Row Labelling algorithm



- 2nd pass:
 - During 1st pass we have tracked label equivalences
 - Row by row change labels with lowest equivalent

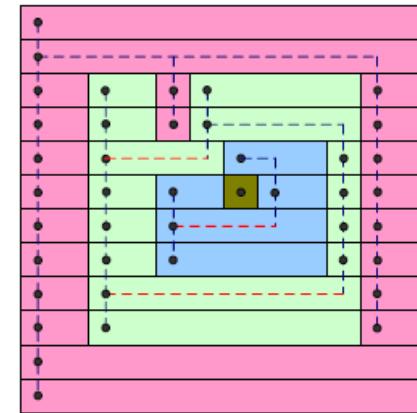
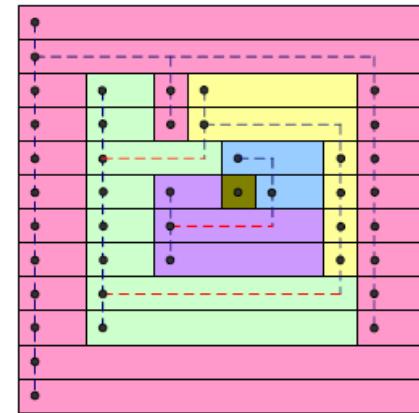
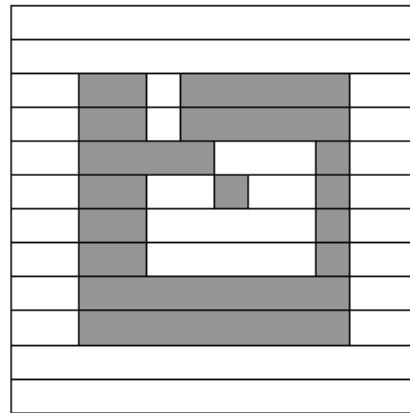


Labelling algorithms for CC

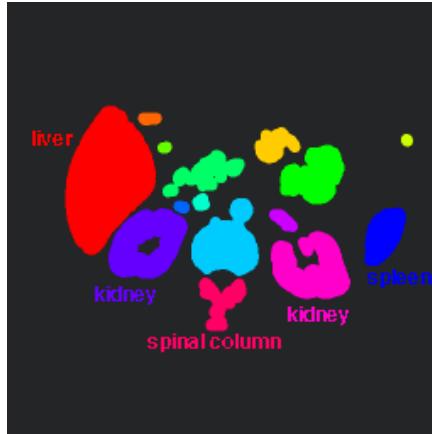
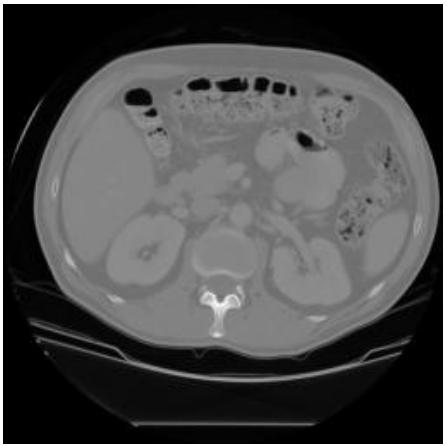


- Row by Row

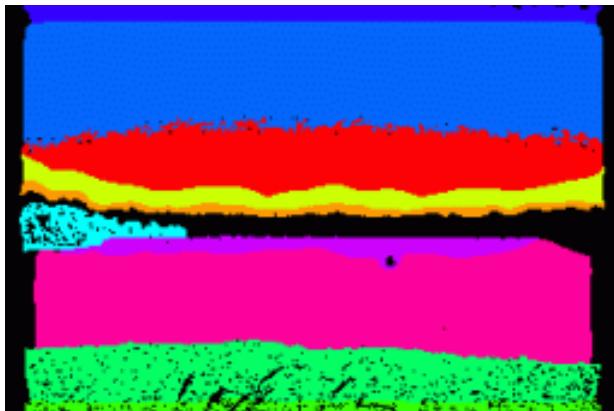
Source: Szeliski



Connected Components



connected
components
of 1's from
cleaned,
thresholded
image



connected
components
of cluster
labels