

SSH Key File Formats

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Private Key

- I expect to find (p, q, n, e, d). I took the PEM file and uploaded it to a ASN.1 decoder to get the DER. The output showed 9 INTEGER values corresponding to the version, modulus, public exponent, private exponent, prime1, prime2, exponent1, exponent2, and coefficient (Figure 1).

ASN.1 name	Meaning	Value (decimal)
version	Tells us the format of the data	0
modulus	This is n where $n = p \times q$	(3072 bit) 5335065194301705493845814952787258971514760375775469803879 7709522258445664369858255015035870391915808056077598960729 8393292955564723921068005109047687770896884905650961373845 0089281982793075060790146120689820862474322576090077184085 4833137230042250601611180452861564211033876771567382204658 9759710906679747956088069746913799863420659084213971935676 5953043580237126825142567744166559198603190073173940161280 8033807158234841381049591111783398702854113330422773833412 3327023459232916175257074154169198915626599378449755329902 4235625184410149719731111600578950547008715731317402925590 1459283913890039011355508707962768378670089912271814269939 7029960262048228258868790549517649965467869270073982543218 9898935278604168262401211289885936468994712162687252315224 6913045970727309543777889345840036230236836446154459358910 8808562662807046966191966361168216090659606397372951397511 4328139205403181703561685657975520291419647125462156171
publicExponent	This is e, public part of key	65537
privateExponent	This is d, secret used to decrypt	(3072 bit) 3931961852845975205734878130438948923251513510083326472026 4402820309217450214817943688012078303857751269002305680794 2379029297141030717175118097748025802555662264489480527306 5257219723986272159409567843743824671229568865644243985359 6125781792701386183505830707137440117142183529051926817938 4652696896463654211010724580705303068542674434695195972734 7182476432687389761222075539176174921826337545575392278102 813435036010041768079216778751315960063104090773477561155 0382903008291662005396657491732428929653132099447168773239 6001162928093340951084350233547636634884120683393198902702 1330018968717191318595367228116178939904447412735228934152 3096780950566384384521241129919214370701496933795679678976 9829047445733558927343501951262512526357312920719427495740 5336633073824427604693036449545554456728660954726227622822 7492793593774913561670308180160797466929634915091701753717 5129441841983328853836715201947778912164754030713835729

prime1	This is p (first prime)	(1536 bit) 2324913895176850160063606233905125295037426465028743 1848780387569975535702097066115225568816523496919327 3796488705107942297769169723067694994007419978275345 5767445312391131144929986285986179616785321104096930 3212975866846849403017290404830074888146886344861232 2916870767802570162242650113836826915282820939739169 1406210340111925756509152296597267055270143894542937 9881344213713404476882250112062372724182924458316113 59845477089905679299497542735030637848129003827
prime2	This is q (second prime)	(1536 bit) 2294736680515164173249039714767750687253002937711786520986 8115127011527452155579071698131221245541126957647746380565 2787185972196290929290720127706470381260627318068750991105 8787690444818549548185021719530062175497386410916325918783 7658568651937554378602226782269686255852407809614696470633 1120870500428448113327753501965419996742591602357101160600 7026571943932666381427875719818656227181457017022938771458 866785212758953671092737250966456040400501108718112998473
exponent1	This is d mod (p-1)	(1535 bit) 6539075305521290110998741735137887691445272446080049914835 4194436327425667448192578536232966870259351810670166109239 8904492848178205488017734186607940483916721261568935192645 2918875934141515308330229322645027482563805996429117076120 5736031977419352664295714954122506047925672151618456284974 2012989518628924456735091485347197508696915226578622418231 3776120726934399794815415587823439009574992990916832092769 68033539713383763052904945092507105989514621472672870707
exponent2	This is d mod (q-1)	(1536 bit) 1637832109614070210230817426766197814165226748468903463778 9202331218871905977224570208459130033132913538473396473706 7836083602170586149938244422137080710954836251735415053480 7602621545796000330590392846067689828967846357889773123228 5492427289363734129018688068838165376867299810832614280640 4695207875368739627218502491843302039575071559452763536449 0054090502302430728560512606165028360813583676827822206902 35977760825202277978903334623295966336174067494674056129
coefficient	This is the value that helps combine results (CRT)	(1536 bit) 2247426497706608657575657837612475043955316228875362406968 9476360977488876705660543592426798207404983589047373093954 7470899626218160361830402907094488358499800193334300396650 1946817440902732258986612894381929980125403782269525285737 6620584579450502659793389154101308642676910951132331515913 2534894112778967816004493827647801786499029784361529529153 1206068030024624544714518714762385152673271985126302161580 211687366502408795928376147741522525049392523758925723486

Table 1: Field results for RSA private key

Public Key

- I expect to get the e and n. I took the OpenSSL format file and converted the pub file to a PEM form so that I can use the ASN.1 decoder. I got 2 elements: Version and modulus.

ASN.1 name	Meaning	Value
modulus	This is n	(3072 bit) 533506519430170549384581495278725897151476037577546980387977 095222584456643698582550150358703919158080560775989607298393 292955564723921068005109047687770896884905650961373845008928 198279307506079014612068982086247432257609007718408548331372 300422506016111804528615642110338767715673822046589759710906 679747956088069746913799863420659084213971935676595304358023 712682514256774416655919860319007317394016128080338071582348 413810495911117833987028541133304227738334123327023459232916 175257074154169198915626599378449755329902423562518441014971 973111160057895054700871573131740292559014592839138900390113 555087079627683786700899122718142699397029960262048228258868 790549517649965467869270073982543218989893527860416826240121 128988593646899471216268725231522469130459707273095437778893 458400362302368364461544593589108808562662807046966191966361 168216090659606397372951397511432813920540318170356168565797 5520291419647125462156171
publicExponent	This is e	65537

Sanity Check

- To confirm that the values we got using the two files are exactly the same if we would've used RSA, we can verify each of the properties. To check we could see if the modulus, n, are the same for the public and private keys and see if $p \times q = n$. We can also check if the $\lambda(n) = \text{lcm}(p-1, q-1)$ and can verify it using $e \cdot d = 1 \pmod{\lambda(n)}$ and $d = 1 \pmod{\lambda(n)}$. After calculations, we can verify that by multiplying p with q this gives us modulus, n, exactly and that the public exponent, e, and private exponent, d, are multiplicative inverse of mod lambda n. We also know from the experiment that the private key and public key share the n and e. Therefore, we can conclude that the private and public key form a valid RSA key pair.

