### **Optimization for Fully Connected Networks**

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient check import eval numerical gradient, eval numerica
        l_gradient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
        n-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
                returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs
        (y))))
In [2]: # Load the (preprocessed) CIFAR10 data.
```

```
In [2]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

# **Building upon your HW #3 implementation**

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine\_forward in nndl/layers.py
- affine\_backward in nndl/layers.py
- relu\_forward in nndl/layers.py
- relu\_backward in nndl/layers.py
- affine\_relu\_forward in nndl/layer\_utils.py
- affine\_relu\_backward in nndl/layer\_utils.py
- The FullyConnectedNet class in nndl/fc\_net.py

#### Test all functions you copy and pasted

```
In [3]: from nndl.layer tests import *
        affine forward test(); print('\n')
        affine backward test(); print('\n')
        relu forward test(); print('\n')
        relu_backward_test(); print('\n')
        affine_relu_test(); print('\n')
        fc net test()
        If affine_forward function is working, difference should be less than 1e-
        difference: 9.769849468192957e-10
        If affine_backward is working, error should be less than 1e-9::
        dx error: 1.7080572793816912e-10
        dw error: 3.635605517502198e-11
        db error: 8.865763799774247e-11
        If relu forward function is working, difference should be around 1e-8:
        difference: 4.999999798022158e-08
        If relu forward function is working, error should be less than 1e-9:
        dx error: 3.2756227385966328e-12
        If affine relu forward and affine relu backward are working, error should
        be less than 1e-9::
        dx error: 3.375302606376472e-11
dw error: 1.718953092920777e-10
        db error: 3.2755304933243622e-12
        Running check with reg = 0
        Initial loss: 2.3036302335690655
        W1 relative error: 1.874059469406586e-07
        W2 relative error: 2.7718383193017137e-07
        W3 relative error: 7.487491764797539e-07
        b1 relative error: 1.0840298013034233e-08
        b2 relative error: 2.192153290300306e-09
        b3 relative error: 8.084625476723435e-11
        Running check with reg = 3.14
        Initial loss: 6.929910430205594
        W1 relative error: 1.3875332034181178e-07
        W2 relative error: 7.526880271955046e-08
        W3 relative error: 4.1706873173251974e-08
        b1 relative error: 9.70713051820796e-08
        b2 relative error: 4.06193540421361e-08
        b3 relative error: 1.5300450731016278e-10
```

# Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

### SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd\_momentum in nndl/optim.py. Test your implementation of sgd momentum by running the cell below.

```
In [4]: from nndl.optim import sgd momentum
        N. D = 4.5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_momentum(w, dw, config=config)
        expected next w = np.asarray([
                                         0.27417895,
            [ 0.1406,
                                                      0.34096842,
                                                                  0.40775789],
                           0.20738947,
            [ 0.47454737,
                                        0.60812632,
                                                      0.67491579,
                                                                   0.74170526],
                           0.54133684,
            [ 0.80849474,
                           0.87528421,
                                         0.94207368,
                                                      1.00886316,
                                                                   1.07565263],
            [ 1.14244211, 1.20923158,
                                       1.27602105,
                                                      1.34281053,
                                                                   1.4096
                                                                             ]])
        expected_velocity = np.asarray([
            [0.\overline{5}406,
                           0.55475789,
                                         0.56891579, 0.58307368,
                                                                  0.59723158],
            [ 0.61138947,
                           0.62554737, 0.63970526,
                                                     0.65386316, 0.66802105],
                                                      0.72465263,
            [ 0.68217895, 0.69633684, 0.71049474,
                                                                   0.73881053],
            [ 0.75296842, 0.76712632, 0.78128421,
                                                      0.79544211,
                                                                   0.8096
                                                                             ]])
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel_error(expected_velocity, config['v
        elocity'])))
```

next\_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

### **SGD** + Nesterov momentum

Implement sgd\_nesterov\_momentum in ndl/optim.py.

```
In [5]: from nndl.optim import sgd_nesterov_momentum
        N, D = 4.5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
        expected next w = np.asarray([
                                         0.21778211,
             [0.08714,
                            0.15246105,
                                                      0.28310316,
                                                                   0.34842421],
             [0.41374526,
                                        0.54438737,
                            0.47906632.
                                                      0.60970842,
                                                                   0.67502947],
                           0.80567158,
                                                                  1.00163474],
1.32824 ]]
            [0.74035053.
                                         0.87099263,
                                                      0.93631368,
             [1.06695579,
                           1.13227684,
                                         1.19759789,
                                                      1.26291895,
        expected velocity = np.asarray([
            [0.\overline{5}406]
                            0.55475789,
                                         0.56891579,
                                                      0.58307368, 0.597231581,
            [ 0.61138947,
                            0.62554737,
                                         0.63970526,
                                                      0.65386316,
                                                                    0.66802105],
            [ 0.68217895,  0.69633684,  0.71049474,
                                                      0.72465263, 0.73881053],
            [ 0.75296842, 0.76712632, 0.78128421,
                                                      0.79544211,
                                                                   0.8096
                                                                              11)
        print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
        print('velocity error: {}'.format(rel_error(expected_velocity, config['v
        elocity'])))
```

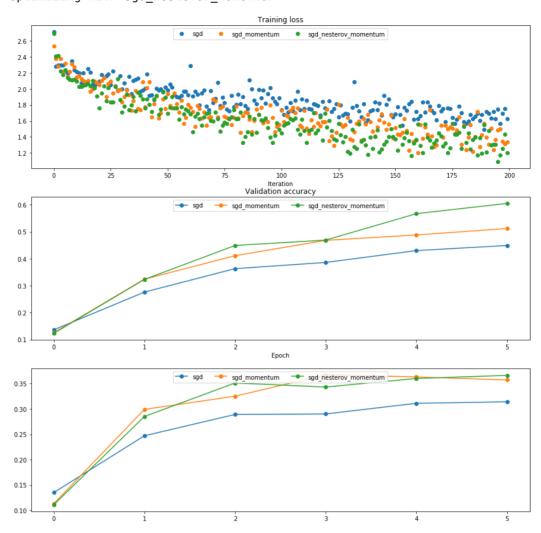
next\_w error: 1.0875186845081027e-08
velocity error: 4.269287743278663e-09

### Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
In [6]:
        num_train = 4000
        small_data = {
             'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
             'y_val': data['y_val'],
        solvers = {}
        for update rule in ['sgd', 'sgd momentum', 'sgd nesterov momentum']:
            print( Optimizing with {} . format(update_rule))
            model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e
        -2)
            solver = Solver(model, small data,
                             num epochs=5, batch size=100,
                             update rule=update rule,
                             optim_config={
                               'learning_rate': 1e-2,
                             },
                             verbose=False)
            solvers[update_rule] = solver
            solver.train()
            print
        fig, axes = plt.subplots(3, 1)
        ax = axes[0]
        ax.set_title('Training loss')
        ax.set_xlabel('Iteration')
        ax = axes[1]
        ax.set_title('Training accuracy')
        ax.set_xlabel('Epoch')
        ax = axes[1]
        ax.set title('Validation accuracy')
        ax.set_xlabel('Epoch')
        for update_rule, solver in solvers.items():
            ax = axes[0]
            ax.plot(solver.loss_history, 'o', label=update_rule)
            ax = axes[1]
            ax.plot(solver.train_acc_history, '-o', label=update_rule)
            ax = axes[2]
            ax.plot(solver.val_acc_history, '-o', label=update_rule)
        for i in [1, 2, 3]:
            ax = axes[i - 1]
            ax.legend(loc='upper center', ncol=4)
        plt.gcf().set_size_inches(15, 15)
        plt.show()
```

```
Optimizing with sgd
Optimizing with sgd_momentum
Optimizing with sgd_nesterov_momentum
```



# **RMSProp**

Now we go to techniques that adapt the gradient. Implement rmsprop in nndl/optim.py. Test your implementation by running the cell below.

```
In [7]: from nndl.optim import rmsprop
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
          dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
          a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
          config = {'learning_rate': 1e-2, 'a': a}
          next_w, _ = rmsprop(w, dw, config=config)
          expected next w = np.asarray([
             \left[ -0.39\overline{2}2384\overline{9}, \ -0.34037513, \ -0.28849239, \ -0.23659121, \ -0.18467247 \right], 
            [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
[ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
[ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
          expected_cache = np.asarray([
            [ 0.5976,
                            0.6126277,
                                             0.6277108,
                                                            0.64284931, 0.65804321],
            [ 0.67329252, 0.68859723,
                                             0.70395734, 0.71937285,
                                                                            0.73484377],
            [ 0.75037008, 0.7659518,
                                             0.78158892, 0.79728144, 0.81302936],
            [\ 0.82883269,\ 0.84469141,\ 0.86060554,\ 0.87657507,\ 0.8926
                                                                                        11)
          print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('cache error: {}'.format(rel_error(expected_cache, config['a'])))
         next w error: 9.524687511038133e-08
```

## **Adaptive moments**

Now, implement adam in nndl/optim.py. Test your implementation by running the cell below.

cache error: 2.6477955807156126e-09

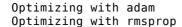
```
In [8]:
         # Test Adam implementation; you should see errors around 1e-7 or less
         from nndl.optim import adam
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
         config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
         next w, = adam(w, dw, config=config)
         expected_next_w = np.asarray([
           [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977], [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
                          0.17744702, 0.23002243, 0.28259667,
           [ 0.1248705,
                                                                    0.335169691
           [ 0.38774145, 0.44031188, 0.49288093, 0.54544852,
                                                                    0.5980145911)
         expected a = np.asarray([
           [ 0.69966,
                         0.68908382, 0.67851319, 0.66794809,
                                                                    0.65738853,],
                                                      0.61520571,
                          0.63628604, 0.6257431,
                                                                    0.60467385,],
           [ 0.64683452,
           [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, [ 0.54159906, 0.53110598, 0.52061845, 0.51013645,
                                                                    0.55209767,],
                                                                    0.49966,
                                                                                ]])
         expected_v = np.asarray([
           [ 0.48,
                       0.49947368,
                                         0.51894737,
                                                      0.53842105,
                                                                    0.55789474],
           [ 0.57736842, 0.59684211,
                                         0.61631579, 0.63578947,
                                                                    0.65526316],
           [ 0.67473684, 0.69421053,
                                        0.71368421, 0.73315789,
                                                                    0.75263158],
           [ 0.77210526, 0.79157895,
                                        0.81105263, 0.83052632,
                                                                    0.85
                                                                               11)
         print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('a error: {}'.format(rel_error(expected_a, config['a'])))
         print('v error: {}'.format(rel_error(expected_v, config['v'])))
        next_w error: 8.699924736323826e-05
```

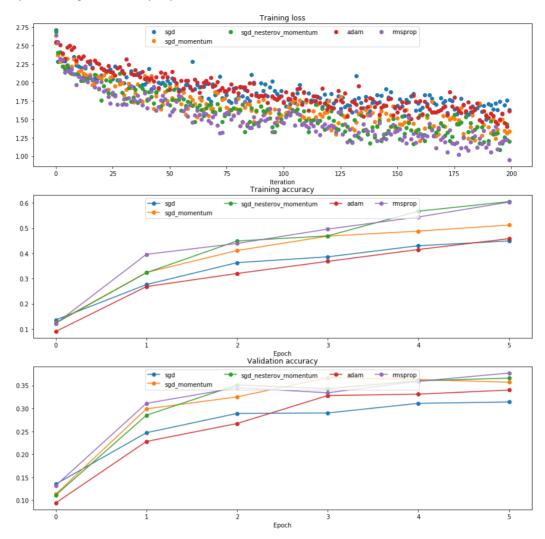
# Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

a error: 0.024836929252383348 v error: 4.214963193114416e-09

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
In [9]: learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
        for update_rule in ['adam', 'rmsprop']:
            print('Optimizing with {}'.format(update rule))
            model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e
        -2)
            solver = Solver(model, small_data,
                             num_epochs=5, batch_size=100,
                             update_rule=update_rule,
                             optim config={
                               'learning_rate': learning_rates[update_rule]
                             verbose=False)
            solvers[update_rule] = solver
            solver.train()
            print
        fig, axes = plt.subplots(3, 1)
        ax = axes[0]
        ax.set_title('Training loss')
        ax.set_xlabel('Iteration')
        ax = axes[1]
        ax.set_title('Training accuracy')
        ax.set_xlabel('Epoch')
        ax = axes[2]
        ax.set_title('Validation accuracy')
        ax.set_xlabel('Epoch')
        for update_rule, solver in solvers.items():
            ax = axes[0]
            ax.plot(solver.loss_history, 'o', label=update_rule)
            ax = axes[1]
            ax.plot(solver.train_acc_history, '-o', label=update_rule)
            ax = axes[2]
            ax.plot(solver.val acc history, '-o', label=update rule)
        for i in [1, 2, 3]:
            ax = axes[i - 1]
            ax.legend(loc='upper center', ncol=4)
        plt.gcf().set_size_inches(15, 15)
        plt.show()
```





# **Easier optimization**

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
In [10]:
         optimizer = 'adam'
         best_model = None
         layer_dims = [500, 500, 500]
         weight scale = 0.01
         learning_rate = 1e-3
         lr_{decay} = 0.9
         model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
                                    use_batchnorm=True)
         solver = Solver(model, data,
                          num_epochs=10, batch_size=100,
                          update_rule=optimizer,
                          optim_config={
                            'learning_rate': learning_rate,
                          lr_decay=lr_decay,
                          verbose=True, print_every=50)
         solver.train()
```

```
(Iteration 1 / 4900) loss: 2.262451
(Epoch 0 / 10) train acc: 0.140000; val acc: 0.155000
(Iteration 51 / 4900) loss: 1.777307
(Iteration 101 / 4900) loss: 1.659956
(Iteration 151 / 4900) loss: 1.613884
(Iteration 201 / 4900) loss: 1.600903
(Iteration 251 / 4900) loss: 1.499103
(Iteration 301 / 4900) loss: 1.413548
(Iteration 351 / 4900) loss: 1.377646
(Iteration 401 / 4900) loss: 1.334849
(Iteration 451 / 4900) loss: 1.427387
(Epoch 1 / 10) train acc: 0.524000; val acc: 0.499000
(Iteration 501 / 4900) loss: 1.409675
(Iteration 551 / 4900) loss: 1.390866
(Iteration 601 / 4900) loss: 1.336394
(Iteration 651 / 4900) loss: 1.517225
(Iteration 701 / 4900) loss: 1.281355
(Iteration 751 / 4900) loss: 1.217513
(Iteration 801 / 4900) loss: 1.404522
(Iteration 851 / 4900) loss: 1.244994
(Iteration 901 / 4900) loss: 1.250716
(Iteration 951 / 4900) loss: 1.307781
(Epoch 2 / 10) train acc: 0.552000; val_acc: 0.526000
(Iteration 1001 / 4900) loss: 1.252200
(Iteration 1051 / 4900) loss: 1.122882
(Iteration 1101 / 4900) loss: 0.991882
(Iteration 1151 / 4900) loss: 1.171788
(Iteration 1201 / 4900) loss: 1.150502
(Iteration 1251 / 4900) loss: 1.176916
(Iteration 1301 / 4900) loss: 0.997382
(Iteration 1351 / 4900) loss: 1.106426
(Iteration 1401 / 4900) loss: 1.003027
(Iteration 1451 / 4900) loss: 1.078969
(Epoch 3 / 10) train acc: 0.605000; val_acc: 0.544000
(Iteration 1501 / 4900) loss: 1.132291
(Iteration 1551 / 4900) loss: 1.048286
(Iteration 1601 / 4900) loss: 0.969781
(Iteration 1651 / 4900) loss: 1.172605
(Iteration 1701 / 4900) loss: 1.013117
(Iteration 1751 / 4900) loss: 0.985120
(Iteration 1801 / 4900) loss: 0.850634
(Iteration 1851 / 4900) loss: 1.064179
(Iteration 1901 / 4900) loss: 0.962034
(Iteration 1951 / 4900) loss: 0.887884
(Epoch 4 / 10) train acc: 0.684000; val_acc: 0.546000
(Iteration 2001 / 4900) loss: 0.969318
(Iteration 2051 / 4900) loss: 0.902149
(Iteration 2101 / 4900) loss: 0.910347
(Iteration 2151 / 4900) loss: 0.856774
(Iteration 2201 / 4900) loss: 0.937697
(Iteration 2251 / 4900) loss: 0.958938
(Iteration 2301 / 4900) loss: 0.839748
(Iteration 2351 / 4900) loss: 0.984624
(Iteration 2401 / 4900) loss: 1.084647
(Epoch 5 / 10) train acc: 0.689000; val acc: 0.541000
(Iteration 2451 / 4900) loss: 1.053752
(Iteration 2501 / 4900) loss: 0.997177
(Iteration 2551 / 4900) loss: 0.750070
(Iteration 2601 / 4900) loss: 0.736606
(Iteration 2651 / 4900) loss: 0.881684
(Iteration 2701 / 4900) loss: 0.812084
(Iteration 2751 / 4900) loss: 0.743127
(Iteration 2801 / 4900) loss: 0.768724
(Iteration 2851 / 4900) loss: 0.742728
(Iteration 2901 / 4900) loss: 0.886776
(Epoch 6 / 10) train acc: 0.720000; val_acc: 0.553000
(Iteration 2951 / 4900) loss: 0.649285
(Iteration 3001 / 4900) loss: 0.861470
```

```
In [11]: 
y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val'])))
print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test_'])))
```

Validation set accuracy: 0.571 Test set accuracy: 0.568

#### **Batch Normalization**

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl fc net import
        from nndl.layers import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient check import eval numerical gradient, eval numerica
        l_gradient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
        n-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
                returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs
        (y))))
```

```
In [2]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

# **Batchnorm forward pass**

Implement the training time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: # Check the training-time forward pass by checking means and variances
        # of features both before and after batch normalization
        # Simulate the forward pass for a two-layer network
        N, D1, D2, D3 = 200, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)
        print('Before batch normalization:')
        print(' means: ', a.mean(axis=0))
        print(' stds: ', a.std(axis=0))
        # Means should be close to zero and stds close to one
        print('After batch normalization (gamma=1, beta=0)')
        a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'tr
        print('
                mean: ', a_norm.mean(axis=0))
        print(' std: ', a_norm.std(axis=0))
        # Now means should be close to beta and stds close to gamma
        gamma = np.asarray([1.0, 2.0, 3.0])
        beta = np.asarray([11.0, 12.0, 13.0])
        a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print('After batch normalization (nontrivial gamma, beta)')
        print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
        Before batch normalization:
          After batch normalization (gamma=1, beta=0)
          mean: [-2.38697950e-16 -2.39808173e-16 -4.60742555e-17]
          std: [1. 1. 1.]
        After batch normalization (nontrivial gamma, beta)
          means: [11. 12. 13.]
                             1.99999999 2.99999999]
          stds: [1.
```

Implement the testing time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [4]: # Check the test-time forward pass by running the training-time
         # forward pass many times to warm up the running averages, and then
         # checking the means and variances of activations after a test-time
         # forward pass.
         N, D1, D2, D3 = 200, 50, 60, 3
         W1 = np.random.randn(D1, D2)
         W2 = np.random.randn(D2, D3)
         bn param = {'mode': 'train'}
         qamma = np.ones(D3)
         beta = np.zeros(D3)
         for t in np.arange(50):
             X = np.random.randn(N. D1)
             a = np.maximum(0, X.dot(W1)).dot(W2)
             batchnorm forward(a, gamma, beta, bn param)
         bn param['mode'] = 'test'
         X = np.random.randn(N, D1)
         a = np.maximum(0, X.dot(W1)).dot(W2)
         a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)
         # Means should be close to zero and stds close to one, but will be
         # noisier than training-time forward passes.
         print('After batch normalization (test-time):')
        print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
        After batch normalization (test-time):
          means: [-0.05967139 \quad 0.00957257 \quad -0.0259153]
          stds: [1.0150653 0.99071727 1.00119239]
```

## **Batchnorm backward pass**

Implement the backward pass for the batchnorm layer, batchnorm\_backward in nndl/layers.py. Check your implementation by running the following cell.

```
In [5]: # Gradient check batchnorm backward pass
         N, D = 4, 5
         x = 5 * np.random.randn(N, D) + 12
         gamma = np.random.randn(D)
         beta = np.random.randn(D)
         dout = np.random.randn(N, D)
         bn_param = {'mode': 'train'}
         fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
         fg = lambda a: batchnorm_forward(x, gamma, beta, bn_param)[0]
         fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0]
         dx_num = eval_numerical_gradient_array(fx, x, dout)
         da_num = eval_numerical_gradient_array(fg, gamma, dout)
db_num = eval_numerical_gradient_array(fb, beta, dout)
          , cache = batchnorm forward(x, gamma, beta, bn param)
         dx, dgamma, dbeta = batchnorm backward(dout, cache)
         print('dx error: ', rel_error(dx_num, dx))
         print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
         dx error: 1.0365309983627649e-08
         dgamma error: 4.235503173805597e-12
         dbeta error: 3.275576553527879e-12
```

# Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in  $nndl/fc_net.py$  to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in \_\_init\_\_.
- (2) The batchnorm\_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine\_batchnorm\_relu() layer in nndl/layer\_utils.py although this is not necessary.
- (3) The batchnorm backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

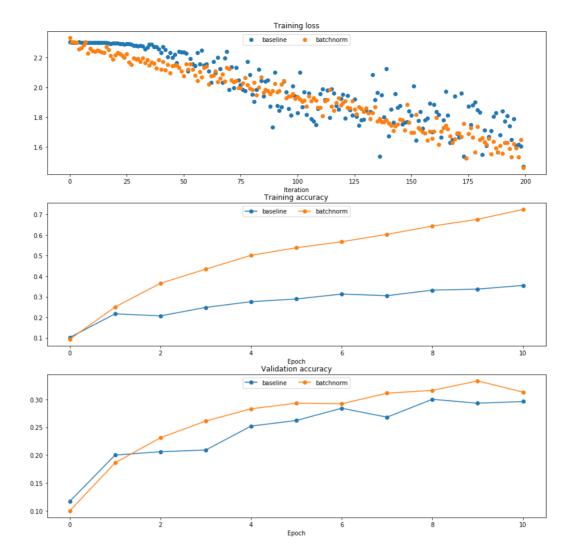
```
In [6]: N, D, H1, H2, C = 2, 15, 20, 30, 10
        X = np.random.randn(N, D)
        y = np.random.randint(C, size=(N,))
        for reg in [0, 3.14]:
            print('Running check with reg = ', reg)
            model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                       reg=reg, weight scale=5e-2, dtype=np.float
        64.
                                      use batchnorm=True)
            loss, grads = model.loss(X, y)
            print('Initial loss: ', loss)
            for name in sorted(grads):
                f = lambda : model.loss(X, y)[0]
                grad num = eval numerical gradient(f, model.params[name], verbos
        e=False, h=1e-5)
                print('{} relative error: {}'.format(name, rel_error(grad_num, g
        rads[name])))
            if reg == 0: print('\n')
        Running check with reg = 0
        Initial loss: 2.495181649437833
        W1 relative error: 5.7133128371328395e-05
        W2 relative error: 6.152107138686845e-06
        W3 relative error: 3.860542911698204e-10
        b1 relative error: 2.220446049250313e-08
        b2 relative error: 5.551115123125783e-09
        b3 relative error: 1.303595543107751e-10
        beta1 relative error: 4.66520471937565e-08
        beta2 relative error: 1.616541206944714e-09
        gamma1 relative error: 3.0691595985183625e-08
        gamma2 relative error: 2.3542593993916706e-09
        Running check with reg = 3.14
        Initial loss: 6.988149746148828
        W1 relative error: 3.63450880030614e-07
        W2 relative error: 1.4399569445718448e-08
        W3 relative error: 6.072364329088387e-08
        b1 relative error: 1.734723475976807e-10
        b2 relative error: 2.7755575615628914e-09
        b3 relative error: 1.4826365551616593e-10
        betal relative error: 3.12891605875848e-06
        beta2 relative error: 4.003822494515134e-08
        gamma1 relative error: 4.038265200968759e-06
        gamma2 relative error: 3.0722719270750266e-08
```

# Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
In [7]:
        # Try training a very deep net with batchnorm
        hidden_dims = [100, 100, 100, 100, 100]
        num train = 1000
        small data = {
             'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
'y_val': data['y_val'],
        }
        weight scale = 2e-2
        bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use
         batchnorm=True)
        model = FullyConnectedNet(hidden dims, weight scale=weight scale, use ba
        tchnorm=False)
        bn solver = Solver(bn model, small data,
                         num_epochs=10, batch_size=50,
                         update_rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
                         verbose=True, print_every=200)
        bn_solver.train()
        solver = Solver(model, small_data,
                         num epochs=10, batch size=50,
                         update rule='adam',
                          optim_config={
                            'learning_rate': 1e-3,
                         verbose=True, print_every=200)
        solver.train()
        (Iteration 1 / 200) loss: 2.330732
        (Epoch 0 / 10) train acc: 0.093000; val_acc: 0.100000
        (Epoch 1 / 10) train acc: 0.250000; val_acc: 0.186000 (Epoch 2 / 10) train acc: 0.365000; val_acc: 0.231000
        (Epoch 3 / 10) train acc: 0.434000; val_acc: 0.261000
        (Epoch 4 / 10) train acc: 0.501000; val_acc: 0.283000
        (Epoch 5 / 10) train acc: 0.538000; val_acc: 0.293000
        (Epoch 6 / 10) train acc: 0.567000; val_acc: 0.292000
        (Epoch 7 / 10) train acc: 0.603000; val_acc: 0.311000
        (Epoch 8 / 10) train acc: 0.643000; val_acc: 0.316000
        (Epoch 9 / 10) train acc: 0.676000; val_acc: 0.333000
        (Epoch 10 / 10) train acc: 0.724000; val_acc: 0.313000
        (Iteration 1 / 200) loss: 2.303350
        (Epoch 0 / 10) train acc: 0.102000; val_acc: 0.117000
        (Epoch 1 / 10) train acc: 0.217000; val_acc: 0.200000
        (Epoch 2 / 10) train acc: 0.207000; val_acc: 0.206000
        (Epoch 3 / 10) train acc: 0.248000; val_acc: 0.209000
        (Epoch 4 / 10) train acc: 0.276000; val_acc: 0.252000
        (Epoch 5 / 10) train acc: 0.289000; val_acc: 0.262000
        (Epoch 6 / 10) train acc: 0.313000; val_acc: 0.284000
        (Epoch 7 / 10) train acc: 0.305000; val_acc: 0.268000
        (Epoch 8 / 10) train acc: 0.332000; val_acc: 0.300000
        (Epoch 9 / 10) train acc: 0.337000; val_acc: 0.293000
        (Epoch 10 / 10) train acc: 0.355000; val_acc: 0.296000
```

```
In [8]: fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set_title('Training accuracy')
ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set_title('Validation accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[0]
         ax.plot(solver.loss_history, 'o', label='baseline')
ax.plot(bn_solver.loss_history, 'o', label='batchnorm')
         ax = axes[1]
         ax.plot(solver.train_acc_history, '-o', label='baseline')
         ax.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
         ax = axes[2]
         ax.plot(solver.val_acc_history, '-o', label='baseline')
         ax.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
         for i in [1, 2, 3]:
              ax = axes[i - 1]
              ax.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```

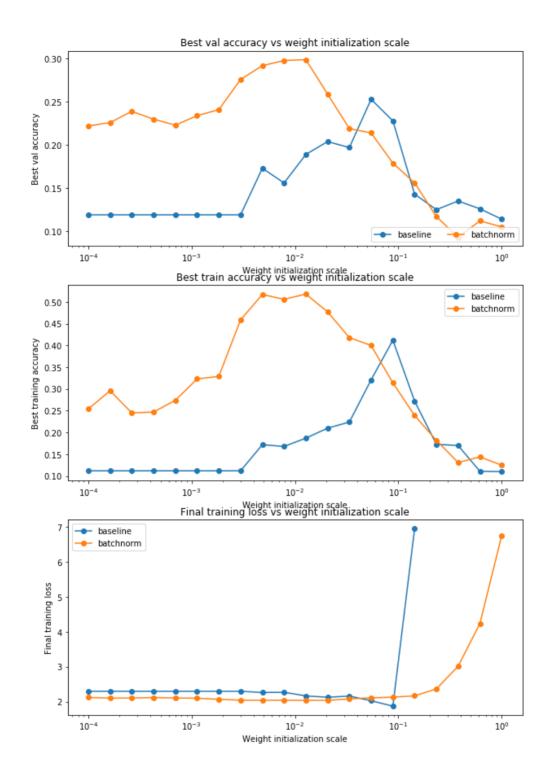


# **Batchnorm and initialization**

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
In [9]:
        # Try training a very deep net with batchnorm
        hidden_dims = [50, 50, 50, 50, 50, 50, 50]
        num train = 1000
        small data = {
             'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
'y_val': data['y_val'],
        }
        bn solvers = {}
        solvers = {}
        weight scales = np.logspace(-4, 0, num=20)
        for i, weight scale in enumerate(weight scales):
            print('Running weight scale {} / {} '.format(i + 1, len(weight_scale
        s)))
             bn model = FullyConnectedNet(hidden dims, weight scale=weight scale,
        use_batchnorm=True)
            model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, us
        e batchnorm=False)
             bn_solver = Solver(bn_model, small_data,
                             num epochs=10, batch size=50,
                             update_rule='adam',
                             optim_config={
                                'learning_rate': 1e-3,
                             },
                             verbose=False, print every=200)
             bn solver.train()
             bn_solvers[weight_scale] = bn_solver
             solver = Solver(model, small_data,
                             num epochs=10, batch size=50,
                             update rule='adam',
                             optim_config={
                               'learning_rate': 1e-3,
                             verbose=False, print_every=200)
             solver.train()
             solvers[weight scale] = solver
        Running weight scale 1 / 20
        Running weight scale 2 / 20
        Running weight scale 3 / 20
        Running weight scale 4 / 20
        Running weight scale 5 / 20
        Running weight scale 6 / 20
        Running weight scale 7 / 20
        Running weight scale 8 / 20
        Running weight scale 9 / 20
        Running weight scale 10 / 20
        Running weight scale 11 / 20
        Running weight scale 12 / 20
        Running weight scale 13 / 20
        Running weight scale 14 / 20
        Running weight scale 15 / 20
        Running weight scale 16 / 20
        /home/dennis/Documents/PY_PROGRAM/UCLA_C247/HW4-code/HW4-code/nndl/layer
        s.py:446: RuntimeWarning: divide by zero encountered in log
          loss = -np.sum(np.log(probs[np.arange(N), y])) / N
        Running weight scale 17 / 20
        Running weight scale 18 / 20
        Running weight scale 19 / 20
        Running weight scale 20 / 20
```

```
In [10]:
         # Plot results of weight scale experiment
          best_train_accs, bn_best_train_accs = [], []
          best_val_accs, bn_best_val_accs = [], []
          final_train_loss, bn_final_train_loss = [], []
          for ws in weight_scales:
              best train accs.append(max(solvers[ws].train acc history))
              bn best train accs.append(max(bn solvers[ws].train acc history))
              best val accs.append(max(solvers[ws].val acc history))
              bn best val accs.append(max(bn solvers[ws].val acc history))
              final train_loss.append(np.mean(solvers[ws].loss_history[-100:]))
              bn final train loss.append(np.mean(bn solvers[ws].loss history[-10
          0:1))
          plt.subplot(3, 1, 1)
          plt.title('Best val accuracy vs weight initialization scale')
          plt.xlabel('Weight initialization scale')
          plt.ylabel('Best val accuracy')
         plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
          plt.legend(ncol=2, loc='lower right')
          plt.subplot(3, 1, 2)
          plt.title('Best train accuracy vs weight initialization scale')
          plt.xlabel('Weight initialization scale')
          plt.ylabel('Best training accuracy')
          plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
          plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
          plt.legend()
          plt.subplot(3, 1, 3)
          plt.title('Final training loss vs weight initialization scale')
          plt.xlabel('Weight initialization scale')
          plt.ylabel('Final training loss')
          plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
          plt.semilogx(weight scales, bn final train loss, '-o', label='batchnorm
          plt.legend()
          plt.gcf().set_size_inches(10, 15)
          plt.show()
```



# **Question:**

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

#### **Answer:**

On one hand, compared to the case without batch normalization, training with batch normalization allows us to train with a less bigger weight initialization scale, which is 2e-3, while the case without batch normalization is 5e-3. On the other hand, training with batch normalization tolerates greater weight initialization scale, meaning that training loss does not goes to ifinity with 1e-1 weight initialization scale. The main reason is that batch normalization acts as a regularization, which to some extent reduces the possibility for each layer of going to extreme values.

# **Dropout**

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [1]: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import
        from nndl.layers import *
        from cs231n.data_utils import get_CIFAR10_data
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerica
        l_gradient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-i
        n-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
                returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs
        (y))))
```

```
In [2]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

# **Dropout forward pass**

Implement the training and test time dropout forward pass, dropout\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: x = np.random.randn(500, 500) + 10
        for p in [0.3, 0.6, 0.75]:
            out, = dropout forward(x, {'mode': 'train', 'p': p})
            out test, = dropout forward(x, {'mode': 'test', 'p': p})
            print('Running tests with p = ', p)
            print('Mean of input: ', x.mean())
            print('Mean of train-time output: ', out.mean())
print('Mean of test-time output: ', out_test.mean())
            print('Fraction of train-time output set to zero: ', (out == 0).mean
        ())
            print('Fraction of test-time output set to zero: ', (out_test == 0).
        mean())
        Running tests with p = 0.3
        Mean of input: 9.997543371838061
        Mean of train-time output: 9.99068001546249
        Mean of test-time output: 9.997543371838061
        Fraction of train-time output set to zero: 0.300588
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.6
        Mean of input: 9.997543371838061
        Mean of train-time output: 9.951918706035858
        Mean of test-time output: 9.997543371838061
        Fraction of train-time output set to zero: 0.60184
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.75
        Mean of input: 9.997543371838061
        Mean of train-time output: 10.016241307563895
        Mean of test-time output: 9.997543371838061
        Fraction of train-time output set to zero: 0.74962
        Fraction of test-time output set to zero: 0.0
```

## **Dropout backward pass**

Implement the backward pass, dropout\_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

### Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc\_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
In [5]: N, D, H1, H2, C = 2, 15, 20, 30, 10
        X = np.random.randn(N, D)
        y = np.random.randint(C, size=(N,))
        for dropout in [0.5, 0.75, 1.0]:
             print('Running check with dropout = ', dropout)
             model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                        weight_scale=5e-2, dtype=np.float64,
                                        dropout=dropout, seed=123)
             loss, grads = model.loss(X, y)
             print('Initial loss: ', loss)
             for name in sorted(grads):
                 f = lambda _: model.loss(X, y)[0]
                 grad_num = eval_numerical_gradient(f, model.params[name], verbos
        e=False, h=1e-5)
                 print('{} relative error: {}'.format(name, rel_error(grad_num, g
        rads[name])))
             print('\n')
        Running check with dropout = 0.5 Initial loss: 2.3130766680585553
        W1 relative error: 3.521651327461513e-07
        W2 relative error: 8.67050333013485e-08
        W3 relative error: 1.7697091527236745e-08
        b1 relative error: 1.3630944494006748e-09
        b2 relative error: 3.369320802894315e-10
        b3 relative error: 1.1749705566445823e-10
        Running check with dropout = 0.75
        Initial loss: 2.3021392488536803
        W1 relative error: 8.48825148891291e-08
        W2 relative error: 7.320957078668507e-10
        W3 relative error: 3.1539905478679266e-09
        b1 relative error: 4.991935528845047e-10
        b2 relative error: 2.3792592457209184e-10
        b3 relative error: 1.480081274701072e-10
        Running check with dropout = 1.0 Initial loss: 2.3053332250963194
        W1 relative error: 1.2744095365229032e-06
        W2 relative error: 4.678743300473988e-07
        W3 relative error: 4.331673892536035e-08
        b1 relative error: 4.0853539035931665e-08
        b2 relative error: 1.951342257912746e-09
        b3 relative error: 9.387142701440351e-11
```

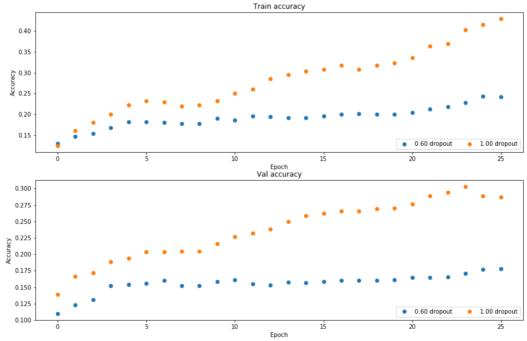
# Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
In [6]: # Train two identical nets, one with dropout and one without
         num_train = 500
         small_data = {
              'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
'X_val': data['X_val'],
'y_val': data['y_val'],
         }
         solvers = {}
         dropout_choices = [0.6, 1.0]
         for dropout in dropout_choices:
             model = FullyConnectedNet([100, 100, 100], dropout=dropout)
             solver = Solver(model, small_data,
                               num_epochs=25, batch_size=100,
                               update rule='adam',
                               optim_config={
                                  'learning_rate': 5e-4,
                               verbose=True, print_every=100)
             solver.train()
             solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.303100
(Epoch 0 / 25) train acc: 0.130000; val acc: 0.110000
(Epoch 1 / 25) train acc: 0.146000; val acc: 0.123000
(Epoch 2 / 25) train acc: 0.154000; val acc: 0.131000
(Epoch 3 / 25) train acc: 0.168000; val_acc: 0.152000
(Epoch 4 / 25) train acc: 0.182000; val acc: 0.154000
(Epoch 5 / 25) train acc: 0.182000; val_acc: 0.156000
(Epoch 6 / 25) train acc: 0.180000; val_acc: 0.160000
(Epoch 7 / 25) train acc: 0.178000; val_acc: 0.152000 (Epoch 8 / 25) train acc: 0.178000; val_acc: 0.152000
(Epoch 9 / 25) train acc: 0.190000; val_acc: 0.159000
(Epoch 10 / 25) train acc: 0.186000; val_acc: 0.161000
(Epoch 11 / 25) train acc: 0.196000; val_acc: 0.155000
(Epoch 12 / 25) train acc: 0.194000; val_acc: 0.153000
(Epoch 13 / 25) train acc: 0.192000; val_acc: 0.158000 (Epoch 14 / 25) train acc: 0.192000; val_acc: 0.157000 (Epoch 15 / 25) train acc: 0.196000; val_acc: 0.159000
(Epoch 16 / 25) train acc: 0.200000; val_acc: 0.160000
(Epoch 17 / 25) train acc: 0.202000; val_acc: 0.160000
(Epoch 18 / 25) train acc: 0.200000; val_acc: 0.160000
(Epoch 19 / 25) train acc: 0.200000; val_acc: 0.161000
(Epoch 20 / 25) train acc: 0.204000; val_acc: 0.165000
(Iteration 101 / 125) loss: 2.251923
(Epoch 21 / 25) train acc: 0.212000; val_acc: 0.165000
(Epoch 22 / 25) train acc: 0.218000; val_acc: 0.166000
(Epoch 23 / 25) train acc: 0.228000; val acc: 0.171000
(Epoch 24 / 25) train acc: 0.244000; val_acc: 0.177000
(Epoch 25 / 25) train acc: 0.242000; val_acc: 0.178000
(Iteration 1 / 125) loss: 2.300607
(Epoch 0 / 25) train acc: 0.124000; val_acc: 0.139000
(Epoch 1 / 25) train acc: 0.160000; val acc: 0.167000
(Epoch 2 / 25) train acc: 0.180000; val_acc: 0.172000
(Epoch 3 / 25) train acc: 0.200000; val_acc: 0.189000
(Epoch 4 / 25) train acc: 0.222000; val_acc: 0.194000
(Epoch 5 / 25) train acc: 0.232000; val_acc: 0.204000
(Epoch 6 / 25) train acc: 0.230000; val_acc: 0.204000
(Epoch 7 / 25) train acc: 0.220000; val_acc: 0.205000
(Epoch 8 / 25) train acc: 0.222000; val_acc: 0.205000
(Epoch 9 / 25) train acc: 0.232000; val acc: 0.216000
(Epoch 10 / 25) train acc: 0.250000; val_acc: 0.227000
(Epoch 11 / 25) train acc: 0.260000; val_acc: 0.232000
(Epoch 12 / 25) train acc: 0.286000; val_acc: 0.238000 (Epoch 13 / 25) train acc: 0.296000; val_acc: 0.250000
(Epoch 14 / 25) train acc: 0.304000; val_acc: 0.259000
(Epoch 15 / 25) train acc: 0.308000; val_acc: 0.262000
(Epoch 16 / 25) train acc: 0.318000; val_acc: 0.266000
(Epoch 17 / 25) train acc: 0.308000; val_acc: 0.266000
(Epoch 18 / 25) train acc: 0.318000; val_acc: 0.269000 (Epoch 19 / 25) train acc: 0.324000; val_acc: 0.270000 (Epoch 20 / 25) train acc: 0.336000; val_acc: 0.276000
(Iteration 101 / 125) loss: 1.753858
(Epoch 21 / 25) train acc: 0.364000; val_acc: 0.289000
(Epoch 22 / 25) train acc: 0.370000; val_acc: 0.294000
(Epoch 23 / 25) train acc: 0.404000; val_acc: 0.303000
(Epoch 24 / 25) train acc: 0.416000; val_acc: 0.289000
(Epoch 25 / 25) train acc: 0.430000; val acc: 0.287000
```

```
In [7]: # Plot train and validation accuracies of the two models
         train_accs = []
         val_accs = []
         for dropout in dropout choices:
             solver = solvers[dropout]
             train_accs.append(solver.train_acc_history[-1])
             val_accs.append(solver.val_acc_history[-1])
         plt.subplot(3, 1, 1)
         for dropout in dropout choices:
             plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropou
         t' % dropout)
         plt.title('Train accuracy')
plt.xlabel('Epoch')
         plt.ylabel('Accuracy')
         plt.legend(ncol=2, loc='lower right')
         plt.subplot(3, 1, 2)
         for dropout in dropout_choices:
             plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout'
         % dropout)
         plt.title('Val accuracy')
plt.xlabel('Epoch')
         plt.ylabel('Accuracy')
         plt.legend(ncol=2, loc='lower right')
         plt.gcf().set size inches(15, 15)
         plt.show()
```



#### Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

#### **Answer:**

Yes, it is. As we can see from our experiment result, training with more dropout rate achieves a better result than training with less dropout rate. That is exactly what regularization is doing.

#### Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
In [8]: # ----- #
       # YOUR CODE HERE:
         Implement a FC-net that achieves at least 55% validation accuracy
         on CIFAR-10.
       hidden_dims = [512, 256, 128, 64]
       lr decay = 0.9
       learning_rate = 5e-3
       weight scale = 0.01
       dropout = 0.2
       reg = 0.0
       update_rule = 'adam'
       model = FullyConnectedNet(hidden dims = hidden dims, weight scale = weig
       ht scale,
                             dropout=dropout, use batchnorm=True, reg=reg)
       solver = Solver(model, data,
                   num_epochs=25, batch_size=1024,
                   update_rule=update_rule,
                   optim_config={
                     'learning_rate': learning_rate,
                   lr_decay=lr_decay,
                   verbose=True, print_every=500)
       solver.train()
       #print out the validation accuracy
       y_test_pred = np.argmax(model.loss(data['X_test']), axis=1)
       y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
       print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y
       _val'])))
       print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test
       '])))
       # ----- #
       # END YOUR CODE HERE
       # ================== #
```

```
(Iteration 1 / 1175) loss: 2.305102
(Epoch 0 / 25) train acc: 0.221000; val acc: 0.208000
(Epoch 1 / 25) train acc: 0.429000; val_acc: 0.408000
(Epoch 2 / 25) train acc: 0.445000; val acc: 0.455000
(Epoch 3 / 25) train acc: 0.476000; val acc: 0.505000
(Epoch 4 / 25) train acc: 0.519000; val acc: 0.508000
(Epoch 5 / 25) train acc: 0.545000; val_acc: 0.519000
(Epoch 6 / 25) train acc: 0.584000; val_acc: 0.527000
(Epoch 7 / 25) train acc: 0.589000; val_acc: 0.535000 (Epoch 8 / 25) train acc: 0.594000; val_acc: 0.547000
(Epoch 9 / 25) train acc: 0.623000; val_acc: 0.553000
(Epoch 10 / 25) train acc: 0.630000; val acc: 0.549000
(Iteration 501 / 1175) loss: 1.158378
(Epoch 11 / 25) train acc: 0.647000; val_acc: 0.551000
(Epoch 12 / 25) train acc: 0.644000; val_acc: 0.545000 (Epoch 13 / 25) train acc: 0.653000; val_acc: 0.556000 (Epoch 14 / 25) train acc: 0.668000; val_acc: 0.558000
(Epoch 15 / 25) train acc: 0.664000; val_acc: 0.564000
(Epoch 16 / 25) train acc: 0.678000; val_acc: 0.563000
(Epoch 17 / 25) train acc: 0.708000; val_acc: 0.558000
(Epoch 18 / 25) train acc: 0.721000; val_acc: 0.573000
(Epoch 19 / 25) train acc: 0.677000; val_acc: 0.573000 (Epoch 20 / 25) train acc: 0.716000; val_acc: 0.571000
(Epoch 21 / 25) train acc: 0.704000; val_acc: 0.570000
(Iteration 1001 / 1175) loss: 0.964139
(Epoch 22 / 25) train acc: 0.721000; val acc: 0.574000
(Epoch 23 / 25) train acc: 0.736000; val_acc: 0.584000
(Epoch 24 / 25) train acc: 0.713000; val_acc: 0.575000
(Epoch 25 / 25) train acc: 0.751000; val acc: 0.566000
Validation set accuracy: 0.584
Test set accuracy: 0.589
```

```
import numpy as np
import pdb
from .layers import *
from .layer utils import *
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
class TwoLayerNet(object):
    A two-layer fully-connected neural network with ReLU nonlinearity and
    softmax loss that uses a modular layer design. We assume an input dimension
    of D, a hidden dimension of H, and perform classification over C classes.
    The architecure should be affine - relu - affine - softmax.
    Note that this class does not implement gradient descent; instead, it
    will interact with a separate Solver object that is responsible for running
    optimization.
    The learnable parameters of the model are stored in the dictionary
    self.params that maps parameter names to numpy arrays.
    def init (self, input dim=3*32*32, hidden dims=100, num classes=10,
                dropout=0, weight scale=1e-3, reg=0.0):
        Initialize a new network.
        - input dim: An integer giving the size of the input
        - hidden_dims: An integer giving the size of the hidden layer
        - num_classes: An integer giving the number of classes to classify
        - dropout: Scalar between 0 and 1 giving dropout strength.
        - weight_scale: Scalar giving the standard deviation for random
         initialization of the weights.
        - reg: Scalar giving L2 regularization strength.
        self.params = {}
        self.reg = reg
        # YOUR CODE HERE:
           Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
           self.params['W2'], self.params['b1'] and self.params['b2']. The
           biases are initialized to zero and the weights are initialized
           so that each parameter has mean 0 and standard deviation weight scale.
           The dimensions of W1 should be (input_dim, hidden_dim) and the
           dimensions of W2 should be (hidden_dims, num_classes)
        self.params['W1'] = np.random.randn(input_dim, hidden_dims) * weight_scale
        self.params['W2'] = np.random.randn(hidden_dims, num_classes) *
weight scale
        self.params['b1'] = np.zeros(hidden_dims)
        self.params['b2'] = np.zeros(num_classes)
```

# END YOUR CODE HERE

```
def loss(self, X, y=None):
       Compute loss and gradient for a minibatch of data.
        - X: Array of input data of shape (N, d 1, ..., d k)
       - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
       Returns:
       If y is None, then run a test-time forward pass of the model and return:
        - scores: Array of shape (N, C) giving classification scores, where
         scores[i, c] is the classification score for X[i] and class c.
       If y is not None, then run a training-time forward and backward pass and
       return a tuple of:
        - loss: Scalar value giving the loss
        - grads: Dictionary with the same keys as self.params, mapping parameter names to gradients of the loss with respect to those parameters.
       scores = None
       # YOUR CODE HERE:
           Implement the forward pass of the two-layer neural network. Store the class scores as the variable 'scores'. Be sure to use the layers
           you prior implemented.
                         ------ #
       out1, cache1 = affine_relu_forward(X, self.params['W1'], self.params['b1'])
        scores, cache2 = affine forward(out1, self.params['W2'], self.params['b2'])
       # END YOUR CODE HERE
       # ============= #
       # If y is None then we are in test mode so just return scores
       if v is None:
           return scores
       loss, grads = 0, {}
        # YOUR CODE HERE:
           Implement the backward pass of the two-layer neural net. Store
           the loss as the variable 'loss' and store the gradients in the
           'grads' dictionary. For the grads dictionary, grads['Wl'] holds the gradient for Wl, grads['bl'] holds the gradient for bl, etc.
           i.e., grads[k] holds the gradient for self.params[k].
           Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
           for each W. Be sure to include the 0.5 multiplying factor to
           match our implementation.
          And be sure to use the layers you prior implemented.
       loss,dscores = softmax_loss(scores, y)
       loss += 0.5 * self.reg * np.sum(self.params['W1'] ** 2) + 0.5 * self.reg *
np.sum(self.params['W2'] ** 2)
       dx2,grads['W2'],grads['b2'] = affine_backward(dscores,cache2)
       dx1,grads['W1'],grads['b1'] = affine_relu_backward(dx2,cache1)
       grads['W2'] += self.reg * self.params['W2']
       grads['W1'] += self.reg * self.params['W1']
       # END YOUR CODE HERE
```

```
return loss, grads
```

```
class FullyConnectedNet(object):
    A fully-connected neural network with an arbitrary number of hidden layers, ReLU nonlinearities, and a softmax loss function. This will also implement
    dropout and batch normalization as options. For a network with L layers,
    the architecture will be
    {affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax
    where batch normalization and dropout are optional, and the \{\ldots\} block is
    repeated L - 1 times.
    Similar to the TwoLayerNet above, learnable parameters are stored in the
    self.params dictionary and will be learned using the Solver class.
    def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
                dropout=0, use_batchnorm=False, reg=0.0,
               weight_scale=1e-2, dtype=np.float32, seed=None):
        Initialize a new FullyConnectedNet.
        Inputs:
        hidden_dims: A list of integers giving the size of each hidden layer.input_dim: An integer giving the size of the input.
        - num_classes: An integer giving the number of classes to classify.
        - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=1
then
          the network should not use dropout at all.
        - use_batchnorm: Whether or not the network should use batch normalization.
        - reg: Scalar giving L2 regularization strength.
        - weight_scale: Scalar giving the standard deviation for random
          initialization of the weights.
        - dtype: A numpy datatype object; all computations will be performed using
          this datatype. float32 is faster but less accurate, so you should use
          float64 for numeric gradient checking.
        - seed: If not None, then pass this random seed to the dropout layers. This
          will make the dropout layers deteriminstic so we can gradient check the
          model.
        self.use batchnorm = use batchnorm
        self.use_dropout = dropout < 1</pre>
        self.reg = reg
        self.num\ layers = 1 + len(hidden\ dims)
        self.dtype = dtype
        self.params = {}
        # YOUR CODE HERE:
            Initialize all parameters of the network in the self.params dictionary.
            The weights and biases of layer 1 are W1 and b1; and in general the
            weights and biases of layer i are Wi and bi. The
            biases are initialized to zero and the weights are initialized
            so that each parameter has mean 0 and standard deviation weight scale.
            BATCHNORM: Initialize the gammas of each layer to 1 and the beta
            parameters to zero. The gamma and beta parameters for layer 1 should
            be self.params['gamma1'] and self.params['beta1']. For layer 2, they
            should be gamma2 and beta2, etc. Only use batchnorm if
self.use_batchnorm
            is true and DO NOT do batch normalize the output scores.
        arbi_input_dim = input_dim
```

```
for i, hd in enumerate(hidden dims):
            arbiW = 'W%d' % (i + 1)
            arbib = 'b%d' % (i + 1)
            self.params[arbiW] = np.random.randn(arbi input dim, hd) *
weight scale
            self.params[arbib] = np.zeros(hd)
            # Initialize
            if self.use batchnorm:
                arbiGamma = 'gamma%d' % (i + 1)
                arbiBeta = 'beta%d' % (i + 1)
                self.params[arbiGamma] = np.ones(hd)
                self.params[arbiBeta] = np.zeros(hd)
            arbi input dim = hd
        self.params['W%d' % self.num_layers] = np.random.randn(arbi_input_dim,
num_classes) * weight_scale
        self.params['b%d' % self.num_layers] = np.zeros(num_classes)
        # END YOUR CODE HERE
        # When using dropout we need to pass a dropout_param dictionary to each
        # dropout layer so that the layer knows the dropout probability and the
mode
        # (train / test). You can pass the same dropout param to each dropout
layer.
        self.dropout param = {}
        if self.use dropout:
            self.dropout param = {'mode': 'train', 'p': dropout}
            if seed is not None:
                self.dropout param['seed'] = seed
        # With batch normalization we need to keep track of running means and
        # variances, so we need to pass a special bn_param object to each batch
        # normalization layer. You should pass self.bn_params[0] to the forward
pass
        # of the first batch normalization layer, self.bn_params[1] to the forward
        # pass of the second batch normalization layer, etc.
        self.bn params = []
        if self.use batchnorm:
            self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers
- 1)]
        # Cast all parameters to the correct datatype
        for k, v in self.params.items():
            self.params[k] = v.astype(dtype)
    def loss(self, X, y=None):
        Compute loss and gradient for the fully-connected net.
        Input / output: Same as TwoLayerNet above.
        X = X.astype(self.dtype)
        mode = 'test' if y is None else 'train'
        # Set train/test mode for batchnorm params and dropout param since they
        # behave differently during training and testing.
        if self.dropout_param is not None:
            self.dropout_param['mode'] = mode
        if self.use batchnorm:
            for bn_param in self.bn_params:
```

```
bn param[mode] = mode
       scores = None
           Implement the forward pass of the FC net and store the output
           scores as the variable "scores".
           BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
           between the affine forward and relu forward layers. You may
           also write an affine_batchnorm_relu() function in layer_utils.py.
          DROPOUT: If dropout is non-zero, insert a dropout layer after
          every ReLU layer.
       fc cache = {}
       relu_cache = {}
       bn_{cache} = \{\}
       dropout_cache = {}
       batch_size = X.shape[0]
       X = np.reshape(X, [batch_size, -1])
       for i in range(self.num_layers-1):
           fc_act, fc_cache['%d' % (i+1)] = affine_forward(X, self.params['W%d' %
(i+1)], self.params['b%d' % (i+1)])
           if self.use batchnorm:
               bn_act, bn_cache['%d' % (i+1)] = batchnorm_forward(fc_act,
self.params['gamma\sqrt[8]{d}' % (i+1)], self.params['beta\sqrt[8]{d}' % (i+1)], self.bn_params[i])
               relu act, relu cache['%d' % (i+1)] = relu forward(bn act)
               relu act, relu cache['%d' % (i+1)] = relu forward(fc act)
           if self.use dropout:
               relu_act, dropout_cache['%d' % (i+1)] = dropout_forward(relu_act,
self.dropout param)
           X = relu_act.copy() # Result of one pass through the affine-relu
block.
       # Output layer is FC layer without relu.
       scores, final_cache = affine_forward(X, self.params['W'+str
(self.num layers)], self.params['b'+str(self.num layers)])
       # END YOUR CODE HERE
       # If test mode return early
       if mode == 'test':
           return scores
       loss, grads = 0.0, {}
                          # YOUR CODE HERE:
           Implement the backwards pass of the FC net and store the gradients
           in the grads dict, so that grads[k] is the gradient of self.params[k]
           Be sure your L2 regularization includes a 0.5 factor.
           BATCHNORM: Incorporate the backward pass of the batchnorm.
          DROPOUT: Incorporate the backward pass of dropout.
       loss, dsm = softmax_loss(scores, y)
       loss += 0.5 * self.reg * (np.sum(np.square(self.params['W%d' %
(self.num_layers)])))
```

```
dx last, dw last, db last = affine backward(dsm, final cache)
       grads['W%d' % (self.num layers)] = dw last + self.reg*self.params['W%d' %
(self.num_layers)]
       grads['b%d' % (self.num layers)] = db last
       for i in range(self.num_layers - 1, 0, -1):
          if self.use_dropout:
              dx last = dropout backward(dx last, dropout cache['%d' % (i)])
          drelu = relu_backward(dx_last, relu_cache['%d' % (i)])
          if self.use_batchnorm:
              dbatchnorm, dgamma, dbeta = batchnorm_backward(drelu, bn_cache['%
d' % (i)])
              dx_last, dw_last, db_last = affine_backward(dbatchnorm, fc_cache['%
d' % (i)])
              grads['beta%d' % (i)] = dbeta
              grads['gamma%d' % (i)] = dgamma
          else:
              dx_last, dw_last, db_last = affine_backward(drelu, fc_cache['%d' %
(i)])
          grads['W%d' % (i)] = dw_last + self.reg * self.params['W%d' % (i)]
          grads['b%d' % (i)] = db_last
          loss += 0.5 * self.reg * (np.sum(np.square(self.params['\dagged' % (i)])))
       # ============= #
       # END YOUR CODE HERE
       return loss, grads
```

```
import numpy as np
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def affine_forward(x, w, b):
    Computes the forward pass for an affine (fully-connected) layer.
    The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
    examples, where each example x[i] has shape (d_1, \ldots, d_k). We will reshape each input into a vector of dimension D = d_1 * \ldots * d_k, and
    then transform it to an output vector of dimension \overline{\mathbf{M}}.
    - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
    - w: A numpy array of weights, of shape (D, M)
    - b: A numpy array of biases, of shape (M,)
    Returns a tuple of:
    - out: output, of shape (N, M)
    - cache: (x, w, b)
    out = None
    # YOUR CODE HERE:
        Calculate the output of the forward pass. Notice the dimensions
        of w are D x M, which is the transpose of what we did in earlier
    # assignments.
    N = x.shape[0]
    D = w.shape[0]
    x inp = x.reshape(N,D)
    \overline{\text{out}} = \text{np.dot}(x \text{ inp,w}) + b
    # END YOUR CODE HERE
    cache = (x, w, b)
    return out, cache
def affine backward(dout, cache):
    Computes the backward pass for an affine layer.
    Inputs:
    - dout: Upstream derivative, of shape (N, M)
    - cache: Tuple of:
      - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
      - w: A numpy array of weights, of shape (D, M)
      - b: A numpy array of biases, of shape (M,)
    Returns a tuple of:
    - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
    - dw: Gradient with respect to w, of shape (D, M)
```

```
- db: Gradient with respect to b, of shape (M,)
   x, w, b = cache
   dx, dw, db = None, None, None
   # YOUR CODE HERE:
     Calculate the gradients for the backward pass.
   # Notice:
      dout is N x M
     dx should be N x d1 x ... x dk; it relates to dout through multiplication
with w, which is D \times M
      dw should be D \times M; it relates to dout through multiplication with \times,
which is N \times D after reshaping
   # db should be M; it is just the sum over dout examples
   N = x.shape[0]
   D = w.shape[0]
   x_{inp} = x.reshape(N,D)
   dx_inp = np.dot(dout,w.T)
   dx = dx_{inp.reshape}(x.shape)
   dw = np.dot(x inp.T,dout)
   db = np.dot(dout.T,np.ones(N))
   # END YOUR CODE HERE
   return dx, dw, db
def relu forward(x):
   Computes the forward pass for a layer of rectified linear units (ReLUs).
   Input:
   - x: Inputs, of any shape
   Returns a tuple of:
   - out: Output, of the same shape as x
   - cache: x
   # YOUR CODE HERE:
   # Implement the ReLU forward pass.
   out = np.maximum(0,x)
                       # END YOUR CODE HERE
   cache = x
   return out, cache
def relu_backward(dout, cache):
   Computes the backward pass for a layer of rectified linear units (ReLUs).
   - dout: Upstream derivatives, of any shape
   - cache: Input x, of same shape as dout
   Returns:
```

```
- dx: Gradient with respect to x
    x = cache
    # YOUR CODE HERE:
      Implement the ReLU backward pass
    dx = np.asarray(dout)
    dx[x <= 0] = 0
    # END YOUR CODE HERE
    return dx
def batchnorm_forward(x, gamma, beta, bn_param):
    Forward pass for batch normalization.
    During training the sample mean and (uncorrected) sample variance are
    computed from minibatch statistics and used to normalize the incoming data.
    During training we also keep an exponentially decaying running mean of the mean
    and variance of each feature, and these averages are used to normalize data
    at test-time.
    At each timestep we update the running averages for mean and variance using
    an exponential decay based on the momentum parameter:
    running mean = momentum * running mean + (1 - momentum) * sample mean
    running var = momentum * running var + (1 - momentum) * sample var
    Note that the batch normalization paper suggests a different test-time
    behavior: they compute sample mean and variance for each feature using a
    large number of training images rather than using a running average. For
    this implementation we have chosen to use running averages instead since
    they do not require an additional estimation step; the torch7 implementation
    of batch normalization also uses running averages.
    Input:
    - x: Data of shape (N, D)
    - gamma: Scale parameter of shape (D,)
    - beta: Shift paremeter of shape (D,)
    bn_param: Dictionary with the following keys:mode: 'train' or 'test'; required
      - eps: Constant for numeric stability
      - momentum: Constant for running mean / variance.
      - running_mean: Array of shape (D,) giving running mean of features
      - running var Array of shape (D,) giving running variance of features
    Returns a tuple of:
    - out: of shape (N. D)
    - cache: A tuple of values needed in the backward pass
    mode = bn_param['mode']
    eps = bn_param.get('eps', 1e-5)
momentum = bn_param.get('momentum', 0.9)
    N, D = x.shape
    running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
    running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
    out, cache = None, None
    if mode == 'train':
```

```
# YOUR CODE HERE:
         A few steps here:
           (1) Calculate the running mean and variance of the minibatch.
           (2) Normalize the activations with the running mean and variance.
           (3) Scale and shift the normalized activations. Store this
              as the variable 'out'
           (4) Store any variables you may need for the backward pass in
              the 'cache' variable.
      # ----- #
      arbiBatch_mean = np.mean(x, axis = 0)
      arbiBatch\_var = np.var(x, axis = 0)
      running_mean = momentum * running_mean + (1 - momentum) * arbiBatch mean
      running var = momentum * running_var + (1 - momentum) * arbiBatch_var
      bn_param['running_mean'] = running_mean
      bn_param['running_var'] = running_var
      arbiBatch_norm = (x - arbiBatch_mean) / np.sqrt(arbiBatch_var + eps)
      out = gamma * arbiBatch_norm + beta
      cache = {
          x minus mean': (x - arbiBatch mean),
          'arbiBatch_norm': arbiBatch_norm,
         'gamma': gamma,
         'inv_var': 1.0 / np.sqrt(arbiBatch_var + eps),
'sqrt_var': np.sqrt(arbiBatch_var + eps)
      }
      # END YOUR CODE HERE
      elif mode == 'test':
      # ============= #
      # YOUR CODE HERE:
        Calculate the testing time normalized activation. Normalize using
         the running mean and variance, and then scale and shift appropriately.
         Store the output as 'out'.
      out = (gamma * x / (np.sqrt(running_var + eps))) + (beta - (gamma *
running mean) / np.sqrt(running var + eps))
      # END YOUR CODE HERE
      else:
      raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn_param['running_mean'] = running_mean
   bn param['running var'] = running var
   return out, cache
def batchnorm backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   Inputs:

    dout: Upstream derivatives, of shape (N, D)
```

```
- cache: Variable of intermediates from batchnorm forward.
   Returns a tuple of:
    - dx: Gradient with respect to inputs x, of shape (N, D)
    - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
    - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
   dx, dgamma, dbeta = None, None, None
   # YOUR CODE HERE:
   # Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   N,D = dout.shape
   x_minus_mean = cache.get('x_minus_mean')
   arbiBatch_norm = cache.get('arbiBatch_norm')
   gamma = cache.get('gamma')
    inv_var = cache.get('inv_var')
   sqrt_var = cache.get('sqrt_var')
   dxhat = dout * gamma
dxmu1 = dxhat * inv_var
   dinv_var = np.sum(dxhat * x_minus_mean, axis = 0)
    dsqrt_var = dinv_var * (-1.\overline{0} / sqrt_var**2)
    dvar = dsqrt_var * 0.5 * (1 / sqrt_var)
   dsq = (1.0 / N) * dvar * np.ones_like(dout)
dxmu2 = dsq * 2 * x_minus_mean
dx1 = dxmu1 + dxmu2
   dmu = -1 * np.sum(dxmu1 + dxmu2, axis = 0)
   dx2 = (1 / N) * dmu * np.ones_like(dout)
    dx = dx1 + dx2
   dbeta = np.sum(dout, axis = 0)
   dgamma = np.sum(dout * arbiBatch norm, axis = 0)
   # END YOUR CODE HERE
   return dx, dgamma, dbeta
def dropout forward(x, dropout param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
    - x: Input data, of any shape
    - dropout_param: A dictionary with the following keys:
     - p: Dropout parameter. We keep each neuron output with probability p. - mode: 'test' or 'train'. If the mode is train, then perform dropout; if the mode is test, then just return the input.
     - seed: Seed for the random number generator. Passing seed makes this
       function deterministic, which is needed for gradient checking but not in
       real networks.
   Outputs:
    - out: Array of the same shape as x.
    - cache: A tuple (dropout param, mask). In training mode, mask is the dropout
     mask that was used to multiply the input; in test mode, mask is None.
   p, mode = dropout_param['p'], dropout_param['mode']
   if 'seed' in dropout_param:
       np.random.seed(dropout_param['seed'])
   mask = None
   out = None
```

```
if mode == 'train':
                   ______ #
      # =========
      # YOUR CODE HERE:
         Implement the inverted dropout forward pass during training time.
         Store the masked and scaled activations in out, and store the
         dropout mask as the variable mask.
      mask = (np.random.random_sample(x.shape) >= p)
      dropout_factor = \frac{1}{p} / (\frac{1}{p})
      mask = mask * dropout_factor
      out = x * mask
      # END YOUR CODE HERE
   elif mode == 'test':
      # YOUR CODE HERE:
       Implement the inverted dropout forward pass during test time.
      out = x
      # END YOUR CODE HERE
      cache = (dropout param, mask)
   out = out.astype(x.dtype, copy=False)
   return out, cache
def dropout backward(dout, cache):
   Perform the backward pass for (inverted) dropout.
   Inputs:
   - dout: Upstream derivatives, of any shape
   - cache: (dropout_param, mask) from dropout_forward.
   dropout param, mask = cache
   mode = dropout param['mode']
   dx = None
   if mode == 'train':
      # ==
      # YOUR CODE HERE:
      # Implement the inverted dropout backward pass during training time.
      dx = dout * mask
      # END YOUR CODE HERE
      elif mode == 'test':
      # YOUR CODE HERE:
      #
       Implement the inverted dropout backward pass during test time.
```

```
dx = dout
       # ======
       # END YOUR CODE HERE
       return dx
def svm loss(x, y):
   Computes the loss and gradient using for multiclass SVM classification.
   Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
     for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
     0 \le y[i] < C
   Returns a tuple of:
   - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
   N = x.shape[0]
   correct_class_scores = x[np.arange(N), y]
   margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
   margins[np.arange(N), y] = 0
   loss = np.sum(margins) / N
   num_pos = np.sum(margins > 0, axis=1)
   dx = np.zeros_like(x)
   dx[margins > \overline{0}] = 1
   dx[np.arange(N), y] -= num_pos
   dx /= N
    return loss, dx
def softmax_loss(x, y):
   Computes the loss and gradient for softmax classification.
   Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
     for the ith input.
   - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
     0 \le y[i] < C
   Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x """
   probs = np.exp(x - np.max(x, axis=1, keepdims=True))
   probs /= np.sum(probs, axis=1, keepdims=True)
   N = x.shape[0]
   loss = -np.sum(np.log(probs[np.arange(N), y])) / N
   dx = probs.copy()
   dx[np.arange(N), y] -= 1
   dx /= N
    return loss, dx
```