$u_t(x,0) = g(x)$