

 $\lim_{N \to \infty} \langle f \rangle_{1:N} (x_{1:N}) = \mathbb{E}_{\pi}[f]$