Relative error of log det $V_{ik}\tilde{V}_{ik}^{-1}$ computed by inverse-free and standard Arnoldi methods with/without recycling subspaces

