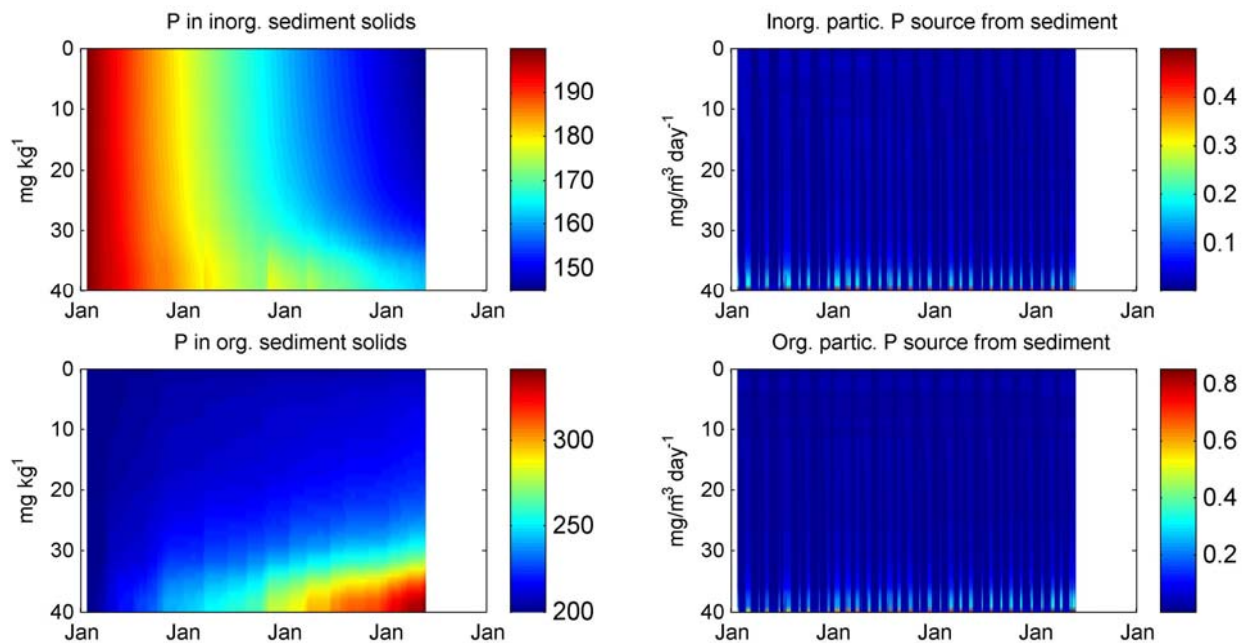




REPORT SNO (unpublished)

## MyLake (v.1.2)

Technical model documentation  
and user's guide for version 1.2



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|   |                             |                     |
|---|-----------------------------|---------------------|
| Title<br>MyLake (v.1.2): Technical model documentation and user's guide for version 1.2 | Serial No.<br>(unpublished) | Date<br>5. 10. 2005 |
|   | Report No.    Sub-No.       | Pages        Price  |
| Author(s)<br>Tuomo M. Saloranta and Tom Andersen  | Topic group                 | Distribution        |
|   | Geographical area           | Printed<br>NIVA     |

|           |             |
|-----------|-------------|
| Client(s) | Client ref. |
|-----------|-------------|

**Abstract**

MyLake (Multi-year Lake simulation model) is a one-dimensional process-based model code for simulation of daily 1) vertical distribution of lake water temperature and thus stratification, 2) evolution of seasonal lake ice and snow cover, and 3) phosphorus-phytoplankton dynamics. MyLake has a relatively simple and transparent model structure, it is easy to set up, and is suitable both for making predictions and scenarios, and to be used as an investigative tool. Short runtime allows application of comprehensive sensitivity and uncertainty analysis as well as simulation of a large number of lakes or over long periods (decades). MyLake aims to include only the most significant physical, chemical and biological processes in a well-balanced and robust way. This report gives a description of the updates and developments made to version 1.2 compared to the previous version 1.1 described in details in Saloranta and Andersen (2004).

|                       |                     |
|-----------------------|---------------------|
| 4 keywords, Norwegian | 4 keywords, English |
| 1.   Modellering      | 1.   modelling      |
| 2.   Innsjø           | 2.   lake           |
| 3.   eutrofiering     | 3.   eutrophication |
| 4.   MyLake           | 4.   MyLake         |

Project manager

Research manager

Head of research department

ISBN

# **MyLake (v.1.2)**

Technical model documentation and user's guide for  
version 1.2

## **Preface**

We thank the Norwegian Institute for Water Research (NIVA) for funding the MyLake model v.1.2 development work in project “Pcode”. The application and testing of MyLake model (v.1.2) was done mainly within the same project.

Oslo, 5. 10. 2005

*Tuomo M. Saloranta*

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## Summary

MyLake (Multi-year Lake simulation model) is a one-dimensional process-based model code for simulation of daily 1) vertical distribution of lake water temperature and thus stratification, 2) evolution of seasonal lake ice and snow cover, and 3) phosphorus-phytoplankton dynamics. MyLake has a relatively simple and transparent model structure, it is easy to set up, and is suitable both for making predictions and scenarios, and to be used as an investigative tool. Short runtime allows application of comprehensive sensitivity and uncertainty analysis as well as simulation of a large number of lakes or over long periods (decades). MyLake aims to include only the most significant physical, chemical and biological processes in a well-balanced and robust way. This report gives a description of the updates and developments made to version 1.2 compared to the previous version 1.1 described in details in Saloranta and Andersen (2004).

# 1. Introduction

MyLake (Multi-year Lake simulation model) is a one-dimensional process-based model code for simulation of daily 1) vertical distribution of lake water temperature and thus stratification, 2) evolution of seasonal lake ice and snow cover, and 3) phosphorus-phytoplankton dynamics. The lake water simulation part of the model code is based on Ford and Stefan (1980), Riley and Stefan (1988), and Hondzo and Stefan (1993), while the ice simulation code is based on Leppäranta (1991) and Saloranta (2000). MyLake has been developed at the Norwegian Institute for Water Research (NIVA), and the model has so far (spring 2005) been applied in BMW, THERMOS and EUROLIMPACS projects (Saloranta 2005, Lydersen et al. 2003). The overall structure of MyLake model code is shown in Table 1.

Strengths of MyLake model code include:

- MyLake has a relatively simple and transparent model structure, it is easy to set up, and is suitable both for making predictions and scenarios, and to be used as an investigative tool.
- Short runtime allows application of comprehensive sensitivity and uncertainty analysis as well as simulation of a large number of lakes or over long periods (decades).
- MyLake aims to include only the most significant physical, chemical and biological processes in a well-balanced and robust way.

There are, of course, limitations too. MyLake is a newcomer and only three previous applications are documented so far. More applications are needed before the model code can be said to be thoroughly tested in practise. However, the model building blocks are based on more or less well-established science and have been used previously in numerous applications. Some users may also consider the model too simple for their purposes, as many processes, e.g. zooplankton grazing and fish population dynamics are left out of the current version (v.1.2) of the model code. Other limitations may be the model time step which is preset to 24 hours and cannot be changed, as well as the 1-dimensional vertical resolution approach, which may not be so well suited for some particular types of problems and lakes.

Generally MyLake model code development aims to take into account the following five criteria adapted from Riley and Stefan (1988): 1) that the model code be general for use on different sites with minimum of alterations, 2) that the model code be capable of simulating a wide range of treatment options, 3) that the model code incorporate the dominant physical, chemical and biological processes, especially processes directly affected by various treatment options, 4) that the physical, chemical and biological components be modelled with similar orders of detail to reduce the possibility of a weak

link in the modelling process, and 5) that the model be economical enough to run to serve as management tool.

This report gives a description of the updates and developments made to version 1.2, compared to the previous version 1.1 described in details in Saloranta and Andersen (2004).

## 2. Updates and developments in MyLake (v.1.2)

### 2.1 New model state variables

The single particulate phosphorus state variable that was used in the previous MyLake version 1.1 is in the current version 1.2 modified to represent only the phosphorus bound to inorganic particles. In addition, dissolved organic phosphorus (DOP) and dissolved organic carbon (DOC) are added as new state variables. Chlorophyll *a* now represents the particulate organic phosphorus fraction. The eight main model state variables, of which vertical profiles are simulated by MyLake v.1.2 are:

|            |   |
|------------|---|
| $T$        | Temperature [°C]  |
| $C$        | Passive tracer [-]  |
| $S$        | Suspended inorganic particulate matter (functions also as a passive sedimenting tracer) [kg m <sup>-3</sup> ] |
| $P_D$      | Dissolved inorganic phosphorus (phosphate) [μg l <sup>-1</sup> = mg m <sup>-3</sup> ]                         |
| $P_{IP}$   | Phosphorus bound to inorganic particles [μg l <sup>-1</sup> = mg m <sup>-3</sup> ]                            |
| $P_{DO}$   | Dissolved organic phosphorus [μg l <sup>-1</sup> = mg m <sup>-3</sup> ]                                       |
| $P_{Chla}$ | Chlorophyll <i>a</i> [μg l <sup>-1</sup> = mg m <sup>-3</sup> ]   |
| $DOC$      | Dissolved organic carbon [μg l <sup>-1</sup> = mg m <sup>-3</sup> ]   |

### 2.2 Modelling the dissolved and particulate phosphorus fractions

The mass fraction of phosphorus bound to the profile  $S$  [kg m<sup>-3</sup>] of suspended inorganic particulate matter in the water column is denoted by  $F_{IP}$  [mg kg<sup>-1</sup>]. The concentration profile of phosphorus bound to suspended inorganic matter  $P_{IP}$  [mg m<sup>-3</sup>] is thus:

$$P_{IP} = v\rho_{sed}F_{IP} = \frac{S}{\rho_{sed}}\rho_{sed}F_{IP} = SF_{IP} \quad (1)$$



where  $v$  is the volume fraction of inorganic solids in water column or sediment ( $v = V_{inorg} / (V_{inorg} + V_{water})$ ), and  $\rho_{sed}$  [kg m<sup>-3</sup>] is the density of inorganic solid matter. Similar equation applies also in the sediment and  $v$  for sediment can be calculated from the volume fraction of solids in the wet bulk sediment (i.e.,  $1 - \text{porosity}$ )  $\phi$  [m<sup>3</sup> m<sup>-3</sup>] and the volume fraction of inorganic matter in these solids  $v_{inorg}$ .

$$v = \frac{\phi v_{inorg}}{\phi v_{inorg} + (1 - \phi)} \quad (1b)$$

We assume an instant ( $\sim$  in a timescale of less than a day) equilibrium partitioning between dissolved inorganic phosphorus  $P_D$  [mg m<sup>-3</sup>] and  $F_{IP}$  [mg kg<sup>-1</sup>] (Webster and Grace, 2001). This equilibrium is modelled using Langmuir isotherm approach. The sum of inorganic phosphorus taking part to the equilibrium partitioning  $P_T$  is assumed to be known ( $P_T = TotP - P_{Chla}/y_c - P_{DO}$ ), where  $y_c$  is the yield coefficient, i.e. chlorophyll  $a$  to phosphorus ratio (see section 3.2.3), which can be assumed equal to one, i.e. 1 mg m<sup>-3</sup> chlorophyll  $a$  = 1 mg m<sup>-3</sup> phosphorus. The following pair of equations then applies to the system:

$$\begin{cases} P_T = P_{IP} + (1 - v)P_D = v\rho_{sed}F_{IP} + (1 - v)P_D \\ F_{IP} = F_{max} \frac{P_D}{P_{sat} + P_D} + F_{stable} \end{cases} \quad (2)$$

where  $F_{max}$  [mg kg<sup>-1</sup>] and  $P_{sat}$  [mg m<sup>-3</sup>] are the saturation level and half saturation  $P_D$  concentration, respectively, describing the Langmuir isotherm, and  $F_{stable}$  [mg kg<sup>-1</sup>] represents the inactive fraction of phosphorus firmly bound in the particles and not available for desorption. Note that the isotherm parameters  $F_{max}$  and  $P_{sat}$  should not include the contribution from  $F_{stable}$ .

An example: let's assume that  $F_{max} = 1000$  mg kg<sup>-1</sup>,  $P_{sat} = 10$  mg m<sup>-3</sup>,  $F_{stable} = 0$  mg kg<sup>-1</sup>,  $\rho_{sed} = 2500$  kg m<sup>-3</sup> and that initially the system is in equilibrium with  $P_D = 10$  mg m<sup>-3</sup>,  $F_{IP} = 500$  mg kg<sup>-1</sup>,  $S = 0.067$  kg m<sup>-3</sup>,  $P_T = 43.5$  mg m<sup>-3</sup>. If we now throw inorganic phosphorus-free particles into the water column so that  $S = 0.2$  kg m<sup>-3</sup> (200% increase), then a new equilibrium would be  $P_D = 2.6$  mg m<sup>-3</sup>,  $F_{IP} = 204.5$  mg kg<sup>-1</sup>,  $P_T = 43.5$  mg m<sup>-3</sup>. Thus  $P_D$  has been reduced by 74%, while  $F_{IP}$  has been reduced by 34%.  $P_T$  has, of course, remained the same.

The two remaining phosphorus fractions are  $P_{Chla}$  and  $P_{DO}$ . The unit of  $P_{Chla}$  is the actual chlorophyll  $a$  concentration [mg m<sup>-3</sup>] but this is related to phosphorus units via the yield coefficient  $y_c$ .  $P_{DO}$  is mineralized to  $P_D$  (usually very slowly, i.e. the temperature dependent specific rate coefficient  $k_{dop}(20) \sim 10^{-3}$ ), but does not otherwise take part in any reactions in the water or sediment.

## 2.3 Dissolved organic carbon (DOC)

To be formulated...

## 2.4 Sediment-water interaction

We define an active, mixed sediment layer with depth  $H_{sed}$ , [m, wet sediment], resuspension rate of dry particles  $U_{res}$  [ $\text{m d}^{-1}$ ] and diffusion rate for pore water-water column interaction  $k_{seddiff}$  [ $\text{m d}^{-1}$ ].  $U_{res}$  equals the thickness of the daily resuspended layer of dry particles and different resuspension value can be defined in the model for epi- and hypolimnion which are separated by the simulated pycnocline depth. The active sediment layer consists of both inorganic ( $S$ ) and organic (chlorophyll  $a$ ) particles sedimenting from the water column, and we further define the volume fraction of dry inorganic matter in the total dry sediment solids,  $F_{IM}$ . Similar fraction of dry organic matter will be consequently  $1-F_{IM}$ , and the conversion from  $P_{Chla}$  [ $\text{mg m}^{-3}$ ] to concentration of dry particular organic matter  $S_{org}$  [ $\text{kg m}^{-3}$ ] is by dividing  $P_{Chla}$  by  $y_c F_{Porg}$ , where  $F_{Porg}=12346 \text{ mg kg}^{-1}$ , assuming a Redfield phosphorus to carbon weight ratio of 1:40 and a 50% carbon content in the organic algal matter.

The resuspended solids are taken as a source for the water column  $S$ ,  $P_{IP}$  and  $P_{Chla}$ , while the net sedimenting matter changes concentrations of sediment  $P_{IP}$  and  $P_{Chla}$  via thickness-weighted averages of the concentrations in the sediment and in the sedimenting matter, where the thickness weights are  $(H_{sed} - H_{newsed})$  and  $H_{newsed}$ , respectively, and where  $H_{newsed}$  denotes the wet bulk thickness of the newly sedimented inorganic or organic matter (assuming constant volume fraction of solids in the sediment  $\phi$ ). This implies also that old sediment of thickness  $H_{newsed}$  will be buried to inactive sediment layer.

A similar partitioning, as in the water column, between dissolved  $P_D$  in the sediment pore water and  $F_{IP}$  in the sediment solids applies also in the sediment. The parameter  $k_{seddiff}$  denotes the thickness of the daily diffused pore water layer, and this pore water is mixed with the corresponding water layer above the sediment column. Similar amount of water from the corresponding water layer above the sediment column is mixed with the pore water. The sedimented chlorophyll  $a$  is assumed to be mineralised to  $P_D$  in the pore water, as in the water column, according to a temperature dependent specific rate coefficient  $k(T)$ . The concentration of  $P_{DO}$  in the pore water is assumed to be the same as in the water column above it, and due to the small volume of the pore water (compared to the water layers) its diffusion is not simulated.

If the active sediment layer is well oxidized, then most of the phosphorus in the sediment is bound to particles and thus particle resuspension (rate  $U_{res}$ ) usually controls the phosphorus source from sediment to water. However, if the active sediment layer is anoxic then the particles' phosphorus sorption capacity is much lowered (i.e.  $F_{max}$  in equation 2 approaches zero) and most of the phosphorus is dissolved in the pore water, and thus pore water diffusion (rate  $k_{seddiff}$ ) becomes the

dominant process for the phosphorus source from sediment to water. (In future versions of MyLake the value  $F_{max}$  in equation 2, controlling the particles' phosphorus sorption capacity, could be coupled to the oxygen conditions in the sediment, e.g. via the oxygen profile in the water).

The amount of sedimentation for each layer is calculated using the difference between the “funnelling” and “non-funnelling” version of the advective-diffusive equation 30 in Saloranta and Andersen (2004), i.e. the concentration difference  $\Delta C_{fun-nonfun}$  between these two versions of the equation

$$A \frac{\partial(\Delta C_{fun-nonfun})}{\partial t} = A \frac{\partial(wC_{nonfun})}{\partial z} - \frac{\partial(AwC_{fun})}{\partial z} \quad (3)$$

is multiplied by the volume of the corresponding layer to get the total amount sedimented during one time step.

Figure 1 shows a schematic illustration of the flow and transport processes between the different phosphorus fractions.

## 2.5 Other model code revisions

The structure of the code is somewhat rearranged from the previous version, as shown in Table 1. Also a new code module *convection.m* is introduced, handling the vertical convection due to instable water stratification.

The heat sources/sinks in the water column are now resolved twice during a day, both at day and night. The solar heat input is applied only in the daytime, while the sediment heat and total daily turbulent and long wave heat sources/sinks are first multiplied by the fractions of day when the sun angle is above and below a preset threshold value (currently 15°), respectively, and then applied for day- and nighttime periods. Convection is allowed to mix the water both after day- and nighttime, and thus the water surface temperature and consequently the turbulent and long wave heat fluxes will be somewhat different compared to the v.1.1 code where the whole daily heat flux was applied once a day.

The simulation of the heat flux from water to the ice is changed so that heat is allowed to diffuse into the first water layer, and the daily temperature increase above freezing point in this layer is used to melt ice at each time step at the bottom of the ice layer. The temperature of the first water layer is then set back to the freezing point.

The “sedimentation switch” with which one could switch off sedimentation processes in the model is removed and only the passive dissolved tracer is currently affected by the “tracer switch”.



**Table 1.** Overview of MyLake v.1.2 model code structure

**(Start)**

*For one model time step (24 h):*

- Calculate daytime surface heat fluxes and wind stress, light attenuation, and phytoplankton growth and loss rates. Calculate also the heat flux between water and sediment.
- Apply daytime heat sources, allow convection, calculate nighttime surface heat sources and apply them, allow convection.
- Calculate profile of the diffusion coefficient  $K$
- Solve new profile for each state variable taking into account advection, diffusion and local sources/sinks. Solving is done in following order: 1) temperature (after which convection is allowed), 2) tracer, 3) dissolved inorganic phosphorus ( $P_{DO}$ ), 4) suspended inorganic particulate matter ( $S$ ) and associated particle bound phosphorus ( $P_{IP}$ ), 5) chlorophyll  $a$  ( $P_{Chla}$ ), 6) dissolved phosphorus ( $P_D$ ), 7) dissolved inorganic carbon ( $DOC$ ).
- Update phosphorus concentration in the sediment (exchange between pore water and water column, net sedimentation and burial to inactive layer, partitioning of phosphorus between dissolved and particle bound phases).
- Add river inflow and update profiles of the state variables accordingly. Allow partitioning of phosphorus between dissolved and particle bound phases, as well as convection.

**If no ice**

- Mix water layers with the available turbulent kinetic energy from wind.

**If ice cover**

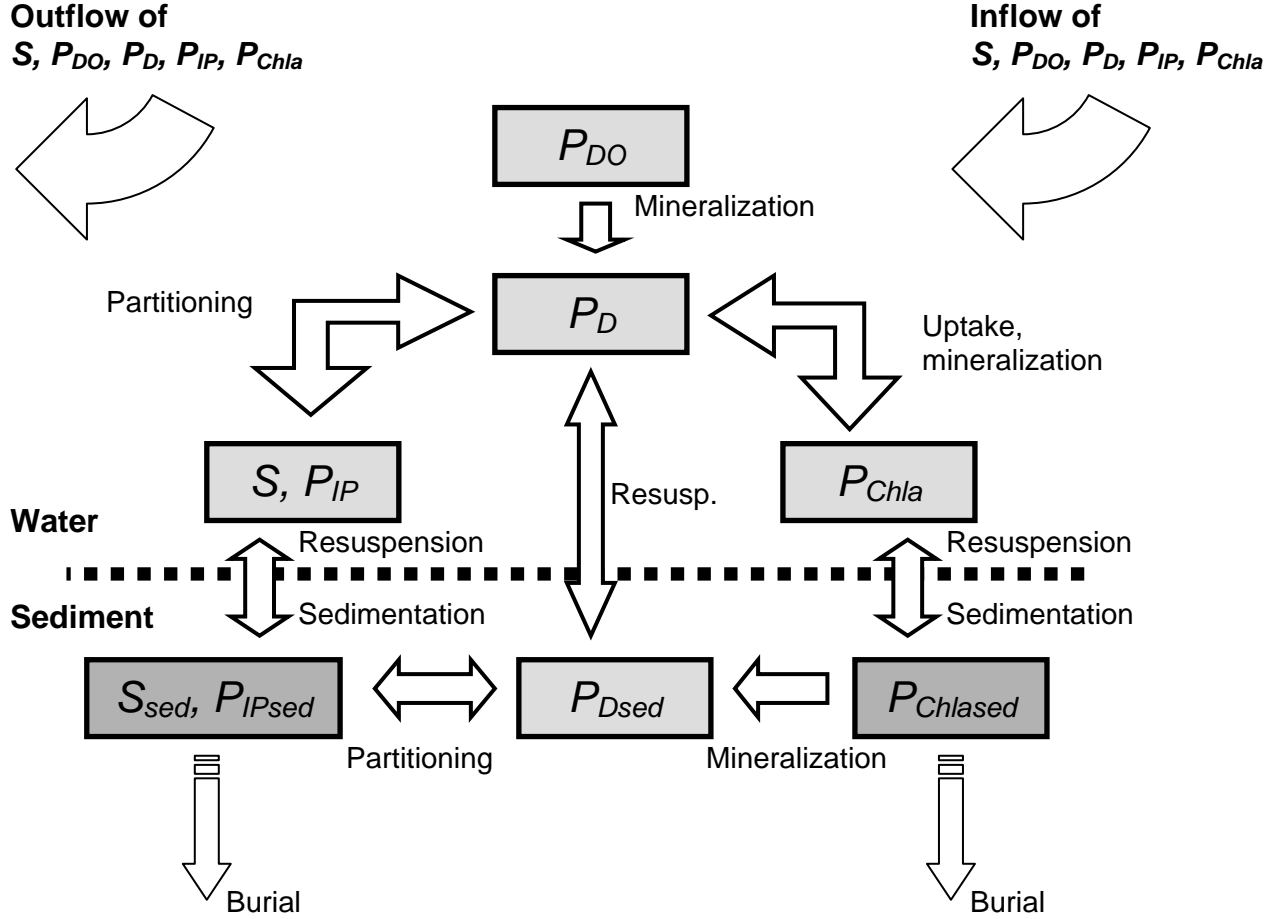
**If  $T_a < T_f$  (freezing)**

- ◆ Calculate ice surface temperature (depending on snow cover, or ice thickness if snow is absent)
- ◆ Calculate snow ice formation in case of isostatic imbalance
- ◆ Calculate congelation ice growth by Stefan's law
- ◆ Accumulate new snow fall and subtract formed snow ice from snow cover

**If  $T_a \geq T_f$  (melting)**

- ◆ Melt snow or ice from top with total surface heat flux
- Melt ice from bottom with the heat diffused to the surface layer (keeping the surface layer temperature at freezing point)
- Update snow density
- Allow partitioning of phosphorus between dissolved and particle bound phases in the water column.
- Check the water column for supercooled layers and turn them into initial ice cover.
- Save results to output matrices.

**(Goto Start)**



**Figure 1.** A schematic illustration of the flows between the main state variables in MyLake v.1.2 model, dissolved inorganic phosphorus (phosphate,  $P_D$ ), phosphorus bound to inorganic particles ( $P_{IP}$ ), dissolved organic phosphorus ( $P_{DO}$ ), chlorophyll a ( $P_{Chla}$ ), and suspended inorganic matter ( $S$ ).

### 3. Running a MyLake v.1.2 model application

#### 3.1 New code modules

The MyLake v.1.2 model code consists of six modules (MATLAB scripts, "m-files"), of which one is entirely new (*convection.m*) and two remain unchanged from the previous version (*IOflow\_v11.m* and *sedimentheat\_v11.m*):

|                         |   |
|-------------------------|---|
| <i>solvemodel_v12.m</i> | Contains most of the model algorithms and numerical solving of the equations. Contains also a number of "switches" with which particular processes can be disabled in the model code; |
|-------------------------|---|

|                           |   |
|---------------------------|---|
| <i>heatflux_v12.m</i>     | Handles calculation of turbulent and radiative heat fluxes, and some other physical and astronomical variables. Utilises MATLAB <i>Air-Sea Toolbox</i> (by Rich Pawlowicz, Woods Hole: <a href="http://sea-mat.whoi.edu/air_sea.html/">http://sea-mat.whoi.edu/air_sea.html/</a> ); |
| <i>sedimentheat_v11.m</i> | Calculates the sediment-water heat exchange;  |
| <i>IOflow_v11.m</i>       | Handles the addition of river inflow;   |
| <i>modelinputs_v12.m</i>  | Handles the reading of input data, initial conditions and parameters from the three Excel files described in sections 3.2.1-3.2.3.  |
| <i>convection_v12.m</i>   | Handles the vertical convection due to instable water stratification.   |

## 3.2 Revisions to parameter and input file structures

In addition to the model code (including the *Air-Sea Toolbox*), three different parameter and input data files are required to run a MyLake model application. These three files contain 1) time series of meteorological variables and inflow properties, 2) lake morphometry and initial profiles, and 3) model parameter values. These files are formatted in Excel spreadsheet software. File formats and required units (the latter are given in square brackets) are explained below and file templates are shown in Figures 2-4. Note that the first cell in the upper left corner (A1) must contain a dummy number (e.g. -999) so that MATLAB reads in the columns and rows correctly.

### 3.2.1 Meteorological and inflow time series

Note that time series with daily resolution are required, and that values for missing observations or measurement dates in the meteorological and inflow time series are in MyLake automatically estimated by linear interpolation.

#### Rows

1-2: Header rows

**(Important!** The first cell on the first row (A1) must contain a number, e.g -999)

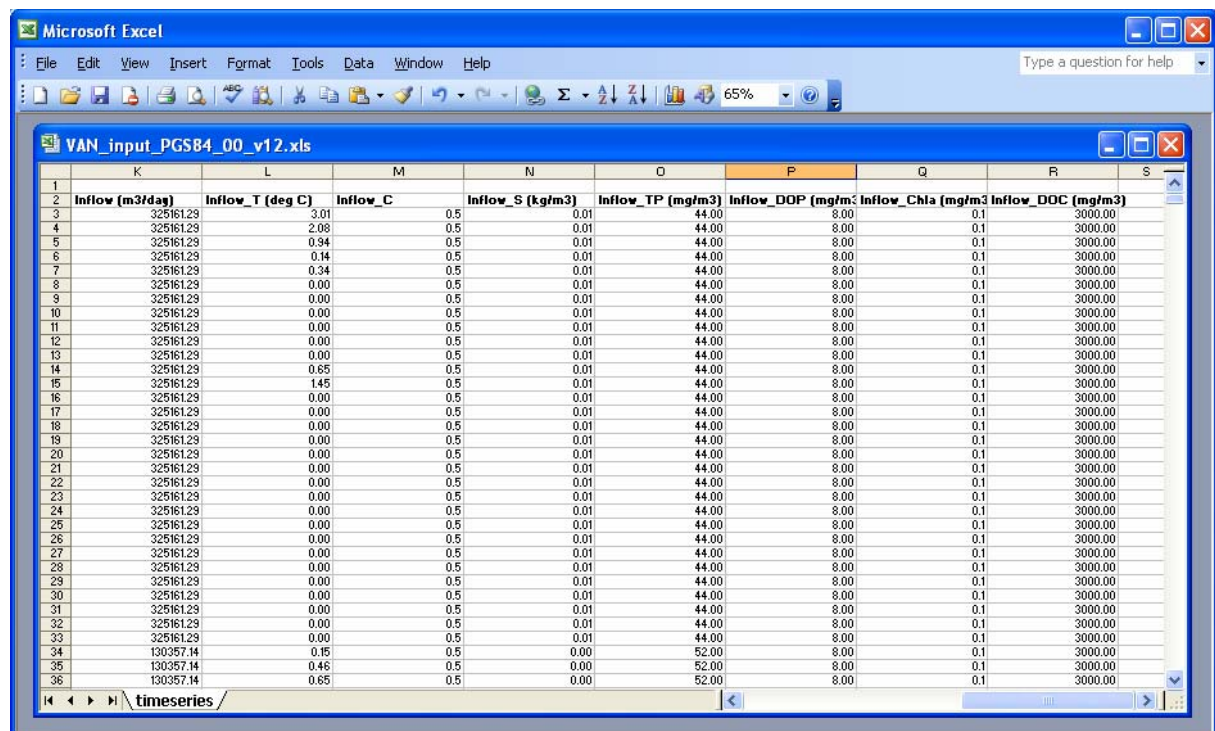
3-end: Data rows

#### Columns

1. Year
2. Month
3. Day
4. Global radiation [ $\text{MJ m}^{-2} \text{day}^{-1}$ ]
5. Cloud cover (0-1)

6. Air temperature at 2 meter height [ $^{\circ}\text{C}$ ]
7. Relative humidity at 2 meter height [%]
8. Air pressure at station level [hPa]
9. Wind speed at 10 m height [ $\text{m s}^{-1}$ ]
10. Precipitation [ $\text{mm d}^{-1}$ ]
11. Inflow volume [ $\text{m}^3 \text{d}^{-1}$ ]
12. Inflow temperature [ $^{\circ}\text{C}$ ]; if "NaN" ("Not a Number", a MATLAB expression for missing value) then the inflow is assumed to mix with the surface layer
13. Inflow concentration of the passive tracer [-]
14. Inflow concentration of the suspended inorganic particulate matter ( $S$ , functions also as a passive sedimenting tracer) [ $\text{kg m}^{-3}$ ]
15. Inflow concentration of total phosphorus ( $P_D + P_{IP} + P_{DO} + P_{Chla}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
16. Inflow concentration of dissolved organic phosphorus ( $P_{DO}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
17. Inflow concentration of chlorophyll  $a$  ( $P_{Chla}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
18. Inflow concentration of dissolved organic carbon ( $DOC$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]





**Figure 2.** Example of a MyLake input forcing data file.

### 3.2.2 Bathymetry and initial profiles

Note that linear temperature profile between the lake water temperature and 4 °C is initially assumed in the sediment columns.

#### Rows

1-2: Header rows

**(Important!** The first cell on the first row (A1) must contain a number, e.g –999)

3-end: Data rows

#### Columns

1. Depth levels (meters from surface; positive values); the first and last levels must be zero and the maximum depth, respectively

*(the following variable values must be given at all depth levels of column 1)*

2. Horizontal areas [ $\text{m}^2$ ]; the first and last levels must be lake surface area and zero, respectively
3. Initial profile of temperature [ $^{\circ}\text{C}$ ]
4. Initial profile of the passive tracer [-]
5. Initial profile of the suspended inorganic particulate matter ( $S$ , functions also as a passive sedimenting tracer) [ $\text{kg m}^{-3}$ ]
6. Initial profile of total phosphorus ( $P_D + P_{IP} + P_{DO} + P_{Chla}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
7. Initial profile of dissolved organic phosphorus ( $P_{DO}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
8. Initial profile of chlorophyll  $a$  ( $P_{Chla}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
9. Initial profile of dissolved organic carbon ( $DOC$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ]
10. Initial profile of sediment bulk concentration of total phosphorus ( $P_D + P_{IP} + P_{DO} + P_{Chla}$ ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$  wet weight]
11. Initial profile of sediment bulk concentration of chlorophyll  $a$  [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$  wet weight]
12. Initial profile of sediment volume fraction of inorganic matter [ $\text{m}^3 \text{ m}^{-3}$  dry weight]
13. Initial value of total ice thickness [m]
14. Initial value of snow thickness [m]

Microsoft Excel

File Edit View Insert Format Tools Data Window Help

Type a question for help

VAN\_init\_v12.xls

|    | A        | B        | C   | D  | E          | F           | G            |
|----|----------|----------|---|----|------------|-------------|--------------|
| 1  |          | -999     | MyLake model input for Vansjoen (Storefjordens) initial state, last modified 21.02.2005 |    |            |             |              |
| 2  | Z (m)    | Az (m2)  | Tz (deg C)  | Cz | Sz (kg/m3) | TPz (mg/m3) | DOPz (mg/m3) |
| 3  | 0.00E+00 | 2.38E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 4  | 5.00E-01 | 2.27E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 5  | 1.50E+00 | 2.04E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 6  | 2.50E+00 | 1.82E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 7  | 3.50E+00 | 1.61E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 8  | 4.50E+00 | 1.42E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 9  | 5.50E+00 | 1.29E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 10 | 6.50E+00 | 1.16E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 11 | 7.50E+00 | 1.05E+07 | 4   | 0  | 0.004      | 21          | 7            |
| 12 | 8.50E+00 | 9.43E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 13 | 9.50E+00 | 8.43E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 14 | 1.05E+01 | 7.48E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 15 | 1.15E+01 | 6.79E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 16 | 1.25E+01 | 6.03E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 17 | 1.35E+01 | 5.34E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 18 | 1.45E+01 | 4.75E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 19 | 1.55E+01 | 4.16E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 20 | 1.65E+01 | 3.63E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 21 | 1.75E+01 | 3.22E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 22 | 1.85E+01 | 2.84E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 23 | 1.95E+01 | 2.46E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 24 | 2.05E+01 | 2.17E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 25 | 2.15E+01 | 1.90E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 26 | 2.25E+01 | 1.65E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 27 | 2.35E+01 | 1.48E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 28 | 2.45E+01 | 1.27E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 29 | 2.55E+01 | 1.11E+06 | 4   | 0  | 0.004      | 21          | 7            |
| 30 | 2.65E+01 | 9.58E+05 | 4   | 0  | 0.004      | 21          | 7            |
| 31 | 2.75E+01 | 8.18E+05 | 4   | 0  | 0.004      | 21          | 7            |
| 32 | 2.85E+01 | 6.85E+05 | 4   | 0  | 0.004      | 21          | 7            |
| 33 | 2.95E+01 | 5.73E+05 | 4   | 0  | 0.004      | 21          | 7            |

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VAN\_init\_v12.xls

|    | H             | I            | J               | K                 | L                    | M        | N         |
|----|---------------|--------------|-----------------|-------------------|----------------------|----------|-----------|
| 1  |               |              |                 |                   |                      |          |           |
| 2  | Chlaz (mg/m3) | DOCz (mg/m3) | TPz_sed (mg/m3) | Chlaz_sed (mg/m3) | Fvol_IM (m3/m3, dry) | Hice (m) | Hsnow (m) |
| 3  | 7             | 3000         | 100000          | 100000            | 0.95                 | 0        | 0         |
| 4  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 5  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 6  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 7  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 8  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 9  | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 10 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 11 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 12 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 13 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 14 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 15 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 16 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 17 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 18 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 19 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 20 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 21 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 22 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 23 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 24 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 25 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 26 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 27 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 28 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 29 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 30 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 31 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 32 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |
| 33 | 7             | 3000         | 100000          | 100000            | 0.95                 |          |           |

lake / Sheet2 / Sheet3 /

Figure 3. Example of a MyLake morphometry and initial profile file.

Note that the initial sediment concentrations of chlorophyll *a* can be estimated by  $P_{Chla} = (1 - F_{IM}) \cdot \phi \cdot \rho_{organic} \cdot F_{Porg} \cdot y_c$ , where  $\rho_{organic}$  is the density of dry organic matter ( $\sim 1000 \text{ kg m}^{-3}$ ). The total phosphorus concentration in sediment can be estimated by assuming same  $P_D$  and  $P_{DO}$  as in the water column, by converting  $P_{Chla}$  to phosphorus units by dividing with the yield coefficient  $y_c$ , and by estimating  $P_{IP} = F_{IP} \cdot F_{IM} \cdot \phi \cdot \rho_{inorg}$ , where  $\rho_{inorg}$  is the density of dry inorganic matter ( $\sim 2500 \text{ kg m}^{-3}$ ) and  $F_{IP}$  is calculated from  $P_D$  using equation 2.

### 3.2.3 Model parameters

The equation and page numbers below refer to the MyLake v.1.1 documentation (Saloranta and Andersen, 2004).

#### Rows

1. Header row

**(Important!** The first cell on the first row (A1) must contain a number, e.g –999)

2. Header row

3.  $dz$  [m], model vertical grid step (i.e., model layer thickness)

4.  $a_k$  [-] (equation 18), diffusion parameter during open water periods; if "NaN" then  $a_k$  is calculated from lake surface area (page 13)

5.  $a_k$  [-] (equation 18), diffusion parameter during lake ice periods; if "NaN" then  $a_k$  is calculated from lake surface area (page 13)

6.  $N_{min}^2$  [ $\text{s}^{-2}$ ] (page 13); if "NaN" then a default value  $7 \times 10^{-5}$  is assumed (page 13)

7.  $W_{str}$  [-] (equations 23, 24); if "NaN" then  $W_{str}$  is calculated from lake surface area (eq. 24)

8. Lake latitude [decimal degrees]

9. Lake longitude [decimal degrees]

10.  $\alpha_{ice}$  [-], melting ice albedo (page 17)

11.  $\alpha_{snow}$  [-], melting snow albedo (page 17)

12.  $I'$  [ $\text{mol (quanta) m}^{-2} \text{ s}^{-1}$ ] (equation 44)

13.  $f_{PAR}$  [-] (equation 47)

14.  $\beta$  [ $\text{m}^2 \text{ mg}^{-1}$ ] (equation 43)

15.  $\lambda_{ice}$  [ $\text{m}^{-1}$ ], PAR light attenuation coefficient for ice

16.  $\lambda_{snow}$  [ $\text{m}^{-1}$ ], PAR light attenuation coefficient for snow

17.  $\phi_{sld}$  [-], volume fraction of solids in the sediment

18.  $I_{scV}$  [-], dimensionless scaling factor for inflow volume

19.  $I_{scT}$  [ $^{\circ}\text{C}$ ], scaling coefficient for inflow temperature

20.  $I_{scC}$  [-], dimensionless scaling factor for inflow concentration of passive tracer
21.  $I_{scS}$  [-], dimensionless scaling factor for inflow concentration of suspended inorganic particulate matter, (or passive sedimenting tracer)
22.  $I_{scTP}$  [-], dimensionless scaling factor for inflow concentration of total phosphorus
23.  $I_{scP_{DO}}$  [-], dimensionless scaling factor for inflow concentration of dissolved organic phosphorus
24.  $I_{scP_{Chla}}$  [-], dimensionless scaling factor for inflow concentration of chlorophyll *a*
25.  $I_{scDOC}$  [-], dimensionless scaling factor for inflow concentration of dissolved organic carbon (DOC)
26.  $\hat{\varepsilon}_0$  [ $\text{m}^{-1}$ ] (equations 20, 43), non-PAR light extinction coefficient for water (non-chlorophyll related)
27.  $\varepsilon_0$  [ $\text{m}^{-1}$ ] (equations 20, 43), PAR light extinction coefficient for water (non-chlorophyll related)
28.  $S_{res\_epi}$  [ $\text{m d}^{-1}$ ], resuspension rate of dry sediment particles in the epilimnion
29.  $S_{res\_hypo}$  [ $\text{m d}^{-1}$ ], resuspension rate of dry sediment particles in the hypolimnion
30.  $H_{sed}$  [m], depth of the active (mixed) sediment layer
31.  $P_{sat}$  [ $\text{mg m}^{-3}$ ], Langmuir isotherm coefficient, see equation 2 in this document
32.  $F_{max}$  [ $\text{mg kg}^{-1}$ ], Langmuir isotherm coefficient, see equation 2 in this document
33.  $w$  [ $\text{m d}^{-1}$ ] (equation 30), for inorganic matter (*S*); must be  $w > 0$
34.  $w$  [ $\text{m d}^{-1}$ ] (equation 30), for organic matter ( $P_{Chla}$ ); must be  $w > 0$
35.  $y_c$  [-] yield coefficient, i.e. chlorophyll *a* to phosphorus ratio
36.  $m(20)$  [ $\text{d}^{-1}$ ] (equation 39)
37.  $\mu(20)$  [ $\text{d}^{-1}$ ] (equation 41)
38.  $k(20)$  [ $\text{d}^{-1}$ ] as  $m(20)$  but in applies in sediment
39.  $k_{dop}(20)$  [ $\text{d}^{-1}$ ] specific  $P_{OD}$  to  $P_D$  mineralization rate coefficient
40.  $P'$  [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (equation 40)

**Columns** (from 3<sup>rd</sup> row)

1. Parameter names (optional; used in connection with e.g. plotting of figures)
2. Nominal parameter values
3. Minimum of the parameter value range (optional for normal single model runs, but at least one dummy value (e.g. -9) must be given so that MATLAB can read the file in correctly)
4. Maximum of the parameter value range (optional for normal single model runs, but at least one dummy value (e.g. -9) must be given so that MATLAB can read the file in correctly)

5. Remarks (optional). In the example of Figure 5 this column is used to denote the units in which parameter values are required by MyLake model code (fixed units, see list above). This is highly recommended.
6. Remarks (optional). In the example of Figure 5 this column is used to explain the parameter symbols.

| Parameter     | Value    | Min      | Max      | Unit             |
|---------------|----------|----------|----------|------------------|
| dz            | 1        | NaN      | NaN      | m                |
| Kz_ak         | 0.0169   | NaN      | NaN      | (-)              |
| Kz_ak_ice     | 0.0036   | NaN      | NaN      | (-)              |
| Kz_N0         | 7.00E-05 | NaN      | NaN      | s-2              |
| C_shelter     | 7.60E-01 | NaN      | NaN      | (-)              |
| latitude      | 59.42    | NaN      | NaN      | deg.deg          |
| longitude     | 10.83    | NaN      | NaN      | deg.deg          |
| alb_melt_ice  | 0.3      | NaN      | NaN      | (-)              |
| alb_melt_snow | 0.77     | NaN      | NaN      | (-)              |
| PAR_sat       | 1.16E-04 | NaN      | NaN      | mol m-2 s-1      |
| f_par         | 0.45     | NaN      | NaN      | (-)              |
| beta_chl      | 0.015    | NaN      | NaN      | m2 mg-1          |
| lambda_l      | 5        | NaN      | NaN      | m-1              |
| lambda_s      | 15       | NaN      | NaN      | m-1              |
| sed_sld       | 0.2      | NaN      | NaN      | (m3/m3)          |
| I_scV         | 2.2      | NaN      | NaN      | (-)              |
| I_scT         | 0        | NaN      | NaN      | deg C            |
| I_scC         | 1        | NaN      | NaN      | (-)              |
| I_scS         | 0.46     | 0.3      | 0.6      | (-)              |
| I_scTP        | 0.46     | 0.3      | 0.6      | (-)              |
| I_scDOP       | 1        | NaN      | NaN      | (-)              |
| I_scChl       | 0.1      | NaN      | NaN      | (-)              |
| I_scDOC       | 0.75     | NaN      | NaN      | (-)              |
| swa_b0        | 2.5      | NaN      | NaN      | m-1              |
| swa_b1        | 1        | NaN      | NaN      | m-1              |
| S_res_epi     | 3.00E-07 | 1.00E-08 | 1.00E-07 | m d-1 (dry mass) |
| S_res_hypo    | 3.00E-08 | 1.00E-09 | 1.00E-08 | m d-1 (dry mass) |
| H_sed         | 0.03     | NaN      | NaN      | m                |
| Psat_Lang     | 10       | NaN      | NaN      | mg m-3           |
| Fmax_Lang     | 1000     | NaN      | NaN      | mg kg-1          |
| Uz_Sz         | 0.25     | 0.1      | 0.5      | m d-1            |
| Uz_Ch1        | 0.25     | NaN      | NaN      | m d-1            |
| Y_cp          | 1        | NaN      | NaN      | (-)              |
| m_twty        | 0.1      | 0.05     | 0.2      | d-1              |
| g_twty        | 1.5      | 1        | 1.5      | d-1              |
| k_sed_twty    | 0.002    | NaN      | NaN      | d-1              |
| k_dop_twty    | 0.002    | NaN      | NaN      | d-1              |
| P_half        | 0.1      | 0.1      | 2        | mg m-3           |

**Figure 4.** Example of a MyLake parameter file. The colouring highlights the more general, the scaling, and the more site-specific parameter groups.

### 3.3 Switches

The module *solvemodel\_v11.m* contains five switches, which can be used to disable some particular model processes. These are:

- snow\_compaction\_switch (simulation of snow compaction: 0=off, 1=on)
- river\_inflow\_switch (simulation of river inflow: 0=off, 1=on)
- sediment\_heatflux\_switch (simulation of heatflux from sediments: 0=off, 1=on)
- selfshading\_switch (simulation of light attenuation by chlorophyll *a*: 0=off, 1=on)
- tracer\_switch (simulation of tracer state variables: 0=off, 1=on)

### 3.4 How to execute a MyLake v.1.2 model run

When the parameter and input data files are ready, a MyLake model application can be run by the following MATLAB command:

```
function [zz,Az,Vz,tt,Qst,Kzt,Tzt,Czt,Szt,Pzt,Chlzt,PPzt,DOPzt,DOCzt,Qzt_sed,lambdazt,...  
        P3zt_sed,P3zt_sed_sc,His,DoF,DoM,MixStat,Wt] =  
        solvemodel_v12(M_start,M_stop,Initfile,Initsheet,Inputfile,Inputsheet,Parafile,Parasheet);
```

where *M\_start* and *M\_stop* [year, month, day] are row vectors of the model start and stop date; *Initfile*, *Inputfile*, and *Parafile* are strings containing the file names (full paths) of the three files containing lake morphometry and initial profiles, time series of meteorological variables and inflow properties, and model parameter values, respectively. Similarly, *Initsheet*, *Inputsheets*, and *Parasheet* are strings containing the Excel worksheet names containing this data.

For example, using the file examples shown in Figures 2-4 and running the model from May 1, 1998 to December 21, 2000, a model execution line would read:

```
function [zz,Az,Vz,tt,Qst,Kzt,Tzt,Czt,Szt,Pzt,Chlzt,PPzt,DOPzt,DOCzt,Qzt_sed,lambdazt,...  
        P3zt_sed,P3zt_sed_sc,His,DoF,DoM,MixStat,Wt] =  
        solvemodel_v12([1998,5,1],[2000,12,31],  
        'H:\MyLake\Applications\Vansjo\v12_applications\Pcode_Eproject\VAN_init_v12.xls','lake',  
        'H:\MyLake\Applications\Vansjo\v12_applications\Pcode_Eproject\  
        VAN_input_PGS84_00_v12.xls','timeseries','H:\MyLake\Applications\Vansjo\v12_applications\Pcode  
        _Eproject\VAN_para_v12.xls','lake');
```

Note that the whole set of parameter values, initial profiles and input data read from the Excel files (*Parafile*, *Initfile*, *Inputfile*) can also be bypassed by entering these variables in correct order directly in the input list after *Parasheet*, i.e:

```
...=solve_model_v12(M_start,M_stop,Initfile,Initsheet,Inputfile,Inputsheets,Parafile,Parasheet,  
In_Z,In_Az,tt,In_Tz,In_Cz,In_Sz,In_TPz,In_DOPz,In_Chla,In_DOCz,In_TPz_sed,In_Chla_sed,  
In_FIM,Ice0,Wt,Inflw,Phys_par,Phys_par_range,Phys_par_names,Bio_par,Bio_par_range,Bio_par_  
names
```

In other words, the output from model module *modelinputs\_v12.m* to *solve\_model\_v12.m* is replaced by a similar input directly to *solve\_model\_v12.m* given by the user on the command line. The meaning and structure of the output variables from *modelinputs\_v12.m* are not explained here, but the user is referred to the header code of that module for detailed information. The possibility to bypass model parameters and other input variables facilitates easier writing of MATLAB scripts for running the model numerous times with different parameter values, e.g. in connection with Monte Carlo simulations and sensitivity analysis.

The model output variables (i.e., from *solve\_model\_v12.m*) are listed below with units indicated in square brackets. Output matrix dimensions are indicated in parentheses.

|              |  |
|--------------|--|
| <i>zz</i>    | Solution depth domain array (length N) [m], i.e. depths at the top of the layers   |
| <i>Az</i>    | Layer interface area [m <sup>2</sup> ] (N)   |
| <i>Vz</i>    | Layer volume [m <sup>3</sup> ] (N)   |
| <i>tt</i>    | Solution time domain array (length M), i.e. model day number, starting from 1 [d]  |
| <i>Qst</i>   | Estimated surface heat fluxes [W m <sup>-2</sup> ] ( $[Q_{sw}, Q_{lw}, Q_{turb}] \times M$ )   |
| <i>Kzt</i>   | Predicted vertical diffusion coefficient [m <sup>2</sup> d <sup>-1</sup> ] (N $\times$ M)  |
| <i>Tzt</i>   | Predicted temperature profile [°C] (N $\times$ M)  |
| <i>Czt</i>   | Predicted passive tracer profile [-] (N $\times$ M)  |
| <i>Szt</i>   | Predicted suspended inorganic particulate matter profile ( <i>S</i> , functions also as a passive sedimenting tracer) [kg m <sup>-3</sup> ] (N $\times$ M) |
| <i>Pzt</i>   | Predicted dissolved inorganic phosphorus ( <i>P<sub>D</sub></i> , phosphate) profile [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (N $\times$ M)            |
| <i>Chlzt</i> | Predicted chlorophyll <i>a</i> profile ( <i>P<sub>Chla</sub></i> ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (N $\times$ M)                              |
| <i>PPzt</i>  | Predicted profile of phosphorus bound to inorganic particles ( <i>P<sub>IP</sub></i> ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (N $\times$ M)          |
| <i>DOPzt</i> | Predicted dissolved organic phosphorus profile ( <i>P<sub>DO</sub></i> ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (N $\times$ M)                        |
| <i>DOCzt</i> | Predicted dissolved organic carbon profile ( <i>DOC</i> ) [ $\mu\text{g l}^{-1} = \text{mg m}^{-3}$ ] (N $\times$ M)                                       |



|                   |  |
|-------------------|--|
| $Qz_{sed}$        | Predicted sediment-water heat flux (normalised values, see page 13) [ $\text{W m}^{-2}$ ] ( $N \times M$ )   |
| $\lambda_{bdazt}$ | Predicted average total light attenuation coefficient down to depth $z$ [ $\text{m}^{-1}$ ] ( $N \times M$ )   |
| $P3zt_{sed}$      | Predicted concentrations of $P_D$ , $P_{IP}$ , and $P_{Chla}$ in the sediment, as well as amount of inorganic and organic net sedimentation (dry matter), and the volume fraction of dry inorganic matter in dry sediment solids [ $\text{mg m}^{-3}$ , $\text{mg kg}^{-1}$ , $\text{mg kg}^{-1}$ , $\text{m d}^{-1}$ , $\text{m d}^{-1}$ , -] ( $N \times M \times 6$ ) |
| $P3zt_{sed}_{sc}$ | Predicted phosphorus resuspension sources for $P_D$ , $P_{IP}$ , and $P_{Chla}$ from the sediment [ $\text{mg m}^{-3} \text{d}^{-1}$ ] ( $N \times M \times 3$ )   |
| $His$             | Ice and snow simulation matrix [ $\text{m}$ , $\text{m}$ , $\text{m}$ , $^{\circ}\text{C}$ , $^{\circ}\text{C}$ , $\text{kg m}^{-3}$ , boolean] ( $[h_{ice} h_s h_{si} T_{ice} T_a \rho_s \text{IceOn/Off}] \times M$ )  |
| $DoF$             | Predicted days of freezing [model day number]  |
| $DoM$             | Predicted days of melting [model day number]   |
| $MixStat$         | Temporary variables used in model testing, see model code ( $X \times M$ )   |
| $Wt$              | Meteorological forcing data ( $M \times$ variables in columns 4-10 described in section 3.2.1)   |

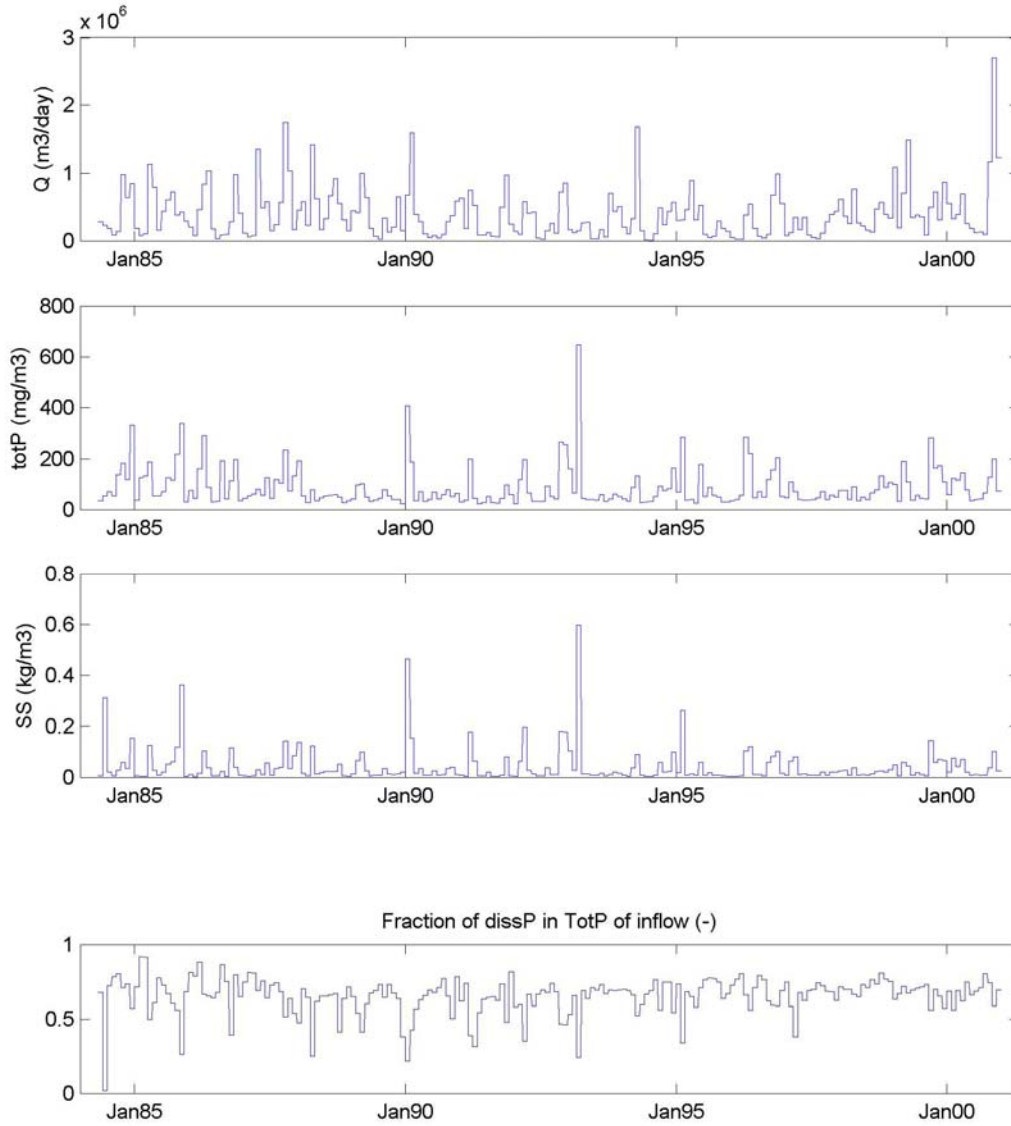
Note that the model execution time can easily be reduced by supplying the table for albedo calculation routine via function call, and by optimizing an iteration loop in the turbulent heatflux function (hfbulktc.m) in the *Air-Sea Toolbox* (contact the report authors for more details on this optimization). Increasing vertical grid step size, and turning off e.g. simulation of the tracers and/or calculation of sediment-water heat fluxes, by using the switches described in section 3.3, will also contribute to shorter model execution times.

## 4. Application example from Lake Vansjø

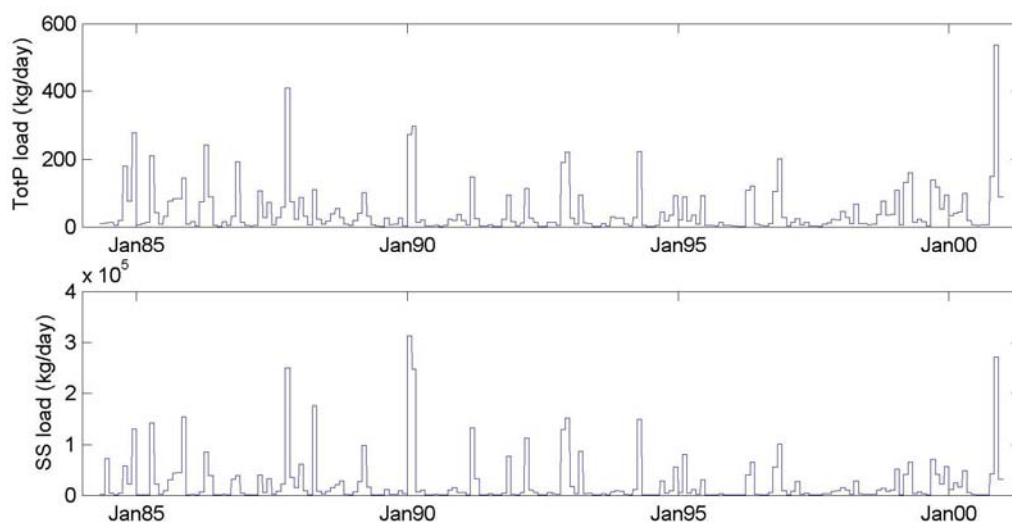
The functioning of MyLake v.1.2 was tested with an application in the Storefjorden subbasin of Lake Vansjø. Daily meteorological time series from Rygge and Ås stations, as well as monthly mean time series of water flow, total phosphorus concentration and suspended solids at Kure station of River Hobøl (Stålnacke et al., 2005; Figures 5-7) were used as model forcing in 1984-2000. Evaluation of model results was done against observed data of monthly mean time series of chlorophyll *a* and total phosphorus (Stålnacke et al., 2005), as well as suspended solids in the 0-4 m water column of Storefjorden subbasin.

Although the time series at Kure provide good data of the long term variability in the main river inflowing to Storefjorden, the distance from Kure station to Vansjø is ~10 km and thus the transports estimated at Kure may not always well represent the actual loads of phosphorus and suspended matter

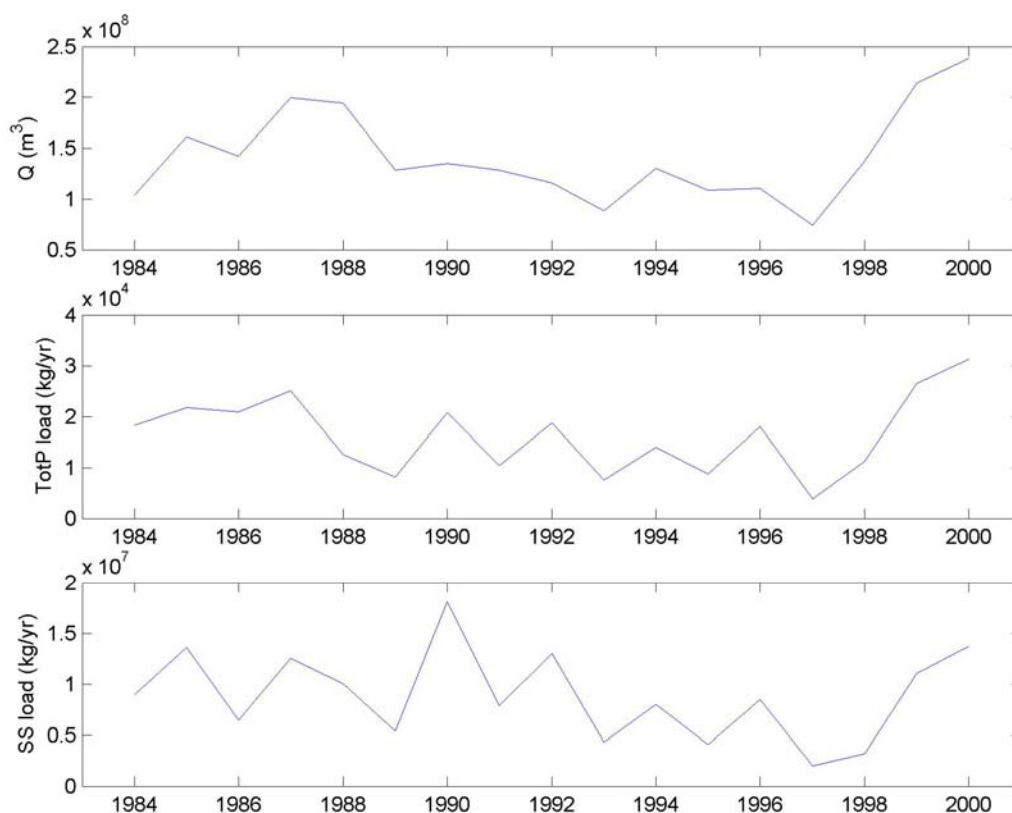
into Storefjorden subbasin, due to, e.g., sedimentation and resuspension processes taking place downstream of Kure. Moreover, the inflow of Hobølvelva is not the only input of water into Storefjorden subbasin. Therefore the time series measured at Kure were scaled for model input to account for estimated yearly loads into and outflow from Storefjorden subbasin. The flow measured at Kure was multiplied by 2.2 to account for the mean estimated outflow of  $3.18 \cdot 10^8 \text{ m}^3$  from Storefjorden in 1984-2000 (measured outflow from the whole Vansjø multiplied by the Storefjorden part of the whole Vansjø catchment, 0.9). To retain the yearly load of total phosphorus at the level ~17 tons per year, estimated in Lyche Solheim et al. (2001), its concentration in the inflow was correspondingly divided by 2.2. Similar scaling was also done for the suspended solids concentration. The concentration of  $P_{DO}$  in the inflow was assumed constant  $8 \text{ mg m}^{-3}$ . Parameter values shown in Figure 4 were applied (the model was not calibrated for this test application in any systematic way). Figures 8-13 show various model results from the Vansjø-Storefjorden application for the period 1984-2000.



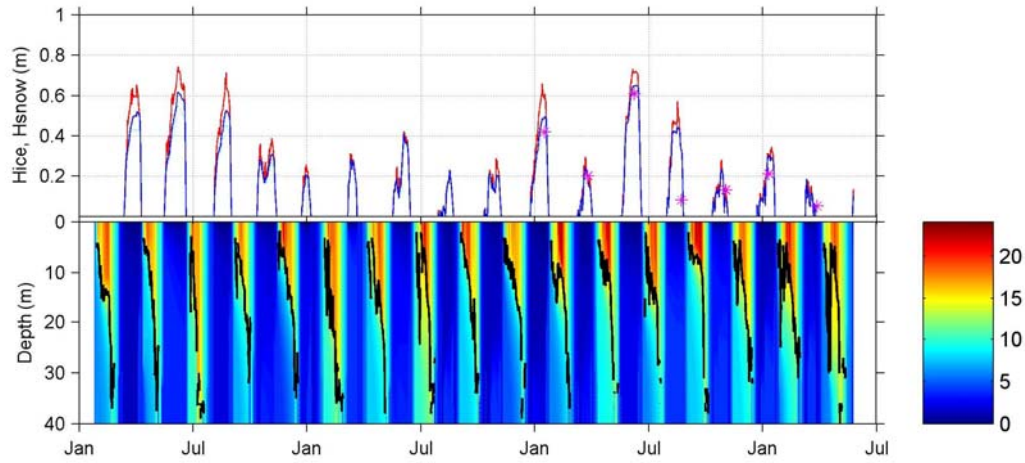
**Figure 5.** Time series of water flow, as well as concentration of total phosphorus and suspended solids at Kure station of River Hobøl in 1984-2000. Yearly mean water flow is  $1.45 \cdot 10^8 \text{ m}^3$ , and the mean concentrations of total phosphorus and suspended solids are  $88 \text{ mg m}^{-3}$  and  $0.042 \text{ kg m}^{-3}$ , respectively. The lowermost figure shows the calculated (equation 2) fraction of dissolved phosphorus in total phosphorus concentration (0.65 in the mean).



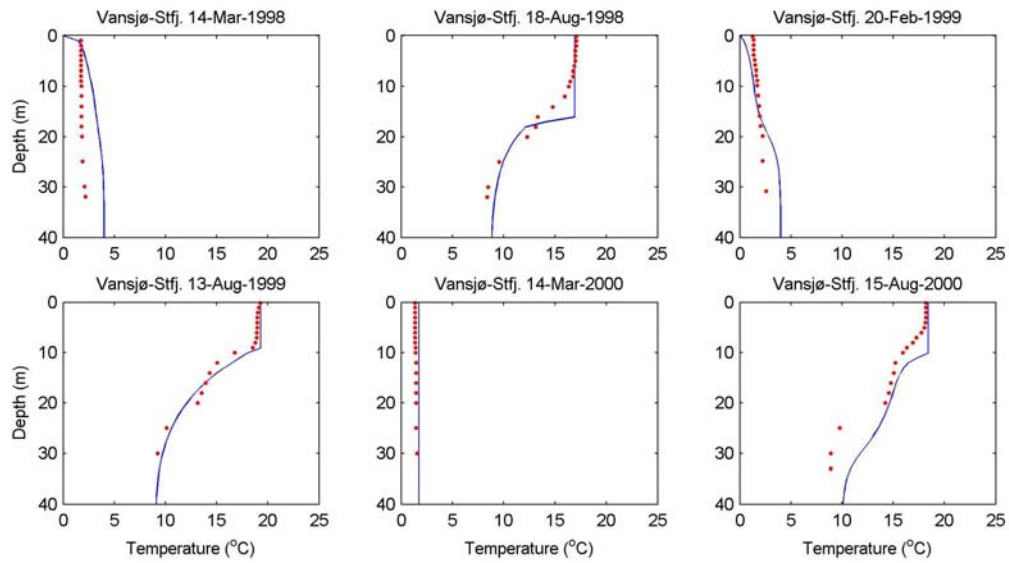
**Figure 6.** Time series of daily transports of total phosphorus and suspended solids at Kure station of River Hobøl in 1984-2000. Mean loads are 16.7 and 9000 tons per year, respectively.



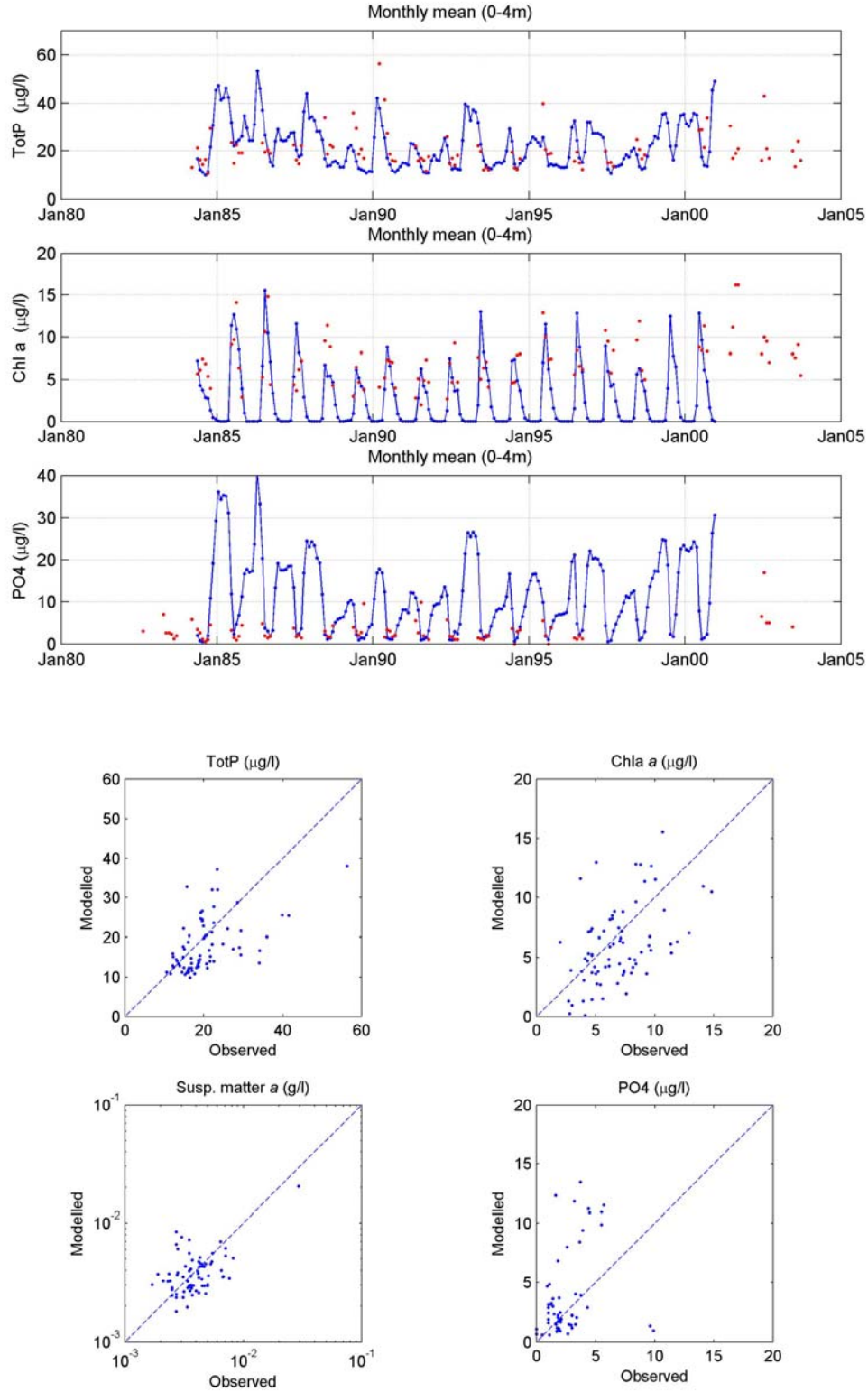
**Figure 7.** Time series of yearly loads of water, total phosphorus and chlorophyll a at Kure station of River Hobøl in 1984-2000.



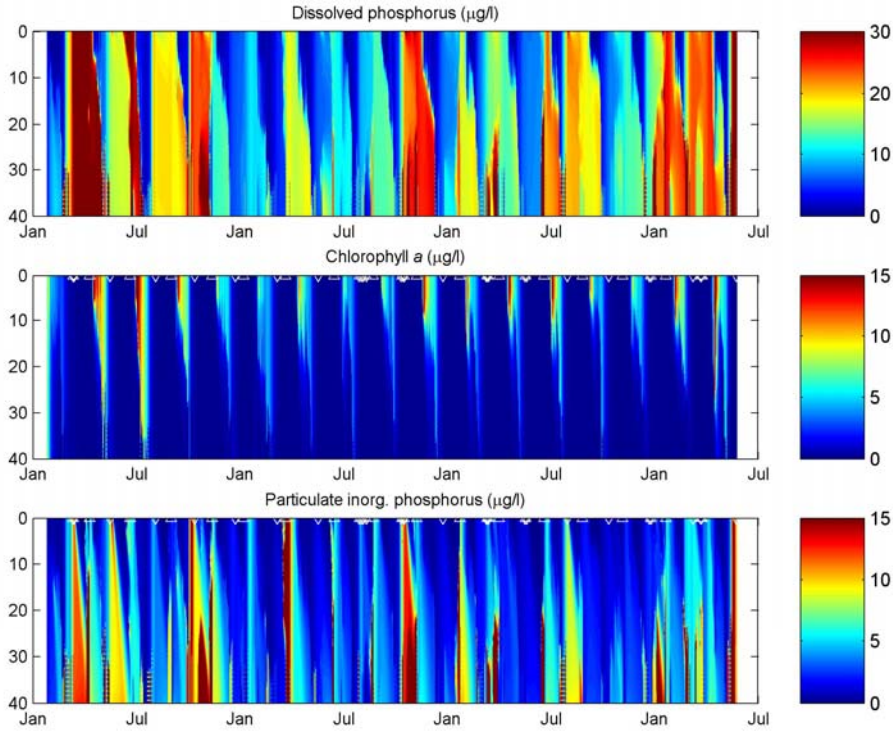
**Figure 8.** *Measured vs. simulated temperature and ice conditions in 1984-2000 in Vansjø-Storefjorden.*



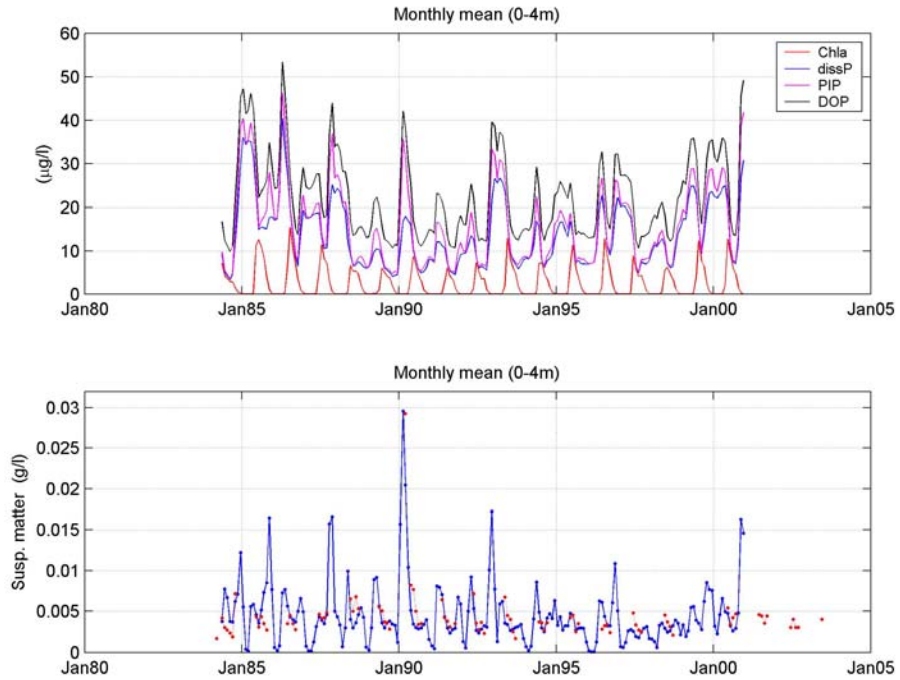
**Figure 9.** *Measured (red dots) vs. simulated temperature in 1998-2000 in Vansjø-Storefjorden.*



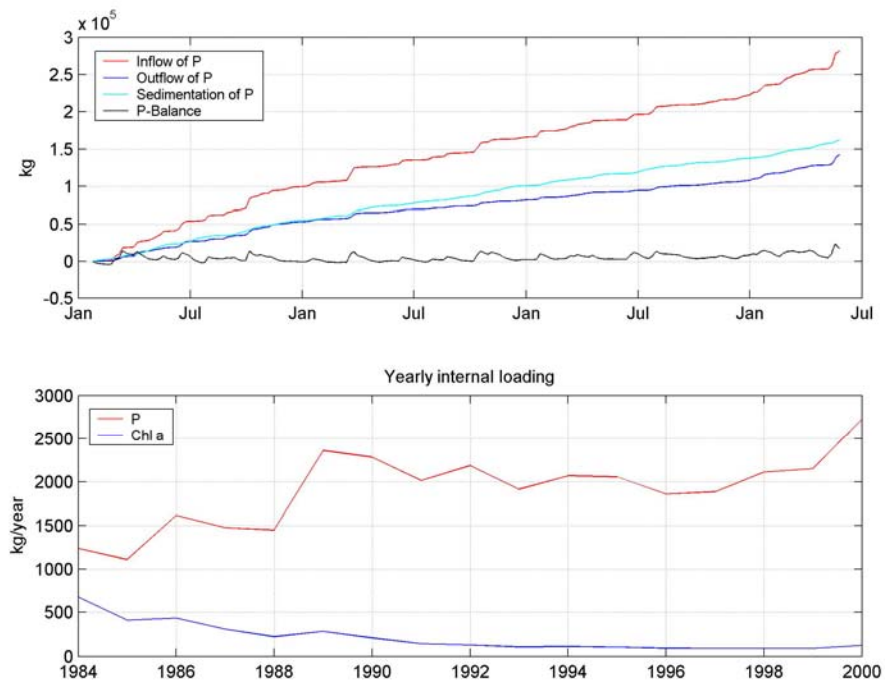
**Figure 10.** Measured (red dots in the upper panel) vs. simulated total phosphorus ( $P_D + P_{IP} + P_{DO} + P_{Chla}$ ),  $P_{Chla}$ ,  $P_D$  ( $PO_4$ ) and suspended matter ( $S + S_{org}$ , lower panel only) in 1984-2000 in Vansjø-Storefjorden.



**Figure 11.** Simulated profiles of  $P_D$ ,  $P_{Chla}$ , and  $P_{IP}$  in 1984-2000 in Vansjø-Storefjorden.



**Figure 12.** Simulated phosphorus fractions (cumulative sum of  $P_{Chla}$ ,  $P_D$ ,  $P_{IP}$ , and  $P_{DO}$ , upper panel), and simulated vs. observed (red dots) suspended matter concentration ( $S+S_{org}$ , lower panel; see also Figure 10) in 1984-2000 in Vansjø-Storefjorden.



**Figure 13.** Simulated cumulative phosphorus balance in the water column (upper panel), and yearly resuspension of phosphorus and chlorophyll a from the sediments (lower panel) in 1984-2000 in Vansjø-Storefjorden (NB! P-balance curve is wrongly plotted).



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