Basics Start/Stop Data Check data/Common Mistakes Multistate Data

Wrangling Survival Data From Time-dependent Covariates to Multistate Endpoints

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Outline

- ► Time to event one observation per subject
- Start/Stop data
 - ▶ Why needed?
 - ► New tools: tmerge, survSplit
 - Check data: survcheck
 - Common mistakes
- Multistate data
 - Competing risk



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Basics



Logistics

- ➤ All code shown based on the latest/greatest version of the survival package (3.0)
- Slides/Example code available at https://github.com/bethatkinson/rmed2019_surv
 - Examples loaded into RStudio Cloud https://rstudio.cloud/project/475200
- ► Email: atkinson@mayo.edu





Background

- ▶ I am a statistician working in medical research
- Many of the questions I work with are "time until ..."
 - Fracture
 - Diagnosis of a chronic comorbidity
 - Liver transplant
 - Death
 - **.**..
- I study osteoporosis in population-based cohorts, so many of my examples deal with fractures
- ▶ I started off using Splus in 1990 so my code is a mix of base R and tidyverse



Premise

Most statistics discussions focus on the analysis and assume the data is already in shape. The reality is that:

- Data wrangling takes much of the time
- Doing it correctly is critical
- ... so that's what I'll talk about



Some principles of data creation

- Correct is more important than fast: Don't worry if the code takes a bit to run. We often do dozens of fits using one dataset
- Correct is more important than clever
- Readable is more important than short
- Use every data check opportunity available
- ► Comments are your friend, or better yet make the data creation an Rmd file with text explaining the code



Key Principle

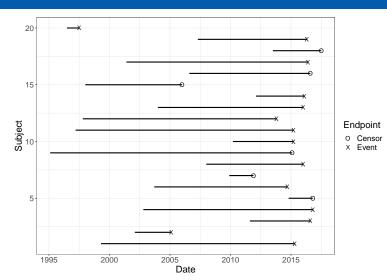
"It takes time to observe time"

Challenges:

- Incomplete information (censoring). At the time of an analysis, not everyone will have yet had the event.
- Dated results.
 - In order to report 5 year survival, from a treatment, patients need to be enrolled and then followed for 5+ years.
 - ▶ By the time recruitment and follow-up is finished, the final report on the treatment might be 8 years old and considered out of date.

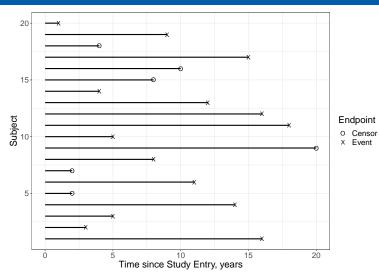


Calendar Year Scale



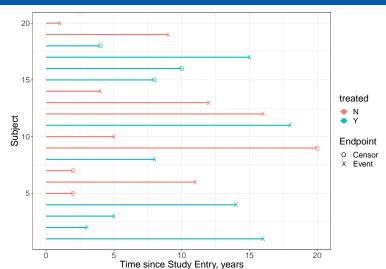


Time from Study Entry Scale





Compare Baseline Treatment Groups





Example: AML data

Does maintainance of the standard course of chemotherapy improve survival for patients with Acute Myelogeous Leukemia?

```
> dim(aml)
[1] 23 3
> head(aml)
  time status
                         х
             1 Maintained
    13
             1 Maintained
3
    13
             0 Maintained
    18
             1 Maintained
4
5
    23
             1 Maintained
6
    28
             0 Maintained
                                                                  CLINIC
```

MAYO

Create endpoint in survival package

A time-to-event outcome consists of 2 pieces of information:

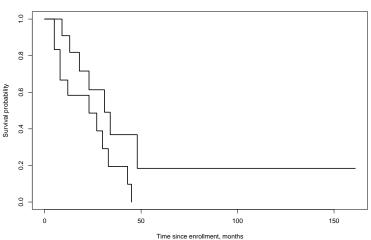
- Length of time over which the patient was observed
- Presence/absence of the event at the end of the time period
 - ► 0=censor/1=event
 - FALSE=censor/TRUE=event
 - ► 1=censor/2=event

```
> with(aml, Surv(time=time, event=status))[1:6]
[1] 9 13 13+ 18 23 28+
> aml$status[1:6]
[1] 1 1 0 1 1 0
```

Kaplan-Meier Curves: default





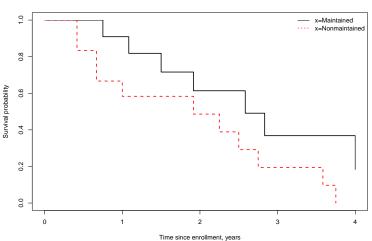




Kaplan-Meier Curves: better

```
> print(fit, scale=12)
Call: survfit(formula = Surv(time, status) ~ x, data = aml)
                n events median 0.95LCL 0.95UCL
x=Maintained 11 7 2.58 1.500
                                           NA
x=Nonmaintained 12 11 1.92 0.667
                                           NA
> plot(fit, xscale=12, xlim=c(0, 4*12),
     col=1:2, lty=1:2,
     xlab='Time since enrollment, years',
     ylab='Survival probability')
> legend('topright', legend=names(fit$strata),
       col=1:2, lty=1:2, bty='n')
```

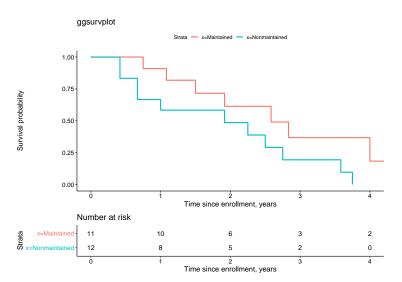




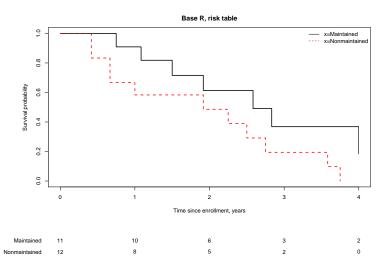


Kaplan-Meier Curves: ggsurvplot











Cox Models



Your Turn - Run basic analysis

► See exercises/1.basic_survival.Rmd



Start/Stop Data Start/Stop Data Check data/Common Mistakes Multistate Data

Start/Stop Data



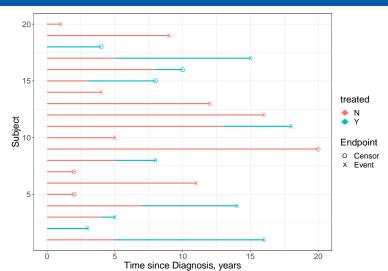
Use Cases

When is start/stop data needed?

- Time-dependent covariates
- ▶ Multiple events of the same type per subject
- Left truncation or gaps in observation
- Analysis by time periods
- Multistate
- => Deceptively simple task, easy to do incorrectly



Time-Dependent Covariates



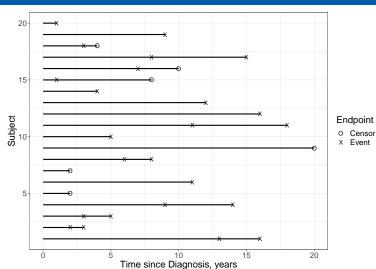


Time-Dependent Covariates

- Lab values that change over time (pbcseq data)
- Medication
 - Ever exposed
 - Cumulative dose
 - On and off
- ▶ Diagnosis of new comorbidity (e.g., diabetes)
- Surgery



Multiple Events/Same Type



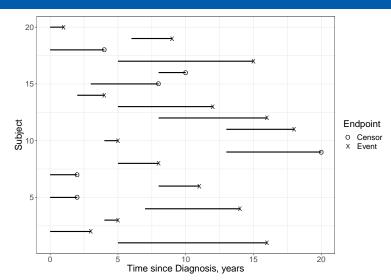


Multiple Events/Same Type

- Fractures
- Repeat infections (rhDNase, cgd data)
- Number of recurrences of cancer (bladder data)



Left Truncation



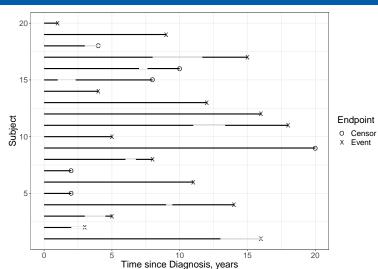


Left Truncation

- Disease started prior to diagnosis, want time-scale to be time-since-onset
- ▶ Population-based cohort, interested in "age" as a time-scale



Gaps in Follow-up



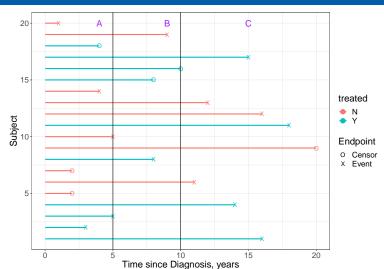


Gaps in Follow-up

- After an event, subjects are not at risk during the course of antibiotics or for 6 days after treatment ends (rhDNase data)
- Subjects move out of the region temporarily and are not "at risk" during that time



Analysis by Time Period





Analysis by Time Period

- Risk of event during first 5 years after cancer is different than afterwards
- ► Effect decreases over time
 - baseline lab variable
 - treatment



Simple Example: Data we have

- Initial dataset has 1 observation per subject
- Surgery is a time-dependent covariate

id	age	tm_fu	event	tm_surg
1	40	10	0	5
2	20	20	1	8
3	50	30	1	NA



Simple Example: What we want

id	tstart	tstop	death	age	surgery
1	0	5	0	40	0
1	5	10	0	40	1
2	0	8	0	20	0
2	8	20	1	20	1
3	0	30	1	50	0



Counting Process data

- ▶ (time1, time2] time interval
- status at the end of time2
- covariates as of time1



Start/Stop Data Check data/Common Mistakes Multistate Data

Creating Start/Stop Data



The tmerge function

- tmerge function in survival package: tool for creating start/stop data
- Sequential insertion
 - Build the dataset one covariate or endpoint at a time
 - ► Each addition will be "slipped in" to the original data in the same way that one would slide a new card into an existing deck of cards



The tmerge function

▶ The basic form of the function call is

- primary arguments:
 - data1: baseline data to be retained in the analysis dataset
 - data2: source for new data including events and time-dependent covariates
 - id: subject identifier used to merge the data together
 - ...: additional arguments that add variables to the dataset
 - tstart, tstop: used to set the time range for each subject
 - options



The tmerge function

- ► The key part of the call are the "..." arguments, which can be one of 4 types:
 - tdc() and cumtdc() add a time-dependent covariate
 - event() and cumevent() add a new endpoint
- Resulting dataset has 3 new variables (at least):
 - ▶ id: identifier indicating which rows belong to the same subject
 - tstart: start of the interval
 - tstop: end of the interval



Example

▶ Baseline data: d1

```
id age
1 1 40
2 2 20
3 3 50
```

► Time varying data: d2

```
id tm_fu event tm_surg
1 1 10 0 5
2 2 20 1 8
3 3 30 1 NA
```

Example: step 1 - create start/stop time



Example: step 2 - create time-dependent covariate



This can also be done in just one step:



```
> attr(step2, "tcount")
```



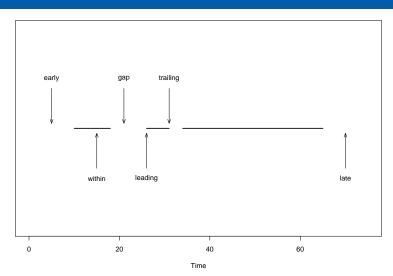
tcount - a tool to check data

- ► Time outside the specified time frame.
 - "early" occur before the first interval for a subject
 - "late" occur after the last interval for a subject
 - "gap" times fall into a gap
 - These events will be discarded.
 - ► A TD covariate value will be applied to later intervals
- "within" fall inside an existing interval and cause it to be split into two



- Observations that fall exactly on the edge of an interval but within the (min, max] time for a subject are counted as being on a "leading" edge, "trailing" edge or "boundary".
- "tied" shows # of additions where the id and time point were identical.







- ▶ 3 trailing deaths
- ▶ 2 *within* splits with surgery

```
    id age tstart tstop death surgery

    1 1 40 0 5 0 0

    2 1 40 5 10 0 1

    3 2 20 0 8 0 0

    4 2 20 8 20 1 1

    5 3 50 0 30 1 0
```



Example: Original Analysis, Stanford heart transplant data

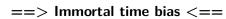
- Original analysis used: futime, fustat, transplant status, and age
 - ► Transplant happened after baseline
 - jasa dataset

```
Call:
```

```
coxph(formula = Surv(futime, fustat) ~ age + transplant, data =
```

```
coef exp(coef) se(coef) z p
age 0.06020 1.06205 0.01531 3.933 8.40e-05
transplant -1.80047 0.16522 0.27225 -6.613 3.76e-11
```

```
Likelihood ratio test=44.46 on 2 df, p=2.214e-10 n= 103, number of events= 75
```





Your Turn - Create the Correct Data

- Stanford heart transplant data (jasa)
 - wait.time: time before transplant (tx)
 - futime: follow-up time
 - fustat: dead or alive
 - age
- Create

id	tstart	tstop	death	age	tx
1					

See the file exercises/2.jasa.Rmd.



Stanford Heart Transplant



What went wrong?

▶ 1 subject died on the day of entry. (0,0) is an illegal time interval for coxph.
It suffices to have them die on day 0.5.

```
> jasa$futime <- pmax(0.5, jasa$futime)</pre>
```



Rerun

```
> attr(sdata, "tcount")
```

```
early late gap within boundary lead trail tied death 0 0 0 0 0 0 103 0 tx 0 0 0 66 0 2 1 0
```



What does "trailing" mean?

➤ Subject died on the same day as their procedure. The problem is resolved by moving the transplant back 0.5 day.

Rerun again

```
> attr(sdata, "tcount")
```

```
death 0 0 0 0 0 0 0 103 0 tx 0 0 0 67 0 2 0 0
```

Yay!



Cox Model

```
> fit <- coxph(Surv(tstart, tstop, death) ~ age + tx,
             data=sdata)
> fit
Call:
coxph(formula = Surv(tstart, tstop, death) ~ age + tx, data = sd
        coef exp(coef) se(coef) z
age 0.030758 1.031236 0.014496 2.122 0.0339
tx -0.006058 0.993960 0.311750 -0.019 0.9845
Likelihood ratio test=5.17 on 2 df, p=0.07541
n= 170, number of events= 75
```

Example: Continuous values that change over time

- pbcseq is from the Mayo Clinic trial in primary biliary cirrhosis (PBC) of the liver conducted between 1974 and 1984. 312 subjects were randomized to placebo or D-penicillamine.
- ► The data has 1945 observations with repeated laboratory values + baseline variables

id	futime	status	trt	day	alk.phos	bili
1	400	2	1	0	1718	14.5
1	400	2	1	192	1612	21.3
5	1505	1	0	0	671	3.4
5	1505	1	0	199	689	1.9
5	1505	1	0	391	652	2.5
5	1505	1	0	769	554	5.7
5	1505	1	0	1098	588	5.2
5	1505	1	0	1455	377	19.0

MAYO

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Create baseline data

```
> # baseline
> pbc_b <- pbcseq %>% select(id:sex) %>% distinct()
> head(pbc b)
 id futime status trt
                         age sex
       400
               2 1 58.76523
     5169
               0 1 56.44627
  3
     1012
               2 1 70.07255
               2 1 54.74059
    1925
                               f
    1505
                   0 38.10541 f
      2503
                   0 66.25873
```



Look at status

After discussion with investigator, decided that in this instance, transplant (1) and death (2) can both be treated as death.

```
> pbc_b$status2 <- as.numeric(pbc_b$status>0)
```



Set range

```
> # set range
> newpbc <- tmerge(pbc_b, pbc_b, id=id,
                death = event(futime, status2))
>
> print(head(newpbc),digits=2)
  id futime status trt age sex status2 tstart tstop death
        400
                        59
                             f
                                                 400
  1
       5169
                        56
                                               5169
3
  3
                     1 70
       1012
                                               1012
      1925
                        55 f
                                               1925
                        38 f
                                               1505
      1505
6
       2503
                     0
                        66
                             f
                                               2503
```



Create new TDC variables



_							
id	tstart	tstop	death	sex	ascites	bili	albumin
1	0	192	0	f	1	14.5	2.60
1	192	400	1	f	1	21.3	2.94
2	0	182	0	f	0	1.1	4.14
2	182	365	0	f	0	8.0	3.60
2	365	768	0	f	0	1.0	3.55
2	768	1790	0	f	0	1.9	3.92



Example: Continuous values that change over time

```
> attr(newpbc, "tcount")
```

	early	late	gap	within	boundary	lead	trail	tied
death	0	0	0	0	0	0	312	0
ascites	0	0	0	1573	0	312	0	0
bili	0	0	0	60	1573	312	0	0
albumin	0	0	0	0	1633	312	0	0



Example: Continuous values that change over time

- Missing values in time or value from data2 are ignored
 - Consequence: "last value carried forward"
- Default can be changed by adding options=list(na.rm=FALSE) to the second call
 - Any tdc calls with a missing time are still ignored, independent of the na.rm value, since we would not know where to insert them.



Basics **Start/Stop Data** Check data/Common Mistakes Multistate Data

Code available in 3.pbc.Rmd



How covariates differ from events

- Time-dependent covariates
 - Apply from the start of a new interval
 - Persist for all remaining intervals unless subsequently changed
- Events
 - Occur at the end of an interval
 - Only occur once



Your Turn

- Chronic Granulotamous Disease (cgd0)
 - id, treat, sex, age
 - futime: follow-up time
 - etime1-etime7: up to 7 infection times/subject
- Create

id	tstart	tstop	infect	treat	enum
1					

where enum is the interval number/id

See exercises/4.cgd.Rmd



CGD



CGD

```
> attr(newcgd, "tcount")
```

	early	late	gap	${\tt within}$	boundary	lead	trail	tied
infect	0	0	0	44	0	0	0	0
infect	0	0	0	16	0	0	1	0
infect	0	0	0	8	0	0	0	0
infect	0	0	0	3	0	0	0	0
infect	0	0	0	2	0	0	0	0
infect	0	0	0	1	0	0	0	0
infect	0	0	0	1	0	0	0	0
enum	0	0	0	0	75	128	0	0



CGD

```
> newcgd %>% filter(id==2) %>%
   select(id, tstart, tstop, infect, enum)
  id tstart tstop infect enum
  2
                8
               26
3
        26
             152
        152
              241
        241
             249
6
        249
              322
                            6
              350
                            7
        322
8
        350
              439
                            8
```



CGD

```
> fit <- coxph(Surv(tstart, tstop, infect) ~ treat +</pre>
           steroids + inherit, id=id, data=newcgd)
> fit
Call:
coxph(formula = Surv(tstart, tstop, infect) ~ treat + steroids +
   inherit, data = newcgd, id = id)
          coef exp(coef) se(coef) robust se
treat -1.0722 0.3422 0.2619 0.3118 -3.438
inherit 0.1777 1.1944 0.2356 0.3180 0.559
treat 0.000585
steroids 0.099310
                                                   MAYO
inherit 0.576395
                                                   CLINIC
```

Likelihood ratio test=22.49 on 3 df, p=5.149e-05

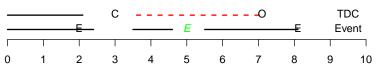
CGD

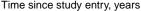
Look at the first infection versus all infections



Gaps

- ➤ Time dependent covariates that occur before the start of a subject's follow-up interval or during a gap in time do not generate a new interval split, but they do set the value of that covariate for future times.
 - During a subject's time under observation we would like the variable "Has diabetes" to be accurate
- Events that occur in a gap are not counted.
 - Don't know the appropriate comparison group, so we ignore those events.







Example: Intentional gaps, rhDNase

- Randomized clinical trial examining a treatment for cystic fibrosis
- Infection is the event of interest, indicated by ivstart
- For 6 days after ivstop, the subject is not at risk for a new infection

id	inst	trt	entry.dt	end.dt	fev	ivstart	ivstop
1	1	1	1992-03-20	1992-09-04	28.8	NA	NA
129	12	0	1992-02-23	1992-08-07	105.6	5	26
129	12	0	1992-02-23	1992-08-07	105.6	44	58
129	12	0	1992-02-23	1992-08-07	105.6	87	108
129	12	0	1992-02-23	1992-08-07	105.6	124	143
129	12	0	1992-02-23	1992-08-07	105.6	163	166



Your Turn

Use the rhDNase data found in the survival package:

- 1. Create range for when subjects are under observation (tmerge)
- 2. Create event for each infection (tmerge)
- 3. Create intervals where they are not at risk (tmerge)
- 4. Remove intervals where not at risk
- Add a counter for each person (tmerge)
- 6. Check data and tcount attribute

See exercises/5.dnase.Rmd



Quick look at the data

```
> dim(rhDNase)
[1] 767
 head(rhDNase)
  id inst trt
                 entry.dt
                              end.dt fev ivstart ivstop
              1992-03-20 1992-09-04 28.8
                                                 NA
                                                        NA
              1992-03-24 1992-09-09 64.0
                                                        NA
                                                 NA
3
            0 1992-03-24 1992-09-08 67.2
                                                 65
                                                        75
4
              1992-03-26 1992-09-10 57.6
                                                 NA
                                                        NA
5
            0 1992-03-24 1992-09-11 57.6
                                                 NA
                                                        NA
6
            1 1992-03-27 1992-09-09 25.6
                                                 NA
                                                        NA
```



```
> table(table(rhDNase$id)) # number obs/id

1  2  3  4  5
565  53  21  7  1
> table(!is.na(rhDNase$ivstart)) # number events

FALSE TRUE
400  367
```



Create range for when subjects are under observation



Create event for each infection

```
> dn2 <- tmerge(dn1, dnase,
              infect=event(ivstart), id=id)
 dn2[dn2$id==129,]
    id inst trt fev tstart tstop infect
         12
204 129
             0 105.6
                          0
205 129 12 0 105.6
                              44
206 129 12
             0 105.6
                        44
                              87
207 129 12 0 105.6
                         87
                             124
208 129 12
             0 105.6
                             163
                        124
209 129
         12
             0 105.6
                        163
                             166
```



Create intervals where they are not at risk

```
> dn3 <- tmerge(dn2, dnase,</pre>
             no.risk=event(ivstop+6), id=id)
 dn3[dn3$id==129,]
    id inst trt
                 fev tstart tstop infect no.risk
271 129
         12
              0 105.6
272 129 12
              0 105.6
                          5
                              32
273 129 12
              0 105.6
                         32
                              44
274 129 12
              0 105.6
                         44 64
275 129
        12
              0 105.6
                         64 87
         12
              0 105.6
                         87
                              114
276 129
277 129
         12
              0 105.6
                        114
                              124
         12
                              149
278 129
              0 105.6
                        124
         12
                              163
279 129
              0 105.6
                        149
280 129
         12
              0 105.6
                        163
                              166
```



Remove intervals where not at risk

```
> dn4 <- dn3[dn3$no.risk!=1,]</pre>
```

Add a counter for each person

```
> newdnase <- tmerge(dn4, dn4, enum=cumtdc(tstart), id=id)
```



Check to make sure code worked correct

```
> newdnase[newdnase$id==129,]
                  fev tstart tstop infect no.risk enum
    id inst trt
204 129
         12
              0 105.6
                           0
205 129 12
              0 105.6
                          32
                                44
206 129 12
              0 105.6
                          64
                                87
207 129
         12
              0 105.6
                         114
                               124
208 129
         12
              0 105.6
                         149
                               163
                                                     5
                                                     6
209 129
         12
              0 105.6
                         163
                               166
```



rhDNase: check tcount

```
> attr(newdnase, "tcount")
```

	early	late	gap	within	boundary	lead	trail	tied
infect	6	0	0	358	0	0	3	0
no.risk	0	51	0	315	0	0	1	0
enum	0	0	0	0	46	958	0	0



tmerge summary

- tmerge is a simple to use, flexible tool to create multiple start/stop intervals per subject
 - time-dependent covariates both binary and continuous
 - multiple outcomes per subject
 - allows for gaps in time
 - sometimes useful to create both tdc and event
- data checks can help avoid errors
 - tcount attribute



The survSplit function

- ► Another approach to create start/stop data
- Breaks follow-up at specified cut points
- Useful when you want separate coefficients within time periods



Go back to d2 data

```
id tm_fu event tm_surg
1 1 10 0 5
2 2 20 1 8
3 3 30 1 NA
```



survSplit

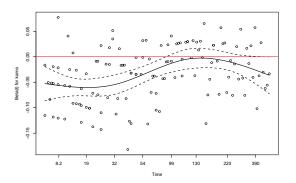
```
> survSplit(Surv(tm_fu, event) ~ ., data=d2,
           cut=c(5,15), episode='timegp')
  id tm_surg tstart tm_fu event timegp
           5
                         5
                        10
3
                        5
                        15
                  15
                        20
  3
6
          NA
                        5
          NA
                        15
8
                                       3
   3
          NA
                  15
                        30
```



Example: Veteran Data

```
> fit1 <- coxph(Surv(time, status) ~ karno, data=veteran)</pre>
```

- > plot(cox.zph(fit1), lwd=2)
- > abline(h=0, col=2)





Example: Veteran Data



```
> # original
> round(coef(fit1), 3)
 karno
-0.033
> # within time period
> tmp <- round(coef(fit2), 3)
> names(tmp) <- c('t0 60','t60 120','t120+')</pre>
>
> tmp
 t0_60 t60_120 t120+
 -0.048 -0.011 -0.007
```



Caution - don't create too many intervals

- Compute time for coxph is proportional to the number of observations in the dataset
- ► If there are no observations that span two event times, then further splitting won't change the results



Start/Stop Data
Check data/Common Mistakes
Multistate Data

Check data/Common Mistakes



The survcheck function

- ▶ The basic form of the function call is
- > ck1 <- survcheck(formula, data, id, istate)

- checks include:
 - overlap: subject is in 2 places at the same time
 - gap: gap in timeline
 - teleport: 2 adjacent intervals, change in state
 - iump: hole in timeline, change in state



Example: Multiple Events/Same type (newcgd)

```
Call:
survcheck(formula = Surv(tstart, tstop, infect) ~ treat, data =
   id = id)

128 subjects available for analysis
Transitions table:
   to
```

from 1 (censored) (s0) 44 84 1 32 43

Number of subjects with 0, 1, \dots transitions to each state:

```
state 0 1 2 3 4 5 7
1 84 27 9 5 1 1 1
(any) 84 27 9 5 1 1 1
```



239

Example: Gaps (newdnase)

Call:

Number of subjects with 0, 1, \dots transitions to each state:

```
state 0 1 2 3 4 5
1 404 162 53 20 7 1
(any) 404 162 53 20 7 1
```

118

Example: Gaps (newdnase)



Common Mistake: Responders vs non-responders

Group people, at baseline, according to whether they eventually had a response to therapy, and then draw the survival curves. Surprise – responders always do better! Why?

- Assume patients are evaluated every 4 weeks
- Response, if it occurs, will happen by week 12
- ► Anyone who dies before week 4 is a non-responder, and most of those who die, do so before week 8
- You have to live longer to be called a responder



Common Mistake: KM Curves using Time-Dep Covariates

Suppose you have created a time-dependent covariate and the researcher wants a Kaplan-Meier curve. Is that ok? How would you interpret it?

Instead, consider using landmark analysis. Consider a point in time (e.g., $1\ \text{year}$) and use the covariate status as it was known at $1\ \text{year}$. Start follow-up at that time point.



Common Mistake: Prophetic variables

Some time-dependent covariates are not predictors of an event as much as they are markers of a failure-in-progress:

- Multiple-organ failure
- Ventilation
- "Called the priest"
- Medication changes
 - Cessation of diuretics in heart failure
- PSA and prostate cancer, if measurement and declaration occur on the same visit

These will tend to be phenomenal predictors.

So what?



Evaluate Time delay

- ► For any dataset containing constructed time-dependent covariates, it is a good idea to re-run the analyses after adding a 7-14 day lag to key variables.
- When the results show a substantial change, understand why this occurred.



Common Mistake: Insidious look-ahead

Smoothed continuous variables:

- A particular lab test has values of
 - ▶ 120 on day 0
 - ▶ 150 on day 90
 - ▶ 180 on day 120
- What should we use for the value at day 100?
- It is tempting to use 160 (1/3 of the way between 150 and 180).
- ► Bad idea!



Common Mistake: Insidious look-ahead

Persistence:

- Patients with a solitary plasmacytoma are treated with local radiation
- The tumor produces an immunoglobulin spike
- ▶ If the spike is still present at the 1 year evaluation, this is a bad thing. (It mean that the 'solitary' lesion likely was not solitary.)
- Want to draw a curve for "survival, post 1 year".
- ▶ Does the patient evaluated at 13 months (with persistence) go in the 'persistent spike' or 'other' group?
- ▶ We know that the spike would have been present at 12 months, if the test had been done then.
- Still, it's a bad idea.

MAYO

Common Mistake: Summaries by event status

Subjects with censored follow-up end up in the non-event category.

- Covariate summaries by event/non-event
- Standard ROC curves

Think about re-distribute to the right



Common Mistake: Using Future Data

"You can't use future information today"

- ▶ Mark an adverse event as midway between visits
- Delete subjects who do not complete treatment



Common Mistake: Immortal Time Bias

- "Last clinical FU" versus "last FU by any means"
 - Fractures can only be detected via clinical follow-up, but we have more knowledge about whether they are alive or dead.
- ➤ Subjects were recruited based on diagnosis at a tertiary care center, but we are interested in follow-up based on when the symptoms 1st appeared. Patients have to live long enough to be included in the study so use left-truncation.



Common Mistake: Electronic Studies

With electronic studies, it is easy to mess up.

One rule used for counting a diagnosis of a chronic condition is that there are "at least 2 instances, 30 days apart". Then an error is made, using the date of the first diagnostic code.



Basics Start/Stop Data Check data/Common Mistakes Multistate Data

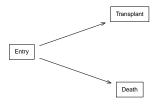
Multistate Data

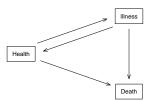


Multistate Scenarios











Monoclonal Gammopathy of Undetermined Significance (MGUS)

- Subjects with a dominant clone in their plasma cell population, but without malignancy ($\geq 2\%$ of plasma cells in the clone).
- Normally found incidentally to other tests.
- Should the patient be worried?
- ▶ About 1% per year convert to overt malignancy.
- Essentially independent of age and sex.



Example: Progression of MGUS

- ▶ 1384 subjects with monoclonal gammopathy of undetermined significance (MGUS)
- R. Kyle, New Engl J Med 346:564-569 (2002)
- Questions
 - Pattern of death and progression
 - Relationship to age, sex, hemoglobin, creatinine, and amount of protein in the "spike"



Example: MGUS data

The mgus2 dataset has two sets of variables that we are interested in. Time and event variables for:

- Progression (i.e., PCM): ptime and pstat.
- Death: futime and death.

```
id age sex dxyr hgb ptime pstat futime death
1379
     73
          M 1994 15.6
                         48
                                      48
1380
     69
          M 1994 15.0
                         22
                                      22
                         35
                                      35
1381 78
          M 1994 14.1
1382
     66
          M 1994 12.1
                         31
                                      31
1383 82
          F 1994 11.5
                         38
                                      61
                          6
1384
     79
          M 1994 9.6
                                0
                                       6
```

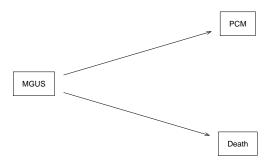


Create a Diagram - Competing Risk

```
> # Create names for the possible states
> states <- c("MGUS", "PCM", "Death")</pre>
> # Create matrix describing relationship between states
> connect <- matrix(0, nrow=3, ncol=3,</pre>
                   dimnames=list(states, states))
> # A non-zero element indicates that an arrow should be
> # drawn between state i (row) and state j (column)
> connect[1, c(2,3)] <- 1
> connect
      MGUS PCM Death
MGUS
         0 1
PCM 0 0
Death
```

MAYO

- > # Plot
- > statefig(layout=c(1,2), connect)





Example: MGUS - Competing Risk

Only need 1st event for each subject, so we only need 1 obs/person.

```
> # time variable will be follow-up time if there is no PCM,
> # and PCM time otherwise
> etime <- with(mgus2, ifelse(pstat==0, futime, ptime))
> # event variable will be 0 for censor or 2 for death
> # if there is no PCM, and 1 for PCM
> event <- with(mgus2, ifelse(pstat==0, 2*death, 1))
>
> # event variable must be a factor for multistate
> event <- factor(event, 0:2,
                 labels=c("censor", "pcm", "death"))
                                                             MAYO
```

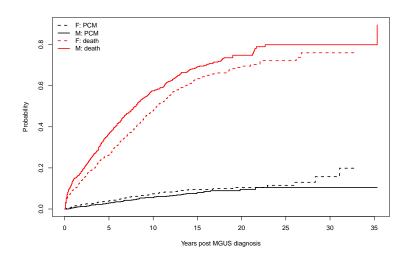
Basics Start/Stop Data Check data/Common Mistakes Multistate Data

- > # confirm coding makes sense
- > library(arsenal)
- > summary(freqlist(~ event+pstat+death, data=mgus2))

event	pstat	death	Freq	Cumulative Freq	Percent	Cumulative
censor	0	0	409	409	29.55	
pcm	1	0	12	421	0.87	
		1	103	524	7.44	
death	0	1	860	1384	62.14	









Double check the legend...

Pick a time on the x-axis and confirm results



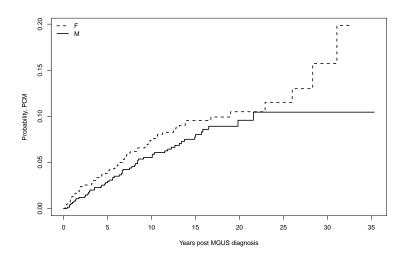
Subset to PCM event

```
> fit$states # columns
[1] "(s0)" "pcm" "death"
> fit$strata # rows
sex=F sex=M
227 227
```

▶ Do not plot this curve

```
> plot(fit, noplot="(s0)")
```







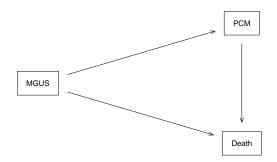
Example: MGUS data - Cox Model

► ID is required

```
> cfit <- coxph(Surv(etime, event) ~ sex, data=mgus2, id=id)</pre>
> cfit
Call:
coxph(formula = Surv(etime, event) ~ sex, data = mgus2, id = id)
1:2 coef exp(coef) se(coef) robust se z p
 sexM -0.05938 0.94235 0.18723 0.18733 -0.317 0.751
1:3 coef exp(coef) se(coef) robust se z
 sexM 0.22800 1.25608 0.06900 0.06869 3.319 0.000902
                                                       MAYO
                                                       CLINIC
States: 1=(s0), 2=pcm, 3=death
```

MGUS: Modify the Diagram

	MGUS	PCM	Death
MGUS	0	1	1
PCM	0	0	1
Death	0	0	0





Are there subjects where PCM and death occur at the same time?

	id	ptime	${\tt futime}$	pstat	death
1	190	101	101	1	1
2	383	147	147	1	1
3	619	81	81	1	1
4	780	39	39	1	1
5	1013	128	128	1	1
6	1037	16	16	1	1
7	1098	74	74	1	1
8	1104	8	8	1	1
9	1262	67	67	1	1



- ▶ What to do with 9 subjects who have PCM & death at the same time?
 - Cannot have a time of length 0, so push progression back by 0.1 month.





```
> attr(newdata, "tcount")
```

```
death 0 0 0 0 0 0 0 1384 0 pcm 0 0 0 115 0 0 1269
```





```
Call:
survcheck(formula = Surv(tstart, tstop, event) ~ sex, data = new
   id = id)
1384 subjects available for analysis
Transitions table:
        to
from   pcm death (censored)
```

from	pcm	${\tt death}$	(censored)
(s0)	115	860	409
pcm	0	103	12
death	0	0	0



Basics Start/Stop Data Check data/Common Mistakes Multistate Data



```
cfit <- coxph(Surv(tstart,tstop,event)~sex, data=newdata, id=i

Call:
coxph(formula = Surv(tstart, tstop, event) ~ sex, data = newdata
  id = id)</pre>
```

```
1:2 coef exp(coef) se(coef) robust se z p
sexM -0.05934 0.94238 0.18723 0.18733 -0.317 0.751
```

```
1:3 coef exp(coef) se(coef) robust se z p
sexM 0.22802 1.25610 0.06900 0.06869 3.32 0.000901
```



MAYO

2:3 coef exp(coef) se(coef) robust se z p sexM 0.02822 1.02862 0.20408 0.22429 0.126 0.9

NAFLD

- A. Allen, Non-alcoholic fatty liver disease incidence and impact on metabolic burden and death, a 20 year community study. Hepatology 2018, 67:1726–1736.
- ► The prevalence of non-alcoholic fatty liver disease (NASH) has risen to 24%.
- Now the most common cause of chronic liver disease.
- Diagnosed with abdominal MRI.
- ▶ NASH = NAFLD + inflammation requires biopsy for diagnosis.

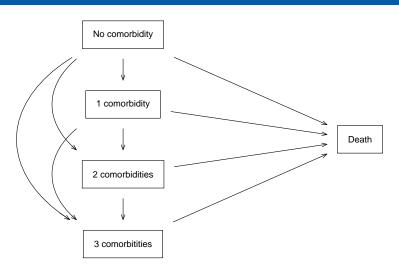


NAFLD Study

- All NAFLD diagnosis from 1997 to 2014 in Olmsted County, Minnesota.
- Utilize the Rochester Epidemiology Project
- One year delay.
- ▶ 4 controls matched on age and sex, then followed forward until the analysis date.
- ▶ 3864 cases of NAFLD and 14016 controls, 331 overlap.



NAFLD: Target





NAFLD: Data

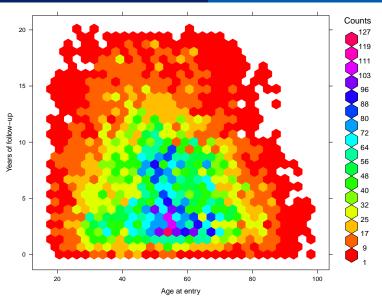
- nafld1: One observation per subject. Baseline covariates plus follow-up time and death.
- nafld2: Variables of id, days, test, and value. Contains selected tests and clinical observations.
- nafld3: Variables of id, days, and event type. One observation for each outcome: occurrence of NASH, hypertension, diabetes, etc.
- ► To anonymize patients, all dates have been replaced with "days since first enrollment".



NAFLD: Data

- Metabolic comorbidities are diabetes, hypertension, and dyslipidemia
- ► Focus on a model with 0, 1, 2, 3, of these + death
- ► The real work is in building and checking a dataset; the fits will be easy.







NAFLD: tmerge

```
> keep <- c("id", "age", "male", "bmi", "ntime")</pre>
> data1 <- tmerge(nafld1[, keep], nafld1, id,</pre>
                  death= event(futime. status))
> data1 <- tmerge(data1, subset(nafld3, event=="nafld"), id,</pre>
                  nafld = tdc(days))
> data1 <- tmerge(data1, subset(nafld3, event=="diabetes"), id,</pre>
                  diab= tdc(days), e1= event(days))
> data1 <- tmerge(data1, subset(nafld3, event=="htn"), id,</pre>
                  htn= tdc(days), e2= event(days))
> data1 <- tmerge(data1, subset(nafld3, event=="dyslipidemia"),</pre>
                  dyslip = tdc(days), e3= event(days))
```



Start/Stop Data Check data/Common Mistakes Multistate Data

> attr(data1, "tcount")

	early	late	gap	${\tt within}$	boundary	lead	trail	tied
death	0	0	0	0	0	0	17549	0
nafld	0	13	0	318	0	3533	0	0
diab	2393	0	0	1058	0	1	0	0
e1	2393	0	0	0	1058	1	0	0
htn	5022	0	0	2045	24	1	5	0
e2	5022	0	0	0	2069	1	5	0
dyslip	8663	0	0	1713	82	2	2	0
e3	8663	0	0	0	1795	2	2	0



NAFLD: Four row subject from data1

	id	age	tstart	tstop	nafld	htn	diab	dyslip	death
159	135	40	0	355	1	0	0	0	0
160	135	40	355	2133	1	0	0	1	0
161	135	40	2133	3220	1	1	0	1	0
162	135	40	3220	5269	1	1	1	1	0



Same subject, naf1d3

```
id days event
252 135 0 nafld
253 135 355 dyslipidemia
254 135 2133 htn
255 135 2343 sleep apnea
256 135 3220 diabetes
```



NAFLD: tmerge



```
> test <- tmerge(nafld1[, 1:2], nafld1, id,
               death = event(futime, status))
> test <- tmerge(test, subset(nafld3, event=="nafld"), id,
               nafld = tdc(days))
>
> attr(test, "tcount")
     early late gap within boundary leading trailing tied
death
         0 0
                                              17549
         0 13 0
                       318
nafld
                                      3533
                                                       0
> subset(test, id==135)
    id age tstart tstop death nafld
138 135 40
                0 5269
```

```
> test <- tmerge(nafld1[, 1:2], nafld1, id,</pre>
               death = event(futime, status))
> test <- tmerge(test, subset(nafld3, event=="nafld"), id,
               nafl = tdc(days))
> test <- tmerge(test, subset(nafld3, event=="diabetes"), id,
                diab= tdc(days), e1= event(days))
> attr(test, "tcount")
     early late gap within boundary leading trailing tied
                                              17549
death
         0 0
                         0
nafl
         0 13 0 318
                                   3533
diab 2393 0 0 1058
      2393 0
                              1058
e1
                         0
> subset(test, id==135)
                                                         MAYO
    id age tstart tstop death nafl diab e1
                                                         CLINIC
142 135 40
                0 3220
143 135 40 3220 5269
                                                       146 / 157
```

```
> test <- tmerge(test, subset(nafld3, event=="htn"), id,
                htn= tdc(days))
> attr(test, "tcount")
     early late gap within boundary leading trailing tied
death
                                              17549
              0
                                                       0
nafl
         0 13
                       318
                                       3533
diab
      2393
                  0 1058
e1
      2393
                         0
                               1058
                                                       0
                  0
htn
      5022
              0
                      2045
                                 24
                                                       0
>
> subset(test, id==135)
     id age tstart tstop death nafl diab e1 htn
155 135 40
                0 2133
156 135 40 2133 3220
                                                         CLINIC
157 135 40
             3220 5269
```

MAYO

```
> test <- tmerge(test, subset(nafld3, event=="dyslipidemia"), id
                 lip= tdc(days), e3= event(days))
> attr(test, "tcount")
      early late gap within boundary leading trailing tied
death
               0
                                                 17549
                                                          0
nafl
              13
                        318
                                         3533
diab
       2393
                   0
                       1058
                                                          0
e1
       2393
                                1058
htn
      5022
                       2045
                                  24
                                                          0
       8663
                   0
                       1713
lip
               0
                                  82
e3
       8663
               0
                          0
                                1795
                                                          0
> subset(test, id==135)
     id age tstart tstop death nafl diab e1 htn lip e3
                                                             MAYO
159 135
         40
                     355
                                                            CLINIC
160 135 40
               355 2133
161 135
         40 2133
                    3220
                                                           148 / 157
```

In any sufficiently large sample, any outrageous thing is likely to happen. P. Diaconis and Mosteller, Method of studying coincidences, JASA 1989.

- Someone will die on the same day as their diabetes diagnosis, have first NAFLD and first hypertension on the same day, or any number of other overlaps.
- ▶ Be prepared to think through these cases.



NAFLD: Last additions

- age1, age2: age at start and end of interval
- cstate: number of metabolic conditions so far
- endpoint: censor, 1mc, 2mc, 3mc, death

```
> data1$age1 <- with(data1, age + tstart/365.25)
```

- > data1\$age2 <- with(data1, age + tstop/365.25)</pre>
- > data1\$cstate <- with(data1, diab + htn + dyslip) # TD cov</pre>



NAFLD: Last additions

```
> tcount <- with(data1, e1 + e2 + e3)</pre>
> temp2 <- with(data1, ifelse(death, 4,
              ifelse(tcount ==0, 0, cstate + tcount)))
> data1$endpoint <- factor(temp2, 0:4,</pre>
         c("censored", "1mc", "2mc", "3mc", "death"))
> data1$cstate <- factor(data1$cstate, 0:3,</pre>
                c("Omc", "1mc", "2mc", "3mc"))
> with(data1, table(cstate, endpoint))
     endpoint
cstate censored 1mc 2mc 3mc death
  Omc
          5755 1829 70
                               263
   1mc 4650
                  0 1843 28 243
  2mc 3784 0 0 1048 417
                            0 441
  3mc
       2308
```

NAFLD: Check data

```
> survcheck(Surv(tstart, tstop, endpoint) ~ male + nafld, data=d
    id=id, istate=cstate)
```

```
Call:
```

```
survcheck(formula = Surv(age1, age2, endpoint) ~ male + nafld,
    data = data1, id = id, istate = cstate)
17549 subjects available for analysis
```

Transitions table:

	UU				
from	1mc	2mc	3mc	${\tt death}$	(censored)
Omc	1829	70	4	263	5705
1mc	0	1843	28	243	4567
2mc	0	0	1048	417	3687
3mc	0	0	0	441	2220
death	. 0	0	0	0	0



Basics Start/Stop Data Check data/Common Mistakes Multistate Data



NAFLD: Time scale

- ► Time since diagnosis
 - makes some sense for the NAFLD cases
 - Time since "your number was chosen out of a hat" for the controls?
 - Age and sex need to be in the model, and the model for them needs to be correct
 - ► The population death rate ranges from .03–500 /1000 over this age span; a small lack of fit in the age*sex modeling can dominate all other covariates.
- Age as a time scale:
 - ► Compares like with like. We can also stratify on sex if desired.
 - Age is not a covariate
- ► Time since index + case-control matching compares each subject to others of the same age and sex.



NAFLD: Models

```
> nfit1 <- coxph(Surv(age1, age2, death) ~ male + nafld,
                data=data1)
> nfit2 <- coxph(Surv(age1, age2, death) ~ male + nafld +
                     as.numeric(cstate),
                data=data1)
> nfit3 <- coxph(Surv(age1, age2, death) ~ male +
                    strata(cstate)/nafld, data= data1)
> nfit4a <- coxph(Surv(age1, age2, endpoint %in% c("1mc", "2mc",</pre>
                        strata(male) + nafld,
                data=data1, subset= (cstate=="Omc"))
> nfit4b <- coxph(Surv(age1, age2, endpoint %in% c("2mc", "3mc")</pre>
                      strata(male) + nafld,
                data=data1, subset= (cstate== "1mc"))
> nfit4c <- coxph(Surv(age1, age2, endpoint=="3mc") ~</pre>
                                                              MAYO
                      strata(male) + nafld,
                                                              CLINIC
                data=data1, subset= (cstate=="2mc"))
```

NAFLD: Aalen-Johansen curves



