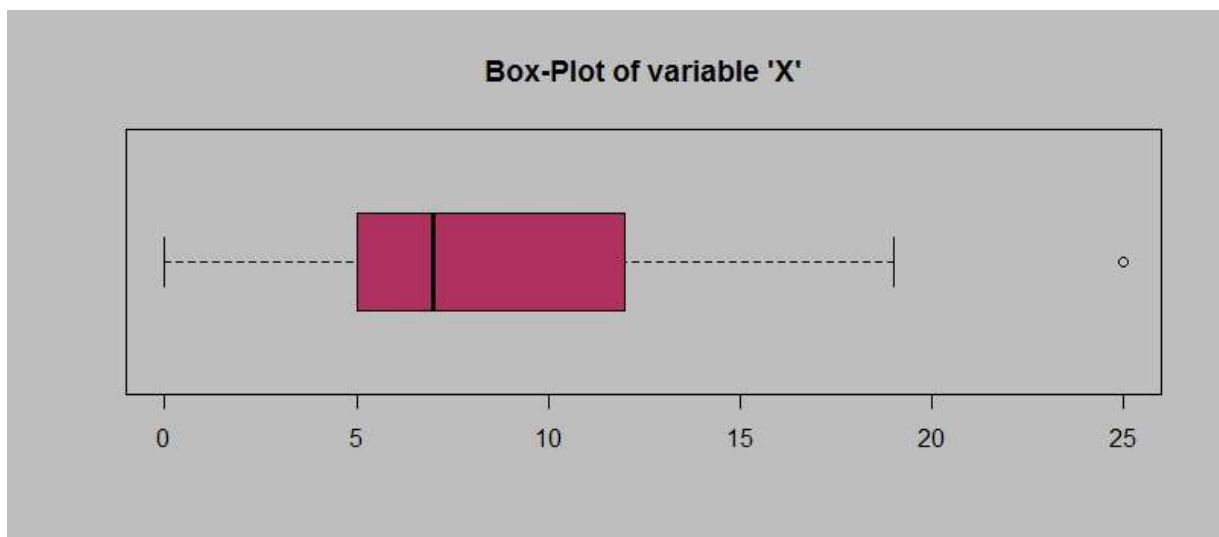


## Topics: Descriptive Statistics and Probability

1. Look at the data given below. Plot the data, find the outliers and find out  $\mu, \sigma, \sigma^2$

Name of company	Measure X
Allied Signal	24.23%
Bankers Trust	25.53%
General Mills	25.41%
ITT Industries	24.14%
J.P.Morgan & Co.	29.62%
Lehman Brothers	28.25%
Marriott	25.81%
MCI	24.39%
Merrill Lynch	40.26%
Microsoft	32.95%
Morgan Stanley	91.36%
Sun Microsystems	25.99%
Travelers	39.42%
US Airways	26.71%
Warner-Lambert	35.00%

2.



Answer the following three questions based on the box-plot above.

- (i) What is inter-quartile range of this dataset? (please approximate the numbers) In one line, explain what this value implies.

**Ans: Approximately**

**Q1=5**

**Q3=12**

**Q2=7**

$$\text{IQR} = Q3 - Q1 = 7$$

**IQR is the median value**

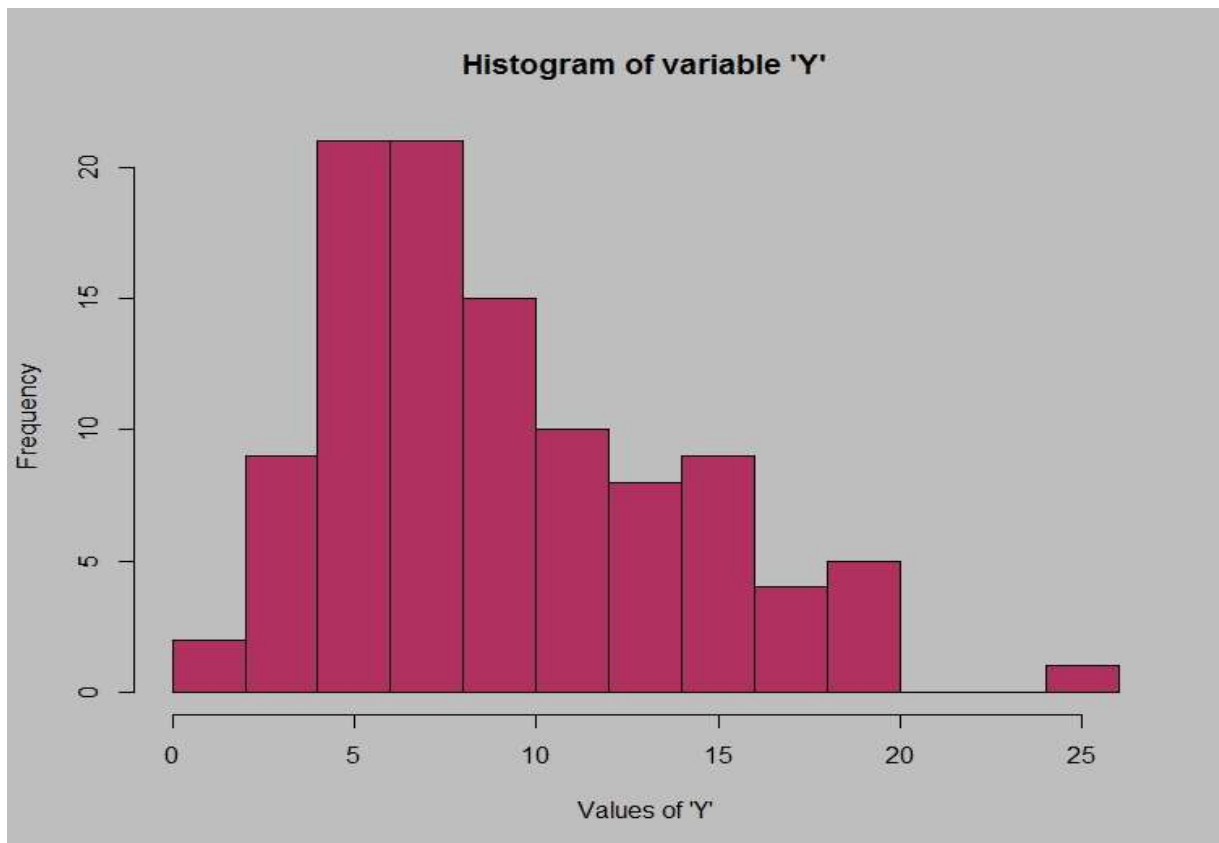
- (ii) What can we say about the skewness of this dataset?

**Ans: It is positively skewed. Hence we can say it is Right Skewness**

- (iii) If it was found that the data point with the value 25 is actually 2.5, how would the new box-plot be affected?

**Ans: In this case there will be no outliers as the outlier lies on 25. Then it will become normal distribution rather than right skewed distribution.**

3.



Answer the following three questions based on the histogram above.

- (i) Where would the mode of this dataset lie?

**Ans: The mode lies between 4 to 8 approximately**

- (ii) Comment on the skewness of the dataset.

**Ans: Right-Skewed; mean > median > mode**

- (iii) Suppose that the above histogram and the box-plot in question 2 are plotted for the same dataset. Explain how these graphs complement each other in providing information about any dataset.

**Ans: They both are right-skewed and both have outliers. The median can be easily visualized in box plot whereas in histogram mode is more visible.**

4. AT&T was running commercials in 1990 aimed at luring back customers who had switched to one of the other long-distance phone service providers. One such commercial shows a businessman trying to reach Phoenix and mistakenly getting Fiji, where a half-naked native on a beach responds incomprehensibly in Polynesian. When asked about this advertisement, AT&T admitted that the portrayed incident did not actually take place but added that this was an enactment of something that "could happen." Suppose that one in 200 long-distance telephone calls is misdirected. What is the probability that at least one in five attempted telephone calls reaches the wrong number? (Assume independence of attempts.)

**Ans: The probability for at least one in five attempted telephone calls reaches the wrong number**

**Number of Calls = 5**

**$n = 5$**

**$p = 1/200$**

**$q = 199/200$**

**$P(x)$  = at least one in five attempted telephone calls reaches the wrong number**

**$P(x) = {}^nC_x p^x q^{n-x}$**

**$P(x) = ({}^nC_x) (p^x) (q^{n-x})$**

**$nCr = n! / r! * (n - r)!$**

**$P(1) = ({}^5C_1) (1/200)^1 (199/200)^{5-1} P(1) = 0.0245037$**

5. Returns on a certain business venture, to the nearest \$1,000, are known to follow the following probability distribution

x	P(x)
-2,000	0.1
-1,000	0.1
0	0.2
1000	0.2
2000	0.3
3000	0.1

- (i) What is the most likely monetary outcome of the business venture?

**Ans: 2000 is the most likely monetary outcome of the business venture**

- (ii) Is the venture likely to be successful? Explain

**Ans: income =  $\sum(p(x) * x)$**

**$-200-100+0+200+600+300=800$**

**Yes, it will be successful as it has positive value in total**

**$p(x>0)+p(x>1000)+p(x>2000)+p(x=3000) = 0.2+0.2+0.3+0.1 = 0.8$  this states that there is a good 80% chance for this venture to be making a profit**

- (iii) What is the long-term average earning of business ventures of this kind? Explain

**Ans: +800 is the long-term average earning of business ventures of this kind because in summation we are getting a positive value**

- (iv) What is the good measure of the risk involved in a venture of this kind? Compute this measure

**Good measure of risk is standard deviation**

**$E(X) = \sum X \cdot P(X)$**

$$E(X^2) = \sum X^2 \cdot P(X)$$

$$\text{Var}(X) = E(X^2) - \{E(X)\}^2$$

$$\text{SD} = \text{squareroot}(\text{Var})$$

$$\text{Var}(X) = E(X^2) - \{E(X)\}^2$$

$$= 2800000 - 800^2$$

$$= 2160000 \text{ (Quite High)}$$

$$\text{SD} = \text{squareroot}(\text{Var}) \approx \$ 1470$$

As Variability is Quite high hence Risk is high