Database Management Systems

Lecture 6
Evaluating Relational Operators
Query Optimization

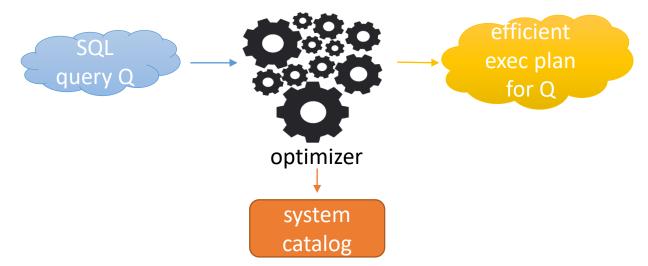
- * queries composed of <u>relational operators</u>:
- selection (σ)
 - selects a subset of records from a relation
- projection (π)
 - eliminates certain columns from a relation
- join (⊗)
 - combines data from two relations
- cross-product (R1 \times R2)
 - returns every record in R1 concatenated with every record in R2
- set-difference (R1 R2)
 - returns records that belong to R1 and don't belong to R2
- union (R1 ∪ R2)
 - returns all records in relations R1 and R2

^{*}Review lecture notes on *Relational Algebra* (*Databases* course)

- * queries composed of <u>relational operators</u>:
- intersection (R1 ∩ R2)
 - returns records that belong to both R1 and R2
- grouping and aggregate operators (algebra extensions)
- every operation returns a relation => operations can be composed
- an operator can have several implementation algorithms

* optimizer

- input: SQL query Q
- output: an efficient execution plan for evaluating Q



- * algorithms for operators based on 3 techniques:
- <u>iteration</u>:
 - examine iteratively:
 - all tuples in input relations

or

- data entries in indexes, provided they contain all the necessary fields (data entries are smaller than data records)
- <u>indexing</u>:
 - used when the query contains a selection condition or a join condition
 - examine only the tuples that meet the condition, using an index
- partitioning:
 - partition the tuples
 - decompose operation into collection of cheaper operations on partitions
 - partitioning techniques: sorting, hashing

- * access paths
- access path = way of retrieving tuples from a relation
 - file scan

or

- an index I + a matching selection condition C
- condition C matches index I if I can be used to retrieve just the tuples satisfying C
- if relation R has an index I that matches selection condition C, then there
 are at least 2 access paths for R (file scan; index)

*Review lecture notes on *Indexes* (*Databases* course)

- * access paths example:
- relation Students[SID, Name, City]
- I tree index on Students with search key <Name>
- query Q: SELECT * FROM Students

WHERE Name = 'lonescu'

- condition C: Name = 'lonescu'
- C matches I, i.e., index I can be used to retrieve only the Students tuples satisfying C
- the following condition also matches the index: Name > 'lonescu'

- * access paths example:
- relation Students[SID, Name, City]
- I hash index on Students with search key <Name>
- query Q:
 SELECT *
 FROM Students
 WHERE Name = 'Ionescu'
- condition C: Name = 'lonescu'
- C matches I, i.e., index I can be used to retrieve only the Students tuples satisfying C
- condition Name > 'lonescu' doesn't match I (since I is a hash index; it cannot be used to retrieve just the tuples satisfying Name > 'lonescu')

- * access paths
- to sum up:
 - condition *C*: attr op value, op $\in \{<, <=, =, <>, >=, >\}$
 - condition C matches index I if:
 - the search key of *I* is *attr* and:
 - I is a tree index or
 - I is a hash index and op is =

- * access paths
- index *I*, selection condition *C*
- / hash index
- condition C of the form:
 - $\bigwedge_{i=1}^n T_i$
 - term T_i : attr = value
- I matches C if C has one term for each attribute in the search key of I

Condition	Hash index with search key <a, b,="" c=""></a,>
a = 10 AND b = 5 AND c = 2	Yes
a = 10 AND b = 5	No
b = 5	No
b = 5 AND c = 2	No

- * access paths
- index I, selection condition C
- *I* tree index
- condition C of the form:
 - $\bigwedge_{i=1}^n T_i$
 - term T_i : attr op value; op $\in \{<, <=, =, <>, >=, >\}$
- I matches C if C has one term for each attribute in a prefix of the search key
 of I

Condition	B+ tree index with search key <a, b,="" c=""></a,>
a = 10 AND b = 5 AND c = 2	Yes
a = 10 AND b = 5	Yes
b = 5	No
b = 5 AND c = 2	No

- * access paths
- <u>selectivity</u> of an access path
 - the number of retrieved pages when using the access path to obtain the desired tuples
 - both data pages and index pages are counted
- example:

SELECT *

FROM Students

WHERE Name = 'lonescu'

- access paths:
 - file scan selectivity could be 1000
 - matching index I with search key <Name> selectivity could be 3
- most selective access path
 - retrieves the fewest pages, i.e., data retrieval cost is minimized

- * general selection conditions
- in general, a selection condition can contain one or several terms of the form:
 - attr op constant
 - attr1 op attr2,
 combined with ∧ and ∨

```
SELECT *
FROM Exams
WHERE SID = 7 AND EDate = '04-01-2021'
\sigma_{SID=7 \; \land \; EDate='04-01-2021'}(Exams)
```

- * general selection conditions
- process a selection operation with a general selection condition
 C -> express C in CNF (conjunctive normal form)
- condition in CNF:
 - collection of conjuncts connected with the ∧ operator
 - a conjunct has one or more terms connected with the V operator
 - *term*:
 - attr op constant
 - attr1 op attr2
- example:

```
condition (EDate < '4-1-2021' \land Grade = 10 ) \lor CID = 5 \lor SID = 3 is rewritten in CNF:
```

$$(EDate < '4-1-2021' \ V CID = 5 \ V SID = 3) \ \land (Grade = 10 \ V CID = 5 \ V SID = 3)$$

- * general selection conditions matching an index
- relation R[a, b, c, d, e], index I with search key <a, b, c>

Condition	B+ tree index	Hash index
a = 10 AND b = 5 AND c = 2	Yes	Yes
a = 10 AND b = 5	Yes	No
b = 5	No	No
b = 5 AND c = 2	No	No
d = 2	No	No
a = 20 AND b = 10 AND c = 5 AND d = 11	Partly	Partly

Condition – CNF selection condition

B+ tree index / Hash index – B+ tree / hash index I matches (Yes) / doesn't match (No) / matches a part of (Partly) the selection condition

- for the condition in the last row (a = 20 AND b = 10 AND c = 5 AND d = 11):
 - use index I to retrieve tuples satisfying a = 20 AND b = 10 AND c = 5, then apply d = 11 to each retrieved tuple

- * general selection conditions matching an index
- relation R[a, b, c, d]
- index I1 with search key <a, b>
- B+ tree index I2 with search key <c>

Condition	Indexes
c < 100 AND a = 3 AND b = 5	 use I1 or I2 to retrieve tuples then check terms in the selection condition that do not match the index for each retrieved tuple e.g., use the B+ tree index to retrieve tuples where c < 100; then apply a = 3 AND b = 5 to each retrieved tuple

- * running example schema
- Students (SID: integer, SName: string, Age: integer)
- Courses (CID: integer, CName: string, Description: string)
- Exams (SID: integer, CID: integer, EDate: date, Grade: integer, FacultyMember: string)
- Students
 - every record has 50 bytes
 - there are 80 records / page
 - 500 pages of Students tuples
- Courses
 - every record has 50 bytes
 - there are 80 records / page
 - 100 pages of Courses tuples

- Exams
 - every record has 40 bytes
 - there are 100 records / page
 - 1000 pages of Exams tuples

* joins

SELECT *

FROM Exams E, Students S

WHERE E.SID = S.SID

- algebra: $E \bigotimes_{E.SID=S.SID} S$
 - to be carefully optimized
 - size of E × S is large, so computing E × S followed by selection is inefficient
- E
 - M pages
 - p_F records / page
- 5
 - N pages
 - p_s records / page
- evaluation: number of I/O operations

- * joins implementation techniques
 - iteration
 - Simple/Page-Oriented Nested Loops Join
 - Block Nested Loops Join
 - indexing
 - Index Nested Loops Join
 - partitioning
 - Sort-Merge Join
 - Hash Join
- equality join, one join column
 - join condition: $E_i = S_j$

Simple Nested Loops Join

```
foreach tuple e \in E do foreach tuple s \in S do if e_i == s_j then add \langle e_i \rangle s > to the result
```

- for each record in the outer relation E, scan the entire inner relation S
- <u>cost</u>
 - $M + p_E^* M * N = 1000 + 100*1000*500 I/Os = 1000 + (5 * 10^7) I/Os$
 - M I/Os cost of scanning E
 - N I/Os cost of scanning S
 - S is scanned p_E^* M times (there are p_E^* M records in the outer relation E)
- * E M pages, p_F records / page * * 1000 pages * * 100 records / page*
- * S N pages, p_S records / page * * 500 pages * * 80 records / page * Sabina S. CS

Page-Oriented Nested Loops Join

```
foreach page pe \in E do foreach page ps \in S do if e_i == s_i then add <e, s> to the result
```

- for each page in E read each page in S
- pairs of records <e, s> that meet the join condition are added to the result (where record e is on page pe, and record s – on page ps)
- refinement of Simple Nested Loops Join

Page-Oriented Nested Loops Join

```
foreach page pe \in E do foreach page ps \in S do if e_i == s_i then add <e, s> to the result
```

- <u>cost</u>
 - M + M*N = 1000 + 1000*500 I/Os = 501.000 I/Os
 - M I/Os cost of scanning E; N I/Os cost of scanning S
 - S is scanned M times
 - significantly lower than the cost of Simple Nested Loops Join (improvement factor of p_F)
 - if the smaller table (S) is chosen as outer table:

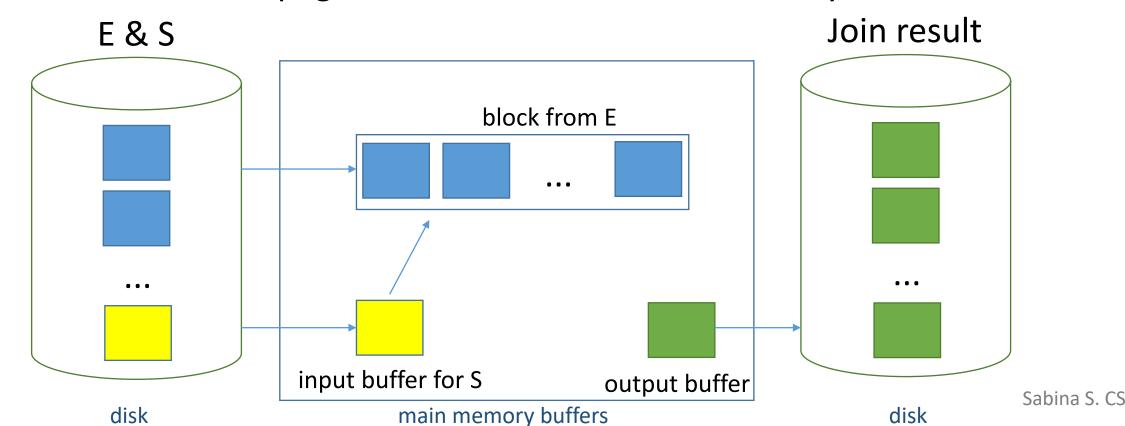
```
=> cost = 500 + 500 * 1000 I/Os = 500.500 I/Os
```

- * E M pages, p_E records / page * * 1000 pages * * 100 records / page*
- * S N pages, p_S records / page * * 500 pages * * 80 records / page * Sabina S. CS

- previously presented join algorithms do not use buffer pages effectively
- join relations R1 and R2; R1 the smaller relation
- assumption the smaller relation fits in main memory
- <u>improvement</u>:
 - store smaller relation R1 in memory
 - keep at least 2 extra buffer pages B1 and B2
 - use B1 to read the larger relation R2 (one page at a time)
 - use B2 as the output buffer (i.e., for tuples in the result of the join)
 - for each tuple in R2, search R1 for matching tuples
 - => optimal cost: *number of pages in R1 + number of pages in R2*, since R1 is scanned only once, R2 is also scanned only once

- <u>refinement</u>
 - don't store the smaller relation in main memory as is, build an in-memory hash table for it instead
 - the I/O cost remains unchanged, but the CPU cost is usually much lower (since for each tuple in the larger relation, the smaller relation is examined to find matching tuples)

- if there isn't enough main memory to hold one of the input relations:
 - use one buffer page to scan the inner table (e.g., S)
 - use one page for the result
 - use all remaining pages to read a block from the outer table (e.g., E)
 - block set of pages from E that fit in main memory

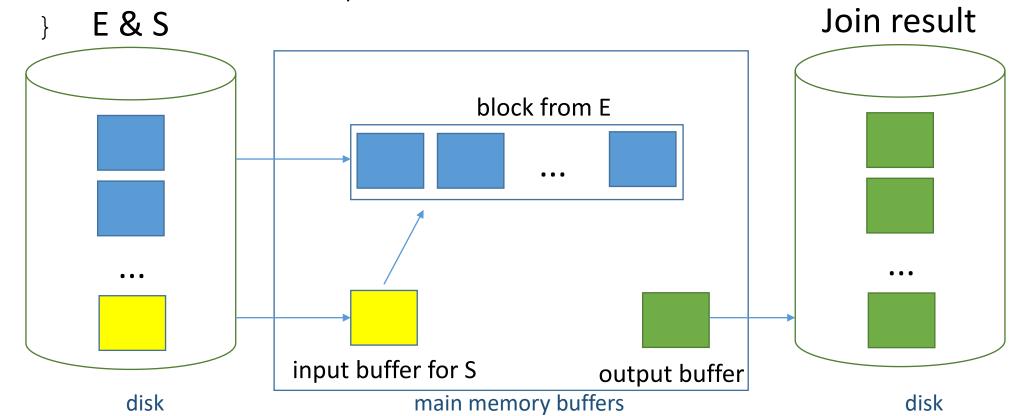


```
foreach block be E E do
   foreach page ps ∈ S do • outer relation E is scanned once
```

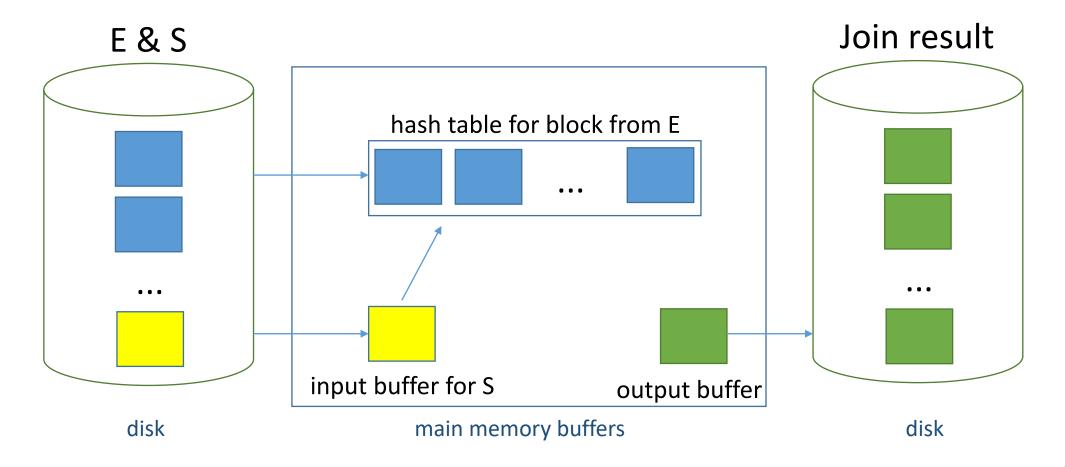
 inner relation S is scanned once for each block in outer relation E

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for all pairs of tuples <e, s> that meet the join condition, where $e \in be$ and $s \in ps$, add <e, s> to the result



- refinement to efficiently find matching tuples
 - build main-memory hash table for the block of E
 - trade-off: reduce size of E block



- <u>cost</u>
 - scan of outer table + number of blocks in outer table * scan of inner table
 - number of outer blocks = $\frac{\text{number of pages in outer table}}{\text{size of block}}$
 - outer table: Exams (E), a block can hold 100 pages
 - scan cost for E: 1000 I/Os
 - number of blocks: $\left[\frac{1000}{100}\right] = 10$
 - foreach block in E, scan Students (S): 10*500 I/Os
 - => total cost = 1000 + 10 * 500 = **6000 I/Os**

- cost
 - scan of outer table + number of blocks in outer table * scan of inner table
 - number of outer blocks = $\frac{\text{number of pages in outer table}}{\text{size of block}}$
 - outer table: Exams (E)
 - suppose the buffer has 90 pages available for E, i.e., block of 90 pages

=> number of blocks:
$$\left[\frac{1000}{90}\right] = 12$$

- => S is scanned 12 times
- scan cost for E: 1000 I/Os
- foreach block in E, scan Students (S): 12*500 I/Os
- => total cost = 1000 + 12 * 500 = **7000 I/Os**

- <u>cost</u>
 - scan of outer table + number of blocks in outer table * scan of inner table
 - number of outer blocks = $\frac{\text{number of pages in outer table}}{\text{size of block}}$
 - outer table: Students (S), block of 100 pages
 - scan cost for S: 500 I/Os
 - number of blocks: $\left[\frac{500}{100}\right] = 5$
 - for each block in S, scan E: 5 * 1000 I/Os
 - => total cost = 500 + 5 * 1000 = **5500 I/Os**

Index Nested Loops Join

```
foreach tuple e in E do foreach tuple s in S where e_i == s_j add \langle e_i, s \rangle to the result
```

- if there is an index on the join column of S, S can be considered as inner table and the index can be used
- <u>cost</u>
 - M + ((M*p_F) * cost of finding corresponding records in S)

```
* E - M pages, p<sub>E</sub> records / page * * 1000 pages * * 100 records / page*

* S - N pages, p<sub>S</sub> records / page * * 500 pages * * 80 records / page *

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```

Index Nested Loops Join

- for a record e in E:
 - the <u>cost</u> of <u>examining</u> the <u>index</u> on S is:
 - approx. 1.2 for a hash index (typical cost for hash indexes)
 - typically 2-4 for a B+-tree index
 - the <u>cost</u> of <u>reading</u> corresponding <u>records</u> in S:
 - for a clustered index:
 - plus one I/O for each outer tuple in E (typically)
 - for an unclustered index:
 - up to one I/O for each corresponding record in S
 (worst case there are n matching records in S located on n different pages!)

Index Nested Loops Join

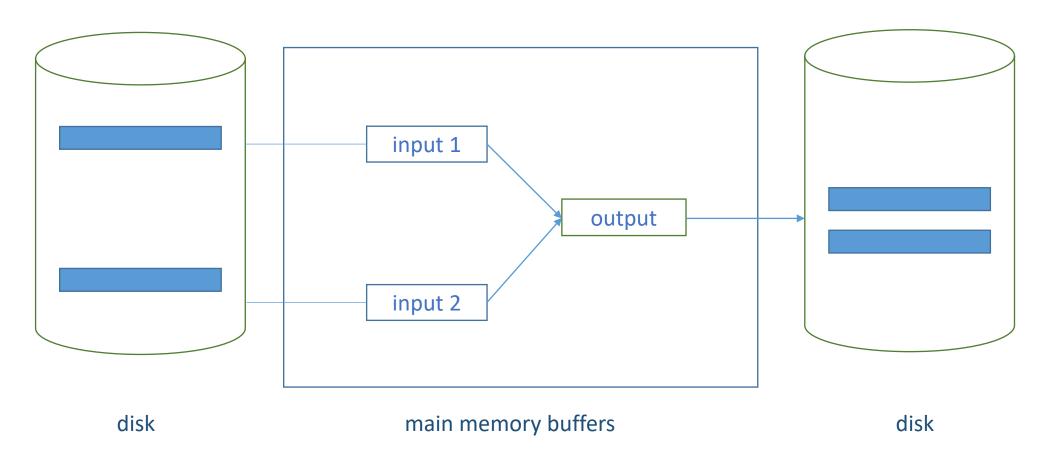
- hash index on SID in Students (Students inner table)
- scan Exams:
 - cost = 1000 I/Os, with a total of 100*1000 records
- for each record in Exams:
 - (on average) 1.2 I/Os to obtain the page in the hash index (i.e., the page containing the rid of the matching Students tuple)
 and
 - 1 I/O to retrieve the page in Students that contains the matching tuple (exactly one! since SID is a key in Students, i.e., there is one matching Students tuple for an exam)
- => cost to retrieve matching Students tuples: 1000 * 100 * (1.2 + 1) = 220.000
- total cost: 1000 + 220.000 = 221.000 I/Os
- * E M pages, p_F records / page * * 1000 pages * * 100 records / page*
- * S N pages, p_S records / page * * 500 pages * * 80 records / page * Sabina S. CS

* sorting

- can be explicitly required (SELECT ... ORDER BY list), used to eliminate duplicates (SELECT DISTINCT), used by operators like:
 - join
 - union
 - intersection
 - set-difference
 - grouping

- * sorting
- e.g., the user wants to sort the collection of Courses records by name
- if the data to be sorted fits into available main memory:
 - use an <u>internal sorting</u> algorithm (Quick Sort or any other in-memory sorting algorithm can be used to sort a collection of records that fits into main memory)
- if the data to be sorted doesn't fit into available main memory:
 - use an <u>external sorting</u> algorithm
 - minimizes the cost of accessing the disk
 - breaks the data collection into subcollections of records
 - sorts the subcollections; a sorted subcollection of records is called a run
 - writes runs to disk
 - merges runs

- uses 3 buffer pages
- passes over the data multiple times
- can sort large data collections using a small amount of main memory

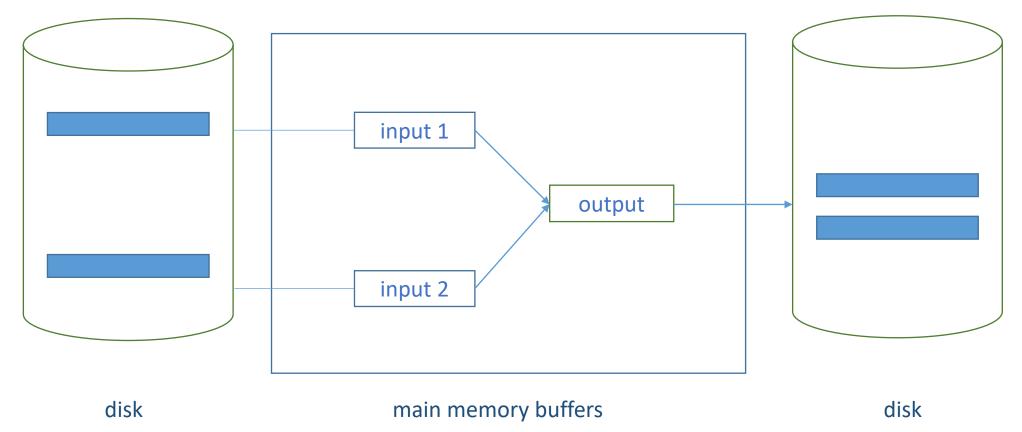


- pass 0:
 - for each page P in the data collection:
 - read in page P -> sort page P -> save page P to disk
 - => 1-page runs (runs that are 1 page long) example: read in the 1st page from Courses, sort the 80 records on it by course name, write out the sorted page to disk (i.e., a *run* that is one page long);
 - read in the 2nd page from Courses, sort the 80 records on it by course name, write out sorted page to disk;

• • •

- read in the 100th page from Courses, sort the 80 records on it by course name, write out sorted page to disk
- => 100 1-page runs saved on disk

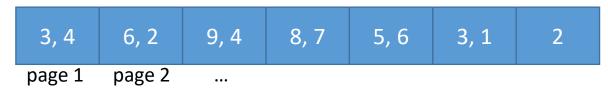
- pass 1, 2, ... etc.:
 - use 3 buffer pages
 - read and merge pairs of runs from the previous pass
 - produce runs that are twice as long



- e.g., pass 1 (pass 0 produced 100 1-page runs):
 - read in 2 runs from pass 0 (i.e., two pages holding Courses records, each of them sorted in pass 0), using 2 buffer pages
 - merge these runs writing to the 3rd available buffer page (the *output* buffer); when the output buffer fills up, write it out to disk (i.e., write a page of 80 sorted records to disk)
 - => a run that is 2 pages long (it contains 160 Courses records, sorted by name)
 - read in and merge the next 2 runs from pass 0 ... => another run that is
 2 pages long
 - continue while there are runs to be processed (read in and merged)
 from pass 0
 - at the end of pass 1 there are 50 2-page runs (each run consists of 2 pages holding 160 records sorted by course name)

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another example – sort data collection (file of records) with 7 pages:



- only the value of the key is displayed (the key on which the user wants to sort the collection, an integer number in the example)
- simplifying assumption that allows us to focus on the idea of the algorithm:
 a page can hold 2 records
- pass 0
 - read in the collection one page at a time
 - sort each page that is read in
 - write out each sorted page to disk
 - => 7 sorted runs that are 1 page long:

3, 4

2, 6

4, 9

7, 8

5, 6

1, 3

2

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runs at the end of pass 0:

3, 4

2, 6

4, 9

7,8

5, 6

1, 3

2

pass 1

- read in & merge pairs of runs from pass 0
- produce runs that are twice as long
- read in runs3,4 and2,6
 - merge the runs and write to the output buffer
 - write the output buffer to disk one page at a time
 - => run 2, 3 4, 6
- read in runs 4,9 and 7,8:

8,9

- merge the runs and write to the output buffer
- write the output buffer to disk one page at a time

=> run 4,7

runs at the end of pass 0:

3, 4

2, 6

4, 9

7, 8

5, 6

1, 3

pass 1

• read in runs 5,6 and 1,3 ...

=> run 1,3 5,6

• read in run 2 (the last run from pass 0) ...

=> run 2

=> 4 sorted runs that are 2 pages long (except for the last run):

2, 3 4, 6

4, 7 8, 9

1, 3

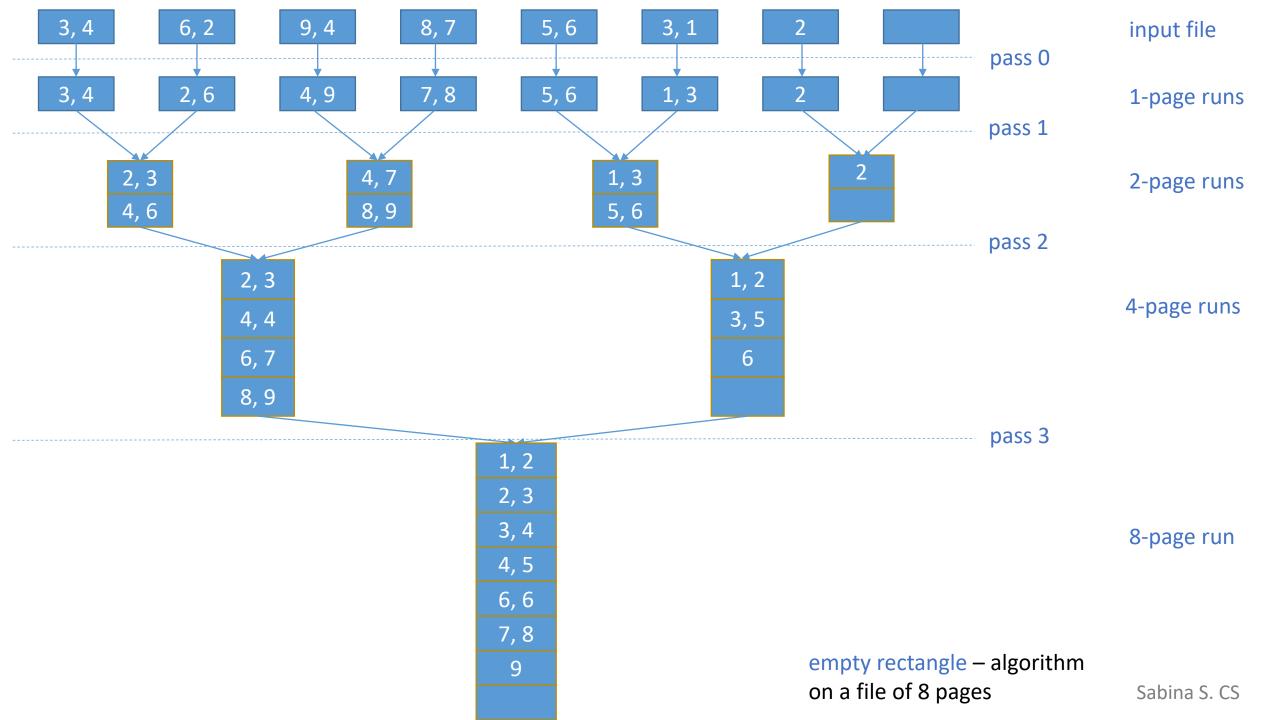
5, 6

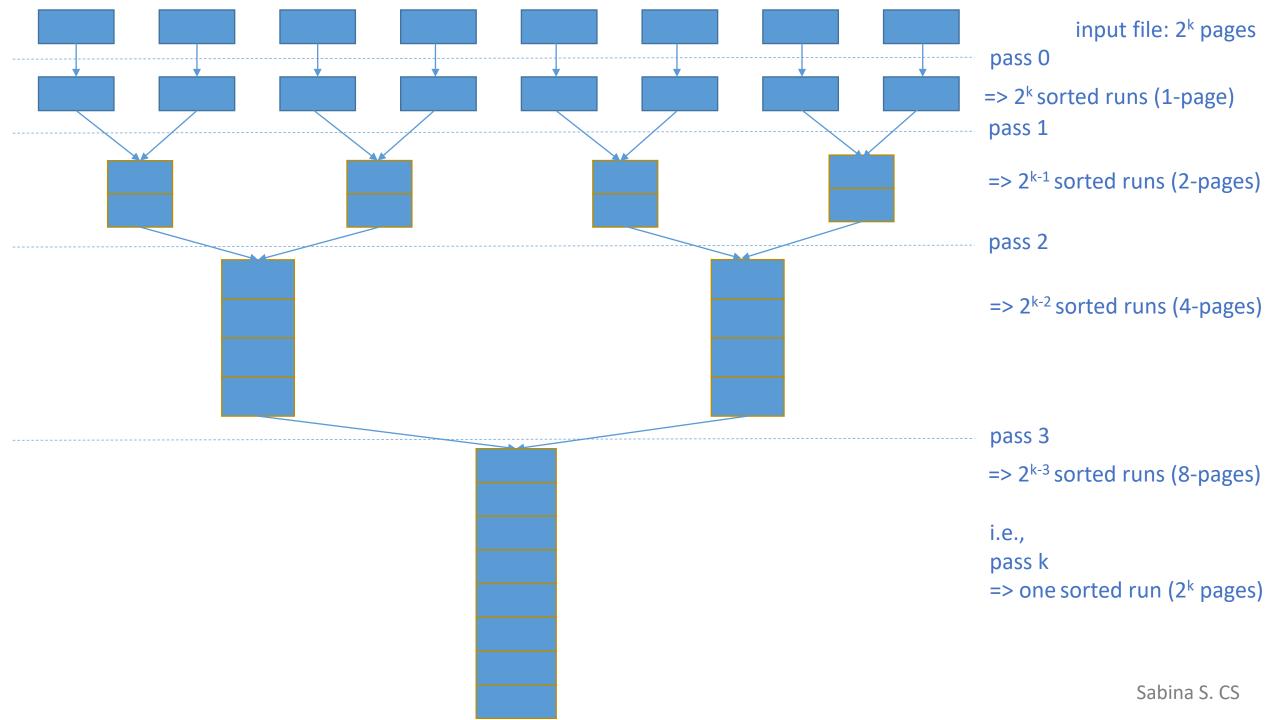
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- pass 2
 - read in & merge pairs of runs from pass 1
 - produce runs that are twice as long

• • •

complete example, with all passes of the algorithm, on the next page ->

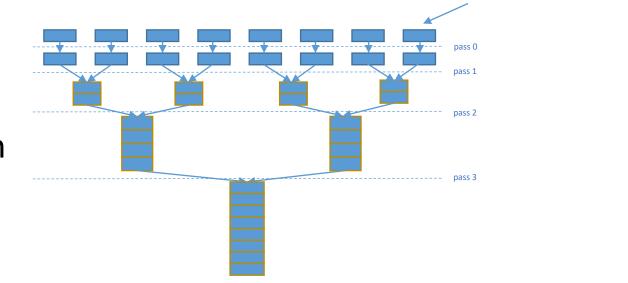




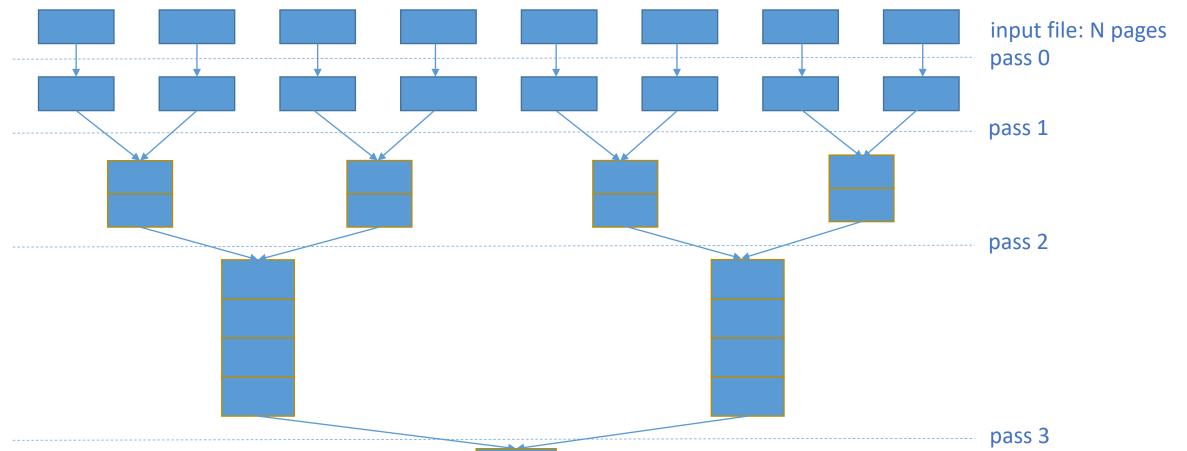
• in each pass, each page in the input file is: read in, processed, and written out; there are 2 I/O operations per page, per pass

input file: N pages

- number of passes:
 - $\lceil log_2 N \rceil + 1$ where N is the number of pages in the file to be sorted



- total cost:
 - 2 * number of pages * number of passes
 - 2 * N * ($[log_2N] + 1$) I/Os



- in each pass: read / process / write each page in the file
- number of passes:
 - $[log_2N] + 1$
- total cost:
 - $2 * N * ([log_2N] + 1) I/Os$

• there are N = 8 pages, 4 passes

•
$$2 * 8 * ([log_2 8] + 1) = 2 * 8 * 4 = 64 I/Os$$

•
$$2 * 7 * (\lceil \log_2 7 \rceil + 1) = 56 \text{ I/Os}$$

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