CUNY SPS DATA 621 - CTG5 - HW3

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Contents

Table 1: Data Dictionary

VARIABLE	DEFINITION	TYPE
target	whether the crime rate is above the median crime rate (1) or not (0)	response
zn	proportion of residential land zoned for large lots (over 25000 square feet)	predictor
indus	proportion of non-retail business acres per suburb	predictor
chas	a dummy var. for whether the suburb borders the Charles River (1) or not (0)	predictor
nox	nitrogen oxides concentration (parts per 10 million)	predictor
rm	average number of rooms per dwelling	predictor
age	proportion of owner-occupied units built prior to 1940	predictor
dis	weighted mean of distances to five Boston employment centers	predictor
rad	index of accessibility to radial highways	predictor
tax	full-value property-tax rate per $10,000	predictor
ptratio	pupil-teacher ratio by town	predictor
black	$1000(B_k - 0.63)^2$ where B_k is the proportion of blacks by town	predictor
lstat	lower status of the population (percent)	predictor
medv	median value of owner-occupied homes in $1000s	predictor

1 DATA EXPLORATION

Relocating to a new city or state can be very stressful. In addition to the stress of packing and moving, you may also be nervous about moving to an unfamiliar area. To better understand their new community, some new residents or people interested in moving to a new city choose to review crime statistics in and around their neighborhood. Crime rate may also influence where people choose to live, raise their families and run their businesses; many potential new residents steer clear of cities with higher than average crime rates.

Data was collected in order to predict whether the neighborhood will be at risk for high crime levels. For each neighborhood the response variable, `target`, represents whether the crime rate is above the median crime rate or not. In addition to that 13 predictor variables were collected representing each neighborhood's: proportion of large lots, non-retail business acres, whether or not it borders the Charles River, nitrogen oxides concentration, average number of rooms per dwelling, proportion of owner-occupied units, distances to five Boston employment centers, accessibility to radial highways, property tax rate, pupil-teacher ratio, proportion of African Americans, percent lower status, and median value of homes. The evaluation data contains the same 13 predictor variables and no target variable so it will be impossible to check the accuracy of our predictions from the testing data.

Table 2: Summary statistics

	n	min	mean	median	max	sd
zn	466	0.0000	11.5772532	0.00000	100.0000	23.3646511
indus	466	0.4600	11.1050215	9.69000	27.7400	6.8458549
chas	466	0.0000	0.0708155	0.00000	1.0000	0.2567920
nox	466	0.3890	0.5543105	0.53800	0.8710	0.1166667
rm	466	3.8630	6.2906738	6.21000	8.7800	0.7048513
age	466	2.9000	68.3675966	77.15000	100.0000	28.3213784
dis	466	1.1296	3.7956929	3.19095	12.1265	2.1069496
rad	466	1.0000	9.5300429	5.00000	24.0000	8.6859272
tax	466	187.0000	409.5021459	334.50000	711.0000	167.9000887
ptratio	466	12.6000	18.3984979	18.90000	22.0000	2.1968447
lstat	466	1.7300	12.6314592	11.35000	37.9700	7.1018907
medv	466	5.0000	22.5892704	21.20000	50.0000	9.2396814
target	466	0.0000	0.4914163	0.00000	1.0000	0.5004636

1.1 Summary Statistics

Looking at the Table. 1, we can see that `chas` and `target` are binary variables. 49% of our target variable is coded as 0's indicating that the crime rate is NOT above the median crime rate. There are potential outliers present in `zn`, `lstat`, `medv` and `dis`.

1.2 Shape of Predictor Distributions

Figure. 1 shows that the distribution of most of the variables seems skewed. There are some outliers in the right tail of `tax` , `rad`, `medv`, `lstat`, `dis` and left tail of `ptratio`.

Even more interestingly, for many of the predictor variables the shape of the distribution is significantly different depending on the value of the `target`. For example, `age` is highly left skewed for homes where the crime rate is above the median crime rate (`target` = 1) while the distribution for homes where the crime rate is not above the median the distribution is normal. Other variables with similar differences are `dis`, `indus`, `lstat`, `nox`, `ptratio`, `rad`, and `tax`.

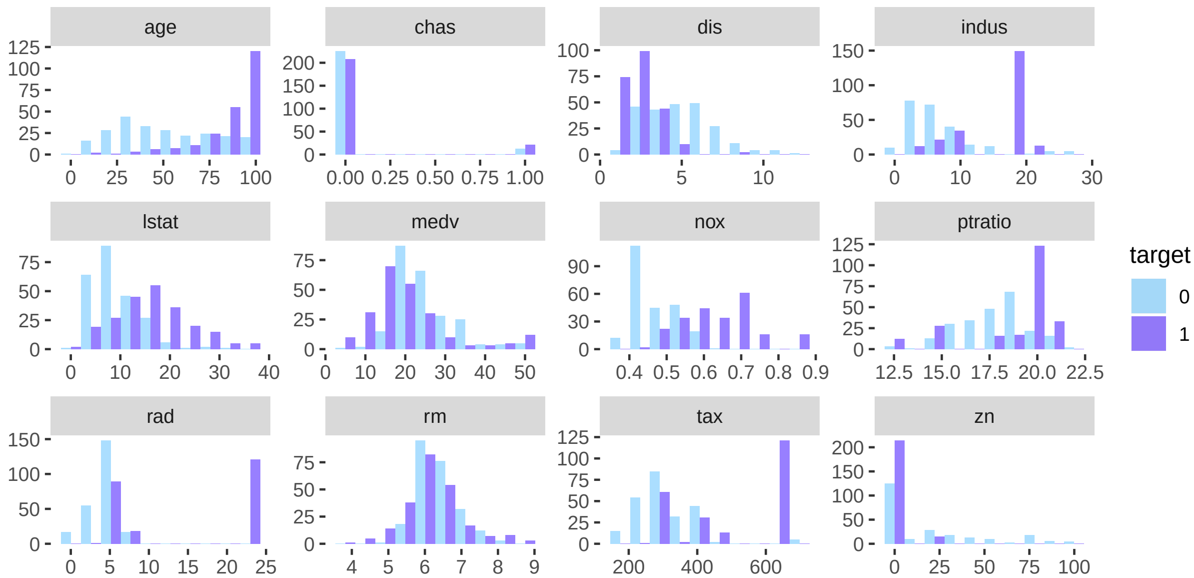


Figure 1: Data Distributions

1.3 Outliers

Figure. 2 shows that there are also a large number of outliers that need to be accounted for, most significantly in `zn` and `medv` and less significantly in `lstat`, `dis` and `rm`. Since `tax` variable has values which are very large compared to other variables in the dataset, it was scaled to fit the boxplot by dividing by 10.

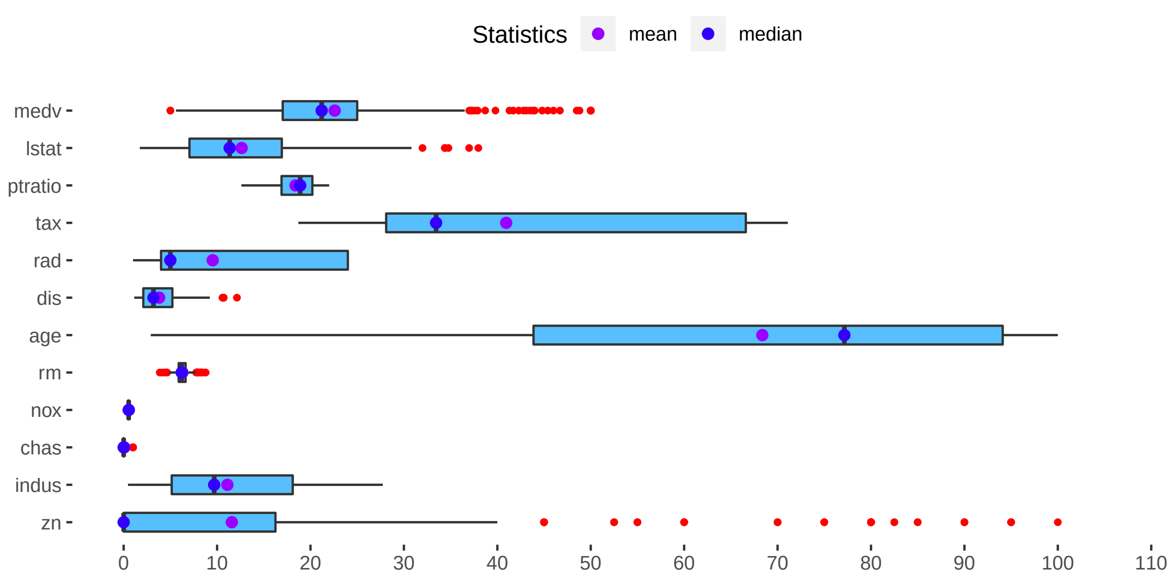


Figure 2: Boxplots highlighting many outliers in the data.

1.4 Missing Values

There are no missing values in any of our observations gathered across the thirteen predictor variables as can be seen in Figure. 3.

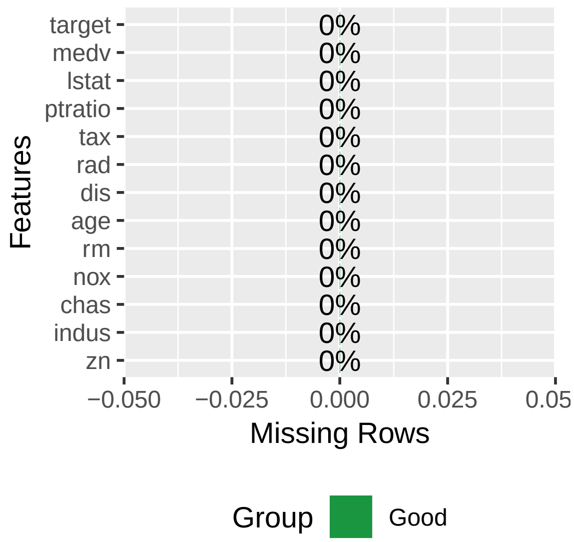


Figure 3: Missing values

1.5 Linearity

Each variable was plotted against the target variable in order to determine at a glance which had the most potential linearity before the dataset was modified.

As can be observed in Figure. 4, all of the predictor variables seem to have an impact on the target. With most of them having a positive impact indicating that the higher the predictor variable values are more likely to correspond to a target that is coded as 1 indicating the crime rate is above the median. The exceptions are `dis`, `medv`, `rm`, `zn`, and possibly `chas` where the distribution of predictor variable values is higher when the target is coded 0.

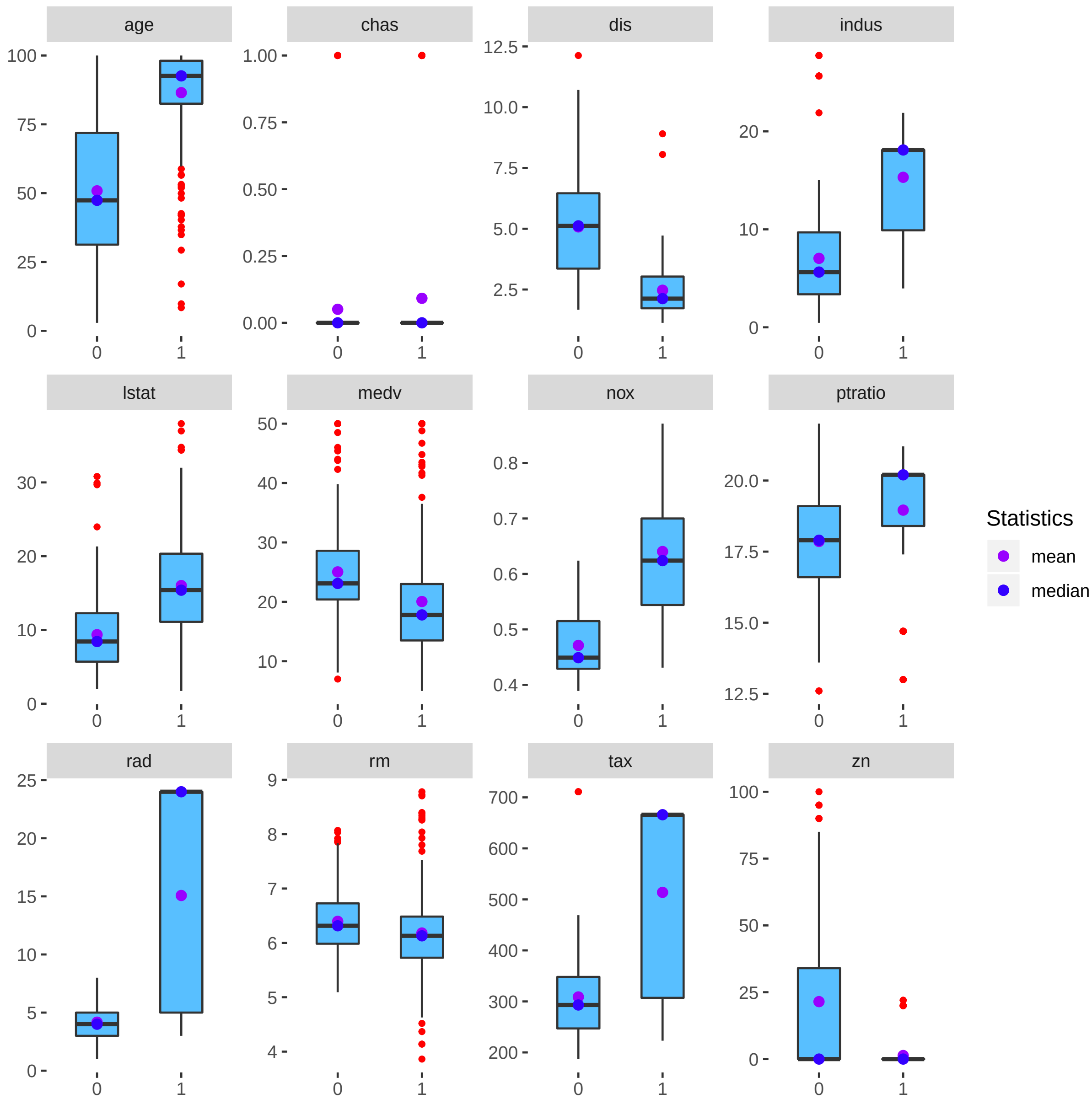


Figure 4: Linear relationships between each predictor and the target

2 DATA PREPARATION

2.1 Missing Values and NA Imputation

Given that the training dataset does include missing values, there's no need to make systematic corrections or imputations.

2.2 Dealing with outliers, leverage, and influence points

While logistic regression can be more robust to leverage points (explanatory variable values, which are distant on the x-axis), outliers (response variable values, which are distant on the y-axis) can exert influence which affects the curve and accuracy of target predictions.

- `dis`, `tax` (property tax rate per $10k), and `medv` (median value of owner-occupied homes) see a few outliers and leverage points in both target classes
- `indus` (the non-retail business acreage proportion) and `lstat` (percent lower status population) both have outliers in the below-mean (0) class
- `ptratio` (pupil-teacher ratio) fit is very impacted by density of low values in the above-mean class, making the linear relationship appear parabolic
- `rad` (highway access index) is influenced by a high-value concentration of locations distant from radial highways that fall in the above-mean class
- `rm` (average rooms per dwelling) sees a wider distribution of house size for the above-mean class then the below-mean; while `zn` (large-lot zoned land proportion) sees the opposite, with a concentration around a few non-residential land proportions for the above-mean class and a wide dispersion for the below-mean class

The figures below examine the linear relationships after a log transformation, which smoothes several relationships but still demonstrates visible influence for several otherr variables: `lstat`, `medv`, `ptratio`, `rad`, `rm`, `tax`, and `zn`. We discuss further in the feature engineering section below.

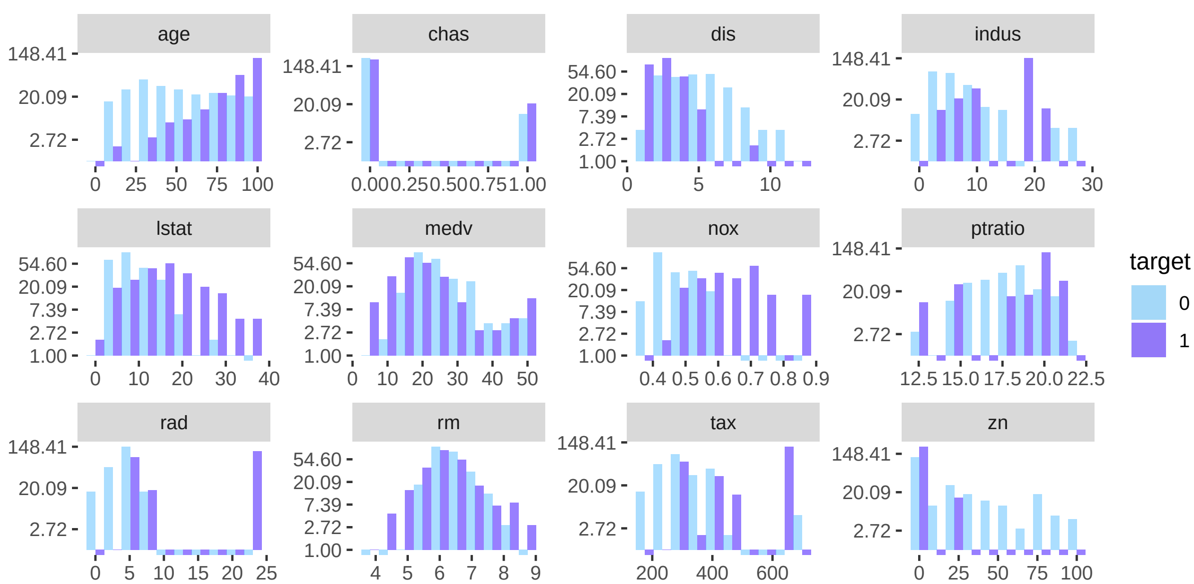


Figure 5: Natural log transformed predictor distributions

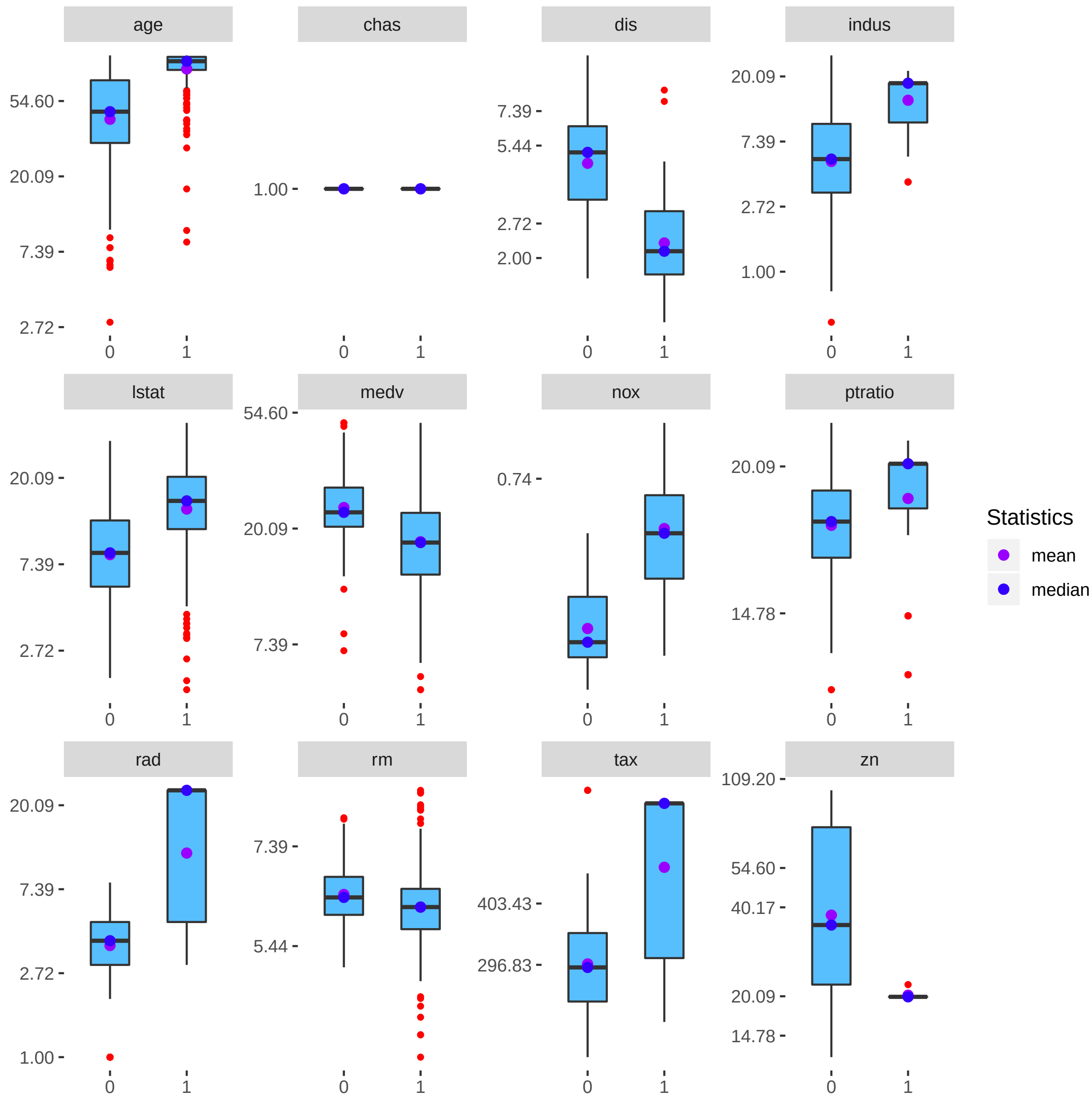


Figure 6: Relationships between natural log transformed predictors and the target

[JEREMY: TEAM, SO WE WANT TO DO FURTHER INVESTIGATION OF OUTLIERS, LOOKING AT R2, STANDARD ERRORS, P-VALS, AND LEVERAGE VALUES FROM THE HAT MATRIX FOR PAIRS OF MODELS, ONE THAT INCLUDES OUTLIERS AND ANOTHER THAT DOESN'T; OR IS THIS ENOUGH?]

2.3 Correlation

An examination of correlation between the explanatory variables reveals the following:

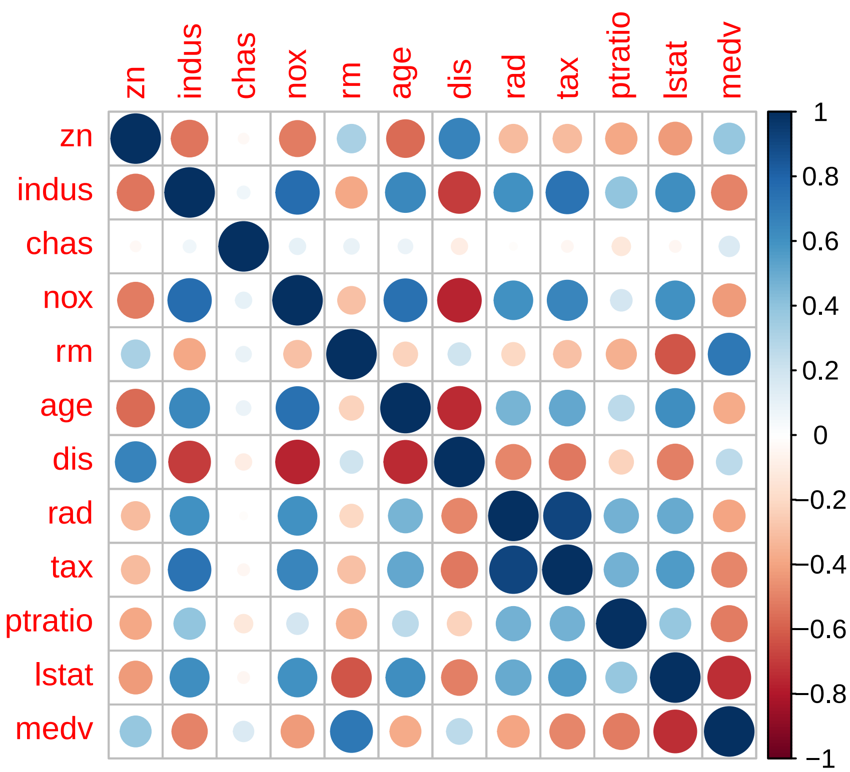
- `indus` (non-retail business acre proportion) is positively correlated with `nox` (pollution concentration,

Table 3: Correlation between predictors

	zn	indus	chas	nox	rm	age	dis	rad	tax	ptratio	lstat	medv
zn	1.00	-0.54	-0.04	-0.52	0.32	-0.57	0.66	-0.32	-0.32	-0.39	-0.43	0.38
indus	-0.54	1.00	0.06	0.76	-0.39	0.64	-0.70	0.60	0.73	0.39	0.61	-0.50
chas	-0.04	0.06	1.00	0.10	0.09	0.08	-0.10	-0.02	-0.05	-0.13	-0.05	0.16
nox	-0.52	0.76	0.10	1.00	-0.30	0.74	-0.77	0.60	0.65	0.18	0.60	-0.43
rm	0.32	-0.39	0.09	-0.30	1.00	-0.23	0.20	-0.21	-0.30	-0.36	-0.63	0.71
age	-0.57	0.64	0.08	0.74	-0.23	1.00	-0.75	0.46	0.51	0.26	0.61	-0.38
dis	0.66	-0.70	-0.10	-0.77	0.20	-0.75	1.00	-0.49	-0.53	-0.23	-0.51	0.26
rad	-0.32	0.60	-0.02	0.60	-0.21	0.46	-0.49	1.00	0.91	0.47	0.50	-0.40
tax	-0.32	0.73	-0.05	0.65	-0.30	0.51	-0.53	0.91	1.00	0.47	0.56	-0.49
ptratio	-0.39	0.39	-0.13	0.18	-0.36	0.26	-0.23	0.47	0.47	1.00	0.38	-0.52
lstat	-0.43	0.61	-0.05	0.60	-0.63	0.61	-0.51	0.50	0.56	0.38	1.00	-0.74
medv	0.38	-0.50	0.16	-0.43	0.71	-0.38	0.26	-0.40	-0.49	-0.52	-0.74	1.00

$r = .76$) and `tax` (property tax rate per \$10k, $r = .73$) and is negatively correlated with `dis` (weighted mean distance to employment centers, $r = -.7$)

- `chas` (bordering Charles river) correlated with `nox` ($r = .97$) and `rm` (average rooms per dwelling, $r = .91$) and `age` (proportion of pre-1940 homes, $r = .79$); and is negatively correlated with `dis` ($r = -.97$)
- `medv` (median value of owner-occupied homes) is correlated with `rm` ($r = .71$); and is negatively correlated with `lstat` (percent lower status population, $r = -.74$)
- `age` is correlated with `nox` ($r = .74$); and is negatively correlated with `dis` ($r = -.75$)
- `rad` (highway access index) correlated with `tax` ($r = .91$)



[JEREMY: TEAM, LET'S DISCUSS HOW WE'D LIKE TO APPLY THESE CORRELATION FINDINGS TO MODEL EVALUATION AND VARIABLE SELECTION]

2.4 Feature Engineering

In MARR, Sheather quotes Cook and Weisberg, suggesting that the best way to determine need for log transformation of skewed predictors is to include both the original and transformed variables in the logistic regression model in order assess their relative contributions directly and prune accordingly

Reexamining the histograms of the predictor distributions above reveals that:

- `age` is left-skewed
- `dis` is right-skewed, and `zn` is extremely so
- `nox` is right-skewed and platykurtic (thin-tailed)
- `rad` and `tax` seem to have normal distributions, with large numbers of outliers at particular levels
- `indus` and `ptratio` reveal peculiar skew, with incidences at particular high level, perhaps due to regulation or infrastructure requirements

We include log transforms of `age`, `dis`, `nox`, `rad`, `tax`, `indus`, and `ptratio` in the dataset for evaluation in models.

[JEREMY: TEAM, DO WE WANT TO ADDRESS THIS BY CALLING log() ON VARIABLES WHEN BUILDING glm(), OR SHOULD WE TRANSFORM IN SOURCE DATASET? I'VE ASSUMED THE FORMER.]

3 BUILD MODELS

3.1 Model 1

$\widehat{y} = -1.95 \times zn - 0.44 \times indus + 0.12 \times chas + 5.65 \times nox - 0.06 \times rm + 0.71 \times age + 1.47 \times dis + 5.54 \times rad - 0.85 \times tax + 0.66 \times ptratio + 0.$

The First model is the binary logistic model including all the explanatory variables. The data is centered and scaled based on the mean and standard deviation of the variables.

```
##
## Call:
## NULL
##
## Deviance Residuals:
##     Min       1Q   Median       3Q      Max
## -1.8464  -0.1445  -0.0017   0.0029   3.4665
##
## Coefficients:
##             Estimate Std. Error z value Pr(>|z|)
## (Intercept)   2.3290     0.7195   3.237  0.00121 **
## zn           -1.5408     0.8097  -1.903  0.05706 .
## indus        -0.4423     0.3260  -1.357  0.17485
## chas          0.2339     0.1940   1.205  0.22803
## nox           5.7309     0.9254   6.193 5.90e-10 ***
## rm           -0.4141     0.5095  -0.813  0.41637
## age           0.9683     0.3912   2.475  0.01333 *
## dis           1.5563     0.4852   3.208  0.00134 **
## rad           5.7880     1.4171   4.084 4.42e-05 ***
## tax          -1.0362     0.4961  -2.089  0.03674 *
## ptratio       0.8844     0.2782   3.179  0.00148 **
## lstat         0.3258     0.3838   0.849  0.39608
```

```
## medv          1.6708     0.6310   2.648  0.00810 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 645.88  on 465  degrees of freedom
## Residual deviance: 192.05  on 453  degrees of freedom
## AIC: 218.05
##
## Number of Fisher Scoring iterations: 9
```

The residual deviance is 147.10 and the AIC is 173.1. We will consider this as the baseline for all models.

	x
zn	304.88578
indus	49.42303
chas	17.50400
nox	398.18024
rm	120.70934
age	71.17422
dis	109.46005
rad	933.83411
tax	114.44284
ptratio	35.98375
lstat	68.51319
medv	185.15264

The review of the VIF output suggests that some variables are highly collinear and may not be necessary to build a model.

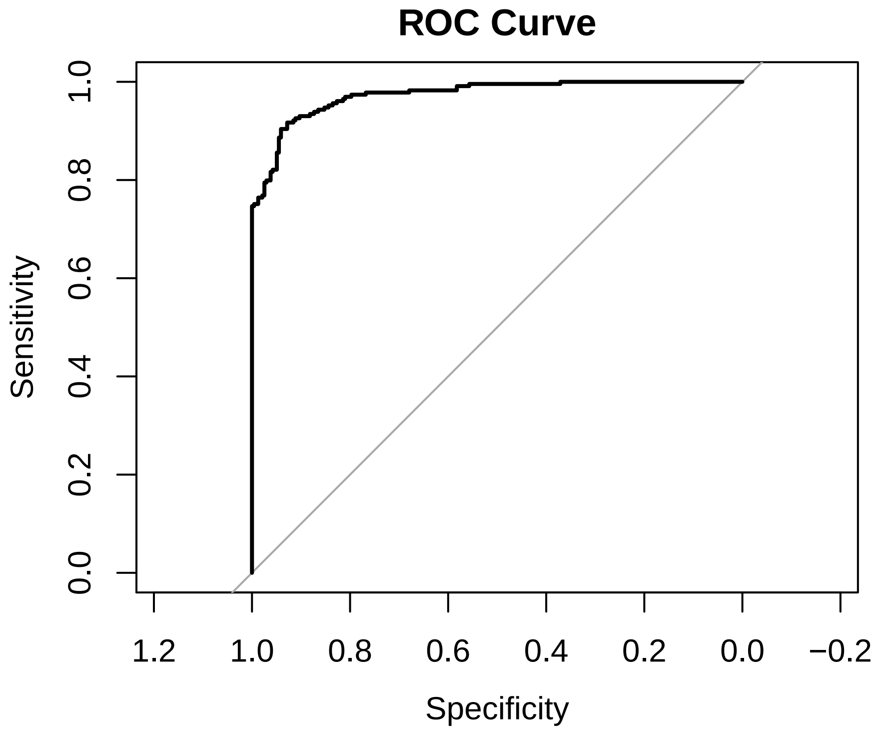


Figure 7: Model 1 ROC Curve

```
## Area under the curve: 0.9738
```

3.2 Model 2

The logarithmic transformation on explanatory variables is used for Model 2 in order to normalize the distribution of the explanatory variables. Model 2 also removes variables that seemed unnecessary in Model 1.

```
##
## Call:
## NULL
##
## Deviance Residuals:
##     Min       1Q   Median       3Q      Max
## -1.8464  -0.1445  -0.0017   0.0029   3.4665
##
## Coefficients:
##             Estimate Std. Error z value Pr(>|z|)
## (Intercept)   2.3290     0.7195   3.237  0.00121 **
## zn           -1.5408     0.8097  -1.903  0.05706 .
## indus        -0.4423     0.3260  -1.357  0.17485
## chas          0.2339     0.1940   1.205  0.22803
## nox           5.7309     0.9254   6.193 5.90e-10 ***
## rm           -0.4141     0.5095  -0.813  0.41637
## age           0.9683     0.3912   2.475  0.01333 *
## dis           1.5563     0.4852   3.208  0.00134 **
```

```
## rad           5.7880     1.4171   4.084 4.42e-05 ***
## tax          -1.0362     0.4961  -2.089  0.03674 *
## ptratio       0.8844     0.2782   3.179  0.00148 **
## lstat         0.3258     0.3838   0.849  0.39608
## medv          1.6708     0.6310   2.648  0.00810 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 645.88  on 465  degrees of freedom
## Residual deviance: 192.05  on 453  degrees of freedom
## AIC: 218.05
##
## Number of Fisher Scoring iterations: 9
```

	x
zn	304.88578
indus	49.42303
chas	17.50400
nox	398.18024
rm	120.70934
age	71.17422
dis	109.46005
rad	933.83411
tax	114.44284
ptratio	35.98375
lstat	68.51319
medv	185.15264

Unfortunately, both Residual deviance and AIC have worsened and the log transformation may not have been the optimal choice.

3.3 Model 3

Model 3 removes the variables with high VIF values from Model 2.

```
##
## Call:
## NULL
##
## Deviance Residuals:
##     Min       1Q   Median       3Q      Max
## -1.8464  -0.1445  -0.0017   0.0029   3.4665
##
## Coefficients:
##             Estimate Std. Error z value Pr(>|z|)
## (Intercept)   2.3290     0.7195   3.237  0.00121 **
## zn           -1.5408     0.8097  -1.903  0.05706 .
## indus        -0.4423     0.3260  -1.357  0.17485
## chas          0.2339     0.1940   1.205  0.22803
## nox           5.7309     0.9254   6.193 5.90e-10 ***
## rm           -0.4141     0.5095  -0.813  0.41637
```

```
## age           0.9683     0.3912   2.475  0.01333 *
## dis           1.5563     0.4852   3.208  0.00134 **
## rad           5.7880     1.4171   4.084 4.42e-05 ***
## tax          -1.0362     0.4961  -2.089  0.03674 *
## ptratio       0.8844     0.2782   3.179  0.00148 **
## lstat         0.3258     0.3838   0.849  0.39608
## medv          1.6708     0.6310   2.648  0.00810 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 645.88  on 465  degrees of freedom
## Residual deviance: 192.05  on 453  degrees of freedom
## AIC: 218.05
##
## Number of Fisher Scoring iterations: 9
```

	x
zn	304.88578
indus	49.42303
chas	17.50400
nox	398.18024
rm	120.70934
age	71.17422
dis	109.46005
rad	933.83411
tax	114.44284
ptratio	35.98375
lstat	68.51319
medv	185.15264

Before we proceed to the next model, Consider different perspective on the built models. Use step approach to see if it is possible to build a model iteratively (forward/backward) and check if there is a room to improve.

3.3.1 Backward Elimination

```
## Call:
## multinom(formula = target ~ zn + nox + age + dis + rad + tax +
##     ptratio + medv, data = train)
##
## Coefficients:
##                    Values   Std. Err.
## (Intercept) -37.420004457 1.760763883
## zn           -0.068657565 0.031406400
## nox          42.812279216 1.566776524
## age           0.032954647 0.010594801
## dis           0.655005663 0.161212399
## rad           0.725172172 0.137468131
## tax          -0.007757457 0.002577425
## ptratio       0.323670155 0.095165901
## medv          0.110489138 0.030246573
##
```

```
## Residual Deviance: 197.3228
## AIC: 215.3228
```

3.3.2 Forward Selection

```
## Call:
## multinom(formula = target ~ zn + indus + chas + nox + rm + age +
##     dis + rad + tax + ptratio + lstat + medv, data = train)
##
## Coefficients:
##                    Values   Std. Err.
## (Intercept) -40.822813404 2.414533568
## zn           -0.065945741 0.034318306
## indus        -0.064613819 0.043886492
## chas          0.910758951 0.735760423
## nox          49.122184372 1.937022648
## rm           -0.587489921 0.720644739
## age           0.034188962 0.013521140
## dis           0.738659039 0.182691053
## rad           0.666362966 0.159297627
## tax          -0.006171376 0.002946741
## ptratio       0.402564041 0.110461647
## lstat         0.045868448 0.053792523
## medv          0.180823739 0.063880285
##
## Residual Deviance: 192.0469
## AIC: 218.0469
```

As you can see above, judging from both Residual Deviance and AIC, the forward/backward stepwise approach did not improve the model.

3.4 Model 4

The first step was to create a logit model, which includes all variables in the training data set. In the second step we are performing backward elimination. The remaining variables are: distance to employment centers (negative effect), accessibility to radial highway (positive effect), and proportion of owner-occupied units built prior to 1940 (positive effect).

```
##
## Call:
## glm(formula = target ~ zn + nox + age + dis + rad + tax + ptratio +
##     medv, family = binomial(logit), data = train)
##
## Deviance Residuals:
##     Min       1Q   Median       3Q      Max
## -1.8295  -0.1752  -0.0021   0.0032   3.4191
##
## Coefficients:
##               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -37.415922   6.035013  -6.200 5.65e-10 ***
## zn           -0.068648   0.032019  -2.144  0.03203 *
## nox          42.807768   6.678692   6.410 1.46e-10 ***
```

```
## age           0.032950   0.010951   3.009  0.00262 **
## dis           0.654896   0.214050   3.060  0.00222 **
## rad           0.725109   0.149788   4.841 1.29e-06 ***
## tax          -0.007756   0.002653  -2.924  0.00346 **
## ptratio       0.323628   0.111390   2.905  0.00367 **
## medv          0.110472   0.035445   3.117  0.00183 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 645.88  on 465  degrees of freedom
## Residual deviance: 197.32  on 457  degrees of freedom
## AIC: 215.32
##
## Number of Fisher Scoring iterations: 9
```

	x
zn	304.88578
indus	49.42303
chas	17.50400
nox	398.18024
rm	120.70934
age	71.17422
dis	109.46005
rad	933.83411
tax	114.44284
ptratio	35.98375
lstat	68.51319
medv	185.15264

3.5 Model 5

```
##
## Call:
## glm(formula = target ~ zn + indus + chas + nox + rm + age + dis +
##     rad + tax + ptratio + lstat + medv + zn:age + zn:tax + zn:ptratio +
##     zn:lstat + indus:chas + indus:rad + indus:ptratio + indus:medv +
##     nox:age + nox:tax + nox:ptratio + nox:lstat + nox:medv +
##     rm:age + age:tax + age:ptratio + dis:tax + dis:ptratio +
##     dis:lstat + dis:medv + rad:tax + tax:medv + lstat:medv, family = binomial(),
##     data = train)
##
## Deviance Residuals:
##        Min          1Q      Median          3Q         Max
## -1.069e-03  -2.000e-08  -2.000e-08   2.000e-08   1.150e-03
##
## Coefficients:
##                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)    3.762e+03  7.586e+05   0.005    0.996
## zn             3.308e+02  1.018e+04   0.033    0.974
## indus         -8.252e+02  1.830e+04  -0.045    0.964
## chas           5.607e+02  3.014e+04   0.019    0.985
```

```
## nox           6.112e+04  1.331e+06   0.046    0.963
## rm           -5.252e+02  1.738e+04  -0.030    0.976
## age          -8.523e+01  2.926e+03  -0.029    0.977
## dis          -4.914e+03  1.426e+05  -0.034    0.973
## rad           1.481e+02  2.866e+03   0.052    0.959
## tax          -7.452e+01  1.585e+03  -0.047    0.962
## ptratio       1.110e+03  2.519e+04   0.044    0.965
## lstat         7.347e+02  1.406e+04   0.052    0.958
## medv         -9.237e+02  2.093e+04  -0.044    0.965
## zn:age       -1.623e+00  5.060e+01  -0.032    0.974
## zn:tax       -3.277e-01  1.264e+01  -0.026    0.979
## zn:ptratio   -1.239e+01  3.604e+02  -0.034    0.973
## zn:lstat      6.001e+00  2.359e+02   0.025    0.980
## indus:chas   -8.051e+01  2.327e+03  -0.035    0.972
## indus:rad     4.608e+01  1.174e+03   0.039    0.969
## indus:ptratio  4.202e+01  9.357e+02   0.045    0.964
## indus:medv   -4.728e+00  2.070e+02  -0.023    0.982
## nox:age      -1.223e+02  2.696e+03  -0.045    0.964
## nox:tax       4.239e+01  1.160e+03   0.037    0.971
## nox:ptratio  -3.981e+03  7.200e+04  -0.055    0.956
## nox:lstat    -8.463e+02  1.671e+04  -0.051    0.960
## nox:medv      1.192e+03  3.257e+04   0.037    0.971
## rm:age        6.344e+00  1.887e+02   0.034    0.973
## age:tax       1.547e-01  3.437e+00   0.045    0.964
## age:ptratio   3.565e+00  9.585e+01   0.037    0.970
## dis:tax       6.290e+00  1.485e+02   0.042    0.966
## dis:ptratio   1.405e+02  5.035e+03   0.028    0.978
## dis:lstat    -2.926e+01  7.928e+02  -0.037    0.971
## dis:medv      3.558e+01  7.316e+02   0.049    0.961
## rad:tax      -9.327e-01  2.180e+01  -0.043    0.966
## tax:medv      9.764e-01  1.759e+01   0.055    0.956
## lstat:medv   -8.433e+00  1.604e+02  -0.053    0.958
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 6.4588e+02  on 465  degrees of freedom
## Residual deviance: 1.4059e-05  on 430  degrees of freedom
## AIC: 72
##
## Number of Fisher Scoring iterations: 25
```

	x
zn	2.628324e+13
indus	7.298197e+12
chas	2.785732e+10
nox	1.122035e+13
rm	6.979989e+10
age	3.193690e+12
dis	4.198177e+13
rad	2.881458e+11
tax	3.291569e+13
ptratio	1.424277e+12
lstat	4.636789e+12
medv	1.739347e+13
‘zn:age‘	7.473315e+11
‘zn:tax‘	3.948133e+12
‘zn:ptratio‘	9.232176e+12
‘zn:lstat‘	5.671803e+11
‘indus:chas‘	3.278729e+10
‘indus:rad‘	1.972460e+13
‘indus:ptratio‘	7.693409e+12
‘indus:medv‘	4.534180e+11
‘nox:age‘	1.625397e+12
‘nox:tax‘	1.181090e+13
‘nox:ptratio‘	1.655525e+13
‘nox:lstat‘	3.666879e+12
‘nox:medv‘	1.116011e+13
‘rm:age‘	5.151923e+11
‘age:tax‘	2.420960e+12
‘age:ptratio‘	1.424587e+12
‘dis:tax‘	4.086323e+12
‘dis:ptratio‘	1.644614e+13
‘dis:lstat‘	1.480446e+11
‘dis:medv‘	1.069405e+12
‘rad:tax‘	9.064989e+12
‘tax:medv‘	2.135431e+12
‘lstat:medv‘	8.933286e+10

4 SELECT MODELS

	Sensitivity	Specificity	Precision	Recall	F1
Model.1	0.92827	0.9039301	0.9090909	0.92827	0.9185804
Model.2	0.92827	0.9039301	0.9090909	0.92827	0.9185804
Model.3	0.92827	0.9039301	0.9090909	0.92827	0.9185804
Model.4	0.92827	0.9039301	0.9090909	0.92827	0.9185804
Model.5	1.00000	1.0000000	1.0000000	1.00000	1.0000000

Three models were explored in order to determine the best way to determine whether or not a neighborhood’s crime rate was above or below the median crime rate. The most efficient model was the second model, with the first model being somewhat efficient, and the third model being least efficient.