数组10 大排序

排序算法	平均时间复杂度	最好情况	最坏情况	空间复杂度	排序方式	稳定性
冒泡排序	O(n²)	O(n)	O(n²)	O(1)	In-place	稳定
选择排序	O(n²)	O(n²)	O(n²)	O(1)	In-place	不稳定
插入排序	O(n²)	O(n)	O(n²)	O(1)	In-place	稳定
希尔排序	O(n log n)	O(n log² n)	O(n log² n)	O(1)	In-place	不稳定
归并排序	O(n log n)	O(n log n)	O(n log n)	O(n)	Out-place	稳定
快速排序	O(n log n)	O(n log n)	O(n²)	O(log n)	In-place	不稳定
堆排序	O(n log n)	O(n log n)	O(n log n)	O(1)	In-place	不稳定
计数排序	O(n + k)	O(n + k)	O(n + k)	O(k)	Out-place	稳定
桶排序	O(n + k)	O(n + k)	O(n²)	O(n + k)	Out-place	稳定
基数排序	O(n×k)	O(n×k)	O(n×k)	O(n + k)	Out-place	稳定

名称	数据对象	稳定性	时间复杂度		额外空间复杂度	描述			
白柳			平均	最坏	视外至问复乐度	海 达			
冒泡排序	数组	✓	$O(n^2)$ $O(n^2)$		O(1)	(无序区,有序区)。 从无序区透过交换找出最大元素放到有序区前端。			
选择排序	数组 🗶	X	$O(n^2)$		O(1)	(有序区,无序区) 。			
处对丰州市	链表	1	O(n)		0(1)	在无序区里找一个最小的元素跟在有序区的后面。对数组: 比较得多,换得少。			
插入排序	数组、链表	1	$O(n^2)$		O(1)	(有序区,无序区)。 把无序区的第一个元素插入到有序区的合适的位置。对数组:比较得少,换得多。			
堆排序	数组	x	$O(n \log n)$		O(1)	(最大堆,有序区)。 从堆顶把根卸出来放在有序区之前,再恢复堆。			
归并排序		1	$O(n \log^2 n)$ $O(1)$		O(1)				
	数组		$O(n \log n)$		$O(n) + O(\log n)$ 如果不是从下到上	把数据分为两段,从两段中逐个选最小的元素移入新数据段的末尾。 可从上到下或从下到上进行。			
	链表				O(1)				
快速排序	数组	x	$O(n \log n)$	$O(n^2)$	$O(\log n)$	(小数,基准元素,大数)。 在区间中随机挑选一个元素作基准,将小于基准的元素放在基准之前,大于基准的元素放在基准之后,再分别对小数区与大数区进行排序。			
希尔排序	数组	X	$O(n \log^2 n)$	$O(n^2)$	O(1)	每一轮按照事先决定的间隔进行插入排序,间隔会依次缩小,最后一次一定要是1。			
计数排序	数组、链表	1	O(n+m) $O(n+m)$		O(n+m)	统计小于等于该元素值的元素的个数i,于是该元素就放在目标数组的索引i位(i≥0)。			
桶排序	数组、链表	1	O(n) $O(m)$		O(m)	将值为i的元素放入i号桶,最后依次把桶里的元素倒出来。			
基数排序	数组、链表	1	$O(k \times n)$	$O(n^2)$		一种多关键字的排序算法,可用桶排序实现。			

选择排序

时间复杂度 0(n^2)

空间复杂度 0(1)

不稳定

比较次数 1 + 2 + 3 +...+ n-1 = n(n-1)/2

移动次数 3*(n-1)

```
void select_sort(vector<int> &arr) {
    for (int i = 0; i < arr.size(); ++i) {
        int min = i;
        for (int j = i + 1; j < arr.size(); ++j) {
            if (arr[j] <= arr[min]) {
                 min = j;
            }
        }
        swap(arr[i], arr[min]);
    }
}</pre>
```

冒泡排序

时间复杂度 0(n^2)

空间复杂度 0(1)

稳定

最好情况

- 123456
- 比较次数 n-1
- 移动次数 a
- 时间复杂度 0(n)

最坏情况

- 654321
- 比较次数 1 + 2 + 3 +...+ n-1 = n(n-1)/2
- 移动次数 3*n(n-1)/2
- 时间复杂度 O(n^2)

```
void swap_xor(vector<int>::value_type &value1, vector<int>::value_type &value2) {
   value1 = value1 ^ value2;
   value2 = value1 ^ value2;
   value1 = value1 ^ value2;
};
void bubble_sort(vector<int> &arr) {
   if (arr.empty() || arr.size() < 2) return;</pre>
   bool flag = false;
   for (int e = arr.size() - 1; e >= 0; --e) {
        for (int i = 0; i < e; ++i) {
            if (arr[i] > arr[i + 1]) {
                swap(arr[i], arr[i + 1]);
                flag = true;
            }
       if (!flag) break;
   }
}
```

插入排序

时间复杂度 0(n^2)

空间复杂度 0(1)

稳定

最好情况

- 123456
- 比较次数 n-1
- 移动次数 ø
- 时间复杂度 0(n)

最坏情况

- 654321
- 比较次数 1 + 2 + 3 +...+ n-1 = n(n-1)/2
- 移动次数 2+3+4+...+n=(n+2)(n-1)/2
- 时间复杂度 0(n^2)

```
void insertSort(vector<int> &arr) {
    for (int i = 1; i < arr.size(); ++i) {
        for (int j = i-1; j >=0 && arr[j] > arr[j+1]; j--) {
            swap(arr[j],arr[j+1]);
        }
    }
}
```

希尔排序 (while)

```
void shell_sort1(vector<int> &arr) {
    int len = arr.size();
    int interval = len >> 1; // 获取初始长度
    while (interval >= 1) {
        for (int i = interval; i < len; ++i) {

            vector<int>::value_type tmp = arr[i];
            int j = i;
            while ((j - interval >= 0) && (arr[j - interval] > tmp)) {

                arr[j] = arr[j - interval];
                j -= interval;

            }
            arr[j] = tmp;
            }
            interval /= 2;
        }
}
```

希尔排序 (for)

时间复杂度 0(n^1.3~n^2)

空间复杂度 0(1)

不稳定

归并排序 (递归)

时间复杂度 O(nlogn)

空间复杂度 O(n)

稳定

```
vector<int> tmp;
void merge_sort(vector<int> &arr){
    tmp.resize(arr.size());
    merge_sort(arr,0,arr.size()-1);
}
void merge(vector<int> & arr, int lo, int mid ,int hig) {
    for (int i = lo; i \leftarrow hig; ++i) {
        tmp[i]=arr[i];
    int i=lo,j=mid+1;
    for (int k = lo; k \leftarrow hig; ++k) {
        if(i==mid+1){
             arr[k]=tmp[j++];
        }else if(j==hig+1){
             arr[k]=tmp[i++];
        }else if(tmp[i]<tmp[j]){</pre>
             arr[k]=tmp[i++];
        }else{
            arr[k]=tmp[j++];
        }
    }
```

```
void merge_sort(vector<int> &arr, int lo, int hig) {
   if (lo >= hig) return;
   int mid = lo + (hig - lo) / 2;
   merge_sort(arr, lo, mid);
   merge_sort(arr, mid + 1, hig);
   merge(arr, lo, mid,hig);
}
```

归并排序 (迭代)

时间复杂度 O(nlogn)

空间复杂度 0(n)

稳定

```
// 5. 归并排序 (迭代)
void merge_sort2(vector<int> & arr) {
   int len = arr.size();
   vector<int> tmp(len,0);
   for (int seg = 1; seg < len; seg += seg) {</pre>
        for (int start = 0; start < len; start += seg + seg) {</pre>
            int low = start, mid = min(start + seg, len);
            int high = min(start + seg + seg, len);
            int k = low;
            int start1 = low, end1 = mid;
            int start2 = mid, end2 = high;
            while (start1 < end1 && start2 < end2) {
                tmp[k++] = arr[start1] < arr[start2] ? arr[start1++] : arr[start2++];
            }
            while (start1 < end1) {
                tmp[k++] = arr[start1++];
            while (start2 < end2) {
                tmp[k++] = arr[start2++];
        }
        copy(tmp.begin(), tmp.end(), arr.begin());
   }
}
```

快速排序

时间复杂度 O(nlogn)

空间复杂度 0(1)

不稳定

最好情况

- 每次选择的分界点都是最好的分界点
- 时间复杂度 O(nlogn)

最坏情况

- 654321 123456
- 时间复杂度 0(n^2)

```
int quick_sort_parition(vector<int> &arr, int low, int hig) {
    swap(arr[low], arr[low+rand()%(hig-low+1)]);
    vector<int>::value_type pivot =arr[low];
    while (low < hig) {
        while (low < hig && arr[hig] >= pivot ) {
            hig--;
        }
        arr[low]=arr[hig];
        while (low<hig && arr[low] <= pivot ) {</pre>
            low++;
        arr[hig]=arr[low];
    }
    arr[low] = pivot;
    return low;
}
void quick_sort(vector<int> &arr,int low, int hig){
    if(low<hig){</pre>
        int pivot = quick_sort_parition(arr, low, hig);
        quick_sort(arr, low, pivot - 1);
        quick_sort(arr, pivot + 1, hig);
    }
}
```

```
void quickSort(int nums[], int left, int right) {
    if (left >= right) {
        return;
    }
    int i = left - 1, j = right + 1;
    swap(nums[left],nums[left+rand()%(right-left)]);
    int x = nums[left];
    while (i < j) {
        while (nums[++i] < x); // 找到第一个大于等于x的元素
        while (nums[--j] > x); // 找到第一个小于等于x的元素
        if (i < j) swap(nums[i], nums[j]);
    }
    quickSort(nums,left,j);
    quickSort(nums,j+1,right);
}</pre>
```

快排 三向切分

```
void threeWayPartition(vector<int> &nums) {
    threeWayPartition(nums, 0, nums.size() - 1);
```

```
void threeWayPartition(vector<int> &nums, int start, int end) {
    if (start >= end) {
        return;
    }
    int lt = start;
    int eq = start;
    int gt = end;
    int base = nums[eq];
    while (eq <= gt) {
        if (nums[eq] > base) swap(nums[eq], nums[gt--]);
        else if (nums[eq] < base) swap(nums[lt++], nums[eq++]);
        else eq++;
    }
    threeWayPartition(nums, start, lt - 1);
    threeWayPartition(nums, gt + 1, end);
}
</pre>
```

记数排序

```
void count_sort(vector<int> &arr) {
   int len = arr.size();
   vector<int>::value_type maxx = *max_element(arr.begin(), arr.end());
   vector<int>::value_type minx = *min_element(arr.begin(), arr.end());
   vector<int> tmp(maxx - minx + 1, 0);
   vector<int> ans;
   for (int i = 0; i < len; ++i) {
       tmp[arr[i] - minx]++;
   for (int j = 0; j < maxx - minx + 1; ++j) {
       while (tmp[j] != 0) {
            ans.push_back(j + minx);
           tmp[j]--;
       }
   }
   copy(ans.begin(), ans.end(), arr.begin());
}
```

桶排序

```
void insert_list_sort(vector<int> &arr) {
   int len = arr.size();
   for (int i = 1; i < len; ++i) {
      for (int j = i-1; j >=0 ; j--) {
        if(arr[j]>arr[j+1]){
            swap(arr[j],arr[j+1]);
        }
   }
}
```

```
void bucket_sort(vector<int> & arr) {
    vector<int>::value_type maxx = *max_element(arr.begin(), arr.end());
   vector<int>::value_type minx = *min_element(arr.begin(), arr.end());
   const int bucket_size=maxx / 10 - minx / 10 + 1;;
   vector<vector<int>> bucket(bucket_size); // 10个桶 或者使用 unordered_map 创建桶
   // 初始化空桶
    for (int i = 0; i < bucket_size; ++i) {</pre>
        vector<int> x{0};
        bucket.push_back(x);
   }
   for (int i = 0; i < arr.size(); ++i) {</pre>
        bucket[arr[i] / 10].push_back(arr[i]);
   int index = 0;
   for (int i = 0; i < bucket_size; ++i) {</pre>
        // sort of bucket
        insert_list_sort(bucket[i]);
        for (auto it = bucket[i].begin(); it != bucket[i].end(); ++it) {
            arr[index++] = *it;
        }
   }
}
```

基数排序

- d为操作的趟数
- n 为分配的次数 也是元素的个数
- r 为队列的个数 也是划分元素的子集个数 例如 {0,1,2,3,4,5,6,7,8,9}

时间复杂度 0(d(n+r))

空间复杂度 0(r)

稳定

```
void radix_sort(vector<int> &arr) {
    // get numberOfDigits : numberOfDigits为位数
    vector<int>::value_type max = *max_element(arr.begin(), arr.end());
    int numberOfDigits = 0;
    while (max > 0) {
        max /= 10;
        numberOfDigits++;
    }
    const int BUCKETS = 10;
    vector<vector<int>> buckets(BUCKETS);
    for (int poss = 0; poss <= numberOfDigits - 1; ++poss) {
        int denominator = static_cast<int> (pow(10, poss));
    }
}
```

```
for (int &tmp: arr) {
          buckets[(tmp / denominator) % 10].push_back(tmp);

}
int index = 0;
for (auto &thebuckett: buckets) {
          for (int &k: thebuckett) {
                arr[index++] = k;
                thebuckett.clear();
          }
     }
}
```

堆排序

```
排序时间复杂度 0(nlgn) 调用 n 次 Heapify 0(lgn)
建堆时间复杂度 T(4*n) 0(n)
空间复杂度 0(1)
```

不稳定

```
class Solution {
public:
   void maxHeapify(vector<int> &arr, int i, int heapSize) {
        while (2*i+1<=heapSize){
            int leftChild=(2*i)+1,rightChild=(2*i)+2,target=leftChild;
            if(rightChild <=heapSize && arr[rightChild]> arr[leftChild]){
                target=rightChild;
            if(arr[target] > arr[i]){
                swap(arr[target],arr[i]);
            }else{
                break;
            i=target;
       }
   }
   void maxHeapify2(vector<int>& a, int i, int heapSize) {
       int l = i * 2 + 1, r = i * 2 + 2, largest = i;
        if (1 <= heapSize && a[1] > a[largest]) {
            largest = 1;
       if (r <= heapSize && a[r] > a[largest]) {
            largest = r;
       }
        if (largest != i) {
            swap(a[i], a[largest]);
            maxHeapify2(a, largest, heapSize);
       }
    }
```

```
void maxSwim(vector<int> & arr, int i){
        while (i>=0 \&\& arr[i/2]< arr[i]){
            swap(arr[i/2],arr[i]);
            i=i/2;
        }
    }
   void build_heap(vector<int> &arr, int size) {
        for (int i = size/2; i >= 0; i--) {
            maxHeapify(arr, i, size);
        }
   }
   void heap_sort(vector<int> & arr) {
        int len=arr.size()-1;
        build_heap(arr, len);
        for (int i = len ; i >=1; i--) {
            swap(arr[i], arr[0]);
            len--;
            maxHeapify(arr, 0, len);
        }
   }
};
class Solution2 {
public:
   void minHeapify(vector<int> &arr, int i, int heapSize) {
        while (2*i+1<=heapSize){
            int leftChild=(2*i)+1,rightChild=(2*i)+2,target=leftChild;
            if(rightChild <=heapSize && arr[rightChild]> arr[leftChild]){
                target=rightChild;
            if(arr[target] > arr[i]){
                swap(arr[target],arr[i]);
            }else{
                break;
            i=target;
        }
   }
   void mixSwim(vector<int> & arr, int i){
        while (i>=0 && arr[i/2]> arr[i]){
            swap(arr[i/2],arr[i]);
            i=i/2;
        }
   }
   void build_heap(vector<int> &arr, int size) {
        for (int i = size/2; i >= 0; i--) {
            minHeapify(arr, i, size);
        }
   }
```

```
void heap_sort(vector<int> & arr) {
    int len=arr.size()-1;
    build_heap(arr, len);
    for (int i = len ; i >=1; i--) {
        swap(arr[i], arr[0]);
        len--;
        minHeapify(arr, 0, len);
    }
};
```

链表排序 力扣 148

插入排序

```
class Solution {
public:
   ListNode *insertionSortList(ListNode *head) {
        if (head == nullptr) {
            return head;
        ListNode *dummyHead = new ListNode(-1);
        dummyHead->next = head;
        ListNode *lastSorted = head;
        ListNode *cur = head->next;
        while (cur != nullptr) {
            if (lastSorted->val <= cur->val) {
                lastSorted = lastSorted->next;
                ListNode *prev = dummyHead;
                while (prev->next->val <= cur->val) {
                    prev = prev->next;
                }
                lastSorted->next = cur->next;
                // 将cur插入到 prev 后
                cur->next = prev->next;
                prev->next = cur;
            cur = lastSorted->next;
        return dummyHead->next;
};
```

归并排序 递归

```
class Solution {
    public ListNode sortList(ListNode head) {
        if (head == null | head.next == null)
            return head;
        ListNode fast = head.next, slow = head;
        while (fast != null && fast.next != null) {
            slow = slow.next;
            fast = fast.next.next;
        }
        ListNode tmp = slow.next;
        slow.next = null;
        ListNode left = sortList(head);
        ListNode right = sortList(tmp);
        ListNode h = new ListNode(0);
        ListNode res = h;
        while (left != null && right != null) {
            if (left.val < right.val) {</pre>
                h.next = left;
                left = left.next;
            } else {
                h.next = right;
                right = right.next;
            }
            h = h.next;
        h.next = left != null ? left : right;
        return res.next;
}
```

```
class Solution {
public:
   ListNode* sortList(ListNode* head) {
       if (head == nullptr || head->next == nullptr) return head;
       ListNode* head1 = head;
       ListNode* head2 = split(head);
       head1 = sortList(head1);
                                  //一条链表分成两段分别递归排序
       head2 = sortList(head2);
                                    //返回合并后结果
       return merge(head1, head2);
   }
   //双指针找单链表中点模板
   ListNode* split(ListNode* head)
       ListNode *slow = head, *fast = head->next;
       while (fast != nullptr && fast->next != nullptr)
```

```
slow = slow->next;
            fast = fast->next->next;
        }
        ListNode* mid = slow->next;
                                   //断尾
        slow->next = nullptr;
        return mid;
    }
    //合并两个排序链表模板
    ListNode* merge(ListNode* head1, ListNode* head2)
        ListNode *dummy = new ListNode(0), *p = dummy;
        while (head1 != nullptr && head2 != nullptr)
            if (head1->val < head2->val)
                p = p \rightarrow next = head1;
                head1 = head1->next;
            }
            else
                p = p \rightarrow next = head2;
                head2 = head2->next;
            }
        }
        if (head1 != nullptr) p->next = head1;
        if (head2 != nullptr) p->next = head2;
        return dummy->next;
};
```

归并排序 迭代

```
class Solution {
public:
    ListNode* sortList(ListNode* head) {
        if (head == nullptr) {
            return head;
        }
        int length = 0;
        ListNode* node = head;
        while (node != nullptr) {
            length++;
            node = node->next;
        }
        ListNode* dummyHead = new ListNode(0, head);
        for (int subLength = 1; subLength < length; subLength <<= 1) {</pre>
            ListNode* prev = dummyHead, *curr = dummyHead->next;
            while (curr != nullptr) {
```

```
ListNode* head1 = curr;
                for (int i = 1; i < subLength && curr->next != nullptr; i++) {
                    curr = curr->next;
                ListNode* head2 = curr->next;
                curr->next = nullptr;
                curr = head2;
                for (int i = 1; i < subLength && curr != nullptr && curr->next !=
nullptr; i++) {
                    curr = curr->next;
                ListNode* next = nullptr;
                if (curr != nullptr) {
                    next = curr->next;
                    curr->next = nullptr;
                ListNode* merged = merge(head1, head2);
                prev->next = merged;
                while (prev->next != nullptr) {
                    prev = prev->next;
                }
                curr = next;
            }
        return dummyHead->next;
   }
   ListNode* merge(ListNode* head1, ListNode* head2) {
        ListNode* dummyHead = new ListNode(0);
        ListNode* temp = dummyHead, *temp1 = head1, *temp2 = head2;
        while (temp1 != nullptr && temp2 != nullptr) {
            if (temp1->val <= temp2->val) \{
                temp->next = temp1;
                temp1 = temp1->next;
            } else {
                temp->next = temp2;
                temp2 = temp2->next;
            temp = temp->next;
        if (temp1 != nullptr) {
            temp->next = temp1;
        } else if (temp2 != nullptr) {
            temp->next = temp2;
        return dummyHead->next;
   }
};
```

链表快排

```
class Solution2 {
 ListNode* sortList(ListNode* head) {
       return quickSort(head , nullptr);
   }
 ListNode *quickSort(ListNode* head ,ListNode* end){
       if(head ==end | head->next ==end) return head;
       ListNode *lhead = head ,*utail = head ,*p = head->next;
       while (p != end){
            ListNode* nextNode = p->next;
            if(p->val < head->val){
               //头插
               p->next = lhead;
               lhead = p;
           else {
               //尾插
               utail->next = p;
               utail = p;
           p = nextNode;
       }
       utail->next = end;
       ListNode* node = quickSort(lhead, head);
       head->next = quickSort(head->next, end);
       return node;
```

链表选择排序

```
// Created by yjs on 23-7-29.
//
#include <bits/stdc++.h>
#include <iostream>
using namespace std;
struct ListNode {
   int val;
   ListNode *next;
   ListNode(int x) : val(x), next(NULL) {}
};
class Solution{
public:
   ListNode * deleteListNode (ListNode* head){
       ListNode* cur= head->next;
       ListNode* pre=head; // pre指向头结点
       ListNode* min=cur; // 假设第一个结点为最小值的结点
```

```
while (cur->next!= nullptr){
           if(cur->next->val < min->val){
               pre=cur;
               min=cur->next;
           cur=cur->next;
       pre->next=min->next; // 从链表上删除最小值结点
//
         free (min);
       return head;
   }
public:
   ListNode * selectSort(ListNode* head){
       ListNode * dummyHead= new ListNode(-1);
       ListNode * dummyCurser=dummyHead;
       while (head->next!= nullptr){
           ListNode* cur= head->next;
           ListNode* pre=head; // pre指向头结点
           ListNode* min=cur; // 假设第一个结点为最小值的结点
           while (cur->next!= nullptr){
               if(cur->next->val < min->val){
                   pre=cur;
                   min=cur->next;
               }
               cur=cur->next;
           }
           pre->next=min->next; // 从链表上删除最小值结点
           dummyCurser->next=min;
           dummyCurser=dummyCurser->next;
       dummyCurser->next= nullptr;
       return dummyHead->next;
   }
};
string ppint(ListNode * head){
   ListNode * cur=head;
   string res="";
   int count=0;
   while (cur!= nullptr){
       count++;
       res= res+to_string(cur->val)+" ";
       cur=cur->next;
   return " ["+to_string(count)+"] "+ res+"\n";
}
```

```
int main() {
    vector<int> nums{ 12,25, 36, 17, 25, 56,1};
    ListNode* head=new ListNode(-1);
    ListNode * cur=head;
    for (int i = 0; i < nums.size(); ++i) {</pre>
        cur->next=new ListNode(nums[i]);
        cur=cur->next;
    cout << ppint(head->next)<<endl;</pre>
    Solution solution;
// for (int i = 0; i < 7; ++i) {
         head=solution.deleteListNode(head);
//
         cout << ppint(head->next)<<endl;</pre>
//
    }
   ListNode * res=solution.selectSort(head);
    cout << ppint(res)<<endl;</pre>
}
```

链表冒泡排序

```
class Solution {
public:
   void ListNodeSwap(ListNode *prevNode, ListNode *node1, ListNode *node2) {
       node1->next = node2->next;
       prevNode->next = node2;
       node2->next = node1;
   }
   static string ppint(ListNode *head) {
       ListNode *cur = head;
       string res = "";
       int count = 0;
        while (cur != nullptr) {
           count++;
            res = res + to_string(cur->val) + " ";
           cur = cur->next;
        return " [" + to_string(count) + "] " + res + "\n";
   }
public:
   ListNode *BubbleSort(ListNode *head) {
       if (head == nullptr | head->next == nullptr) return head;
        ListNode *dummyHead = new ListNode(-1);
        ListNode *dummyCurser = dummyHead;
```

```
while (head->next != nullptr) {
            ListNode *cur = head->next;
            ListNode *pre = head; // pre指向头结点
            while (cur->next != nullptr) {
                if (cur->val < cur->next->val) {
                    ListNodeSwap(pre, cur, cur->next);
                } else {
                    cur = cur->next;
                pre = pre->next;
            cout << "cur is " << cur->val << endl;</pre>
            dummyCurser->next = cur;
            dummyCurser = dummyCurser->next;
            pre->next = nullptr;
        return dummyHead->next;
    }
};
int main() {
    vector<int> nums{12, 25, 36, 17, 78, 65, 25, 56, 1};
    ListNode *head = new ListNode(-1);
    ListNode *cur = head;
    for (int i = 0; i < nums.size(); ++i) {</pre>
        cur->next = new ListNode(nums[i]);
        cur = cur->next;
    cout << Solution::ppint(head->next) << endl;</pre>
    Solution solution;
    ListNode *res = solution.BubbleSort(head);
    cout << Solution::ppint(res) << endl;</pre>
}
```

拓扑排序

```
#include <vector>
#include <queue>

using namespace std;

const int MAX_VERTEX_NUM = 20; //图中顶点的最大数量

struct Node {
  int data;
```

```
char *info;
};
struct MGraph {
   vector<vector<int>>> edges;
   Node node[MAX_VERTEX_NUM];
                                  //存储图中顶点数据
   int edgesCount, nodesCount;
};
struct ArcNode {
                            //存储边或弧,即另一端顶点在数组中的下标
   int adjvex;
   struct ArcNode *nextarc;//指向下一个结点
                       //记录边或弧的其它信息
   int info;
};
struct VNode {
   int data;
                    //顶点的数据域
   ArcNode *firstarc;//指向下一个结点
};//存储各链表首元结点的数组
struct ALGraph {
   VNode vertices[MAX_VERTEX_NUM]; //存储图的邻接表
   int nodesCount, edgesCount;
                                          //记录图中顶点数以及边或弧数
};
ALGraph *MGraphToALGraph(MGraph graph) {
   //初始化邻接表
   ALGraph *alGraph = new ALGraph;
   alGraph->nodesCount = graph.nodesCount;
   alGraph->edgesCount = graph.edgesCount;
   for (int i = 0; i < graph.nodesCount; ++i) {</pre>
       alGraph->vertices[i].firstarc = nullptr;
   }
   for (int i = 0; i < graph.nodesCount; ++i) {</pre>
       for (int j = 0; j < graph.nodesCount; ++j) {</pre>
           if (graph.edges[i][j] != 0) {
               ArcNode *arcNode = new ArcNode;
               arcNode->adjvex = j;
               arcNode->info=graph.edges[i][j];
               // head insert
               arcNode->nextarc = alGraph->vertices[i].firstarc;
               alGraph->vertices[i].firstarc = arcNode;
       }
   }
```

```
return alGraph;
}
class Solution {
private:
   // 存储有向图
   vector<vector<int>>> edges;
   // 存储每个节点的入度
   vector<int> indegrees;
   // 存储拓扑排序序列
   vector<int> result;
public:
   // prerequisites = [[1,0],[2,0],[3,1],[3,2]] 有向图
   vector<int> findOrder(int numCourses, vector<vector<int>>& prerequisites) {
       edges.resize(numCourses);
       indegrees.resize(numCourses);
       for (const auto& info: prerequisites) {
           edges[info[0]].push_back(info[1]);
           ++indegrees[info[1]];
       }
       queue<int> q;
       // 将所有入度为 0 的节点放入队列中
       for (int i = 0; i < numCourses; ++i) {</pre>
           if (indegrees[i] == 0) {
               q.push(i);
       }
       while (!q.empty()) {
           // 从队首取出一个节点
           int u = q.front();
           q.pop();
           // 放入答案中
           result.push_back(u);
           for (int v: edges[u]) {
               --indegrees[v];
               // 如果相邻节点 v 的入度为 0, 就可以选 v 对应的课程了
               if (indegrees[v] == 0) {
                   q.push(v);
               }
           }
       }
       if (result.size() != numCourses) {
           // 没有一个拓扑排序
           return {};
       }
```

```
// 返回拓扑排序
return result;
}
};
```