

STATISTICS

ASSIGNMENT (CONFIDENCE INTERVALS)

EXERCISE 1.

Suppose scores on exams in statistics are normally distributed with an unknown population mean and a population standard deviation of 3 points. A random sample of 36 scores is taken and gives a sample mean (sample mean score) of 68. Find a confidence interval estimate for the population mean exam score (the mean score on all exams).

Find a 90% confidence interval for the true (population) mean of statistics exam scores.

Solution:

$$S_x=3$$

$$n=36$$

$$\bar{X}=68$$

%90 confidence interval-one sample test:

$$(68-1,645.3/\sqrt{36}, 68+1,645.3/\sqrt{36})=(67.17, 68.82)$$

EXERCISE 2.

What is the normal body temperature for healthy humans? A random sample of 130 healthy human body temperatures provided by Allen Shoemaker⁷ yielded 98.25 degrees and standard deviation 0.73 degrees.

Give a 99% confidence interval for the average body temperature of healthy people.

Solution:

$$n=130$$

$$\bar{X}=98,25$$

$$S_x=0,73$$

%99 confidence Interval:

$$(98.25-2.58*0.73/\sqrt{130}) , (98.25+2.58*0.73/\sqrt{130})=97.09 , 98.41$$

EXERCISE 3.

The administrators for a hospital wished to estimate the average number of days required for inpatient treatment of patients between the ages of 25 and 34. A random sample of 500 hospital patients between these ages produced a mean and standard deviation equal to 5.4 and 3.1 days, respectively.

Construct a 95% confidence interval for the mean length of stay for the population of patients from which the sample was drawn.

Solution:

$$n=500$$

$$S_x=5,4$$

$$\bar{X}=3,1$$

%95 lik güven aralığı için :

$$(3.1-1.96*5.4/\sqrt{500}, 3.1+1.96*5.4/\sqrt{500})=(2.62, 3.57)$$