

Assignment: Comparison of Prim and Dijkstra's Algorithm

Low level Pseudo code:

Algorithm: Prim-MST (G)

Input: Graph $G=(V,E)$ with edge-weights.

```
// Initialize priorities and place in priority
queue.
1.  priority[i] = infinity for each vertex i
2.  Insert vertices and priorities into
priorityQueue;
    // Set the priority of vertex 0 to 0.
3.  priorityQueue.decreaseKey (0, 0) //

// Process vertices one by one in order of priority

4.  while priorityQueue.notEmpty()
    // Get "best" vertex out of queue.
5.    v = priorityQueue.extractMin()
6.    Add v to MST;
    // Explore edges from v.
7.    for each edge e=(v, u) in adjList[v]
8.        w = weight of edge e=(v, u);

// If it's shorter to get to MST via v, then update.
9.        if priority[u] > w
10.           priorityQueue.decreaseKey (u, w)
11.           predecessor[u] = v
12.        endif
13.    endfor
14. endwhile

15. Build MST;
16. return MST
```

Output: A minimum spanning tree of the graph G.

Source: pseudo code modified by tjk

<http://www.seas.gwu.edu/~simhaweb/alg/lectures/module8/module8.html>

Low level Pseudo code:

Algorithm: Dijkstra-SPT (G, s)

Input: Graph $G=(V,E)$ with non-negative edge weights and designated source vertex s.

```
// Initialize priorities and place in priority
queue.
1. priority[i] = infinity for each vertex i;
2. Insert vertices and priorities into priorityQueue;
    // Source s has priority 0
3. priorityQueue.decreaseKey (s, 0)

// Process vertices one by one in order of priority

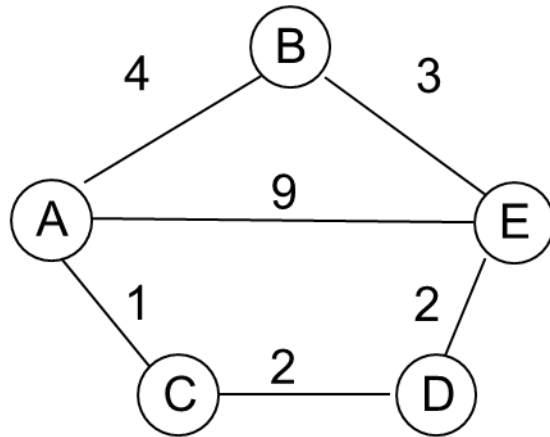
4. while priorityQueue.notEmpty()
    // Get "best" vertex out of queue.
5.    v = priorityQueue.extractMin()
6.    Add v to SPT;
    // Explore edges from v.
7.    for each edge e=(v, u) in adjList[v]
8.        w = weight of edge e=(v, u);

// If it's shorter to get to u from s via v, update.
9.        if priority[u] > priority[v] + w
10.           priorityQueue.decreaseKey (u,
priority[v]+w)
11.           predecessor[u] = v
12.        endif
13.    endfor
14. endwhile

15. Build SPT;
16. return SPT
```

Output: Shortest Path Tree (SPT) rooted at s.

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PRIM'S ALGORITHM (prev, dist)

MST	A	B	C	D	E
INIT/SetStart	<u>(-, 0)</u>	(-, ∞)	(-, ∞)	(-, ∞)	(-, ∞)
A	(-, 0)	(A, 4)	<u>(A, 1)</u>	(-, ∞)	(A, 9)
C	(-, 0)	(A, 4)	(A, 1)	<u>(C, 2)</u>	(A, 9)
D	(-, 0)	(A, 4)	(A, 1)	(C, 2)	<u>(D, 2)</u>
E	(-, 0)	<u>(E, 3)</u>	(A, 1)	(C, 2)	(D, 2)
B	(-, 0)	(E, 3)	(A, 1)	(C, 2)	(D, 2)

DIJKSTRA'S ALGORITHM (prev, dist)

MST	A	B	C	D	E
INIT/ SetStart	<u>(-, 0)</u>	(-, ∞)	(-, ∞)	(-, ∞)	(-, ∞)
A	(-, 0)	(A, 4)	<u>(A, 1)</u>	(-, ∞)	(A, 9)
C	(-, 0)	(A, 4)	(A, 1)	<u>(C, 3)</u>	(A, 9)
D	(-, 0)	<u>(A, 4)</u>	(A, 1)	(C, 3)	(D, 5)
B	(-, 0)	(A, 4)	(A, 1)	(C, 3)	<u>(D, 5)</u>
E	(-, 0)	(A, 4)	(A, 1)	(C, 3)	(D, 5)