point-neuron-network-simulator

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May 23, 2016

1 Simulator Overview

• simple

Spike interaction happens at the end of each dt. Poisson input still injected at the exact timing.

• SSC

Spike-spike correction.

• SSC-Sparse

Spike-spike correction, optimized for sparse network.

• SSC-Sparse2

Spike-spike correction, optimized for sparse network, version 2.

• big-delay

Network with constant delay. The delay must larger than 1dt (hence the name "big"). Use option "-synaptic-delay" to set the delay.

• big-net-delay

Network with delay. The delay is set by a "delay matrix", by passing a text numerical matrix file path to the option "—synaptic-net-delay".

• cont-syn

Simulate the network with continuous synaptic interaction. Specially for model "HH-GH-cont-syn".

• auto

Auto choose a simulator according to the neuronal model.

Table 1: Compatibility matrix

	simple	SSC/SSC-Sparse/	cont-syn	big-delay	big-net-delay	auto
		SSC-Sparse2				
LIF-G/LIF-GH	y	у	-	-	-	SSC
HH-G/HH-GH	у	У	-	-	-	SSC
HH-GH-cont-syn	-	-	у	-	-	cont-syn
-synaptic-delay	-	-	-	у	-	big-delay
-synaptic-net-delay	-	-	-	-	У	big-net-delay
-sine						
-extI						

$\mathbf{2}$ Neuron Model Used

HH-GH 2.1

It is the classical Hodgkin-Huxley (HH) neuron model. For neuron i, its membrane potential V_i obey

$$\begin{cases} C \frac{\mathrm{d}V_i}{\mathrm{d}t} = -(V_i - V_{\mathrm{Na}})G_{\mathrm{Na}}h_i m_i^3 - (V_i - V_{\mathrm{K}})G_{\mathrm{K}}n_i^4 - (V_i - V_{\mathrm{L}})G_{\mathrm{L}} + I_i^{\mathrm{input}} \\ \frac{\mathrm{d}m_i}{\mathrm{d}t} = (1 - m_i)\alpha_m(V_i) - m_i\beta_m(V_i) \\ \frac{\mathrm{d}h_i}{\mathrm{d}t} = (1 - h_i)\alpha_h(V_i) - h_i\beta_h(V_i) \\ \frac{\mathrm{d}n_i}{\mathrm{d}t} = (1 - n_i)\alpha_n(V_i) - n_i\beta_n(V_i) \end{cases}$$

$$(1)$$

where

$$\alpha_n(V_i) = \frac{0.1 - 0.01V_i}{\exp(1 - 0.1V_i) - 1} \qquad \beta_n(V_i) = 0.125 \exp(-V_i/80)$$

$$\alpha_m(V_i) = \frac{2.5 - 0.1V_i}{\exp(2.5 - 0.1V_i) - 1} \qquad \beta_m(V_i) = 4 \exp(-V_i/18)$$

$$\alpha_h(V_i) = 0.07 \exp(-V_i/20) \qquad \beta_h(V_i) = \frac{1}{\exp(3 - 0.1V_i) + 1}$$

 $V_i, m_i, n_i, h_i, I_i^{\mathrm{input}}$ are functions of t, and others are constants: $V_{\mathrm{Na}} = 115\,\mathrm{mV}, V_{\mathrm{K}} = -12\,\mathrm{mV}, V_{\mathrm{L}} = 10.6\,\mathrm{mV}$ (resting potential set to $0\,\mathrm{mV}$), $G_{\mathrm{Na}} = 120\,\mathrm{mS}\cdot\mathrm{cm}^{-2}, G_{\mathrm{K}} = 36\,\mathrm{mS}\cdot\mathrm{cm}^{-2}, G_{\mathrm{L}} = 0.3\,\mathrm{mS}\cdot\mathrm{cm}^{-2}$ and membrane capacity $C = 1 \,\mu\text{F} \cdot \text{cm}^{-2}$.

The interaction between neurons and external inputs come from I_i^{input}

$$I_i^{\text{input}} = I_i^{\text{E}} + I_i^{\text{I}},\tag{2}$$

$$I_i^{\rm E} = -(V_i - V_G^{\rm E})G_i^{\rm E}, \quad I_i^{\rm I} = -(V_i - V_G^{\rm I})G_i^{\rm I}$$
 (3)

 $I_i^{\rm E},~I_i^{\rm I}$ are excitatory and inhibitory input respectively, and $V_G^{\rm E},~V_G^{\rm I}$ is their reversal potential. conductances G_i^Q ($Q \in \{{\rm E},{\rm I}\}$) evolves according to The

$$\frac{\mathrm{d}G_i^Q}{\mathrm{d}t} = -\frac{G_i^Q}{\sigma_r^Q} + H_i^Q,\tag{4}$$

$$\frac{\mathrm{d}H_i^Q}{\mathrm{d}t} = -\frac{H_i^Q}{\sigma_d^Q} + \sum_k F_i^Q \delta(t - T_{i,k}^F) + \sum_{j \neq i} S_{ij} \delta(t - T_j^S)$$
(5)

where F_i^Q is the strength of external input to neuron i, $T_{i,k}^F$ is its time of k-th input event, which is a Poisson process with rate μ_i . We call this term the Poisson input. S_{ij} is the coupling strength from j-th neuron to i-th neuron. σ_r^Q , σ_d^Q are the fast rising and slow decaying timescales in the α function. $V_G^{\rm E}=65\,{\rm mV},\,V_G^{\rm I}=-15\,{\rm mV},\,\sigma_c^F=0.5,\,\sigma_d^E=3.0,\,\sigma_r^I=0.5,\,\sigma_d^I=7.0.$ We use adjacency matrix $A=(A_{ij})$ to denote the neural network structure, i.e. $S_{ij}=A_{ij}S^{Q_iQ_j}$, and $S^{Q_iQ_j}$ is one of $S^{\rm EE},\,S^{\rm EI},\,S^{\rm IE},\,S^{\rm II}$, depends on the type of corresponding neuron pair (E for excitatory, I

for inhibitory). $A_{ij} \neq 0$ means there is a direct affection to i-th neuron from j-th neuron.

 $F, \mu, A, S^{Q_i Q_j}, \sigma_r^Q, \sigma_d^Q$ are parameters relate to synaptic and input to neurons. For all neurons $F_i^{\rm E} = F, F_i^{\rm I} = 0, \mu_i = \mu$. During one simulation, these parameters are all constant.

The threshold is 65 mV above the resting potential (0 mV). And the synaptic interaction is performed at the time of this crossing.

In numerical simulation, we use explicit fourth-order Runge-Kutta method with time step 1/32 ms. When we talk about spike train data, we mean $x_t = 1$ if $V_i(t)$ just pass through the threshold from low to high, otherwise $x_t = 0$.

2.2 HH-G

Eq. (4)(5) change to

$$\frac{\mathrm{d}G_i^Q}{\mathrm{d}t} = -\frac{G_i^Q}{\sigma_r^Q} + \sum_k F_i^Q \delta(t - T_{i,k}^F) + \sum_{j \neq i} S_{ij} \delta(t - T_j^S),\tag{6}$$

2.3 HH-GH-cont-syn

Eq. (5) change to

$$\frac{\mathrm{d}H_i^Q}{\mathrm{d}t} = -\frac{H_i^Q}{\sigma_d^Q} + \sum_k F_i^Q \delta(t - T_{i,k}^F) + \sum_{j \neq i} S_{ij} g(V_j^{\mathrm{pre}}),\tag{7}$$

$$g(V_j^{\text{pre}}) = 1/\left(1 + \exp(-(V_j^{\text{pre}} - 85 \,\text{mV})/2)\right).$$
 (8)

 V_i^{pre} is the (presynaptic) membrane potential of j-th neuron.

Note: In this model, the voltage is scaled as V/10.

2.4 HH-PT-GH

Same as HH-GH, except that the spike timing is at the spike peak.

3 Neuron Properties

3.1 Single neuron property (HH-G, HH-GH, HH-GH-cont-syn)

3.1.1 Setting threshold

A common setting for threshold is 15 mV above the resting state.

From Fig.(1) we can see that there is some non-spike been counted as spike.

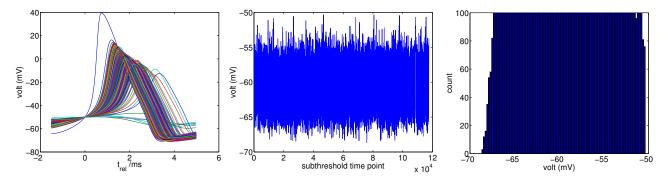


Figure 1: Threshold= $-65 + 15 \,\text{mV}$, HH-GH, pr= $10.0 \,\text{kHz}$, ps= $0.05 \,\Omega^{-1} \text{ms}^{-2}$ (strong input, 97 Hz)

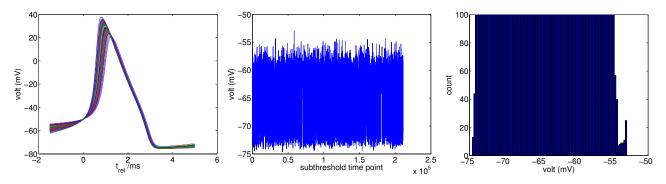


Figure 2: Threshold= $-65 + 15 \,\mathrm{mV}$, HH-GH, pr= $2.0 \,\mathrm{kHz}$, ps= $0.05 \,\Omega^{-1} \mathrm{ms}^{-2}$ (median input, $52 \,\mathrm{Hz}$)

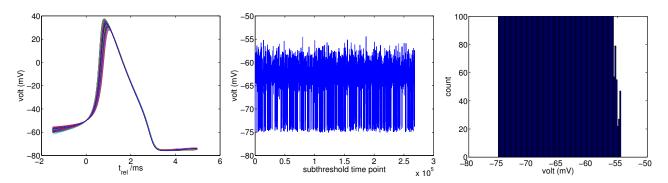


Figure 3: Threshold= $-65 + 15 \,\text{mV}$, HH-GH, pr= $1.0 \,\text{kHz}$, ps= $0.04 \,\Omega^{-1} \text{ms}^{-2}$ (low input, 24 Hz)

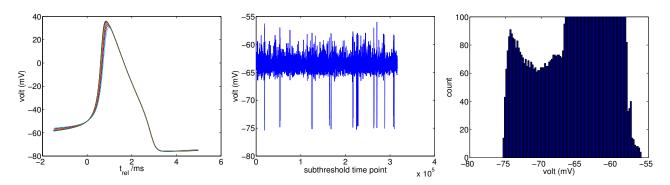
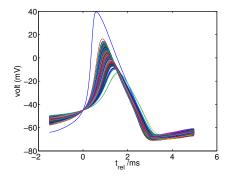


Figure 4: Threshold= $-65 + 15 \,\text{mV}$, HH-GH, pr= $1.0 \,\text{kHz}$, ps= $0.02 \,\Omega^{-1} \text{ms}^{-2}$ (tiny input, $1.4 \,\text{Hz}$)

3.1.2 Higher threshold

Use 20 mV above resting as threshold.

(Fig.(5)) Compare to Fig.(1), we see no mis-counted spikes, and the timing is more accurate.



 $\label{eq:figure 5: Threshold} Figure \ 5: \ Threshold = -65 + 20 \, mV, \ HH-GH, \ pr = 10.0 \, kHz, \ ps = 0.05 \, \Omega^{-1} ms^{-2} \ (strong \ input, \ 97 \, Hz).$

Use 84 mV above resting as threshold.

Reason: In "HH-GH-cont-syn" model, only when volt above around 85 mV will the synaptic transmit a signal. In function Eq.(8), $g(84 \,\mathrm{mV}) \approx 0.0067$, $g(85 \,\mathrm{mV}) = 0.5$.

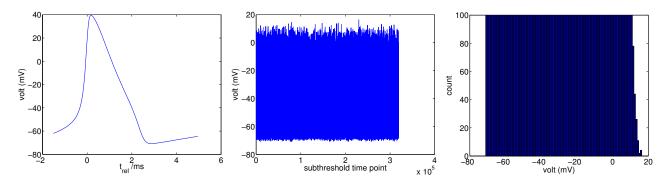


Figure 6: Threshold= $-65 + 84 \,\mathrm{mV}$. Strong input, (see Fig. (1)). Essentially all spikes are "missed".

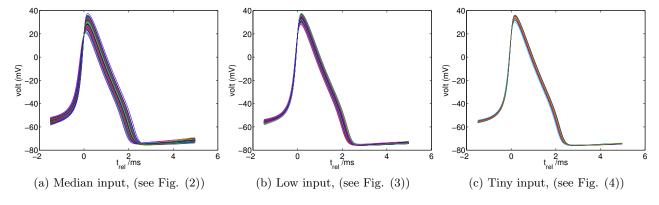


Figure 7: Threshold= $-65 + 84 \,\text{mV}$.

3.1.3 Discussion of the "threshold"

The concept of the threshold actually has two distinct meanings:

- 1. Once the voltage pass it (from low to high), then the neuron will fire (sooner or later).
- 2. The neuron will sent a signal to it down stream around this time.

A related fact is that (in this model, with Poisson input), the action potential is not in a fixed size, there are big and small action potentials. This is what makes the above two concepts essentially differ.

In the simulation and exact understanding of spiking dynamics. The concept 2 is desired. The proper timing should be the peak time.

4 Convergence

refer to code
mfile/HH_test_convergence.m
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