

Consensus Convolutional Sparse Coding

Biswarup Choudhury¹, Robin Swanson², Felix Heide³, Gordon Wetzstein³, Wolfgang Heidrich¹

1. King Abdullah University of Science and Technology (KAUST)

2. University of Toronto 3. Stanford University

Abstract

Convolutional sparse coding (CSC) is a promising direction for unsupervised learning in computer vision. In contrast to recent supervised methods, CSC allows for convolutional image representations to be learned that are equally useful for high-level vision tasks and low-level image reconstruction and can be applied to a wide range of tasks without problem-specific retraining. Due to their extreme memory requirements, however, existing CSC solvers have so far been limited to low-dimensional problems and datasets using a handful of low-resolution example images at a time.

In this paper, we propose a new approach to solving CSC as a consensus optimization problem, which lifts these limitations. By learning CSC features from large-scale image datasets for the first time, we achieve significant quality improvements in a number of imaging tasks. Moreover, the proposed method enables new applications in high dimensional feature learning that has been intractable using existing CSC methods. This is demonstrated for a variety of reconstruction problems across diverse problem domains, including 3D multispectral demosaicking and 4D light field view synthesis.

Mathematical Framework

Classical CSC learning

$$\operatorname{argmin}_{d,z} \frac{1}{2} \sum_{j=1}^n (\|b_j - DZ_j\|_2^2 + \beta \sum_{w=1}^W \|z_{jw}\|_1) + \sum_{w=1}^W \operatorname{ind}_c(d_w)$$

- b_j is our dataset used for learning ($j \in [1, n]$)
- z_{jw} are the w sparse feature maps corresponding to element j
- For good feature learning, n is often very large!

- Partition data matrix \mathbf{b} and feature maps \mathbf{Z} as

$$\mathbf{b} = \begin{bmatrix} b_1 \\ \vdots \\ b_j \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ b_i \\ \vdots \\ b_N \end{bmatrix}, \quad \mathbf{Z} = \begin{bmatrix} Z_1 \\ \vdots \\ Z_i \\ \vdots \\ Z_N \end{bmatrix}$$

- b_i : i^{th} block of data with respective Z_i ($i \in [1, N]$, $N \leq n$)

- Can each block be handled independently? D ?
- To facilitate independence of each block:

$$\operatorname{argmin}_{d_i, Z_i} \sum_{i=1}^n \frac{1}{2} \|b_i - Z_i D_i\|_2^2 + \|Z_i\|_1 + \operatorname{ind}_c(D_i)$$

- Multiple kernels D_i ?
- Desire single kernel for entire data matrix \mathbf{b}
- Add equality constraint on the D_i

$$\operatorname{argmin}_{D_i} \frac{1}{2} \|b_i - Z_i D_i\|_2^2 + \|Z_i\|_1 + \operatorname{ind}_c(y)$$

subject to $D_i - y = 0, i = 1, \dots, N$

Global Consensus Form

- Consensus among local variables D_i to be equal
- Each equal to global variable y

Consensus CSC learning

ADMM Algorithm for d^{opt}

```

1: for all  $k = 1$  to  $V$  do
2:   for all  $i = 1$  to  $N$  do
3:      $D_i^{k+1} := \operatorname{argmin}_{D_i} \left( \left( \frac{1}{2} \right) \|b_i - Z_i D_i\|_2^2 + (\rho/2) \|D_i - y^k + u_i^k\|_2^2 \right)$ 
4:   end for
5:    $\bar{D}^{k+1} = \frac{1}{N} \sum_{i=1}^N D_i^{k+1}$ 
6:    $\bar{u}^k = \frac{1}{N} \sum_{i=1}^N u_i^k$ 
7:    $y^{k+1} := \operatorname{argmin}_y \left( \operatorname{ind}_c(y) + (N\rho/2) \|y - \bar{D}^{k+1} - \bar{u}^k\|_2^2 \right)$ 
8:   for all  $i = 1$  to  $N$  do
9:      $u_i^{k+1} := u_i^k + D_i^{k+1} - y^{k+1}$ 
10:  end for
11: end for
12:  $D^{opt} = y^{k+1}$ 

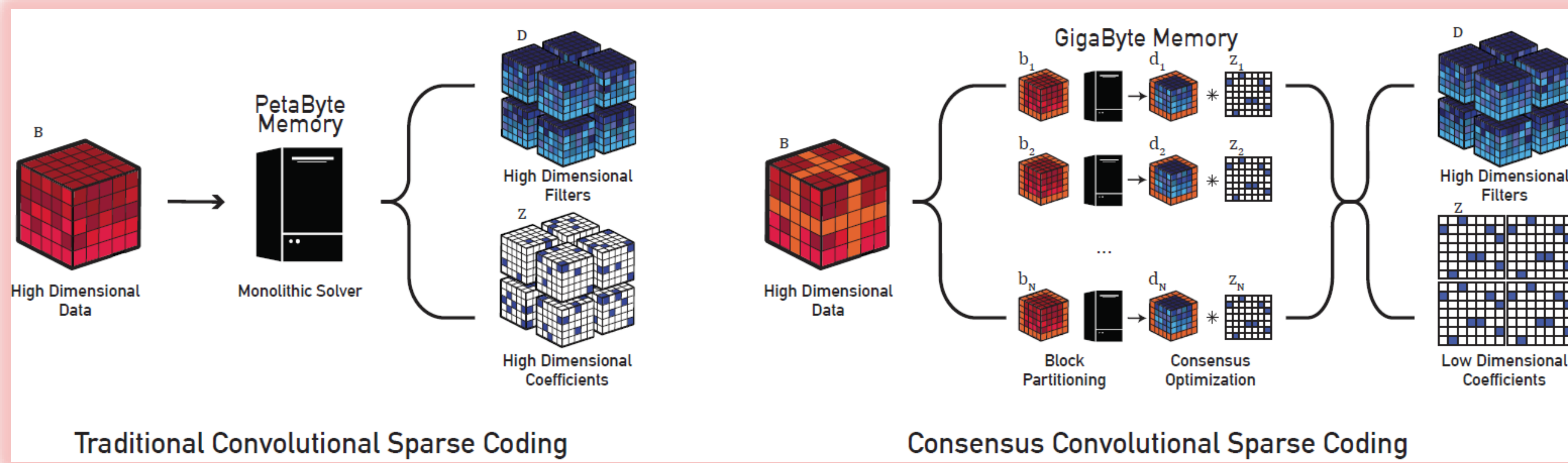
```

ADMM Algorithm for Z_i^{opt}

```

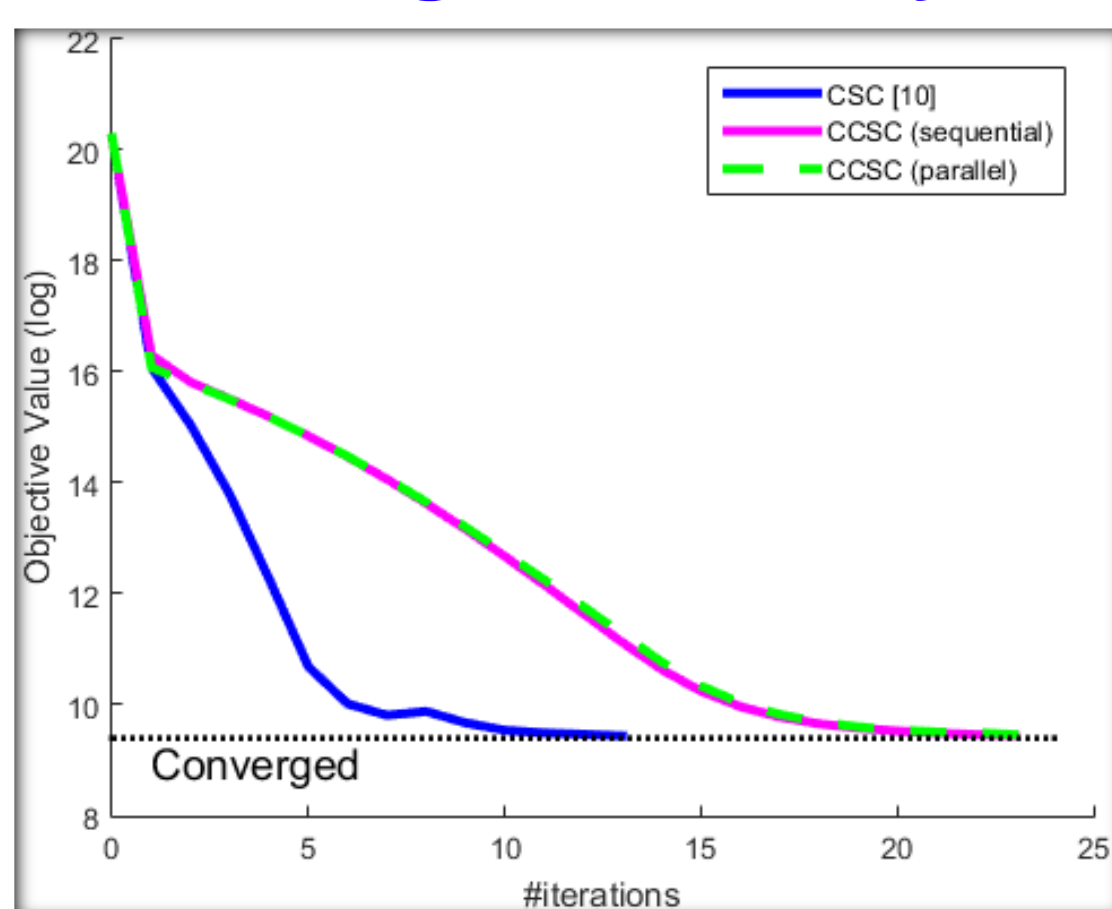
1: for all  $i = 1$  to  $N$  do
2:   for all  $k = 1$  to  $V$  do
3:      $Z_i^{k+1} := \operatorname{argmin}_{Z_i} \left( \left( \frac{1}{2} \right) \|b_i - D_i Z_i\|_2^2 + (\rho/2) \|Z_i - y_i^k + u_i^k\|_2^2 \right)$ 
4:      $y_i^{k+1} := \operatorname{argmin}_{y_i} \left( \beta \|y_i\|_1 + (\rho/2) \|y_i - Z_i^{k+1} - u_i^k\|_2^2 \right)$ 
5:      $u_i^{k+1} := u_i^k + Z_i^{k+1} - y_i^{k+1}$ 
6:   end for
7:    $Z_i^{opt} = Z_i^{k+1}$ 
8: end for

```

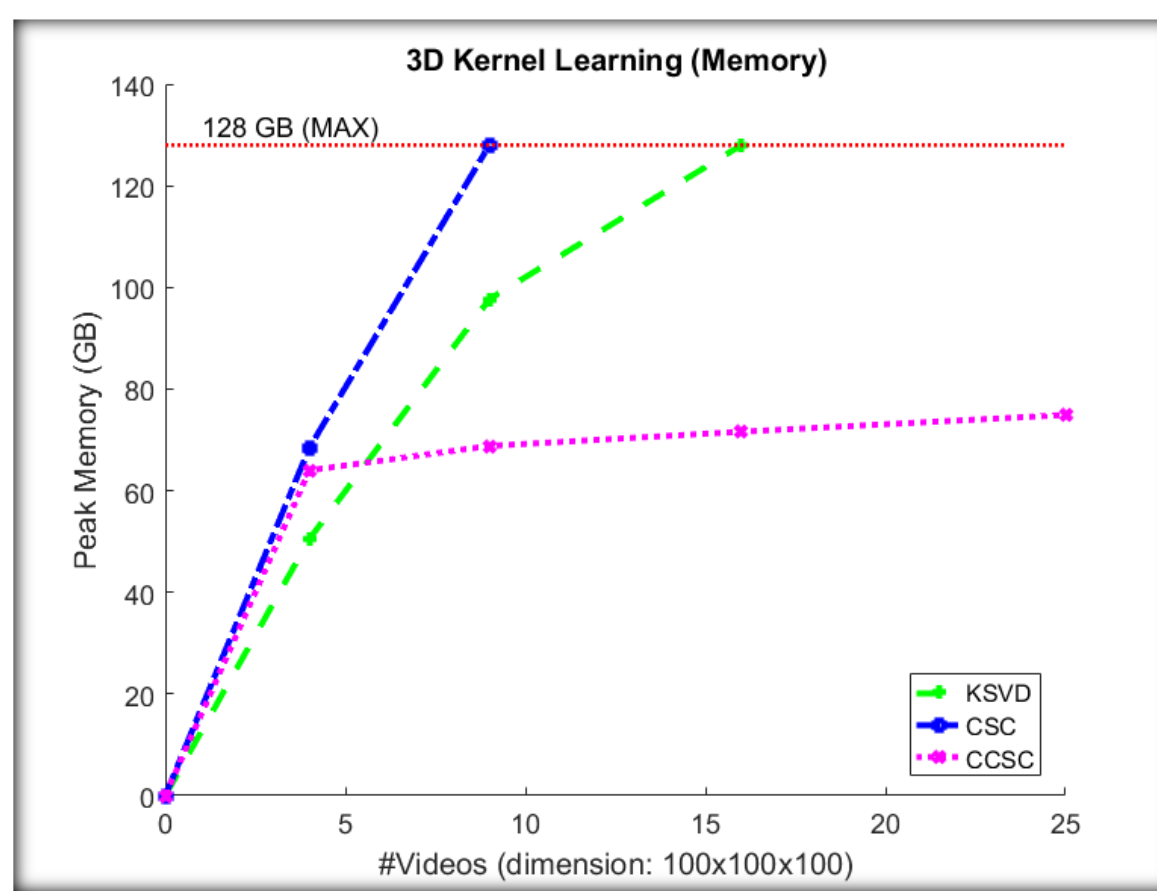
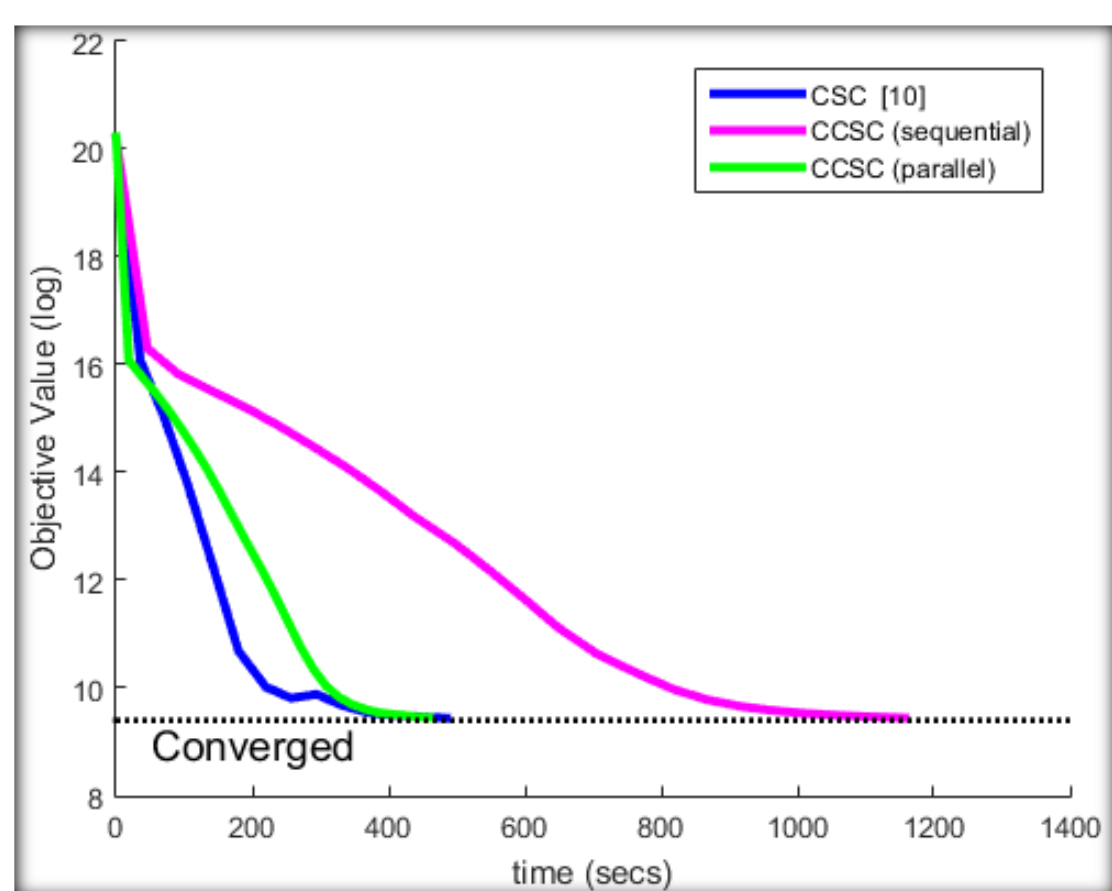
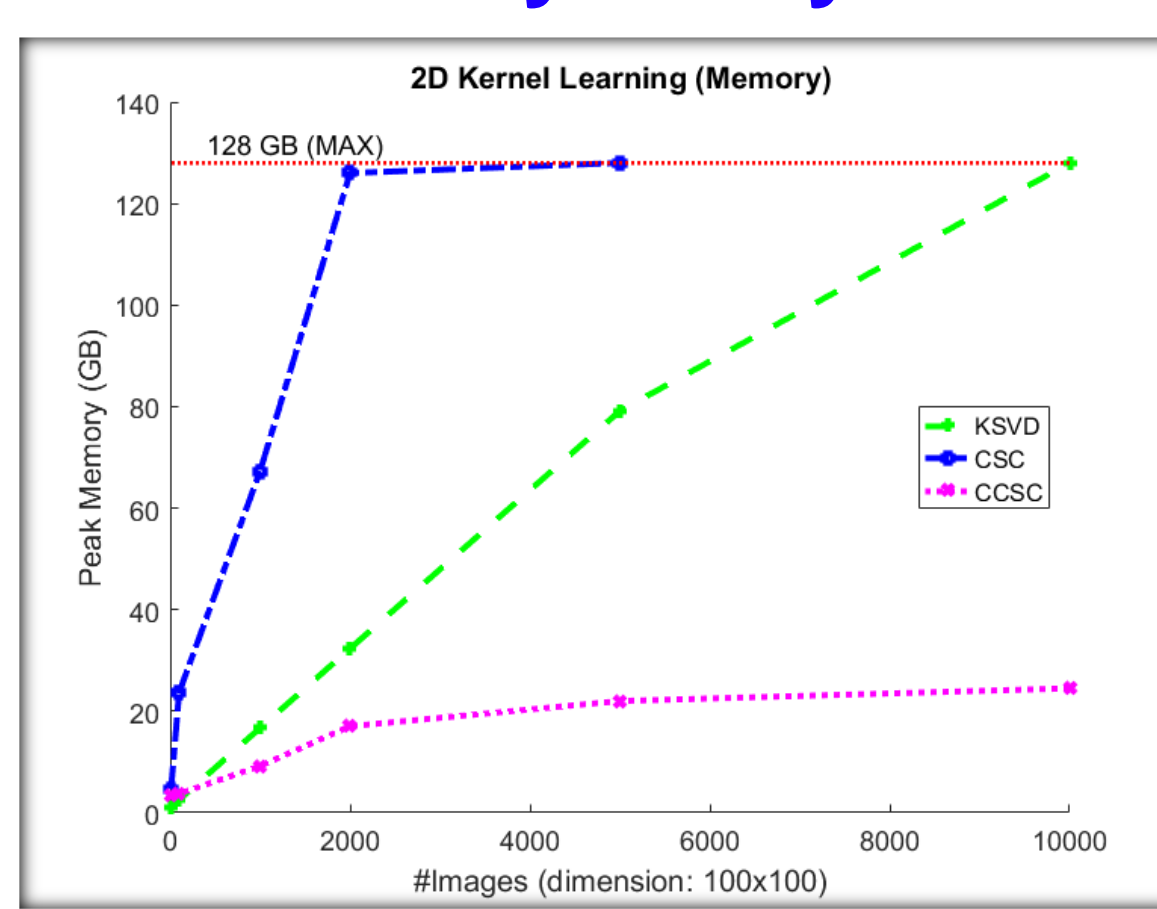


Evaluation

Convergence Analysis



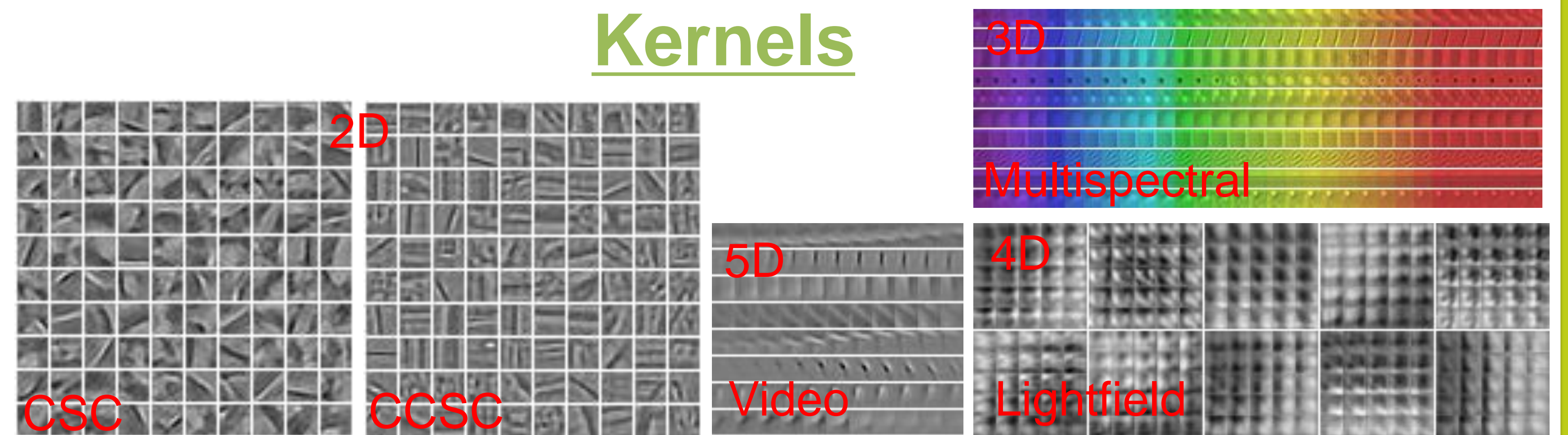
Memory Analysis



Runtime Analysis

2D Dataset Size	Classical CSC (sec.)	CCSC (U = #PCs) (sec.)		
		U=5	U=10	U=50
100	203.56	35.35	25.69	25.20
500	1530.71	259.30	82.69	28.57
1000	Out of Memory!	387.68	255.38	35.63

Kernels



Results

