Boolean Axioms

	Axiom		Dual	Name
A1	$B = 0 \text{ if } B \neq 1$	A1′	$B = 1 \text{ if } B \neq 0$	Binary field
A2	$\overline{0} = 1$	A2′	$\overline{1} = 0$	NOT
A3	$0 \bullet 0 = 0$	A3′	1 + 1 = 1	AND/OR
A4	1 • 1 = 1	A4′	0 + 0 = 0	AND/OR
A5	$0 \bullet 1 = 1 \bullet 0 = 0$	A5'	1 + 0 = 0 + 1 = 1	AND/OR

	Theorem		Dual	Name
T1	$B \bullet 1 = B$	T1'	B+0=B	Identity
T2	$B \bullet 0 = 0$	T2'	B + 1 = 1	Null Element
Т3	$B \bullet B = B$	T3'	B + B = B	Idempotency
T4		$\bar{\bar{B}} = B$		Involution
T5	$B \bullet \overline{B} = 0$	T5'	$B + \overline{B} = 1$	Complements



Boolean Theorems of Several Variables

	Theorem		Dual	Name
T6	$B \bullet C = C \bullet B$	T6′	B + C = C + B	Commutativity
T 7	$(B \bullet C) \bullet D = B \bullet (C \bullet D)$	T7'	(B+C)+D=B+(C+D)	Associativity
T8	$(B \bullet C) + B \bullet D = B \bullet (C + D)$	T8'	$(B+C) \bullet (B+D) = B + (C \bullet D)$	Distributivity
T9	$B \bullet (B + C) = B$	T9′	$B + (B \bullet C) = B$	Covering
T10	$(B \bullet C) + (B \bullet \overline{C}) = B$	T10'	$(B + C) \bullet (B + \overline{C}) = B$	Combining
T11	$(B \bullet C) + (\overline{B} \bullet D) + (C \bullet D)$	T11'	$(B + C) \bullet (\overline{B} + D) \bullet (C + D)$	Consensus
	$= B \bullet C + \overline{B} \bullet D$		$= (B + C) \bullet (\overline{B} + D)$	
T12	$B_0 \bullet B_1 \bullet B_2 \dots$	T12'	$B_0 + B_1 + B_2$	De Morgan's
	$= (\overline{B_0} + \overline{B_1} + \overline{B_2} \dots)$		$= (\overline{B_0} \bullet \overline{B_1} \bullet \overline{B_2})$	Theorem

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