



THE STATE UNIVERSITY  
OF NEW JERSEY

# ECE-332:437

# DIGITAL SYSTEMS DESIGN (DSD)

## Fall 2016 – Lecture 1

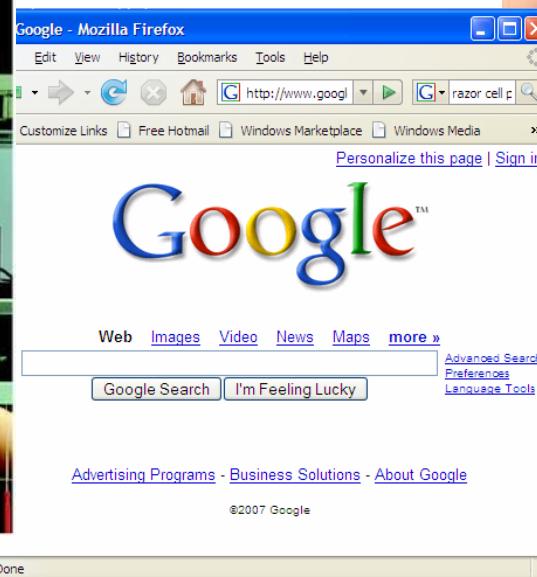
Nagi Naganathan  
September 8, 2016

# Chapter 1 :: Topics

- **Background**
- **The Game Plan**
- **The Art of Managing Complexity**
- **The Digital Abstraction**
- **Number Systems**
- **Logic Gates**
- **Logic Levels**
- **CMOS Transistors**
- **Power Consumption**

# Background

- Microprocessors have revolutionized our world
  - Cell phones, Internet, rapid advances in medicine, etc.
- The semiconductor industry has grown from \$21 billion in 1985 to over \$300 billion in 2013



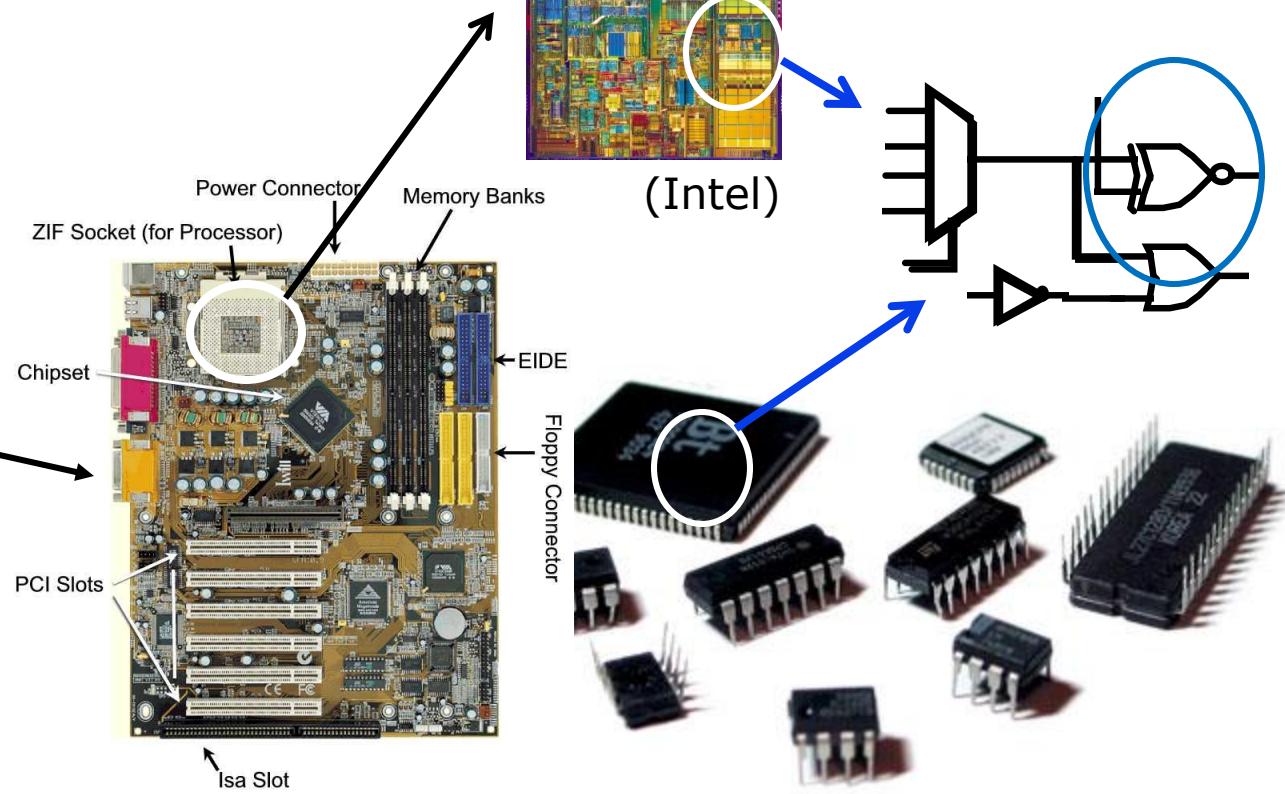
# The Game Plan

- Purpose of course:
  - Understand what's under the hood of a computer
  - Learn the principles of digital design
  - Learn to systematically debug increasingly complex designs
  - Design and build a microprocessor

FROM ZERO TO ONE

# Digital Logic Design

Deals with building blocks of digital systems



# Topics to cover today – September 8, 2016

- Lecture 1
  - Historical Perspectives
  - Basic Hardware Concepts
  - Integrated Circuits
  - Digital Devices
  - Analog vs Digital
  - Basic Boolean Gates
- Lecture 2
  - Number systems
  - Representation of negative numbers
  - 2's complement
  - Binary addition, subtraction

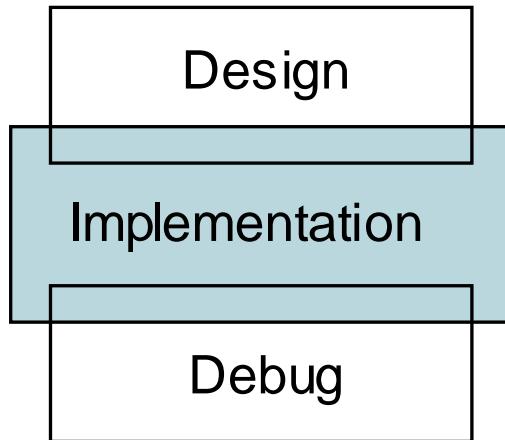
# Part 1

# Historical Perspectives

# General Principles

- Technology changes fast
  - State-of-the-art this year becomes obsolete next week
- Understand general principles
  - Apply Problem Solving Principles
  - Optimization, Tradeoffs
- Concepts remain the same:
  - Example: relays -> tubes -> bipolar transistors -> MOS transistors

# The Process of Design



## *Design*

**Initial concept: what is the function performed by the object?**

**Constraints: How fast? How much area? How much cost?**

**Refine abstract functional blocks into more concrete realizations**

## *Implementation*

**Assemble primitives into more complex building blocks**

**Composition via wiring**

**Choose among alternatives to improve the design**

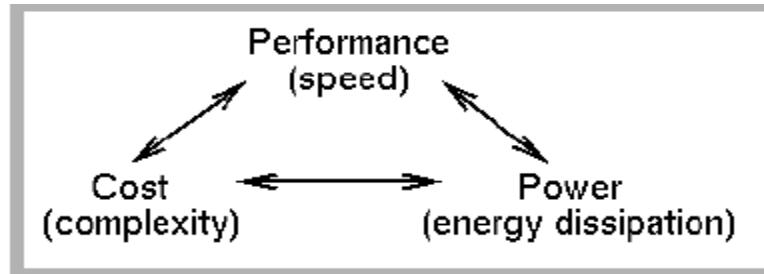
## *Debug*

**Faulty systems: design flaws, composition flaws, component flaws**

**Design to make debugging easier**

**Hypothesis formation and troubleshooting skills**

# Design Tradeoffs



- You can improve on one at the expense of worsening one or both of the others.
- These tradeoffs exist at every level in the system design - every sub-piece and component.
- Design Specification -
  - Functional Description.
  - Performance, cost, power constraints.
- As a designer you must make the tradeoffs necessary to achieve the function within the constraints.

# Themes in Digital Design

## IMPORTANT THEMES IN DIGITAL DESIGN

- Good tools do not guarantee good design, but they help a lot by taking the pain out of doing things right.
- Digital circuits have analog characteristics.
- Know when to worry and when not to worry about the analog aspects of digital design.
- Always document your designs to make them understandable by yourself and others.
- Associate active levels with signal names and practice bubble-to-bubble logic design.
- Understand and use standard functional building blocks.
- Design for minimum cost at the system level, including your own engineering effort as part of the cost.
- State-machine design is like programming; approach it that way.
- Use programmable logic to simplify designs, reduce cost, and accommodate last-minute modifications.
- Avoid asynchronous design. Practice synchronous design until a better methodology comes along.
- Pinpoint the unavoidable asynchronous interfaces between different subsystems and the outside world, and provide reliable synchronizers.
- Catching a glitch in time saves nine.

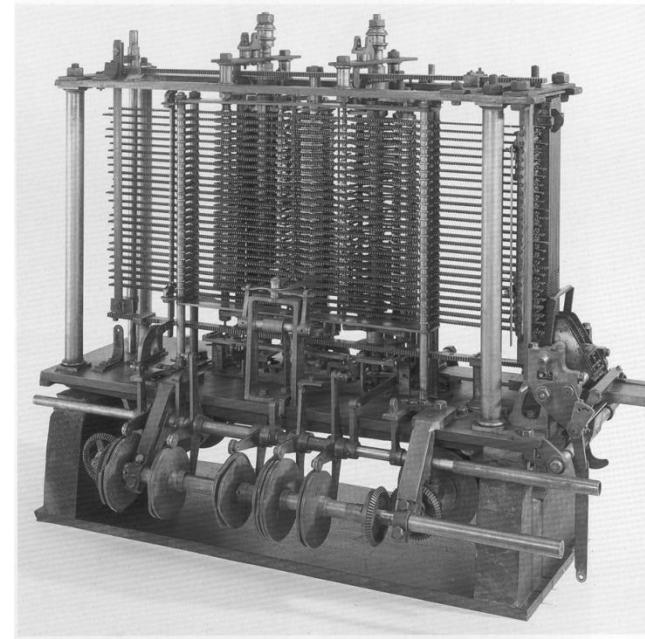
# Areas for successful digital design

- Debugging
  - Trouble shooter, systematic planning and patience
- Business Requirements and Practices
  - Documentation, Feature Definitions
- Risk Taking
- Communication

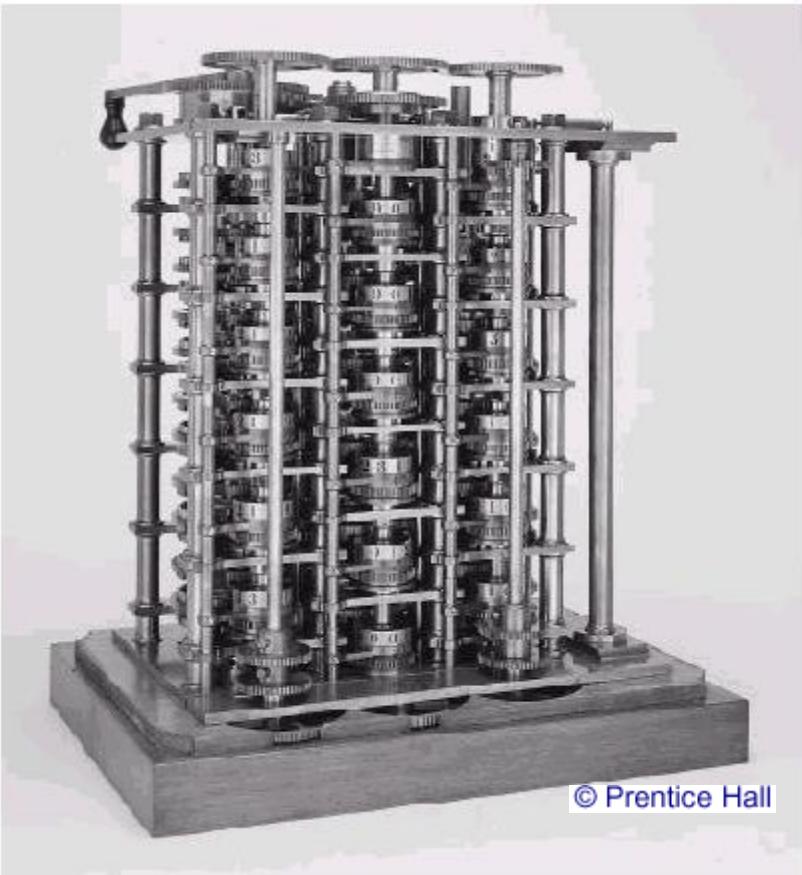
# Historical Perspectives

# The Analytical Engine

- Designed by Charles Babbage from 1834 – 1871
- Considered to be the first digital computer
- Built from mechanical gears, where each gear represented a discrete value (0-9)
- Babbage died before it was finished



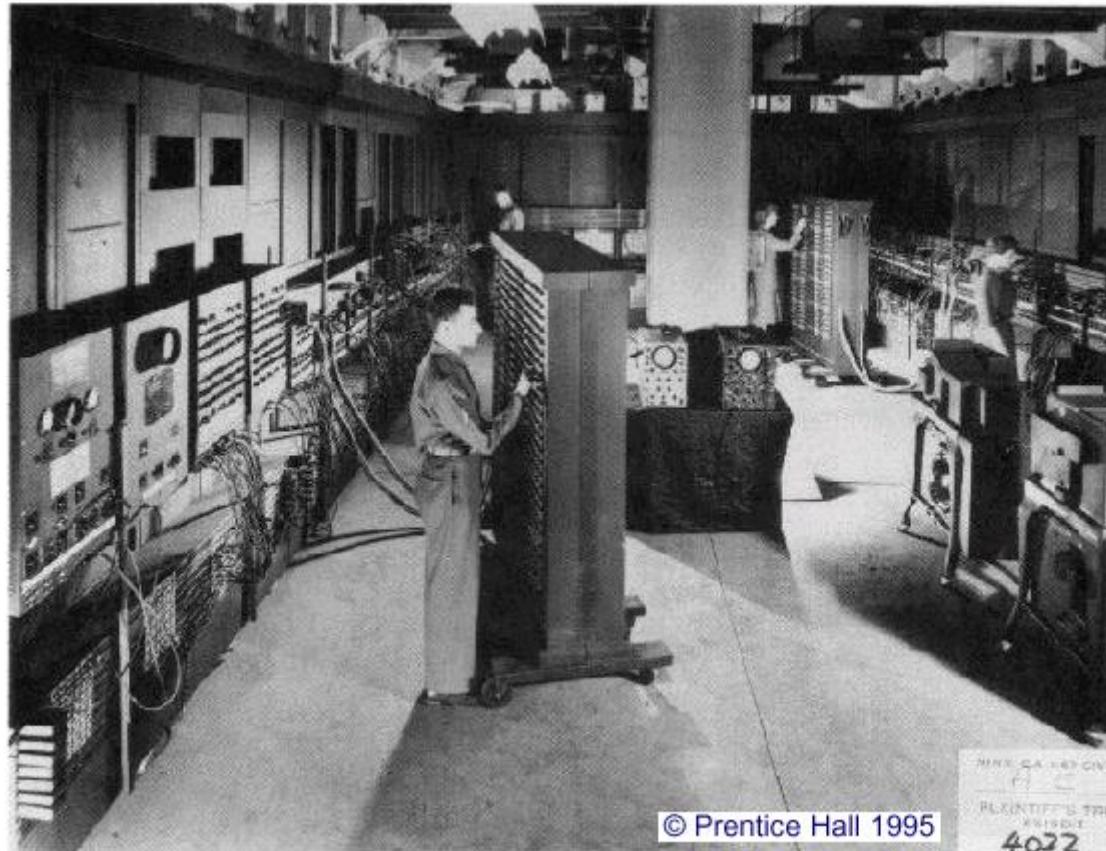
## History



- **Made in 1832**
- **25,000 Parts**
- **17,470 Pounds**

The Babbage Difference Engine

## History



© Prentice Hall 1995

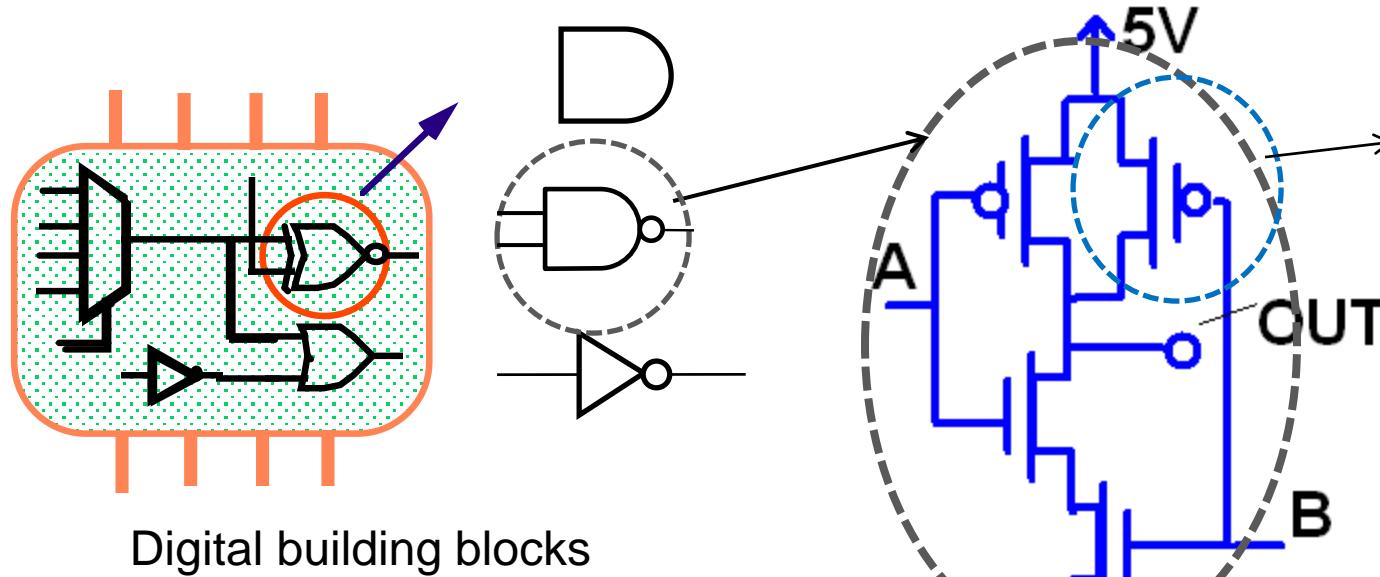
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**ENIAC - The first electronic Computer (1946)**  
**(18000 vacuum tubes, 30 tons, 80'x8.5', 1900 adds/sec)**

# What are Logic Gates built from?

## Transistors:

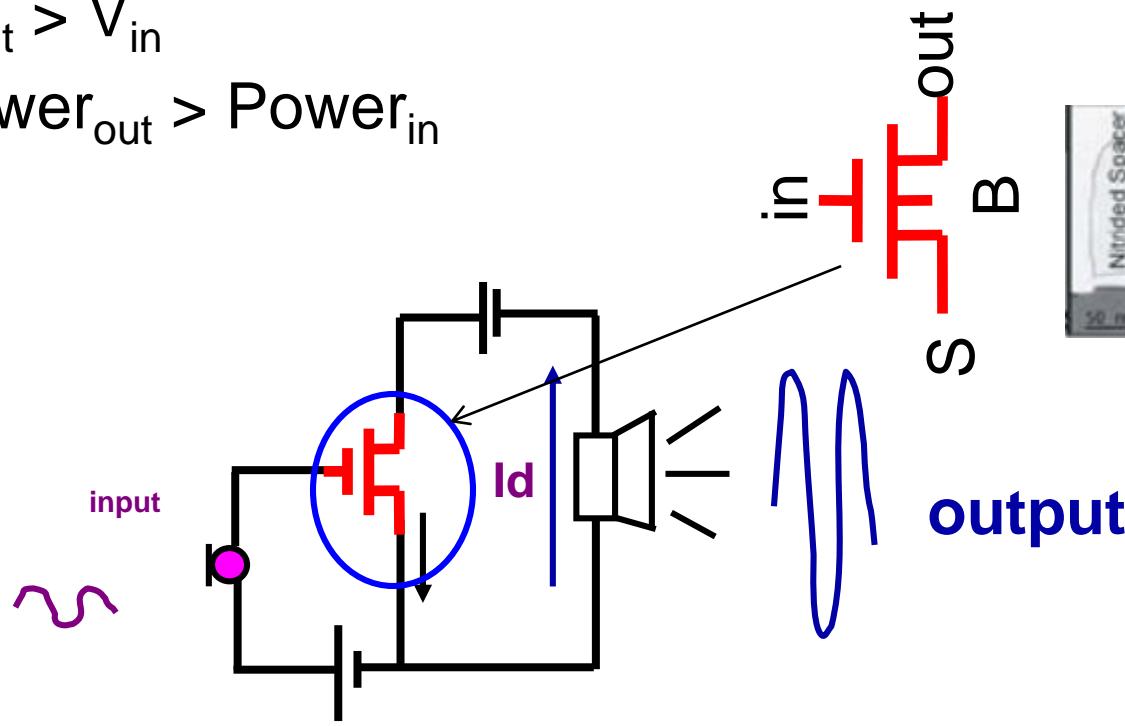
- The transistor is the workhorse of every electronic device.



# What is a Transistor?

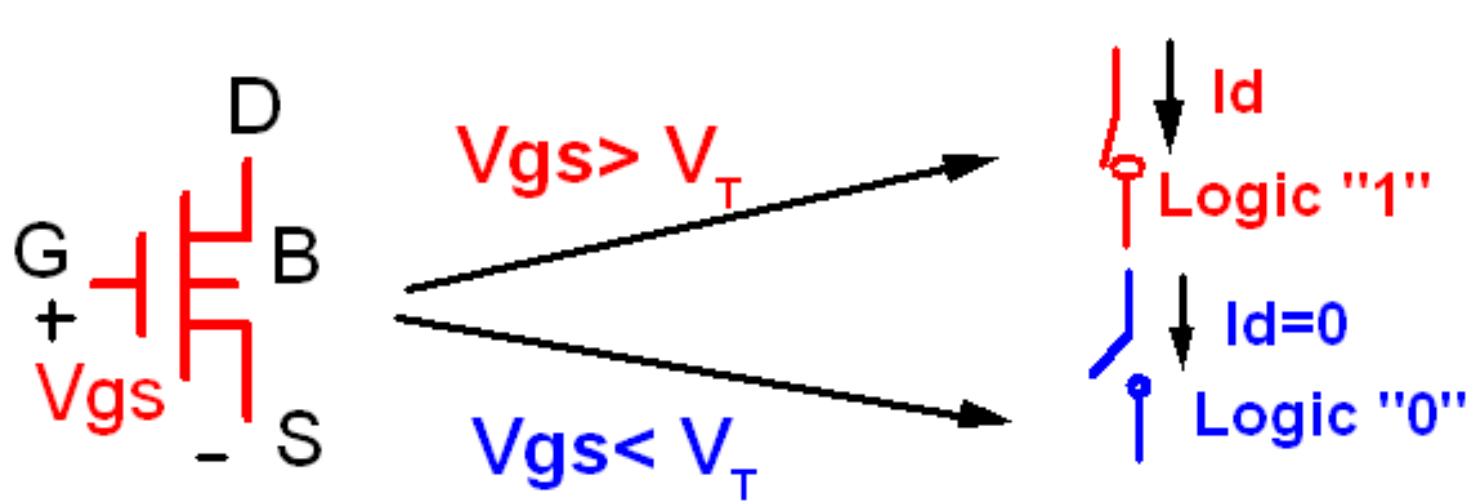
- Electronic, solid-state device that can amplify an electric signal:

- »  $V_{out} > V_{in}$
- »  $\text{Power}_{out} > \text{Power}_{in}$



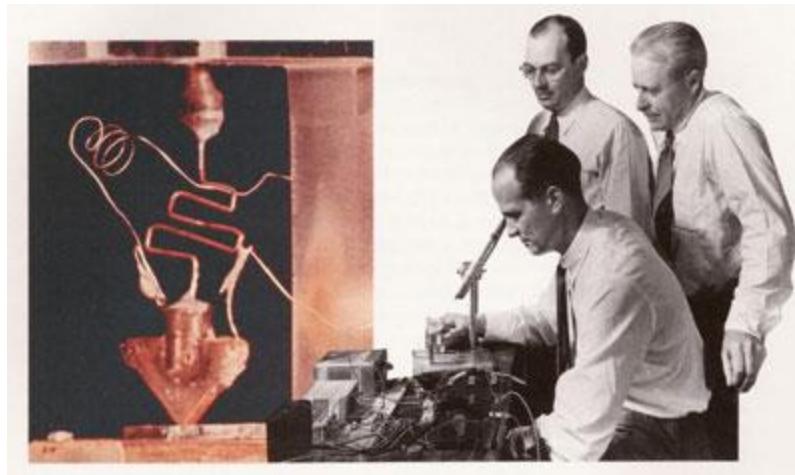
# Digital Model of a Transistor

- We make abstraction of the signals: 0 or 1
- As a result a transistors can be considered a switch (on or off; 1 or ;):



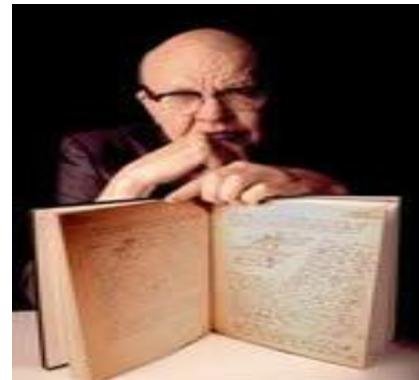
## Invention of Transistor

- Bardeen, Brattain, Shockley invented in Bell Labs in 1947
- Nobel Prize



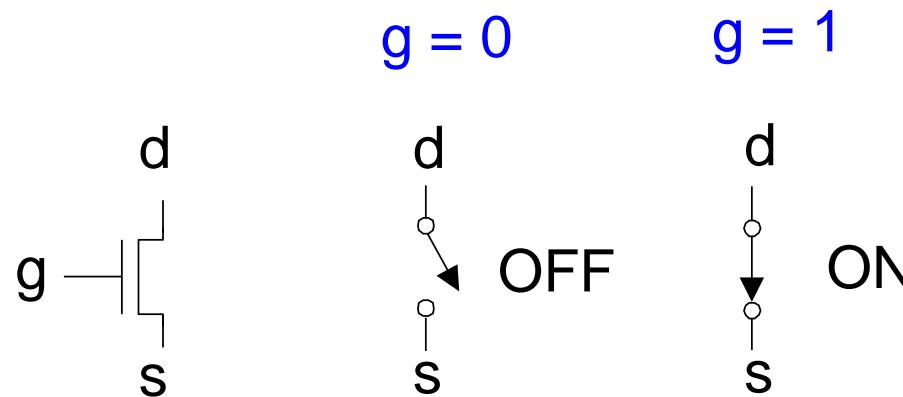
# Integrated Circuit

- Jack Kilby of Texas Instruments built the first integrated circuit (IC) with 2 transistors – 1958
- Nobel Prize in Physics



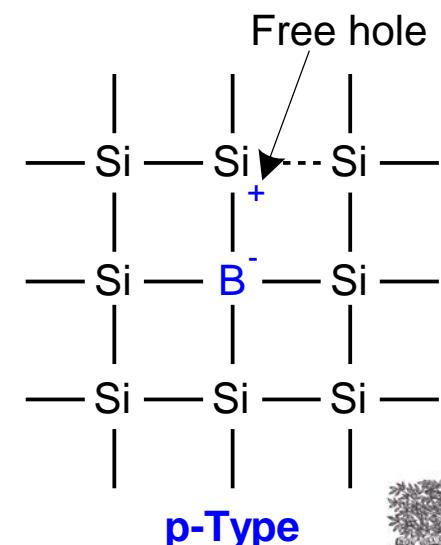
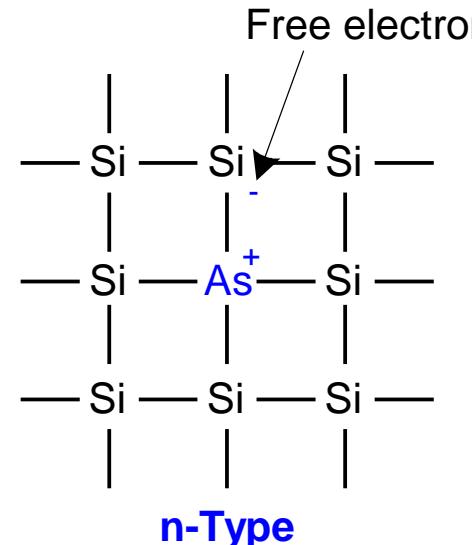
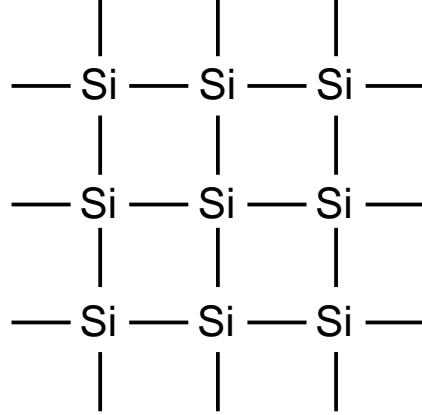
# Transistors

- Logic gates built from transistors
- 3-port voltage-controlled switch
  - 2 ports connected depending on voltage of 3rd
  - d and s are connected (ON) when g is 1



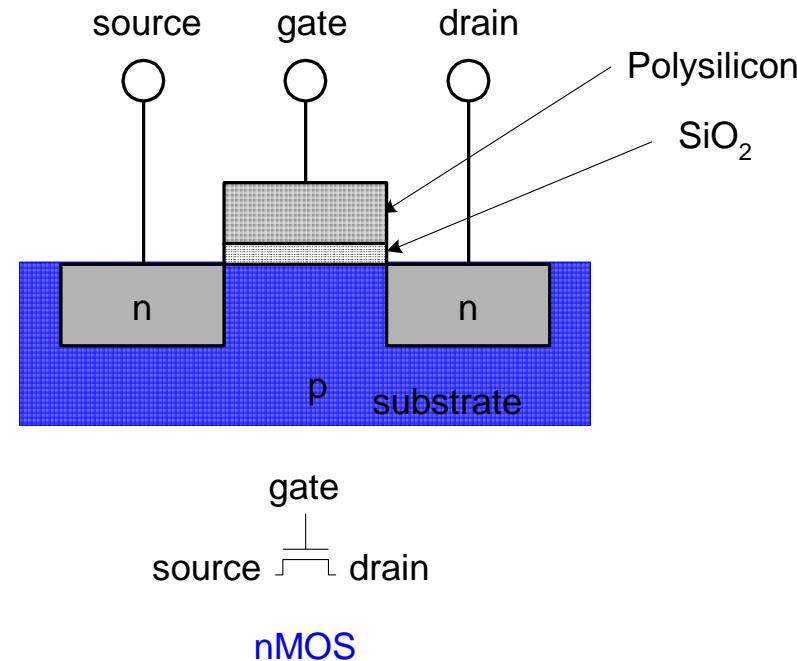
# Silicon

- Transistors built from silicon, a semiconductor
- Pure silicon is a poor conductor (no free charges)
- Doped silicon is a good conductor (free charges)
  - n-type (free *negative* charges, electrons)
  - p-type (free *positive* charges, holes)



# MOS Transistors

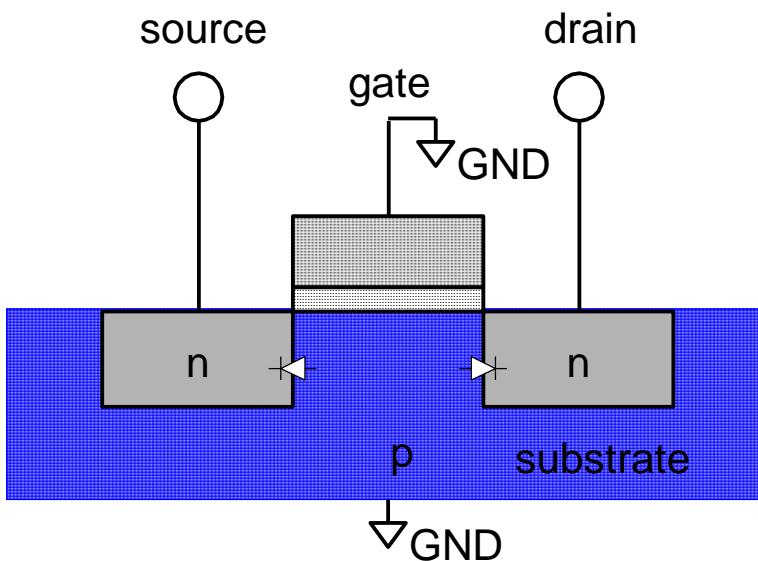
- **Metal oxide silicon (MOS) transistors:**
  - Polysilicon (used to be **metal**) gate
  - **Oxide** (silicon dioxide) insulator
  - Doped **silicon**



# Transistors: nMOS

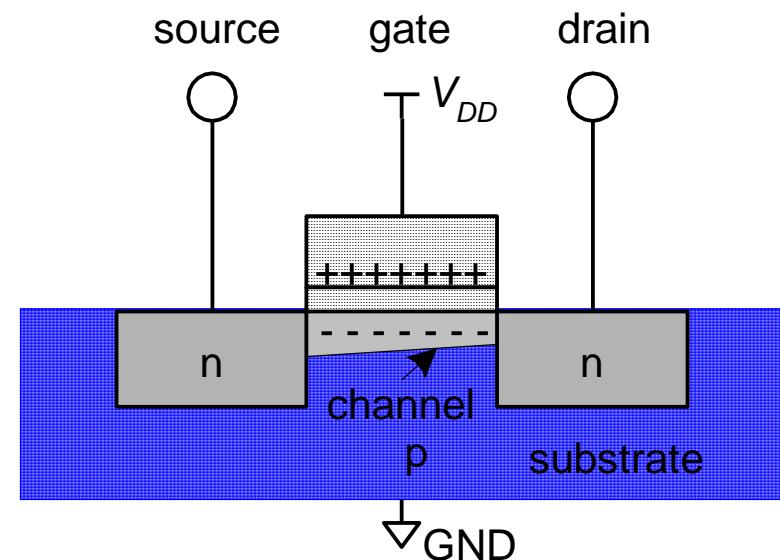
Gate = 0

OFF (no connection between source and drain)



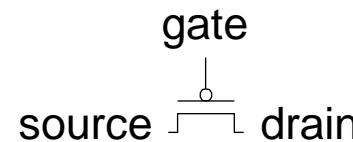
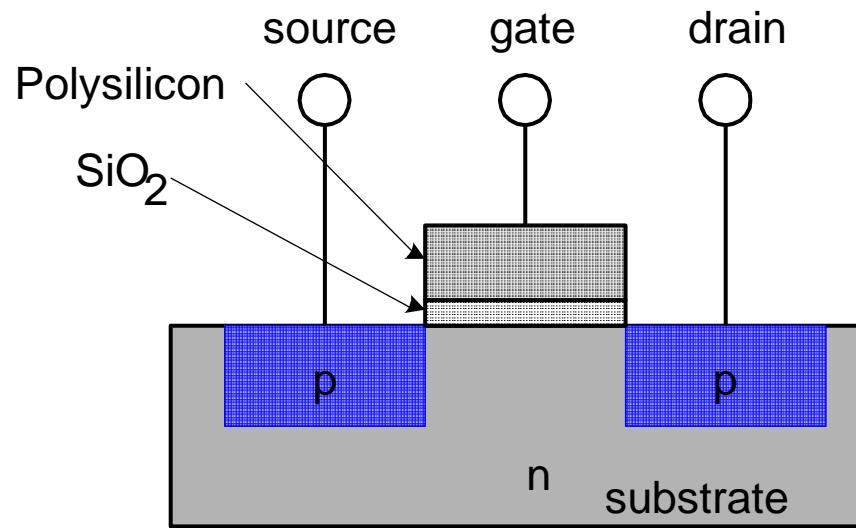
Gate = 1

ON (channel between source and drain)



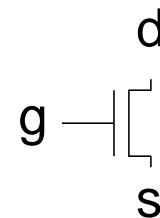
# Transistors: pMOS

- pMOS transistor is opposite
  - ON when Gate = 0
  - OFF when Gate = 1

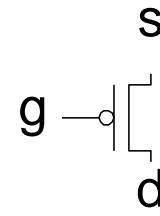


# Transistor Function

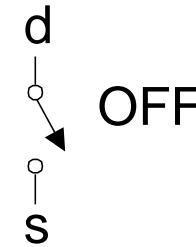
nMOS



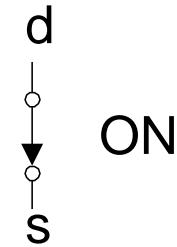
pMOS



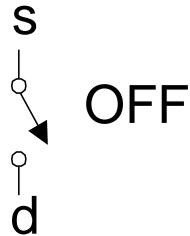
$g = 0$



$g = 1$



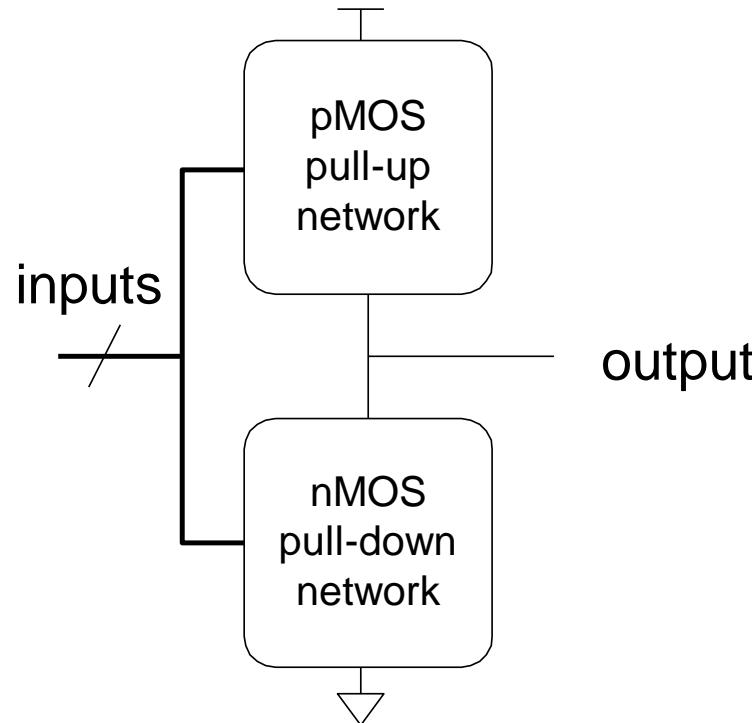
OFF



ON

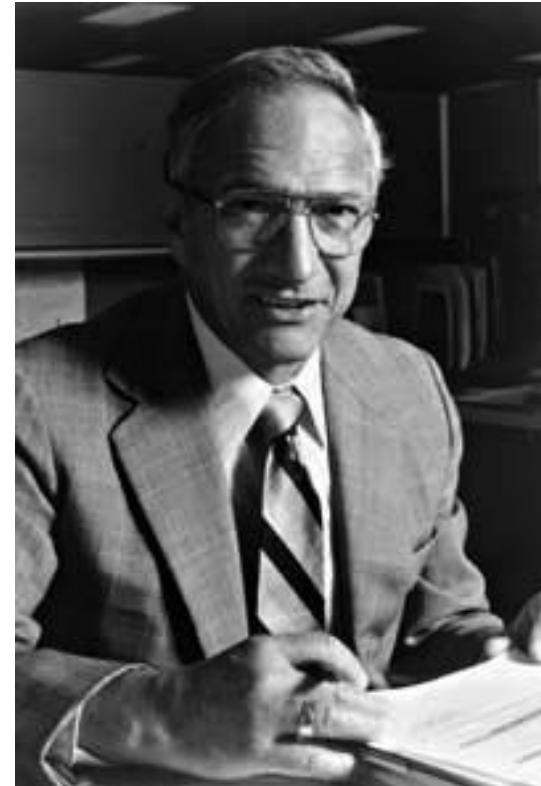
# Transistor Function

- **nMOS:** pass good 0's, so connect source to GND
- **pMOS:** pass good 1's, so connect source to  $V_{DD}$



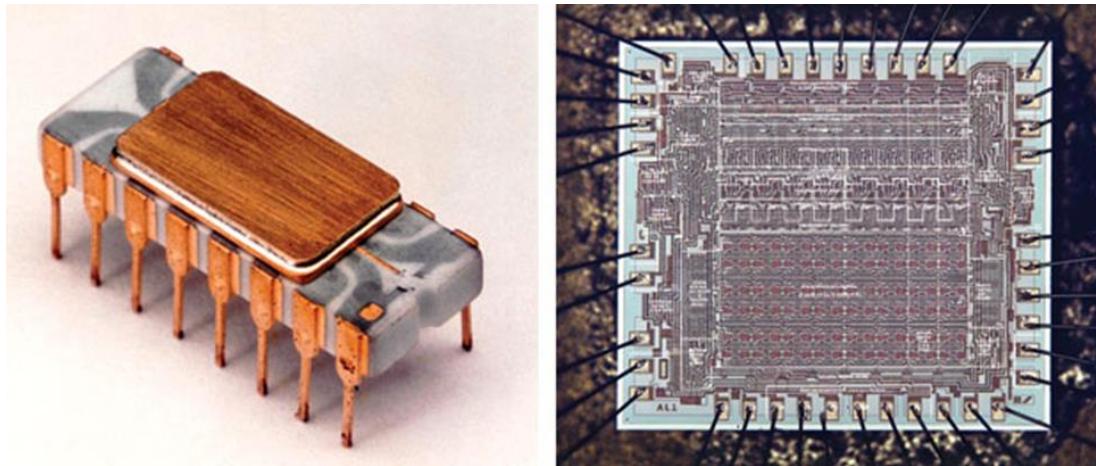
# **Robert Noyce, 1927 - 1990**

- Nicknamed “Mayor of Silicon Valley”
- Cofounded Fairchild Semiconductor in 1957
- Cofounded Intel in 1968
- Co-invented the integrated circuit



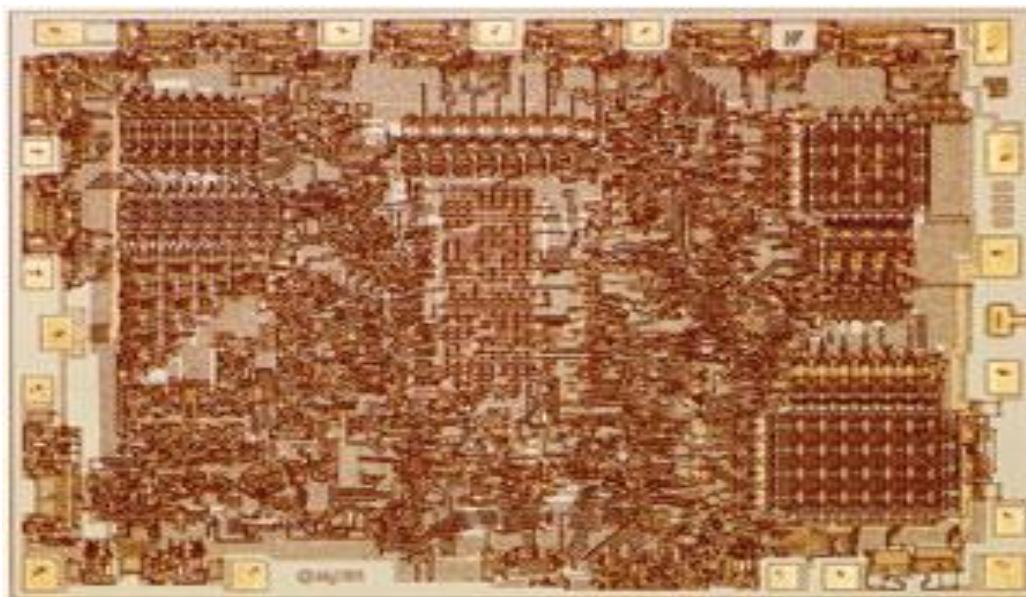
# Intel Microprocessor – 4004

- Intel 4004 – 4-bit microprocessor – 1971 – 2300 Transistors
- First Microprocessor – Used in Calculator



## Intel Microprocessor – 8008 -

- Intel 8008 – 8-bit microprocessor – 1972 – 3908 Transistors
- Intel Itanium microprocessor – 2 B transistors, 16 GB Flash Memory – 4 B transistors – 2008
- 



# Brief History of IC

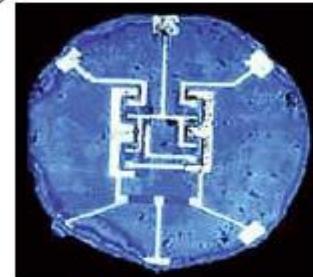
## A Brief History of Integrated Circuits

1 Transistor  
3 Resistors  
1 Capacitor



Germanium IC  
Jack Kilby  
Texas Instruments

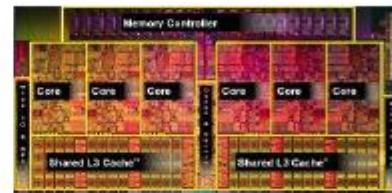
From



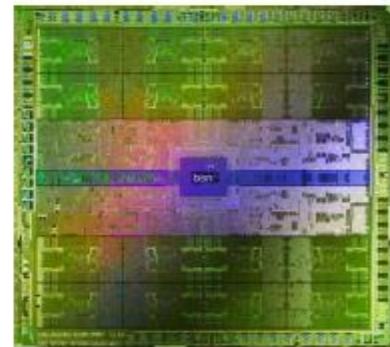
Silicon IC  
Robert Noyce  
Fairchild  
Semiconductor

circa 1958

To



Intel Gulftown (six-core  
microprocessor)  
1.17 Billion transistors  
(32 nm)



NVIDIA GTX580  
(Graphics processor  
with 512 "cores")  
3.05 Billion transistors  
(40 nm)

circa 2011

A 1,500,000,000 fold  
increase in 50 years

# Growth Rate

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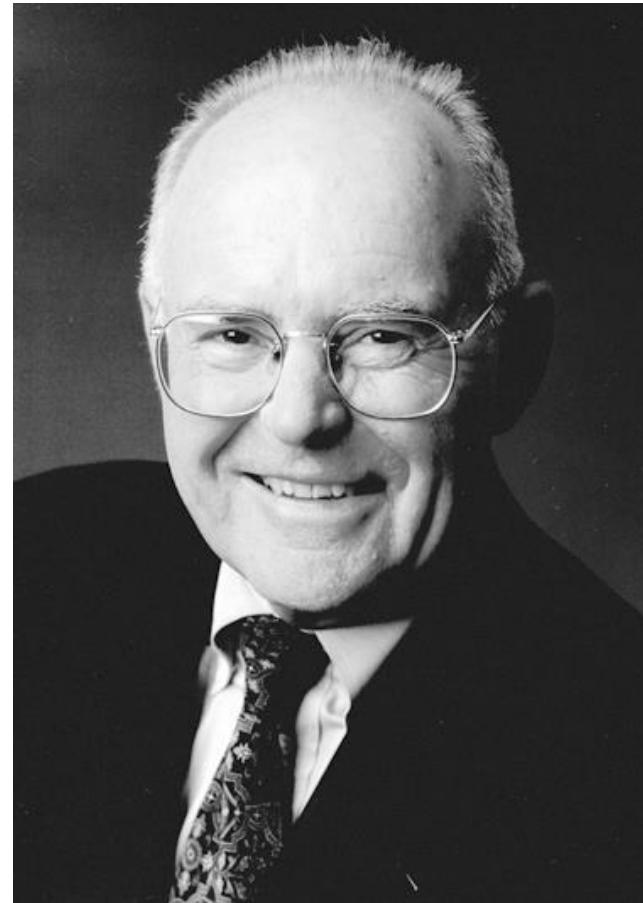
- 53% compound annual growth rate over 50 years
  - No other technology has grown so fast so long
- Driven by miniaturization of transistors
  - Smaller is cheaper, faster, lower in power!
  - Revolutionary effects on society



[Moore65]  
Electronics Magazine

# Gordon Moore, 1929 -

- Cofounded Intel in 1968 with Robert Noyce.
- **Moore's Law:** the number of transistors on a computer chip doubles every year (observed in 1965)
- Since 1975, transistor counts have doubled every two years.

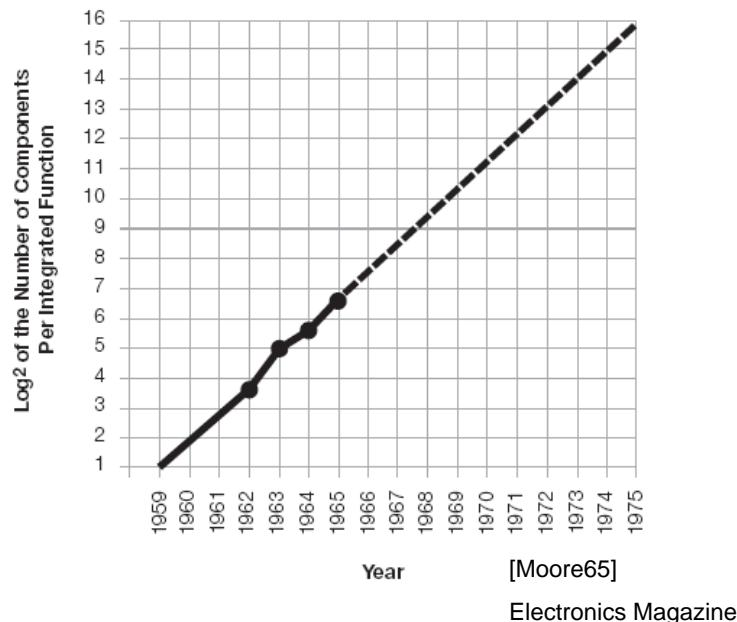


# *Moore's Law*

- In 1965, Gordon Moore noted that the number of transistors on a chip doubled every 18 to 24 months.
- He made a prediction that semiconductor technology will double its effectiveness every 18 months

# Moore's Law: Then

- 1965: Gordon Moore plotted transistor on each chip
  - Fit straight line on semilog scale
  - Transistor counts have doubled every 26 months



## Integration Levels

**SSI:** 10 gates

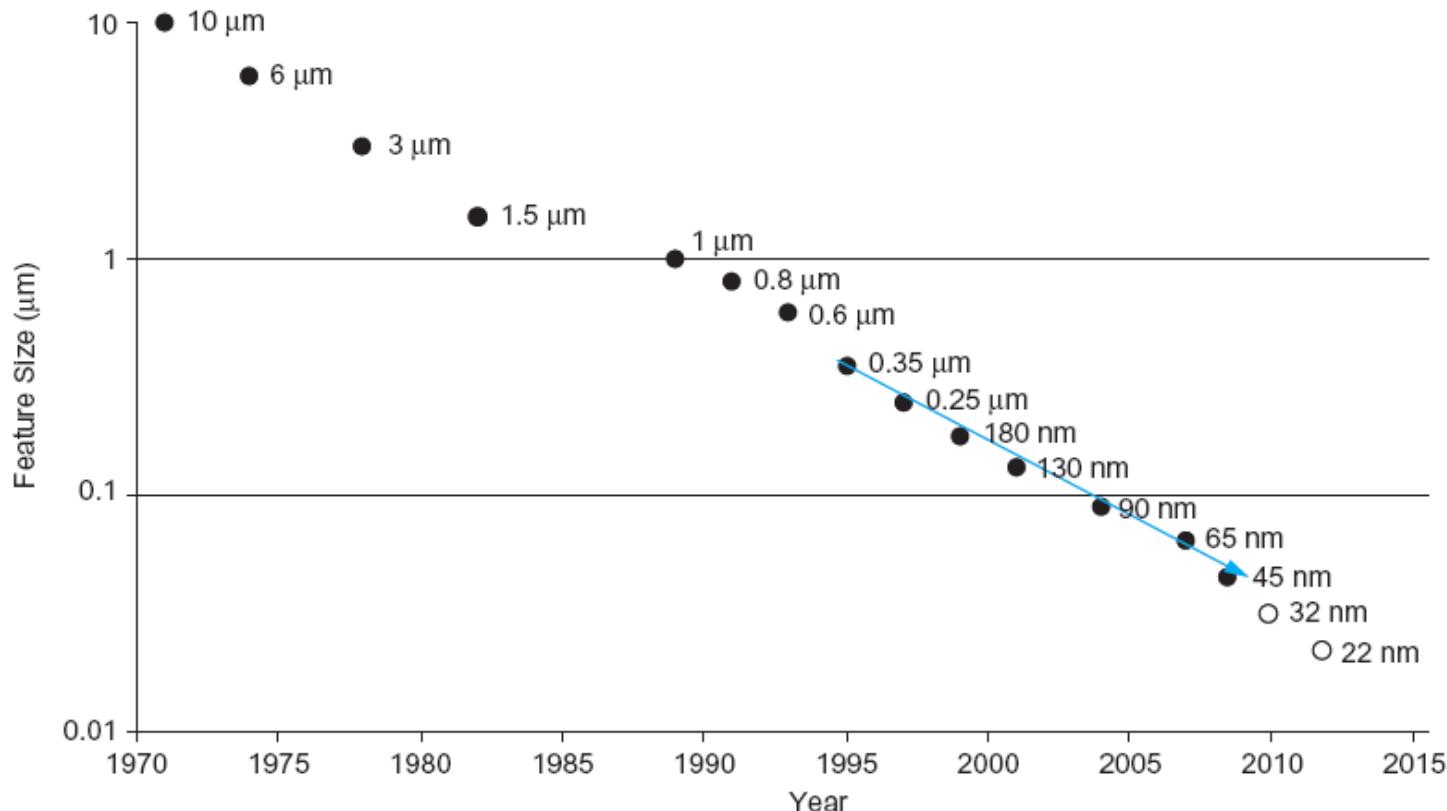
**MSI:** 1000 gates

**LSI:** 10,000 gates

**VLSI:** > 10k gates

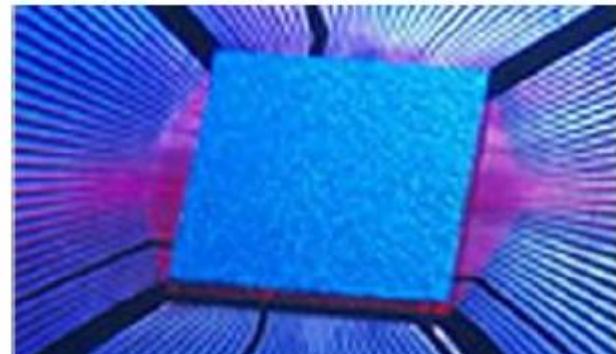
# Feature Size

- Minimum feature size shrinking 30% every 2-3 years

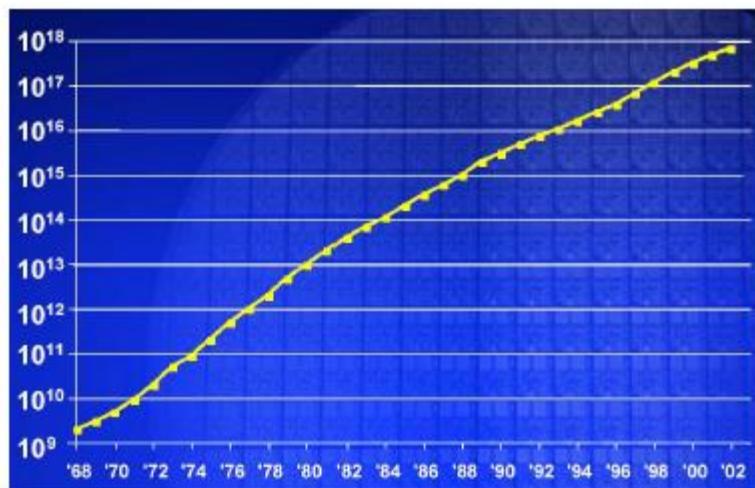


# We are drowning in transistors

- Ten quintillion:  $10^*10^{18}$ 
  - ~ The number of transistors shipped in 2004!
  - > The estimated number of grains of rice harvested in 2004
  - 100 times estimated number of ants on earth



Transistors shipped worldwide



Sources: "A Law of Continuing Returns", Los Angeles Times, April 17 2005  
ISSCC 2004 Keynote, Gordon Moore

# We are drowning in transistors

- Option #1 (general-purpose products)
  - Microprocessors, GPUs
    - Pre-2005: Deeper pipelines, more complex logic for instruction-level parallelism, more cache
    - 2005- : More cores, more cache
  - Memory chips
    - Easy – just keep increasing capacity
  - ???

## We are drowning in transistors

- Option #2 (98 % of “computing” systems)
  - Integrate more and more system functions onto a chip



- Benefits of integration
  - Size (miniaturization)
  - Cost
  - Performance
  - Power

# System On a Chip (SoC)



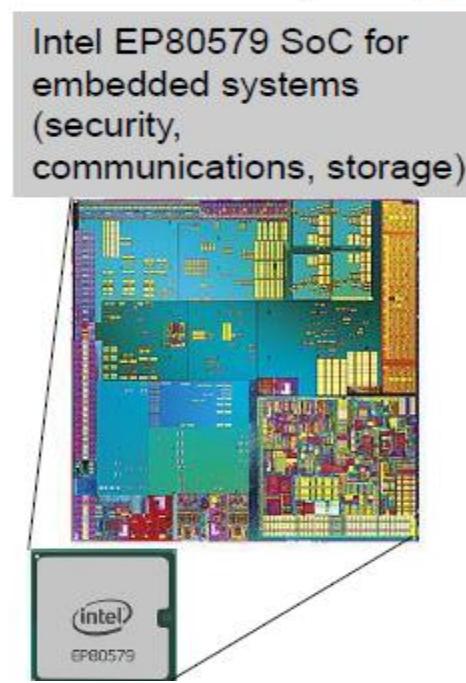
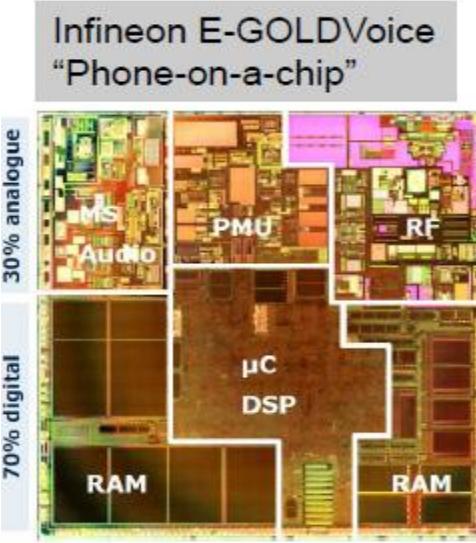
Honey I shrunk  
the Chip

How many people fit in a mini cooper? -  
How many IPs/Features in an SoC?

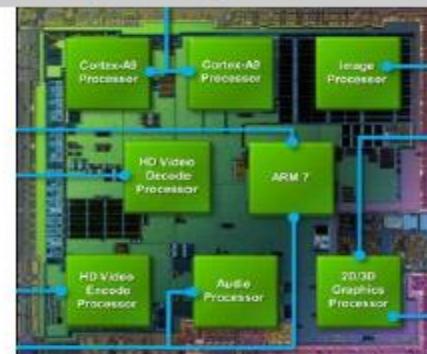


# System on a Chip - SoC

- Direct consequence of increasing scales of integration (Moore's Law)
  - Integrate hitherto discrete system components into a single chip
  - Tremendous benefits in cost, size, performance, power consumption



NVIDIA Tegra2 SoC for  
tablets, slates, e-readers,  
MIDs, set-top boxes



# Ubiquitous Integrated Circuits

Integrated Circuits are everywhere –  
Transformational effect on the way we live, work, play ...



(Source: C. Claeys, IMEC)

# Historical Perspectives

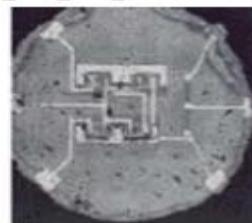
## Technology Origins . . .



1947 Invention  
of the transistor  
(Bell Labs)



1954: First  
commercial transistor  
(TI)



1958: Invention IC  
(J. Kilby, TI & Noyce, Fairchild)



Intel

and the rest is history ...



Shockley (seated),  
Bardeen (left), and  
Brattain (right)

### 1954: First ISSCC

#### SESSION IV

Friday, 2:30 p.m. - 5 p.m.

**Nonlinear Applications of Junction Transistors**  
Chairman: A. W. Lo, *RCA Laboratories, Princeton, N. J.*

**15. Large-Signal D-C Behavior of Junction Transistors**  
J. J. Ebers and J. L. Moll, *Bell Telephone Laboratories, Murray Hill, N. J.*  
(about 3:30 p.m., Thursday)

**7. Neutralization of Transistor Bandpass Amplifiers**  
F. P. Keiper, Jr., *Philco Corp., Philadelphia*

This paper will discuss the utilization of surface-barrier and junction transistors in bandpass amplifier circuits.  
The equivalent circuits useful in bandpass amplifier design will

### ISSCC 1956

2:30 p.m.-5:30 p.m.—Irvine Auditorium  
**SWITCHING CIRCUITS**

Chairman: H. E. Tompkins, *Burroughs Corporation*  
**2.1 Direct-Coupled Transistor Logic Circuitry in Digital Computers**  
J. R. Harris, *Bell Telephone Laboratories, Murray Hill*

(Source: <http://sscs.org/History/isscc50/index.html>)

# Life Changers

## A World Transformed: What Are the Top 30 Innovations of the Last 30 Years?

Published: February 18, 2009 in Knowledge@Wharton



Of these 30 innovations , 10 are directly related to advances in Digital Logic and Solid State Circuits;

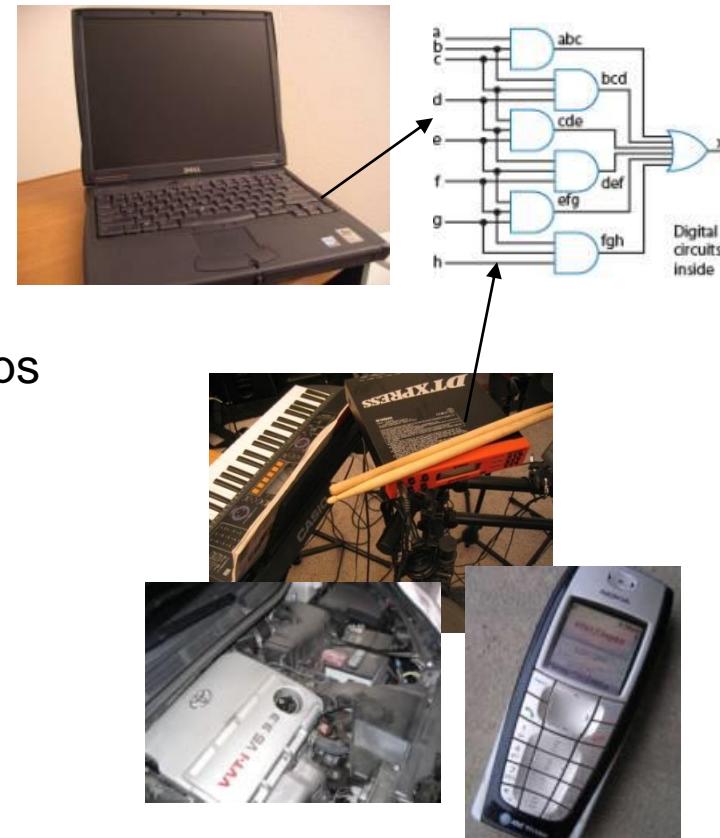
Another 8 are the indirect results of ICs.

- 1. Internet, broadband, WWW (browser and html)
- 2. PC/laptop computers
- 3. Mobile phones
- 4. E-mail
- 5. DNA testing and sequencing/Human genome mapping
- 6. Magnetic Resonance Imaging (MRI)
- 7. Microprocessors
- 8. Fiber optics
- 9. Office software (spreadsheets, word processors)
- 10. Non-invasive laser/robotic surgery (laparoscopy)
- 11. Open source software and services (e.g., Linux, Wikipedia)
- 12. Light emitting diodes
- 13. Liquid crystal display (LCD)
- 14. GPS systems
- 15. Online shopping/ecommerce/auctions (e.g., eBay)
- 16. Media file compression (jpeg, mpeg, mp3)
- 17. Microfinance
- 18. Photovoltaic Solar Energy
- 19. Large scale wind turbines
- 20. Social networking via the Internet
- 21. Graphic user interface (GUI)
- 22. Digital photography/videography
- 23. RFID and applications (e.g., EZ Pass)
- 24. Genetically modified plants
- 25. Bio fuels
- 26. Bar codes and scanners
- 27. ATMs
- 28. Stents
- 29. SRAM flash memory
- 30. Anti retroviral treatment for AIDS

# Part 2 – Basics of Digital Systems

# Why Study Digital Design?

- Look “under the hood” of computers
  - Solid understanding --> confidence, insight, even better programmer when aware of hardware resource issues
- Electronic devices becoming digital
  - Enabled by shrinking and more capable chips
  - Enables:
    - Better devices: Sound recorders, cameras, cars, cell phones, medical devices,...
    - New devices: Video games, PDAs, ...
  - Known as “embedded systems”
    - Thousands of new devices every year
    - Designers needed: Potential career direction



# Discipline

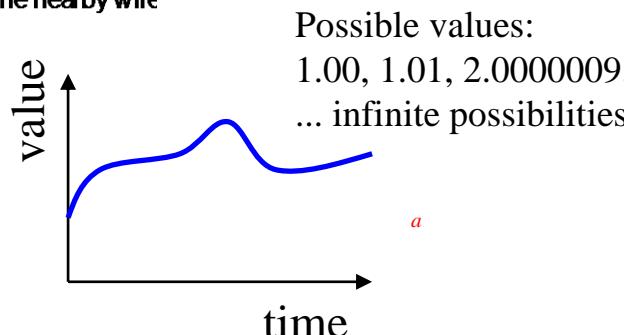
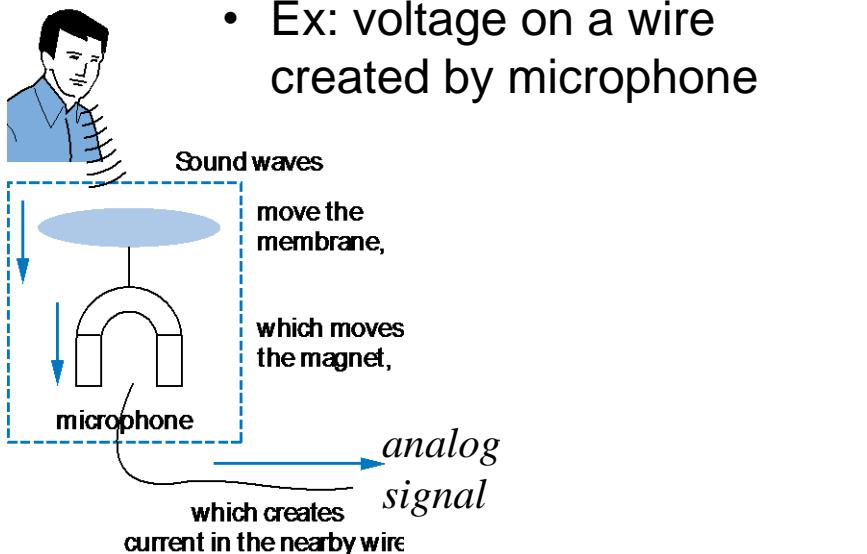
- Intentionally restrict design choices
- Example: Digital discipline
  - Discrete voltages instead of continuous
  - Simpler to design than analog circuits – can build more sophisticated systems
  - Digital systems replacing analog predecessors:
    - i.e., digital cameras, digital television, cell phones, CDs

# The Digital Abstraction

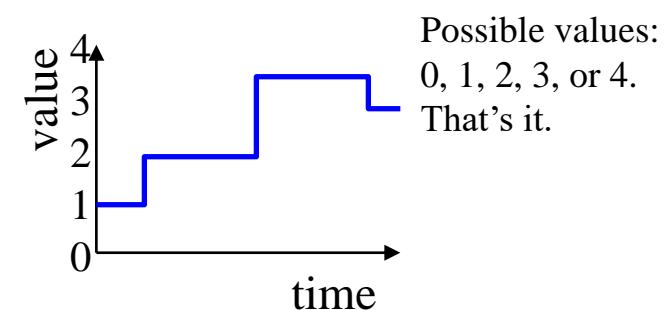
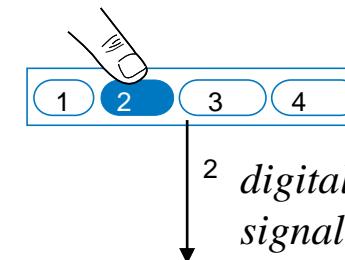
- Most physical variables are continuous, for example
  - Voltage on a wire
  - Frequency of an oscillation
  - Position of a mass
- Instead of considering all values, the digital abstraction considers only a discrete subset of values

# What Does “Digital” Mean?

- Analog signal
  - Infinite possible values
    - Ex: voltage on a wire created by microphone

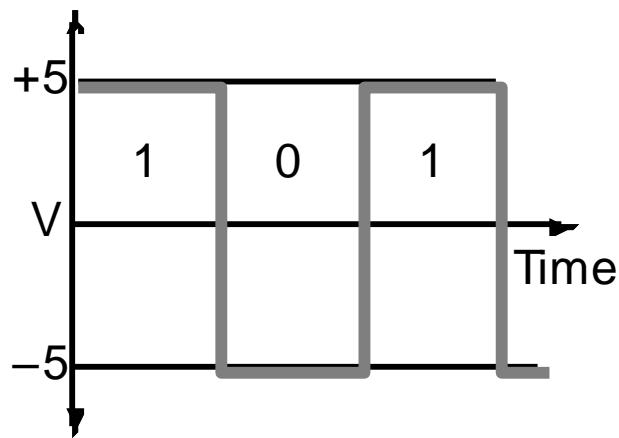


- Digital signal
  - Finite possible values
    - Ex: button pressed on a keypad

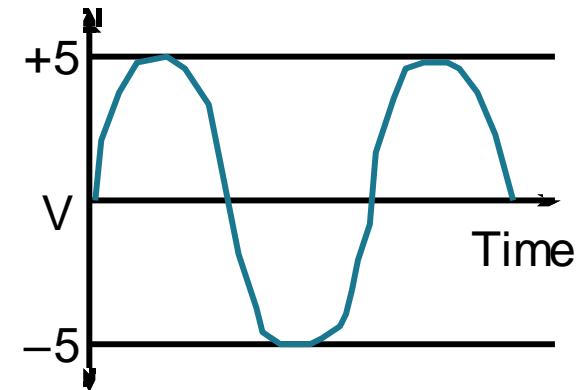


# Digital Systems

## Digital vs. Analog Waveforms



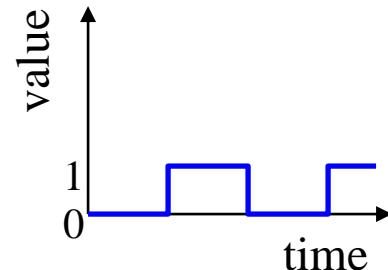
**Digital:**  
only assumes discrete values



**Analog:**  
values vary over a broad range  
continuously

# Digital Signals with Only Two Values: Binary

- **Binary** digital signal -- only *two* possible values
  - Typically represented as **0** and **1**
  - One *binary digit* is a **bit**
  - We'll only consider *binary* digital signals
  - Binary is popular because
    - Transistors, the basic digital electric component, operate using *two* voltages (more in Chpt. 2)
    - Storing/transmitting one of *two* values is easier than three or more (e.g., loud beep or quiet beep, reflection or no reflection)



# Example of Digitization Benefit

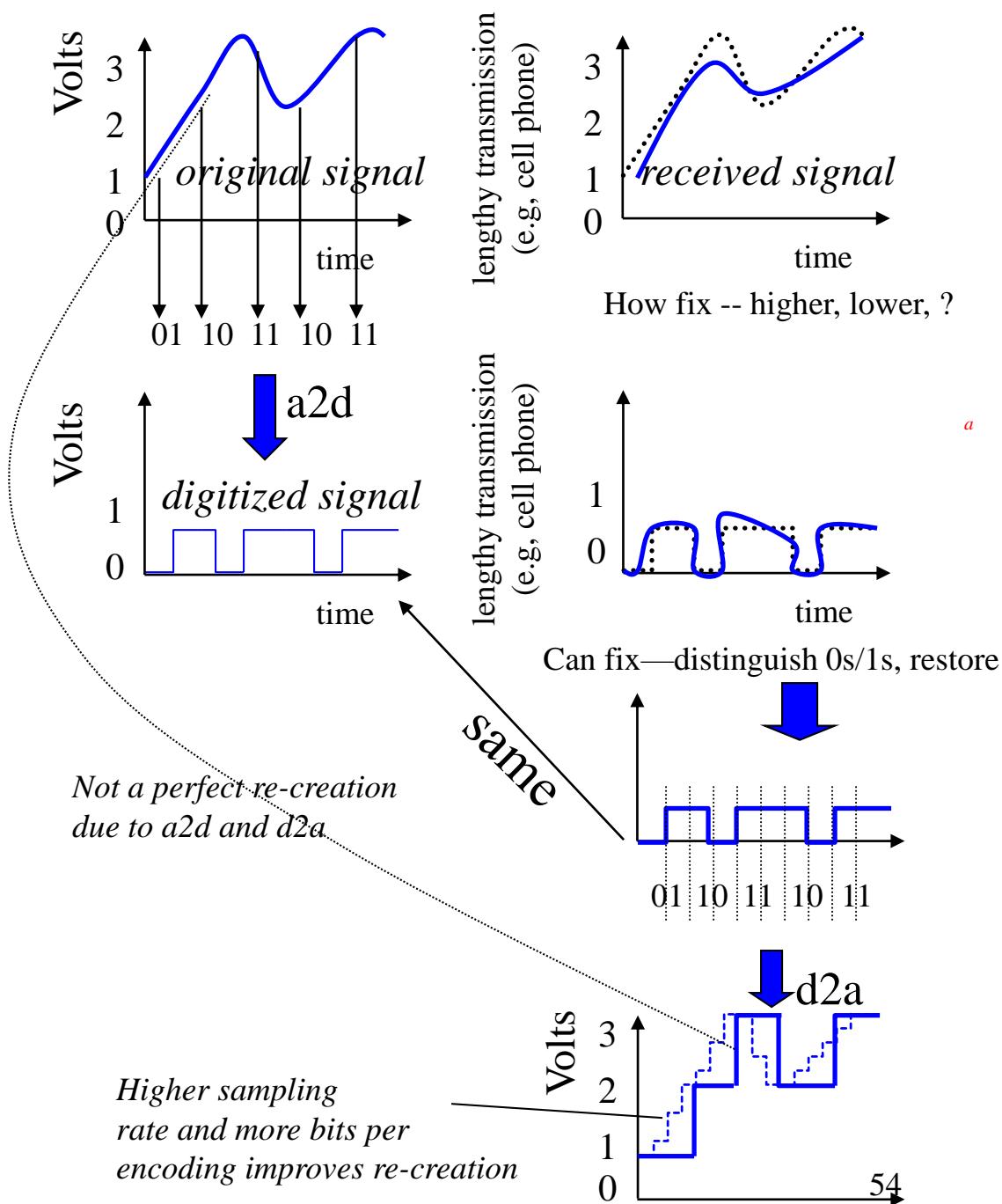
- Analog signal (e.g., audio, video) may lose quality
  - Voltage levels not saved/copied/transmitted perfectly
- Digitized version enables near-perfect save/cpy/tran.
  - “Sample” voltage at particular rate, save sample using bit encoding
  - Voltage levels still not kept perfectly
  - But we can distinguish 0s from 1s

Let bit encoding be:

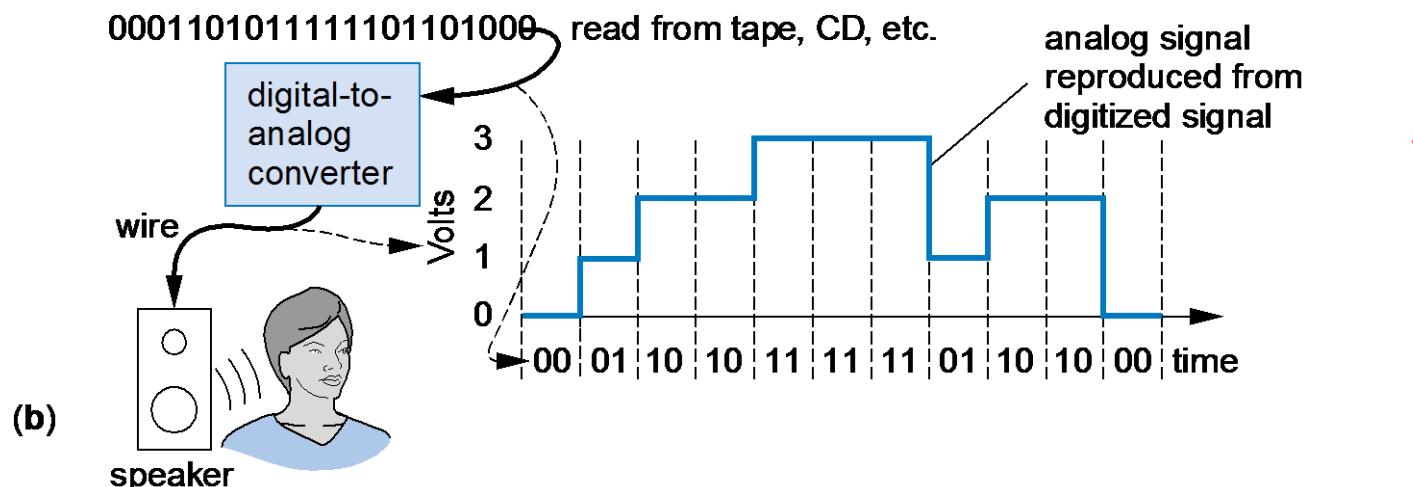
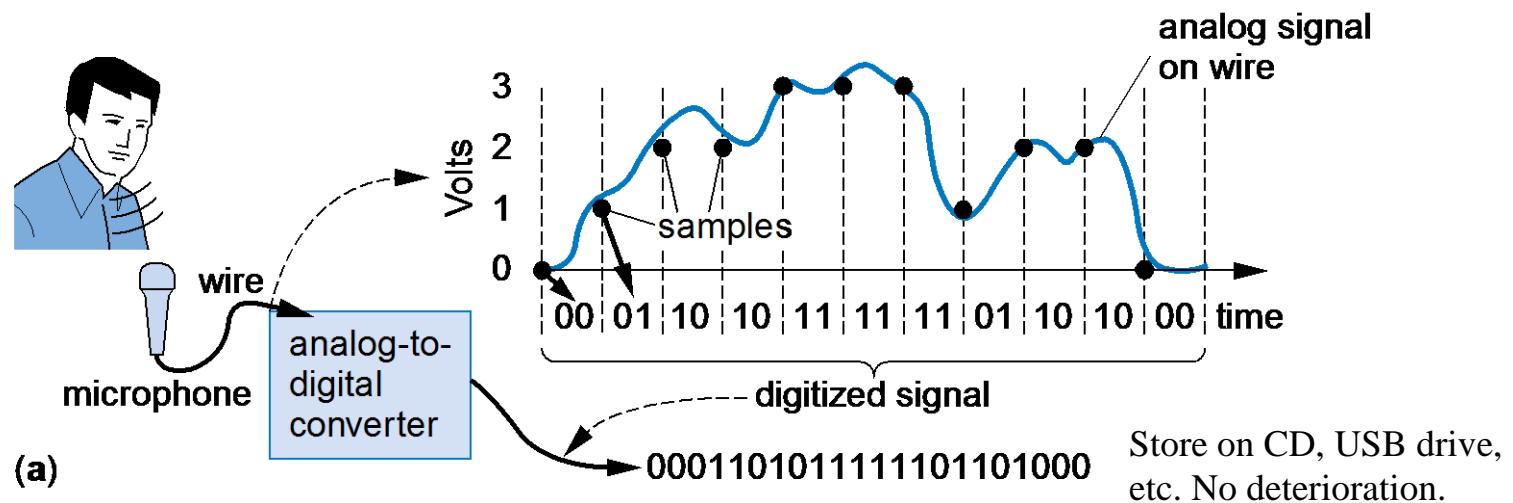
1 V: “01”

2 V: “10”

3 V: “11”



# Digitization Benefit: Can Store on Digital Media



# Digitized Audio: Compression Benefit

- Digitized audio can be compressed
  - e.g., MP3s
  - A CD can hold about 20 songs uncompressed, but about 200 compressed
- Compression also done on digitized pictures (jpeg), movies (mpeg), and more
- Digitization has many other benefits too

Example compression scheme:

00 means 0000000000

01 means 1111111111

1X means X

0000000000 0000000000 0000001111 1111111111  
↓      ↓      ↓      ↓  
00    00    1000000111    01

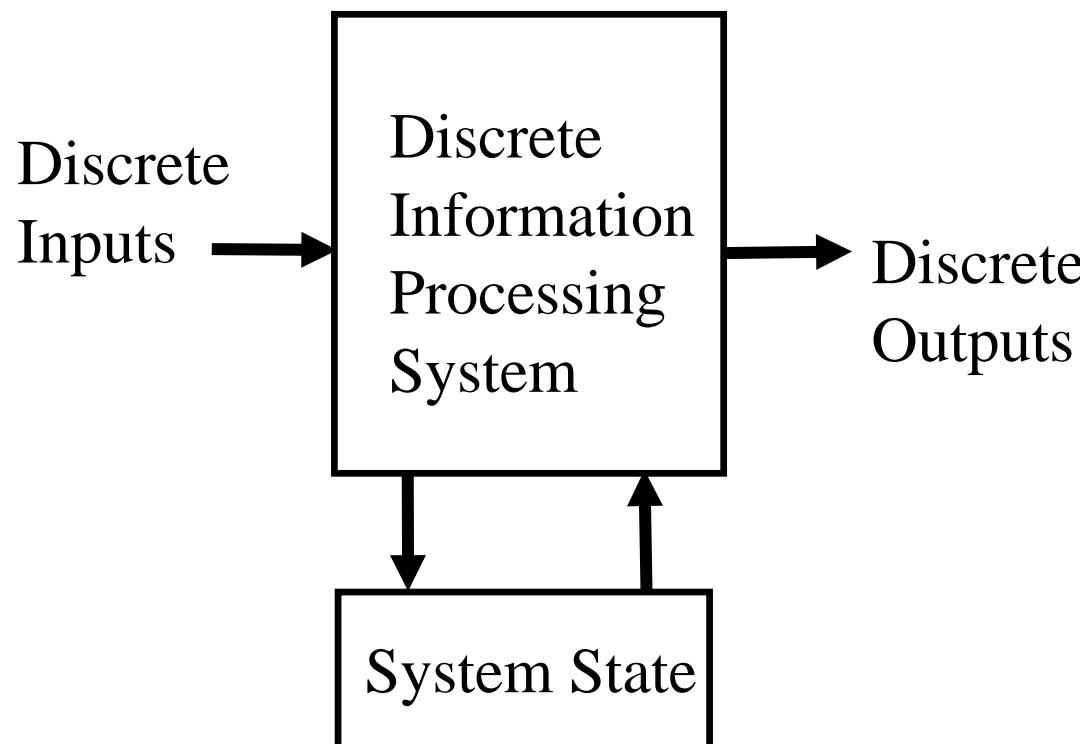
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# DIGITAL & COMPUTER SYSTEMS - Digital System

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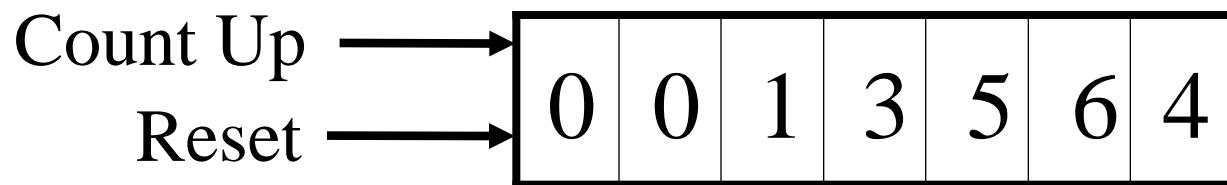
- Takes a set of discrete information inputs and discrete internal information (system state) and generates a set of discrete information outputs.



# Digital System Example:

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A Digital Counter (e. g., odometer):

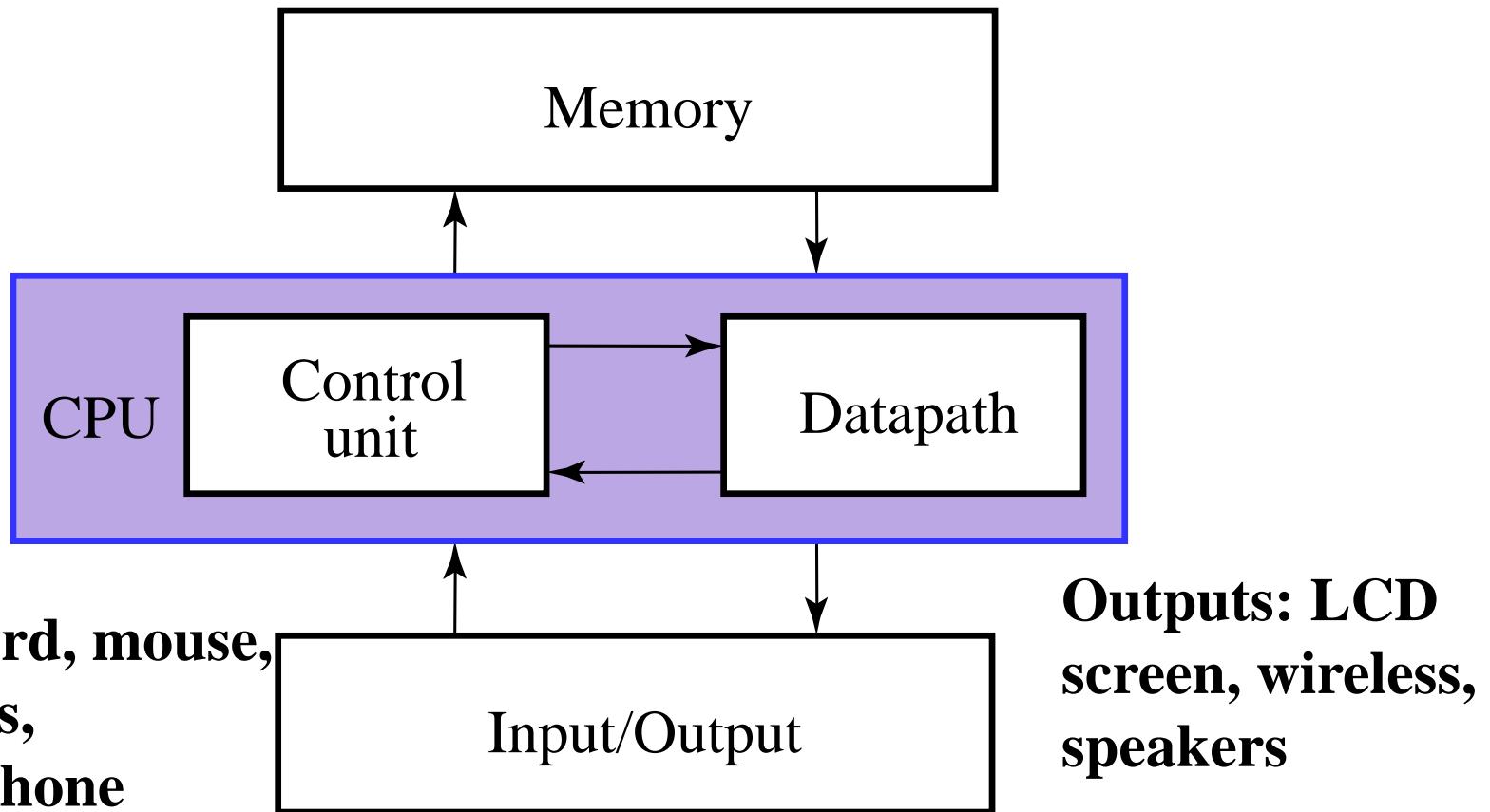


**Inputs:** Count Up, Reset

**Outputs:** Visual Display

**State:** "Value" of stored digits

# Digital Computer Example



# And Beyond – Embedded Systems

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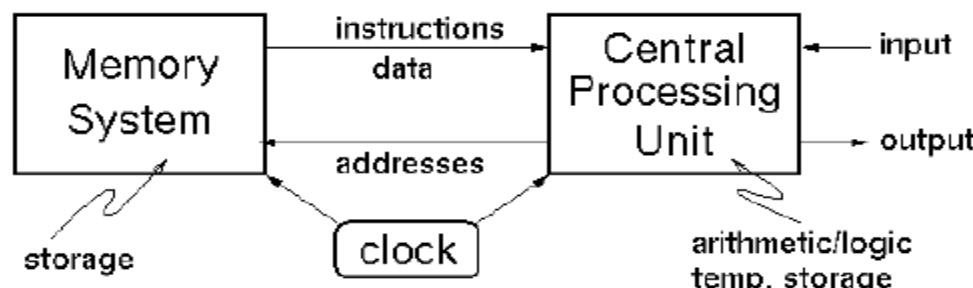
- Computers as integral parts of other products
- Examples of embedded computers
  - Microcomputers
  - Microcontrollers
  - Digital signal processors

## Examples of Digital Revolution

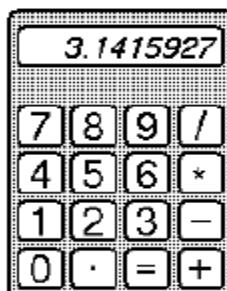
- Digital Cameras – Still Pictures
- Video Recordings
- Audio Recordings
- Traffic Lights
- Movie Effects

# Examples of Digital Revolution

- Digital Computer



- Usually design to maximize performance. "Optimized for speed"
- Handheld Calculator



- Usually designed to minimize cost.  
"Optimized for low cost"
- Of course, low cost comes at the expense of speed.

# Advantages of Digital

- Digital Watch



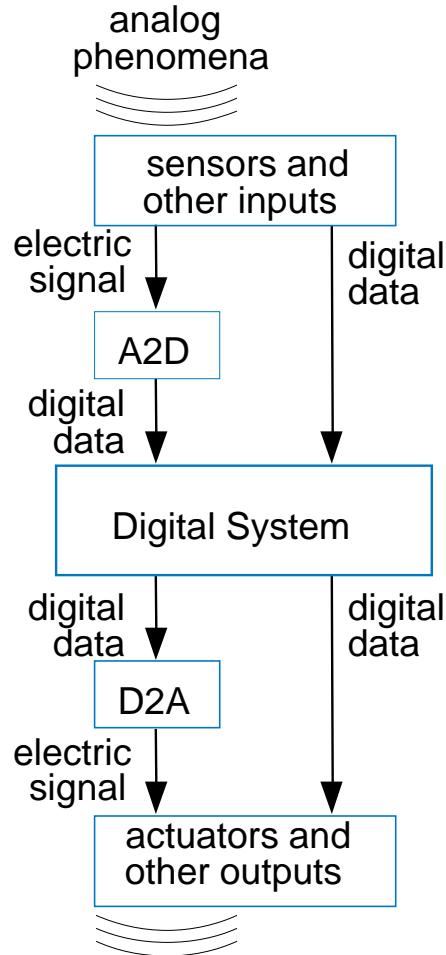
Designed to minimize power.  
Single battery must last for years.

- Low power operation comes at the expense of:
  - lower speed
  - higher cost

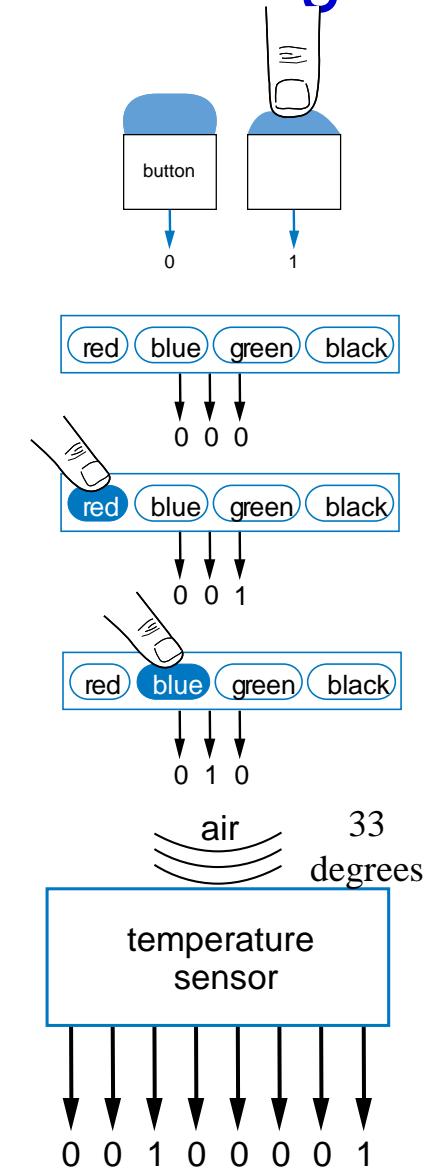
# Advantages of Digital

- Reproducibility of results – Analog depends on temperature, power supply voltage, component aging etc.,
- Ease of design
  - Logic Design – No Math – Operation viewed mentally without insights about the operation of capacitors, transistors etc.,
- Flexibility and Functionality – scrambling voice
- Programmable
- Speed
- Economy
- Steadily advancing technology

# How Do We Encode Data as Binary for Our Digital System?



- Some inputs inherently binary
  - Button: not pressed (0), pressed (1)
- Some inputs inherently digital
  - Just need encoding in binary
  - e.g., multi-button input: encode red=001, blue=010, ...
- Some inputs analog
  - Need analog-to-digital conversion
  - As done in earlier slide -- sample and encode with bits



# The Art of Managing Complexity

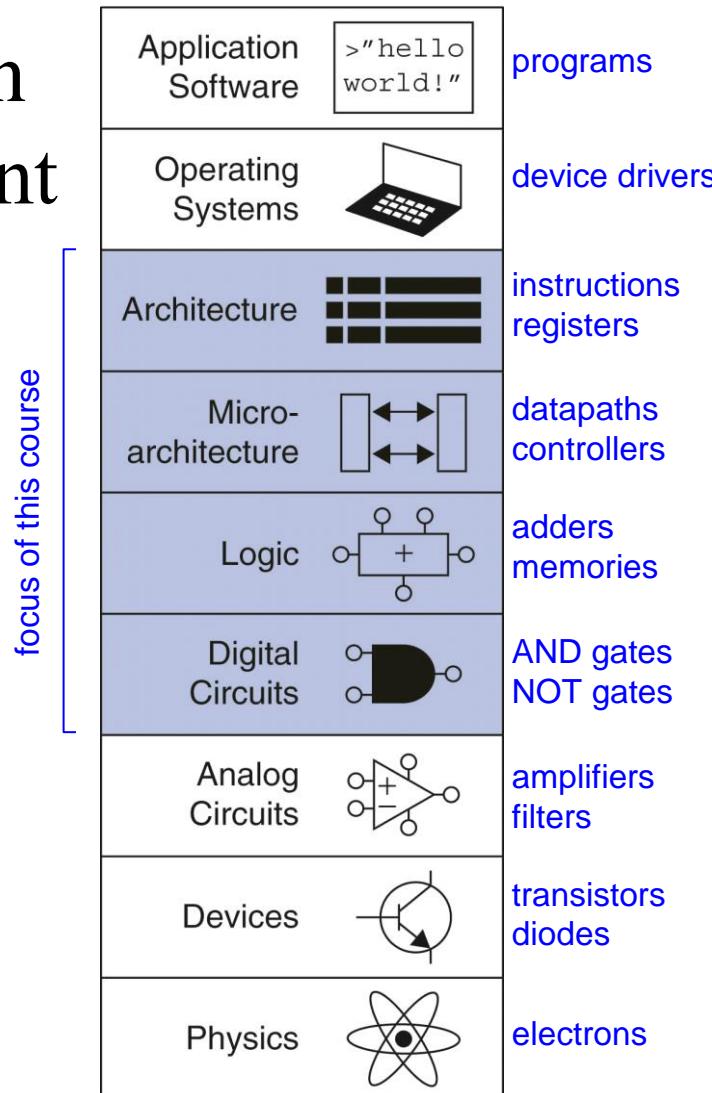
- Abstraction
- Discipline
- The Three –y's
  - Hierarchy
  - Modularity
  - Regularity

# Thoughts on Complexity - Whack-A-Mole Design Fixes



# Abstraction

- Hiding details when they aren't important



# The Three -y's

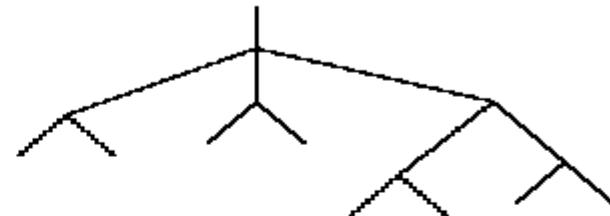
- **Hierarchy**
- **Modularity**
- **Regularity**

# The Three -Y's

- **Hierarchy**
  - A system divided into modules and submodules
- **Modularity**
  - Having well-defined functions and interfaces
- **Regularity**
  - Encouraging uniformity, so modules can be easily reused

# Design Hierarchy

- Helps control complexity -
  - by hiding details and reducing the total number of things to handle at any time.
- Modularizes the design -
  - divide and conquer
  - simplifies implementation and debugging
- Top-Down Design
  - Starts at the top (root) and works down by successive refinement.
- Bottom-up Design
  - Starts at the leaves & puts pieces together to build up the design.
- Which is better?
  - In practice both are needed & used.
    - Need top-down divide and conquer to handle the complexity.
    - Need bottom-up because in a well designed system, the structure is influenced by what primitives are available.

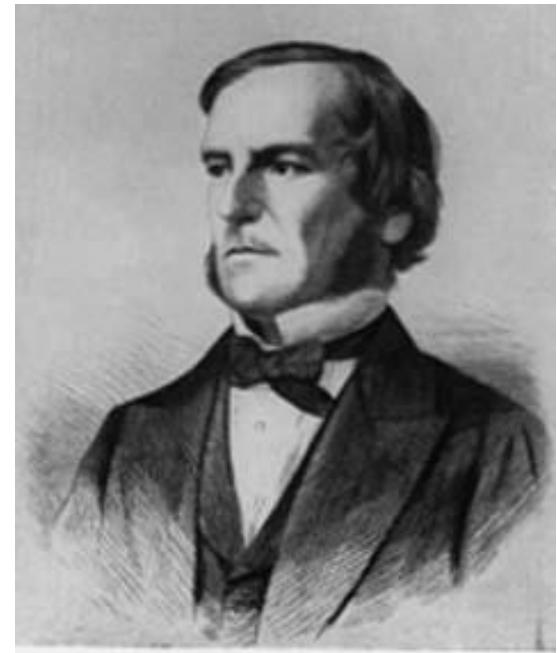


# Part 3

# Basics of Digital Logic

# George Boole, 1815 - 1864

- Born to working class parents
- Taught himself mathematics and joined the faculty of Queen's College in Ireland.
- Wrote *An Investigation of the Laws of Thought* (1854)
- Introduced binary variables
- Introduced the three fundamental logic operations: AND, OR, and NOT.



GEORGE BOOLE  
Scanned at the American  
Institute of Physics

# Digital Discipline: Binary Values

- Typically consider only two discrete values:
  - 1's and 0's
  - 1, TRUE, HIGH
  - 0, FALSE, LOW
- 1 and 0 can be represented by specific voltage levels, rotating gears, fluid levels, etc.
- Digital circuits usually depend on specific voltage levels to represent 1 and 0
- *Bit: Binary digit*

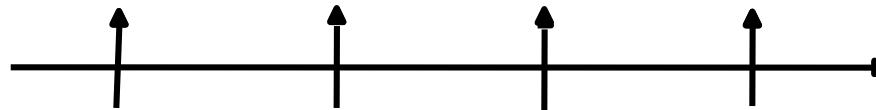
# INFORMATION REPRESENTATION - Signals

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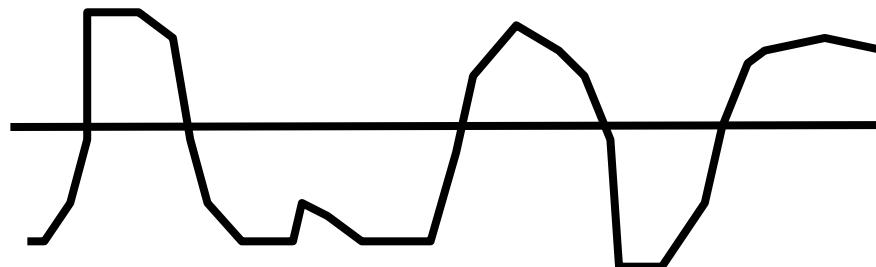
- **Information variables represented by physical quantities.**
- **For digital systems, the variables take on discrete values.**
- **Two level, or binary values are the most prevalent values in digital systems.**
- **Binary values are represented abstractly by:**
  - digits 0 and 1
  - words (symbols) False (F) and True (T)
  - words (symbols) Low (L) and High (H)
  - and words On and Off.
- **Binary values are represented by values or ranges of values of physical quantities**

# Signal Examples Over Time

Time



Analog



Continuous  
in value &  
time

Digital

Asynchronous



Discrete in  
value &  
continuous  
in time

Synchronous



Discrete in  
value & time

# Boolean Algebra and its Relation to Digital Circuits

- To understand the benefits of “logic gates” vs. switches, we should first understand Boolean algebra
- “Traditional” algebra
  - Variables represent real numbers (x, y)
  - Operators operate on variables, return real numbers ( $2.5*x + y - 3$ )
- **Boolean Algebra**
  - Variables represent 0 or 1 only
  - Operators return 0 or 1 only
  - Basic operators
    - AND:  $a \text{ AND } b$  returns 1 only when both  $a=1$  and  $b=1$
    - OR:  $a \text{ OR } b$  returns 1 if either (or both)  $a=1$  or  $b=1$
    - NOT:  $\text{NOT } a$  returns the opposite of  $a$  (1 if  $a=0$ , 0 if  $a=1$ )

a	b	AND
0	0	0
0	1	0
1	0	0
1	1	1

*a*

a	b	OR
0	0	0
0	1	1
1	0	1
1	1	1

a	NOT
0	1
1	0



# Relating Boolean Algebra to Digital Design

Boolean algebra  
(mid-1800s)

*Boole's intent: formalize  
human thought*

Switches  
(1930s)

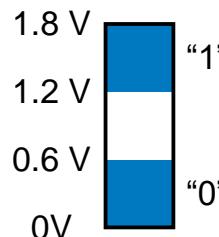
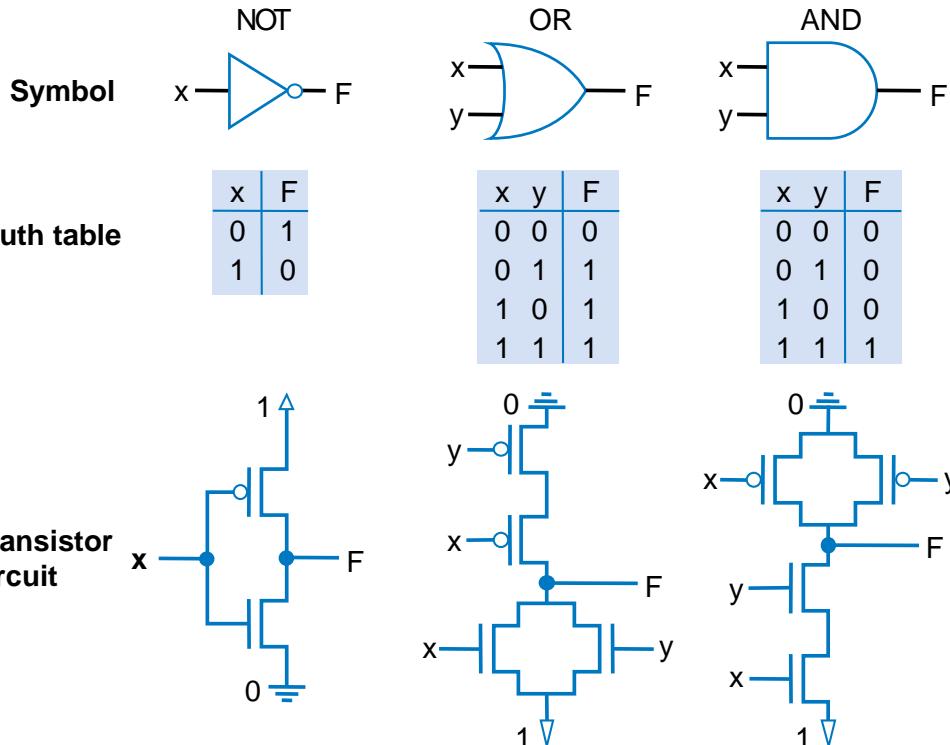
*For telephone  
switching and other  
electronic uses*

Shannon (1938)

*Showed application  
of Boolean algebra  
to design of switch-  
based circuits*

Digital design

- Implement Boolean operators using transistors
  - Call those implementations **logic gates**.
  - Lets us build circuits by doing math -
    - powerful concept



1 and 0 each actually corresponds to a voltage range

Next slides show how these circuits work.  
Note: The above OR/AND implementations are inefficient; we'll show why, and show better ones, later.



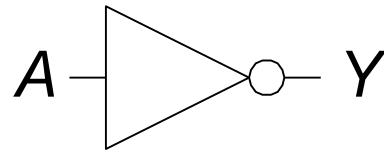
# Logic Gates

- **Perform logic functions:**
  - inversion (NOT), AND, OR, NAND, NOR, etc.
- **Single-input:**
  - NOT gate, buffer
- **Two-input:**
  - AND, OR, XOR, NAND, NOR, XNOR
- **Multiple-input**

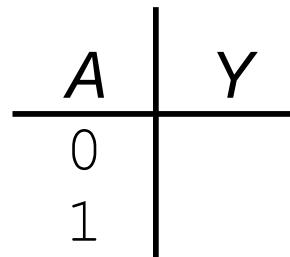


# Single-Input Logic Gates

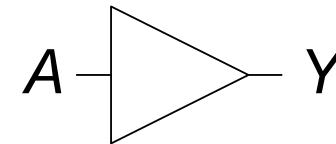
**NOT**



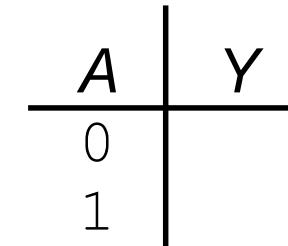
$$Y = \overline{A}$$



**BUF**

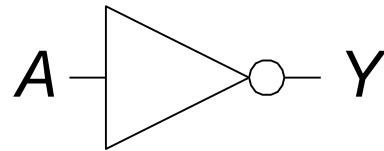


$$Y = A$$



# Single-Input Logic Gates

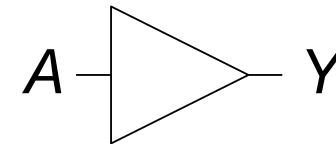
**NOT**



$$Y = \overline{A}$$

$A$	$Y$
0	1
1	0

**BUF**

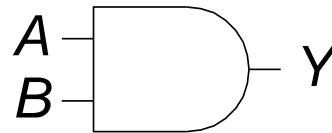


$$Y = A$$

$A$	$Y$
0	0
1	1

# Two-Input Logic Gates

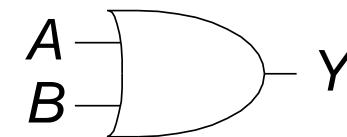
**AND**



$$Y = AB$$

A	B	Y
0	0	
0	1	
1	0	
1	1	

**OR**

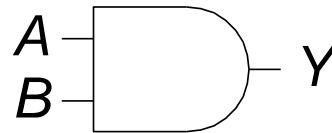


$$Y = A + B$$

A	B	Y
0	0	
0	1	
1	0	
1	1	

# Two-Input Logic Gates

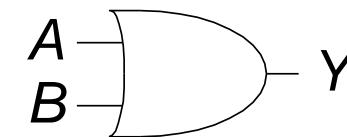
**AND**



$$Y = AB$$

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

**OR**

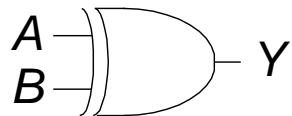


$$Y = A + B$$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

# More Two-Input Logic Gates

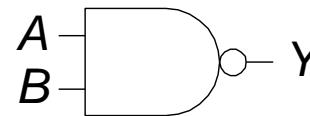
**XOR**



$$Y = A \oplus B$$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

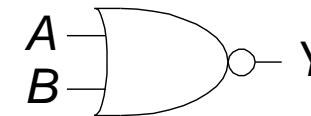
**NAND**



$$Y = \overline{AB}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

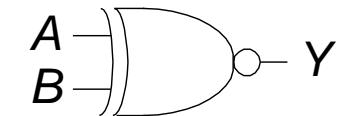
**NOR**



$$Y = \overline{A + B}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

**XNOR**

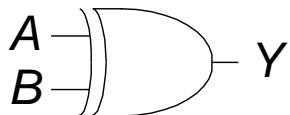


$$Y = \overline{A \oplus B}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

# More Two-Input Logic Gates

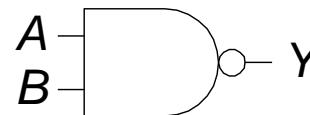
**XOR**



$$Y = A \oplus B$$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

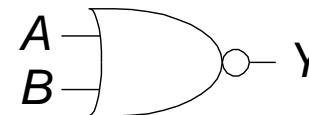
**NAND**



$$Y = \overline{AB}$$

A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

**NOR**



$$Y = \overline{A + B}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

**XNOR**

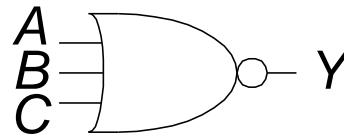


$$Y = \overline{A \oplus B}$$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

# Multiple-Input Logic Gates

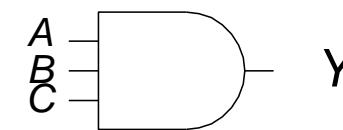
NOR3



$$Y = \overline{A+B+C}$$

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

AND3

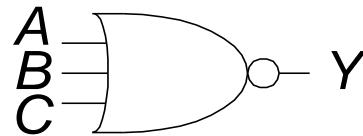


$$Y = ABC$$

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

# Multiple-Input Logic Gates

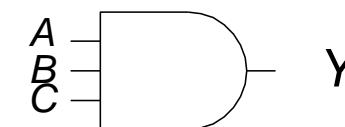
NOR3



$$Y = \overline{A+B+C}$$

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

AND3



$$Y = ABC$$

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

- Multi-input XOR: Odd parity

# Logic Levels

- Discrete voltages represent 1 and 0
- For example:
  - 0 = *ground* (GND) or 0 volts
  - 1 =  $V_{DD}$  or 5 volts
- What about 4.99 volts? Is that a 0 or a 1?
- What about 3.2 volts?

# Logic Levels

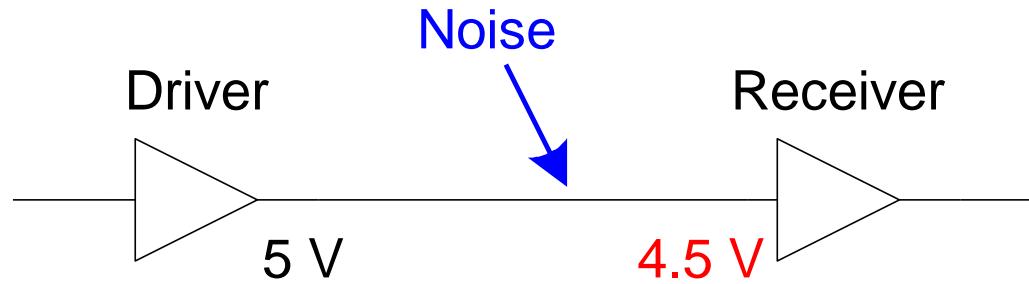
- *Range* of voltages for 1 and 0
- Different ranges for inputs and outputs to allow for *noise*

FROM ZERO TO ONE

# What is Noise?

# What is Noise?

- **Anything that degrades the signal**
  - E.g., resistance, power supply noise, coupling to neighboring wires, etc.
- **Example:** a gate (driver) outputs 5 V but, because of resistance in a long wire, receiver gets 4.5 V

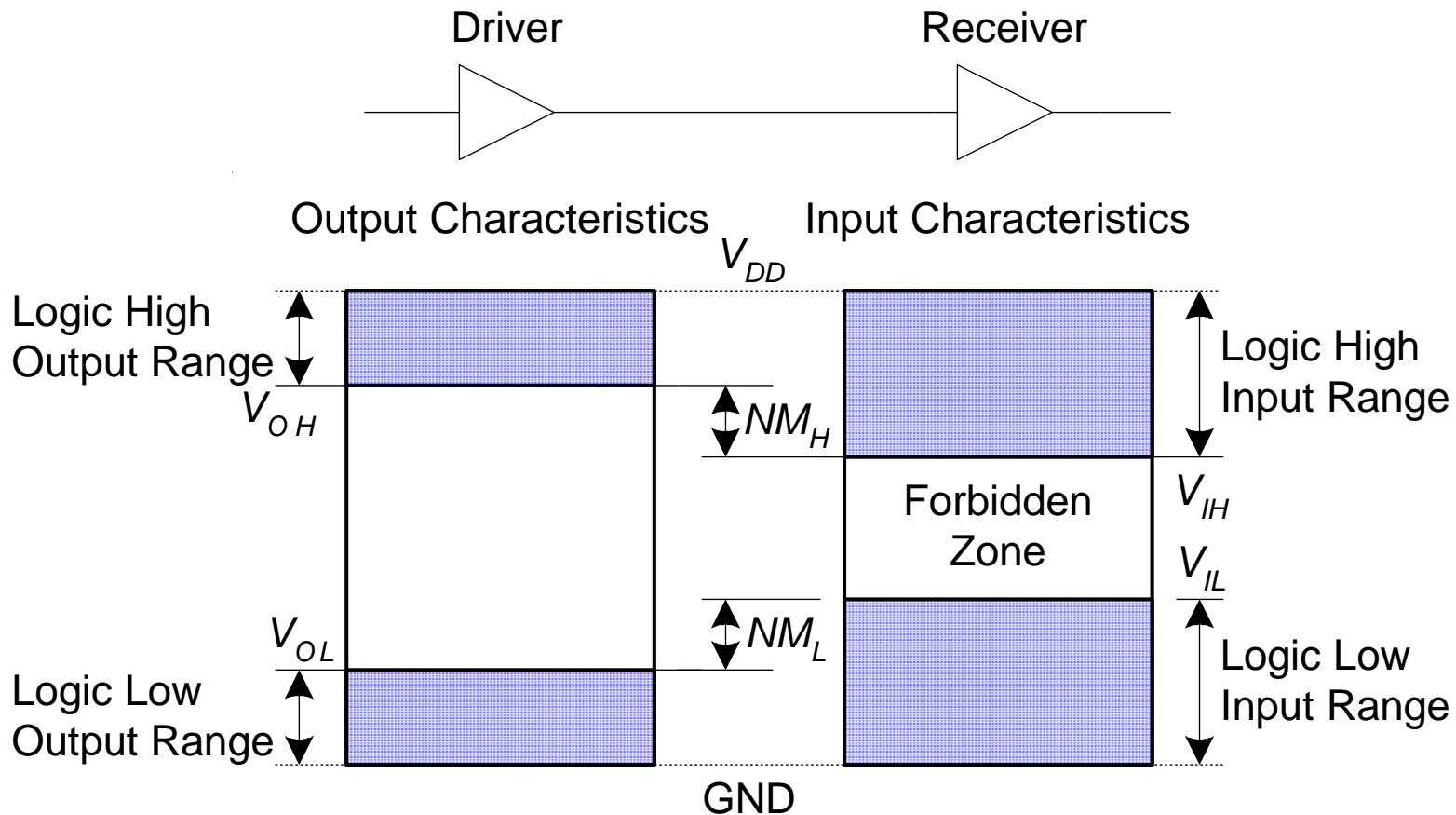


# The Static Discipline

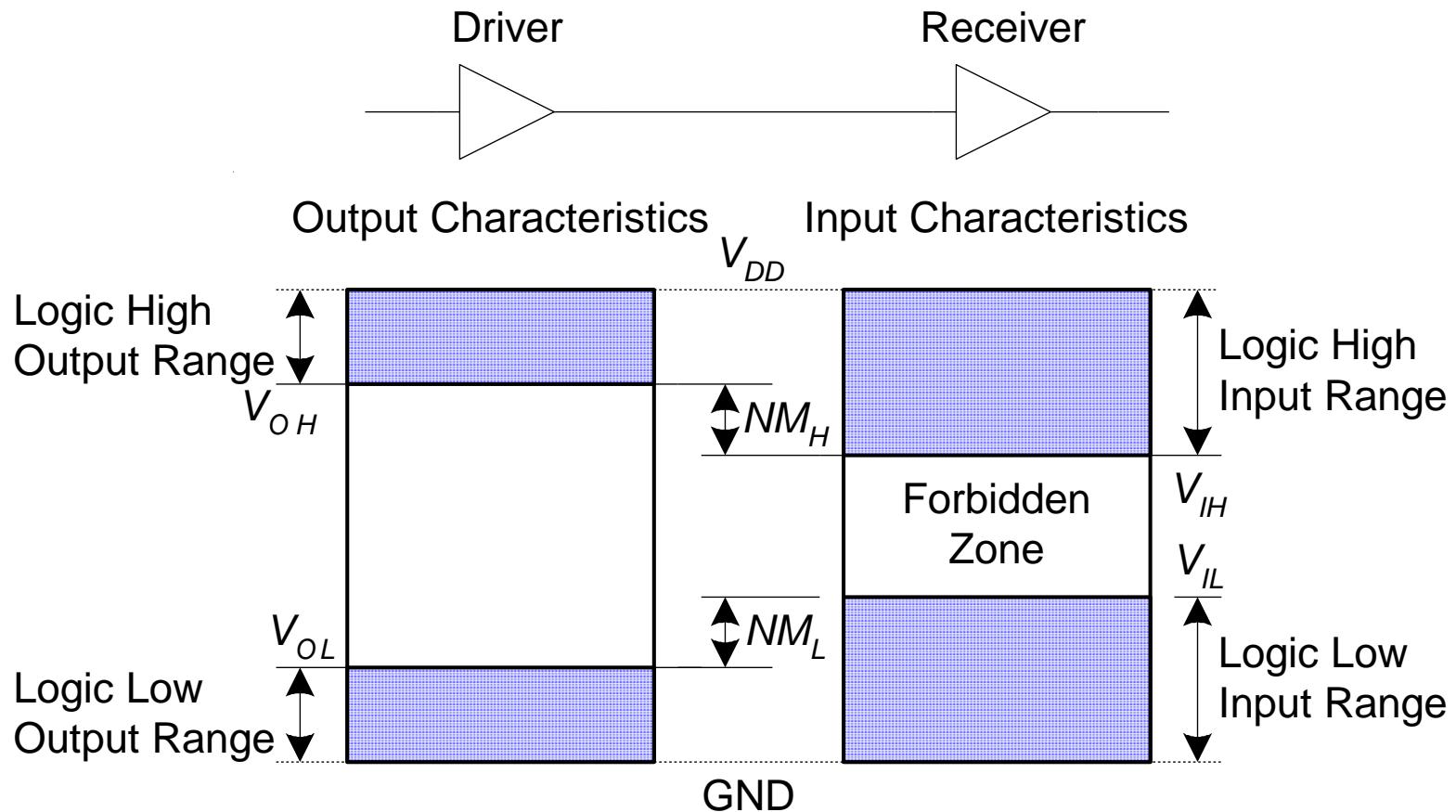
- With logically valid inputs, every circuit element must produce logically valid outputs
- Use limited ranges of voltages to represent discrete values



# Logic Levels



# Noise Margins

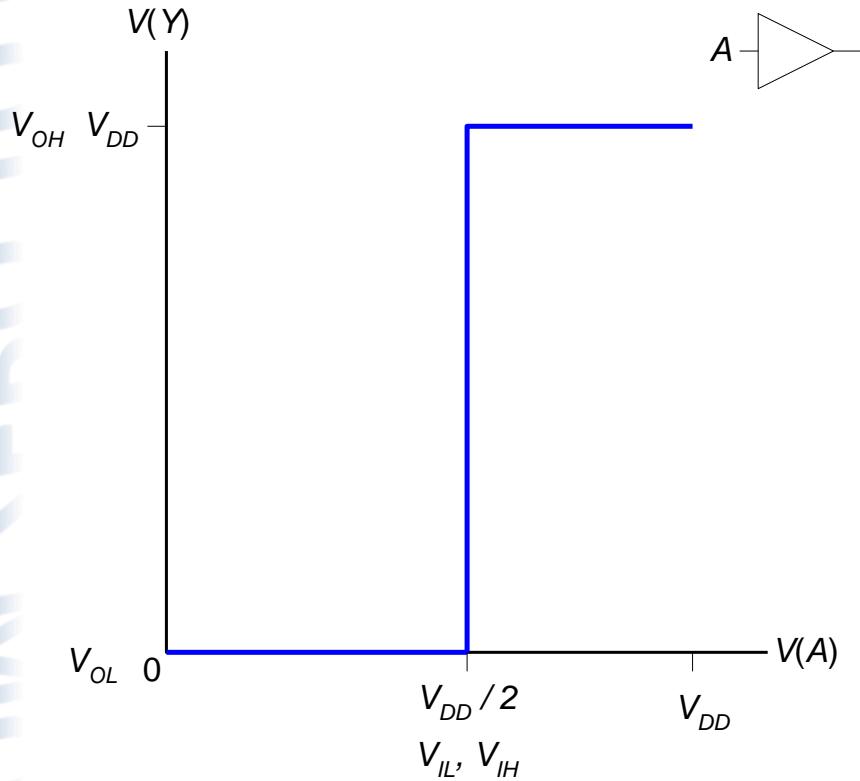


$$NM_H = V_{OH} - V_{IH}$$

$$NM_L = V_{IL} - V_{OL}$$

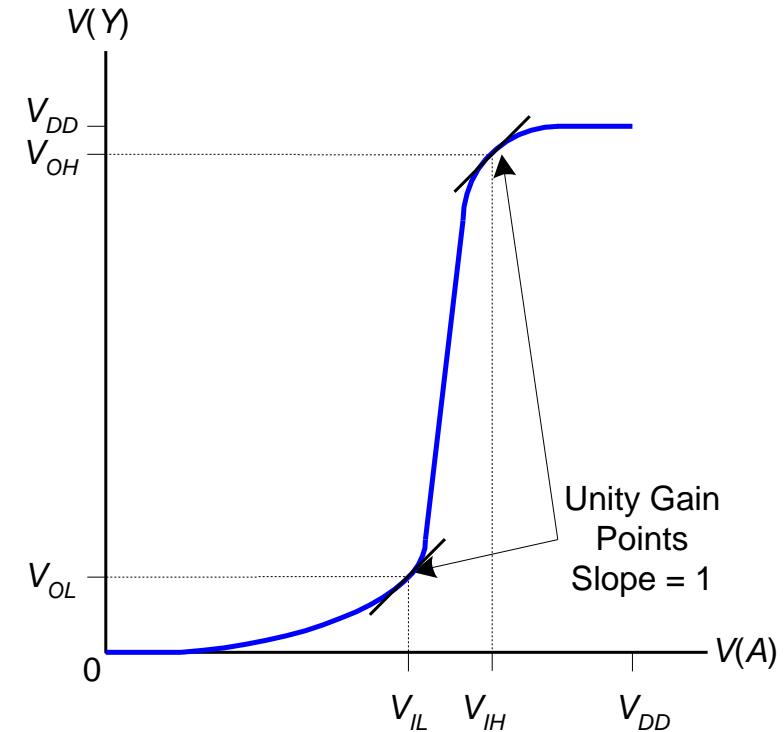
# DC Transfer Characteristics

Ideal Buffer:



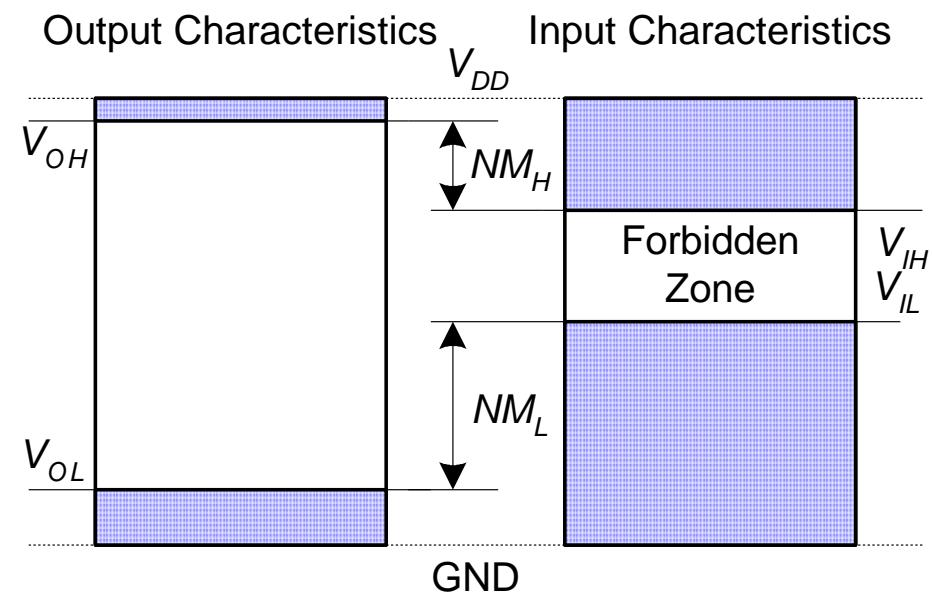
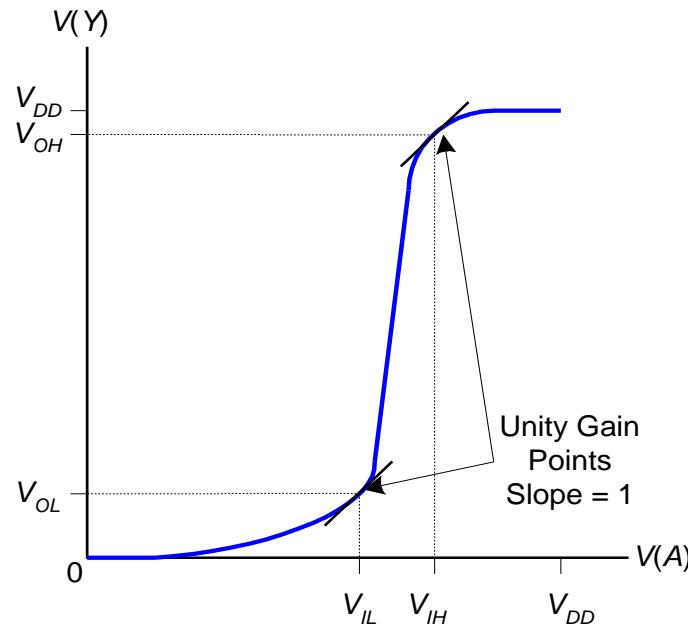
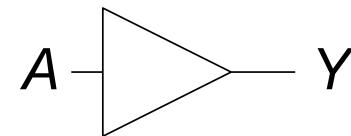
$$NM_H = NM_L = V_{DD}/2$$

Real Buffer:



$$NM_H, NM_L < V_{DD}/2$$

# DC Transfer Characteristics



# Logic Family Examples

Logic Family	$V_{DD}$	$V_{IL}$	$V_{IH}$	$V_{OL}$	$V_{OH}$
TTL	5 (4.75 - 5.25)	0.8	2.0	0.4	2.4
CMOS	5 (4.5 - 6)	1.35	3.15	0.33	3.84
LV TTL	3.3 (3 - 3.6)	0.8	2.0	0.4	2.4
LV CMOS	3.3 (3 - 3.6)	0.9	1.8	0.36	2.7

# Boolean Algebra and its Relation to Digital Circuits

- Developed mid-1800's by George Boole to formalize human thought
  - Ex: "I'll go to lunch if Mary goes OR John goes, AND Sally does not go."
    - Let F represent my going to lunch (1 means I go, 0 I don't go)
    - Likewise, m for Mary going, j for John, and s for Sally
    - Then  $F = (m \text{ OR } j) \text{ AND } \text{NOT}(s)$
  - Nice features
    - Formally evaluate
      - $m=1, j=0, s=1 \rightarrow F = (1 \text{ OR } 0) \text{ AND } \text{NOT}(1) = 1 \text{ AND } 0 = \underline{0}$
    - Formally transform
      - $F = (m \text{ and } \text{NOT}(s)) \text{ OR } (j \text{ and } \text{NOT}(s))$ 
        - » Looks different, but same function
        - » We'll show transformation techniques soon
    - Formally prove
      - Prove that if Sally goes to lunch ( $s=1$ ), then I don't go ( $F=0$ )
      - $F = (m \text{ OR } j) \text{ AND } \text{NOT}(1) = (m \text{ OR } j) \text{ AND } 0 = 0$

a	b	AND
0	0	0
0	1	0
1	0	0
1	1	1

a	b	OR
0	0	0
0	1	1
1	0	1
1	1	1

a	NOT
0	1
1	0



# Converting to Boolean Equations

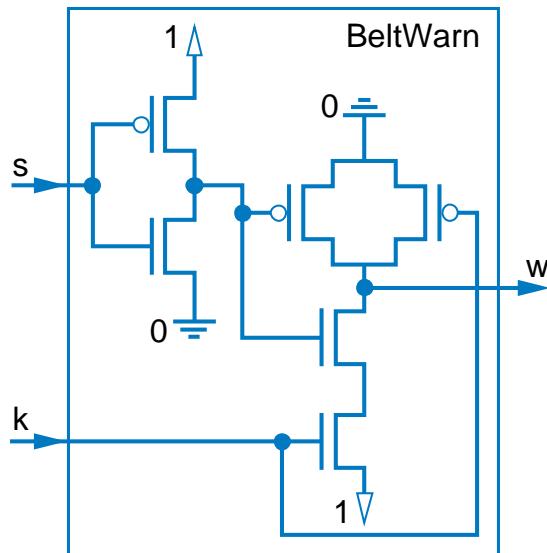
- Q1. A fire sprinkler system should spray water if high heat is sensed and the system is set to enabled.
  - Answer: Let Boolean variable  $h$  represent “high heat is sensed,”  $e$  represent “enabled,” and  $F$  represent “spraying water.” Then an equation is:  $F = h \text{ AND } e$ .
- Q2. A car alarm should sound if the alarm is enabled, and either the car is shaken or the door is opened.
  - Answer: Let  $a$  represent “alarm is enabled,”  $s$  represent “car is shaken,”  $d$  represent “door is opened,” and  $F$  represent “alarm sounds.” Then an equation is:  $F = a \text{ AND } (s \text{ OR } d)$ .
  - (a) Alternatively, assuming that our door sensor  $d$  represents “door is closed” instead of open (meaning  $d=1$  when the door is closed, 0 when open), we obtain the following equation:  $F = a \text{ AND } (s \text{ OR } \text{NOT}(d))$ .



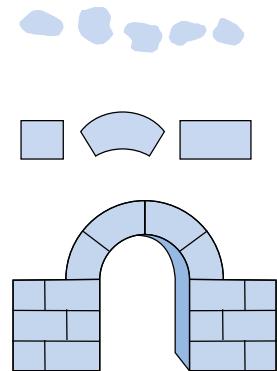
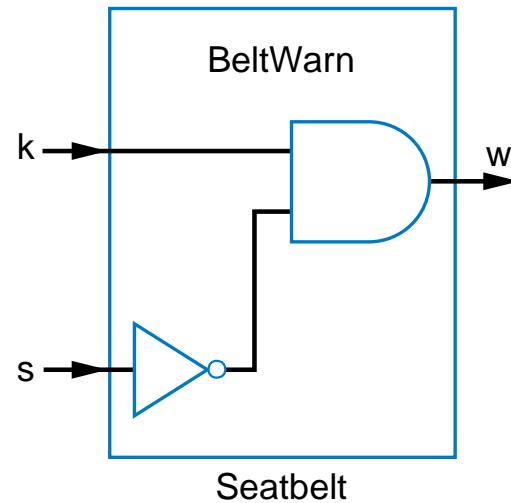
# Gates vs. switches

## Notice

- Boolean algebra enables easy capture as equation and conversion to circuit
  - How design with switches?
  - Of course, logic gates are built from switches, but we think at level of logic gates, not switches



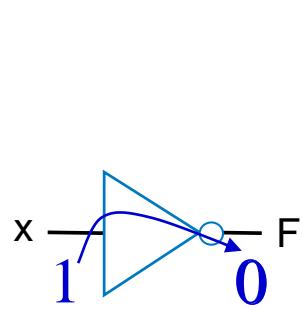
$$w = \text{NOT}(s) \text{ AND } k$$



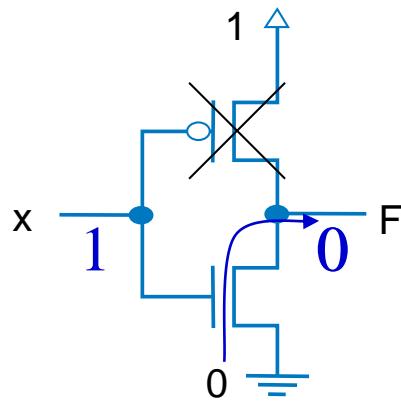
# State Representing a bit

Technology	State Representing Bit	
	0	1
Relay logic	Circuit open	Circuit closed
CMOS logic	0-1.5V	3.5-5V
Transistor-transistor logic	0-0.8V	2-5V
Fiber optics	Light off	Light on
Dynamic memory	Capacitor discharged	Capacitor charged
Nonvolatile, erasable memory	Electrons trapped	Electrons released
Bipolar read-only memory	Fuse blown	Fuse intact
Magnetic tape or disk	Flux direction N	Flux direction S
Read-only compact disc	No pit	Pit
Writable compact disc (CD-R)	Dye in crystalline state	Dye in noncrystalline state

# Relating a Logic Gate Symbol, Circuit, Truth Table, and Timing Diagram



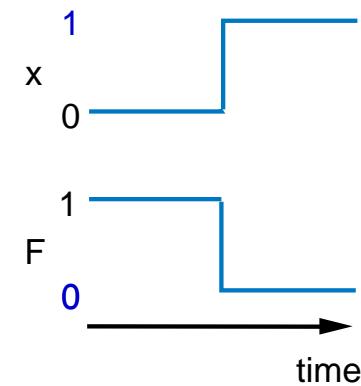
Symbol



Transistor circuit

$x$	$F$
0	1
1	0

Truth table

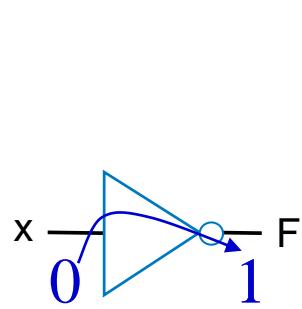


Timing diagram

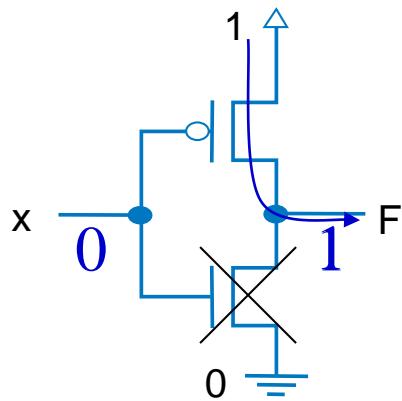
Setting  $x$  to 1 causes  $F$  to be 0



# Relating a Logic Gate Symbol, Circuit, Truth Table, and Timing Diagram



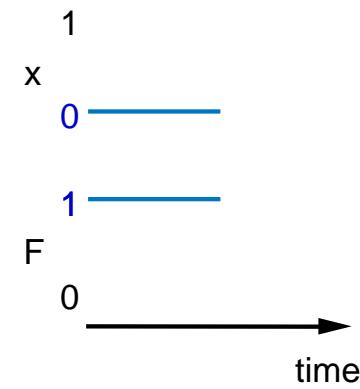
Symbol



Transistor circuit

$x$	$F$
0	1
1	0

Truth table



Timing diagram

Setting  $x$  to 0 causes  $F$  to be 1

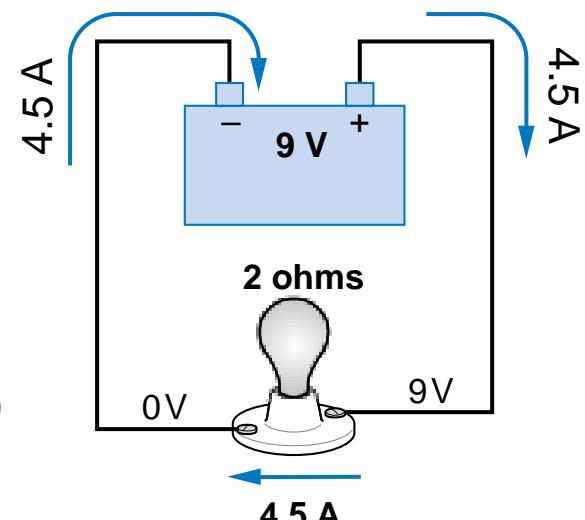


# Switches

- Electronic switches are the basis of binary digital circuits

- Electrical terminology

- **Voltage:** Difference in electric potential between two points (volts, V)
  - Analogous to water pressure
- **Resistance:** Tendency of wire to resist current flow (ohms,  $\Omega$ )
  - Analogous to water pipe diameter
- **Current:** Flow of charged particles (amps, A)
  - Analogous to water flow
- $V = I * R$  (Ohm's Law)
  - $9V = I * 2\ \Omega$
  - $I = 4.5\ A$

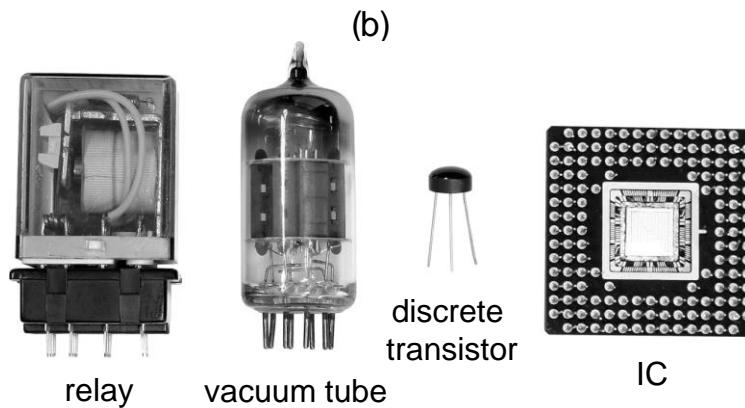
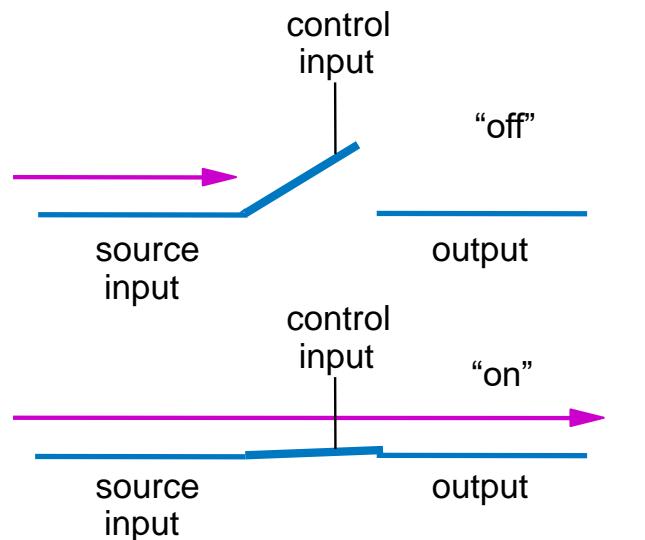


If a 9V potential difference is applied across a 2 ohm resistor, then 4.5 A of current will flow.



# Switches

- A switch has three parts
  - Source input, and output
    - Current tries to flow from source input to output
  - Control input
    - Voltage that controls whether that current can flow
- The amazing shrinking switch
  - 1930s: Relays
  - 1940s: Vacuum tubes
  - 1950s: Discrete transistor
  - 1960s: Integrated circuits (ICs)
    - Initially just a few transistors on IC
    - Then tens, hundreds, thousands...

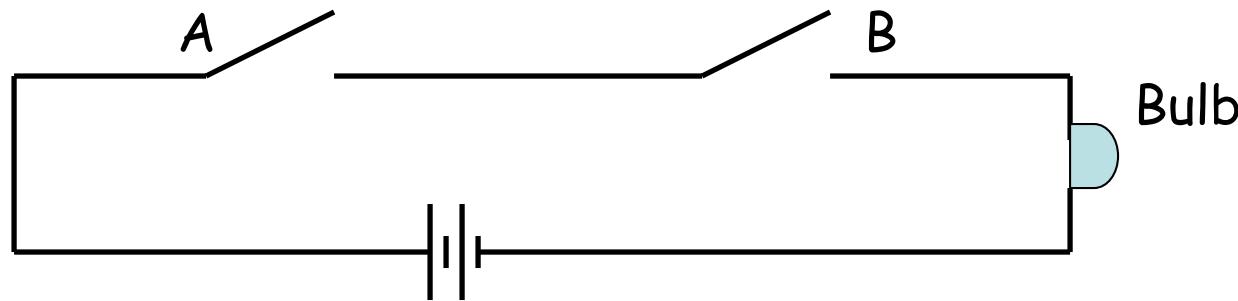


quarter  
(to see the relative size)



## Logic gates

As a first example consider the following lighting circuit with two switches A and B



Q. Under what conditions will the bulb light ?

A.

The bulb will light  
ONLY when both switches A AND B are closed. This can be represented in a Truth Table.

Switch A	Switch B	Output y
Open	Open	NO
Open	Closed	NO
Closed	Open	NO
Closed	Closed	YES

In binary logic we will denote a zero or low voltage by a digital 0 and a high voltage by a digital 1.

This type of truth table is called an AND table.

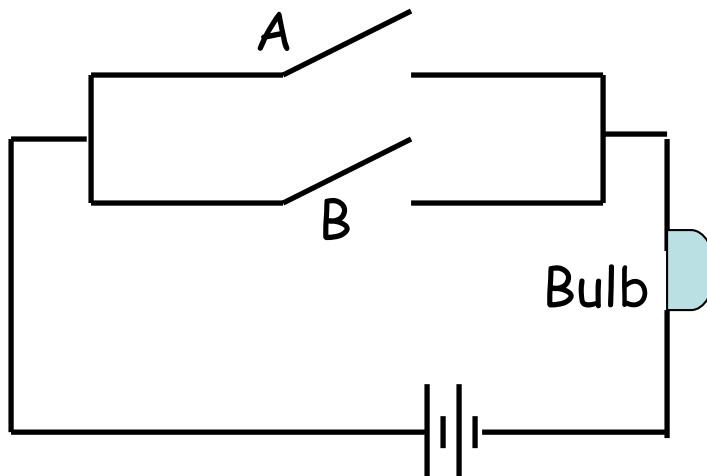
2 Input AND truth table. 1 output

A	B	y
0	0	0
0	1	0
1	0	0
1	1	1

Symbolically (Boolean) it is written as  
 $y = A \bullet B$  and is read as

'A AND B gives the output Y'

Here is another possible arrangement for the two switches.



In this arrangement the bulb can light if either switch A or B is closed.

This is an example of a circuit based on an OR gate.

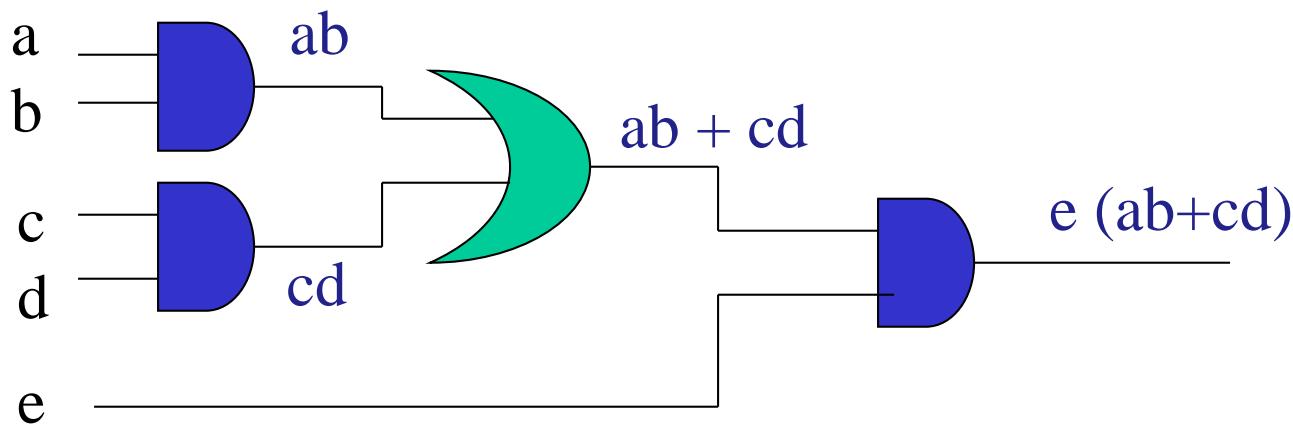
A	B	y
0	0	0
0	1	1
1	0	1
1	1	1

The 2 input OR table shows that if one or both inputs A and B are digital 1, the output is a digital 1.

The Boolean expression for an OR gate is  $Y = A + B$  and is read as

'Y is the output of A OR B'.

# Combinational Logic vs Boolean Algebra



Schematic Diagram:

5 primary inputs

4 components

9 signal nets

12 pins

Boolean Algebra:

5 literals

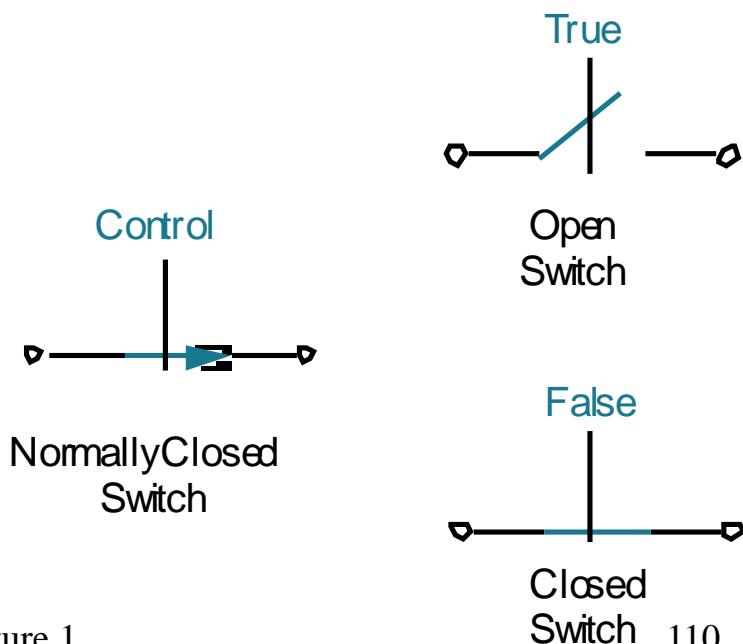
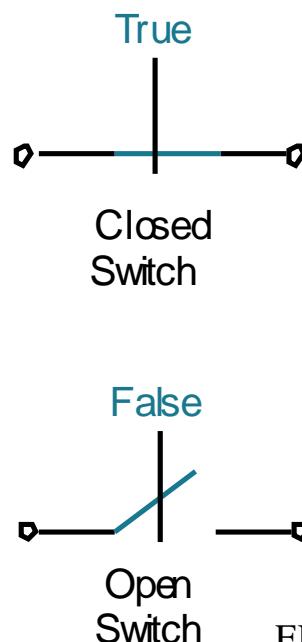
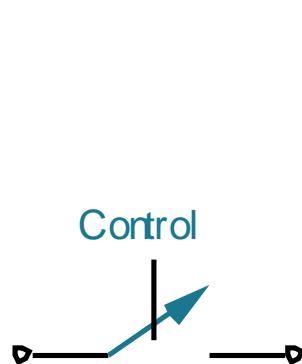
4 operators

# Digital Design: Switches

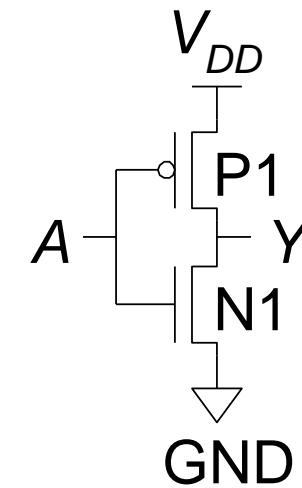
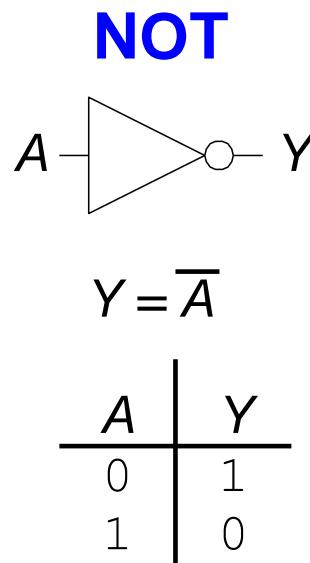
A switch connects two points under control signal.

**Normally Open**    when the control signal is 0 (false), the switch is open  
                          when it is 1 (true), the switch is closed

**Normally Closed**    when control is 1 (true), switch is open  
                          when control is 0 (false), switch is closed



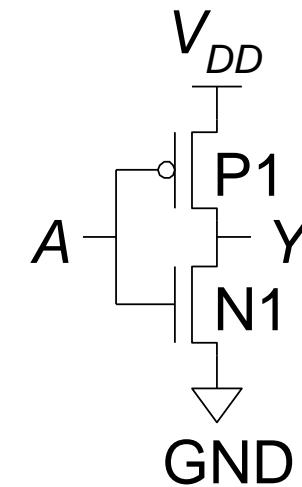
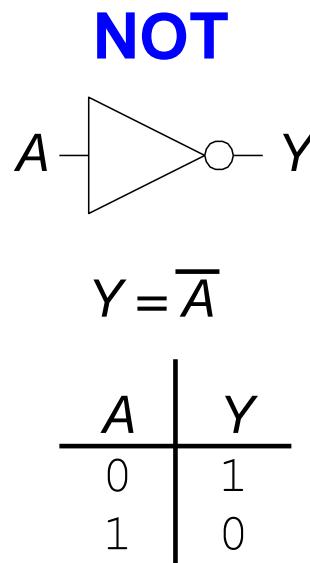
# CMOS Gates: NOT Gate



A	P1	N1	Y
0			
1			



# CMOS Gates: NOT Gate



A	P1	N1	Y
0	ON	OFF	1
1	OFF	ON	0



# Power Consumption

- Power = Energy consumed per unit time
  - Dynamic power consumption
  - Static power consumption

# Dynamic Power Consumption

- **Power to charge transistor gate capacitances**
  - Energy required to charge a capacitance,  $C$ , to  $V_{DD}$  is  $CV_{DD}^2$
  - Circuit running at frequency  $f$ : transistors switch (from 1 to 0 or vice versa) at that frequency
  - Capacitor is charged  $f/2$  times per second (discharging from 1 to 0 is free)
- Dynamic power consumption:

$$P_{dynamic} = \frac{1}{2}CV_{DD}^2f$$



# Static Power Consumption

- Power consumed when no gates are switching
- Caused by the *quiescent supply current*,  $I_{DD}$  (also called the *leakage current*)
- Static power consumption:

$$P_{static} = I_{DD}V_{DD}$$

# Power Consumption Example

- Estimate the power consumption of a wireless handheld computer
  - $V_{DD} = 1.2 \text{ V}$
  - $C = 20 \text{ nF}$
  - $f = 1 \text{ GHz}$
  - $I_{DD} = 20 \text{ mA}$

# Power Consumption Example

- Estimate the power consumption of a wireless handheld computer
  - $V_{DD} = 1.2 \text{ V}$
  - $C = 20 \text{ nF}$
  - $f = 1 \text{ GHz}$
  - $I_{DD} = 20 \text{ mA}$

$$\begin{aligned}P &= \frac{1}{2}CV_{DD}^2f + I_{DD}V_{DD} \\&= \frac{1}{2}(20 \text{ nF})(1.2 \text{ V})^2(1 \text{ GHz}) + \\&\quad (20 \text{ mA})(1.2 \text{ V}) \\&= \mathbf{(14.4 + 0.024) \text{ W} \approx 14.4 \text{ W}}\end{aligned}$$



# Chapter Summary

- Digital systems surround us
  - Inside computers
  - Inside many other electronic devices (embedded systems)
- Digital systems use 0s and 1s
  - Encoding analog signals to digital can provide many benefits
    - e.g., audio—higher-quality storage/transmission, compression, etc.
  - Encoding integers as 0s and 1s: Binary numbers
- Microprocessors (themselves digital) can implement many digital systems easily and inexpensively
  - But often not good enough—need custom digital circuits

