## **GIML: Tutorial Three**

1. Paste each of the following function definitions into ML and evaluate each a a few values. Be sure that you can see

```
fun d(0)= "de"
 2 | d(n)= "do"^d(n-1)^"da";
 4 fun h(0) = 1
   | h(n) = h(n-1) + h(n-1);
    fun m(a,0) = 0
 8
   \mid m(a,b) = a+m(a,b-1);
 9
10 fun f(0)= true
11 | f(n)= not(f(n-1));
12
13 fun g(0) = nil
   | g(n) = 0::g(n-1);
14
15
16 fun l(0)= nil
17 | l(n)= n mod 10 :: l(n div 10);
18
19 fun j(0) = 0
20 | j(n)= (n \mod 10) + j(n \operatorname{div} 10);
- val d = fn : int -> string
val h = fn : int -> int
val m = fn : int * int -> int
val f = fn : int -> bool
val g = fn : int -> int list
val l = fn : int -> int list
val j = fn : int -> int
```

2. Each of the following functions can be defined in a similar way. An example has been given in each case:

```
fun sumto(0) = 0
    | sumto(n) = n + sumto(n - 1);
 3
    fun listfrom(0) = nil
    listfrom(n) = n :: listfrom(n - 1);
    fun strcopy(a, \emptyset) = ""
    | strcopy(a, nr) = a \wedge strcopy(a, nr - 1);
 9
10
    fun power(nr, \emptyset) = 1
11
    | power(nr, pow) = nr * power(nr, pow - 1);
12
13
    fun listcopy(ls, 0) = nil
    listcopy(ls, nr) = ls :: listcopy(ls, nr - 1
14
        );
15
    fun sumEvens(0) = 0
16
    | sumEvens(nr) = if nr mod 2 = 0 then nr +
        sumEvens(nr - 1)
18
    else sumEvens(nr - 1);
19
20 fun listOdds(0) = nil
21
    | listOdds(nr) = if nr mod 2 = 1 then nr ::
        listOdds(nr - 1)
    else listOdds(nr - 1);
22
22
    else list0dds(nr - 1);
23
    fun nat(0) = "zero"
24
    | nat(nr) = "succ(" ^ nat(nr - 1) ^ ")";
25
26
27 fun listto(0) = nil
   listto(nr) = listto(nr - 1) @ [nr];
- val sumto = fn : int -> int
val listfrom = fn : int -> int list
val strcopy = fn : string * int -> string
val power = fn : int * int -> int
val listcopy = fn : 'a * int -> 'a list
val sumEvens = fn : int -> int
val listOdds = fn : int -> int list
val nat = fn : int -> string
val listto = fn : int -> int list
```