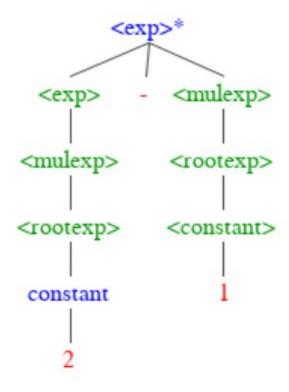
CSC 301 Assignment 13 Baheem Ferrell

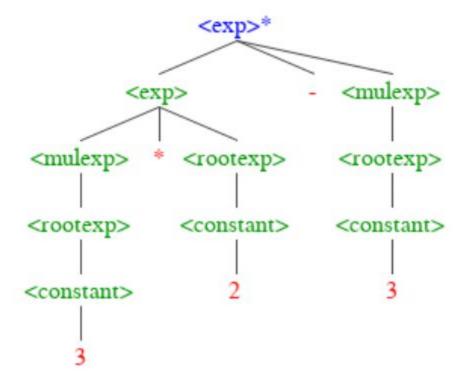
```
1.)
<exp>* ::= <exp> + <mulexp> | <exp> - <mulexp> | <mulexp>
       <mulexp> ::= <mulexp> * <rootexp> | <rootexp>
       <rootexp> ::= (<exp>) | <constant>
       <constant> ::= all valid integer constants
2.)
       val1(plus(X,Y),Value) :-
         val1(X, XValue),
         val1(Y, YValue),
         Value is XValue + YValue.
       val1(minus(X,Y),Value) :-
         val1(X, XValue),
         val1(Y, YValue),
         Value is XValue - YValue.
       val1(times(X,Y),Value):-
         val1(X,XValue),
         val1(Y,YValue),
         Value is XValue * YValue.
       val1(const(X),Value) :- Value is X.
3.)
```

 $\frac{E_1 \rightarrow V_1 E_2 \rightarrow V_2}{\text{minus}(E_1, E_2) \rightarrow V_1 - V_2}$

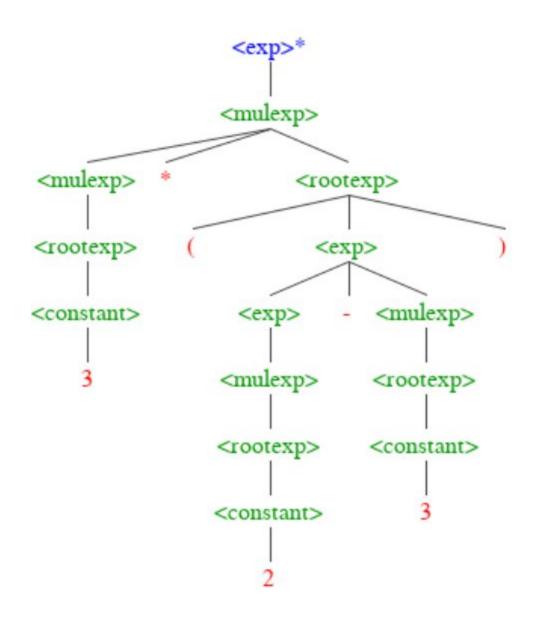
Parse tree for "2-1"



Parse tree for "3*2-3"



Parse tree for "3*(2-3)"



5.)

```
?- consult('reverse_list.pl').
true.
?- myflip([a,b,c,d,e,f],X).
X = [f, e, d, c, b, a].
?- myflip([a1,a2,a3,a4],X).
X = [a4, a3, a2, a1].
```

Natural semantic proof for "2-1"

$$\frac{\text{const (2)} \rightarrow 2 \text{ const (1)} \rightarrow 1}{\text{minus(const(2),const(1))} \rightarrow 2 - 1 = 1}$$

Natural semantic proof for "3*2-3"

$$\frac{const(3) \rightarrow 3 \ const(2) \rightarrow 2}{times(const(3), const(2)) \rightarrow 3 \ x \ 2 = 6 \ const(3) \rightarrow 3}$$
$$minus(times(const(3), const(2)), const(3)) \rightarrow 6 - 3 = 3$$

Natural semantic proof for "3*(2-3)"

$$\frac{const(2) \rightarrow 2 \ const(3) \rightarrow 3}{const(3) \rightarrow 3} \frac{const(3) \rightarrow 3}{minus(const(2), const(3)) \rightarrow 2 - 3 = -1}} times(const(3), minus(const(2), const(3))) \rightarrow 3 \ x \ (-1) = -3$$