Home Base, Part A

Beginning problems about numbers in various bases.

If you haven't already practiced, take an opportunity now.

Geogebra link: `https://tube.geogebra.org/m/1529377`

Geogebra link: `https://tube.geogebra.org/m/1527705`

Note: The "free response" answers are not checked for accuracy. To optimize your learning, submit your own answer before revealing the hint.

Problem 1 *To optimize my learning, I plan to* [*submit*] *my own answer (before ✓/ after) revealing the* [*hint*].

Problem 2 *Explain why the following "joke" is "funny:" There are* 10 *types of people in the world. Those who understand base two and those who don't.*

Free Response: ***Hint:*** *In base two, 10 is actually two. So people who do not understand base two will not get the joke.*

Problem 3 *You meet some Tripod aliens, they tally by threes. Thankfully for everyone involved, they use the symbols* 0, 1, *and* 2.

(a) *Demonstrate how a Tripod would count, beginning at* 11.

11, [12], [20], [21], [22], [100], [101], [102],
[110], [111], [112], [120], [121], [122], [200], [201]

(b) *What number comes immediately before* 10*?* [2]

(c) *Before* 210*?* [202]

(d) *Before* 20110*?* [20102] *Explain your reasoning.*

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Problem 4 *You meet some people who tally by sevens. They use the symbols O, A, B, C, D, E, and F, in that order. (Note: Although it is common to use the letters A through F for digits greater than ten, these people are doing something different.)*

(a) *What do the individual symbols O, A, B, C, D, E, and F mean? (Note O is not 0.)*

Free Response: ***Hint:*** *0, 1, 2, 3, 4, 5, and 6, respectively.*

(b) *Demonstrate how to count from DD to AOC? (Note: Case matters.)*

$DD, \boxed{DE}, \boxed{DF}, \boxed{EO}, \boxed{EA},$
$\boxed{EB}, \boxed{EC}, \boxed{ED}, \boxed{EF}, \boxed{FO},$
$\boxed{FA}, \boxed{FB}, \boxed{FC}, \boxed{FD}, \boxed{FE},$
$\boxed{FF}, \boxed{AOO}, \boxed{AOA}, \boxed{AOB}, \boxed{AOC}$

(c) *What number comes immediately before AO?* $\boxed{F}$

(d) *Before ABO?* $\boxed{AAF}$

(e) *Before $EOFFA$?* $\boxed{EOFFO}$

Problem 5 *Now, suppose that you meet a hermit who tallies by thirteens. Demonstrate the hermit's counting below.*

$8, 9, \boxed{A}, \boxed{B}, \boxed{C}, \boxed{10}, \boxed{11}, \boxed{12}, \ldots,$
$18, \boxed{19}, \boxed{1A}, \boxed{1B}, \boxed{1C}, \boxed{20}, \boxed{21}$
