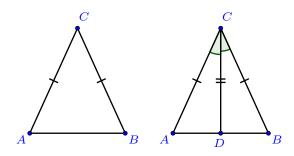
## The Isosceles Triangle Theorem

Proofs updated.

**Problem** 1 Prove that the base angles of an isosceles triangle are congruent.

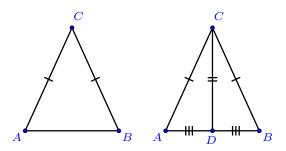
Fixnote: Below are several different proofs, along with one that is not a proof. Please consider them separately.



- (a) Beginning with the given figure on the left, Morgan draws  $\overline{CD}$  and marks the figure intending that this new segment is a(n) (median/ angle bisector  $\sqrt{\ }$  perpendicular bisector/ altitude).
- (b) Based on the marked figure, Morgan claims that the  $\triangle ACD \cong \triangle BCD$  by  $(SAS \checkmark/SSS/SSA/ASA/HL)$ .
- (c) Finally, Morgan concludes that  $\angle A\cong \angle B$ , as they are corresponding parts of congruent triangles.

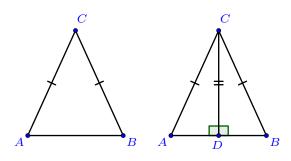
**Problem 2** Prove that the base angles of an isosceles triangle are congruent.

Learning outcomes: Author(s): Brad Findell



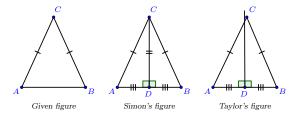
- (a) Beginning with the given figure on the left, Deja draws  $\overline{CD}$  and marks the figure intending that this new segment is a(n) (median  $\checkmark$ / angle bisector / perpendicular bisector / altitude).
- (b) Based on the marked figure, Deja claims that the  $\triangle ACD \cong \triangle BCD$  by  $(SAS/SSS \checkmark/SSA/ASA/HL)$ .
- (c) Finally, Deja concludes that  $\angle A \cong \angle B$ , as they are corresponding parts of congruent triangles.

**Problem 3** Prove that the base angles of an isosceles triangle are congruent.



- (a) Beginning with the given figure on the left, Elle draws  $\overline{CD}$  and marks the figure intending that this new segment is a(n) (median/ angle bisector/ perpendicular bisector/ altitude  $\checkmark$ ).
- (b) Based on the marked figure, Deja claims that the  $\triangle ACD \cong \triangle \boxed{BCD}$  by  $(SAS/SSS/SSA/ASA/HL \checkmark)$ .
- (c) Finally, Deja concludes that  $\angle A \cong \angle B$ , as they are corresponding parts of congruent triangles.

**Problem 4** Simon and Taylor are trying to prove that the base angles of an isosceles triangle are congruent.



Beginning with the given figure on the left, Simon draws  $\overline{CD}$  and marks the second figure intending that this new segment is a perpendicular bisector of  $\overline{AB}$ .

Taylor claims that a perpendicular bisector of a side of a triangle usually misses the opposite vertex. So without using other properties of isosceles triangles or perpendicular bisectors, the figure should allow for that possibility.

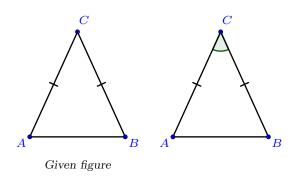
Fixnote: Taylor's claim needs some work, as is the case for the choices below.

Choose the best response to their argument:

## Multiple Choice:

- (a) Simon is correct, and  $\triangle ACD \cong \triangle BCD$  by SAS.
- (b) Simon is correct, and  $\triangle ACD \cong \triangle BCD$  by SSS
- (c) Taylor is correct, and the perpendicular bisector cannot be used to complete this proof.  $\checkmark$
- (d) Neither of them are correct.

**Problem 5** Prove that the base angles of an isosceles triangle are congruent.



- (a) Examining the given figure on the left, Lissy notices symmetry in the triangle and claims that the triangle is congruent to itself by a (translation / reflection  $\sqrt{}$  rotation).
- (b) Based on the marked figure, Lissy claims that the  $\triangle ACB \cong \triangle \boxed{BCA}$  by  $(SAS \checkmark/SSS/SSA/ASA/HL)$ .
- (c) Finally, Lissy concludes that  $\angle A\cong \angle B$ , as they are corresponding parts of congruent triangles.