# HW 1: Sets, Vocabulary, and Measuring

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### Set Theory Problems

Short-answer problems.

**Problem** 1 Given two sets X and Y,  $X \cup Y$  is the set of elements that are

#### Multiple Choice:

- (a) in X or in Y (but not in both).
- (b) in X or in Y (or both, as the "or" is inclusive).
- (c) in X and in Y.
- (d) in X but not in Y.
- (e) in Y but not in X.

**Problem 2** Given two sets X and Y,  $X \cap Y$  is the set of elements that are

#### Multiple Choice:

- (a) in X or in Y (but not in both).
- (b) in X or in Y (or both, as the "or" is inclusive).
- (c) in X and in Y.
- (d) in X but not in Y.
- (e) in Y but not in X.

**Problem 3** Given two sets X and Y, X - Y is the set of elements that are

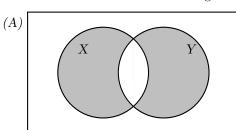
#### Multiple Choice:

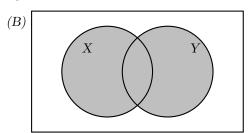
- (a) in X or in Y (but not in both).
- (b) in X or in Y (or both, as the "or" is inclusive).

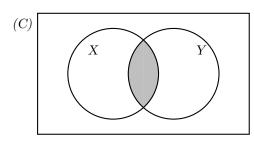
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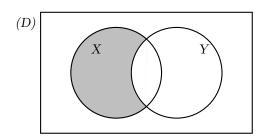
- (c) in X and in Y.
- (d) in X but not in Y.
- (e) in Y but not in X.

**Problem 4** Consider the following Venn diagrams:









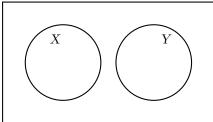
For each set expression below, identify the Venn diagram above in which the corresponding region is shaded:

- (a)  $X \cap Y$  is figure ?
- (b)  $X \cup Y$  is figure ?
- (c) X Y is figure ?

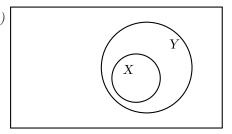
**Problem 5** Draw a Venn diagram for the set of elements that are in X or Y but not both. How does it differ from the Venn diagram for  $X \cup Y$ ?

**Problem 6** Consider the following Venn diagrams:

(A)



(B)



- (a) If Venn diagram (A) above shows the relationship between sets X and Y, then  $X \cap Y = (0/\emptyset/X \cup Y)$  and the sets are said to be (disjoint/empty/subsets).
- (b) If Venn diagram (B) above shows the relationship between sets X and Y, then we say that  $(X \text{ and } Y \text{ are disjoint} / X \subseteq Y / Y \subseteq X)$ .
- (c) If we let X be the set of "right triangles" and we let Y be the set of "equilateral triangles" which diagram above shows the relationship between these two sets?

#### Multiple Choice:

- (i) Diagram (A).
- (ii) Diagram (B).
- (iii) Neither of these.
- (iv) Not enough information.

Explain your reasoning.

**Problem 7** If  $X = \{1, 2, 3, 4, 5\}$  and  $Y = \{3, 4, 5, 6\}$  find the following: (List elements in ascending order, separated by commas, with no spaces.)

- (a)  $X \cup Y = \{ ? \}$
- (b)  $X \cap Y = \{ \boxed{?} \}$
- (c)  $X Y = \{ ? \}$
- (d)  $Y X = \{ ? \}$

**Problem 8** Let  $n\mathbb{Z}$  represent the integer multiples of n. So for example:

$$3\mathbb{Z} = \{\dots, -12, -9, -6, -3, 0, 3, 6, 9, 12, \dots\}$$

Compute the following (use capital Z for  $\mathbb{Z}$ ):

- (a)  $3\mathbb{Z} \cap 4\mathbb{Z} = \boxed{?}$
- (b)  $2\mathbb{Z} \cap 5\mathbb{Z} = \boxed{?}$
- (c)  $3\mathbb{Z} \cap 6\mathbb{Z} = \boxed{?}$
- (d)  $4\mathbb{Z} \cap 6\mathbb{Z} = \boxed{?}$
- (e)  $4\mathbb{Z} \cap 10\mathbb{Z} = \boxed{?}$

**Problem 9** Make a general rule for intersecting sets of the form  $n\mathbb{Z}$  and  $m\mathbb{Z}$ . Explain why your rule works.

**Problem 10** If  $X \cup Y = X$ , what can we say about the relationship between the sets X and Y? Explain your reasoning.

 $(X\subseteq Y\ /\ X=Y\ /\ Y\subseteq X\ /\ X=\emptyset)$  because every element of  $(X\ /\ Y)$  must be in  $(X\ /\ Y).$ 

**Problem** 11 If  $X \cap Y = X$ , what can we say about the relationship between the sets X and Y? Explain your reasoning.

 $(X \subseteq Y / X = Y / Y \subseteq X / X = \emptyset)$  because every element of (X / Y) must be in (X / Y).

**Problem 12** If  $X - Y = \emptyset$ , what can we say about the relationship between the sets X and Y? Explain your reasoning.

 $(X\subseteq Y\,/\,X=Y\,/\,Y\subseteq X\,/\,X=\emptyset)$  because every element of  $(X\,/\,Y)$  must be in  $(X\,/\,Y)$ .

## Extra Set Theory Problems

More short-answer problems.

#### Reminders

- Sets are collections of objects such as numbers or points. The objects are called *elements* of the set, and the order elements are listed is not important.
- The notation  $\{7,3\}$  means "The set containing 7 and 3."
- Note that {8} is not the same as the number 8 but rather is a set that contains one element that happens to be a number.
- The set containing zero elements, sometimes call the *empty set* is denoted  $\{\}$  or  $\emptyset$ .
- The elements of a set can themselves be sets.

**Problem 13** Indicate the number of elements in each set:

- (a) The set  $\{3,5,6,9,10\}$  has ? element(s).
- (b) The set  $\{\{3,2,7\},\{4,5\},\{2\},\emptyset\}$  has ? element(s).
- (c) The set  $\{\{\}\}$  has  $\boxed{?}$  element(s).
- (d) The set  $\{\}$  has ? element(s).
- (e) The set  $\emptyset$  has ? element(s).
- (f) The set  $\{\emptyset\}$  has  $\boxed{?}$  element(s).

**Problem 14** Indicate whether each statement is true or false:

- (a)  $2 \in \{3, 2, 5\}$ . (True/False)
- (b)  $2 \subseteq \{3, 2, 5\}$ . (*True* / *False*)
- (c)  $\{2\} \in \{3, 2, 5\}$ . (True/False)

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#### Extra Set Theory Problems

- (d)  $\{2\} \subseteq \{3, 2, 5\}$ . (True/False)
- (e)  $\emptyset = \{\}$ . (True/False)
- (f)  $\emptyset = {\emptyset}$ . (True/False)
- (g)  $\{\emptyset\} = \{\{\}\}\$ . (True/False)
- (h)  $\emptyset \in \{\emptyset\}$ . (True/False)
- (i)  $\emptyset \subseteq \{\emptyset\}$ . (True/False)
- (j)  $2 \in \{\{3, 2, 7\}, \{4, 5\}, \{2\}, \emptyset\}$ . (True/False)
- (k)  $2 \subseteq \{\{3,2,7\}, \{4,5\}, \{2\}, \emptyset\}$ . (True/False)
- (l)  $\{2\} \in \{\{3,2,7\},\{4,5\},\{2\},\emptyset\}$ . (True/False)
- (m)  $\{2\} \subseteq \{\{3,2,7\},\{4,5\},\{2\},\emptyset\}$ . (True/False)
- (n)  $\{\{2\}\} \in \{\{3, 2, 7\}, \{4, 5\}, \{2\}, \emptyset\}$ . (True/False)
- (o)  $\{\{2\}\}\subseteq \{\{3,2,7\},\{4,5\},\{2\},\emptyset\}$ . (True/False)

**Problem 15** Explain the difference between the symbols  $\in$  and  $\subseteq$ .

**Problem 16** How is  $\{\emptyset\}$  different from  $\emptyset$ ?

# Vocabulary and Notation

 $Short\text{-}answer\ questions.$ 

Question 17 An equilateral quadrilateral is called a ?.
Question 18 An equiangular quadrilateral is called a ?.
Question 19 An regular quadrilateral is called a ?. (Note: A regular polygon is both equilateral and equiangular.)
Question 20 If A and B are points, then
(a) $\overrightarrow{AB}$ denotes a $?$ ,
(b) $\overrightarrow{AB}$ denotes a $?$ with endpoint $?$ ,
(c) $\overline{AB}$ denotes a $?$ , and
(d) $AB$ denotes the $\boxed{?}$ of $\overline{AB}$ or (equivalently) the $\boxed{?}$ from $A$ to $B$ .
Question 21 As a set of points, an angle is the ? of two ? with a common ?, which is called the ? of the angle.
Question 22 When two lines intersect so that all four angles are congruent, the angles are said to be ? and the lines are said to be ?.
Question 23 A ? measures 180°. (Hint: Answer with two words.)
A : ( ) P : (

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#### Vocabulary and Notation

**Question 24** Two angles whose measures sum to 180° are said to be ?.

**Question 25** Two angles whose measures sum to  $90^{\circ}$  are said to be  $\boxed{?}$ .

# Triangle Area

 $Short\text{-}answer\ measuring\ problems.$ 

**Problem 26** Geogebra link: https://tube.geogebra.org/m/mjscvuw3 Measure the area of the triangle above in three ways.

- (a) When AB is the base, the height is  $\boxed{?}$ , so the area is  $\boxed{?}$ .
- (b) When BC is the base, the height is  $\boxed{?}$ , so the area is  $\boxed{?}$ .
- (c) When CA is the base, the height is  $\boxed{?}$ , so the area is  $\boxed{?}$ .

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# Measuring by Sight

Short-answer measuring problems.

#### Instructions

Adjust the figures to fit the given conditions within **eyeball accuracy**. Enter the requested measurements.

**Problem 27** Geogebra link: https://tube.geogebra.org/m/gjf28er6 In figure above, when point C is adjusted so that  $\overline{BC}$  is perpendicular to  $\overline{AC}$ , AC = ?.

**Problem 28** Geogebra link: https://tube.geogebra.org/m/a888zyw2 In  $\triangle ABC$  above, the height to base  $\overline{AC}$  is  $\boxed{?}$ .

**Problem 29** Geogebra link: https://tube.geogebra.org/m/kta9hbuf In  $\triangle ABC$  above, the height to base  $\overline{AC}$  is ?.

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