# Analysis of TCP Westwood+ in high speed networks

E. Altman<sup>†</sup>, C. Barakat<sup>†</sup>, S. Mascolo°, N. Möller\*, J.Sun<sup>‡</sup>

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† INRIA, Sophia Antipolis, France
• Politenico di Bari, Bari, Italy
* KTH, Stockholm, Sweden
‡ M.I.T, Boston, Usa
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#### Outline

- TCP Westwood.
- Stochastic model.
- Stability conditions.
- Explicit throughput expression.
- Numerical results.

#### TCP Westwood+

- Proposed improvement of TCP's window control.
- Absense of losses: Standard additive increase,  $\beta$ .
- At loss event: New window size based estimated bandwidth.
- State variables: Window W, bandwidth estimate B.
- Parameter: Filter coefficient  $\alpha = 0.9$ .

#### Link model

- High speed link.
- Random i.i.d. delays, e.g., due to local retransmissions.
- Poisson loss process, independent of delay process.
- Loss indicator:  $Z_n = 1$  if loss occurs during roundtrip n.

#### Stochastic matrices

$$\begin{pmatrix}
X_{n+1} \\
B_{n+1}
\end{pmatrix} = A_n \begin{pmatrix}
X_n \\
B_n
\end{pmatrix} + C_n \quad A_n = \begin{pmatrix}
\overline{Z}_n & Z_n \\
\overline{\alpha} \overline{Z}_n \frac{\mathsf{RTT}_{\min}}{RTT_n} & \alpha \overline{Z}_n + Z_n
\end{pmatrix}$$

$$X_n = W_n / \mathsf{RTT}_{\min} \quad C_n = \begin{pmatrix}
\frac{\beta \overline{Z}_n}{\mathsf{RTT}_{\min}} \\
0
\end{pmatrix}$$

Main object of study:  $E[A_n]$ 



### Explicit throughput computation

Constants p and q computed from the delay and loss processes.

$$E[A_n] = \begin{pmatrix} \overline{p} & p \\ \overline{\alpha}qRTT_{\min} & \alpha + \overline{\alpha}p \end{pmatrix} \qquad E[C_n] = \begin{pmatrix} \frac{\beta p}{RTT_{\min}} \\ 0 \end{pmatrix}$$

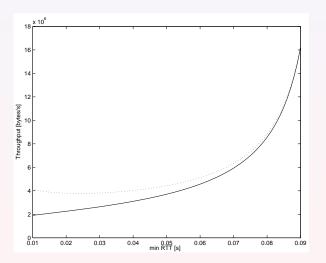
**Theorem:** Finite throughput iff  $\alpha < 1$  and  $E[RTT_n] > RTT_{min}$ .

Throughput = 
$$(1,0)(I - E[A_0])^{-1}E[C_0]\frac{RTT_{min}}{E[RTT_0]}$$

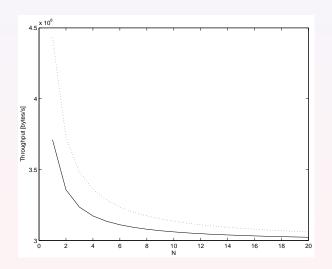
Does not depend on  $\alpha$ .



## Influence of RTT<sub>min</sub>



#### Influence of RTT variance



#### Conclusions

- Stochastic i.i.d. and Poisson losses ⇒ finite stationary throughput with TCP Westwood+.
- Stationary throughput is independent of the  $\alpha$  filter parameter.