

# Adaptive Multi-View Path Tracing

Basile Fraboni, Jean-Claude Iehl, Vincent Nivoliers, Guillaume Bouchard

LIRIS  
INSA de Lyon  
Université Claude Bernard Lyon 1  
Mercenaries Engineering

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## Path tracing

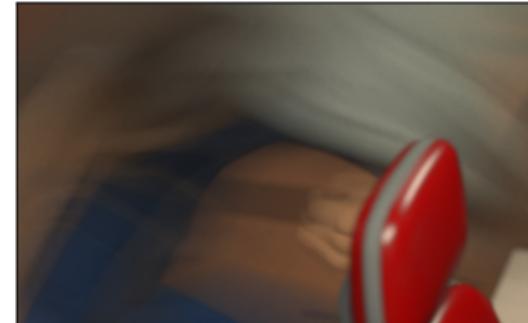
- Heavy computations to render noise-free images
  - Even more computations to remove flickering in sequences



1 minute

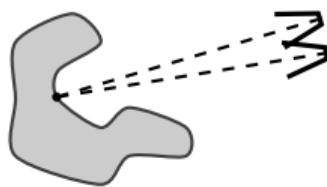


2 hours

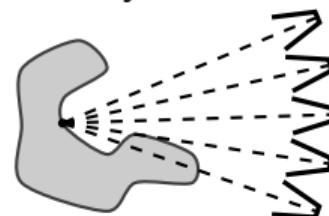


## Multi-view rendering

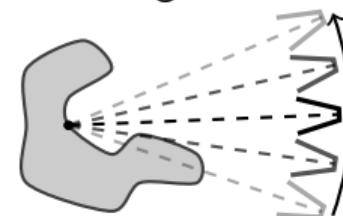
## Close viewpoints



## Many cameras



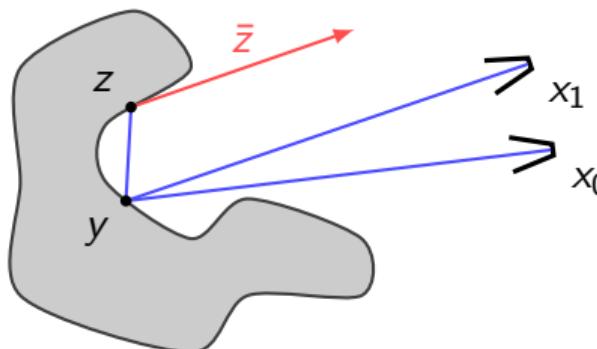
## Moving camera



- Heavy computations despite high similarity of nearby frames
  - Redundant light paths may be reused

# Approach

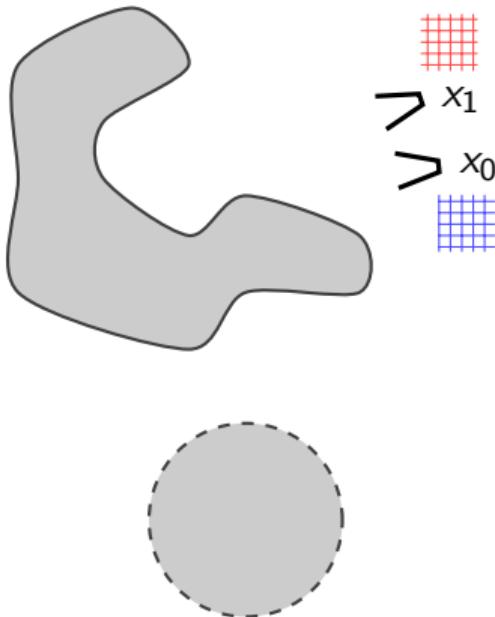
Observation can be decoupled from light transport



- At fixed time  $t$
- For any visible point  $y$  (non truly specular)
- Common suffix paths  $\bar{z}$  exist

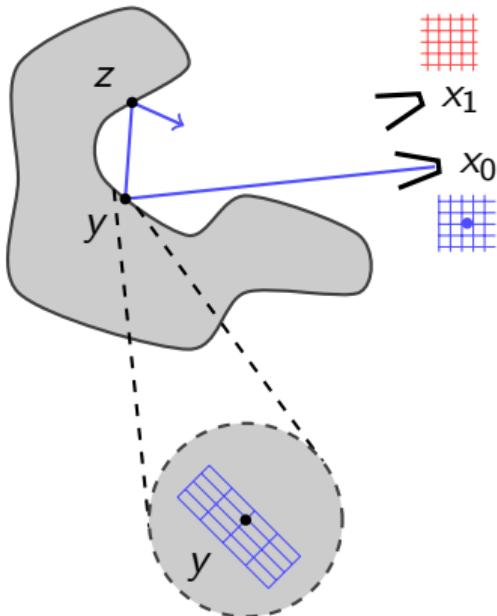
How to sample  $y$  ? How to sample  $z$  ? How to weight contributions ?

## Multiple view path reuse



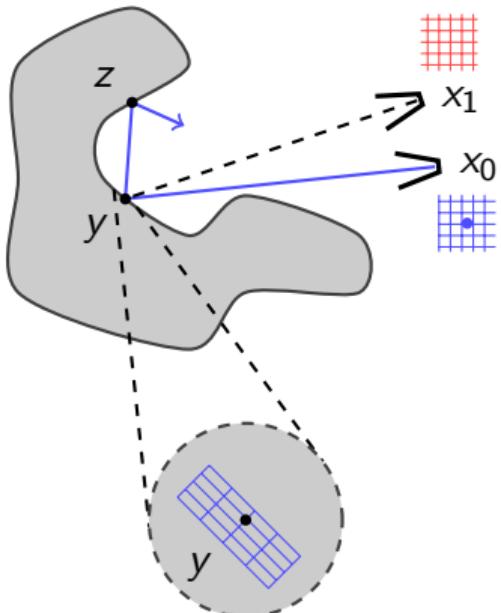
- Havran et al, 2003, Feliu et al. 2006, Henrich et al. 2011
  - reuse paths to increase the number of contributions
  - do not consider the change in density in MIS weights
  - may add variance to the result with glossy materials
- Lethinen et al. 2013
  - use path transformations
  - account for the change in density

## Multiple view path reuse



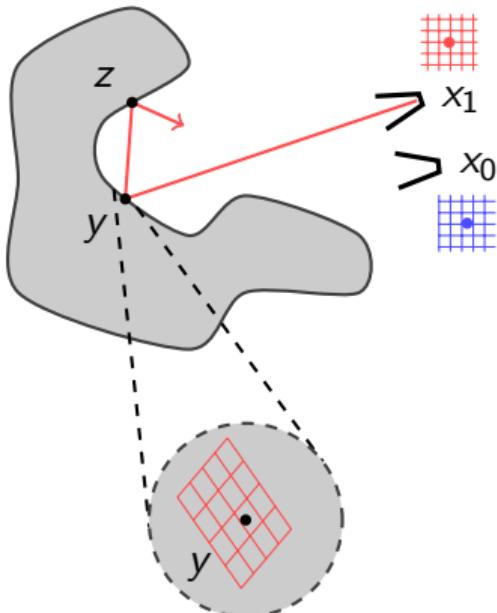
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## Multiple view path reuse



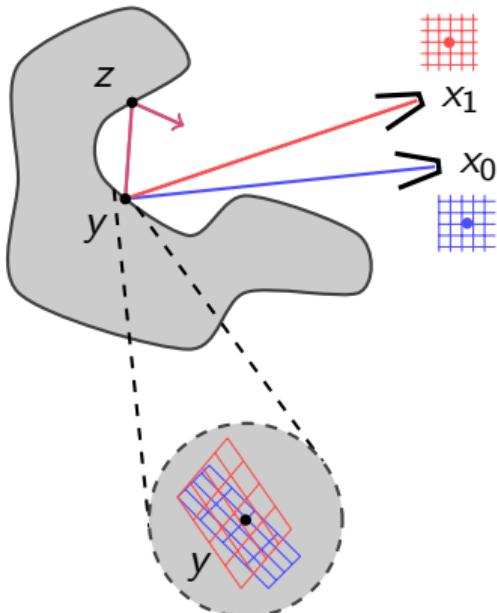
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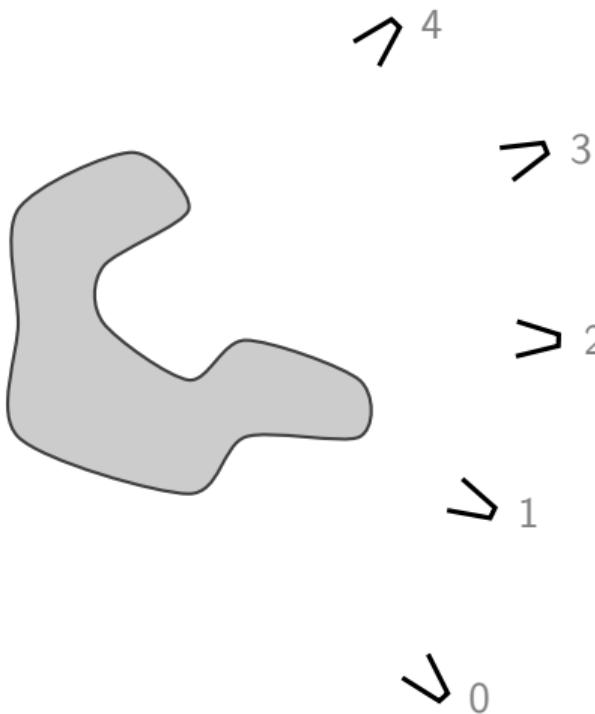
## Multiple view path reuse



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## Contribution

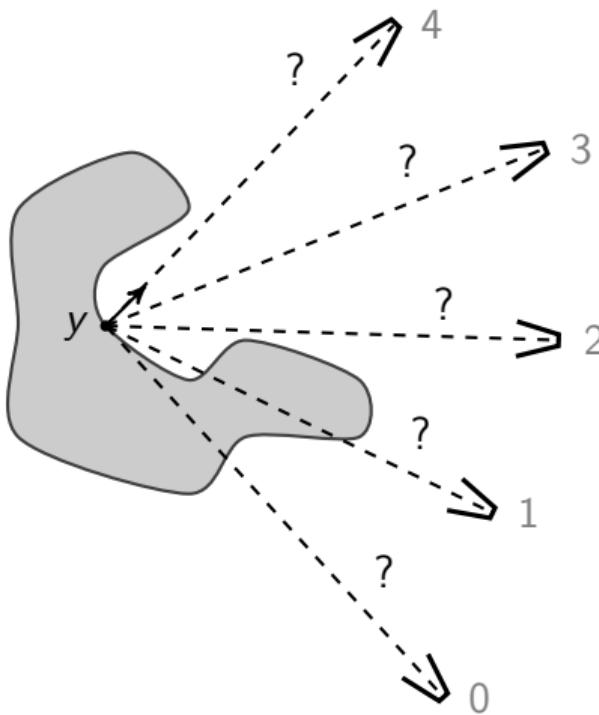
## Overview



## Progressive path construction

1. Hit point sampling
  2. Camera selection
  3. Suffix path sampling

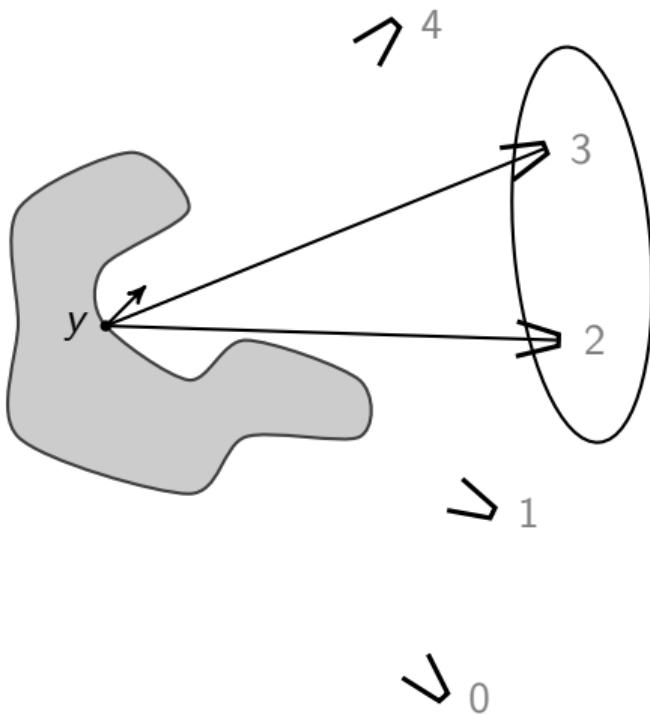
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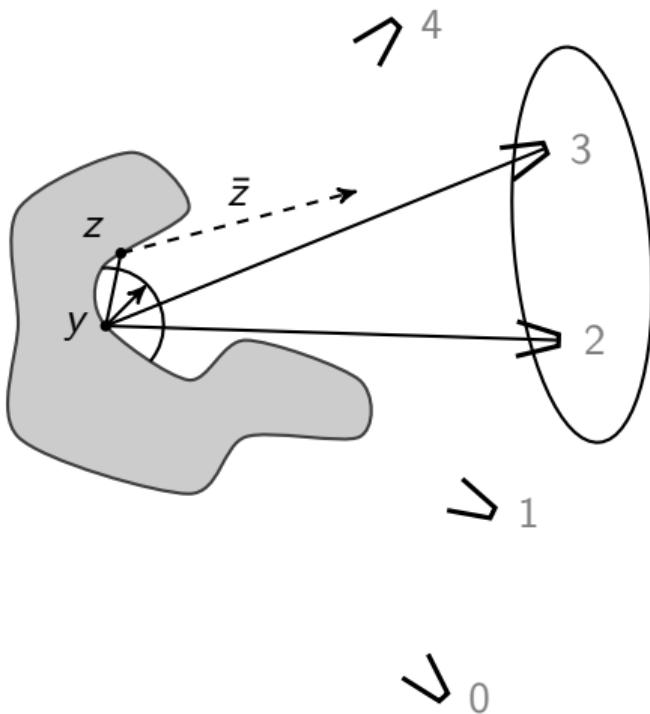
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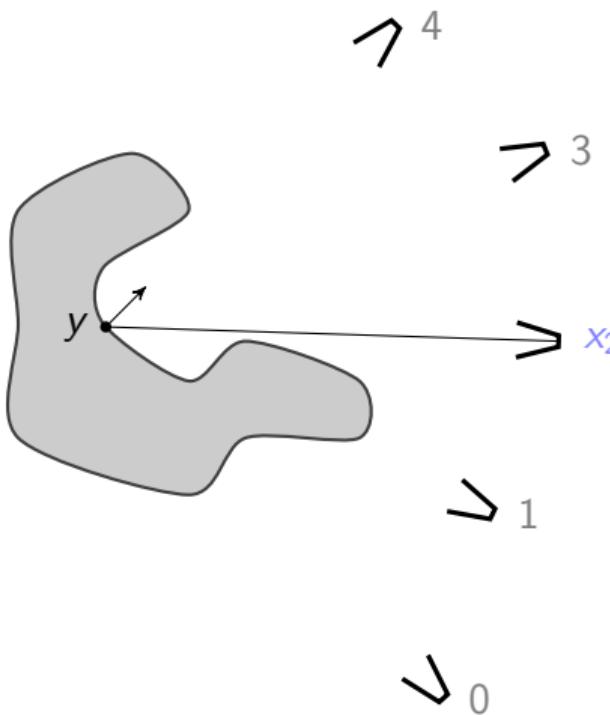
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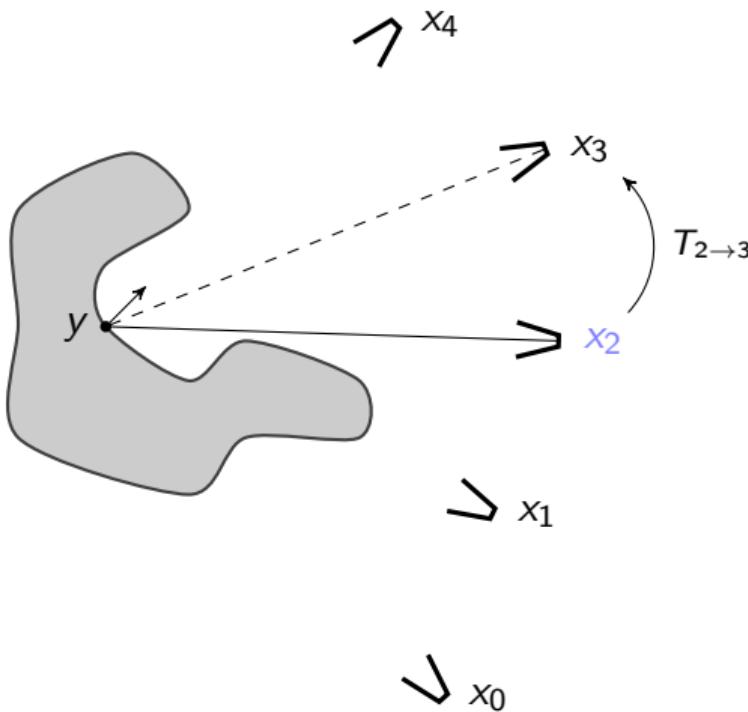
## Camera sampling



Given a camera and a pixel :

- sample a time  $t$  in the shutter interval
- sample a point in the pixel
- sample a point on the lens ( $x_2$ )
- cast a ray and find a hit point  $y$

## Prefix transformation

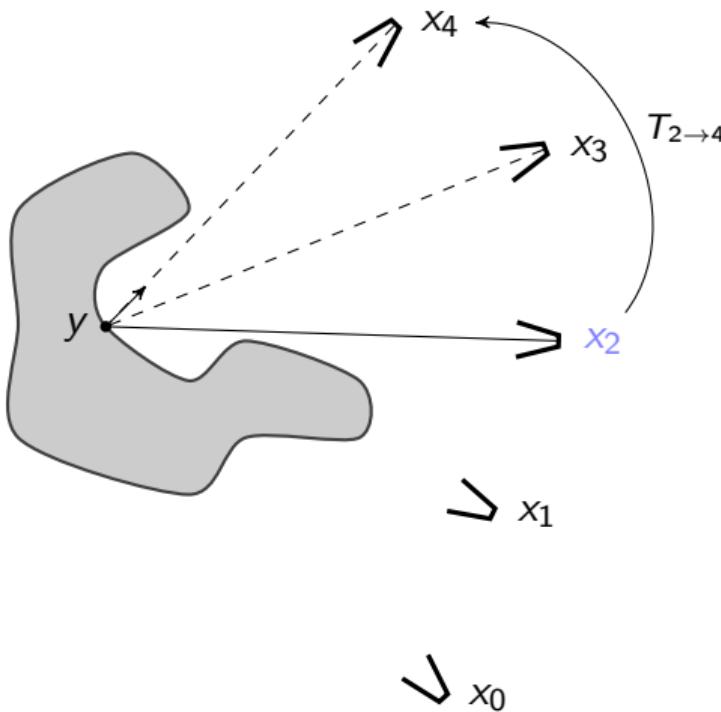


Shift the initial lens position onto other cameras:

$$T_{\ell \rightarrow k}(\{x_\ell, y\}) = \{x_k, y\} \quad x_k = \frac{r_k}{r_\ell} x_\ell$$

$r_k$  and  $r_\ell$  are the respective lens radii.

## Prefix transformation

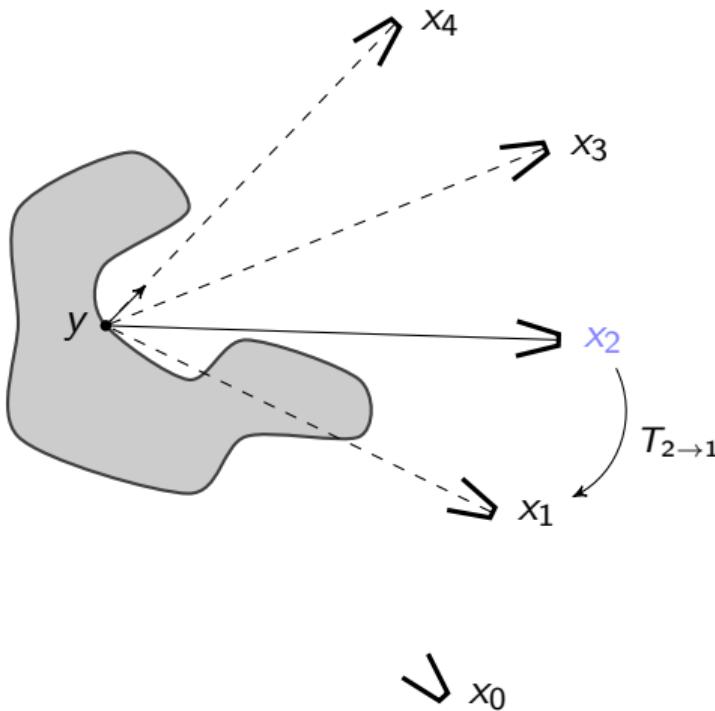


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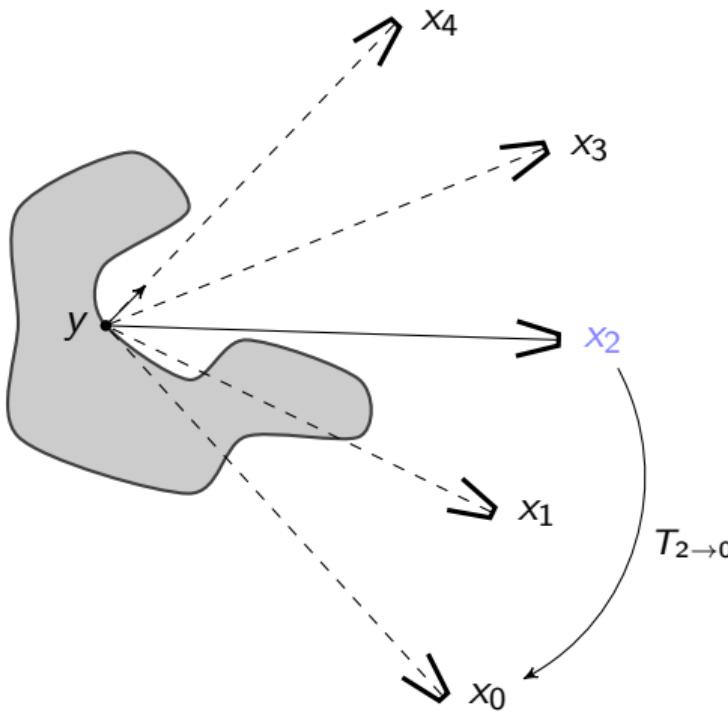


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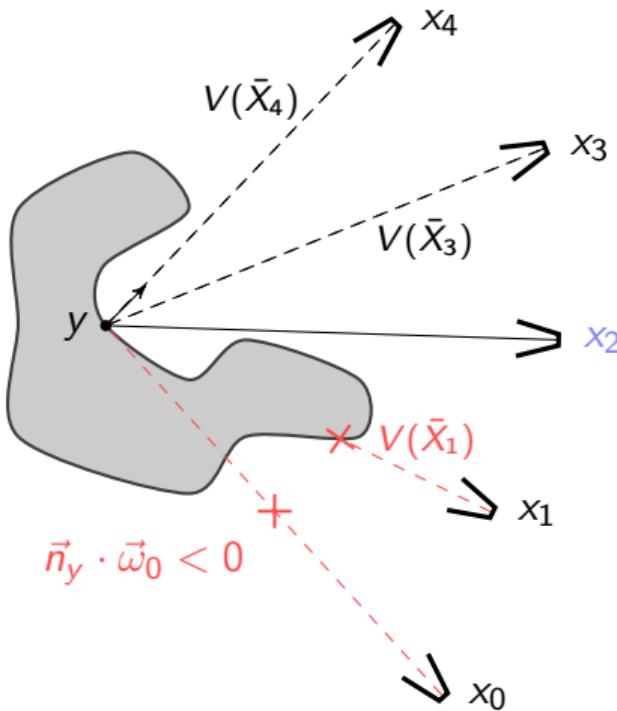


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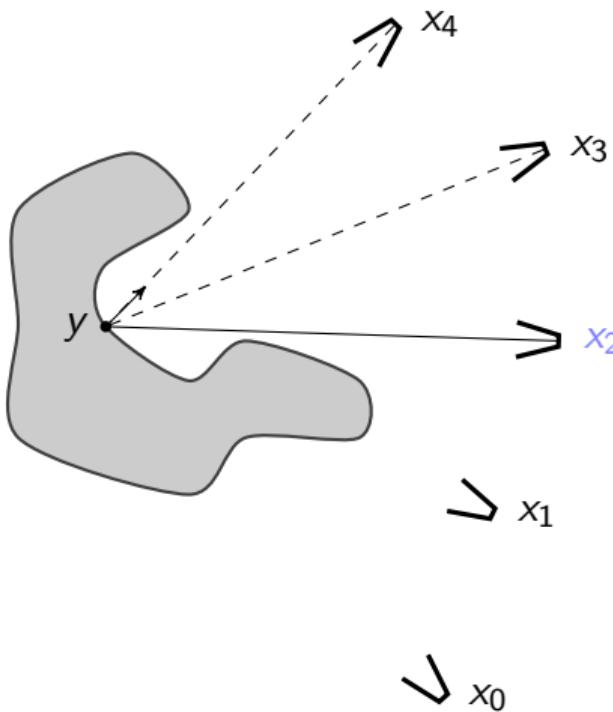
## Check prefix validity



- Check shutter interval
  - Check camera orientation
  - Check image projection of y
  - Check visibility

# Camera selection

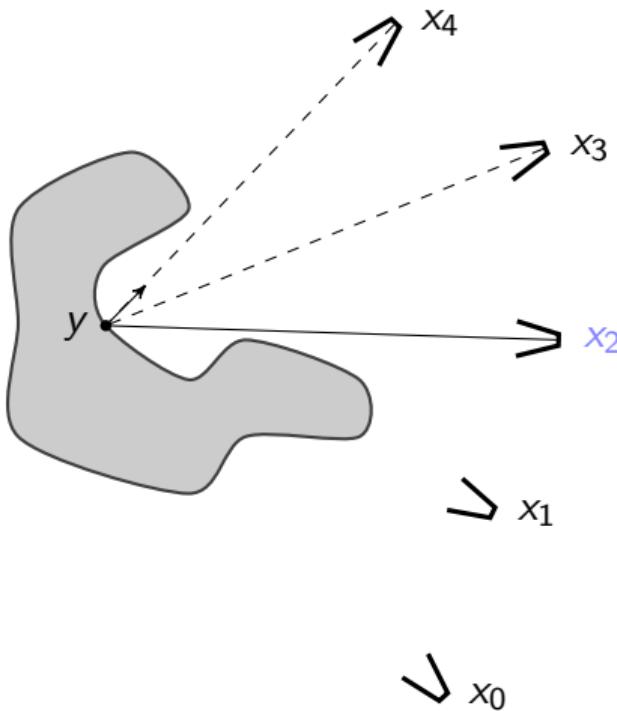
## Prefix probability density



$$p_{\ell \rightarrow k}(\{x_\ell, y\}) = \frac{p_\ell(\{x_\ell, y\}) |T'_{\ell \rightarrow k}|}{K_{\ell \rightarrow k}}$$

- Initial prefix pdf
- Jacobian of the transformation
- Normalization term

## Multiple importance sampling

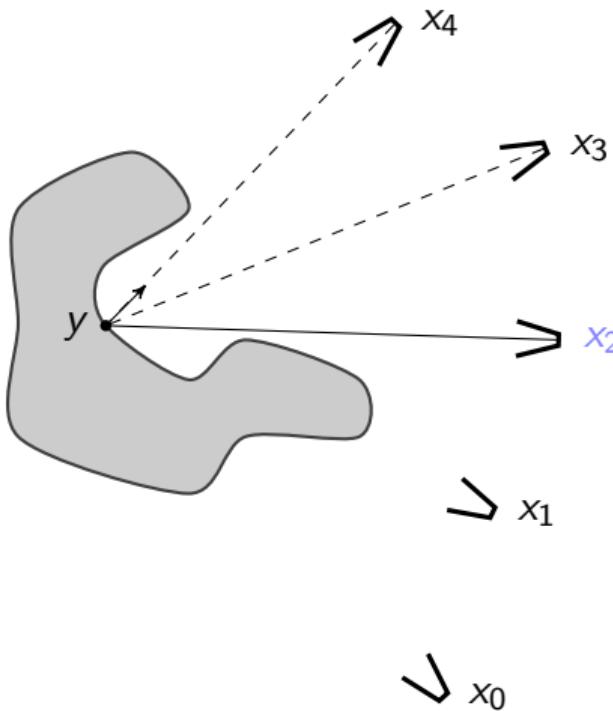


Several available strategies to sample  $y \rightarrow$  MIS

$$w_{\ell \rightarrow k}(\{x_\ell, y\}) = \frac{p_\ell(\{x_\ell, y\}) |T'_{\ell \rightarrow k}| K_{\ell \rightarrow k}^{-1}}{\sum_j p_j(\{x_j, y\}) |T'_{j \rightarrow k}| K_{j \rightarrow k}^{-1}}$$

- Normalization terms are costly to evaluate (integration)
- Suppose terms  $K$  constant to cancel them out

## Multiple importance sampling

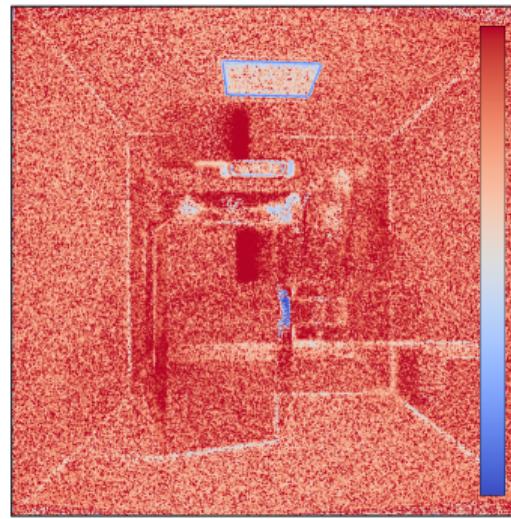
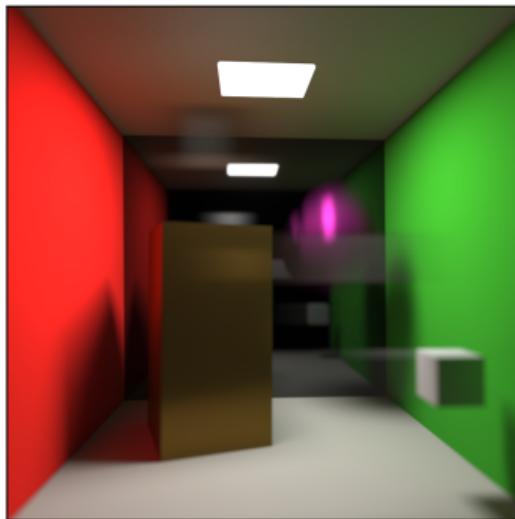


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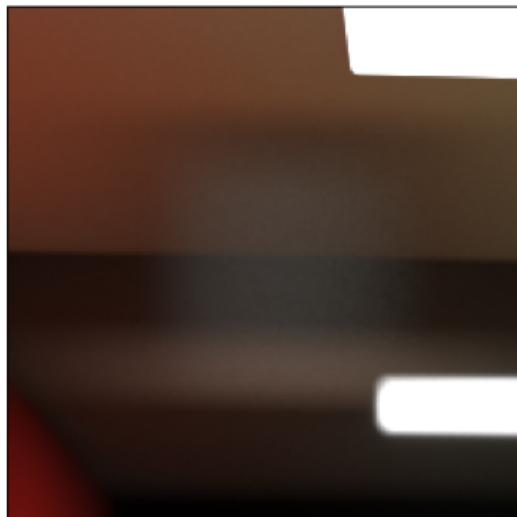
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## Variations of the normalization terms

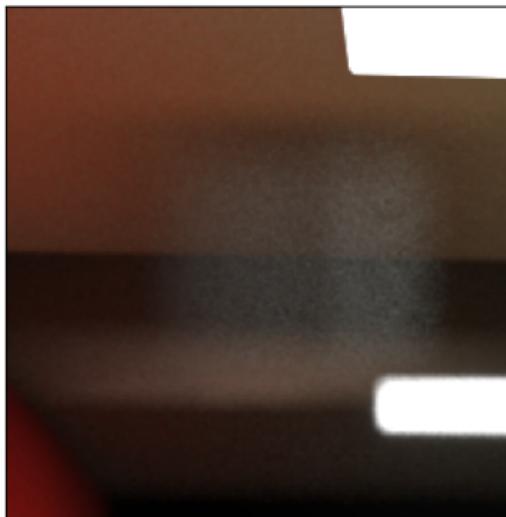


relative standard deviation

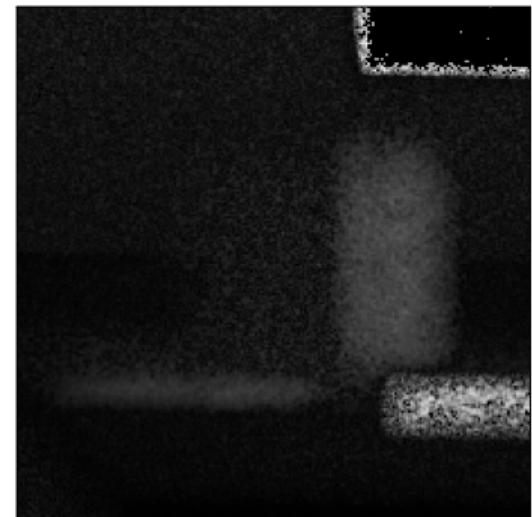
## Variations of the normalization terms



reference

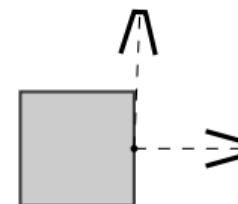
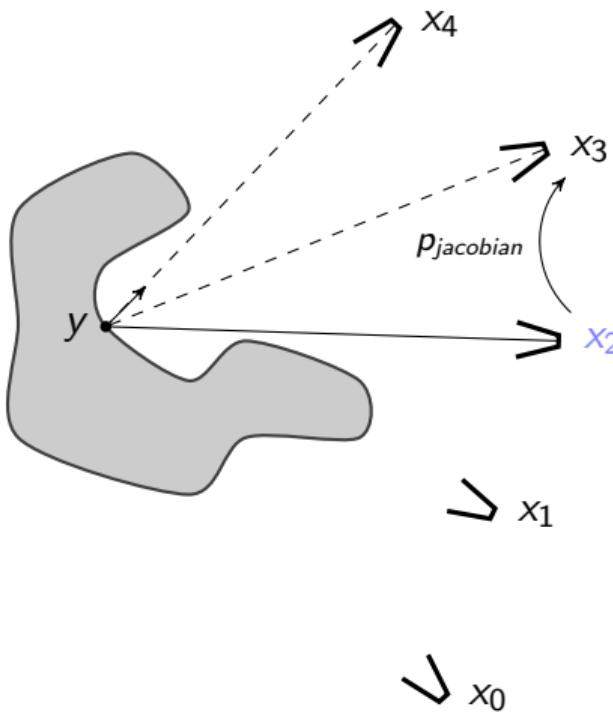


biased result



difference

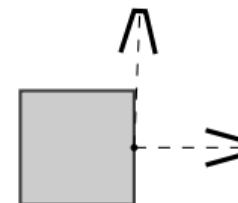
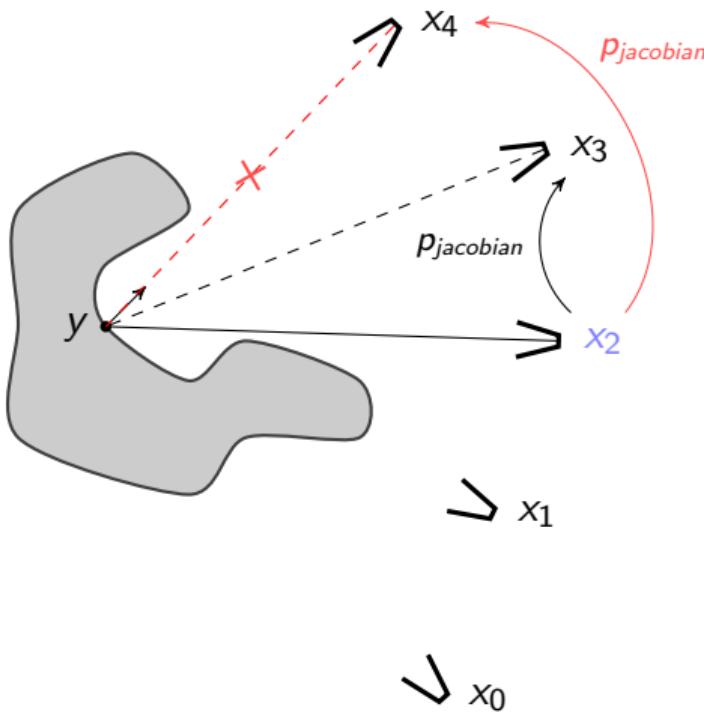
## Similarity selection: Jacobian



- Limiting the variations of the Jacobian
- Using a selection probability

$$p_{jacobian} = \begin{cases} \left| T'_{\ell \rightarrow k} \right|^{-1} & \text{if } \left| T'_{\ell \rightarrow k} \right| > 1 \\ & \text{otherwise} \end{cases}$$

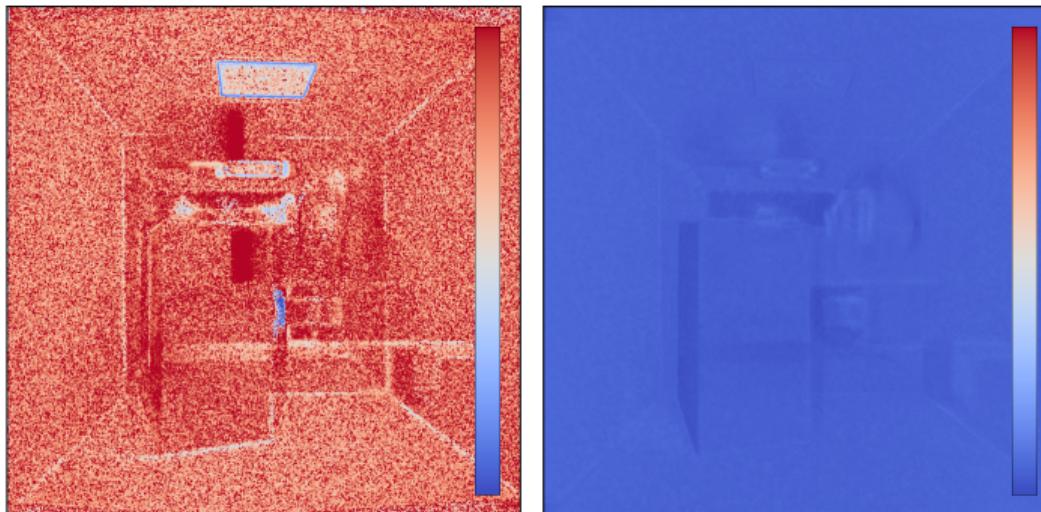
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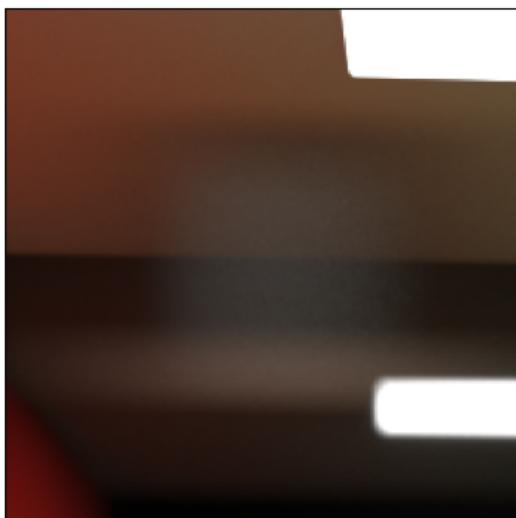
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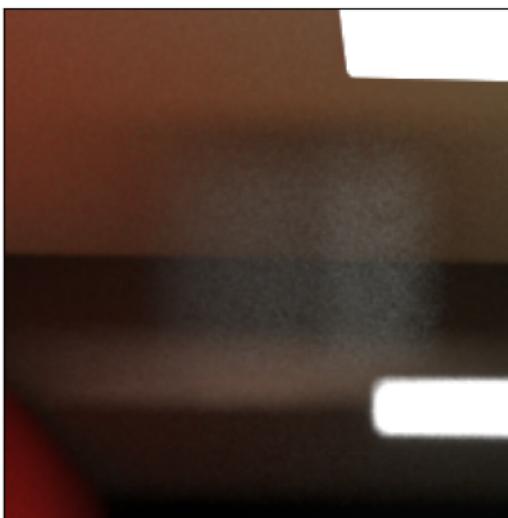
w/o selection

w/ selection

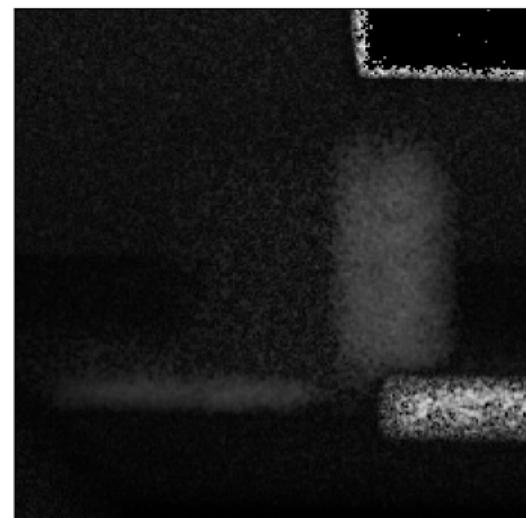
## Similarity selection: Jacobian



reference

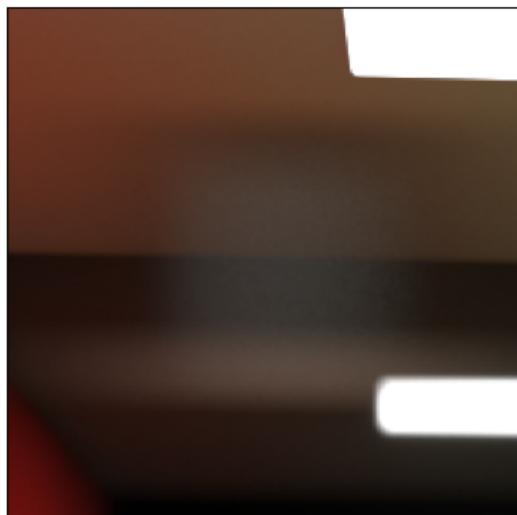


w/o selection

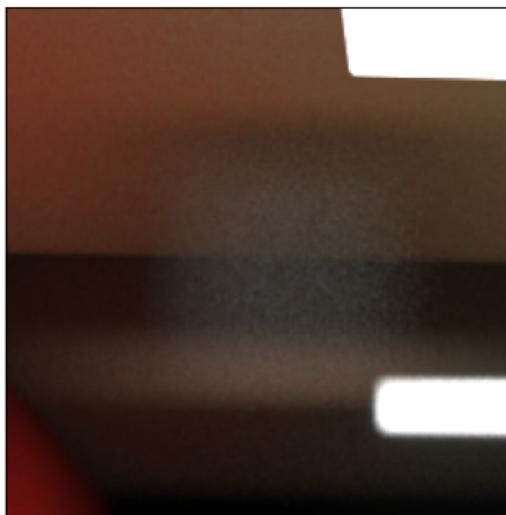


difference

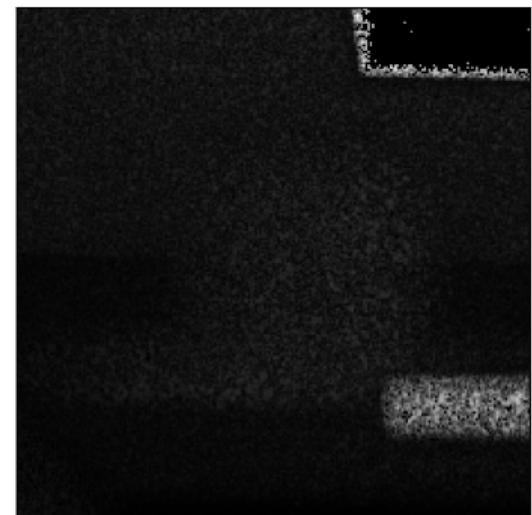
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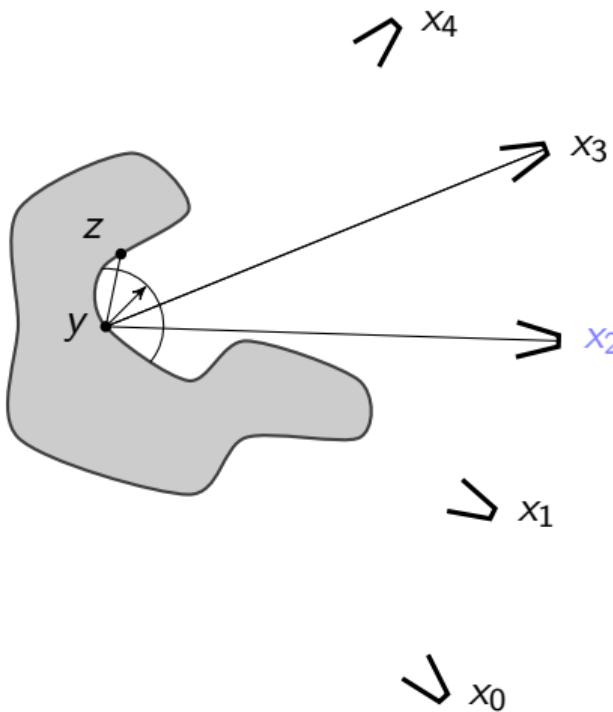
w/ selection



difference

# Suffix path sampling

## Sampling second hit point

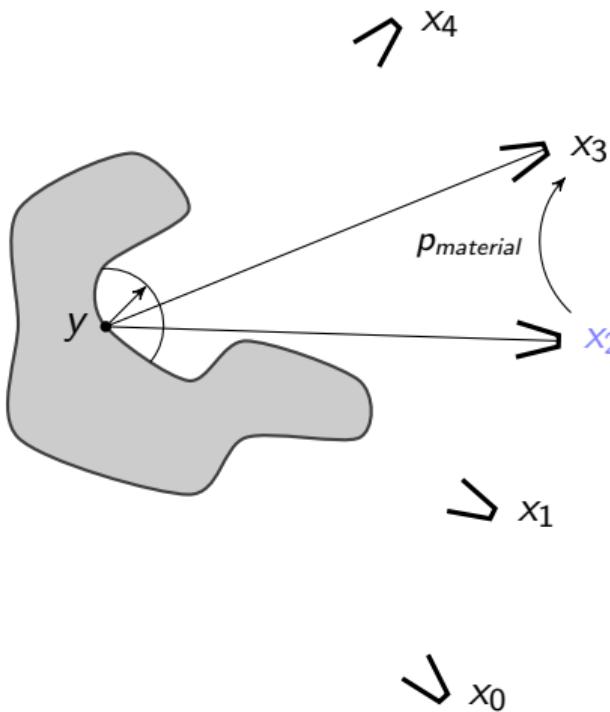


- Each camera has an associated importance function to sample  $z$
- We build a mixture importance function

Problem:

- Poor importance sampling may increase variance
- The observers must have similar importance

## Similarity selection: Material

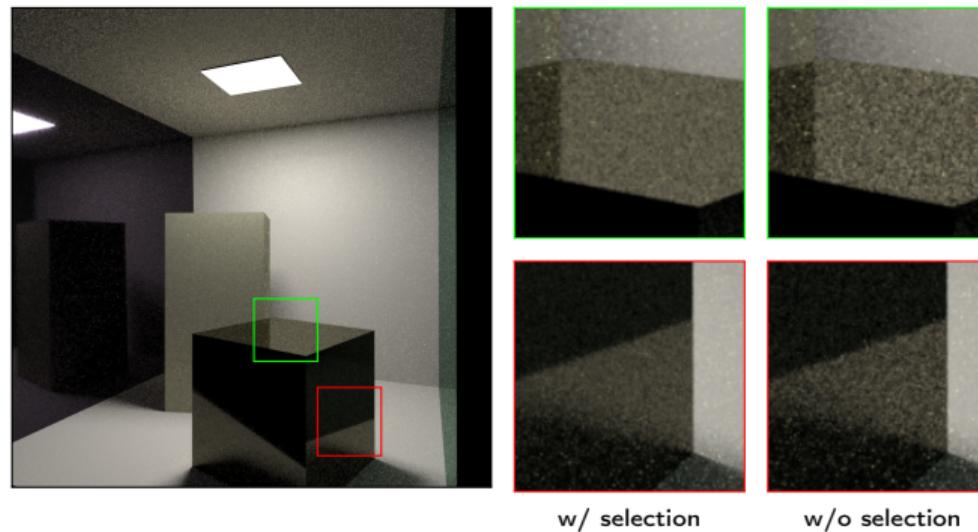


- Limiting poor importance sampling of the brdf
- Using a second selection probability

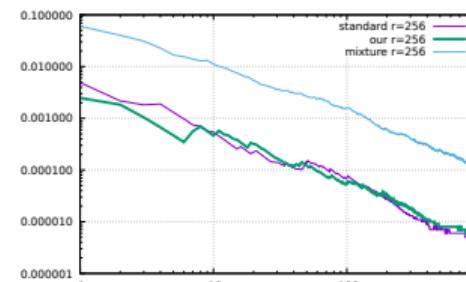
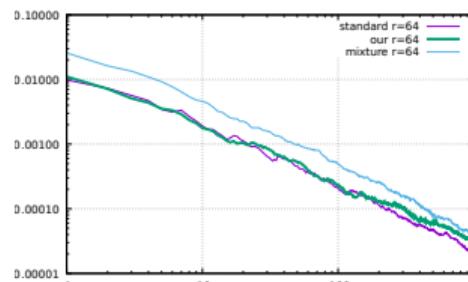
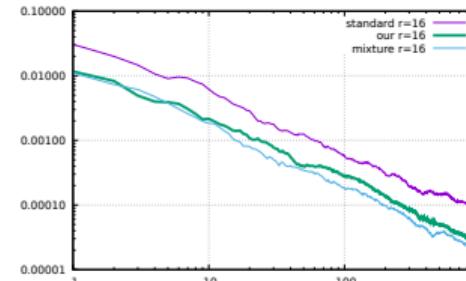
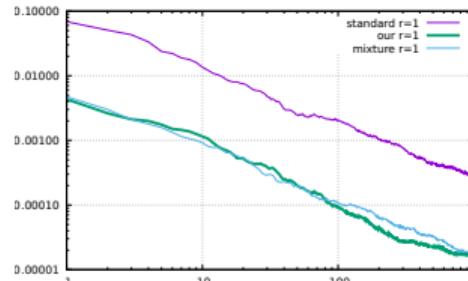
$$p_{\text{material}} = \left(1 - \tilde{\delta}(\rho_\ell, \rho_k)\right)^{\frac{1}{\alpha}}$$

- $\tilde{\delta}$  is the total variation distance
- $\alpha$  is the roughness of the material
- $\rho_i$  is the distribution associated with camera  $i$

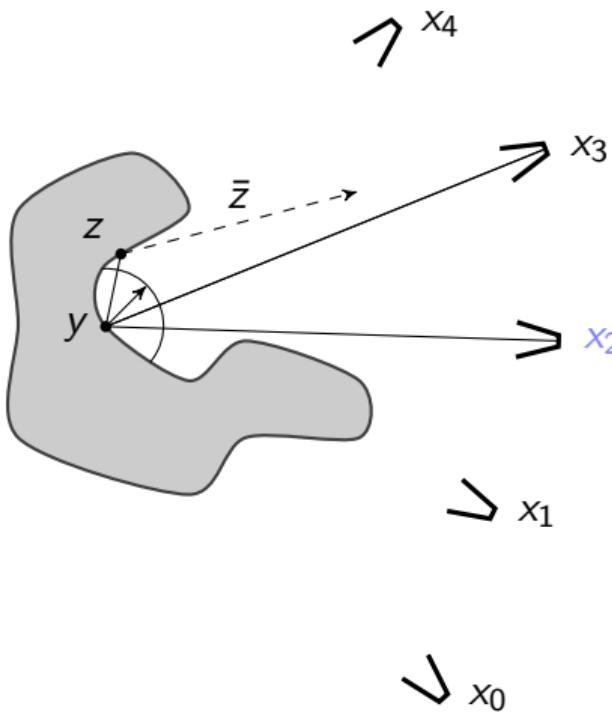
## Similarity selection: Material



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## Suffix path sampling



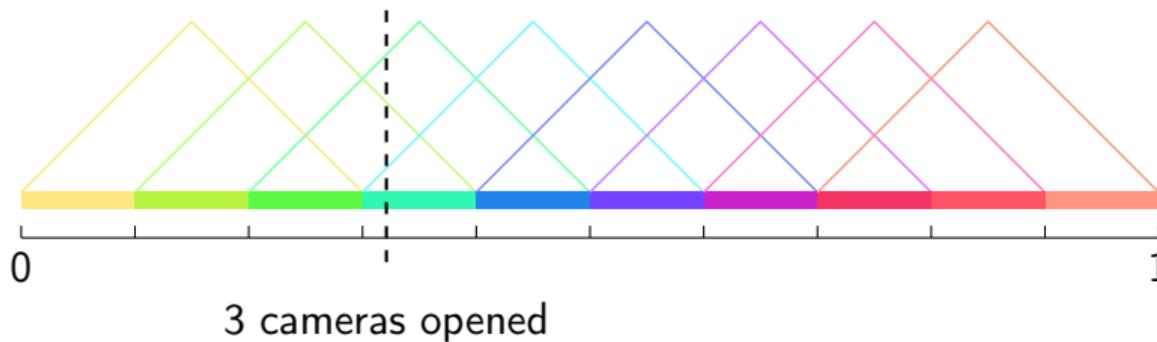
- continue path using regular path tracing
- weight contributions with MIS

$$w_{\ell \rightarrow k}(\bar{X}_\ell) = \frac{n_\ell p_{\ell \rightarrow k}(\bar{X}_\ell) p_{\text{jacobian}} p_{\text{material}}}{\sum_j n_j p_{j \rightarrow k}(\bar{X}_j) p_{\text{jacobian}} p_{\text{material}}}$$

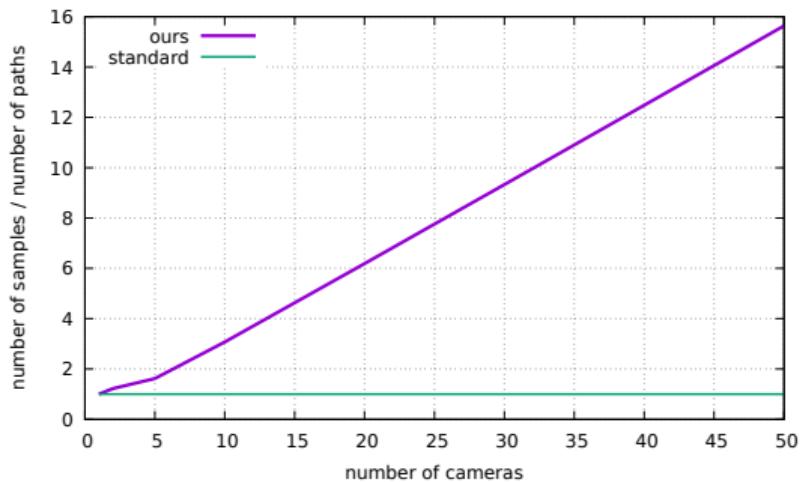
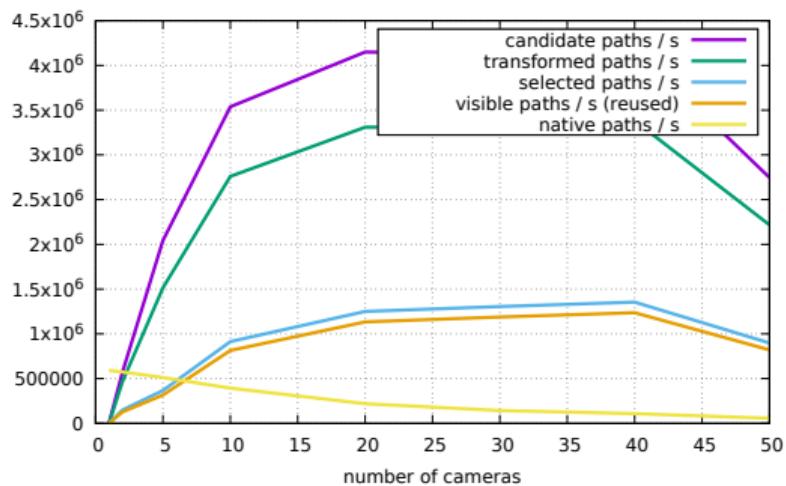
- $n$  is the number of samples generated in the pixel
- may vary when adaptive sampling is used

## Results

- Animations are computed with the same time budget
- Cameras with overlapping exposure intervals



# Performance



## Conclusion

## Contributions

- reuse aware path construction
  - observer selection strategies
    - jacobian similarity
    - material similarity
  - adaptive sampling support

Perspectives

- extend the method to depth of field (in progress)
  - formal study of brdf similarity
  - unify path reuse techniques (Bekaert et al. 2002)

# Questions



path tracing



ours - equal time

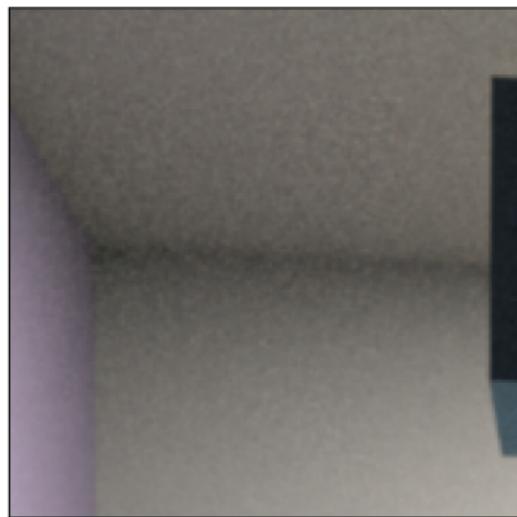
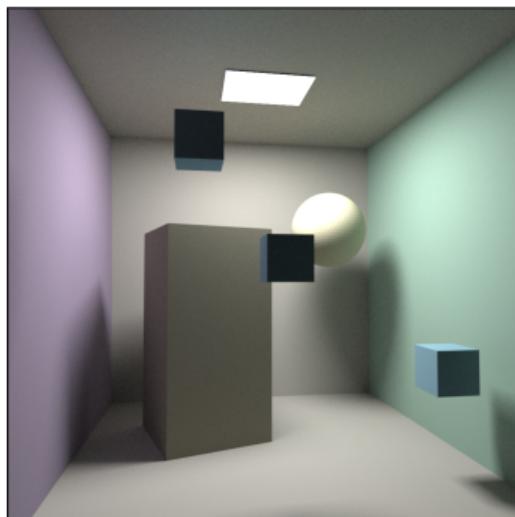
Acknowledgements:

Yasutoshi Mori for the Mori Knob model

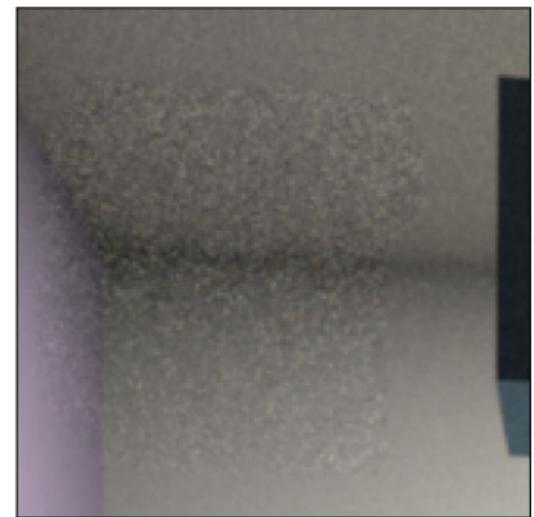
Blender Institute for making freely available assets from the open movie Agent 327

## Adaptive

- Selective reuse + occlusions → inhomogeneous sample distribution

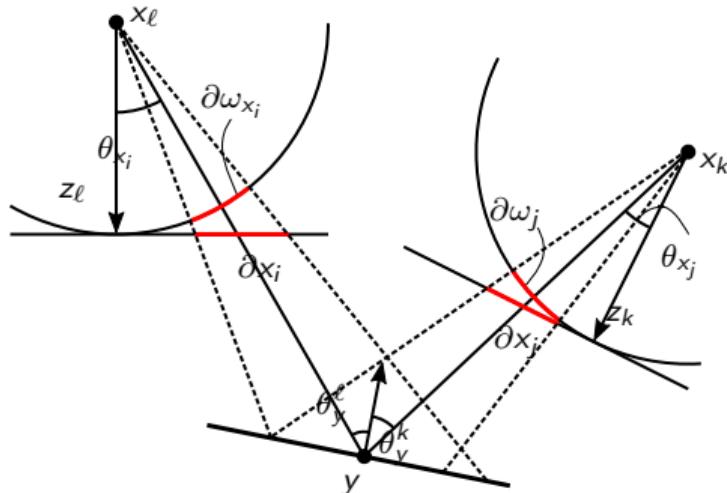


w/ adaptive



w/o adaptive

# Jacobian



$$|T'_{\ell \rightarrow k}| = \frac{r_\ell^2}{r_k^2} \frac{\cos \theta_y^k}{\|y - x_k\|^2} \frac{d_k^2}{\cos^3 \theta_{x_i}} \frac{\|y - x_\ell\|^2}{\cos \theta_y^\ell} \frac{\cos^3 \theta_{x_j}}{d_\ell^2}$$