CSC6013 - Worksheet for Week 6

Russian Peasants Multiplication

- 1. Trace the Russian Peasants Multiplication algorithm for the following products. Show each recursive call and the final result, as shown in the live session (table).
 - a. 64 * 13
 - b. 60 * 13
 - c. 59 * 13

Problem A - 64 * 13

n	m	Steps
64	13	64 is even
32	26	32 is even
16	52	16 is even
8	104	8 is even
4	208	4 is even
2	416	2 is even
1	832	832

Problem B - 60 * 13

n	m	Steps
60	13	60 is even
30	26	30 is even
15	52	15 is odd (+52)
7	104	7 is odd (+104)
3	208	3 is odd (+208)
1	416	416+52+104+208 = 780

Problem c - 59 * 13

n	m	Steps
59	13	59 is odd (+13)
29	26	29 is odd (+26)
14	52	14 is even
7	104	7 is odd (+104)
3	208	3 is odd (+208)
1	416	416+13+26+104+208 = 767

Lomuto partition

- 2. Trace the Lomuto partition with the array:
 - a. A = [100, 33, 22, 213, 65, 29, 153, 199, 47, 181, 85] Using A[10] = 85 as pivot the final array will be:
 - A = [33, 22, 65, 29, 47, 85, 153, 199, 100, 181, 213]

In your trace, write down to each change in either i or j, stating: the values of i and j, swaps made, and elements divided into lesser than the pivot, greater than the pivot, and yet to compare.

```
Step 1
i = 0, j = 0
Pivot at index 10: 85
Elements lesser than pivot: []
Elements greater than pivot: []
Elements still to be sorted: [100, 33, 22, 213, 65, 29, 153, 199, 47, 3
Step 2:
i = 0, j = 0 -> i = 0, j = 1
A[j]: 100 > Pivot: 85, no swap made | Total swaps = 0
Elements lesser than pivot: []
Elements greater than pivot: [100]
Elements still to be sorted: [33, 22, 213, 65, 29, 153, 199, 47, 181]
Step 3:
i = 0, j = 1 \rightarrow i = 1, j = 2
A[j]: 33 \le Pivot: 85, swap A[i]: 100 with A[j]: 33 \mid Total swaps = 1
Elements lesser than pivot: [33]
Elements greater than pivot: [100]
Elements still to be sorted: [22, 213, 65, 29, 153, 199, 47, 181]
Step 4:
i = 1, j = 2 \rightarrow i = 2, j = 3
A[j]: 22 \le Pivot: 85, swap A[i]: 100 with A[j]: 22 \mid Total swaps = 2
Elements lesser than pivot: [33, 22]
Elements greater than pivot: [100]
Elements still to be sorted: [213, 65, 29, 153, 199, 47, 181]
Step 5:
i = 2, j = 3 -> i = 2, j = 4
A[j]: 213 > Pivot: 85, no swap made | Total swaps = 2
Elements lesser than pivot: [33, 22]
Elements greater than pivot: [100, 213]
Elements still to be sorted: [65, 29, 153, 199, 47, 181]
Step 6:
i = 2, j = 4 -> i = 3, j = 5
A[j]: 65 \le Pivot: 85, swap A[i]: 100 with A[j]: 65 \mid Total swaps = 3
Elements lesser than pivot: [33, 22, 65]
Elements greater than pivot: [213, 100]
Elements still to be sorted: [29, 153, 199, 47, 181]
Step 7:
i = 3, j = 5 -> i = 4, j = 6
A[j]: 29 \le Pivot: 85, swap A[i]: 213 with A[j]: 29 \mid Total swaps = 4
Elements lesser than pivot: [33, 22, 65, 29]
Elements greater than pivot: [100, 213]
Elements still to be sorted: [153, 199, 47, 181]
Step 8:
i = 4, j = 6 -> i = 4, j = 7
A[j]: 153 > Pivot: 85, no swap made | Total swaps = 4
Elements lesser than pivot: [33, 22, 65, 29]
Elements greater than pivot: [100, 213, 153]
Elements still to be sorted: [199, 47, 181]
```

```
Step 9:
i = 4, j = 7 -> i = 4, j = 8
A[j]: 199 > Pivot: 85, no swap made | Total swaps = 4
Elements lesser than pivot: [33, 22, 65, 29]
Elements greater than pivot: [100, 213, 153, 199]
Elements still to be sorted: [47, 181]
Step 10:
i = 4, j = 8 \rightarrow i = 5, j = 9
A[j]: 47 \le Pivot: 85, swap A[i]: 100 with A[j]: 47 \mid Total swaps = 5
Elements lesser than pivot: [33, 22, 65, 29, 47]
Elements greater than pivot: [213, 153, 199, 100]
Elements still to be sorted: [181]
Step 11:
i = 5, j = 9 \rightarrow i = 5, j = 10
A[j]: 181 > Pivot: 85, no swap made | Total swaps = 5
Elements lesser than pivot: [33, 22, 65, 29, 47]
Elements greater than pivot: [213, 153, 199, 100, 181]
Elements still to be sorted: []
Step 12:
Swap A[i]: 213 with Pivot: 85
Elements lesser than pivot: [33, 22, 65, 29, 47]
Elements greater than pivot: [85, 153, 199, 100, 181]
Pivot: 85 at index 5
Final Array: Lomuto with pivot at index 5: 85
[33, 22, 65, 29, 47, 85, 153, 199, 100, 181, 85]
```