

# SST–VAM Translation

*Omar Iskandarani\**

August 27, 2025

## Abstract

This note provides a rigorous nomenclature concordance between the legacy VAM presentation and the Swirl–String Theory (SST) house style. It establishes a one-to-one mapping of symbols and terminology while preserving the underlying kinematics, operators, and calibrated constants. In particular, it fixes the canonical SST equalities

$$\rho_E = \frac{1}{2} \rho_f \|\mathbf{v}_\odot\|^2, \quad \rho_m = \rho_E / c^2, \quad K = \frac{\rho_{\text{core}} r_c}{v_s}, \quad \rho_f = K \Omega,$$

and records that all published numerical values for  $v_s$ ,  $r_c$ ,  $\rho_{\text{core}}$ , the background density, and the sectoral force bounds carry over unchanged. The document includes compact translation tables (fields/kinematics/operators; densities/velocities/coarse-graining; global scales) and a minimal macro layer (`\rhoF`, `\rhoE`, `\rhoM`, `\rhoC`, `\vswirl`, `\vnorm`) to prevent notation drift in large projects. Legacy wording is restricted to historical citations; narrative prose adopts the neutral SST vocabulary (e.g., *foliation*, *swirl string*) without altering the mathematics. Compatibility is ensured both for standalone use (title page + metadata) and for modular inclusion (`\providecommand` guards and no additional package requirements). The result is a drop-in “translation guide” that guarantees dimensional consistency, unambiguous symbol usage, and reproducible cross-referencing across manuscripts that span the VAM→SST transition.

---

\* Independent Researcher, Groningen, The Netherlands

Email: [info@omariskandarani.com](mailto:info@omariskandarani.com)

ORCID: [0009-0006-1686-3961](https://orcid.org/0009-0006-1686-3961)

DOI: [10.5281/zenodo.xxxxxxx](https://doi.org/10.5281/zenodo.xxxxxxx)

License: CC-BY-NC 4.0 International

# 1 SST–VAM Translation and Constant Overlaps (Extended)

## Canonical equalities (SST form)

$$\begin{aligned}\rho_E &= \frac{1}{2} \rho_f \|\mathbf{v}_\odot\|^2, & \rho_m &= \rho_E / c^2, \\ K &= \frac{\rho_{\text{core}} r_c}{v_s}, & \rho_f &= K \Omega.\end{aligned}$$

## Dimensional check

$$\begin{aligned}[\rho_f] &= \text{kg m}^{-3} \\ [\|\mathbf{v}_\odot\|] &= \text{m s}^{-1} \\ [v_s] &= \text{m s}^{-1} \\ [\rho_E] &= \text{J m}^{-3} \\ [\rho_m] &= \text{kg m}^{-3} \\ [K] &= \text{kg m}^{-3} \text{ s}\end{aligned}$$

## Temporal Ontology in SST

We distinguish absolute parameter time  $\mathcal{N}$  (preferred foliation label), external observer time  $\tau$ , and internal clocks carried by swirl strings: a phase accumulator  $S(t)$  and a loop “proper time”  $T_s$ . These appear in the field equations and separate global synchronization from local rotational dynamics.

$\mathcal{N}$	Absolute time (foliation)	Global causal parameter
$v_0$	Now-point	Localized synchronization label
$\tau$	External/chronos time	Measured time of external observer
$S(t)$	Swirl clock	Internal phase memory along a string
$T_s$	String proper time	Loop-duration functional
$\mathbb{K}$	Kairos event	Topological/phase transition moment

## Fields, kinematics, operators (mapping)

VAM (legacy)	SST (house)	Meaning	Units	Overlap
“æther time”	absolute time parametrization	foliation time label	—	Yes
$T(x)$	$T(x)$	scalar clock field	—	Yes
$u_\mu$ (unit “æther” vector)	$u_\mu$ (unit time-like field)	$u_\mu = \partial_\mu T / \sqrt{-g^{\alpha\beta} \partial_\alpha T \partial_\beta T}$	—	Yes
“vortex line(s)”	swirl string(s)	object name only	—	Yes
$B_{\mu\nu}, H_{\mu\nu\rho}$	same	Kalb–Ramond 2-form; $H = \partial_{[\mu} B_{\nu\rho]}$	—	Yes
$W_\mu$	$W_\mu$	coarse-grained frame connection	—	Yes
$C(K), L(K), \mathcal{H}(K)$	same	crossing #, ropelength, hyperbolic proxy	—	Yes

## Densities, velocities, coarse–graining (mapping)

VAM (legacy)	SST (macro)	Meaning	Units	Overlap
$\rho_0, \rho_{\text{æ}}^{(\text{fluid})}, \rho_{\text{æ}}^{(\text{vacuum})}$	$\rho_f, \rho_f^{\text{bg}}$ or $\rho_f^{(0)}$	effective fluid density	$\text{kg m}^{-3}$	Yes
$\rho_{\text{æ}}^{(\text{core})}, \rho_{\text{æ}}^{(\text{mass})}$	$\rho_{\text{core}}$	core/material density	$\text{kg m}^{-3}$	Yes
$\rho_{\text{æ}}^{(\text{energy})}$	$\rho_E$ (or $\rho_{\text{core}} c^2$ )	energy density	$\text{J m}^{-3}$	Yes
$C_e$ (tangential)	$v_s$	characteristic swirl speed ( $= \ \mathbf{v}_\odot\ $ at $r = r_e$ )	$\text{m s}^{-1}$	Yes
$K = \frac{\rho^{(\text{mass})} r_c}{C_e}$	$K = \frac{\rho_{\text{core}} r_c}{v_s}$	coarse–graining coefficient	$\text{kg m}^{-3} \text{ s}$	Yes
$\Omega$	$\Omega$	leaf angular rate	$\text{s}^{-1}$	Yes

## Global scales and bounds

VAM (legacy)	SST (house)	Meaning	Units	Overlap
$F^{\max}_{\text{Coulomb}}$	$F^{\max}_{\text{EM}}$	Coulomb-sector bound	N	Yes
$F^{\max}_{\text{gr}}$ (Universal)	$F^{\max}_{\text{G}}$	gravitational/universal bound	N	Yes
$\Gamma$	$\Gamma$	loop circulation	$\text{m}^2 \text{s}^{-1}$	Yes
$\Omega_R, \Omega_c$	same	outer rigid vs. core spin	$\text{s}^{-1}$	Yes

## Numeric overlaps (published values)

Quantity	Symbol (SST)	Value	Units
Characteristic swirl speed	$v_s$	1,093,845.63	$\text{m s}^{-1}$
Core radius	$r_c$	$1.40897017 \times 10^{-15}$	m
Core density	$\rho_{\text{core}}$	$3.8934358266918687 \times 10^{18}$	$\text{kg m}^{-3}$
Background density	$\rho_f^{\text{bg}}$	$7.0 \times 10^{-7}$	$\text{kg m}^{-3}$
Max Coulomb force	$F^{\max}_{\text{EM}}$	29.053507	N
Max universal force	$F^{\max}_{\text{G}}$	$3.02563 \times 10^{43}$	N

## Macro glossary (house style)

Use the macros to avoid drift:

$\rho_f$  (effective density),  $\rho_E$  (energy density),  $\rho_m$  (mass-equivalent),  $\rho_{\text{core}}$  (core density),  $\mathbf{v}_\odot$  (swirl velocity)

## Prose guardrails (rebrand policy)

Use *foliation* and *swirl string(s)* in narrative text. Reserve legacy words (“æther”, “vortex”) strictly for quoting historical titles or citations. Retain *vorticity* as standard.

## Sentence rewrites (examples)

Legacy: “The æther sector fixes the vortex core density.”

SST: “The *foliation* sector fixes the *core density*  $\rho_{\text{core}}$  of the swirl string.”

Legacy: “Kelvin’s vortex theorem implies conserved  $R^2\omega$ .”

SST: “Kelvin’s *circulation* theorem implies  $\frac{D}{Dt}(R^2\omega) = 0$  under incompressible, inviscid, barotropic flow.”

## Scale-dependent Effective Densities in SST

**Effective densities (house style).**

$\rho_f \equiv$  effective fluid density,  $\rho_E \equiv \frac{1}{2} \rho_f \|\mathbf{v}_\odot\|^2$  (swirl energy density),  $\rho_m \equiv \rho_E / c^2$  (mass-equivalent density)

Background value:  $\rho_f^{\text{bg}} \approx 7.0 \times 10^{-7} \text{ kg m}^{-3}$ . Core (material) density:  $\rho_{\text{core}} \approx 3.8934358267 \times 10^{18} \text{ kg m}^{-3}$ . Hence core energy density

$$\rho_E^{\text{core}} = \rho_{\text{core}} c^2 \approx 3.499 \times 10^{35} \text{ J m}^{-3}.$$

**Radial profile (phenomenology).** It is convenient to model the near-core energy density with an exponential relaxation to the background:

$$\rho_E(r) = \rho_E^{\text{bg}} + (\rho_E^{\text{core}} - \rho_E^{\text{bg}}) e^{-r/r_*},$$

with a microscopic decay scale  $r_*$  (fit parameter). This empirical profile does not replace the exact tube energetics below.

**String energetics (Rankine core + irrotational envelope).** For a core of radius  $r_c$  and length  $\ell$  with solid-body rotation  $v_\phi(r) = \Omega r$  for  $r \leq r_c$ ,

$$E_{\text{core}} = \int_0^{r_c} \frac{1}{2} \rho_f (\Omega r)^2 (2\pi r \ell) dr = \frac{\pi}{4} \rho_f \Omega^2 r_c^4 \ell.$$

Outside the core,  $v_\phi(r) = \Gamma / (2\pi r)$  with  $\Gamma = 2\pi \Omega r_c^2$ , giving the slender-tube envelope term

$$E_{\text{env}} \simeq \frac{\rho_f \Gamma^2}{4\pi} \ell \ln \frac{R}{r_c},$$

where  $R$  is an outer cutoff set by the nearest boundary or neighboring strings. Both contributions are standard in vortex-tube energetics (core + Biot–Savart envelope).

**Coarse-graining.** At macroscales, we use the canonical identity

$$K = \frac{\rho_{\text{core}} r_c}{v_s}, \quad \rho_f = K \Omega_{\text{leaf}}.$$

where  $\Omega_{\text{leaf}}$  is a coarse-grained (leaf-averaged) angular rate. Numerically,  $\Omega_{\text{leaf}} \sim 10^{-4} \text{ s}^{-1}$  in the Canon fit; it must not be confused with the microscopic core rate below.

## 2 Layered Time Scaling from Swirl Dynamics

Adopt the SR-like local rule

$$\frac{d\tau}{dt} = \sqrt{1 - \frac{v_\phi^2(r)}{c^2}}.$$

With a Rankine profile,

$$v_\phi(r) = \begin{cases} \Omega_{\text{core}} r, & r \leq r_c, \\ \frac{\Gamma}{2\pi r}, & r \geq r_c, \end{cases} \quad \Gamma = 2\pi \Omega_{\text{core}} r_c^2.$$

Continuity at  $r = r_c$  gives  $v_\phi(r_c) = \Omega_{\text{core}} r_c \equiv v_s$ , hence

$$\Omega_{\text{core}} = \frac{v_s}{r_c} \approx \frac{1.09384563 \times 10^6}{1.40897017 \times 10^{-15}} \approx 7.763 \times 10^{20} \text{ s}^{-1}.$$

Thus

$$\frac{d\tau}{dt} = \begin{cases} \sqrt{1 - \frac{\Omega_{\text{core}}^2 r^2}{c^2}}, & r \leq r_c, \\ \sqrt{1 - \frac{\Gamma^2}{4\pi^2 c^2 r^2}}, & r \geq r_c. \end{cases}$$

The earlier ansatz  $d\tau/d\bar{t} = e^{-r/r_c}$  can be used only as a phenomenological fit; it does not follow from the SR-like form unless one imposes a special  $v_\phi(r)$  inconsistent with Rankine.