himpunan 8 A B AC B AVC ANB A В B В B v AVB AC BVC (CUA) OB в В A Ce UBAC BC ABBAC V B В B C BC U ACOB AAC A B B B B C AVB Ans BUNA (BUCI O A B C (BAC') V (AACAB') (AVC) +(AVB)+(BVC) - (AAB'AC') V(BAC) (ACUBU Ce)

TYPE OF ROTATION	Matrix to be multiplied	
Rotation of 90° (clock wise)	$ \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} $	
Rotation of 90° (counter clock wise)	$ \left[\begin{array}{cc} 0 & -1 \\ 1 & 0 \right] $	
Rotation of 180° (clock wise & counter clock wise)	$ \left[\begin{array}{cc} -1 & 0 \\ 0 & -1 \end{array}\right] $	
Rotation of 270° (clock wise)	$ \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} $	
Rotation of 270° (counter clock wise)	$ \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} $	

Calculus Symbols

$\lim_{x\to 0} f(x)$	ε	y'	y''
limit	epsilon	derivative	second derivative
$y^{\scriptscriptstyle(n)}$	$\frac{dy}{dx}$	$\frac{d^2y}{dx^2}$	$\frac{d^n y}{dx^n}$
n th derivative	derivative	second derivative	n th derivative
\dot{y}	\ddot{y}	$D_x y$	$D_x^{\ 2}y$
time derivative	time second derivative	derivative	second derivative
$\frac{\partial f(x,y)}{\partial x}$	\int	\iint	
partial derivative	integral	double integral	triple integral
∮	∯	<i>∰</i>	i
closed line integral	closed surface integral	closed volume integral	imaginary unit
z^*	$ar{z}$	$ec{x}$	\hat{x}
complex conjugate	complex conjugate	vector	unit vector
x*y	L	${\mathcal F}$	8
convolution	laplace transform	fourier transform	delta function

LAWSOF

EXPONENTS

Law
Example

$$a^0 = 1$$
 $a^1 = a$
 $17^1 = 17$
 $\sqrt{a} = a^{\frac{1}{2}}$
 $\sqrt{4} = 4^{\frac{1}{2}}$

$$\sqrt[n]{a} = a^{\frac{1}{n}}$$

$$\sqrt[3]{27} = 27^{\frac{1}{3}}$$

$$a^{-m} = \frac{1}{a^m}$$

$$9^{-2} = \frac{1}{9^2}$$

$$a^{-m} = \frac{1}{a^m} \qquad 9^{-2} = \frac{1}{9^2}$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m} \qquad \left(\frac{5}{6}\right)^2 = \frac{5^2}{6^2}$$

$$a^m \times a^n = a^{m+n} 5^2 \times 5^4 = 5^{2+4}$$

$$\frac{a^m}{a^n} = a^{m-n} \qquad \frac{4^5}{4^3} = 4^{5-3}$$

$$(a^m)^n = a^{m \times n} \qquad (2^5)^3 = 2^{5 \times 3}$$

$$a^n \times b^n = (a \times b)^n$$
 $2^5 \times 3^5 = (2 \times 3)^5$

$$a^{\frac{m}{n}} = \sqrt[n]{a^m}$$

$$81^{\frac{3}{2}} = \sqrt[2]{81^3}$$

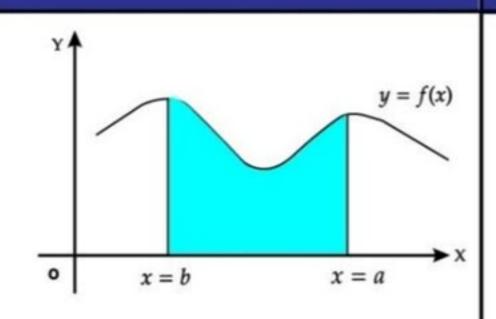
$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$$

$$\left(\frac{3}{4}\right)^{-2} = \left(\frac{4}{3}\right)^2$$

$$\frac{a^{-n}}{b^{-m}} = \frac{b^m}{a^n} \qquad \frac{3^{-2}}{4^{-5}} = \frac{4^5}{3^2}$$

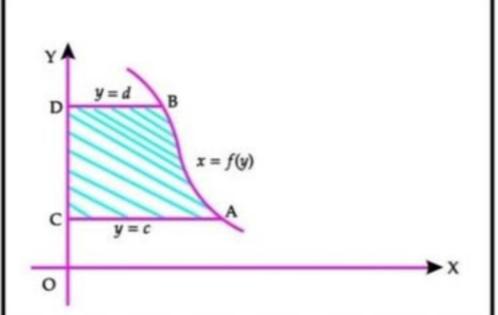
Graph

Area



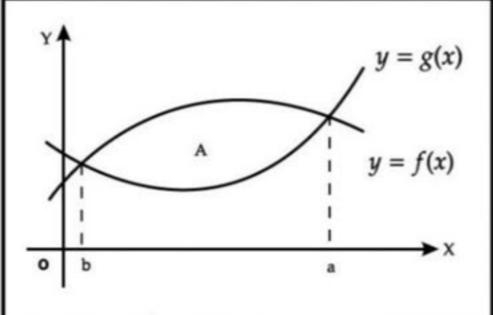
Area of the curve bounded by x - axis

$$Area = \int_{b}^{a} f(x)dx$$



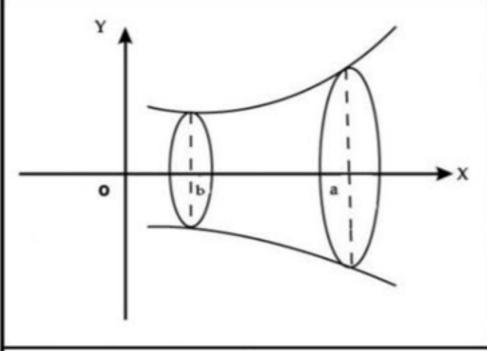
Area of the curve bounded by y - axis

$$Area = \int_{c}^{d} f(y)dy$$



Area between two curves

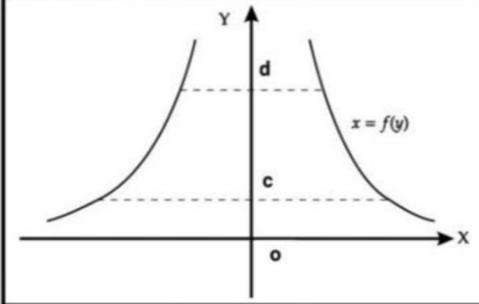
$$Area = \int_{b}^{a} (f(x) - g(x))dx$$



Volume of Revolution

Rotation about x - axis:

Area:
$$\pi \int_{b}^{a} y^{2} dx$$



Volume of Revolution

Rotation about y - axis:

Area:
$$\pi \int_{c}^{d} x^{2} dx$$

$$\log_{\bullet} = \bigoplus_{\bullet} \bigoplus_{\bullet} = \bigoplus_{\bullet} \bigoplus_{\bullet}$$

$$\log_{\bullet}(\sqrt{}) = \frac{\log_{\bullet}}{\log_{\bullet}}$$

$$= (\log_{\bullet})$$

PHYSICS

STOKE'S LAW

$$V = \frac{2}{9} \frac{\left(\rho_p - \rho_f\right)}{\mu} g R^2$$

(i) mathsolverr

- g is the gravitational field strength (m/s²)
- R is the radius of the spherical particle (m)
- ρ_p is the mass density of the particle (kg/m³)
- ρ_f is the mass density of the fluid (kg/m³)
- μ is the dynamic viscosity (kg/(m*s)).

$$F = 6\pi \eta r v$$

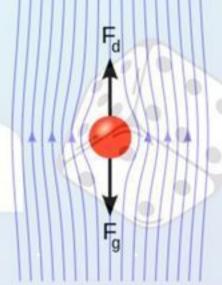
$$F$$
 = drag force

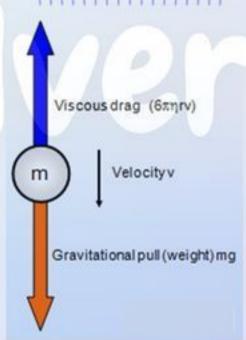
$$\pi = pi$$

r = sphere radius

 η = fluid viscosity

v = velocity of the sphere







SAVE IT FOR LATER

MATH

Euler's Formula

$$I = \int \frac{dx}{1 + x^2} = \tan^{-1}(x)$$
 1

$$I = \frac{1}{i} \int \frac{idx}{1 - (ix)^2} = \frac{1}{2i} \ln \left(\frac{1 + ix}{1 - ix} \right)$$

from 1 and 2

$$\therefore \tan^{-1}(x) = \frac{1}{2i} \ln \left(\frac{1+ix}{1-ix} \right)$$

$$\therefore 2i \tan^{-1}(x) = \ln\left(\frac{1+ix}{1-ix}\right)$$

Put $x = \tan(\theta)$

$$\lim_{i} e^{i\varphi} = \cos \varphi + i \sin \varphi$$

$$\lim_{i} e^{i\varphi} = \cos \varphi + i \sin \varphi$$

$$\lim_{i} e^{i\varphi} = \cos \varphi + i \sin \varphi$$

$$\lim_{i} e^{i\varphi} = \cos \varphi + i \sin \varphi$$

$$\lim_{i} e^{i\varphi} = \cos \varphi + i \sin \varphi$$

$$e^{ix} = \cos x + i \sin x$$

$$\therefore 2i \tan^{-1}(\tan(\theta)) = \ln\left(\frac{1+i\tan(\theta)}{1-i\tan(\theta)} \times \frac{\cos\theta}{\cos\theta}\right)$$

$$\therefore 2i\theta = \ln\left(\frac{\cos\theta + i\sin\theta}{\cos\theta - i\sin\theta}\right)$$

$$\therefore 2i\theta = \ln\left(\frac{\cos\theta + i\sin\theta}{\cos\theta - i\sin\theta} \times \frac{\cos\theta + i\sin\theta}{\cos\theta + i\sin\theta}\right)$$

$$2i\theta = \ln\left(\frac{(\cos\theta + i\sin\theta)^2}{\cos^2\theta + \sin^2\theta}\right) = \ln[(\cos\theta + i\sin\theta)^2]$$

 $\therefore 2i\theta = 2\ln(\cos\theta + i\sin\theta)$

$$\therefore i\theta = \ln(\cos\theta + i\sin\theta)$$

$$\therefore e^{i\theta} = \cos\theta + i\sin\theta$$



2.71828183

SAVE IT FOR LATER



Coulomb's Law & Newton's Law

classes

Coulomb's Law

The Force between two point charges is directly proportional to the product of the CHARGES and inversely proportional to the square of their distance apart.

$$F \propto Q_1 Q_2 \qquad F \propto \frac{1}{r^2}$$

$$F = k \frac{Q_1 Q_2}{r^2}$$

 $k = 9 \times 10^9 \, \text{Nm}^2 \text{C}^{-2}$

Newton's Law

The Force between two point masses is directly proportional to the product of the MASSES and inversely proportional to the square of their distance apart.

$$F \propto m_1 m_2 \quad F \propto \frac{1}{r^2}$$

$$F = G \frac{m_1 m_2}{r^2}$$

G= 6.6742 x 10-11 m3kg-1s-2

Gauss's Law

The total of the electric flux out of a closed surface is equal to the charge enclosed divided by the permittivity.

$$\Delta \Phi = E \Delta A$$

perpendicular

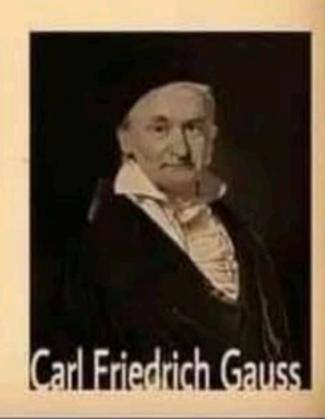
$$\Phi_{electric} = \frac{Q}{\mathcal{E}_0}$$



The sum of the flux is proportional to the total charge enclosed.

$$\oint \vec{E} \cdot \vec{dA} = \frac{Q}{\varepsilon_0}$$

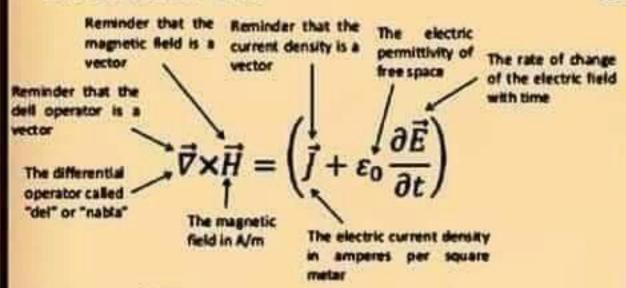
The area integral of the electric field over any closed surface is equal to the net charge enclosed in the surface divided by the permittivity of space.



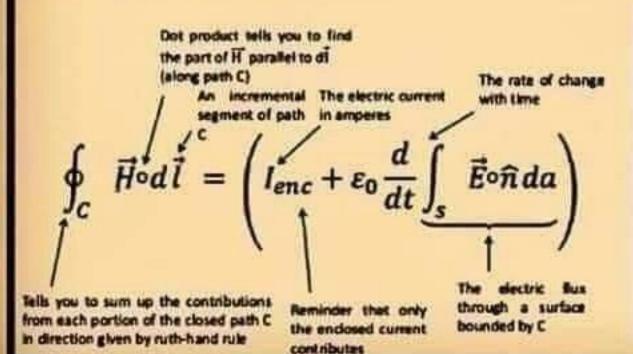
Ampere-Maxwell equation

Differential Form

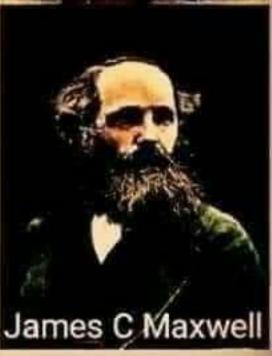
@joshi_physics_classes



Integral Form







Ohm's Law



$$V_{ab} = -\int_{b}^{a} \vec{E} \cdot d\vec{l} = \int_{a}^{b} \vec{E} \cdot d\vec{l}$$

 \vec{E} is constant and parallel to $d\vec{l}$ along l



$$V_{ab} = E l_{ab} \to \mathbf{V} = \mathbf{E} \mathbf{l}$$
$$I = \iint_{S} \vec{J} \cdot d\vec{S}$$

 \vec{J} is constant and parallel to $d\vec{S}$ on S

$$I = JS$$

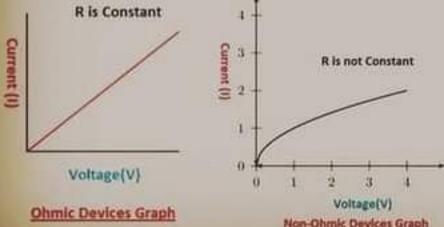
$$R = \frac{l}{\sigma S} \rightarrow R = \frac{V}{I} \frac{J}{\sigma E}$$

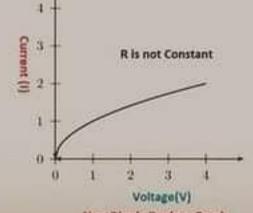
$$\vec{J} = \sigma \vec{E} \to \vec{J} = \sigma \vec{E}$$

$$R = \frac{VJ}{IJ} \to R = \frac{V}{I}$$

= RI

E: electric field



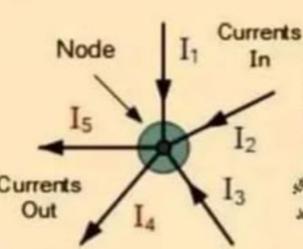


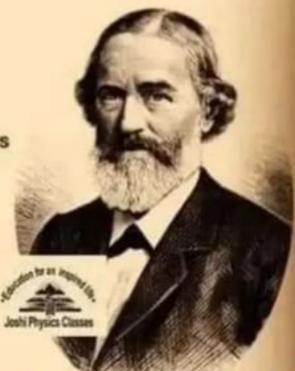
Kirchhoff's Circuit Law

Kirchhoff's Current Law

Currents Entering the Node Equals Currents Leaving the Node

$$I_1 + I_2 + I_3 + (-I_4 + -I_5) = 0$$
 Currents





Gustav Kirchhoff

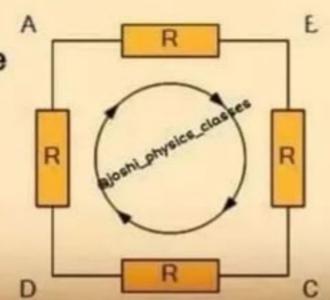
Also Known for:

- Kirchhoff's law of thermal radiation
- Kirchhoff's laws of spectroscopy
- Kirchhoff's law of thermochemistry

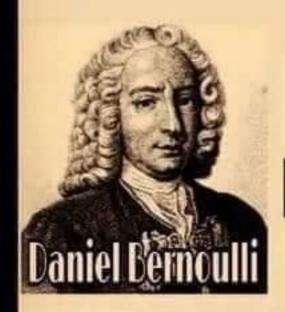
Kirchhoff's Voltage Law

The sum of all the Voltage Drops around the loop is equal to Zero

$$V_{AB} + V_{BC} + V_{CD} + V_{DA} = 0$$



Bernoulli's principle

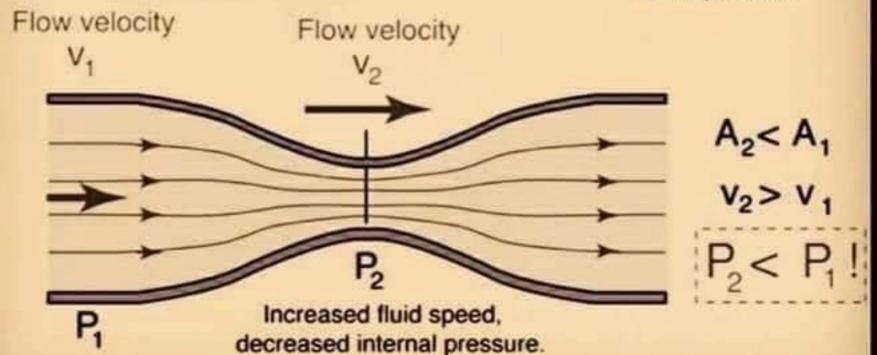


Energy per unit volume before = Energy per unit volume after

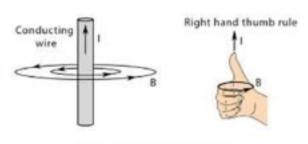
$$P_1 + {}_2^1 \rho v_1^2 + \rho g h_1 = P_2 + {}_2^1 \rho v_2^2 + \rho g h_2$$

Pressure Energy Kinetic Energy per unit volume Potential Energy per unit volume

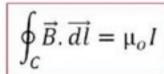




AMPERE'S CIRCUITAL LAW



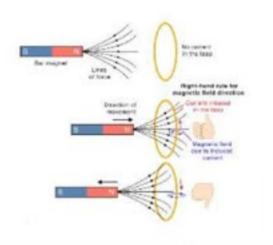




The magnetic field created by an electric current is proportional to the size of that electric current with a constant of proportionality equal to the permeability of free space.

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LENZ'S LAW



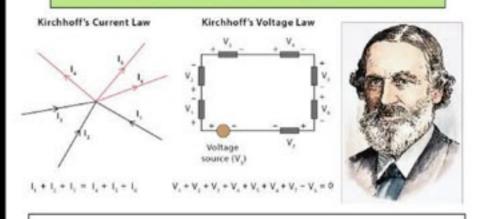


$$\mathcal{E} = -N \frac{\Delta \Phi}{\Delta t}$$

The direction of an electric current induced in a conductor by a changing magnetic field is such that the magnetic field created by the induced current opposes changes in the initial magnetic field.

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KIRCHOFF'S LAW

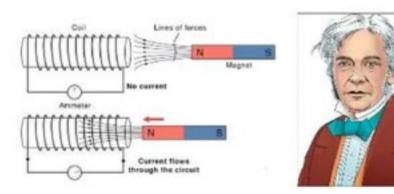


The total current entering a junction or a node is equal to the charge leaving the node as no charge is lost.

The voltage around a loop equals the sum of every voltage drop in the same loop for any closed network and equals zero.

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FARADAY'S LAW OF EMI



1st LAW

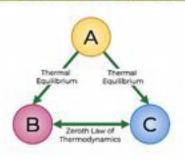
Whenever a conductor is placed in a varying magnetic field, an electromotive force is induced. If the conductor circuit is closed, a current is induced, which is called induced current.

2nd LAW

The induced emf in a coil is equal to the rate of change of flux linkage.

 $\mathcal{E}=-N\frac{\Delta\Phi}{\Delta t}$

ZEROTH LAW OF THERMODYNAMICS





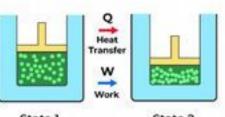
ROLPH H FOWLER

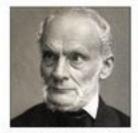
If two thermodynamic systems are both in thermal equilibrium with a third system, then the two systems are in thermal equilibrium with each other.

Two systems are said to be in thermal equilibrium if they are linked by a wall permeable only to heat, and they do not change over time.

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FIRST LAW OF THERMODYNAMICS





State 1

State 2

RUDOLPH CLAUSIUS

$$\Delta U = Q - W$$

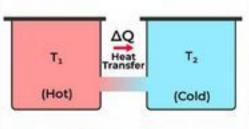
 ΔU = change in internal energy

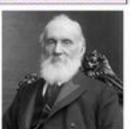
Q = heat added

W - work done by the system.

The change in internal energy of a system equals the net heat transfer into the system minus the net work done by the system. It is based on Conservation of Energy.

SECOND LAW OF THERMODYNAMICS





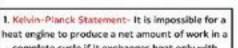
WILLIAM THOMSON

Entropy of an isolated system will never decrease over time.

bodies at a single fixed temperature.

produces no other effect than the transfer of

heat from a cooler body to a hotter body.



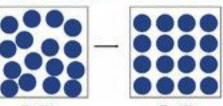
complete cycle if it exchanges heat only with 2. The Clausius statement: It is impossible to construct a device that operates on a cycle and

 $\Delta S = Entropy = \frac{\Delta Q}{R}$

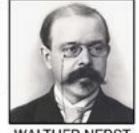
Reservoir Q, Reservoir

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THIRD LAW OF THERMODYNAMICS



5>0 Entropy becomes zero at 0K

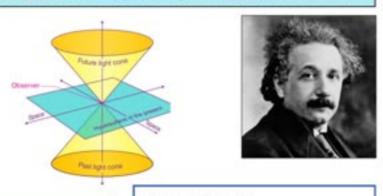


WALTHER NERST

$$\Delta S = \int_{T_1}^{T_2} \frac{C(T) \ \mathrm{d}T}{T}$$

The entropy of a closed system at thermodynamic equilibrium approaches a constant value when its temperature approaches absolute zero.

EINSTEIN THEORY OF RELATIVITY



 $E = mc^2$

E = Energy in Joule

m = Mass of an object in Kg

c = Speed of light = 3,00,00,000 m/sec

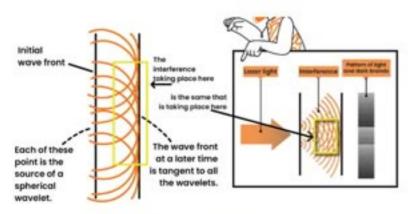
- The laws of physics are the same for all observers in any inertial frame of reference relative to one another (principle of relativity).
- The speed of light in a vacuum is the same for all observers, regardless of their relative motion or of the motion of the light source.

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HUYGEN'S PRINCIPLE

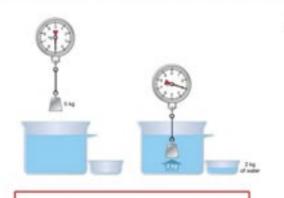
Every point on a wavefront is in itself the source of spherical wavelets which spread out in the forward direction at the speed of light. The sum of these spherical wavelets forms the wavefront.

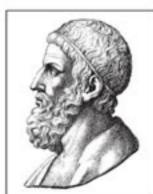




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ARCHIMEDES PRINCIPLE



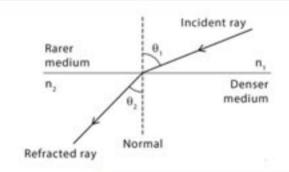


$$F_b = -
ho g V$$

Archimedes' principle states that the upward buoyant force that is exerted on a body immersed in a fluid, whether fully or partially, is equal to the weight of the fluid that the body displaces.

Pinterest: @Shadabalfaaz98

SNELL'S LAW





$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

Snell's Law gives a relationship between the angles of incidence (Ø₁) and refraction (Ø₂) when a ray of light travels from a rarer medium of refractive index (n₁) to a denser medium of refractive index (n₂).

NEWTON'S LAWS OF MOTION





A body remains in the state of rest or uniform motion in a straight line unless and until an external force acts on it.



2nd Law

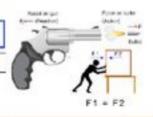


The net force on a body is equal to the body's acceleration multiplied by its mass or, equivalently, the rate at which the body's momentum changes with time.



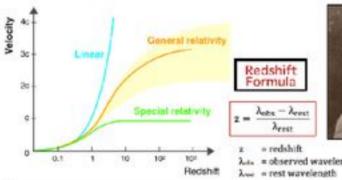
3rd Law

For every action, there is an equal and opposite reaction.



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HUBBLE'S LAW



= observed wavelength

The greater the distance of a galaxy, the faster it recedes. Hubble established the cosmological velocity-distance law:

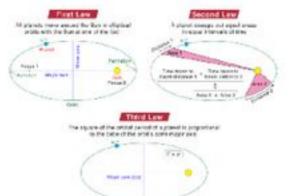
$$v = H_0 D$$

v = recessional velocity

 H_0 = Hubble's constant = 71 $\frac{km/s}{}$ $=2.3x10^{-18}s^{-1}$

D = proper distance

KEPLER'S LAW OF PLANETARY MOTION

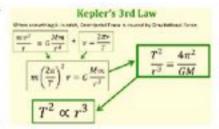




1st Law -> The orbit of a planet is an ellipse with the Sun at one of the two foci.

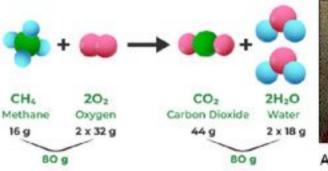
2nd Law -> A line segment joining a planet and the Sun sweeps out equal areas during equal intervals

3rd Law -> The square of a planet's orbital period is proportional to the cube of the length of the semi-major axis of its orbit.



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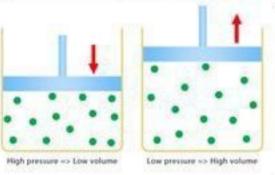
LAW OF CONSERVATION OF MASS



ANTOINE LAVOISIER

Matter can neither be created nor be destroyed in a chemical reaction. In other words, the mass of products in chemical reactions equals the mass of reactants.

BOYLE'S LAW



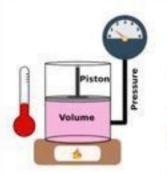


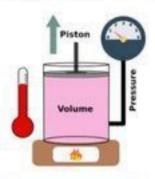
$$P_1V_1 = P_2V_2$$

The absolute pressure exerted by a given mass of an ideal gas is inversely proportional to the volume it occupies if the temperature and amount of gas remain unchanged within a closed system.

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CHARLES' LAW





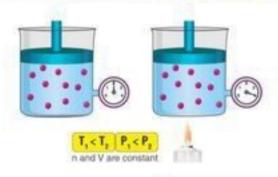


$$\frac{V_1}{T_1}=\frac{V_2}{T_2}$$

The volume occupied by a fixed amount of gas is directly proportional to its absolute temperature, if the pressure remains constant.

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GAY LUSAAC'S LAW



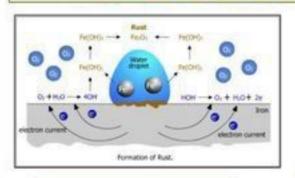


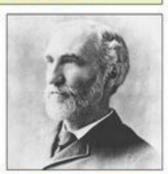
$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

The pressure exerted by a gas (of a given mass and kept at a constant volume) varies directly with the absolute temperature of the gas.

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GIBBS FREE ENERGY





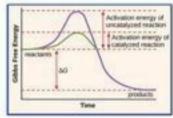
$$\Delta G = \Delta H - T \Delta S$$

 ΔG = change in Gibbs Free Energy

 ΔH = change in enthalpy

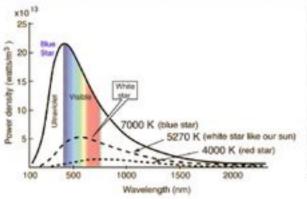
T - temperature in Kelvin

 ΔS = change in entropy



Gibbs free energy is a thermodynamic potential that can be used to calculate the maximum amount of work, other than pressure-volume work, that may be performed by a thermodynamically closed system at constant temperature and pressure.

WIEN DISPLACEMENT LAW





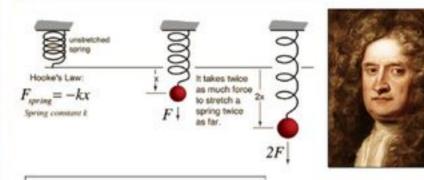
$$\lambda_{m} = \frac{b}{T}$$

b = Wein's Displacement Constant = 0.002898 m T = absolute Temperature in Kelvin

Wien's displacement law states that the black-body radiation curve for different temperatures will peak at different wavelengths that are inversely proportional to the temperature.

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HOOKE'S LAW



 F_s = spring force

k = spring constant

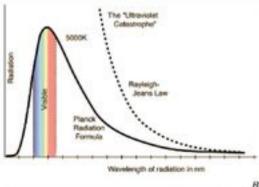
x = spring stretch or compression

 $F_s = -kx$

Hooke's law states that the force required to extend or compress a spring by some distance is directly proportional to that distance.

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PLANCK'S LAW





$$B_{\lambda}(\lambda,T) = rac{2hc^2}{\lambda^5} rac{1}{e^{rac{hc}{\lambda k_{
m B}T}} - 1}.$$

B - spectral raciance of a body

* frequency

T = absolute temperature

Re - Boltzmann constant

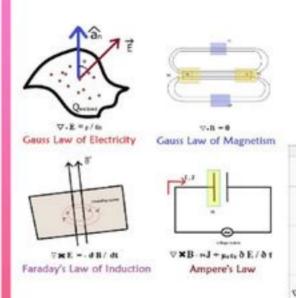
h = Planck constant

repeed of light in the medium

Electromagnetic radiation from heated bodies is not emitted as a continuous flow but is made up of discrete units or quanta of energy, the size of which involves a fundamental physical constant (Planck's constant).

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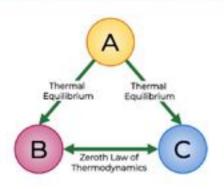
MAXWELL'S LAW





Commercial equations	Meaning
$\nabla \cdot \mathbf{E} = \frac{\rho}{c_0}$	The electric battleaving a volume a proportional is the charge inside:
$\nabla \cdot \mathbf{B} = 0$	There are no magnetic manapoles. Be total magnetic flar plenting in closed serface in seria.
$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$	The relage accumulated around a risted crook is proportional to the time rate of change of the magnetic fluid overses.
$\times \mathbf{B} = \mu_0 \left(\mathbf{J} + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right)$	Decinic carrents and changes in electric fields are procedures to the magnetic field consisting about the same tray person

ZEROTH LAW OF THERMODYNAMICS



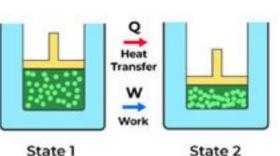


ROLPH H FOWLER

If two thermodynamic systems are both in thermal equilibrium with a third system, then the two systems are in thermal equilibrium with each other.

Two systems are said to be in thermal equilibrium if they are linked by a wall permeable only to heat, and they do not change over time.

FIRST LAW OF THERMODYNAMICS





State 2

RUDOLPH CLAUSIUS

$$\Delta U = Q - W$$

 ΔU = change in internal energy

= heat added

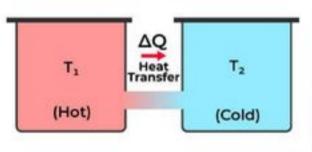
W = work done by the system

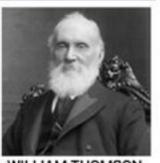
The change in internal energy of a system equals the net heat transfer into the system minus the net work done by the system. It is based on Conservation of Energy.

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SECOND LAW OF THERMODYNAMICS

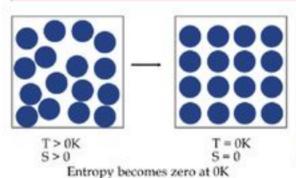




WILLIAM THOMSON

 $\Delta S = Entropy = \frac{\Delta Q}{Q}$

THIRD LAW OF THERMODYNAMICS





WALTHER NERST

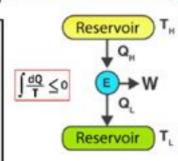
 $\Delta S = \int_{T_c}^{T_2} \frac{C(T) dT}{T}$

The entropy of a closed system at thermodynamic equilibrium approaches a constant value when its temperature approaches absolute zero.

Entropy of an isolated system will never decrease over time.

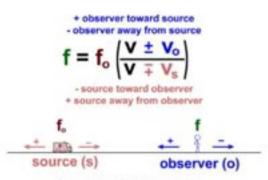
1. Kelvin-Planck Statement- It is impossible for a heat engine to produce a net amount of work in a complete cycle if it exchanges heat only with bodies at a single fixed temperature.

2. The Clausius statement: It is impossible to construct a device that operates on a cycle and produces no other effect than the transfer of heat from a cooler body to a hotter body.



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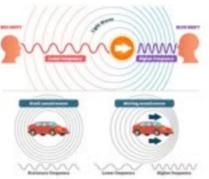
DOPPLER EFFECT



v : velocity of sound

The Doppler effect or the Doppler shift describes the changes in the frequency of any sound or light wave produced by a moving source with respect to an observer.





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SCHRODINGER EQUATION

$$i\hbar \frac{1}{\xi(t)} \frac{\delta \xi(t)}{\delta t} = -\frac{1}{\phi(x)} \frac{\hbar^2}{2m} \frac{\delta^2}{\delta x^2} \phi(x) + \hat{V}$$

$$(t) = e^{-(iEt/\hbar)} \qquad -\frac{\hbar^2}{2m} \frac{\delta^2}{\delta x^2} \psi(x) + \hat{V} \psi(x) = E \psi(x)$$

$$\psi(x, t) = \phi(x) e^{-(iEt/\hbar)}$$

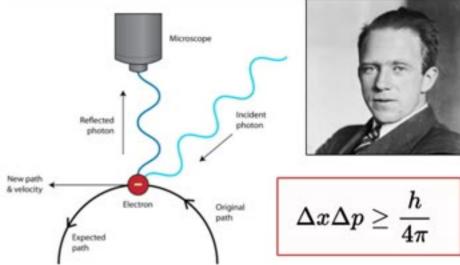
solving the time-independent Schrödinger equation is enough to know about the time-evolution of a particle



The Schrodinger wave equation is a mathematical expression describing the energy and position of the electron in space and time, taking into account the matter wave nature of the electron inside an atom.

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HEISENBERG UNCERTAINTY PRINCIPLE

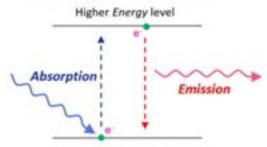


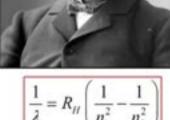
There is a limit to the precision with which certain pairs of physical properties, such as position and momentum, can be simultaneously known. It is impossible to accurately measure the energy of a system in some finite amount of time.

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RYDBERG EQUATION

Emission occurs when the electron falls from an excited (high energy) to the ground, or in general, a lower energy level.





Lower Energy level

Absorbing light with sufficient energy moves the electron in a higher energy level.

Rx = Rydberg constant = mg⁴/_{Sur-brie} = 1.0973 x 10⁵ m⁵

The Rydberg formula is the mathematical formula to determine the wavelength of light emitted by an electron moving between the energy levels of an atom.