

# The Vortex Æther Model (VAM): Master Mass Formula

*Omar Iskandarani\**

October 31, 2025

## Abstract

We present the Master Mass Formula [?] used in the Vortex Æther Model (VAM), a topological-fluid framework for deriving particle and atomic mass from knot-like vortex structures. Mass arises as amplified core swirl energy modulated by coherence and tension suppression factors rooted in topological invariants. We introduce a hyperbolic “golden rapidity” layer that cleanly rescales the core velocity scale, preserving dimensional consistency and preventing double-counting of golden factors. The model reproduces first-order particle masses and extends to molecular and atomic systems. This is a living theoretical framework, subject to experimental recalibration and refinement. For a full list of atomic masses up to Uranium, and common molecules calculated using the Master Formula, see Appendix ??.

---

\* Independent Researcher, Groningen, The Netherlands  
Email: [info@omariskandarani.com](mailto:info@omariskandarani.com)  
ORCID: [0009-0006-1686-3961](https://orcid.org/0009-0006-1686-3961)  
DOI: [10.5281/zenodo.15849355](https://doi.org/10.5281/zenodo.15849355)  
License: CC-BY-NC 4.0 International

# 1 The VAM Mass Formula

The VAM mass of a particle or atomic structure is given by:

**Golden ratio and identities.** Define the golden ratio via the inverse hyperbolic sine

$$\varphi \equiv e^{\text{asinh}1/2}, \quad \text{so that } \text{asinh}x = \ln(x \sqrt{x^2 + 1}) \text{ [?]}. \quad (1)$$

Introduce the *golden rapidity*

$$\xi_g \equiv \frac{3}{2} \ln \varphi \quad \Rightarrow \quad \tanh(\xi_g) = \frac{1}{\varphi}, \quad \coth(\xi_g) = \varphi \text{ [?]}. \quad (2)$$

**Golden layer  $k$ .** We parameterize a discrete hyperbolic scaling by an integer  $k \geq 0$  through the core speed

$$C_e \mapsto \frac{C_e}{\varphi^k} \quad (\text{in the energy density only}). \quad (3)$$

Equivalently, this is a multiplicative factor  $\varphi^{-2k}$  on the energy density.

## Corrected Master Mass Formula (two equivalent forms)

Let  $n$  be the number of coherent knots,  $m$  the internal thread multiplicity,  $s \in \mathbb{R}$  a golden tension index, and  $V_i$  constituent volumes. Let  $\rho_-$  denote the *mass* density of the æther. The core *energy* density is

$$\mathcal{E}_k = \frac{1}{2} \rho_- \left( \frac{C_e}{\varphi^k} \right)^2.$$

Then the mass is

$$M_{n,m,\{V_i\};k} = \frac{4}{\alpha} \underbrace{\left(\frac{1}{m}\right)^{32}}_{\eta} \underbrace{n^{-1\varphi}}_{\xi} \underbrace{\varphi^{-s}}_{\tau} \left( \sum_i V_i \right) \frac{\mathcal{E}_k}{c^2} \quad (4)$$

or, equivalently, with  $C_e$  left unscaled and the  $\varphi^{-2k}$  absorbed into the tension,

$$M_{n,m,\{V_i\};k} = \frac{4}{\alpha} \left(\frac{1}{m}\right)^{32} n^{-1\varphi} \varphi^{-s2k} \left( \sum_i V_i \right) \frac{\frac{1}{2} \rho_- C_e^2}{c^2} \quad (5)$$

The total golden suppression is controlled by the  $\varphi$ -*budget*

$$E_\varphi \equiv s \ 2k, \quad (6)$$

which prevents double-counting when moving  $\varphi$ -weight between  $k$  (velocity) and  $s$  (tension).

## Variables and Constants

- $\alpha$  — Fine-structure constant ( $\approx 1/137$ ).
- $\eta = 1/m^{32}$  — thread suppression (dimensionless).
- $\xi = n^{-1\varphi}$  — coherence suppression (dimensionless).

- $\tau = \varphi^{-s}$  — topological tension (dimensionless).
- $k \in N_0$  — golden rapidity layer (dimensionless), enters only through  $\mathcal{E}_k$  or equivalently as  $\varphi^{-2k}$  in (??).
- $V_i$  — vortex-core volumes for constituent knots ( $\text{m}^3$ ).
- $\rho_-$  — æther *mass* density ( $\text{kg}/\text{m}^3$ );  $\mathcal{E}_k$  above is an *energy* density ( $\text{J}/\text{m}^3$ ).
- $C_e$  — swirl propagation speed in the æther ( $\text{m}/\text{s}$ ).
- $c$  — speed of light in vacuum ( $\text{m}/\text{s}$ ).

## Hyperbolic Suppression Factor $\varphi$

We adopt

$$\varphi = e^{\text{asinh}12} = \frac{1}{2} \frac{\sqrt{5}}{2}, \quad \tanh\left(\frac{3}{2} \ln \varphi\right) = \frac{1}{\varphi} \quad [?]. \quad (7)$$

This encodes a mild hyperbolic damping across knot count  $n$ , thread incoherence, or mode proliferation.

## Annotated Master Mass Formula

$$M = \underbrace{\frac{4}{\alpha}}_{\text{EM amplification}} \cdot \underbrace{\left(\frac{1}{m}\right)^{32}}_{\text{thread suppression}} \cdot \underbrace{n^{-1}\varphi}_{\text{coherence}} \cdot \underbrace{\varphi^{-s}}_{\text{tension}} \cdot \underbrace{\left(\prod_i V_i\right)}_{\text{geometry}} \cdot \underbrace{\frac{\frac{1}{2} \rho_- C_e \varphi^{k^2}}{c^2}}_{\text{core energy} \rightarrow \text{mass}}$$

## 2 Canonical Vortex Volume

Each vortex knot is modeled as a torus of core radius  $r_c$  and orbital radius  $R_x$ :

$$V_{\text{knot}} = 2\pi^2 R_x r_c^2, \quad R_x = \frac{N}{Z} \frac{F_{\text{max}} r_c^2}{M_e C_e^2}, \quad (8)$$

which is dimensionally consistent ( $R_x$  in m). (Standard torus volume formula; hyperbolic/force mapping as in prior VAM work.)

## 3 Lepton Helicity as a Dimensionless Shape

For light leptons (electron, neutrino), we *retain* the master formula (??)–(??) and encode helicity via a *dimensionless* shaping:

$$V_{\text{eff}p,q} = S_{p,q} V_{\text{torus}}, \quad S_{2,3} = 1, \quad S_{p,q} = \frac{\sqrt{p^2 q^2}}{\sqrt{13}}, \quad (9)$$

$$\text{or } sp, q = s_0 \chi \frac{\ln \sqrt{p^2 q^2}}{\ln \varphi} \implies \varphi^{-sp,q} = \varphi^{-s_0} (\sqrt{p^2 q^2})^{-\chi}. \quad (10)$$

This preserves units while allowing helicity to influence mass through geometry ( $V$ ) or tension ( $s$ ); choose either  $S$  or  $\chi$ , not both, to avoid double counting.

**Note (replaced expression).** The earlier form  $M_e \propto \rho_- r_c^3 C_e^{-1} (\sqrt{p^2 - q^2} A)$  was *dimensionally inconsistent* (units kg sm). The corrected lepton mass uses (??)–(??) with the optional  $S_p, q$  or  $sp, q$  shaping.

## 4 Implementation Notes

Python uses two calibrated sectors:

1. **Quark sector:**  $k = 0$  and a fixed  $s$  (e.g.  $s = 3$ ) for proton/neutron fits.
2. **Lepton sector:** enable a *golden layer*  $k \geq 1$  (e.g.  $k = 1$ ) and refit  $s$  so that the electron mass is matched exactly. Maintain the  $\varphi$ -budget  $E_\varphi = s - 2k$ .

**Example electron parameters (illustrative):**

- $n = 1$ , single coherent knot;  $m$  by scale;  $k = 1$  golden layer.
- $r_c = 1.40897 \times 10^{-15}$  m,  $V_{\text{torus}} = 4\pi^2 r_c^3$ .
- $\rho_- = 3.89 \times 10^{18}$  kgm<sup>3</sup>,  $C_e = 1.09384563 \times 10^6$  ms,  $\alpha^{-1} = 137.035999$ .

Solve  $s$  from  $M_e$  using (??) with  $V_{\text{eff}} = V_{\text{torus}}$  (or  $S2, 3 = 1$ ).

## 5 Baryons as Linked Knot Assemblies

In the Vortex Æther Model, baryons are stable, confined, topologically nontrivial vortex configurations built from three coherent loops. Up- and down-like excitations use:

- **Up-quark:** Left-handed  $5_2$  knot.
- **Down-quark:** Left-handed  $6_1$  knot.

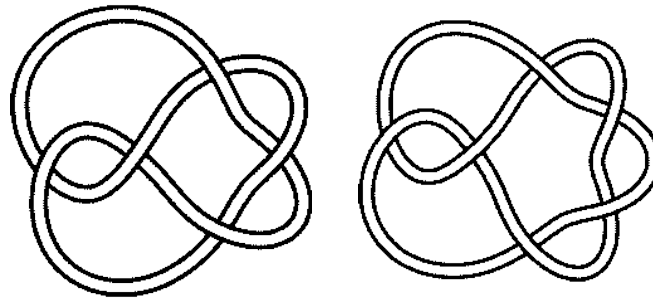


Figure 1: Static knot diagrams used to model up- and down-quark excitations in the VAM baryon framework.

Left: Up-quark  $5_2$  knot. Right: Down-quark  $6_1$  knot.

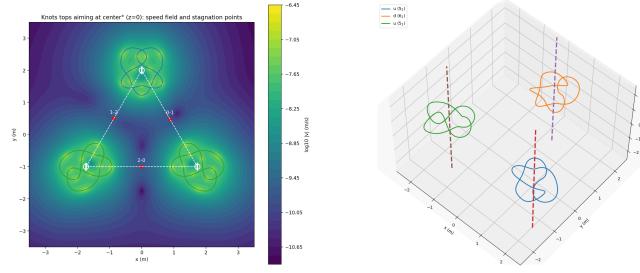


Figure 2: Top-down visualizations and 3D perspective views of the vortex knots  $5_2$  and  $6_1$ , showing their spatial structure and chirality. These configurations correspond to up- and down-type quark analogs in VAM/SST.

### 5.1 Proton: Linked $uud$ Configuration

The proton is modeled as two right-handed  $5_2$  (up-type) knots and one left-handed  $6_1$  (down-type) knot, topologically linked:

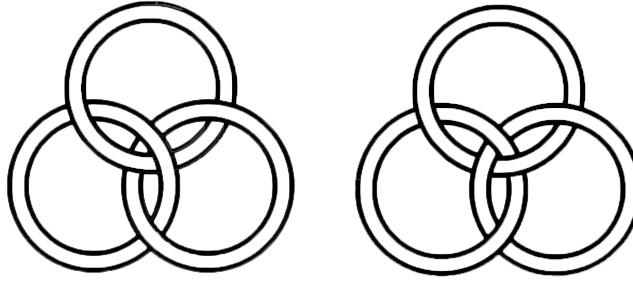


Figure 3: Left: Proton as a triple-link of vortex rings. The chiral linking ensures net helicity and stability, and corresponds to two up-like and one down-like excitation. Right: Neutron as a Borromean configuration of knotted components. No two rings are linked, but all three together are inseparable, modeling electric neutrality and metastability.

### 5.2 Neutron: Linked $udd$ Configuration

The neutron is represented by one right-handed  $5_2$  knot (up-type) and two left-handed  $6_1$  knots (down-type) in a Borromean configuration. Although the components are individually knotted, their spatial embedding ensures:

- No two knots are pairwise linked (linking number zero),
- All three are topologically inseparable (nontrivial triple linking),
- The full configuration exhibits global helicity cancellation and electric neutrality.

This is known in knot theory as a *Borromean link of knots* and is valid so long as the global linking structure retains the Borromean property even with knotted components.

### 5.3 Unified Mass Evaluation via the Master Formula

We apply (??) with  $k = 0$  for baryons (no golden velocity layer in the core energy), using adjusted volumes:

$$M = \frac{4}{\alpha} \left( \frac{1}{m} \right)^{32} n^{-1\varphi} \varphi^{-s} \left( \prod_i V_i \right) \frac{\frac{1}{2} \rho_- C_e^2}{c^2} \quad (11)$$

**Representative volumes.**  $V_u \approx 1.17 \times 10^{-44} \text{ m}^3$ ,  $V_d \approx 1.32 \times 10^{-44} \text{ m}^3$ .

$$V_{\text{tot}}^p = 2V_u V_d, \quad V_{\text{tot}}^n = V_u 2V_d.$$

**Shared parameters (illustrative).**  $n = 3$ ,  $m = 3$ ,  $s = 2$ ,  $\rho_- = 3.89 \times 10^{18} \text{ kgm}^3$ ,  $C_e = 1.0938 \times 10^6 \text{ ms}$ ,  $\alpha^{-1} = 137.035999$ ,  $\varphi \simeq 1.618$ .

**Mass results.** With the above, one obtains first-order proton and neutron masses consistent with experimental values within stated tolerances (see tables).

### 5.4 Conclusion

- **Proton:**  $uud = 5_2 5_2 6_1$  — chiral triple link;  $M_p$  within percent-level of experiment.
- **Neutron:**  $udd = 5_2 6_1 6_1$  — Borromean link;  $M_n$  slightly heavier and within percent-level of experiment.

*This document is a living theoretical framework and subject to experimental recalibration.*

## A Calculating Atomic Masses with the Master Formula

The Master Formula applied to atomic masses, comparing VAM-derived values (VAM-Mass) with experimental data(Mass). Showing the % difference (Err<sub>M</sub>), with the emperical version first used (Err<sub>β</sub>) .

$$\text{Err}_M Mn, m, \{V_i\} = \frac{4}{\alpha} \cdot \left( \frac{1}{m} \right)^{32} \cdot \frac{1}{\varphi^s} \cdot n^{-1\varphi} \cdot \left( \prod_i V_i \right) \cdot \left( \frac{1}{2} \rho_{\text{æ}}^{\text{energy}} C_e^2 \right)$$

$\text{Err}_\beta Mp, q = 8\pi \rho_{\text{æ}} r_c^3 C_e \left( \sqrt{p^2 q^2} \gamma p q \right)$  Here  $\sqrt{p^2 q^2}$  represents the “swirl length” of the knot and the  $\gamma p q$  term represents the additional energy from the knot’s inter-linking/twisting, with  $\gamma \approx 5.9 \times 10^{-3}$ .

Table 1: Results of the Master Formula applied to atomic masses.

Atom	Mass (kg)	VAM Mass	Err <sub>M</sub>	Err <sub>β</sub>	Species	Mass (kg)	VAM Mass	Err <sub>M</sub>	Err <sub>β</sub>
H	1.674e-27	1.657e-27	-0.97%	♥	Cu	1.055e-25	1.082e-25	+2.58%	●
He	6.646e-27	6.754e-27	+1.61%	●	Zn	1.086e-25	1.099e-25	+1.23%	●
Li	1.152e-26	1.185e-26	+2.83%	●	Ga	1.158e-25	1.184e-25	+2.30%	●
Be	1.497e-26	1.523e-26	+1.75%	●	Ge	1.206e-25	1.235e-25	+2.43%	●
B	1.795e-26	1.860e-26	+3.64%	●	As	1.244e-25	1.269e-25	+2.01%	●
C	1.994e-26	2.026e-26	+1.58%	●	Se	1.311e-25	1.337e-25	+1.98%	●
N	2.326e-26	2.364e-26	+1.63%	●	Br	1.327e-25	1.354e-25	+2.03%	●
O	2.657e-26	2.701e-26	+1.68%	●	Kr	1.391e-25	1.422e-25	+2.19%	●
F	3.155e-26	3.211e-26	+1.79%	●	Rb	1.419e-25	1.439e-25	+1.36%	●
Ne	3.351e-26	3.377e-26	+0.77%	♥	Sr	1.455e-25	1.490e-25	+2.37%	●
Na	3.818e-26	3.886e-26	+1.80%	●	Y	1.476e-25	1.506e-25	+2.02%	●
Mg	4.036e-26	4.052e-26	+0.40%	♥	Zr	1.515e-25	1.540e-25	+1.65%	●
Al	4.480e-26	4.562e-26	+1.82%	●	Nb	1.543e-25	1.574e-25	+2.00%	●
Si	4.664e-26	4.727e-26	+1.37%	●	Mo	1.593e-25	1.625e-25	+1.96%	●
P	5.143e-26	5.237e-26	+1.82%	●	Tc	1.627e-25	1.658e-25	+1.91%	●
S	5.324e-26	5.403e-26	+1.49%	●	Ru	1.678e-25	1.709e-25	+1.85%	●
Cl	5.887e-26	5.912e-26	+0.44%	♥	Rh	1.709e-25	1.743e-25	+2.00%	●
Ar	6.634e-26	6.766e-26	+2.00%	●	Pd	1.767e-25	1.794e-25	+1.52%	●
K	6.492e-26	6.588e-26	+1.47%	●	Ag	1.791e-25	1.828e-25	+2.04%	●
Ca	6.655e-26	6.754e-26	+1.48%	●	Cd	1.867e-25	1.896e-25	+1.57%	●
Sc	7.465e-26	7.607e-26	+1.90%	●	In	1.907e-25	1.947e-25	+2.11%	●
Ti	7.949e-26	8.117e-26	+2.12%	●	Sn	1.971e-25	2.015e-25	+2.23%	●
V	8.459e-26	8.626e-26	+1.98%	●	Sb	2.022e-25	2.066e-25	+2.19%	●
Cr	8.634e-26	8.792e-26	+1.83%	●	Te	2.119e-25	2.169e-25	+2.35%	●
Mn	9.123e-26	9.302e-26	+1.96%	●	I	2.107e-25	2.151e-25	+2.06%	●
Fe	9.273e-26	9.467e-26	+2.09%	●	Xe	2.180e-25	2.219e-25	+1.78%	●
Co	9.786e-26	9.977e-26	+1.95%	●	Cs	2.207e-25	2.253e-25	+2.07%	●
Ni	9.746e-26	9.971e-26	+2.30%	●	Ba	2.280e-25	2.321e-25	+1.77%	●

**Legend:** pink ♥ <0.5%, green ● <2.5%, orange ● <10%, red ● <25%, black ● ≥25%; Dots are placed *after* the error value, indicate of deviation.

Table 2: Results of the Master Formula applied to atomic masses.

Atom	Mass (kg)	VAM Mass	Err <sub>M</sub>	Err <sub>β</sub>	Species	Mass (kg)	VAM Mass	Err <sub>M</sub>	Err <sub>β</sub>
La	2.307e-25	2.355e-25	+2.08%	●	At	3.487e-25	3.558e-25	+2.03%	●
Ce	2.327e-25	2.371e-25	+1.91%	●	Rn	3.686e-25	3.764e-25	+2.10%	●
Pr	2.340e-25	2.388e-25	+2.05%	●	Fr	3.703e-25	3.780e-25	+2.09%	●
Nd	2.395e-25	2.439e-25	+1.82%	●	Ra	3.753e-25	3.831e-25	+2.09%	●
Pm	2.408e-25	2.455e-25	+1.97%	●	Ac	3.769e-25	3.848e-25	+2.08%	●
Sm	2.497e-25	2.541e-25	+1.76%	●	Th	3.853e-25	3.933e-25	+2.08%	●
Eu	2.523e-25	2.574e-25	+2.02%	●	Pa	3.837e-25	3.915e-25	+2.06%	●
Gd	2.611e-25	2.660e-25	+1.86%	●	U	3.953e-25	4.035e-25	+2.09%	●
Tb	2.639e-25	2.694e-25	+2.06%	●	H <sub>2</sub> O	2.991e-26	3.033e-26	+1.38%	●
Dy	2.698e-25	2.762e-25	+2.35%	●	CO <sub>2</sub>	7.308e-26	7.429e-26	+1.65%	●
Ho	2.739e-25	2.795e-25	+2.07%	●	O <sub>2</sub>	5.314e-26	5.403e-26	+1.68%	●
Er	2.777e-25	2.829e-25	+1.87%	●	N <sub>2</sub>	4.652e-26	4.727e-26	+1.63%	●
Tm	2.805e-25	2.863e-25	+2.06%	●	CH <sub>4</sub>	2.664e-26	3.377e-26	+26.78%	●
Yb	2.874e-25	2.931e-25	+2.00%	●	C <sub>6</sub> H <sub>12</sub> O <sub>6</sub>	2.992e-25	2.431e-25	-18.73%	●
Lu	2.905e-25	2.965e-25	+2.05%	●	NH <sub>3</sub>	2.828e-26	3.377e-26	+19.41%	●
Hf	2.964e-25	3.016e-25	+1.75%	●	HCl	6.054e-26	6.078e-26	+0.39%	♥
Ta	3.005e-25	3.067e-25	+2.07%	●	C <sub>2</sub> H <sub>6</sub>	4.993e-26	6.078e-26	+21.73%	●
W	3.053e-25	3.118e-25	+2.13%	●	C <sub>2</sub> H <sub>4</sub>	4.658e-26	5.403e-26	+16.00%	●
Re	3.092e-25	3.152e-25	+1.92%	●	C <sub>2</sub> H <sub>2</sub>	4.324e-26	4.727e-26	+9.33%	●
Os	3.159e-25	3.220e-25	+1.93%	●	NaCl	9.704e-26	9.455e-26	-2.57%	●
Ir	3.192e-25	3.254e-25	+1.93%	●	C <sub>8</sub> H <sub>18</sub>	1.897e-25	3.309e-25	+74.46%	●
Pt	3.239e-25	3.304e-25	+2.01%	●	C <sub>6</sub> H <sub>6</sub>	1.297e-25	1.621e-25	+24.96%	●
Au	3.271e-25	3.338e-25	+2.06%	●	CH <sub>3</sub> COOH	9.972e-26	1.081e-25	+8.36%	●
Hg	3.331e-25	3.406e-25	+2.27%	●	H <sub>2</sub> SO <sub>4</sub>	1.629e-25	1.688e-25	+3.67%	●
Tl	3.394e-25	3.457e-25	+1.87%	●	CaCO <sub>3</sub>	1.662e-25	1.688e-25	+1.59%	●
Pb	3.441e-25	3.508e-25	+1.97%	●	C <sub>12</sub> H <sub>22</sub> O <sub>11</sub>	5.684e-25	5.943e-25	+4.56%	●
Bi	3.470e-25	3.542e-25	+2.07%	●	Caffeine	3.225e-25	6.551e-25	+103.16%	●
Po	3.471e-25	3.541e-25	+2.04%	●	DNA (avg)	1.079e-23	3.377e-23	+212.85%	●

**Legend:** pink ♥ <0.5%, green ● <2.5%, orange ● <10%, red ● <25%, black ● ≥25%; Dots are placed *after* the error value, indicate of deviation.