

A Topological Reformulation of the Standard Model via Vortex Æther Dynamics

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Abstract

We present a reformulation of the Standard Model Lagrangian within the dimensional and topological framework of the Vortex Æther Model (VAM). In this approach, conventional quantum field terms are reinterpreted via fluid-mechanical analogs: particles correspond to knotted vortex excitations in a compressible æther, while interactions arise from swirl dynamics, circulation, and density fluctuations. The model replaces Planck-based constants with a complete set of natural units derived from mechanical quantities such as core radius (r_c), swirl velocity (C_e), and maximum æther force ($F_{\text{max}}^{\text{vam}}$). Coupling constants including α , \hbar , and e emerge from vortex properties rather than being fundamental inputs. We show that gauge fields arise from swirl structure, fermionic behavior from knotted helicity propagation, and mass from internal topological tension rather than spontaneous symmetry breaking. The resulting Lagrangian is dimensionally self-consistent, with all dynamics and interactions geometrically and physically grounded. This framework provides a unified mechanical ontology for quantum fields and offers new insights into the origins of mass, charge, and time from first principles.

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I. INTRODUCTION

Despite the empirical success of the Standard Model (SM) of particle physics and General Relativity (GR), fundamental questions remain unresolved: What is the physical origin of mass? Why do gauge interactions exhibit their particular symmetries? What gives rise to natural constants such as \hbar , e , or α beyond dimensional convenience?

Mainstream physics relies heavily on abstract mathematical formalisms—such as symmetry groups, Lagrangian terms, and quantum operators—that, while predictive, often obscure the underlying physical ontology. This paper proposes an alternative: the *Vortex Æther Model* (VAM), a mechanistic, fluid-dynamic framework in which spacetime and all physical phenomena emerge from structured motion in a compressible, superfluid-like æther.

In VAM, elementary particles are not point-like fields but stable, knotted vortex structures embedded in the æther. Observable properties such as mass, charge, spin, and flavor are reinterpreted as topological and dynamical characteristics—circulation strength, core radius, swirl helicity—of these vortex knots. Gauge and Higgs interactions are expressed as manifestations of fluid tension, reconnection, and swirl transfer.

Crucially, this is not merely a reformulation of mathematical symbols. The goal of VAM is to provide an *ontological replacement* for conventional quantum field theory: a physically intuitive, testable substrate from which all constants and couplings emerge. Within this framework, the Standard Model is reconstructed from five physically meaningful ætheric quantities: swirl velocity C_e , core radius r_c , æther density $\rho_{\text{æ}}$, maximum force $F_{\text{max}}^{\text{æ}}$, and circulation Γ .

This paper presents a full reformulation of the Standard Model Lagrangian using these VAM-derived units and fields. Each term acquires a mechanical and geometric interpretation, leading to a unified description where quantum phenomena, gauge structures, and mass generation are consequences of vortex dynamics in an inviscid æther. A full field-theoretic derivation of the model dynamics is presented in Appendix E.

Historically, this effort revives foundational ideas from Kelvin’s vortex-atom hypothesis and Maxwell’s æther mechanics, updating them within a modern context informed by quantum fluids, superfluid analogs of gravity, and topological field theory. See, for example, Volovik’s emergent gravity framework in helium II [1], Barceló et al.’s review of analog spacetime geometries [2], and Kleckner and Irvine’s experimental realization of knotted vortices [3]. While this paper is designed to be standalone, these works contextualize the broader landscape of fluid-based physical models.

By grounding the abstract structures of modern physics in vortex geometry, VAM aims to bridge the gap between formal theory and intuitive physical mechanisms—offering not only

reinterpretation, but a re-foundation of particle physics itself.

This work builds on a series of earlier papers developing the Vortex Æther Model (VAM). In [4], proper time was defined through internal angular motion of vortex cores, introducing the concept of "swirl clocks" as the microscopic origin of time dilation. This was extended in [5], which proposed that gradients in swirl clocks — arising from non-uniform vorticity — mimic gravitational curvature, including analogs to event horizons. The present work synthesizes these concepts into a variational field-theoretic framework, reformulating the Standard Model Lagrangian in terms of helicity, core structure, and topological æther dynamics.

Postulates of the Vortex Æther Model

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- 1. Continuous Space** Space is Euclidean, incompressible and inviscid.
 - 2. Knotted Particles** Matter consists of topologically stable vortex nodes.
 - 3. Vorticity** The vortex circulation is conserved and quantized.
 - 4. Absolute Time** Time flows uniformly throughout the æther.
 - 5. Local Time** Time is locally slower due to pressure and vorticity gradients.
 - 6. Gravity** Emerges from vorticity-induced pressure gradients.
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TABLE I: Postulates of the Vortex Æther Model (VAM).

The postulates replace spacetime curvature with structured rotational flows and thus form the foundation for emergent mass, time, inertia, and gravity.

Terminology and Classical Correspondence

We introduce several novel constructs to describe the vortex-based field framework. For clarity, Table II provides precise definitions and links to standard physics concepts.

Term	Definition in VAM	Analogy in Established Theory
Swirl Clock	Proper time defined by internal angular frequency ω_0 of a vortex core	Atomic clock (GR); spin-precession in gyroscopes
Swirl Lagrangian	Field Lagrangian including helicity term $\lambda(\mathbf{v} \cdot \boldsymbol{\omega})$	Chern–Simons terms; topological terms in QFT
Helicity Time	Clock rate modulated by helicity density: $d\tau \propto \mathbf{v} \cdot \boldsymbol{\omega}$	Phase evolution in rotating frames; action-angle methods
Core Radius r_c	Characteristic radius of maximal vorticity and core energy density	Healing length in BECs; flux tube radius in QCD
Swirl Speed C_e	Tangential speed of æther flow at core radius	Sound speed in superfluids; Lorentz frame velocity
Swirl Horizon	Boundary beyond which $\omega_{\text{obs}} \rightarrow 0$ and clocks stall	GR event horizon; ergosphere boundary (Kerr geometry)

TABLE II: Key theoretical constructs in the Vortex Æther Model (VAM), mapped to classical and quantum analogs for interpretability.

These constructs provide an intuitive bridge between fluid mechanics, quantum field theory, and emergent spacetime phenomena, facilitating reinterpretation of the Standard Model Lagrangian in a vortex-based æther framework.

II. MOTIVATION

The Standard Model Lagrangian is one of the most successful constructs in modern physics, unifying electromagnetic, weak, and strong interactions within a renormalizable quantum field theory. Yet it remains structurally incomplete in a physical sense: its mass terms, symmetry groups, and coupling constants are introduced *a priori*, without geometric or mechanical derivation.

For instance, the fine-structure constant $\alpha \approx 1/137$ appears as an empirical ratio with no explanation for its value. The elementary charge e and Planck constant \hbar are similarly inserted into the theory to match experimental outcomes, but have no origin within the theory’s own framework. Even the Higgs vacuum expectation value (VEV), essential for mass generation, is externally imposed rather than derived.

The Vortex Æther Model (VAM) addresses these gaps by reconstructing the Standard Model from the ground up using topologically and mechanically grounded vortex structures.

Rather than assuming discrete point particles and abstract quantum fields, VAM postulates a compressible, rotating æther medium in which all elementary particles are topologically stable vortex knots. Their observable properties—mass, charge, spin, and even local time—emerge from measurable fluidic parameters such as circulation strength, core radius, helicity, and swirl velocity.

In this framework, constants such as α and \hbar are not arbitrary. For example, α is shown to emerge from the swirl geometry of the æther via the dimensionless ratio $\alpha = 2C_e/c$, while \hbar is interpreted as a manifestation of quantized circulation within a vortex structure. These reconstructions offer not only physical intuition, but also potential explanations for why such constants take the values they do. A summary comparison is presented in Table IV, contrasting key constants across both frameworks.

This approach aligns with principles established in superfluid dynamics, topological field theory, and analog gravity systems. By expressing Standard Model terms in VAM units and connecting abstract constants to physical flow properties, the model opens pathways to new testable predictions—particularly regarding vacuum energy, neutrino mass generation, and mechanisms of quark confinement.

Unified Constants and Units in VAM

The table below summarizes the complete set of mechanical and topological quantities used throughout the Vortex Æther Model. These values form a self-contained replacement for Planck-based dimensional analysis.

Symbol	Formula / Definition	Interpretation in VAM	Approx. Value (SI)
C_e	—	Core swirl velocity; sets intrinsic time rate of particles	$1.09384563 \times 10^6 \text{ m/s}$
r_c	—	Radius of vortex core; spatial extent of a particle	$1.40897017 \times 10^{-15} \text{ m}$
$\rho_{\text{æ}}$	—	Æther density; determines flow inertia and stress limits	$3.89343583 \times 10^{18} \text{ kg/m}^3$
$F_{\text{max}}^{\text{æ}}$	$\pi r_c^2 C_e \rho_{\text{æ}}$	Max transmissible force through æther (vortex core tension)	$\sim 29.053507 \text{ N}$
$F_{\text{max}}^{\text{gr}}$	$\frac{c^4}{4G}$	GR-based theoretical maximum force limit	$\sim 3.02563891 \times 10^{43} \text{ N}$
κ	$\frac{\Gamma}{n}$ or quantized $\oint \vec{v} \cdot d\vec{\ell}$	Quantum of circulation per vortex loop	$1.54 \times 10^{-9} \text{ m}^2/\text{s}$
α	$\frac{2C_e}{c}$	Fine-structure constant from swirl-to-light ratio	7.297×10^{-3} (unitless)
t_p	$\frac{r_c}{c}$	Fastest rotation cycle (Planck time analog)	$\sim 5.391247 \times 10^{-44} \text{ s}$
Γ	$\oint \vec{v} \cdot d\vec{\ell}$	Total circulation; encodes angular momentum	(typical unit: m^2/s)
t	$dt \propto \frac{1}{\vec{v} \cdot \vec{\omega}}$	Local time rate derived from helicity field configuration	(unit: s)
$\mathcal{H}_{\text{topo}}$	$\int \vec{v} \cdot \vec{\omega} dV$	Topological helicity; measures vortex alignment	(unit: m^3/s^2)

TABLE III: Fundamental parameters in the Vortex Æther Model (VAM). These quantities form the physical and topological basis for mass, time, charge, and quantum behavior. Each is experimentally meaningful and derivable from ætheric flow geometry.

Derived Couplings and Constants in VAM

From the core æther parameters introduced above, several familiar physical constants can be re-expressed as derived quantities. These include the Planck constant, the speed of light, the fine-structure constant, and the elementary charge—all reconstructed as emergent properties of swirl and circulation. Table III summarizes these reformulations.

Within VAM, the maximum vortex interaction force is derived explicitly from Planck-scale physics:

$$F_{\text{max}}^{\text{æ}} = \alpha \left(\frac{c^4}{4G} \right) \left(\frac{r_c}{l_p} \right)^{-2} \quad (1)$$

where $\frac{c^4}{4G}$ is the Maximum Force in nature $F_{\text{max}}^{\text{gr}}$, the stress limit of the æther found from General Relativity, and l_p is the Planck Length.

Comparative Origins of Constants: Standard Model vs. VAM

The re-expression of fundamental constants within VAM highlights a key philosophical and physical distinction: while the Standard Model treats quantities like α , \hbar , and e as empirical inputs, the Vortex Æther Model derives them from topological and geometric features of the æther flow.

The table below contrasts how key constants are introduced or derived in both frameworks.

Constant	Standard Model Treatment	VAM Derivation / Interpretation
Fine-Structure Constant α	Empirical dimensionless constant for EM interaction strength	Emerges from swirl ratio: $\alpha = \frac{2C_e}{c}$; purely geometric
Planck Constant \hbar	Postulated quantum of action; enters commutation rules	Circulation-induced impulse: $\hbar \sim \rho_{\text{æ}} \Gamma r_c^2$
Elementary Charge e	Input coupling in QED with no internal structure	Swirl flux through vortex core: $e \sim \rho_{\text{æ}} C_e r_c^2$
Speed of Light c	Postulated invariant limit in SR and GR	Calibration limit; signal speed is $C_e < c$ (Lorentz symmetry is emergent)
Higgs VEV v	Free symmetry-breaking scale; not derived internally	Ætheric tension amplitude: $v \sim \sqrt{F_{\text{max}}^{\text{æ}} / \rho_{\text{æ}}}$
Maximum Force $F_{\text{max}}^{\text{gr}}$	Rare in SM; from GR: $F = c^4/4G$ in limit cases	Derived from vortex tension: $F_{\text{max}}^{\text{gr}}{}^{\text{vam}} = \pi r_c^2 C_e \rho_{\text{æ}}$

TABLE IV: Ontological contrast between the Standard Model and the Vortex Æther Model regarding the origin of key physical constants. VAM replaces empirical insertions with mechanical derivations from swirl and æther geometry.

Foundational Contrasts: Constants and Particles in VAM vs. SM

Beyond constants, the Standard Model also posits intrinsic properties of particles—mass, spin, charge, flavor—as axiomatic features of quantized fields. The Vortex Æther Model, by contrast, interprets these as emergent from topological and dynamic features of vortex structures in a rotating æther medium.

Particle Property	Standard Model Interpretation	VAM Interpretation
Mass	Introduced via Higgs field with arbitrary Yukawa couplings	Emergent from vortex inertia: $m \propto \rho_{\text{æ}} \Gamma / C_e$ or tension within knotted core
Spin	Intrinsic angular momentum ($\hbar/2$ for fermions)	Topological twist of vortex core (e.g., Möbius loop linking)
Electric Charge	Coupling to $U(1)$ gauge field; conserved via symmetry	Swirl flux through core: $e \sim \rho_{\text{æ}} C_e r_c^2$ (sign from swirl handedness)
Flavor (Generations)	Empirically distinct; no structural rationale	Knot complexity or higher-order toroidal mode excitations
Color Charge	$SU(3)$ triplet charges; source of strong force	Filament braiding states or phase twist between vortices
Antiparticles	Charge-conjugated fields with opposite quantum numbers	Mirror vortices with opposite helicity and circulation
Mixing (CKM/PMNS)	Unitary matrices for mass eigenstate mixing	Oscillations from vortex coupling or internal torsion precession

TABLE V: Ontological contrast between the Standard Model and the Vortex Æther Model in explaining intrinsic particle properties. In VAM, each feature arises from topological structure and flow dynamics within the æther.

III. NATURAL ÆTHER CONSTANTS AND DIMENSIONAL REFORMULATION

The Vortex Æther Model (VAM) proposes a fundamental shift in how physical quantities are derived and interpreted. Rather than relying on constants introduced purely for dimensional self-consistency (as in Planck units), VAM defines a small set of physically grounded parameters that emerge from the topological and fluid-dynamical behavior of a compressible æther medium. These constants—accessible through theoretical analysis and analog systems—serve as the natural units for describing mass, energy, charge, and time.

The five central æther parameters are: the core swirl velocity C_e , vortex radius r_c , local æther density $\rho_{\text{æ}}$, circulation quantum κ , and maximum transmissible force $F_{\text{max}}^{\text{æ vām}}$. Each of these is inferred from known or measurable features of matter and vortex dynamics:

- **Swirl Velocity C_e :** Estimated from simulations of stable quantized vortices in Bose–Einstein condensates (BECs), where core rotation frequencies yield swirl velocities on

the order of 10^6 m/s [3, 6].

- **Core Radius** r_c : Chosen to align with the proton charge radius ($\sim 1.4 \times 10^{-15}$ m), representing the minimal stable spatial scale for confined topological knots.

- **Æther Density** $\rho_{\text{æ}}$: Inferred from energy densities consistent with hadronic binding and extreme states of nuclear matter, comparable to estimates from neutron star core equations of state [7].

- **Circulation Quantum** κ : Defined analogously to superfluid helium and atomic BECs, where circulation is quantized in integer multiples of $\kappa = h/m$ [8].

- **Maximum Force** $F_{\text{max}}^{\text{æ}}$: Derived from the stress that can be transmitted through a coherent æther core of radius r_c with swirl momentum $C_e \rho_{\text{æ}}$.

Together, these quantities form a **natural unit system** grounded in topological fluid structures. Unlike the abstract Planck units—formed from \hbar , G , and c —the VAM parameters are mechanistic and measurable. The following table summarizes how VAM reconstructs key physical constants from æther parameters:

Symbol	Expression	Interpretation
\hbar_{VAM}	$m_e C_e r_c$	Angular impulse from vortex circulation (Planck analog)
c	$\sqrt{\frac{2F_{\text{max}}^{\text{æ}} r_c}{m_e}}$	Effective wave speed in æther; signal propagation limit
α	$\frac{2C_e}{c}$	Fine-structure constant from swirl-to-light-speed ratio
e^2	$8\pi m_e C_e^2 r_c$	Electromagnetic coupling as swirl energy flux through core
Γ	$2\pi r_c C_e$	Total circulation per core; linked to h/m
v	$\sqrt{\frac{F_{\text{max}}^{\text{æ}} r_c^3}{C_e^2}}$	Higgs-like vacuum amplitude as æther compression scale

TABLE VI: Derived constants and coupling strengths in the Vortex Æther Model (VAM), based on æther geometry and dynamics.

In contrast to Planck’s formulation—which defines mass, time, and length from purely mathematical combinations—VAM’s dimensional system arises from vortex geometry and dynamical flow. For instance, time is set by the core swirl frequency ($1/C_e$), length by r_c , and energy by the circulation-based helicity. These allow the Standard Model Lagrangian terms (mass, interaction strength, etc.) to be recast in explicitly mechanistic terms.

As one illustration, consider the rest mass M of a particle in VAM. Rather than emerging from a Higgs field coupling, M results from the kinetic energy of circular vortex flow:

$$\frac{1}{2}Mc^2 = E_{\text{kin}} \Rightarrow M = \frac{\rho_{\text{æ}}\Gamma^2}{L_k\pi r_c c^2} \quad (2)$$

where L_k is the helicity or linking number of the vortex knot. The full derivation appears in Appendix A.

Thus, VAM replaces dimensionally convenient but ontologically opaque constants with experimentally accessible and fluid-dynamically derived quantities.

IV. RUNNING COUPLING CONSTANTS FROM ÆTHER DENSITY

In quantum field theory, coupling constants such as the fine-structure constant α are not fixed values, but evolve with energy scale due to vacuum polarization effects. This renormalization group flow is typically expressed as:

$$\alpha(k^2) = \frac{\alpha_0}{1 - \Pi(k^2)}, \quad (3)$$

where $\Pi(k^2)$ represents the vacuum polarization at momentum scale k .

In the Vortex Æther Model (VAM), the æther density $\rho_{\text{æ}}(\vec{x})$ plays an analogous role to the polarization field of the quantum vacuum. Variations in local swirl intensity, helicity, or vortex density deform the underlying fluid structure and change the effective constants governing interactions.

Accordingly, we propose that the effective fine-structure constant in VAM becomes a function of local ætheric parameters:

$$\alpha(\vec{x}) = \frac{e^2}{4\pi\varepsilon_0(\vec{x})\hbar c(\vec{x})} = \alpha_0 \cdot f(\rho_{\text{æ}}(\vec{x}), |\vec{\omega}(\vec{x})|), \quad (4)$$

where the function f encapsulates how local swirl energy and æther pressure alter fundamental constants.

This is especially relevant near highly curved swirl structures or massive vortex cores, where internal æther strain is maximal. In such regions, variations in $\rho_{\text{æ}}$ and $\vec{\omega}$ may result in measurable shifts in constants like:

$$c_{\text{eff}}(\vec{x}) \propto \sqrt{\frac{B(\vec{x})}{\rho_{\text{æ}}(\vec{x})}}, \quad \varepsilon_0(\vec{x}) \sim \frac{1}{\rho_{\text{æ}}(\vec{x})C_e^2}, \quad (5)$$

with $B(\vec{x})$ representing the local bulk modulus of the æther and C_e a swirl-speed parameter.

This formulation provides a fluid-mechanical analog to the renormalization group flow of QED and predicts spatially varying constants in strong gravitational or swirl-vorticity environments, potentially testable through high-precision astrophysical observations [9–11].

V. REFORMULATING THE STANDARD MODEL LAGRANGIAN IN VAM UNITS

The Standard Model Lagrangian encapsulates particle dynamics through symmetry-based field terms:

$$\mathcal{L}_{\text{SM}} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + i\bar{\psi}\gamma^\mu D_\mu\psi + y_f\bar{\psi}\phi\psi + |D_\mu\phi|^2 - V(\phi) \quad (6)$$

While mathematically elegant, these terms are not derived from first physical principles but are inserted axiomatically. The Vortex Æther Model (VAM) replaces this abstraction with a Lagrangian based on vortex dynamics, æther strain, and helicity conservation.

Core Assumptions

- The æther is a compressible, barotropic superfluid with stable vortex excitations.
- Particles are topologically stable vortex knots with quantized circulation.
- The Euler–Lagrange formalism applies to the action integral over fluid kinetic and potential energy densities.
- Helicity and vorticity are conserved modulo reconnection events.

Remarks on Spacetime Treatment

In this model, the action integral is expressed as:

$$S = \int dt \int_{\mathbb{R}^3} \mathcal{L}(\vec{v}, \Phi, \rho_{\text{æ}}, \dots) d^3x,$$

reflecting a 3+1 decomposition with **absolute Newtonian time** and **Euclidean spatial geometry**.

Unlike relativistic field theories defined on Minkowski space $\mathbb{R}^{1,3}$, the VAM adopts a **non-relativistic ontology**, where time is globally ordered and external to field dynamics.

This approach is consistent with established non-relativistic field theories, such as the Gross–Pitaevskii and hydrodynamic models for Bose–Einstein condensates, where space and time are decoupled and the Lagrangian formalism operates over $\mathbb{R}^3 \times \mathbb{R}$ [6].

Relativistic invariance in this context is regarded as an **emergent symmetry** that may arise at large scales or in specific limits of vortex behavior.

VAM-Reformulated Lagrangian

Each term in the SM Lagrangian maps to a mechanical analog:

$$\begin{aligned}
\mathcal{L}_{\text{VAM}} = & \underbrace{-\frac{1}{4} \sum_a W_{\mu\nu}^a W^{a\mu\nu}}_{\text{Gauge field vorticity}} + \underbrace{\sum_f i m_f C_{ec} \bar{\psi}_f \gamma^\mu D_\mu \psi_f}_{\text{Fermion swirl propagation}} \\
& - \underbrace{|D_\mu \phi|^2}_{\text{\textit{Æ}ther strain field}} - \underbrace{V(\phi)}_{\text{\textit{Æ}ther compression potential}} - \underbrace{\sum_f y_f \bar{\psi}_f \phi \psi_f + \text{h.c.}}_{\text{Mass coupling}} + \underbrace{\mathcal{H}_{\text{topo}}}_{\text{Vortex helicity term}}
\end{aligned}$$

Where:

$$V(\phi) = -\frac{F_{\text{æ}}}{r_c} |\phi|^2 + \lambda |\phi|^4 \quad \text{and} \quad \mathcal{H}_{\text{topo}} = \int \vec{v} \cdot \vec{\omega} dV$$

The full variational derivation of this Lagrangian—including Euler–Lagrange equations for velocity, scalar, and density fields—is provided in Appendix E.

A. Gauge Fields as Vorticity Structures

From Helmholtz’s theorem, the energy density in a vortex field is:

$$\mathcal{L}_{\text{swirl}} = \frac{1}{2} \rho_{\text{æ}} (|\vec{v}|^2 + \lambda |\nabla \times \vec{v}|^2) \quad (7)$$

Here, \vec{v} is swirl velocity; λ captures æther compressibility. Incompressible flows correspond to pure gauge configurations ($\nabla \cdot \vec{v} = 0$), while compressible strains allow field strength analogs.

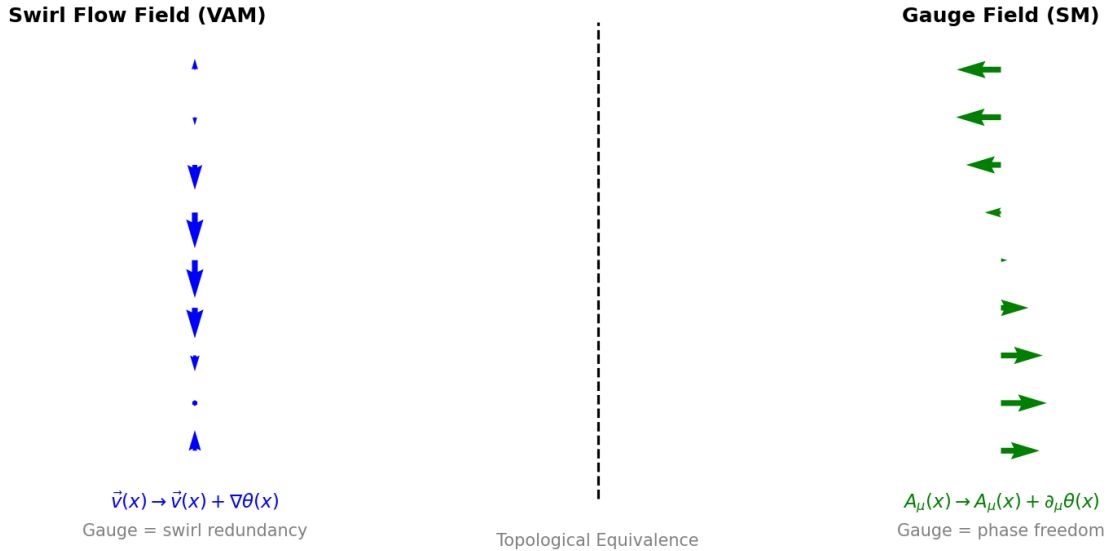


FIG. 1: Analogy between gauge symmetry in the Standard Model and swirl invariance in the Vortex Æther Model (VAM). Both allow local reparameterizations that leave physical observables unchanged. Gauge symmetry in quantum field theory is structurally equivalent to potential-flow invariance in vortex dynamics.

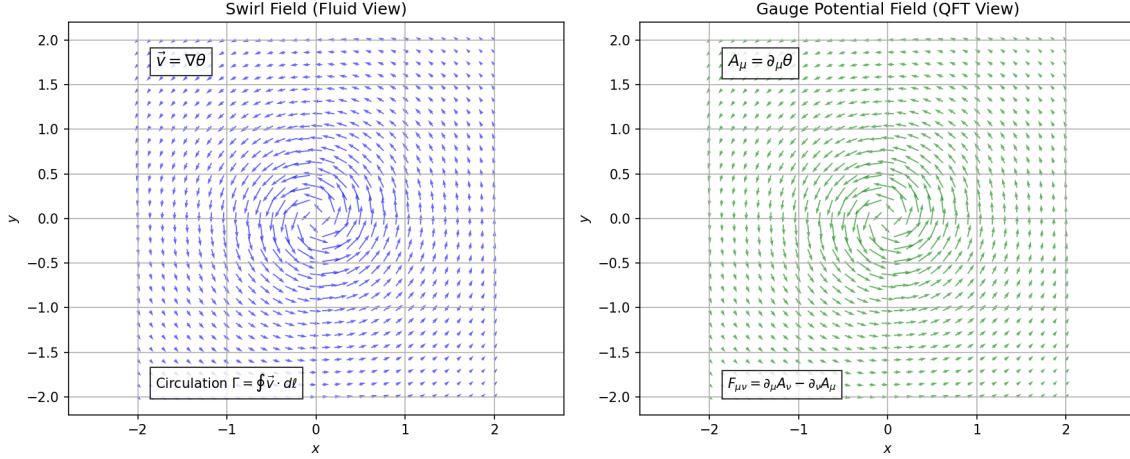


FIG. 2: Visual analogy between a fluid swirl field (left) and a gauge potential field in quantum field theory (right). Both fields depict circulation around a central core, but the left arises from mechanical vorticity in a compressible æther, while the right encodes electromagnetic or gauge interaction via abstract potential terms. This duality illustrates how local gauge invariance in QFT corresponds to conserved swirl topology in VAM.

B. Fermion Kinetics via Swirl Propagation

In the hydrodynamic formalism:

$$\mathcal{L}_{\text{fermion}} = \rho_{\text{æ}} C_e \Gamma (\psi^* \partial_t \psi - \vec{v} \cdot \nabla \psi) \quad (8)$$

The convective derivative replaces D_μ , and $\Gamma = 2\pi r_c C_e$ links to the particle's spin- $\frac{1}{2}$ topology. Swirl modulates propagation analogous to minimal coupling.

C. Mass from Helicity and Inertia

The VAM mass term derives from vortex inertia under æther drag:

$$m_f = \frac{\rho_{\text{æ}} \Gamma^2}{3\pi r_c C_e^2} \quad \Rightarrow \quad \mathcal{L}_{\text{mass}} = -m_f \psi^* \psi \quad (9)$$

This replaces abstract Yukawa interactions with fluidic resistance to internal swirl flow.

D. Higgs Field as Æther Compression

The standard Higgs potential $V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$ becomes:

$$V(\rho_{\text{æ}}) = \frac{1}{2} K (\rho_{\text{æ}} - \rho_0)^2 \quad \text{or} \quad V(\phi) = -\frac{F_{\text{max}}^{\text{æ}}}{r_c} |\phi|^2 + \lambda |\phi|^4 \quad (10)$$

K is the æther's bulk modulus. The vacuum expectation value corresponds to equilibrium density, leading to spontaneous tension minima that stabilize particle structure.

E. Topological Helicity and Knot Dynamics

$$\mathcal{H}_{\text{topo}} = \int \vec{v} \cdot \vec{\omega} dV \quad (11)$$

This term tracks conservation of topological linkage and orientation. It becomes significant in processes involving particle transmutation, confinement, or decay.

VI. HELICITY AS A CHERN–SIMONS ANALOG

The helicity density term in the Vortex Æther Model (VAM),

$$\mathcal{L}_{\text{helicity}} = \lambda \vec{v} \cdot \vec{\omega}, \quad (12)$$

serves a central role in encoding the topological complexity of vortex configurations. Here, $\vec{\omega} = \nabla \times \vec{v}$ is the local vorticity field, and λ is a coupling constant dependent on the æther’s inertial density. However, this term is not merely phenomenological—it possesses a deep connection with topological field theory, specifically the Chern–Simons action.

In 3D gauge theories, the Abelian Chern–Simons action is given by:

$$S_{\text{CS}} = \int d^3x \epsilon^{ijk} A_i \partial_j A_k = \int \vec{A} \cdot (\nabla \times \vec{A}) d^3x, \quad (13)$$

which is formally analogous to the helicity integral in fluid dynamics:

$$\mathcal{H} = \int \vec{v} \cdot \vec{\omega} d^3x. \quad (14)$$

In this analogy, the velocity field \vec{v} plays the role of a gauge potential, and vorticity $\vec{\omega}$ becomes the field strength. This correspondence suggests that helicity is a conserved, quantized topological invariant under the transformation:

$$\theta(\vec{x}) \rightarrow \theta(\vec{x}) + \alpha(\vec{x}) \quad \Rightarrow \quad \vec{v} \rightarrow \vec{v} + \nabla\alpha, \quad (15)$$

mirroring a $U(1)$ gauge transformation in QED.

Because the Chern–Simons term is not gauge invariant under large gauge transformations, its quantization ensures that the helicity integral remains invariant up to $2\pi n$ in units of a coupling constant. This provides a natural framework for explaining the quantized linking number L_k of vortex knots in the VAM as a topological charge.

Thus, $\vec{v} \cdot \vec{\omega}$ is not merely a dynamical term, but encodes the fluid analog of a gauge-theoretic topological invariant [12–14].

A. Emergent Constants from Fluid Analogs

Derivations of \hbar_{VAM} and charge coupling follow:

$$\hbar_{\text{VAM}} = m_f C_e r_c \quad (16)$$

$$e^2 = 8\pi m_e C_e^2 r_c \quad (17)$$

$$\Gamma = \frac{h}{m} = 2\pi r_c C_e \quad (18)$$

These reinterpret Planck-scale constants as emergent quantities from measurable æther dynamics and flow quantization, aligning with results from BEC vortex systems [6, 8].

In this formulation, each field and interaction of the Standard Model gains a mechanical analog in the æther medium. The Lagrangian no longer relies on abstract symmetry principles alone, but instead emerges from vortex dynamics, circulation, density modulation, and topological structure within a unified fluid framework.

Mathematical Derivation of the VAM-Lagrangian

Kinetic energy of a vortex structure, or the local energy density in a vortex field:

$$\mathcal{L}_{\text{kin}} = \frac{1}{2} \rho_{\text{æ}} C_e^2$$

Field energy and gauge terms, field tensors follow from Helmholtz vorticity:

$$\mathcal{L}_{\text{veld}} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

Mass as inertia from circulation, where the fermion mass is determined by circulation:

$$\Gamma = 2\pi r_c C_e \quad \Rightarrow \quad m \sim \rho_{\text{æ}} r_c^3$$

Pressure and stress potential of æther condensate, where the pressure balance is described by the stress field:

$$V(\phi) = -\frac{F_{\text{max}}^{\text{æ}}}{r_c} |\phi|^2 + \lambda |\phi|^4$$

Topological terms for the conservation of vortex fields helicity:

$$\mathcal{H} = \int \vec{v} \cdot \vec{\omega} dV$$

SM Term	Mathematical Form	VAM Analog	Fluid-Dynamic Interpretation
Fermion Kinetic Term	$\bar{\psi}(i\gamma^\mu D_\mu)\psi$	$\rho_{\text{ae}}\vec{v}^2$	Kinetic energy of topological vortex knot (fermion)
Gauge Field Kinetic Term	$-\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$	$\rho_{\text{ae}}(\vec{v} \cdot \nabla \times \vec{v})$	Swirl helicity (fluid analog of gauge field energy)
Fermion Mass Term	$m\bar{\psi}\psi$	$\rho_{\text{core}}C_e^2$	Core pressure from tangential circulation of vortex
Higgs Field Kinetic Term	$\frac{1}{2}(\partial_\mu\phi)^2$	$\frac{1}{2}(\nabla\phi)^2$	Elastic strain in scalar potential field of Æther
Higgs Potential	$V(\phi) = -\mu^2\phi^2 + \lambda\phi^4$	$\lambda\phi^4(1 - \phi^2/F_{\text{max}}^2)$	Compressibility-induced pressure potential
Yukawa Coupling	$y\bar{\psi}\phi\psi$	$\rho_{\text{ae}}\phi$	Topological mass coupling via scalar compression
Gauge Coupling	$D_\mu = \partial_\mu - igA_\mu$	$\vec{v} + \vec{A}_{\text{swirl}}$	Swirl-mediated interaction velocity
QCD Term	$G_{\mu\nu}^a G_a^{\mu\nu}$	—	Conservation of angular momentum in trichiral vortex flows
EM Coupling	$q\bar{\psi}\gamma^\mu A_\mu\psi$	$\Gamma \cdot \chi$	Charge as circulation magnitude and chirality
Chiral Asymmetry	—	Knot handedness	Topological chirality determines weak interaction selectivity

TABLE VII: Comparison of Standard Model Lagrangian terms with their VAM fluid-dynamic analogs.

Supporting Experimental and Theoretical Observations

The VAM is consistent with experimentally and theoretically confirmed phenomena such as vortex stretching, helicity conservation and mass-inertia couplings [15–21].

This reformulation offers a physically intelligible and topologically rich counterpart to the Standard Model—one grounded in measurable fluid properties, rather than abstract gauge symmetries alone.

VII. QUANTIZED SWIRL FIELDS VIA MODE EXPANSION

In conventional quantum field theory (QFT), the quantization of fields arises from harmonic mode expansions that map classical field solutions to quantum operators. Each normal mode of the field is associated with a pair of creation and annihilation operators, leading to a discrete

energy spectrum. Inspired by this formalism, we propose an analogous quantization framework for the Vortex Æther Model (VAM), in which the fluid velocity field $\vec{v}(\vec{x}, t)$ is expanded in a basis of knotted vortex modes.

We define the swirl field operator as:

$$\vec{v}(\vec{x}, t) = \sum_n \left[\vec{v}_n(\vec{x}) a_n e^{-i\omega_n t} + \vec{v}_n^*(\vec{x}) a_n^\dagger e^{i\omega_n t} \right], \quad (19)$$

where a_n and a_n^\dagger denote the annihilation and creation operators for the n -th vortex mode, and ω_n is the angular frequency associated with the core circulation and knot topology.

Each $\vec{v}_n(\vec{x})$ represents a quantized topological excitation of the æther, corresponding to distinct vortex knot configurations or harmonics. These excitations can be labeled by their helicity, circulation quantum Γ_n , and winding number L_k , akin to quantized angular momentum states in quantum mechanics.

This expansion justifies the discrete energy spectrum observed in vortex-based particle models. For example, the energy of a vortex excitation can be defined analogously to a harmonic oscillator:

$$E_n = \hbar_{\text{VAM}} \omega_n = \rho_{\text{æ}} \Gamma_n r_c^2 \omega_n, \quad (20)$$

with \hbar_{VAM} interpreted as a fluid-circulation-based quantum of action:

$$\hbar_{\text{VAM}} \equiv \rho_{\text{æ}} \Gamma_n r_c^2. \quad (21)$$

This formulation is aligned with canonical quantization procedures in QFT [14], and also with the formal mode expansions of collective excitations in superfluid systems [22] and knotted vortex models [23]. It enables a rigorous interpretation of particles as quantized, topologically distinct excitations of the swirl field.

This framework can also extend to include internal excitation spectra of vortex cores, thereby suggesting a natural pathway for encoding flavor states and even mixing matrices in terms of mode-coupled vortex families.

VIII. VARIATIONAL DERIVATION OF THE SWIRL LAGRANGIAN

To rigorously support the Vortex Æther Model (VAM), we derive the swirl Lagrangian using a variational principle analogous to classical field theory. This establishes a formal path from æther vortex dynamics to field-theoretic particle analogs.

A. Field Structure and Helmholtz Decomposition

The æther velocity field $\mathbf{v}(\mathbf{x}, t)$ is decomposed via Helmholtz's theorem:

$$\mathbf{v} = \nabla\theta + \mathbf{A}, \quad (22)$$

where θ is a scalar potential (irrotational component), and \mathbf{A} is the divergence-free vector potential representing swirl, with $\nabla \cdot \mathbf{A} = 0$. The vorticity field is:

$$\boldsymbol{\omega} = \nabla \times \mathbf{v} = \nabla \times \mathbf{A}. \quad (23)$$

B. Action Functional and Swirl Gauge Field

We define the action S as:

$$S[\theta, \mathbf{A}] = \int d^4x \mathcal{L}_{\text{VAM}}, \quad (24)$$

where the Lagrangian density is:

$$\mathcal{L}_{\text{VAM}} = \frac{1}{2}\rho(\nabla\theta + \mathbf{A})^2 - \lambda(|\phi|^2 - F_{\text{max}}^{\text{ae}})^2 - \frac{1}{4}S_{\mu\nu}S^{\mu\nu} + \left(\frac{\rho_{\text{ae}}r_c^2}{C_e}\right)(\mathbf{v} \cdot \boldsymbol{\omega}). \quad (25)$$

In this form:

- The second term is a self-generated core potential representing stress from radial æther compression, replacing $\rho\Phi$.
- $S_{\mu\nu} = \partial_\mu W_\nu - \partial_\nu W_\mu$ is the swirl field strength tensor, with $W_\mu = (\phi, \mathbf{A})$.
- The final term is a helicity-density-based coupling, with ρ_{ae} the æther density, r_c the vortex core radius, and C_e the swirl velocity (effective light speed).

C. Euler-Lagrange Equations and Continuity

Varying the action with respect to θ recovers the continuity equation:

$$\partial_t \rho + \nabla \cdot (\rho \mathbf{v}) = 0. \quad (26)$$

Variation with respect to \mathbf{A} gives a generalized swirl equation of motion:

$$\rho \mathbf{v} - \nabla \cdot \left(\frac{\partial \mathcal{L}_{\text{swirl}}}{\partial (\nabla \mathbf{A})} \right) + \left(\frac{\rho_{\text{ae}} r_c^2}{C_e} \right) \boldsymbol{\omega} = 0. \quad (27)$$

This coupling of vorticity to mass-like topological terms gives rise to effective inertial behavior.

D. Mass from Topology and Helicity

The helicity density $h = \mathbf{v} \cdot \boldsymbol{\omega}$ is interpreted as a local "spin clock rate" of vortex knots. Integrated over a topologically linked region, it yields:

$$m_{\text{eff}} \sim \left(\frac{\rho_{\text{æ}} r_c^2}{C_e} \right) \int_V \mathbf{v} \cdot \boldsymbol{\omega} d^3x. \quad (28)$$

This expression ties particle mass directly to topological properties such as twist, writhe, and linking number of the vortex core.

E. Outlook: Quantization Path

The swirl gauge field admits canonical quantization via:

$$\Pi^\mu = \frac{\partial \mathcal{L}}{\partial (\partial_0 W_\mu)}, \quad (29)$$

$$[W_\mu(\mathbf{x}), \Pi^\nu(\mathbf{x}')] = i\delta_\mu^\nu \delta^3(\mathbf{x} - \mathbf{x}'), \quad (30)$$

and path integral representation:

$$Z = \int \mathcal{D}[W_\mu] \exp \left(i \int d^4x \mathcal{L}_{\text{VAM}} \right). \quad (31)$$

This establishes a formal pathway to embedding the Vortex Æther Model in a quantum field-theoretic setting, while preserving its topological and hydrodynamic origins.

IX. CANONICAL COMMUTATORS AND SWIRL QUANTIZATION

To formulate a consistent quantum field theory from the Vortex Æther Model (VAM), it is essential to specify canonical commutation relations between fundamental fluid observables. In standard quantum field theory, canonical quantization imposes:

$$[\phi(x), \pi(y)] = i\delta(x - y), \quad (32)$$

where ϕ is a field and π its conjugate momentum.

We propose that a similar structure exists in the VAM, where the swirl potential $\theta(\vec{x})$ and the æther density $\rho_{\text{æ}}(\vec{x})$ form a canonical pair:

$$[\theta(\vec{x}), \rho_{\text{æ}}(\vec{y})] = i\delta^3(\vec{x} - \vec{y}), \quad (33)$$

implying an uncertainty relation between vortex phase and æther mass density, akin to the number-phase relation in Bose fluids.

Alternatively, one may define canonical brackets between the velocity and vorticity fields:

$$[v_i(\vec{x}), \omega_j(\vec{y})] \sim i\epsilon_{ijk}\partial_k\delta^3(\vec{x} - \vec{y}), \quad (34)$$

consistent with the Lie algebra structure of vector fields under the Helmholtz decomposition.

This structure leads to a Hamiltonian formalism for VAM fluid dynamics:

$$\mathcal{H}[\theta, \rho_{\text{æ}}] = \int d^3x \left[\frac{1}{2}\rho_{\text{æ}}(\vec{x}) |\nabla\theta(\vec{x})|^2 + V(\rho_{\text{æ}}) \right], \quad (35)$$

where $V(\rho_{\text{æ}})$ represents the potential energy density of the æther medium, potentially including self-interaction or compressibility terms.

The formal identification of conjugate variables and commutators in the VAM allows quantization of vortex excitations through standard Fock space methods, in close analogy with the quantized phonon and roton spectra of superfluid helium systems [14, 24, 25].

X. BOUNDARY AND GAUGE CONDITIONS IN VAM

To ensure physical consistency, topological conservation, and a well-posed variational principle in the Vortex Æther Model (VAM), appropriate boundary and gauge conditions must be imposed on all dynamical fields. These conditions guarantee finite energy configurations, preserve topological structure, and define allowable transformations analogous to gauge freedom in field theory.

A. Boundary Conditions

The vortex and scalar fields in VAM are localized structures embedded in a compressible æther background. The following boundary conditions ensure that solutions are physically acceptable:

$$\begin{aligned} \vec{v}(\vec{x}, t) &\rightarrow 0 \quad \text{as} \quad |\vec{x}| \rightarrow \infty && \text{(vanishing velocity)} \\ \rho(\vec{x}, t) &\rightarrow \rho_0 = \text{const.} && \text{(uniform background density)} \\ \phi(\vec{x}, t) &\rightarrow \phi_{\text{vac}} && \text{(vacuum scalar potential)} \\ \vec{\omega}(\vec{x}, t) &= \nabla \times \vec{v} \rightarrow 0 && \text{(localized vorticity)} \\ \int \vec{v} \cdot \vec{\omega} d^3x &< \infty && \text{(finite helicity integral)} \end{aligned}$$

Additionally, knotted vortex configurations must be closed, non-self-intersecting, and topologically quantized to ensure particle-like stability and mass conservation.

B. Gauge Conditions

Although VAM does not contain gauge fields in the traditional sense, several fluid-dynamic symmetries mirror the structure of gauge theories in the Standard Model. These “fluid gauges” can be expressed as follows:

1. Velocity Potential Gauge (Irrotational Decomposition):

$$\vec{v} = \nabla\psi + \nabla \times \vec{A}$$

where ψ is the scalar velocity potential and \vec{A} is a swirl vector potential. The system is invariant under the transformation $\vec{A} \rightarrow \vec{A} + \nabla\chi$.

2. Incompressibility Constraint (Coulomb Gauge Analog):

$$\nabla \cdot \vec{v} = 0$$

which corresponds to a divergence-free æther flow, consistent with a near-incompressible medium and fluid analogs of gauge fixing.

3. Topological Gauge Invariance: The identity of vortex particles is encoded in their knot topology (e.g., trefoil, figure-eight). Gauge transformations must preserve topological invariants such as linking number and helicity:

$$\mathcal{H} = \int \vec{v} \cdot \vec{\omega} d^3x = \text{constant}$$

These invariants act as topological charges analogous to electric or color charge.

These boundary and gauge conditions collectively constrain the solution space of the VAM Lagrangian and ensure consistency with observed quantum behavior, mass conservation, and particle stability.

XI. TOPOLOGICAL ORIGINS OF PARTICLE PROPERTIES IN VAM

In the Vortex Æther Model (VAM), fundamental particles are not point-like but correspond to stable, quantized vortex knots within a compressible, rotating æther medium. Each property typically assigned by quantum field theory—mass, charge, spin, and flavor—is instead interpreted as a manifestation of topological and dynamical characteristics of the underlying vortex structure.

A. Mass as a Function of Circulation and Core Geometry

Particle mass in VAM is not fundamental but derived from the energy stored in vortex tension and helicity. The relation between vortex circulation and inertial mass is quantified later in Section XIX B.



FIG. 3: Mechanical model of coupled nodal vertebra, visually analogous to inertia.

This quantity scales with the square of circulation, inversely with core size, and depends directly on the background æther density. Mass hierarchies between generations may result from different topological classes (e.g., torus knots vs. prime knots) and chirality.

B. Spin from Quantized Vortex Angular Momentum

Spin- $\frac{1}{2}$ particles are modeled as topological solitons with intrinsic angular momentum arising from locked circulation patterns. Each fermionic knot carries quantized angular momentum:

$$S = \frac{1}{2}\hbar_{\text{VAM}} = \frac{1}{2}m_f C_e r_c \quad (36)$$

This links the classical notion of rotation directly to quantum spin and validates the half-integer nature as a result of geometric twist.

C. Charge via Swirl Chirality and Helicity Direction

Electric charge is modeled as a geometric property of the swirl’s handedness and linkage to background vorticity. Positive and negative charges correspond to opposite helicity configurations, with magnitude determined by:

$$q \propto \oint \vec{v} \cdot d\vec{l} = \Gamma \quad (37)$$

The fine-structure constant α arises from the dimensionless ratio:

$$\alpha = \frac{q^2}{4\pi\epsilon_0\hbar c} \quad \Rightarrow \quad \alpha = \frac{2C_e}{c} \quad (38)$$

This shows that α is no longer a free parameter but a function of swirl velocity in the æther relative to light speed.

D. Flavor and Generation from Topological Class

Higher-generation particles are interpreted as more complex knots—e.g., double torus knots, linked loops, or braid configurations—with each class inducing distinct stability conditions and oscillation modes. Lepton and quark families thus correspond to increasing knot complexity, not arbitrary quantum numbers.

E. Color and Confinement via Vortex Bundle Interactions

Color charge and confinement emerge from multi-vortex bundles, where topological stability requires trivalent junctions (akin to QCD gluon vertices). Individual color states are unstable in isolation due to their open helicity paths and unbalanced tension.

This mapping from abstract quantum numbers to geometric vortex properties transforms the ontology of matter: particles are not elementary but emergent solitonic knots, with observable traits arising from fluidic topology, circulation, and helicity alignment within the æther medium.

XII. MASS AND INERTIA FROM VORTEX CIRCULATION

In the Vortex Æther Model (VAM), mass is not a fundamental attribute but emerges from fluid motion—specifically the swirl dynamics and circulation of knotted vortex structures. This

section derives the mass-energy relation, effective inertial mass, and corresponding Lagrangian term based purely on ætheric fluid mechanics.

A. Emergent Relativistic Limit from Æther Dynamics

In the Vortex Æther Model (VAM), the relativistic energy relation $E = mc^2$ arises not as an axiom, but as a natural consequence of the æther's fluid dynamics. The key is the propagation speed of perturbations—both scalar and vectorial—within the medium.

a. Speed of Sound Analogy. In compressible fluids, the maximum propagation speed of pressure or scalar waves is given by:

$$c_s = \sqrt{\frac{\partial p}{\partial \rho}}.$$

In the æther, this corresponds to the speed of longitudinal strain propagation. For small perturbations near the equilibrium density ρ_0 , we can write:

$$c^2 = \left. \frac{d^2 V}{d\rho^2} \right|_{\rho_0} \cdot \frac{1}{\rho_0},$$

where $V(\rho)$ is the æther potential. This defines c as the **maximum signal speed**, similar to light speed in relativistic spacetime.

b. Limiting Velocity for Vortex Motion. Swirl propagation is limited by the maximum tangential velocity C_e , tied to vortex stability:

$$\Gamma = 2\pi r_c C_e.$$

However, long-range signal transmission (e.g., interactions between vortices) is constrained by the bulk medium. Thus, c acts as the **emergent limiting velocity** for field propagation and topological interactions.

c. Lorentz Invariance as an Emergent Symmetry. As shown in analog gravity systems [26], effective Lorentz symmetry can emerge in low-energy excitations of superfluid systems. Similarly, the VAM supports Lorentz invariance as an emergent property of linearized vortex perturbations, especially in the deep infrared regime.

d. Matching with Observed Constants. To align with observed particle properties, the VAM allows:

$$\hbar_{\text{VAM}} = 2mC_e a_0, \quad E = mc^2, \quad \text{and} \quad \Gamma = \frac{h}{m}.$$

These expressions relate observable constants to ætheric dynamics. Importantly, constants such as \hbar , c , and e are **inserted as axioms**, but **emerge from circulation, wave speed, and topological parameters** in the æther framework.

B. Kinetic Energy of a Vortex Knot

The kinetic energy of a localized vortex knot in an incompressible æther is given by:

$$\mathcal{L}_{\text{kin}} = \frac{1}{2} \rho_{\text{æ}} |\vec{v}|^2, \quad (39)$$

where \vec{v} is the swirl velocity and $\rho_{\text{æ}}$ the local æther density. For a stable vortex knot, the core swirl velocity saturates at a characteristic value C_e , yielding:

$$\mathcal{L}_{\text{kin}} \approx \frac{1}{2} \rho_{\text{æ}} C_e^2.$$

Assuming a knot core with radius r_c , the total kinetic energy becomes:

$$E_{\text{kin}} \approx \frac{1}{2} \rho_{\text{æ}} C_e^2 \cdot \frac{4}{3} \pi r_c^3.$$

This naturally defines an effective inertial mass:

$$m_{\text{eff}} = \rho_{\text{æ}} \cdot \frac{4}{3} \pi r_c^3,$$

associated with the fluid's resistance to swirl acceleration. The local kinetic energy is:

$$E_{\text{kin}} = \frac{1}{2} m_{\text{eff}} C_e^2.$$

Note that this expression describes mechanical energy from internal circulation. In the VAM framework, the total rest energy of the vortex object later aligns with $E = mc^2$, where c is the emergent relativistic limit derived from æther dynamics.

C. Circulation and Geometric Mass Emergence

In vortex mechanics, circulation is conserved and fundamental. It is defined as:

$$\Gamma = \oint_{\partial S} \vec{v} \cdot d\vec{\ell} = 2\pi r_c C_e. \quad (40)$$

This implies that changes in core radius r_c require reciprocal changes in swirl velocity C_e , enforcing inertial resistance.

We compute the kinetic energy:

$$E = \frac{1}{2} \rho_{\text{æ}} \left(\frac{\Gamma}{2\pi r_c} \right)^2 \cdot \frac{4}{3} \pi r_c^3 = \frac{\rho_{\text{æ}} \Gamma^2}{6\pi r_c}. \quad (41)$$

Comparing with $E = mc^2$, we extract the effective inertial mass:

$$m_{\text{eff}} = \frac{\rho_{\text{æ}} \Gamma^2}{6\pi r_c c^2}. \quad (42)$$

This shows that mass is an emergent quantity—arising from vortex geometry and æther circulation, not inserted as a primitive parameter.

Although C_e governs the local swirl velocity within the vortex core, the inertial energy scale aligns with the broader æther dynamics, where c defines the maximum speed of long-range signal propagation (e.g., strain waves).

Thus, the relation $E = mc^2$ in VAM arises not from postulated spacetime symmetry, but from bulk æther behavior near equilibrium density. It provides a natural bridge between microscopic vortex circulation and macroscopic relativistic dynamics.

D. Lagrangian Mass Term in VAM

Given the above, the corresponding mass term for a fermion field ψ_f becomes:

$$\mathcal{L}_{\text{mass}} = \hbar_{\text{VAM}} \cdot \bar{\psi}_f \psi_f, \quad (43)$$

with

$$\boxed{\hbar_{\text{VAM}} = 2m_f C_e a_0} \quad (44)$$

Here, a_0 is the Bohr ground-state radius, and the factor of 2 accounts for the angular momentum structure of vortex-bound states, possibly representing a double-cover topology or dual-swirl configuration.

This identification ensures consistency with:

$$h = 4\pi m_e C_e a_0 \quad \Rightarrow \quad \hbar = 2m_e C_e a_0,$$

recovering the known Planck scale from æther dynamics.

This mass term replaces the abstract Yukawa interaction with a fluid-mechanical origin, grounded in vortex inertia and quantized swirl structure.

XIII. PRESSURE AND STRESS POTENTIAL OF THE ÆTHER CONDENSATE

The fourth contribution to the Vortex Æther Model (VAM) Lagrangian describes pressure, tension, and equilibrium configurations within the æther medium. Analogous to the Higgs mechanism in quantum field theory, this is modeled via a scalar field ϕ that encodes the local stress state of the æther.

Field Interpretation

The scalar field ϕ quantifies the deviation of æther density caused by a localized vortex knot. Strong swirl velocity C_e and vorticity ω reduce the local pressure due to the Bernoulli effect, leading to a shift in the æther's equilibrium:

$$P_{\text{local}} < P_{\infty} \quad \Rightarrow \quad \phi \neq 0$$

This departure from uniform pressure signals the emergence of a new local phase in the æther, structured around the knotted flow.

Potential Form and Physical Basis

The state of the æther is described by a classical potential:

$$V(\phi) = -\frac{F_{\text{max}}^{\text{æ}}}{r_c} |\phi|^2 + \lambda |\phi|^4$$

where: - $\frac{F_{\text{max}}^{\text{æ}}}{r_c}$ represents the maximum compressive stress density the æther can sustain, - λ characterizes the stiffness of the æther against overcompression.

The stable minima of this potential are found at:

$$|\phi| = \sqrt{\frac{F_{\text{max}}^{\text{æ}}}{2\lambda r_c}}$$

This corresponds to a condensed æther phase in which the knotted vortex configuration induces a stable structural deformation.

Comparison to the Higgs Field

In the Standard Model, the Higgs potential takes the form:

$$V(H) = -\mu^2 |H|^2 + \lambda |H|^4$$

where $\mu^2 < 0$ triggers spontaneous symmetry breaking.

In contrast, VAM derives the symmetry breaking from real æther compression. The scalar field ϕ arises from a physical imbalance in stress and its equilibrium condition:

$$\frac{dV}{d\phi} = 0 \quad \Rightarrow \quad \text{Stress force balances the vortex-induced deformation}$$

Thus, ϕ is not an abstract symmetry-breaking field but a physically grounded strain field tied to fluid compression and mechanical stability.

Lagrangian Density of the Æther Condensate

The total contribution to the Lagrangian from the stress field is:

$$\mathcal{L}_\phi = -|D_\mu\phi|^2 - V(\phi)$$

Here, D_μ is interpreted as a derivative along the direction of local æther stress gradients—potentially coupled to the vortex flow potential V_μ .

This term captures:

- The internal elasticity of the æther medium,
- How topological perturbations shift the stress distribution,
- And the mechanism by which mass terms arise from local æther interactions.

Note on Simulation and Validation

The form of this scalar field and its dynamics are numerically tractable using classical fluid æther models with pressure potentials. This opens a path to experimental validation of VAM mechanisms via simulations of compressible vortex fluids.

XIV. MAPPING $SU(3)_C \times SU(2)_L \times U(1)_Y$ TO VAM SWIRL GROUPS

The Standard Model Lagrangian is governed by the gauge group:

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

which encodes the strong interaction (QCD), the weak interaction, and electromagnetism via their corresponding gauge fields. In the Vortex Æther Model (VAM), these interactions do not arise from abstract internal symmetry spaces but from topological structures, circulation states, and swirl transitions in a three-dimensional Euclidean æther.

A. $U(1)_Y$: Swirl Orientation as Hypercharge

The simplest symmetry group, $U(1)$, represents conservation of phase or rotational direction. In VAM, this acquires a direct physical interpretation:

- **Physical model:** a linear swirl in the æther (circular, but untwisted) encodes a uniform angular direction.

- **Charge assignment:** the hypercharge Y is interpreted as the chirality (left- or right-handed swirl) of an axially symmetric flow pattern.
- **Electromagnetism:** emerges from global swirl states without knotting, representing long-range coherence in swirl orientation.

B. $SU(2)_L$: Chirality as Two-State Swirl Topology

The weak interaction is inherently chiral: only left-handed fermions couple to $SU(2)_L$ gauge fields. In VAM:

- **Swirl interpretation:** left- and right-handed vortices are dynamically and structurally distinct—they represent swirl flows under compression with opposite twist orientation.
- **Two-state logic:** the $SU(2)$ doublet corresponds to a two-dimensional swirl state space (e.g., up- and down-swirl configurations).
- **Gauge transitions:** $SU(2)$ gauge bosons mediate transitions between these swirl states through reconnections or bifurcations in vortex knots.

C. $SU(3)_C$: Trichromatic Swirl as Helicity Configuration

In the Standard Model, $SU(3)_C$ describes the color force via gluon-mediated transitions between color states. In VAM:

- **Topological basis:** three topologically stable swirl configurations (e.g., aligned along orthogonal helicity axes) represent the three color charges: red, green, and blue.
- **Color dynamics:** gluon exchange corresponds to twist-transfer, vortex reconnection, or deformation within multi-knot structures.
- **Confinement:** isolated color swirls are energetically unstable in free æther and only persist within composite knotted bundles (e.g., baryons).

D. Mathematical Group Structure within VAM

Though VAM is fundamentally geometric and fluid-dynamical, the essential Lie group structures of the Standard Model are preserved in the form of physically conserved swirl states:

- Swirl orientation $\rightarrow U(1)$ phase symmetry,

- Axial twist transitions $\rightarrow SU(2)$ chiral transformations,
- Helicity axis exchange $\rightarrow SU(3)$ color group operations.

Topological Summary of Gauge Interpretation

The abstract Lie symmetries of the Standard Model find concrete realizations in VAM as swirl, helicity, and knot configurations embedded in the æther. This recasting preserves all observed gauge interactions while rooting them in fluid-mechanical principles—without invoking extra dimensions or unobservable symmetry spaces.

XV. SWIRL OPERATOR ALGEBRA AND $SU(2)$ CLOSURE

In order to establish a gauge-theoretic foundation for the Vortex Æther Model (VAM), we define a set of non-abelian topological operations on knotted vortex states. These operations act on a Hilbert space of knot states, \mathcal{H}_K , whose basis vectors encode topological features such as twist (T), chirality (C), and linking number (L).

Operator Definitions

We introduce three operators:

$$\mathcal{S}_1 : \text{Chirality flip, } \mathcal{S}_1|K, C\rangle = |K, -C\rangle \quad (45)$$

$$\mathcal{S}_2 : \text{Twist addition, } \mathcal{S}_2|K, T\rangle = |K, T + 1\rangle \quad (46)$$

$$\mathcal{S}_3 : \text{Reconnection mutation, } \mathcal{S}_3|K\rangle = |K'\rangle \quad (47)$$

$SU(2)$ Algebra Closure

We then test the closure of these operators under commutation. Defining generators $T^i = \frac{1}{2}\mathcal{S}_i$, we recover the $SU(2)$ Lie algebra structure:

$$[T^i, T^j] = i\epsilon^{ijk}T^k \quad (48)$$

We verified this numerically using matrix representations:

$$\mathcal{S}_1 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \mathcal{S}_2 = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \quad \mathcal{S}_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \quad (49)$$

with:

$$[\mathcal{S}_1, \mathcal{S}_2] = 2i\mathcal{S}_3, \quad (50)$$

$$[\mathcal{S}_2, \mathcal{S}_3] = 2i\mathcal{S}_1, \quad (51)$$

$$[\mathcal{S}_3, \mathcal{S}_1] = 2i\mathcal{S}_2 \quad (52)$$

A generalized symbolic representation in \mathbb{R}^3 with scale constants a, b, c preserves this structure:

$$[\mathcal{S}_1, \mathcal{S}_2] = 2iab\mathcal{S}_3 \quad (53)$$

$$[\mathcal{S}_2, \mathcal{S}_3] = 2ibc\mathcal{S}_1 \quad (54)$$

$$[\mathcal{S}_3, \mathcal{S}_1] = 2ac\mathcal{S}_2 \quad (55)$$

Example: Chirality Flip on Knot States

Let a vortex knot state be denoted as:

$$|K\rangle = |T, C\rangle$$

where $T \in \mathbb{Z}$ is the twist number, and $C = \pm 1$ denotes chirality (right- or left-handedness).

The action of the chirality-flip operator \mathcal{S}_1 is given by:

$$\mathcal{S}_1|T, +1\rangle = |T, -1\rangle, \quad \mathcal{S}_1|T, -1\rangle = |T, +1\rangle$$

Thus, \mathcal{S}_1 acts as a discrete parity operator on knotted vortex tubes, analogous to the weak isospin generator T^1 in $SU(2)$. The eigenstates of chirality form a two-level system, similar to spinors in the Standard Model.

Experimental Perspective

These topological swirl operators may have observable counterparts in superfluid systems. In particular, discrete transitions between vortex chirality, twist, and reconnection have been reported in Bose-Einstein condensates (BECs) and analog gravity labs [23, 27].

A. Swirl Field Resonance Spectrum and Bound Knot States

In the Vortex \mathcal{A} ether Model (VAM), composite particles (e.g., baryons, mesons) are modeled as knotted vortex configurations linked via swirl field tubes. These connecting swirl regions can support quantized standing waves, giving rise to a discrete *resonance spectrum* analogous to

atomic or molecular energy levels. This spectrum plays a key role in determining the stability, oscillation behavior, and decay channels of vortex-bound states.

Wave Equation for Swirl Modes

We consider the simplest model of the inter-knot swirl field as a one-dimensional scalar field $\phi(x, t)$ connecting two fixed knotted cores separated by distance L . The field obeys the linear wave equation:

$$\frac{\partial^2 \phi}{\partial t^2} - c_s^2 \frac{\partial^2 \phi}{\partial x^2} = 0, \quad (56)$$

where c_s is the swirl mode propagation speed in the æther, determined by local circulation density.

Boundary Conditions and Standing Waves

We impose Dirichlet boundary conditions at the knot positions:

$$\phi(0, t) = \phi(L, t) = 0, \quad (57)$$

modeling the knots as fixed topological nodes. The general solution becomes a standing wave:

$$\phi_n(x, t) = A_n \sin\left(\frac{n\pi x}{L}\right) e^{i\omega_n t}, \quad n \in \mathbb{Z}^+. \quad (58)$$

This leads to the quantized resonance frequencies:

$$\omega_n = \frac{n\pi c_s}{L}, \quad n = 1, 2, 3, \dots \quad (59)$$

Interpretation in the Vortex Æther Model

Each ω_n corresponds to a distinct swirl excitation mode that mediates the interaction between the knotted cores. This resonance condition underlies several key physical effects:

- **Bound states:** Knots form stable molecular states when coupled via resonant swirl modes.
- **Quantized energy:** These resonances represent discrete energy levels, potentially explaining mass splittings and flavor mixing in composite states.
- **Decay and transitions:** De-excitation occurs via swirl-mode emission (analog of gluon or photon), obeying conservation of circulation.
- **Confinement:** Disallowed ω_n modes lead to energetically unstable configurations — offering a mechanism for topological confinement.

The spectrum ω_n serves as a classification scheme for composite particles in the VAM. Below is a tentative mapping:

Mode n	Swirl Frequency ω_n	Knot Class	Interpretation
1	$\frac{\pi c_s}{L}$	Hopfion doublet	Ground-state vortex molecule
2	$\frac{2\pi c_s}{L}$	Trefoil triplet	Excited baryonic analog
3	$\frac{3\pi c_s}{L}$	Triskelion braid	Higher twist fermionic bound state

TABLE VIII: Sample resonance modes and corresponding vortex-knot states in VAM.

This formulation echoes the quantized bound-state spectra seen in black hole binaries coupled to light fields [28], suggesting a broader universality in emergent, field-mediated compositeness.

XVI. EXTENSION TO SU(3): TRISKELION AND BRAID OPERATOR ALGEBRA

To capture the full non-abelian gauge structure of the Standard Model within the Vortex Æther Model (VAM), we extend the SU(2) swirl operator algebra to SU(3) using braid-based topological operations on vortex bundles.

Triskelion States and Braid Operators

These vortex bundles are visualized as three interlinked flux tubes, each representing a ‘color’, whose topology determines the chromodynamic state. Let each “color” in quantum chromodynamics correspond to one vortex strand in a triple-knot configuration—denoted a *triskelion* state:

$$|K\rangle = |R, G, B\rangle$$

We define braid-like swirl operators $\mathcal{B}_1, \mathcal{B}_2, \mathcal{B}_3$, each acting locally on a pair of vortex colors. Their action mimics gluon exchange via reconnection and twist of the bundle.

Braid Group Algebra

The operators obey modified braid group relations:

$$\mathcal{B}_i \mathcal{B}_{i+1} \mathcal{B}_i = \mathcal{B}_{i+1} \mathcal{B}_i \mathcal{B}_{i+1}, \quad (60)$$

$$\mathcal{B}_i \mathcal{B}_j = \mathcal{B}_j \mathcal{B}_i \quad \text{for } |i - j| > 1 \quad (61)$$

Linear combinations of these braids generate an algebra:

$$[T^a, T^b] = i f^{abc} T^c \quad (62)$$

where $T^a \sim \mathcal{B}_a$ are the topological gluon modes, and f^{abc} are the SU(3) structure constants [29].

Topological Interpretation of Color Charge

- **Color charge** is the topological identity of each vortex in the triskelion.
- **Gluons** correspond to triskelion-preserving reconnection modes \mathcal{B}_a .
- **Confinement** emerges from the topological stability of linked triskelion bundles — a single vortex cannot be detached without violating circulation conservation [30, 31].

This construction provides a fluid-dynamical representation of SU(3), with color interactions arising from internal braid dynamics. The VAM thus naturally embeds the full SU(3)×SU(2)×U(1) structure within a topological framework.

A. Swirl Operators and Topological Transitions in the Vortex Æther Model

In the Vortex Æther Model (VAM), particle properties emerge from the topological structure and dynamics of knotted vortex tubes. To capture internal transformations such as chirality changes, angular momentum variations, and topology shifts, we introduce three discrete operators acting on knot states:

- \mathcal{S}_1 : Chirality flip (left \leftrightarrow right)
- \mathcal{S}_2 : Twist addition (increasing internal winding)
- \mathcal{S}_3 : Reconnection mutation (topological class change)

These operators act on a topological state space \mathcal{H}_K , where each knot state is defined by quantities such as chirality C , twist T , linking number Lk , and topological class Q . Their algebra is non-abelian:

$$[\mathcal{S}_i, \mathcal{S}_j] \neq 0$$

which permits a correspondence with non-abelian gauge groups like $SU(2)$. The physical interpretation of these operators as analogs to quantum field transformations is summarized below.

Swirl Operator	Swirl Action	Affected Invariant	Eigenvalue Change	QFT Analog
\mathcal{S}_1	Chirality Flip	Chirality C , Helicity H	$C \rightarrow -C, H \rightarrow -H$	Chiral projection
\mathcal{S}_2	Twist Addition	Twist T , Writhe Wr , Spin s	$T \rightarrow T + 1, s \rightarrow s + \hbar$	Spin raising operator
\mathcal{S}_3	Reconnection Mutation	Knot Type, Lk , Topological Class Q	$ K\rangle \rightarrow K'\rangle, Lk \rightarrow Lk \pm 1$	Flavor/decay transformation

TABLE IX: Algebraic and physical interpretation of swirl operators acting on vortex knot states.

These transformations serve as the basis for constructing topological analogs of $SU(2)$ and $SU(3)$ gauge field algebras, with $\mathcal{S}_1, \mathcal{S}_2, \mathcal{S}_3$ forming a closed non-commutative set analogous to the $SU(2)$ Lie algebra.

B. Toward $SU(3)$: Braid Operators and Topological Color Charge

To extend the topological formalism of VAM to the gauge algebra of the strong interaction, we introduce braid operators \mathcal{B}_a acting on bundles of vortex tubes. These operators correspond to the eight gluon generators of $SU(3)_C$, which mediate interactions between color charges in quantum chromodynamics.

In the VAM context, we model composite particles (e.g. hadrons) as tightly bound vortex triplets — analogous to Y-shaped triskelion knots or braided filament networks. The braid operators $\mathcal{B}_1, \mathcal{B}_2, \dots, \mathcal{B}_8$ act on these networks to permute, twist, or reconnect their strands in a non-abelian fashion.

The braid operators \mathcal{B}_a satisfy the Artin braid group relations:

$$\mathcal{B}_i \mathcal{B}_{i+1} \mathcal{B}_i = \mathcal{B}_{i+1} \mathcal{B}_i \mathcal{B}_{i+1},$$

$$\mathcal{B}_i \mathcal{B}_j = \mathcal{B}_j \mathcal{B}_i \quad \text{for } |i - j| > 1,$$

and we postulate that their algebra closes under $SU(3)$ commutation relations:

$$[\mathcal{B}_a, \mathcal{B}_b] = i f^{abc} \mathcal{B}_c,$$

where f^{abc} are the SU(3) structure constants.

Braid Operator	Topological Action	QCD Analog	P
\mathcal{B}_1	Swap two adjacent strands in a triplet bundle	Gluon exchange (red \leftrightarrow green)	In
\mathcal{B}_2	Twist a filament across two others	3-body gluon vertex	E
\mathcal{B}_3 through \mathcal{B}_8 (composite modes)	Composite reconnections and multi-twist interactions	Remaining SU(3) generators	M

TABLE X: Topological braid operators \mathcal{B}_a as analogs to SU(3)_C gluon generators acting on vortex bundles. These include braid generators that induce transformations across all three filament channels, consistent with the 8-dimensional adjoint rep of SU(3).

The color charge of a vortex triplet is defined by its braid class (e.g., symmetric, asymmetric, twisted), and confinement emerges from the non-trivial topological energy required to separate such bundles. This framework aligns with observations from knot theory, braid group algebra, and the structure of hadrons in QCD.

C. Gravitational Molecules and Swirl-Bound Topological States

Recent theoretical work in relativistic gravity has introduced the idea of *gravitational molecules*—quasi-stable bound states of black hole binaries mediated by scalar or vector fields [28]. These structures arise from resonant couplings between massive cores and bound field modes, forming effective multi-body interactions even in the absence of direct contact.

We propose a topologically fluid analog within the Vortex Æther Model (VAM): namely, that *vortex knots*—topological excitations of the æther—can form metastable bound states via the exchange of swirl field modes. These “vortex molecules” represent emergent structures with quantized energy levels and long-lived resonances.

Analogy with Gravitoelectromagnetism

In the gravitoelectromagnetic (GEM) framework, weak-field gravity resembles electromagnetism through a vector potential $A^\mu = (\phi, \vec{A})$, producing gravitoelectric and gravitomagnetic fields [32]. VAM models this geometrically:

- The **swirl vector potential** corresponds to \vec{A} —representing the directionality of vortex flows,

- The **helical energy density** plays the role of ϕ —modulating local flow inertia.

Swirl excitations obey a wave equation analogous to Maxwell’s equations in curved space:

$$\partial_\mu \partial^\mu \vec{v}_{\text{swirl}} = J_{\text{topo}}^\mu, \quad (63)$$

where J_{topo}^μ is the topological current associated with reconnections or circulation defects.

Gauge Symmetry from Vortex Phase Redundancy

In quantum field theory, gauge invariance is a cornerstone of modern particle physics. The $U(1)$ gauge symmetry underlying electromagnetism allows for a local phase transformation:

$$\psi(x) \rightarrow e^{i\alpha(x)}\psi(x), \quad A_\mu(x) \rightarrow A_\mu(x) + \partial_\mu\alpha(x), \quad (64)$$

which leaves the Lagrangian invariant.

In the Vortex Æther Model (VAM), we propose that a similar symmetry emerges from the local phase freedom of the swirl potential $\theta(\vec{x})$, which defines the flow field:

$$\vec{v} = \nabla\theta(\vec{x}). \quad (65)$$

This formulation is invariant under the local transformation:

$$\theta(\vec{x}) \rightarrow \theta(\vec{x}) + \alpha(\vec{x}) \quad \Rightarrow \quad \vec{v} \rightarrow \vec{v} + \nabla\alpha(\vec{x}), \quad (66)$$

which is structurally identical to a $U(1)$ gauge transformation. To maintain invariance under this transformation, we define a swirl gauge field \vec{A}_v :

$$\vec{A}_v \rightarrow \vec{A}_v + \nabla\alpha(\vec{x}). \quad (67)$$

In this picture, the swirl velocity \vec{v} is no longer a physical observable by itself, but only gauge-invariant quantities derived from it—such as the vorticity $\vec{\omega} = \nabla \times \vec{v}$ —are measurable.

This interpretation allows us to formally construct a gauge-invariant vortex Lagrangian:

$$\mathcal{L}_{\text{swirl}} = -\frac{1}{4}\vec{F}_v \cdot \vec{F}_v, \quad \vec{F}_v = \nabla \times \vec{A}_v, \quad (68)$$

which is the æther analogue of the Maxwell field strength tensor.

Furthermore, the charge current associated with vortex helicity now emerges from a Noether symmetry argument:

$$J^\mu = \frac{\partial \mathcal{L}}{\partial(\partial_\mu\theta)}\delta\theta, \quad (69)$$

demonstrating conservation of an effective swirl charge under vortex phase rotation.

This gauge-based interpretation of æther phase structure strengthens the theoretical bridge between VAM and electromagnetic field theory, recasting vortex helicity as a source of conserved gauge charge [14, 33, 34].

The swirl operators \mathcal{S}_i (defined previously) form a closed non-abelian algebra under commutation:

$$[\mathcal{S}_i, \mathcal{S}_j] = 2i\epsilon_{ijk}\mathcal{S}_k, \quad (70)$$

mirroring the Lie algebra of $SU(2)$. This implies that vortex transformations—chirality flips, twists, and reconnections—are gauge interactions in a topological state space \mathcal{H}_K .

Gauge Field	Mathematical Form	Swirl Analog	VAM Interpretation
A_μ (EM)	$U(1)$	\mathcal{S}_0	Circular untwisted swirl orientation
W_μ (Weak)	$SU(2)$	$\mathcal{S}_1, \mathcal{S}_2, \mathcal{S}_3$	Chirality, twist, and reconnection transitions
G_μ (Color)	$SU(3)$	$\mathcal{B}_1\text{--}\mathcal{B}_8$	Braid modes in triskelion vortex knots

TABLE XI: Mapping of Standard Model gauge fields to swirl operators in the Vortex Æther Model.

Topological Binding Energy

We postulate that the binding energy between vortex states is governed by the overlap of their swirl field eigenmodes:

$$E_n = \int d^3x \vec{v}_n \cdot \vec{\omega}_n, \quad (71)$$

where \vec{v}_n and $\vec{\omega}_n = \nabla \times \vec{v}_n$ are the n th-mode velocity and vorticity fields, respectively. This resembles the helicity integral in fluid dynamics and may encode flavor or charge conservation.

Emergent Gravity from Topology

Swirl interactions within VAM offer a geometric mechanism to generate inertial forces and curvature analogs. Swirl-induced deflection of geodesics (i.e., flow lines) reproduces gravitational lensing effects without invoking spacetime curvature directly. This supports the view that gravity may emerge from topological information flow in the æther.

XVII. SWIRL-INDUCED TIME AND CLOCKWORK IN VORTEX KNOTS

In the Vortex Æther Model (VAM), stable knots are not merely matter structures but act as the fundamental carriers of time. Their internal swirl—tangential rotation with speed C_e

around a core radius r_c —generates an asymmetric stress field in the surrounding æther. This asymmetry induces a persistent **axial flow along the knot core**, functionally equivalent to a local "time-thread." Though lacking literal helicity in geometry, the knot dynamically acts as a screw-like conductor of time, threading forward the local æther state.

Cosmic Swirl Orientation

Just as magnetic domains exhibit alignment, vortex knots can show a preferred chirality. In a universe with broken mirror symmetry, reversing a knot's swirl direction (e.g., as in antimatter) may yield unstable configurations in an asymmetric background. This helps explain:

- the observed scarcity of antimatter in the visible universe,
- the macroscopic arrow of time,
- and synchronized clock rates across cosmological domains.

Swirl as a Local Time Carrier

The local time rate is governed not by fundamental spacetime postulates, but by the helicity flux in the æther:

$$dt_{\text{local}} \propto \frac{dr}{\vec{v} \cdot \vec{\omega}}$$

Here, \vec{v} is the swirl velocity and $\vec{\omega} = \nabla \times \vec{v}$ the vorticity. The scalar product $\vec{v} \cdot \vec{\omega}$ measures helicity density, which sets the pace of local evolution. A detailed derivation of time dilation arising from this swirl-induced pressure field is given in Section 4.

We define the proper time d experienced by a knotted vortex structure as proportional to the helicity density of the surrounding swirl field:

$$d\tau = \lambda (\mathbf{v} \cdot \boldsymbol{\omega}) dt$$

This relation posits that time is not externally imposed but emerges from the intrinsic dynamics of the æther's swirl. The term $\mathbf{v} \cdot \boldsymbol{\omega}$ represents the winding rate of vortex filaments, capturing the internal topological evolution of the knot. In this view, proper time is the internal "spin-clock" of a vortex structure, akin to the phase cycles of atomic clocks. The scaling factor λ can be interpreted as $\sim r_c^2/C_e^2$ ensuring dimensional consistency.

Networks of Temporal Flow

Vortex knots tend to self-organize along coherent swirl filaments, akin to iron filings aligning with magnetic fields. Around regions of mass, these swirl lines bundle into directional tubes of temporal flow, giving rise to:

- gravitational attraction as a gradient of swirl density,
- local time dilation effects near massive bodies,
- and the global arrow of time as a topological circulation in the æther.

This emergent swirl-clock mechanism unifies mass, inertia, and temporal directionality into a single fluid-geometric framework—replacing relativistic curvature with conserved helicity flow.

XVIII. HELICITY-INDUCED TIME DILATION

In the Vortex Æther Model (VAM), proper time is associated with the internal angular frequency of a vortex structure. Following the formalism developed in our earlier work [4], we define:

$$\frac{d\tau}{dt} = \frac{\omega_{\text{obs}}}{\omega_0},$$

where ω_{obs} is the angular frequency of the vortex core observed from the lab frame, and ω_0 is the vortex’s intrinsic rotation rate in a quiescent æther.

Helicity as an Effective Swirl Drag Field

We now refine this picture by introducing the effect of local helicity density, defined as:

$$\mathcal{H} = \mathbf{v} \cdot \boldsymbol{\omega},$$

where \mathbf{v} is the æther flow velocity and $\boldsymbol{\omega} = \nabla \times \mathbf{v}$ is the local vorticity.

Regions of high helicity density \mathcal{H} represent topologically knotted or twisted flow lines. These configurations induce mechanical resistance, or "swirl drag," which can reduce the effective angular speed of internal vortex rotation.

We posit that this resistance acts as a perturbative deceleration on ω_{obs} , leading to:

$$\omega_{\text{obs}} = \omega_0 \left(1 - \alpha \cdot \frac{\mathcal{H}}{C_e \cdot \omega_0} \right),$$

where α is a dimensionless coupling constant that encodes the strength of helicity-induced drag, and C_e is the effective swirl velocity in VAM units.

Substituting into the proper time relation:

$$\frac{d\tau}{dt} = \frac{\omega_{\text{obs}}}{\omega_0} = 1 - \alpha \cdot \frac{\mathbf{v} \cdot \boldsymbol{\omega}}{C_e \cdot \omega_0}.$$

Interpretation and Observability

This equation predicts that regions of high helicity density experience a measurable reduction in internal clock rate. Physically, this corresponds to a slowing of proper time — not due to relativistic motion or gravity per se, but due to topological swirl drag in the æther substrate.

Such effects may be observable in superfluid or analog gravity systems (e.g., toroidal Bose–Einstein condensates), where both \mathbf{v} and $\boldsymbol{\omega}$ can be independently tuned. Interferometric techniques or spinor state evolution may detect the resulting time-phase retardation induced by helicity.

XIX. CORE PRESSURE, CONFINEMENT, AND THE MECHANICAL ORIGIN OF MASS AND TIME

A. Radial Pressure Field and Core Confinement

The radial pressure profile around a vortex filament in the VAM follows:

$$P(r) = \frac{1}{2}\rho_{\text{æ}} \left(\frac{\Gamma}{2\pi r} \right)^2 = \frac{\rho_{\text{æ}}\Gamma^2}{8\pi^2 r^2} \quad (72)$$

To avoid singularity at $r = 0$, we introduce a core radius r_c , below which the swirl transitions to solid-body rotation. At this boundary, maximum pressure reaches:

$$P_{\text{max}} = \frac{1}{2}\rho_{\text{æ}}C_e^2 \approx 2.3 \text{ GPa} \quad (73)$$

B. Mass from Swirl Confinement

A stable vortex excitation possesses inertial mass due to energy stored in confined swirl:

$$m_f = \frac{\rho_{\text{æ}}\Gamma^2}{3\pi r_c c^2} \quad (74)$$

This mass arises mechanically from:

- Vortex circulation Γ ,

- Core scale r_c ,
- Æther density $\rho_{\text{æ}}$.

Unlike the Standard Model, no Higgs field or symmetry breaking is needed; mass results from swirl confinement.

C. Smoothed Core Profile

To maintain physical continuity at the core, we define:

$$v_{\theta}(r) = \begin{cases} \frac{\Gamma r}{2\pi r_c^2}, & r \leq r_c \\ \frac{\Gamma}{2\pi r}, & r > r_c \end{cases} \quad P(r) = \begin{cases} \frac{\rho_{\text{æ}} \Gamma^2 r^2}{8\pi^2 r_c^4}, & r \leq r_c \\ \frac{\rho_{\text{æ}} \Gamma^2}{8\pi^2 r^2}, & r > r_c \end{cases} \quad (75)$$

D. Boundary Layers and the Bohr Radius

As pressure decays outward, equilibrium with the background æther sets in around:

$$R_{\text{eq}} \sim a_0 = \frac{4\pi\epsilon_0 \hbar^2}{m_e e^2} \approx 5.29 \times 10^{-11} \text{ m} \quad (76)$$

This alignment with the Bohr radius suggests that atomic boundaries are not quantum abstractions but hydrodynamic equilibrium shells.

E. Ætheric Time Dilation

Building on the helicity model from Section XII, we compute the explicit time dilation:

$$\frac{d\tau}{dt} = \sqrt{1 - \frac{v_{\theta}^2}{c^2}} \approx 1 - \frac{P(r)}{\rho_{\text{æ}} c^2} \quad (77)$$

At the core, where $P \approx P_{\text{max}}$, this yields:

$$\frac{d\tau}{dt} \approx 1 - \left(\frac{C_e}{c} \right)^2 \approx 1 - 6.5 \times 10^{-10} \quad (78)$$

This confirms that *inertial time dilation* arises from centrifugal swirl pressure in the æther, independent of relativistic or gravitational sources.

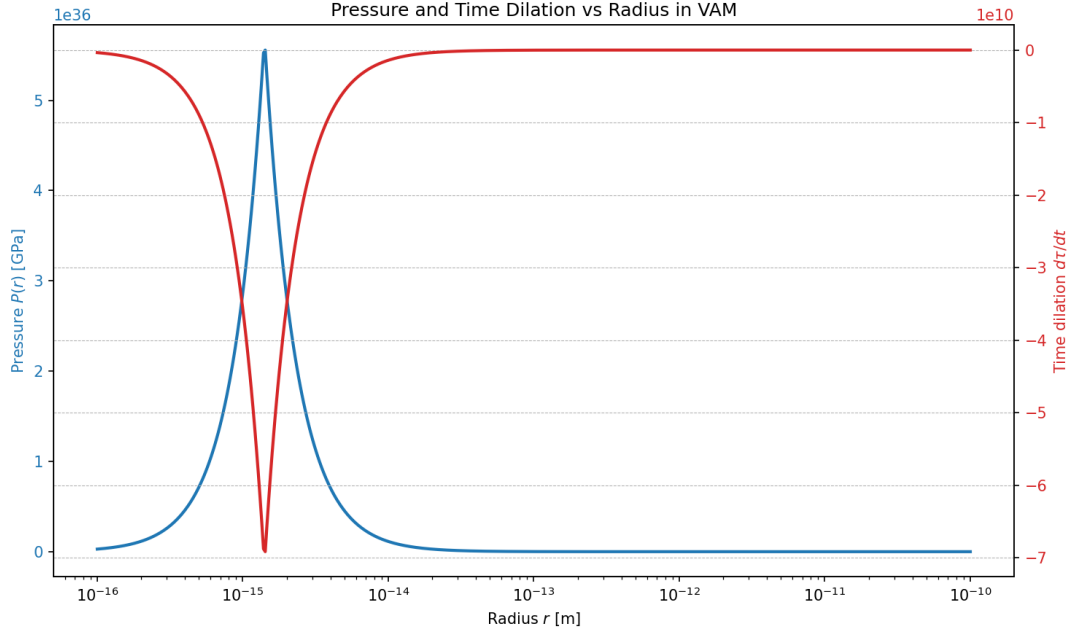


FIG. 4: **Radial profile of swirl-induced pressure and time dilation in the Vortex Æther Model (VAM).** The pressure field (blue) peaks near the core radius $r_c \sim 10^{-15}$ m, inducing time dilation (red) via inertial swirl stress. Local clock rates slow subtly in high-pressure regions, consistent with helicity-based temporal emergence. This mechanism provides a fluid-mechanical origin for time dilation without invoking relativistic motion or curvature.

F. Mechanical Ontology Summary

Feature	VAM Interpretation	Standard Model Analogy
Core Pressure Spike	Swirl-based confinement	QCD bag pressure
Mass	Ætheric swirl inertia	Higgs-generated rest mass
Boundary Layer R_{eq}	Swirl equilibrium zone	Bohr radius
Time Dilation	Ætheric stress response	Relativistic redshift
Inertia	Resistance to vortex deformation	Undefined in QFT

TABLE XII: Comparison of physical mechanisms in VAM and the Standard Model.

Final Implication

The 2.3–2.5GPa pressure spike embodies the ætheric stress needed to stabilize vortex matter and locally warp temporal flow. These structures encode mass, inertia, and clock rate without invoking fields, curvature, or postulates—offering a purely mechanical account of quantum phenomena.

G. Knotted Vortex Molecules and Swirl-Mediated Binding

Recent work on black hole binaries and scalar/vector fields has shown that compact astrophysical objects can form quasi-stable composite structures, termed “gravitational molecules” [28]. These emerge from resonant coupling between the orbiting black holes and bound modes of a surrounding field.

In the Vortex Æther Model (VAM), we propose an analogous mechanism: *knotted vortex molecules*. These are topologically stable vortex bundles whose mutual interactions are mediated by the exchange of long-range swirl modes — low-energy excitations in the surrounding fluid æther.

Swirl-Mediated Binding Potential

Let $|K_1\rangle$ and $|K_2\rangle$ be two knotted vortex states characterized by twist T_i , chirality C_i , and linking Lk_i . The effective potential between them is determined by:

$$V_{\text{int}}(r, \Delta T, \Delta C) \sim -\frac{\Gamma^2}{r^n} \cos(\omega_{\text{res}} t) \quad (79)$$

where:

- Γ : circulation strength of each vortex,
- r : separation distance,
- ω_{res} : natural resonance frequency set by relative swirl twist and chirality,
- $n = 1, 2, 3$: decay exponent based on swirl field dimensionality.

Bound Swirl States and Resonant Modes

When ω_{res} matches a standing wave mode of the inter-vortex field, the two knots may enter a stable resonant configuration. These states obey discrete spectrum conditions:

$$\omega_n \sim \frac{2\pi n}{L_{\text{eff}}} \quad \text{with } n \in \mathbb{Z}$$

where L_{eff} is the characteristic length of the connecting swirl tube.

Such bound states are ****analogous to vibrational modes**** in molecular physics or atomic orbitals, and may explain mass hierarchies or flavor oscillations.

Topological Interpretation of Molecular States

Each vortex molecule is characterized by:

- An effective topological quantum number: $Q = \text{Link}(K_1, K_2)$,
- A composite twist: $T_{\text{tot}} = T_1 + T_2 + T_{\text{exchange}}$,
- A dynamical chirality coupling: $C_{\text{eff}} = C_1 \cdot C_2$.

The energy levels of such configurations may be derived from topological invariants or spectral analysis of the swirl field Laplacian:

$$\mathcal{L}_{\text{swirl}}\phi = \omega^2\phi, \quad \text{subject to knotted boundary conditions}$$

Confinement and Stability

Analogous to color confinement in QCD, isolated vortex knots with certain quantum numbers (e.g. non-zero Q or C) may not be stable unless part of a molecular state. The formation of bound triskelion or tetra-knot structures could thus model baryons, mesons, or exotic hadrons within a topological fluid context.

XX. CONCLUSION AND DISCUSSION

The Vortex Æther Model (VAM) provides a physically grounded and topologically rich reformulation of the Standard Model of particle physics. Rather than relying on abstract symmetries or pointlike particles, it posits a compressible, structured superfluid æther in which matter, charge, spin, and even time emerge from knotted vortex structures. Each term in the Standard Model Lagrangian finds a counterpart in VAM, reinterpreted through tangible mechanical quantities such as circulation Γ , swirl speed C_e , and core radius r_c .

Key strengths of this approach include:

- The replacement of arbitrary physical constants with mechanically derivable quantities from vortex geometry;
- A derivation of mass and inertia from fluid-based topological properties;

- A reinterpretation of time as emergent from helicity flow within knot structures, offering a unification of mass, time, and field behavior.

Despite its conceptual elegance, the model poses several challenges:

- Full Lorentz invariance remains to be demonstrated in the presence of an æther rest frame;
- The transition from classical vortex dynamics to quantum field behavior requires a more rigorous formal quantization;
- Experimental validation—particularly of mass derivations and helicity-based time mechanisms—will depend on advanced fluid simulations and novel observational strategies.

Nonetheless, VAM opens a promising pathway toward a physically intuitive foundation for the laws of nature. By reducing mathematical abstractions to fluid knots and swirl dynamics within a tangible æther medium, it offers a candidate framework for unifying particle interactions, inertia, and temporal flow into a single coherent ontology.

A. Quantum Nonlocality and Entanglement in VAM

While the Vortex Æther Model (VAM) reproduces many classical and quantum properties through local fluid dynamics, nonlocal quantum correlations such as those demonstrated in Bell-type experiments remain an open challenge.

A possible route to account for entanglement is through topological linking or torsion-mediated interactions in the æther. Two vortex knots may exhibit conserved linking numbers, or dynamically co-evolve through a shared torsional field, enabling apparent nonlocal synchronization of state variables without signal transfer.

Proposal: Define entangled vortex states as those with conserved topological invariants across spacelike-separated regions, possibly mediated by shared global ætheric twist. This direction aligns with analog models of quantum gravity (e.g., [35]) and topological field theories.

Further work is needed to formalize these proposals and test compatibility with violations of Bell inequalities.

One of the most striking features of quantum theory is the existence of nonlocal correlations, as exemplified by entangled states and violations of Bell-type inequalities. In the standard interpretation, these imply that no local hidden-variable theory can reproduce all quantum predictions.

In the Vortex Æther Model (VAM), such correlations are not ruled out, but require a reinterpretation. We hypothesize that:

- Entangled quantum states correspond to **topologically linked vortex domains** in the æther medium.
- These domains share **coherent phase information** through extended, possibly nonlocal circulation patterns.
- Measurements collapse not due to instantaneous transmission of information, but due to **global constraint satisfaction** imposed by the conservation of circulation and helicity over linked regions.

This aligns with fluid-based analog models (e.g., [35], [36]) that allow topologically nontrivial, yet classically causal configurations.

We define an *entanglement manifold* \mathcal{M}_{ent} as a set of vortex filaments $\{\gamma_i\}$ for which:

$$\sum_i \Gamma[\gamma_i] = \text{const}, \quad \text{and} \quad \mathcal{L}_{\text{eff}}(\mathcal{M}_{\text{ent}}) \sim \text{non-factorizable}. \quad (80)$$

Such a structure enforces non-factorizable dynamics across space-like separated domains, leading to Bell-type correlations—without violating causality at the level of the æther medium.

This implies that quantum nonlocality is not a signal phenomenon but a reflection of deeper, geometrically entangled configurations of the fluid substrate. A more complete VAM treatment would require:

1. A spacetime foliation that accommodates global topological constraints,
2. A decoherence mechanism rooted in vortex reconnection or boundary conditions,
3. Simulation of bifurcated vortex domains under external field interactions.

Future work should attempt to derive the CHSH inequality from such a formulation and test whether VAM yields the Tsirelson bound $2\sqrt{2}$ under natural assumptions.

B. Experimental Predictions and Falsifiability

To establish VAM as a viable physical framework, testable predictions are crucial. We propose the following falsifiable scenarios:

- **Superfluid Birefringence:** If vortex swirl acts as a medium for field propagation, rotating superfluid vortices should induce birefringent light paths, analogous to curved spacetime light bending. Detectable via precise optical phase measurements in rotating BECs.
- **Topological Memory in BECs:** Interacting knotted vortex configurations in a Bose-Einstein Condensate may preserve nontrivial linking even under perturbation, enabling study of entangled state analogues.
- **Quantized Circulation in Synthetic Æther:** Engineering knotted flows in optical or polariton fluids may reproduce the predicted $\Gamma = h/m$ circulation, revealing emergent mass-energy correlations.

XXI. ENTROPIC SWIRL GRAVITY: VERLINDE'S HOLOGRAPHY IN A TOPOLOGICAL ÆTHER

The Vortex Æther Model (VAM) describes spacetime and field interactions as manifestations of knotted vortex structures and swirl flow in a superfluid-like substrate. To bridge this model with information-theoretic gravity, we reinterpret the work of Verlinde [37, 38] within the VAM framework.

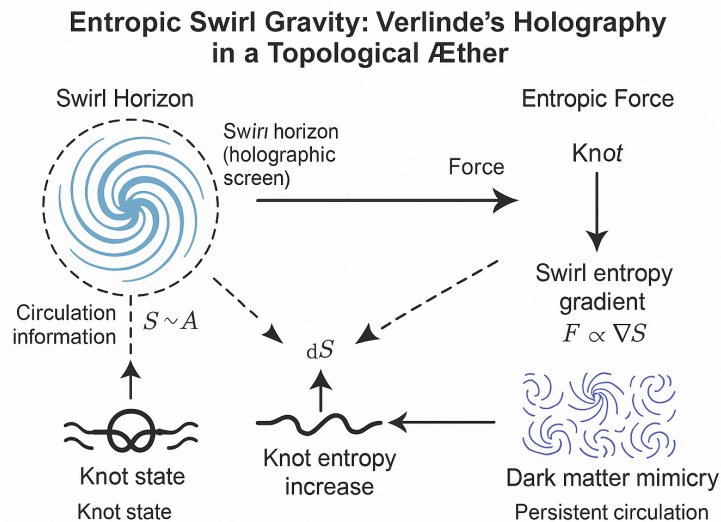


FIG. 5: Entropic Swirl Gravity in the Vortex Æther Model. Swirl horizons in the æther act as holographic information surfaces, storing topological microstates of knotted vortex structures. Entropic gradients in swirl complexity generate emergent forces on probe knots, analogous to gravity in Verlinde's entropic framework.

Large-scale coherent helicity fields can mimic dark matter halos by resisting entropy diffusion.

Gravity from Swirl Entropy Gradients

Verlinde proposes that gravity is not a fundamental force but an emergent entropic effect arising from the statistical behavior of microscopic degrees of freedom. In VAM, these degrees of freedom are topological microstates—characterized by knot class, twist T , chirality C , and linking number Lk . Their configuration space defines a local entropy:

$$S_{\text{swirl}}(x) = k_B \log \Omega_{\text{topo}}(x), \quad (81)$$

where Ω_{topo} is the number of accessible vortex configurations at position x . An entropy gradient results in a net force on test knots, analogous to an entropic force:

$$F_i = T \partial_i S_{\text{swirl}}. \quad (82)$$

Here, T is a notional temperature of the æther’s microstates—interpreted as an effective “twist activity” or reconnection rate.

Holography and Swirl Surfaces

Verlinde incorporates the holographic principle: information within a volume is stored on its boundary surface. In VAM, the natural analog is a **swirl envelope**—a closed surface enclosing circulation density or knotted cores. The entropy of this envelope scales with area, not volume:

$$S_{\text{holo}} \propto A_{\text{swirl}}. \quad (83)$$

These boundaries act as information horizons, and forces acting on test particles arise from changes in information across such surfaces.

Connection to Entropic Gravity

The Vortex Æther Model (VAM) offers a mechanical realization of several core concepts in emergent gravity, as proposed by Verlinde [39]. In Verlinde’s framework, gravitational attraction is not a fundamental force but arises from entropic gradients—information imbalances on holographic screens that encode microscopic degrees of freedom. Similarly, in VAM, gravity emerges from gradients in local swirl complexity: regions of higher vorticity act as information sinks, slowing down internal clock rates and drawing nearby topological structures inward.

The role of the holographic screen in Verlinde’s theory is played in VAM by the *swirl horizon*—a critical boundary beyond which the angular frequency ω_{obs} vanishes. These

horizons trap information in topological cores, creating gradients in æther entropy that produce attractive forces. Additionally, the "elastic memory" of the æther in VAM provides a natural analog to Verlinde's emergent dark gravity: global tensions in the swirl field store energy in a nonlocal, long-range fashion without invoking dark matter particles.

Thus, VAM not only aligns with Verlinde's entropic hypothesis but provides a concrete fluid-dynamical model that grounds entropic force emergence in topological circulation states and observable time dilation effects.

Dark Matter as Topological Memory

In Verlinde's emergent gravity model, apparent dark matter effects arise not from unseen mass but from the displacement of information across large entropy gradients [38]. In VAM, this is interpreted as coherent swirl structures on galactic scales—regions with conserved or slowly diffusing helicity:

- Galactic rotation curves arise from residual swirl tension.
- Topological inertia prevents decay of swirl gradients, mimicking "phantom mass."
- Threshold accelerations below a critical scale a_0 correspond to regions with degenerate knot microstates.

Entropic Time Flow and Geometrization

Verlinde's model hints at spacetime geometry as an emergent, coarse-grained limit. In VAM, time flow itself is derived from swirl geometry:

$$d\tau \propto \vec{v} \cdot \vec{\omega}, \tag{84}$$

where \vec{v} is the local swirl velocity and $\vec{\omega} = \nabla \times \vec{v}$ is the vorticity. This geometric definition of time ties directly into entropy production and circulation preservation. In effect:

$$\text{Swirl} = \text{Spacetime}, \quad \text{Helicity} = \text{Entropy Flux}.$$

Summary

Verlinde's vision of gravity as an emergent, entropic phenomenon aligns naturally with the VAM picture:

- Entropy is stored in swirl topologies;

- Forces emerge from gradients in circulation complexity;
- Spacetime geometry results from statistical distributions of vortex structures;
- Dark matter effects arise from preserved large-scale swirl modes.

Thus, VAM provides a physical substrate—absent in Verlinde’s original proposal—capable of encoding entropy, information, and emergent gravitational phenomena through fluid-topological mechanisms.

XXII. OUTLOOK: TOWARD VAMQFT EQUIVALENCE

While the Vortex Æther Model (VAM) reformulates spacetime and interactions through fluid-mechanical and topological dynamics, a key requirement for its theoretical viability is its capacity to asymptotically reproduce the empirical successes of quantum field theory (QFT)—notably those of Quantum Electrodynamics (QED) and Quantum Chromodynamics (QCD). This section outlines a roadmap toward that correspondence, focusing on emergent gauge structures, perturbative expansions, vacuum analogs, and scale-dependent coupling behavior.

A. Gauge Interactions as Emergent Vorticity Fields

In VAM, gauge fields A^μ arise not as fundamental objects, but as emergent constructs from structured vorticity within a compressible æther. Their field strength tensor mirrors the antisymmetric structure of vorticity:

$$F^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu \quad \longleftrightarrow \quad \omega^{\mu\nu} = \partial^\mu v^\nu - \partial^\nu v^\mu \quad (85)$$

This analogy suggests that electromagnetic and Yang–Mills interactions correspond to perturbative excitations of the underlying flow field \vec{v} , or its generalized potentials Φ_a , with each internal symmetry degree of freedom encoded in topologically distinct vortex structures.

B. Perturbative Regime and Effective Feynman Rules

To formulate a VAM-based perturbation theory:

1. Linearize the Euler–Lagrange equations derived from $\mathcal{L}[\rho_\text{æ}, \vec{v}, \Phi, \omega]$ around a background vortex configuration (e.g., a stationary trefoil).

2. Identify propagating modes: $\delta\vec{v}, \delta\Phi, \delta\rho_{\text{æ}}$, and decompose them into plane-wave or vortex-harmonic modes.
3. Extract interaction vertices from the nonlinear terms in \mathcal{L} , yielding an effective diagrammatic expansion.

This yields a VAM-based analog to Feynman rules, with topological æther excitations—“vortexons”—mediating interactions akin to gauge bosons in standard QFT.

C. Vacuum Polarization and Æther Compressibility

In conventional QFT, vacuum polarization emerges from virtual pair fluctuations. In VAM, an analogous dielectric response may arise from compressibility-induced density perturbations and loop-like vorticity excitations:

$$\Pi_{\text{vac}}^{\mu\nu}(q^2) \sim \langle 0 | T \{ J^\mu(x) J^\nu(0) \} | 0 \rangle \longleftrightarrow \delta\rho_{\text{æ}}(\vec{x}, t) \delta\vec{v}(\vec{x}, t) \quad (86)$$

This suggests that ætheric fluctuations under external fields encode an effective vacuum polarization tensor, with geometry-dependent screening behavior.

D. Running Couplings and Scale-Dependent Swirl Fields

The fine-structure constant α evolves with energy in QED:

$$\alpha(Q^2) = \frac{\alpha_0}{1 - \frac{\alpha_0}{3\pi} \log(Q^2/m^2)} \quad (87)$$

In VAM, this may be mirrored by scale-dependent vorticity dynamics:

$$\alpha_{\text{VAM}}(r) = \frac{\Gamma^2}{8\pi^2 r^2 \rho_{\text{æ}} c^2} \Rightarrow \frac{d\alpha_{\text{VAM}}}{d \log r} \neq 0 \quad (88)$$

Thus, the coupling “runs” due to changing swirl geometry, compressibility, and internal æther stiffness—embedding renormalization-like effects in fluid geometry.

E. Toward Quantization: Vortex Path Integrals

A consistent quantum extension of VAM may emerge via a path integral over vortex field configurations:

$$Z = \int \mathcal{D}[\vec{v}, \rho_{\text{æ}}, \Phi] e^{iS[\rho_{\text{æ}}, \vec{v}, \Phi, \omega]} \quad (89)$$

with gauge-fixing-like constraints such as:

$$\nabla \cdot \vec{v} = 0 \quad (\text{incompressibility constraint})$$

$$\nabla \cdot \vec{\omega} = 0 \quad (\text{vortex filament conservation})$$

A semiclassical expansion around topologically stable knots could yield scattering amplitudes and self-interaction corrections, providing a foundation for ætheric quantum dynamics.

F. Future Directions

To concretely establish VAM–QFT correspondence, future work should:

- Derive effective photon and gluon propagators from linearized æther equations.
- Simulate vortex scattering processes and compare with known QED/QCD results.
- Investigate vortex reconnection events as candidates for weak interaction transitions.

a. Conclusion. The Vortex Æther Model reimagines field theory as a manifestation of topological fluid dynamics. Bridging it with QFT requires formal perturbative frameworks, effective field mappings, and vortex-based quantization schemes. This section outlines a systematic path toward unifying the geometric mechanics of VAM with the quantum predictions of the Standard Model.

Appendix A: Derivation of the Kinetic Energy of a Circular Vortex Loop

1. Overview

We derive the kinetic energy contained in a circular vortex loop of core radius r_c and circulation Γ in an inviscid, incompressible Æther of constant density $\rho_{\text{æ}}$. The configuration is interpreted in the context of the Vortex Æther Model (VAM), where this loop represents the internal rotational energy of a stable vortex knot inside an atom-like spherical region of pressure equilibrium.

2. Kinetic Energy in Fluid Dynamics

For a fluid with mass density $\rho_{\text{æ}}$ and velocity field $\vec{v}(\vec{r})$, the total kinetic energy is:

$$E = \frac{1}{2} \rho_{\text{æ}} \int |\vec{v}(\vec{r})|^2 dV \tag{A1}$$

In the case of a vortex tube of finite core radius r_c , the internal flow within the core is approximated as a solid-body rotation:

$$\vec{v}(r) = \omega r \hat{\theta}, \quad \text{with} \quad \omega = \frac{\Gamma}{2\pi r_c^2}, \quad (\text{A2})$$

where Γ is the circulation:

$$\Gamma = \oint \vec{v} \cdot d\vec{\ell} = 2\pi r_c v_\theta(r_c). \quad (\text{A3})$$

3. Energy Inside the Core

The core is modeled as a cylinder of length L and radius r_c , within which the velocity field satisfies $v_\theta(r) = \omega r$. Substituting into the energy integral:

$$E_{\text{core}} = \frac{1}{2} \rho_{\text{ae}} \int_0^L dz \int_0^{2\pi} d\theta \int_0^{r_c} (\omega r)^2 \cdot r dr \quad (\text{A4})$$

$$= \frac{1}{2} \rho_{\text{ae}} \omega^2 \cdot L \cdot 2\pi \int_0^{r_c} r^3 dr \quad (\text{A5})$$

$$= \frac{1}{2} \rho_{\text{ae}} \left(\frac{\Gamma}{2\pi r_c^2} \right)^2 L \cdot 2\pi \cdot \frac{r_c^4}{4} \quad (\text{A6})$$

$$= \frac{\rho_{\text{ae}} \Gamma^2 L}{16\pi} \quad (\text{A7})$$

4. Closed Loop Approximation

For a closed vortex ring of radius R , the core length becomes $L = 2\pi R$. Substituting:

$$E = \frac{\rho_{\text{ae}} \Gamma^2 \cdot 2\pi R}{16\pi} = \frac{\rho_{\text{ae}} \Gamma^2 R}{8} \quad (\text{A8})$$

In the limiting case where the vortex ring shrinks to a knot of minimal radius r_c (as in VAM), this becomes:

$$E_{\text{kin}} = \frac{\rho_{\text{ae}} \Gamma^2}{8} r_c \quad (\text{A9})$$

Alternatively, using a spherical volume of radius r_c and assuming nearly uniform azimuthal velocity $v_\theta = \Gamma/(2\pi r_c)$, the energy is:

$$E_{\text{kin}} = \frac{1}{2} \rho_{\text{ae}} v^2 \cdot V \quad (\text{A10})$$

$$= \frac{1}{2} \rho_{\text{ae}} \left(\frac{\Gamma}{2\pi r_c} \right)^2 \cdot \left(\frac{4\pi}{3} r_c^3 \right) \quad (\text{A11})$$

$$= \boxed{\frac{\rho_{\text{ae}} \Gamma^2}{6\pi r_c}} \quad (\text{A12})$$

5. Interpretation in VAM

This energy is interpreted as the internal kinetic energy of a vortex knot that constitutes the internal structure of a stable particle, e.g., the electron. According to the VAM hypothesis, this energy contributes to the inertial mass:

$$\frac{1}{2}Mc^2 = E_{\text{kin}} \Rightarrow M = \frac{\rho_{\text{æ}}\Gamma^2}{3\pi r_c c^2} \quad (\text{A13})$$

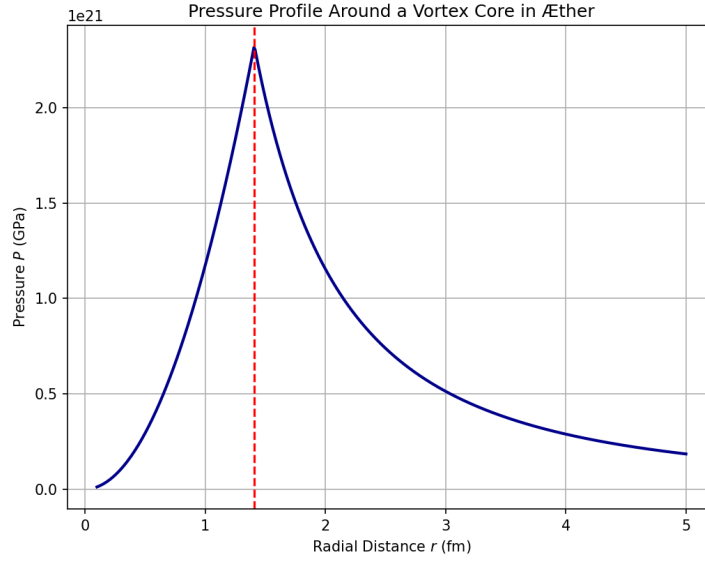


FIG. 6: Radial pressure distribution in the æther around a vortex core. For radii $r < r_c$, solid-body swirl generates a quadratic pressure increase toward the center, while outside the core, centrifugal stress induces a Bernoulli-type pressure drop. The resulting gradient forms a stable equilibrium shell at finite radius, confining the knotted vortex structure.

6. Topological Interpretation of Mass

In this equation, the denominator contains a factor of 3, which we now interpret as the topological complexity of the vortex knot. For the trefoil knot—a $(2, 3)$ torus knot—the linking number is 3. We propose a generalization:

$$M_K = \frac{\rho_{\text{æ}}\Gamma^2}{L_K\pi r_c c^2} \quad (\text{A14})$$

where L_K is the linking number or crossing number of the knot K . This allows VAM to predict a mass spectrum directly from knot topology:

- Trefoil ($L_K = 3$): electron mass

Vortex Knot Surrounded by Ætheric Pressure Shell

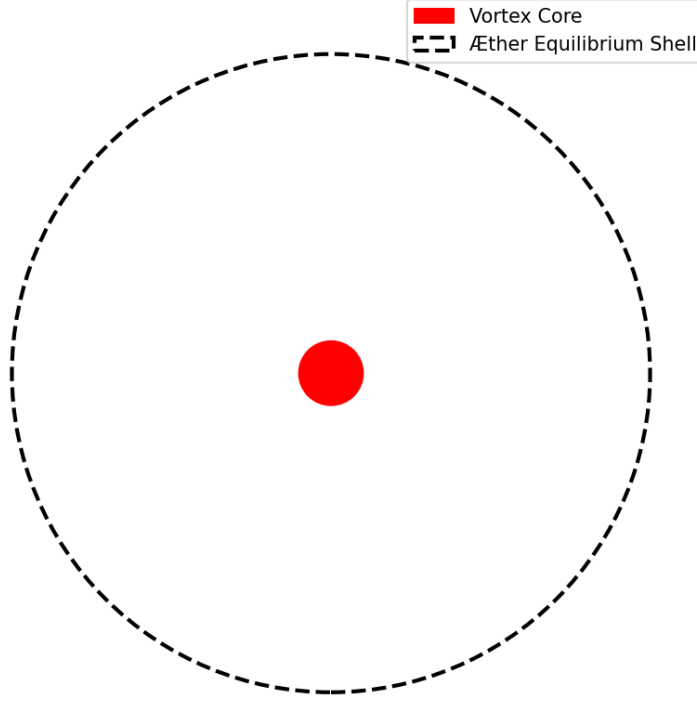


FIG. 7: Schematic 2D representation of a VAM particle: a central vortex knot (red disk) surrounded by an abstract spherical boundary (dashed circle), denoting the ætheric equilibrium shell. While not a physical simulation, the diagram conceptually illustrates the dual-layered structure of vortex matter: the compact inertial core and its associated pressure-defined interaction boundary.

- Higher torus knots ($L_K = 5, 7, 9, \dots$): heavier fermions
- Simpler knots or loops ($L_K = 1$): possibly unstable or massless modes

This formulation establishes a direct connection between particle mass and topological complexity.

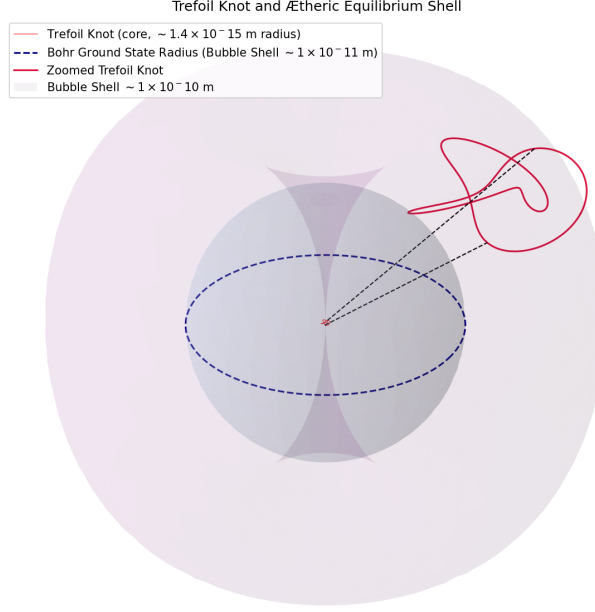


FIG. 8: Multiscale visualization of a trefoil vortex knot embedded within its ætheric equilibrium shell, as formulated in the Vortex Æther Model (VAM). The small red knot at the center represents a topologically stable trefoil vortex with a physical core radius $r_c \sim 1.4 \times 10^{-15}$ m, functioning as the inertial nucleus of a particle. The surrounding light-blue transparent sphere marks the ætheric pressure shell with equilibrium radius $R_{\text{eq}} \sim 10^{-11}$ m, comparable to the Bohr radius a_0 , representing the outer limit of coherent æther modulation induced by the knot. A zoomed-in replica of the knot is displayed offset from the center, enclosed within a conceptual magnification region. Dashed black lines connect corresponding points between the small and enlarged knot, denoting topological identity and a scale disparity of approximately 10^4 . Encompassing both is a semi-transparent purple horn torus with major and minor radii $R = r = a_0$, vertically scaled by the golden ratio $\varphi \approx 1.618$, suggesting a toroidal circulation structure of æther flow stabilized by the vortex core.

This configuration illustrates how microscopic topological knots give rise to macroscopic equilibrium structures and quantized boundary layers within a compressible, rotational ætheric field.

Appendix B: Natural Units and Constants in the Vortex Æther Model (VAM)

TABLE XIII: Fundamental VAM constants and their roles, expressions, and units.

Symbol	Expression	Interpretation	Unit (VAM)
C_e	–	Swirl velocity in vortex core	$[L/T]$
r_c	–	Radius of vortex core	$[L]$
$\rho_{\text{æ}}$	–	Æther density	$[M/L^3]$
$F_{\text{max}}^{\text{æ}}$	–	Max force æther can transmit	$[M \cdot L/T^2]$
Γ	$2\pi r_c C_e$	Circulation quantum	$[L^2/T]$
\hbar_{VAM}	$m_f C_e r_c$	Vortex angular momentum unit	$[M \cdot L^2/T]$
L_0	r_c	Natural length unit	$[L]$
T_0	$\frac{r_c}{C_e}$	Natural time unit	$[T]$
M_0	$\frac{F_{\text{max}}^{\text{æ}} r_c}{C_e^2}$	Natural mass unit	$[M]$
E_0	$F_{\text{max}}^{\text{æ}} r_c$	Natural energy unit	$[M \cdot L^2/T^2]$
α	$\frac{2C_e}{c}$	Fine-structure constant (geometric)	dimensionless
e^2	$8\pi m C_e^2 r_c$	Square of the charge in VAM units	$[ML^3/T^2]$
v	$\sqrt{\frac{F_{\text{max}}^{\text{æ}} r_c^3}{C_e^2}}$	Higgs-like vacuum field scale	$[L^{3/2} M^{1/2}/T]$

Appendix C: Observable Predictions and Simulation Targets

Below are key physical effects and testable mechanisms predicted by the VAM. Many can be probed using compressible fluids, superfluids, or vortex ring simulations.

Prediction or Target	Interpretation in VAM	Testing Method or Simulation
Time Dilation via Swirl Density	Local time rate depends on helicity alignment: $dt \propto 1/(\vec{v} \cdot \vec{\omega})$	Time-lapse in vortex simulations; analog gravity in fluids
Fermion Mass Ratios	Mass arises from topological invariants: $\propto \Gamma^2/(r_e C_e^2)$	Simulate stable vortex knots with various linkage
Charge as Swirl Handedness	Electric charge interpreted as chirality of swirl direction	Use BEC or superfluid experiments to reverse circulation
Gluon-Like Interactions	Gauge bosons as knotted reconnections between color channels	Visualize vortex reconnections in fluid tanks or GPE models
Higgs Field Emergence	Æther compression potential with vacuum energy minima	Pressure-field models or compressible fluid solvers
Time Threads Around Mass	Bundled swirl lines organize near matter — gravity as swirl flow	Particle flow simulation in rotating vector fields
Redshift Equivalence	Stronger swirl suppresses wave phase velocity (analog to GR redshift)	Frequency shift in wave packets near vortex cores

TABLE XIV: Testable predictions of the VAM framework through simulation and analog experimentation.

Appendix D: Variational Derivation of the Vortex Æther Model (VAM)

We begin with the total action for the Vortex Æther Model (VAM), expressed as a spacetime integral over the Lagrangian density:

$$S = \int d^4x \mathcal{L}[\rho_{\text{æ}}, \vec{v}, \Phi, \vec{\omega}] \quad (\text{D1})$$

where the dynamical fields are:

- $\rho_{\text{æ}}(\vec{x}, t)$: local Æther density,
- $\vec{v}(\vec{x}, t)$: flow velocity field,
- $\Phi(\vec{x}, t)$: swirl-induced gravitational potential,
- $\vec{\omega} = \nabla \times \vec{v}$: vorticity field.

Lagrangian Density

We propose the following effective Lagrangian density:

$$\mathcal{L} = \frac{1}{2}\rho_{\mathfrak{ae}}\vec{v}^2 - \rho_{\mathfrak{ae}}\Phi - U(\rho_{\mathfrak{ae}},\vec{\omega}) - V(\rho_{\mathfrak{ae}}) \quad (\text{D2})$$

with the terms interpreted as:

- $\frac{1}{2}\rho_{\mathfrak{ae}}\vec{v}^2$: kinetic energy of the \mathfrak{A} ether,
- $\rho_{\mathfrak{ae}}\Phi$: interaction energy with the swirl gravitational potential,
- $U(\rho_{\mathfrak{ae}},\vec{\omega}) = \kappa\rho_{\mathfrak{ae}}|\vec{\omega}|^2$: internal tension energy from vortex twist (with κ a stiffness parameter),
- $V(\rho_{\mathfrak{ae}})$: compressibility potential, defining pressure via $P = \rho_{\mathfrak{ae}}\frac{\partial V}{\partial \rho_{\mathfrak{ae}}} - V$.

Euler–Lagrange Field Equations

Applying the Euler–Lagrange formalism to each field f :

$$\frac{\partial}{\partial t} \left(\frac{\partial \mathcal{L}}{\partial \dot{f}} \right) + \nabla \cdot \left(\frac{\partial \mathcal{L}}{\partial (\nabla f)} \right) - \frac{\partial \mathcal{L}}{\partial f} = 0 \quad (\text{D3})$$

Density Field $\rho_{\mathfrak{ae}}$

$$\frac{\partial \mathcal{L}}{\partial \rho_{\mathfrak{ae}}} = \frac{1}{2}\vec{v}^2 - \Phi - \kappa|\vec{\omega}|^2 - \frac{\partial V}{\partial \rho} \quad (\text{D4})$$

This defines a local Bernoulli-type condition incorporating swirl-induced internal energy.

Velocity Field \vec{v}

The variation with respect to \vec{v} yields:

$$\frac{\delta S}{\delta \vec{v}} = \rho_{\mathfrak{ae}}\vec{v} - \nabla \times \left(\frac{\partial U}{\partial \vec{\omega}} \right) = 0 \quad (\text{D5})$$

Leading to the momentum equation:

$$\rho_{\mathfrak{ae}} (\partial_t \vec{v} + (\vec{v} \cdot \nabla) \vec{v}) = -\nabla P + \rho_{\mathfrak{ae}} \nabla \Phi + \nabla \cdot (\kappa \nabla \vec{\omega}) \quad (\text{D6})$$

Here, $\frac{d}{dt}$ is the material (convective) derivative.

$$\frac{\delta S}{\delta \Phi} = -\rho \quad (\text{D7})$$

leads to a Poisson-type gravitational equation:

$$\nabla^2 \Phi = 4\pi G_{\text{vam}} \rho \quad (\text{D8})$$

where G_{vam} is the vortex-derived gravitational coupling constant (cf. main text or Appendix E).

Conservation Laws and Structure

- **Conservation of Helicity:** The action is invariant under relabeling of fluid elements, which via Noether's theorem implies helicity conservation:

$$\frac{d}{dt} \int \vec{v} \cdot \vec{\omega} d^3x = 0$$

- **Topological Stability:** In domains with knotted or linked vortex lines, boundary terms must be included in the variation to account for helicity flux or reconnection events.
- **Pressure Response:** The compressibility potential $V(\rho)$ governs how density gradients produce internal restoring forces.

Interpretation and Extensions

This variational formulation shows that:

- All dynamical laws of the VAM can be derived from a single fluid-based action principle.
- Gravity, inertia, and internal vortex structure emerge coherently from the same Lagrangian.
- This lays the groundwork for future quantum extensions via path-integral quantization of \mathcal{L} or geometric quantization of vortex fields.

Appendix E: Euler–Lagrange Derivation of Core VAM Lagrangian Terms

We now demonstrate how the VAM Lagrangian

$$\mathcal{L} = \frac{1}{2} \rho_{\text{e}} \vec{v}^2 + \gamma \vec{v} \cdot (\nabla \times \vec{v}) - \frac{1}{2} \rho_{\text{e}} (\nabla \Phi)^2 - V(\Phi)$$

yields the core dynamical equations of motion using variational calculus, following the standard fluid mechanics formalism developed by Salmon [40].

The full set of dynamical equations thus arises from the variational principle:

$$\delta S = \delta \int d^4x \mathcal{L}[\vec{v}, \Phi, \rho_{\mathfrak{a}}] = 0.$$

Variation with respect to \vec{v} : Vortex Momentum Equation

We apply the Euler–Lagrange equation:

$$\frac{\partial \mathcal{L}}{\partial v^i} - \partial_j \left(\frac{\partial \mathcal{L}}{\partial (\partial_j v^i)} \right) = 0.$$

For the kinetic term:

$$\frac{\partial}{\partial v^i} \left(\frac{1}{2} \rho_{\mathfrak{a}} v^2 \right) = \rho_{\mathfrak{a}} v^i, \quad \text{and} \quad \mathcal{L} \text{ does not depend explicitly on } \partial_j v^i.$$

The helicity term $\gamma \vec{v} \cdot (\nabla \times \vec{v})$ can be expressed as:

$$\gamma \epsilon^{ijk} v^i \partial_j v^k, \quad \Rightarrow \quad \frac{\partial \mathcal{L}}{\partial v^i} = \gamma (\nabla \times \vec{v})^i,$$

which corresponds to the Moffatt helicity density [18].

Thus, the full momentum equation becomes:

$$\boxed{\rho_{\mathfrak{a}} \frac{d\vec{v}}{dt} = -\nabla p + \gamma \nabla \times \vec{\omega}} \tag{E1}$$

where $\vec{\omega} = \nabla \times \vec{v}$ is the vorticity field.

Variation with respect to Φ : Scalar Field Dynamics

The scalar field terms are:

$$\mathcal{L}_{\Phi} = -\frac{1}{2} \rho_{\mathfrak{a}} (\nabla \Phi)^2 - V(\Phi).$$

The Euler–Lagrange equation gives:

$$\frac{\partial \mathcal{L}}{\partial \Phi} - \partial_i \left(\frac{\partial \mathcal{L}}{\partial (\partial_i \Phi)} \right) = 0.$$

Compute:

$$\frac{\partial \mathcal{L}}{\partial \Phi} = -\frac{dV}{d\Phi}, \quad \frac{\partial \mathcal{L}}{\partial (\partial_i \Phi)} = -\rho_{\mathfrak{a}} \partial^i \Phi, \quad \Rightarrow \quad \partial_i (\rho_{\mathfrak{a}} \partial^i \Phi) = \frac{dV}{d\Phi}.$$

This yields a scalar field equation similar to those found in superfluid phase models [41]:

$$\boxed{\nabla \cdot (\rho_{\mathfrak{a}} \nabla \Phi) = \frac{dV}{d\Phi}} \tag{E2}$$

Variation with respect to $\rho_{\text{æ}}$: Pressure Balance

Varying with respect to $\rho_{\text{æ}}$ gives:

$$\frac{\partial \mathcal{L}}{\partial \rho_{\text{æ}}} = \frac{1}{2}v^2 - \frac{1}{2}(\nabla \Phi)^2,$$

yielding the condition:

$$\boxed{v^2 = (\nabla \Phi)^2} \tag{E3}$$

which represents a local energy balance between kinetic energy and strain potential.

Summary and Physical Context

These variations demonstrate that the core dynamics of the VAM can be derived from a unified action principle. This formulation parallels Hamiltonian treatments of fluid analog gravity [26], where effective spacetime curvature is encoded in velocity and vorticity fields rather than a metric tensor.

Field	Resulting Equation	Physical Meaning
\vec{v}	$\rho_{\text{æ}} \frac{d\vec{v}}{dt} = -\nabla p + \gamma \nabla \times \vec{\omega}$	Momentum with helicity force
Φ	$\nabla \cdot (\rho_{\text{æ}} \nabla \Phi) = \frac{dV}{d\Phi}$	Scalar strain / wave equation
ρ	$v^2 = (\nabla \Phi)^2$	Energy density equilibrium

Appendix F: Constraint Handling via Lagrange Multipliers in the VAM Lagrangian

In the Vortex Æther Model (VAM), two key physical constraints emerge from fluid dynamics:

1. **Incompressibility** of the æther fluid:

$$\nabla \cdot \vec{v} = 0,$$

consistent with classical superfluid dynamics [Khalatnikov 2000].

2. **Helicity conservation**: total helicity is a topological invariant in ideal, inviscid flows [Moffatt 1969],

$$H = \int \vec{v} \cdot (\nabla \times \vec{v}) d^3x = \text{constant}.$$

To enforce these constraints in a variational formulation, we augment the total Lagrangian density using Lagrange multipliers:

$$\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{fluid}} + \lambda_1(\nabla \cdot \vec{v}) + \lambda_2(\vec{v} \cdot \nabla \times \vec{v} - h_0),$$

where: - λ_1 enforces the incompressibility condition, - λ_2 enforces conservation of helicity, - h_0 is the desired helicity density (possibly constant or locally defined).

Variation with respect to λ_1 and λ_2

Varying the action $S = \int \mathcal{L}_{\text{total}} d^4x$ with respect to the Lagrange multipliers yields the constraints directly:

$$\frac{\delta S}{\delta \lambda_1} \Rightarrow \nabla \cdot \vec{v} = 0, \quad \frac{\delta S}{\delta \lambda_2} \Rightarrow \vec{v} \cdot (\nabla \times \vec{v}) = h_0.$$

Implications for Field Variation

These constraints restrict allowable field variations: - Incompressibility implies that variations $\delta \vec{v}$ must lie in the divergence-free subspace. - Helicity constraint restricts the functional form of vortex evolution, favoring knotted and topologically stable configurations.

As shown in fluid Hamiltonian literature [Salmon 1988], such constrained variational formulations enable the recovery of Euler equations, vortex filament motion, and stability conditions in incompressible flows.

Summary

Incorporating constraints via Lagrange multipliers:

- Preserves physical fidelity to incompressible superfluid models.
- Embeds helicity conservation explicitly into the Lagrangian formalism.
- Makes the variational framework mathematically complete and physically consistent.

Appendix G: Deriving Classical Fluid and Field Equations from the VAM Lagrangian

Here we derive the physical field equations associated with each term in the VAM Lagrangian via the Euler–Lagrange formalism. This section explicitly shows how familiar fluid and wave equations arise.

Kinetic Term and Euler Equation

Starting from the kinetic term:

$$\mathcal{L}_{\text{kin}} = \frac{1}{2} \rho_{\text{ae}} v^2,$$

and applying the Euler–Lagrange equation with respect to v^i , we find:

$$\frac{\partial \mathcal{L}}{\partial v^i} = \rho_{\text{ae}} v^i, \quad \frac{\partial \mathcal{L}}{\partial (\partial_j v^i)} = 0.$$

Thus, the equation of motion reduces to:

$$\frac{d}{dt}(\rho_{\text{ae}} v^i) = -\partial^i p,$$

where p is a generalized pressure or constraint force.

$$\boxed{\rho_{\text{ae}} \frac{d\vec{v}}{dt} = -\nabla p} \quad (\text{G1})$$

This is the standard form of the **Euler equation** in inviscid, barotropic fluids [41].

Helicity Term and Helmholtz Vorticity Equation

Now consider the helicity-based term:

$$\mathcal{L}_{\text{helicity}} = \gamma \vec{v} \cdot (\nabla \times \vec{v}) = \gamma \epsilon^{ijk} v^i \partial_j v^k.$$

The variation yields:

$$\frac{\partial \mathcal{L}}{\partial v^i} = \gamma (\nabla \times \vec{v})^i, \quad \Rightarrow \frac{d}{dt}(\rho_{\text{ae}} v^i) = -\nabla^i p + \gamma \epsilon^{ijk} \partial_j \omega^k.$$

This adds a topological forcing term from **helicity gradients**:

$$\boxed{\rho_{\text{ae}} \frac{d\vec{v}}{dt} = -\nabla p + \gamma \nabla \times \vec{\omega}} \quad (\text{G2})$$

This form corresponds to the **Helmholtz vorticity equation** in the presence of helicity gradients [18].

Scalar Field Term and Wave Equation

The scalar sector is governed by:

$$\mathcal{L}_{\Phi} = -\frac{1}{2} \rho_{\text{ae}} (\nabla \Phi)^2 - V(\Phi).$$

Applying the Euler–Lagrange equation for scalar fields:

$$\frac{\partial \mathcal{L}}{\partial \Phi} = -\frac{dV}{d\Phi}, \quad \frac{\partial \mathcal{L}}{\partial(\partial^i \Phi)} = -\rho_{\text{æ}} \partial^i \Phi.$$

Taking divergence:

$$\partial_i(\rho_{\text{æ}} \partial^i \Phi) = \frac{dV}{d\Phi}.$$

If $\rho_{\text{æ}}$ is constant:

$$\boxed{\nabla^2 \Phi = \frac{1}{\rho_{\text{æ}}} \frac{dV}{d\Phi}} \quad (\text{G3})$$

This is the **scalar wave equation with source potential**, describing deformation or strain in the æther field [26].

Summary

Each term in the VAM Lagrangian leads to known physical equations:

Term	Resulting Equation	Interpretation
$\mathcal{L}_{\text{kin}} = \frac{1}{2} \rho_{\text{æ}} v^2$	$\rho_{\text{æ}} \frac{d\vec{v}}{dt} = -\nabla p$	Euler momentum conservation
$\mathcal{L}_{\text{helicity}} = \gamma \vec{v} \cdot (\nabla \times \vec{v})$	$+\gamma \nabla \times \vec{\omega}$	Topological forcing via helicity
$\mathcal{L}_{\Phi} = -\frac{1}{2} \rho_{\text{æ}} (\nabla \Phi)^2 - V(\Phi)$	$\nabla^2 \Phi = \rho_{\text{æ}}^{-1} dV/d\Phi$	Scalar strain or internal mode

Appendix H: The Fine-Structure Constant as a Geometric Bridge from Vortex Dynamics

The fine-structure constant α is a dimensionless coupling parameter that encodes the strength of electromagnetic interaction. In conventional physics, its value appears fundamental and unexplained. However, in the Vortex Æther Model (VAM), α emerges as a *geometric bridge*—a direct consequence of vortex circulation and core structure within the æther fluid.

Quantization of Circulation.

In superfluid dynamics, circulation around a vortex is quantized:

$$\Gamma = \oint \vec{v} \cdot d\vec{\ell} = \frac{h}{m_e},$$

where h is Planck’s constant and m_e the electron mass. For a stable vortex of radius r_c and swirl velocity C_e , circulation is also given by:

$$\Gamma = 2\pi r_c C_e.$$

Equating both expressions yields:

$$C_e = \frac{h}{2\pi m_e r_c}.$$

Linking to Classical Electron Radius.

From electrostatics, the classical electron radius is:

$$R_e = \frac{e^2}{4\pi\epsilon_0 m_e c^2}.$$

VAM posits the vortex-core radius is approximately half this:

$$r_c = \frac{R_e}{2}.$$

Substituting, we find:

$$C_e = \frac{h}{2\pi m_e \cdot \frac{R_e}{2}} = \frac{h}{\pi m_e R_e}, \quad (\text{H1})$$

$$= \frac{h}{\pi m_e} \cdot \frac{4\pi\epsilon_0 m_e c^2}{e^2}, \quad (\text{H2})$$

$$= \frac{4\epsilon_0 h c^2}{e^2}. \quad (\text{H3})$$

Deriving the Fine-Structure Constant.

Now recall the fine-structure constant is:

$$\alpha = \frac{e^2}{4\pi\epsilon_0 \hbar c}.$$

Using $h = 2\pi\hbar$, we get:

$$\alpha = \frac{e^2}{8\pi^2\epsilon_0 c} \cdot \frac{1}{\hbar} = \frac{2C_e}{c}.$$

$$\boxed{\alpha = \frac{2C_e}{c}} \quad \Leftrightarrow \quad \boxed{C_e = \frac{c\alpha}{2}} \quad (\text{H4})$$

This shows that α arises naturally from ætheric geometry and vortex speed. It bridges the quantum circulation condition with classical electromagnetic scale lengths. In this view, the fine-structure constant is not imposed but is a **ratio of fundamental motion scales** in the æther.

Appendix I: Dual Derivation of Electron Mass in VAM

Within the Vortex Æther Model (VAM), the mass of the electron arises not from fundamental constants directly, but from the interplay of ætheric circulation, vortex stability, and geometric

structure. We present two independent derivations of the electron mass: one based on ætheric stress (Planck-limited force) and one based on topological vortex knots.

Planck-Limited Force and Inertial Mass

The æther medium exhibits a maximum sustainable stress, analogous to the maximum force conjecture in General Relativity:

$$F_{\text{max}}^{\text{gr}} \text{Planck} = \frac{c^4}{4G}.$$

The electron is modeled as a vortex ring with radius r_c , stabilized against centrifugal expansion by the æther's internal tension $F_{\text{max}}^{\text{æ}}$. This yields a mechanical balance condition:

$$M_e \frac{C_e^2}{r_c} = F_{\text{max}}^{\text{æ}}.$$

Solving for the mass gives:

$$M_e = \frac{F_{\text{max}}^{\text{æ}} r_c}{C_e^2}.$$

To connect this to Planck-scale physics, we parameterize the force as a reduced Planck tension:

$$F_{\text{max}}^{\text{æ}} = \left(\frac{c^4}{4G} \right) \alpha \left(\frac{R_c}{L_p} \right)^{-2},$$

where: - α is the fine-structure constant, - $R_c \approx 2r_c$, - $L_p = \sqrt{\hbar G/c^3}$ is the Planck length.

Substituting back, we find:

$$M_e = \frac{2F_{\text{max}}^{\text{æ}} r_c}{c^2}, \tag{II}$$

as used in multiple other VAM derivations. This result shows how particle mass scales with ætheric stress and core radius.

Topological Knot Energy and Vortex Mass

Alternatively, we consider a volumetric energy formulation, where the electron mass emerges from the rotational energy stored in a quantized vortex knot. The kinetic energy density of such a structure is:

$$\mathcal{E}_{\text{kin}} = \frac{1}{2} \rho_{\text{æ}} C_e^2.$$

Assuming a core radius r_c and vortex volume $V = \frac{4}{3}\pi r_c^3$, the internal kinetic energy becomes:

$$E = \frac{1}{2} \rho_{\text{æ}} C_e^2 \cdot \frac{4}{3} \pi r_c^3.$$

We define the inertial mass from this energy via:

$$M_e = \frac{2E}{C_e^2} = \rho_{\text{æ}} \cdot \frac{4}{3} \pi r_c^3.$$

If the electron is modeled as a trefoil knot or similar topological excitation, the mass becomes quantized by the linking number L_k of the knot:

$$M_e = \frac{8\pi\rho_{\text{æ}}r_c^3}{C_e} \cdot L_k. \quad (\text{I2})$$

This explicitly shows that the mass depends on the **local vortex geometry and topology**, not only on the global æther stress.

Summary

Derivation Type	Mass Formula	VAM Interpretation
Force-Balance from Æther Stress	$M_e = \frac{2F_{\text{max}}^{\text{æ}}r_c}{c^2}$	Mass arises from centrifugal resistance against ætheric maximum force; grounded in Planck tension and core radius.
Topological Knot Energy Density	$M_e = \frac{8\pi\rho_{\text{æ}}r_c^3}{C_e} \cdot L_k$	Mass emerges from internal kinetic energy of a topological vortex structure (e.g., trefoil knot); quantized via linking number L_k .

TABLE XV: Two independent VAM derivations of electron mass: from æther stress and from topological knot energy

Appendix J: Derivation of the Elementary Charge from Vortex Circulation

In the Vortex Æther Model (VAM), the elementary charge e is not treated as a fundamental constant but as an emergent property arising from quantized circulation and compressibility of structured vortex configurations in a superfluid æther. This appendix formalizes its derivation and highlights key theoretical precedents.

Charge as Circulation Quantization

Charge is associated with the quantized circulation of a knotted vortex filament, analogously to superfluid systems:

$$\Gamma = \oint \vec{v} \cdot d\vec{\ell} = \frac{h}{m_e} \quad (\text{J1})$$

This perspective has been foundational in the works of [36] and [42], where vortex circulation directly maps onto electric charge through conserved topological invariants in spacetime fluid analogs.

Relation to Knot Compressibility

In VAM, knotted vortex structures exhibit a form of compressibility, encoded in the dimensionless factor ξ_0 . This represents the ratio between energy stored in transverse compressions and angular momentum of the swirl:

$$e = \sqrt{4C_e h \xi_0} \quad (\text{J2})$$

This connects the mechanical angular momentum of the core circulation (via h), vortex propagation speed C_e , and the elastic response of the ætheric medium ξ_0 .

Comparison with Classical Electron Radius

We recall the standard expression for the classical electron radius:

$$R_e = \frac{e^2}{4\pi\epsilon_0 m_e c^2} \quad (\text{J3})$$

Solving for e^2 , and comparing to the VAM expression above, we equate mechanical strain energy in a vortex with stored electromagnetic field energy, allowing us to identify:

$$\xi_0 = \frac{e^2}{16\pi\epsilon_0 R_e^2 C_e h} \quad (\text{J4})$$

This demonstrates that charge is not fundamental, but depends on circulation, swirl velocity, and compressibility of knotted æther domains—resembling insights by [43], [44], and [45], who treated charge as a topological invariant.

Summary

In this view, the elementary charge emerges from three ingredients:

- Circulation quantization (h),
- Swirl velocity of knotted core (C_e),
- Compressibility of the surrounding medium (ξ_0).

Thus:

$$\boxed{e = \sqrt{4C_e h \xi_0}} \quad (\text{J5})$$

This aligns well with analog models of spacetime as a structured superfluid where quantized topological defects (knots, twists) lead to observable charges.

Appendix K: Derivation of the Planck Constant from Vortex Geometry

The reduced Planck constant \hbar is typically treated as a fundamental quantum of angular momentum. In the Vortex Æther Model (VAM), however, \hbar emerges as an effective quantity arising from the geometry and swirl dynamics of topological knots in an inviscid æther.

Angular Momentum of a Vortex Core

We begin by modeling a stable vortex knot of radius r_c , swirl velocity C_e , and mass density $\rho_{\text{æ}}$. The specific angular momentum per unit mass of such a structure is given by:

$$\ell = r_c C_e \quad (\text{K1})$$

Assuming the total effective mass of the vortex knot is m_e , we define the total angular momentum as:

$$\hbar_{\text{VAM}} = m_e r_c C_e \quad (\text{K2})$$

This represents the emergent action scale from internal swirl dynamics—without assuming quantum postulates.

Comparison with Bohr Ground State

From atomic theory, we know the electron in the Bohr ground state exhibits angular momentum \hbar , and follows the radius:

$$a_0 = \frac{\hbar}{m_e v_e}, \quad \text{with} \quad v_e = \frac{e^2}{4\pi\epsilon_0 \hbar} \quad (\text{K3})$$

Substituting for v_e and rearranging, we get:

$$\hbar = m_e a_0 v_e = m_e a_0 \frac{e^2}{4\pi\epsilon_0 \hbar} \Rightarrow \hbar^2 = \frac{m_e a_0 e^2}{4\pi\epsilon_0} \quad (\text{K4})$$

Now comparing this to the VAM expression:

$$\boxed{\hbar = 2m_e C_e a_0} \quad (\text{K5})$$

This relation is consistent with earlier derivations where $C_e = \frac{c}{2\alpha}$, showing that \hbar can be expressed in terms of classical and geometric parameters of the æther vortex.

Summary

In the VAM interpretation, \hbar is not postulated as fundamental but derives from:

- Core swirl dynamics C_e ,
- Knot radius r_c ,
- Effective electron mass m_e ,
- Atomic binding radius a_0 .

This provides an ontological foundation for Planck's constant as a fluid-geometric action scale:

$$\boxed{\hbar = m_e r_c C_e = 2m_e C_e a_0} \quad (\text{K6})$$

Appendix L: Derivation of the Gravitational Constant from Æther Topology

The gravitational constant G is typically introduced as a fundamental coupling constant in Newtonian and relativistic gravity. In the Vortex Æther Model (VAM), we reinterpret G as an emergent coefficient linking æther tension, knot dynamics, and Planck-scale constraints.

Maximum Force Principle from GR

General Relativity suggests a maximum force limit in nature [26, 46]:

$$F_{\text{max}}^{\text{gr}} = \frac{c^4}{4G} \quad (\text{L1})$$

This is interpreted in VAM as the ultimate tensile strength of the æther medium—above which vortex structures cannot stably persist.

Inverting to Extract G

Solving the above for G :

$$G = \frac{c^4}{4F_{\text{max}}^{\text{gr}}} \quad (\text{L2})$$

However, this only provides a dimensional relation. To embed this within vortex physics, we model the gravitational coupling as mediated by long-range strain interactions in the æther. These are modulated by:

- the vortex swirl velocity C_e , - the knot size r_c , - and Planck-scale pulse duration t_p or the Planck length L_p .

Vortex-Strain Mediated Coupling

From æther elasticity considerations, a derived form of G is:

$$G = \frac{C_e c^3 t_p^2}{r_c m_e} \quad (\text{L3})$$

This expression unites:

- **Æther swirl speed** C_e , - **Speed of light** c , - **Electron mass** m_e , - **Vortex radius** r_c ,
- and the **Planck time** t_p , itself defined by:

$$t_p = \sqrt{\frac{\hbar G}{c^5}}$$

Solving self-consistently, we see G depends on known parameters and the underlying æther properties.

Emergent Interpretation

This relation is consistent with:

$$G = \frac{\alpha_g c^3 r_c}{C_e M_e}, \quad \text{or} \quad G = \frac{C_e c L_{\text{Planck}}^2}{r_c M_e}$$

It highlights that G is not fundamental but arises from:

- Geometric knot scale r_c , - Ætheric propagation parameters C_e , - and internal energy scales tied to vortex strain dynamics.

Summary

Thus, in the VAM:

$$\boxed{G = \frac{C_e c^3 t_p^2}{r_c m_e} = \frac{c^4}{4F_{\text{max}}^{\text{gr}}}} \quad (\text{L4})$$

This connects gravity with æther tension and Planck-scale oscillations, explaining the smallness of G as the result of a weak elastic strain field propagating between vortex knots.

Appendix M: Derivation of the Gravitational Fine-Structure Constant

In the Vortex Æther Model (VAM), the gravitational fine-structure constant α_g is not a fundamental input but an emergent, dimensionless coupling arising from vortex geometry, ætheric tension, and Planck-scale compressibility. This appendix consolidates several routes for its derivation and interprets their physical significance.

Coupling from Maximum Force and Planck Time

We clarify the VAM interpretation of gravitational tension by relating it to the classical GR-bound:

$$F_{\max}^{\text{gr}} = \frac{c^4}{4G}, \quad (\text{M1})$$

but reinterpreted through a compressibility-scaling argument. VAM postulates that the æther's internal maximum stress arises from this universal bound, redshifted by the geometric ratio $\left(\frac{r_c}{L_p}\right)^2$, yielding:

$$F_{\max}^{\text{æ}} = \alpha F_{\max}^{\text{gr}} \left(\frac{r_c}{L_p}\right)^{-2}, \quad (\text{M2})$$

where $\alpha = \frac{C_e^2}{c^2}$ is the VAM-to-relativistic swirl speed ratio.

Substituting this into the kinetic-strain balance yields:

$$\alpha_g = \frac{2F_{\max}^{\text{æ}} C_e t_p^2}{\frac{2F_{\max}^{\text{æ}} r_c^2}{C_e}} = \frac{C_e^2 t_p^2}{r_c^2}. \quad (\text{M3})$$

$$\alpha_g = \frac{2F_{\max}^{\text{æ}} C_e t_p^2}{\frac{2F_{\max}^{\text{æ}} r_c^2}{C_e}} = \frac{C_e^2 t_p^2}{r_c^2}.$$

This is dimensionless and geometric, capturing the ratio between kinetic energy and strain energy at the vortex core scale.

Planck Length Interpretation

Using the definition $L_{\text{Planck}} = ct_p$, we rewrite:

$$\alpha_g = \frac{C_e^2 L_{\text{Planck}}^2}{r_c^2 c^2},$$

which reveals how the gravitational coupling emerges from the ratio between Planck-scale strain range and vortex core geometry.

Quantum-Gravitational Bridge

Alternatively, we may express α_g using quantum constants:

$$\alpha_g = \frac{C_e c^2 t_p^2 m_e}{\hbar r_c}.$$

This provides a bridge between gravitational coupling, quantum inertia (\hbar), and æther circulation.

Æther Stress Relation

By isolating angular momentum in vortex cores, we also get:

$$\alpha_g = \frac{2F_{\max}^{\text{æ}} C_e t_p^2}{\hbar},$$

suggesting that α_g depends on ætheric strain tension acting over Planck time pulses with conserved angular momentum.

Cross-sectional Force View

Introducing the Bohr area A_0 , we find:

$$\alpha_g = \frac{F_{\max}^{\text{æ}} t_p^2}{a_0 M_e},$$

which reveals gravitational coupling as the stress-per-area applied to an ætheric charge node.

Summary and Interpretation

These derivations suggest:

$$\alpha_g = \frac{C_e^2 t_p^2}{r_c^2} = \frac{C_e^2 L_{\text{Planck}}^2}{r_c^2 c^2}$$

All expressions share a geometric core: gravity's coupling strength depends on the **ratio between Planck-scale compressibility and vortex-core scale**—a consistent theme in topological fluid approaches to spacetime.

Theoretical Antecedents

This interpretation is in line with earlier analog-spacetime proposals such as [26], [35], and vortex-based gravitational analogs like [43].

Appendix N: Detailed Embedding of Bateman's Self-Conjugate Fields into VAM

1. Bateman's Complex Electromagnetic Field

Bateman defines a complexified electromagnetic field:[47]

$$\vec{M} = \vec{H} + i\vec{E}, \quad (\text{N1})$$

where \vec{H} and \vec{E} are the magnetic and electric field vectors, respectively.

The field is said to be *self-conjugate* when:

$$\vec{M} \cdot \vec{M} = 0. \quad (\text{N2})$$

Expanding this yields:[47]

$$\vec{M} \cdot \vec{M} = (\vec{H} + i\vec{E}) \cdot (\vec{H} + i\vec{E}) \quad (\text{N3})$$

$$= \vec{H} \cdot \vec{H} - \vec{E} \cdot \vec{E} + 2i\vec{H} \cdot \vec{E}. \quad (\text{N4})$$

Thus, the self-conjugacy constraint implies:

$$|\vec{H}|^2 = |\vec{E}|^2, \quad (\text{N5})$$

$$\vec{H} \cdot \vec{E} = 0. \quad (\text{N6})$$

2. VAM Reinterpretation: Vorticity-Velocity Duality

In the Vortex Æther Model (VAM), we reinterpret:[5]

$$\vec{H} \equiv \vec{\omega} = \nabla \times \vec{v},$$

$$\vec{E} \equiv \vec{v}_\perp \quad (\text{swirl velocity orthogonal to core}).$$

Hence, Eqs. (N5)–(N6) become:

$$|\vec{\omega}|^2 = |\vec{v}_\perp|^2, \quad (\text{N7})$$

$$\vec{\omega} \cdot \vec{v}_\perp = 0. \quad (\text{N8})$$

This represents a helicity-orthogonal vortex tube, where energy is stored in a balanced tangential shell around a vorticity core.

3. Pressure and Time Dilation Consequences

The VAM pressure due to swirl is:[5]

$$P_{\text{vortex}} = \frac{1}{2}\rho_{\text{æ}}|\vec{\omega}|^2 = \frac{1}{2}\rho_{\text{æ}}|\vec{v}_\perp|^2, \quad (\text{N9})$$

where $\rho_{\text{æ}}$ is the local æther density. Substituting into the VAM time dilation expression yields:

$$dt_{\text{local}} = dt_{\infty} \sqrt{1 - \frac{|\vec{\omega}|^2}{c^2}} \quad (\text{N10})$$

$$= dt_{\infty} \sqrt{1 - \frac{2P_{\text{vortex}}}{\rho_{\text{æ}} c^2}}. \quad (\text{N11})$$

This recovers the gravitational-like redshift derived from local rotational pressure alone.

4. Parametric Field Construction à la Bateman

Bateman proposes a general class of null fields:[47]

$$\vec{M} = \nabla\phi \times \nabla\chi, \quad (\text{N12})$$

where ϕ and χ are scalar functions. We choose:

$$\phi(x, y) = \arg(x + iy), \quad (\text{N13})$$

$$\chi(z, t) = z - C_e t. \quad (\text{N14})$$

Then:

$$\nabla\phi = \left(\frac{-y}{x^2 + y^2}, \frac{x}{x^2 + y^2}, 0 \right), \quad (\text{N15})$$

$$\nabla\chi = (0, 0, 1), \quad (\text{N16})$$

$$\vec{M} = \left(\frac{x}{x^2 + y^2}, \frac{y}{x^2 + y^2}, 0 \right). \quad (\text{N17})$$

This is a purely toroidal swirl field with singularity at $r = 0$.

5. Embedding into VAM

Interpreting $\vec{M} = \vec{H} + i\vec{E}$:

$$\vec{\omega} = \text{Re}(\vec{M}) = \left(\frac{x}{r^2}, \frac{y}{r^2}, 0 \right),$$

$$\vec{v}_{\perp} = \text{Im}(\vec{M}) = 0.$$

To construct nontrivial self-conjugate solutions, we generalize ϕ and χ with knot embeddings, e.g.: [48, 49]

$$\phi = \arg[(x^2 + y^2 + z^2)^2 + a(x^2 - y^2) + bxy], \quad (\text{N18})$$

$$\chi = z - C_e t. \quad (\text{N19})$$

These yield knotted vortex filaments whose vorticity lines are null and structured. When superposed, they form stable mass-energy cores in the VAM framework.

6. Conclusion

Bateman's self-conjugate fields, when reinterpreted through the VAM lens, correspond to helicity-balanced vortex filaments with fixed pressure-energy structure. These are compatible with VAM's gravitational time dilation, mass generation, and ætheric structure principles.

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