## Extending the Vortex Æther Model (VAM): Path-Integral Formulation, Gauge Theory, and Relativity Corrections

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#### Abstract

This paper extends the Vortex Æther Model (VAM) by incorporating a path-integral formulation, linking vorticity to gauge theory, and introducing a relativity correction based on vorticity gradients. The approach replaces traditional space-time curvature with vorticity-induced time dilation and establishes a topological field theory interpretation of quantum vortex dynamics. We present a Hamiltonian formalism, construct a path-integral for quantized vorticity, and explore implications for quantum field theory.

#### 1 Introduction

The Vortex Æther Model (VAM) proposes a fluid-dynamical foundation for matter, where protons and electrons exist as vortex knots within an incompressible, inviscid æther. We extend this idea by formalizing a Lagrangian-Hamiltonian approach, deriving a quantum path-integral, and linking vorticity evolution to gauge field dynamics.

### 2 Hamiltonian Formulation for Vorticity

The system is described by a five-dimensional vorticity field  $\Omega = \nabla_3 \times \mathbf{U}$ , where  $\mathbf{U}$  is the velocity potential. The Lagrangian density is:

$$\mathcal{L}_3 = \frac{1}{2} \rho_{\text{ex}} |\mathbf{\Omega}|^2 - P(\nabla_3 \cdot \mathbf{\Omega}) - \nu |\nabla_3 \mathbf{\Omega}|^2.$$
 (1)

Performing the Legendre transformation, the Hamiltonian density is obtained:

$$\mathcal{H}_3 = \frac{1}{2\rho_{\infty}} |\Pi_{\mathbf{\Omega}}|^2 + P(\nabla_3 \cdot \mathbf{\Omega}) + \nu |\nabla_3 \mathbf{\Omega}|^2.$$
 (2)

with canonical equations:

$$\frac{\partial \mathbf{\Omega}}{\partial t} = \frac{\delta \mathcal{H}_3}{\delta \Pi_{\mathbf{\Omega}}},\tag{3}$$

$$\frac{\partial \Pi_{\Omega}}{\partial t} = -\frac{\delta \mathcal{H}_3}{\delta \Omega}.\tag{4}$$

#### 3 Path-Integral Quantization of Vorticity

Following a field-theoretic approach, we define the partition function for vorticity:

$$Z = \int \mathcal{D}\Omega \, e^{iS[\Omega]/\hbar},\tag{5}$$

where the action is:

$$S = \int d^3x \left( \frac{1}{2} \rho_{\text{ee}} |\mathbf{\Omega}|^2 - P(\nabla_3 \cdot \mathbf{\Omega}) \right). \tag{6}$$

The constraint term  $P(\nabla_3 \cdot \Omega)$  ensures divergence-free vorticity.

#### 4 Gauge Theory Interpretation

Since  $\Omega = \nabla_3 \times \mathbf{U}$ , the system resembles a Yang-Mills gauge theory:

$$F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}. \tag{7}$$

Introducing a Chern-Simons term:

$$S_{CS} = k \int d^3x \, \epsilon^{\mu\nu\rho\sigma\lambda} A_{\mu} \partial_{\nu} A_{\rho} \partial_{\sigma} A_{\lambda}. \tag{8}$$

This encodes the topology of vortex knots and suggests quantized circulation.

# 5 Relativity Correction: Time Dilation from Vorticity

Instead of spacetime curvature, we propose time dilation from vorticity gradients:

$$d\tau = \frac{dt}{\sqrt{1 - \frac{\Omega^2}{c^2} e^{-r/r_c}}}.$$
(9)

Gravity is replaced by a Navier-Stokes-like pressure gradient:

$$\nabla^2 P = -\rho_{\text{ee}}(\nabla \times \mathbf{v})^2. \tag{10}$$

#### 6 Conclusion and Future Work

This work reformulates the Vortex Æther Model in a Hamiltonian and path-integral framework, linking it to gauge field theory and replacing gravity with vorticity-induced effects. Future directions include a numerical simulation of vortex quantization and deeper connections to string theory.