

Vortex Velocity and Stream Function

$$\begin{aligned}V_{\theta} &= \frac{\Gamma}{2\pi r} \\V_{\theta} &= -\frac{d\psi}{dr} \\V_r &= -\frac{1}{r} \frac{d\psi}{d\theta}\end{aligned}$$

Stream function:

$$\psi = \frac{\Gamma}{2\pi} \ln(r)$$

Potential function:

$$\phi = \frac{\Gamma}{2\pi} \theta$$

Circulation:

$$\begin{aligned}\Gamma &= \oint \mathbf{V} \cdot d\mathbf{s} = \iint_S (\nabla \times \mathbf{v}) \cdot \hat{n} dS \\ \Gamma &= \iint (u dx + v dy) = \int V \cos(\phi) ds\end{aligned}$$

Boyle's Law for Ideal Gases (Kinetic Theory)

$$pV = \frac{1}{3}T - \frac{1}{6}\rho \iiint (u^2 + v^2 + w^2)(x dy dz + y dz dx + z dx dy)$$

Newton's Potential around the Sun

$$\Phi = -\frac{GM}{r} + \frac{1}{6}\Delta c^2 r^2$$

Vacuum Energy Density Estimate

$$\frac{1}{V} \int \frac{1}{2} \hbar \omega \approx \frac{\hbar}{2\pi^2 c^3} \int_0^{\omega_{\max}} \omega^3 d\omega = \frac{\hbar}{2\pi^2 c^3} \omega_{\max}^4$$

Cosmological constant:

$$\Lambda \approx \frac{G^2 m^6}{\hbar^4}$$

Triple Integral Volume Identity

$$\int_S (x dy dz + y dz dx + z dx dy) = \iiint (1 + 1 + 1) dx dy dz = 3 \int_0^1 dx \int_0^1 dy \int_0^1 dz = \boxed{3}$$