

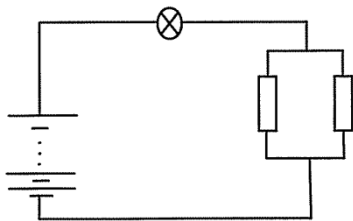
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b)  $\Delta m = m_{\text{Po}} - m_{\alpha} - m_{\text{Pb}} = (218,00897 - 4,002603 - 213,99980)u = 0,006567u = 1,09 \cdot 10^{-29} \text{kg}$   
 Frigjort energi:  $\Delta E = \Delta mc^2 = (1,09 \cdot 10^{-29} \cdot (3,00 \cdot 10^8)^2) \text{J} = \underline{9,81 \cdot 10^{-13} \text{J}}$

c)  $hf = E_4 - E_1 \Leftrightarrow \frac{hc}{\lambda} = -\frac{B}{16} + \frac{B}{1} \Leftrightarrow \lambda = \frac{6,63 \cdot 10^{-34} \cdot 3 \cdot 10^8}{2,18 \cdot 10^{-18} (1 - \frac{1}{16})} \text{m} = \underline{97,3 \text{nm}}$

d)



e)  $P_L = U_L \cdot I \Leftrightarrow I = \frac{P_L}{U_L} = \frac{9}{6} \text{A} = \underline{1,5 \text{A}}$

f)  $\varepsilon = 5 \cdot 1,5 \text{V} = 7,5 \text{V}$

$U_{\text{par}} = 7,5 \text{V} - 6,0 \text{V} = 1,5 \text{V}$

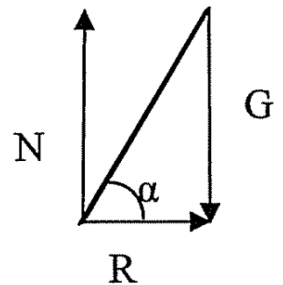
$I_1 = \frac{1,5}{10} \text{A} = 0,15 \text{A}$

$I_2 = (1,5 - 0,15) \text{A} = 1,35 \text{A}$

$U_{\text{par}} = R_2 \cdot I_2 \Leftrightarrow R_2 = \frac{U_{\text{par}}}{I_2} = \frac{1,5}{1,35} \Omega = \underline{1,1 \Omega}$

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- a) Termodynamikkens 1. Lov sier at øking av indre energi er arbeid pluss varme. Her gjør vi et arbeid på systemet, varmeutvekslingen er liten og dermed øker indre energi og dermed temperaturen. Friksjon gir også varme og høgre temperatur.



b)  $v = 50 \text{km/h} = 13,9 \text{m/s}$

$\tan \alpha = \frac{G}{R} = \frac{mg}{m \frac{v^2}{r}} = \frac{gr}{v^2} = \frac{9,81 \cdot 50}{13,9^2} \quad \alpha = 68,5^\circ \approx 69^\circ$

c)  $v_{j0} = 36 \text{km/h} = 10 \text{m/s}$ ,  $s_{j0} = v_{j0} \cdot t \Rightarrow t_{j0} = \frac{300}{10} \text{s} = 30 \text{s}$        $v_0 = 30 \text{km/h} = 8,33 \text{m/s}$

$s_o = v_0 + \frac{1}{2}at^2 = 300 \text{m} + 30 \text{m} \Rightarrow \frac{1}{2} \cdot 0,20 \frac{\text{m}}{\text{s}^2} \cdot t^2 + 8,33 \frac{\text{m}}{\text{s}} \cdot t - 330 \text{m} = 0$

Andregradslikning gir:  $t = 29,3 \text{s}$  eller  $t = -112,6 \text{s}$       Ola vinner

d)  $v_0 = 30 \text{km/h} = 8,33 \text{m/s}$ ,  $m_o = 85 \text{kg}$ ,  $m_d = 55 \text{kg}$ ,  $v_d = 0 \text{m/s}$ .

Bevegelsesmengde bevart:

$(m_o + m_d)v = m_o v_o + m_d v_d \quad v = \frac{85 \cdot 8,33 + 0}{85 + 55} \frac{\text{m}}{\text{s}} = \underline{5,1 \text{m/s} = 18 \text{km/h}}$

3.a) Energibev.  $\frac{1}{2}kx^2 = \frac{1}{2}mv^2 \Rightarrow v = \sqrt{\frac{kx^2}{m}} = \sqrt{\frac{30 \cdot 0,30^2}{0,040}} \frac{\text{m}}{\text{s}} = \underline{8,2 \text{m/s}}$

b)  $v_{0y} = 12 \frac{\text{m}}{\text{s}} \cdot \sin 30^\circ = 6,0 \text{m/s}$        $v_{0x} = 12 \frac{\text{m}}{\text{s}} \cdot \cos 30^\circ = 10,4 \text{m/s}$

Bevegelseslikning:

$2a_y y = v_y^2 - v_{0y}^2 \Rightarrow y = \frac{0 - 6^2}{2 \cdot (-9,81)} \text{m} = 1,83 \text{m}$       Maks høgd:  $(0,45 + 1,83) \text{m} = \underline{2,28 \text{m} \approx 2,3 \text{m}}$

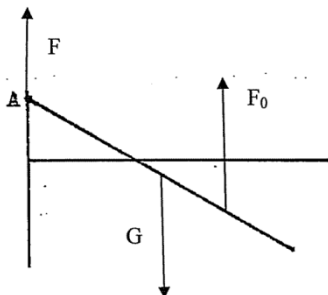
c)  $y = -0,45 \text{m}$ .

Bevegelseslikning:  $y = v_{0y}t + \frac{1}{2}at^2 \Leftrightarrow \frac{1}{2}at^2 + v_{0y}t - y = 0 \Rightarrow -4,905 \frac{\text{m}}{\text{s}^2} + 6,0 \frac{\text{m}}{\text{s}}t + 0,45 \text{m} = 0$   
 $\Rightarrow t_1 = -0,07 \text{s}$  og  $t_2 = 1,29 \text{s}$

Kastelengda blir:  $x = (10,4 \cdot 1,29) \text{m} = \underline{13,4 \text{m} \approx 13 \text{m}}$

d)  $\frac{1}{2}mv_o^2 + mgh = \frac{1}{2}mv^2 \Rightarrow v = \sqrt{v_o^2 + 2gh} = \sqrt{12^2 + 2 \cdot 9,91 \cdot 0,45} \frac{m}{s} = 12,36 \text{ m/s}$   
 $\cos\alpha = \frac{10,4}{12,35} \Rightarrow \alpha = 32,8^\circ$  Hastigheten danner  $32,8^\circ \approx 33^\circ$  med horisonten på skrå nedover.

4a)



b) Oppdrift:  $F_o = \rho V g = (1,025 \cdot 10^3 \cdot 4 \cdot 0,223 \cdot 0,048 \cdot 9,81) N = \underline{431 N \approx 0,43 kN}$

c) Moment om A.

$$G \cdot 3m \cdot \cos\alpha = F_o \cdot 4m \cdot \cos\alpha$$

$$G = \frac{430,5 N \cdot 4}{3} = 574 N$$

$$m = \frac{574}{9,81} kg = 58,5 kg$$

Massetetthet:  $\rho = \frac{58,5}{6 \cdot 0,223 \cdot 0,048} \frac{kg}{m^3} = \underline{911 kg/m^3 \approx 0,91 \cdot 10^3 kg/m^3}$

d) Trykk:  $p_1 = p_o + \rho gh = (1,013 \cdot 10^5 + 1025 \cdot 9,81 \cdot 2) Pa = \underline{121 kPa \approx 0,12 MPa}$

e)  $V_1 = 25 cm^3$ ,  $T_1 = (35 + 273) K = 308 K$ ,  $p_1 = 121,4 kPa$ ,  $p_2 = 101,3 kPa$ ,  $T_2 = (20 + 273) K = 293 K$

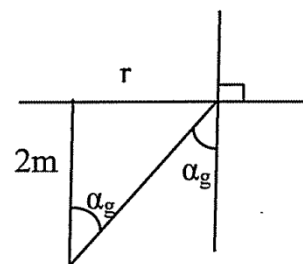
Tilstandslikning:  $\frac{p_1 \cdot V_1}{T_1} = \frac{p_2 \cdot V_2}{T_2} \Leftrightarrow V_2 = \frac{p_1 \cdot V_1 \cdot T_2}{T_1 \cdot p_2} = \frac{121,4 \cdot 25 \cdot 293}{308 \cdot 101,3} cm^3 = \underline{28,5 cm^3 \approx 29 cm^3}$

f)

Snell:  $1,33 \cdot \sin\alpha_g = 1 \cdot \sin 90^\circ$

$$\sin\alpha_g = \frac{1}{1,33} \quad \alpha_g = 48,75^\circ$$

$$\tan\alpha_g = \frac{r}{2,00m} \Leftrightarrow r = 2,00m \cdot \tan 48,75^\circ = \underline{2,28m}$$



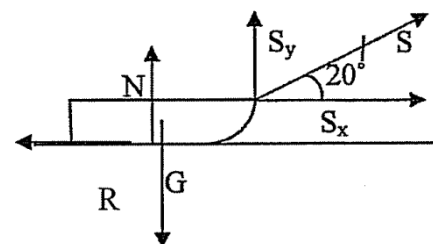
5a) Arbeid:  $W = S \cdot s \cdot \cos 20^\circ = 70 N \cdot 200 m \cdot \cos 20^\circ = \underline{13,2 kJ \approx 13 kJ}$

b) N.I.L. Friksjonskraft:  $R = S_x = 70 N \cdot \cos 20^\circ = \underline{65,8 N \approx 66 N}$

c) N.I.L. vert.  $N + S \cdot \sin 20^\circ = G$

$$N = G - S \cdot \sin 20^\circ = (70 \cdot 9,81 - 70 \sin 20^\circ) N = 662,8 N$$

Friksjonstall:  $\mu = \frac{R}{N} = \frac{65,8}{662,8} = \underline{0,099}$



d)  $G = (70 \cdot 9,81) N = \underline{687 N \approx 0,69 kN}$

N.I.L hor.:  $S \cdot \cos 20^\circ = 0,11 \cdot N$  (1)

N.I.L vert.:  $S \cdot \sin 20^\circ + N = mg \Leftrightarrow N = mg - S \cdot \sin 20^\circ$  (2)

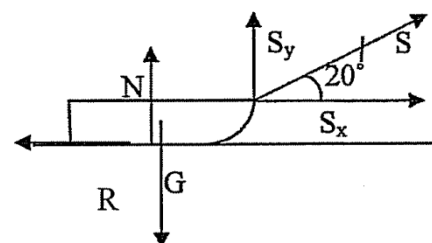
(2) inn i (1) gir:  $S \cdot \cos 20^\circ = 0,11 \cdot (mg - S \cdot \sin 20^\circ)$

$$S \cdot \cos 20^\circ + 0,11 \cdot S \cdot \sin 20^\circ = 0,11 \cdot mg$$

Snordrag:  $S = \frac{0,11 \cdot 687 N}{\cos 20^\circ + 0,11 \sin 20^\circ} = \underline{77,3 N \approx 77 N}$

(2) gir: Normalkraft:  $N = 687 N - 77,3 N \cdot \sin 20^\circ = \underline{660 N \approx 0,66 kN}$

Friksjonskraft:  $R = 0,11 \cdot 660 N = \underline{72,6 N \approx 73 N}$



e) Varmer:  $Q = c_i \cdot m_i \cdot 2K + l_s \cdot m_i + c_v \cdot m_i \cdot 37K = (2100 \cdot 0,005 \cdot 2 + 334000 \cdot 0,005 + 4180 \cdot 0,005 \cdot 37) J = \underline{2,5 kJ}$