

## OPPSUMMERING

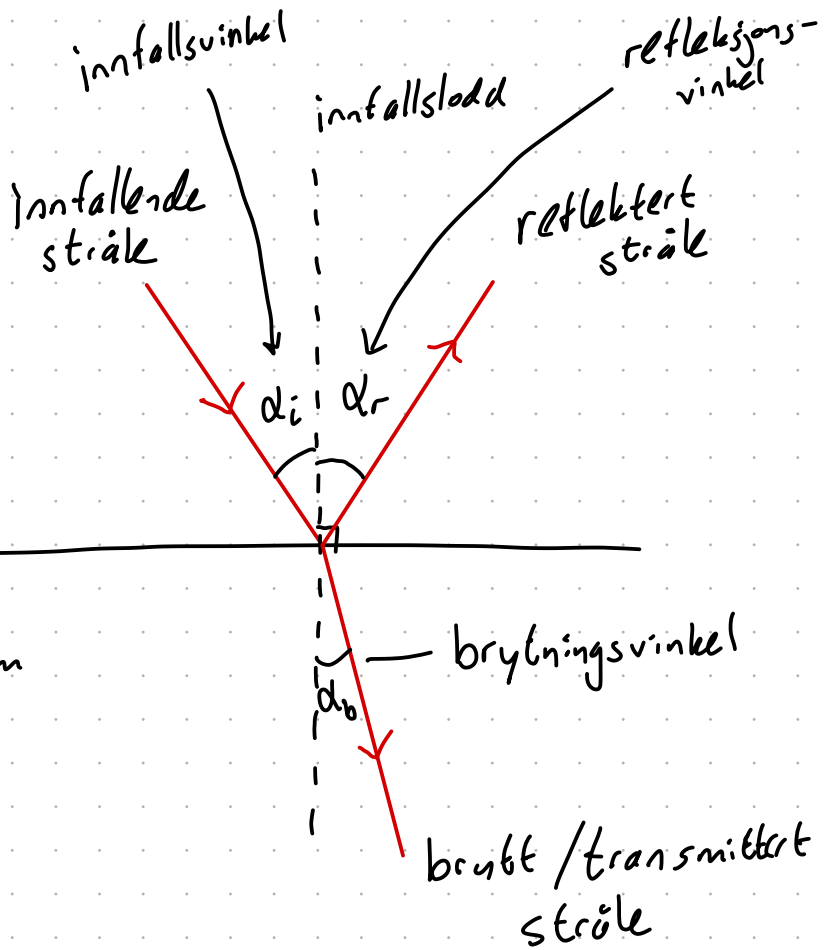
## brytningsindeks

Stoff 1,  $n_1 = \frac{c_0}{c_1}$

Stoff 2,  $n_2 = \frac{c_0}{c_2} \leftarrow \begin{matrix} \text{ljstark} \\ \text{i vakuum} \end{matrix}$

$\uparrow$

ljstark i  
stoff 2

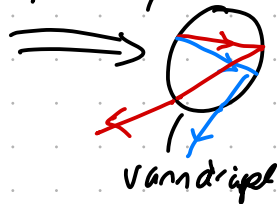


Refleksjonslov:  $\alpha_i = \alpha_r$

Snells brytningslov:  $n_1 \sin \alpha_1 = n_2 \sin \alpha_2$

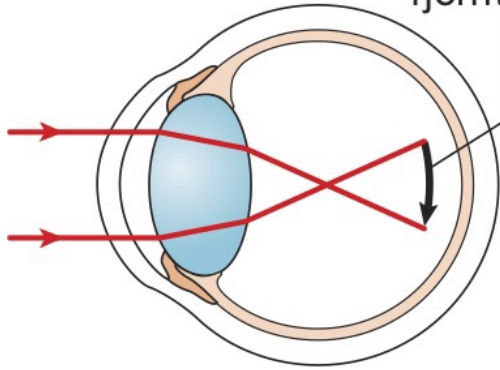
NB! Brytningsindeksen afhænger af bølgelængden til lyset.

Gir opphav til regnbue hvitt lys

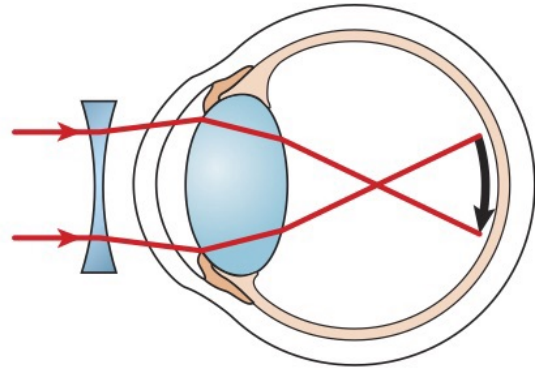


## Nærsynthet

Bilde av et  
fjernt objekt



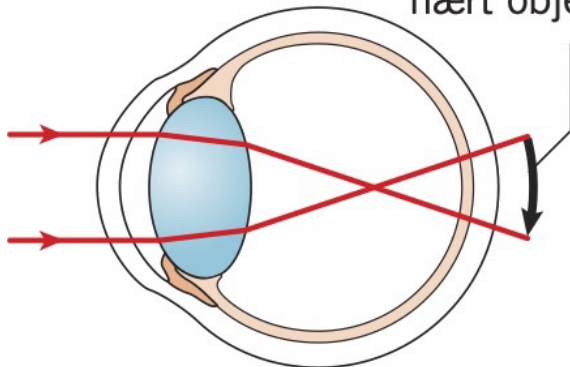
Ukorrigert



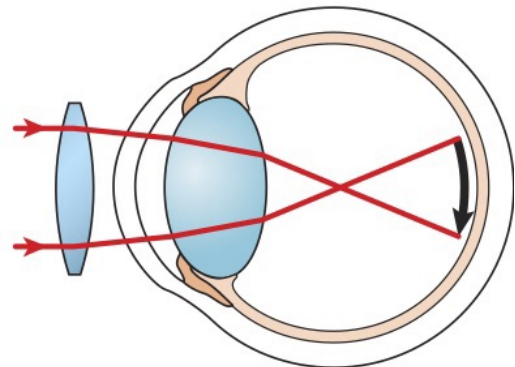
Korrigert

## Langsynthet

Bilde av et  
nært objekt

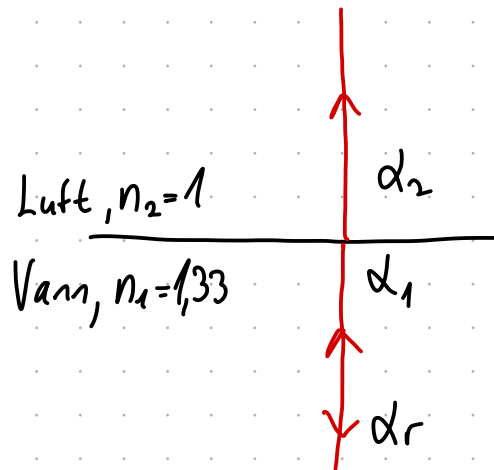


Ukorrigert



Korrigert

# 8.3 TOTALREFLEKSJON

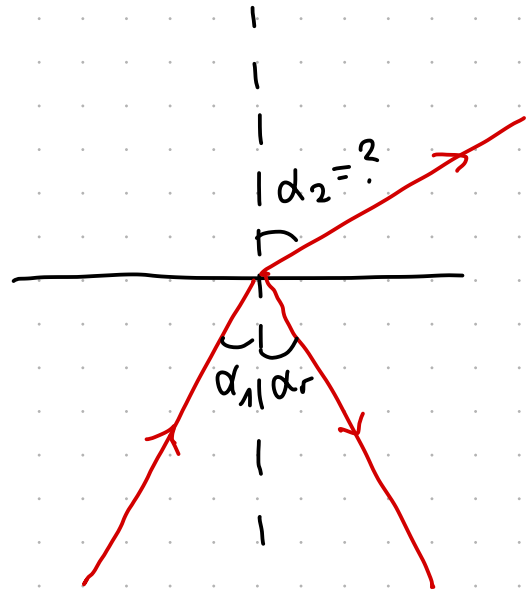


$$\alpha_1 = \alpha_r$$

$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

$$n_1 \cdot 0 = n_2 \sin \alpha_2$$

$$\alpha_2 = 0$$



$$\alpha_1 = 30^\circ$$

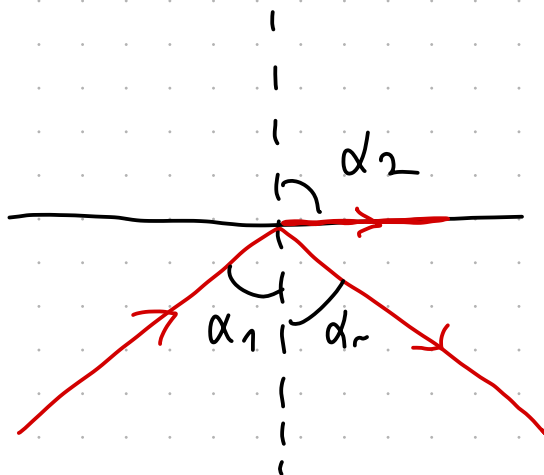
$$\alpha_r = \alpha_1 = 30^\circ$$

$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

$$1,33 \cdot \sin 30^\circ = 1 \cdot \sin \alpha_2$$

$$\sin \alpha_2 = \frac{1}{2} \cdot 1,33 = 0,665$$

$$\alpha_2 = \sin^{-1}(0,665) = 42^\circ$$



$$\alpha_1 = 49^\circ$$

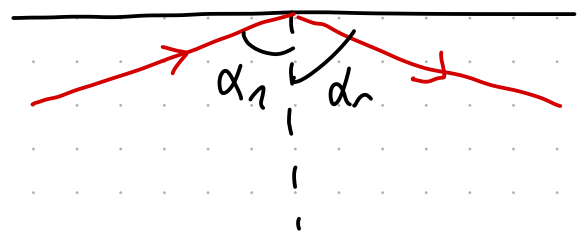
$$\alpha_r = \alpha_1 = 49^\circ$$

$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

$$\sin \alpha_2 = 1,33 \cdot \sin 49^\circ$$

$$= 1,33 \cdot 0,7547 = 1,00$$

$$\alpha_2 = \sin^{-1}(1,00) = 90^\circ$$



$$\alpha_1 = 70^\circ$$

$$\sin \alpha_2 = 1,33 \cdot \sin 70^\circ$$

$$= 1,25$$

$\alpha_2$  fins ikke

$$\alpha_r = \alpha_1 = 70^\circ$$

Når brytningsvinkelen er  $90^\circ$  har innfallsvinkelen nådd den såkalte grensevinkelen  $\alpha_{gr}$ .

$\alpha_{gr}$  er gitt ved:

$$\alpha_{gr} = \sin^{-1} \left( \frac{n_2}{n_1} \right)$$

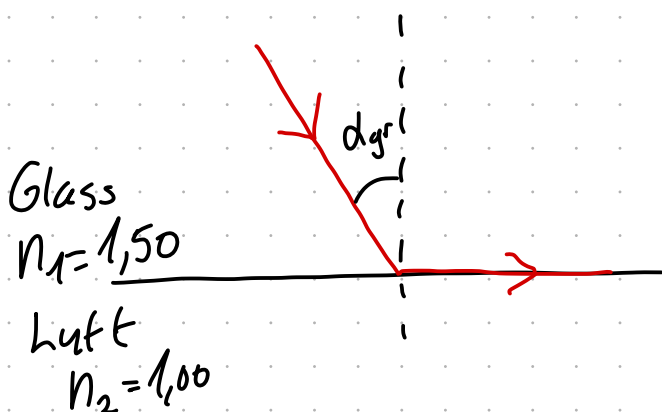
$$n_2 < n_1$$

Totalrefleksjon oppstår når:

1. lysstrålen møter et stoff med mindre brytningsindeks
2. innfallsvinkelen er større enn grensevinkelen

Grensevinkelen er gitt ved  $\alpha_{gr} = \sin^{-1} \left( \frac{n_2}{n_1} \right)$

### Eksempel



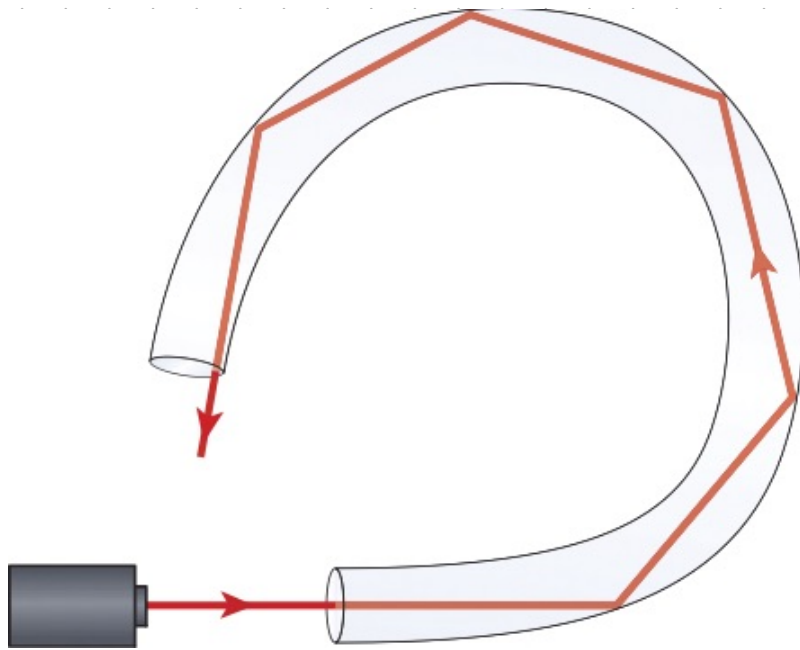
Hva er grensevinkelen?

$$n_1 \sin \alpha_{gr} = n_2 \underbrace{\sin(90^\circ)}_{=1}$$

$$\sin \alpha_{gr} = \frac{n_2}{n_1}$$

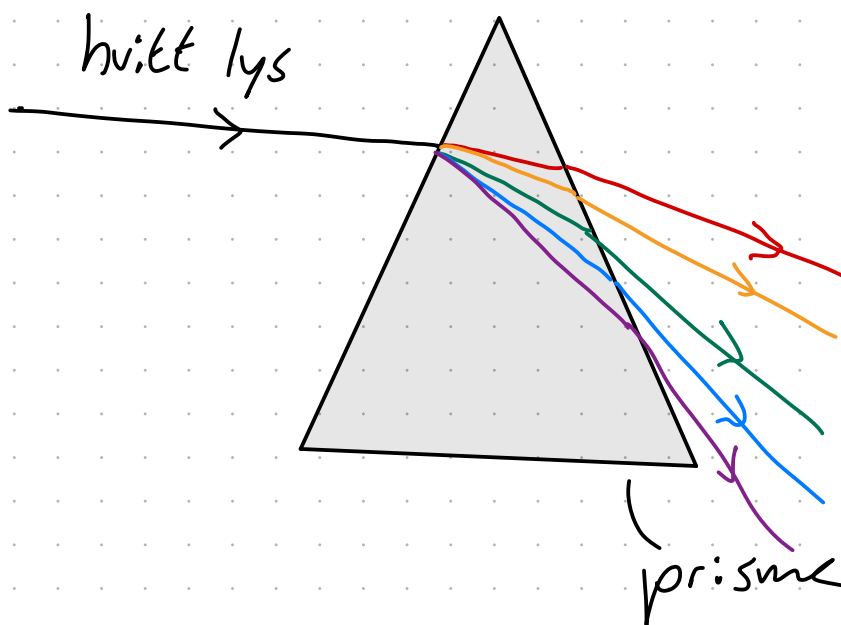
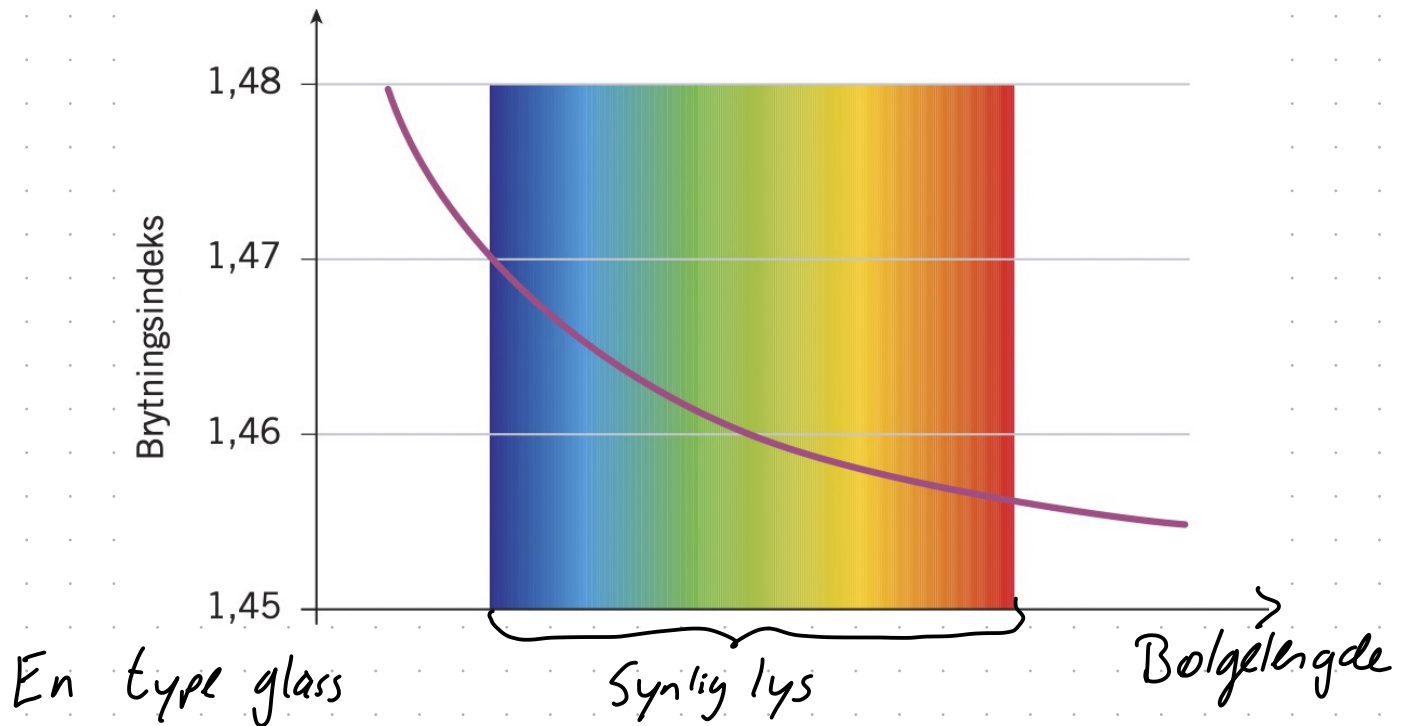
$$\alpha_{gr} = \sin^{-1} \left( \frac{1,00}{1,50} \right) = \underline{\underline{41,8^\circ}}$$

Optisk fiber til f.eks. bredbånd  
benytter totalrefleksjon inni fiberen




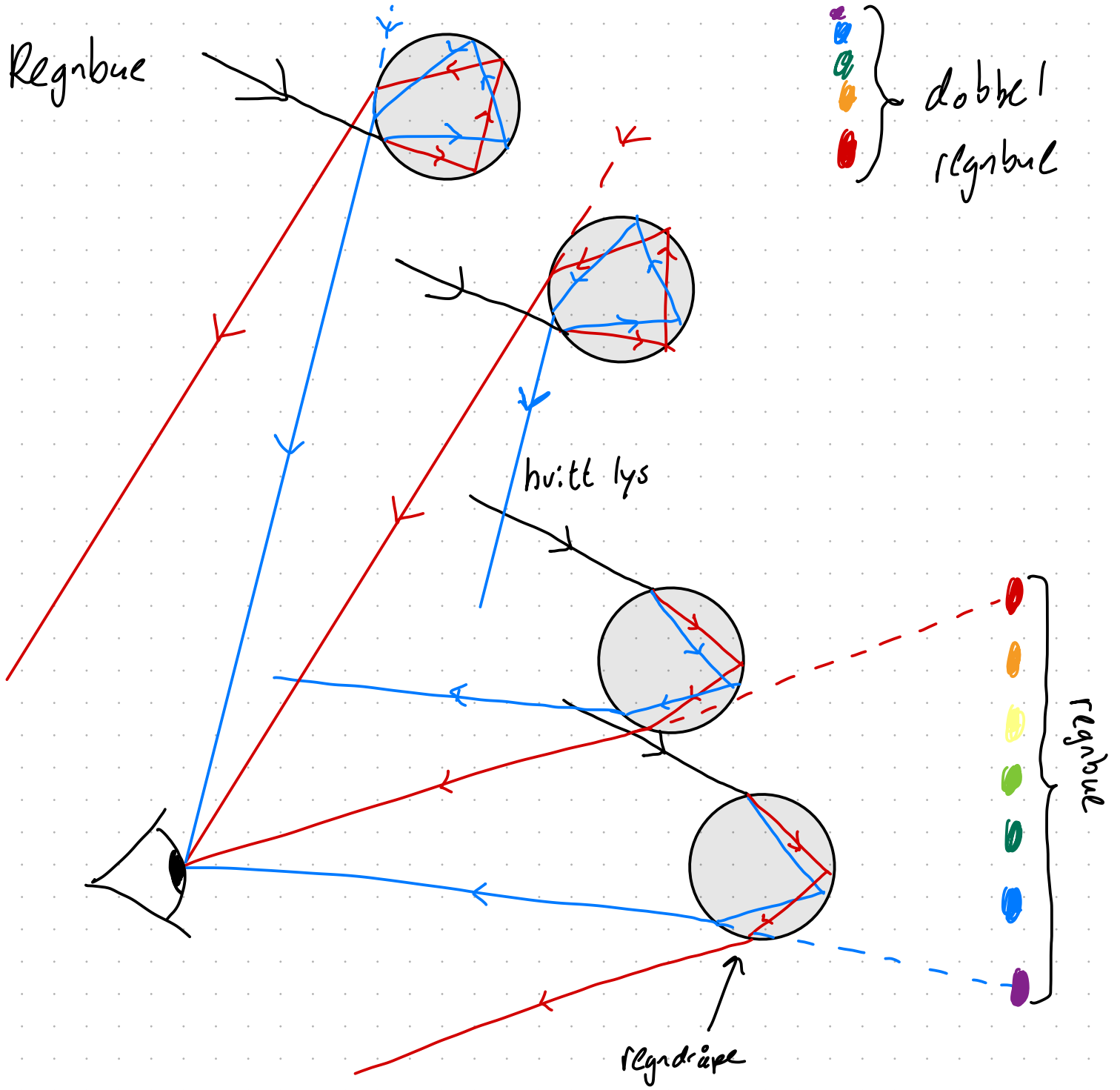
## 8.4 LYSBRYTNING OG FARGER

Brytningsindeksen i materialer varierer med bølglengden / frekvensen til lyset

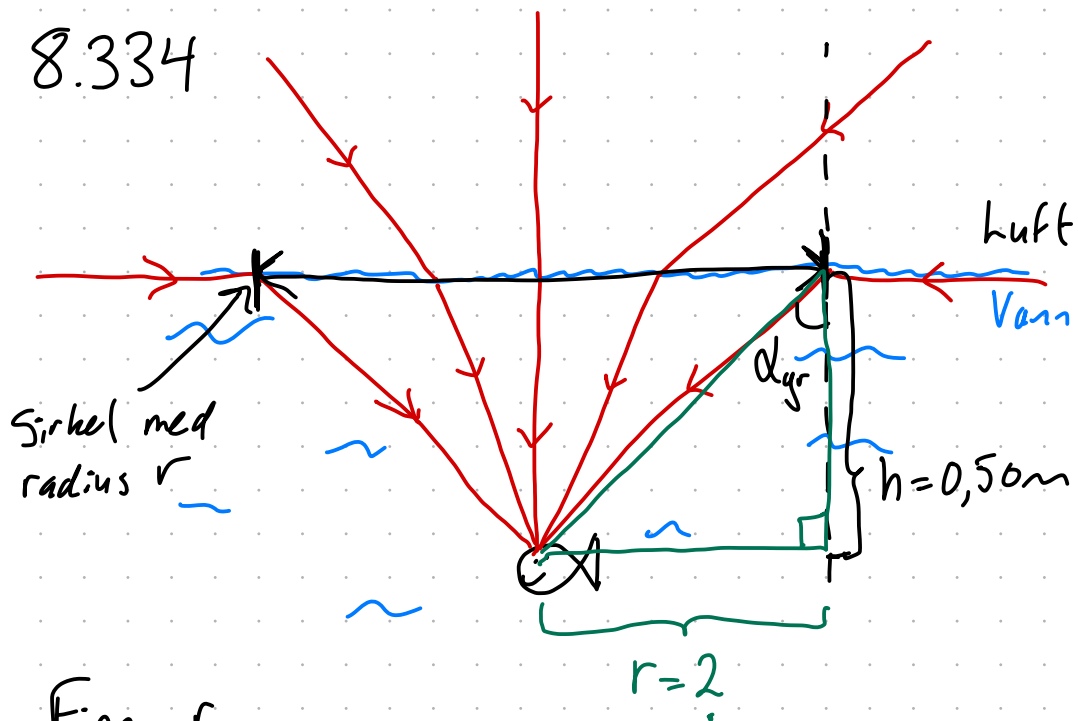


Regnbue

 } dobbel regnbue



8.334

Finn  $r$ .

Opplysninger:  $n_2 = 1,33$   
 $n_1 = 1,00$   
 $h = 0,50 \text{ m}$

Snells lov:  $n_1 \sin \alpha_1 = n_2 \sin \alpha_2$ 

$$1 \cdot \underbrace{\sin 90^\circ}_{=1} = 1,33 \sin \alpha_{gr}$$

$$\sin \alpha_{gr} = \frac{1}{1,33}$$

$$\alpha_{gr} = \sin^{-1}\left(\frac{1}{1,33}\right) = 48,753^\circ$$

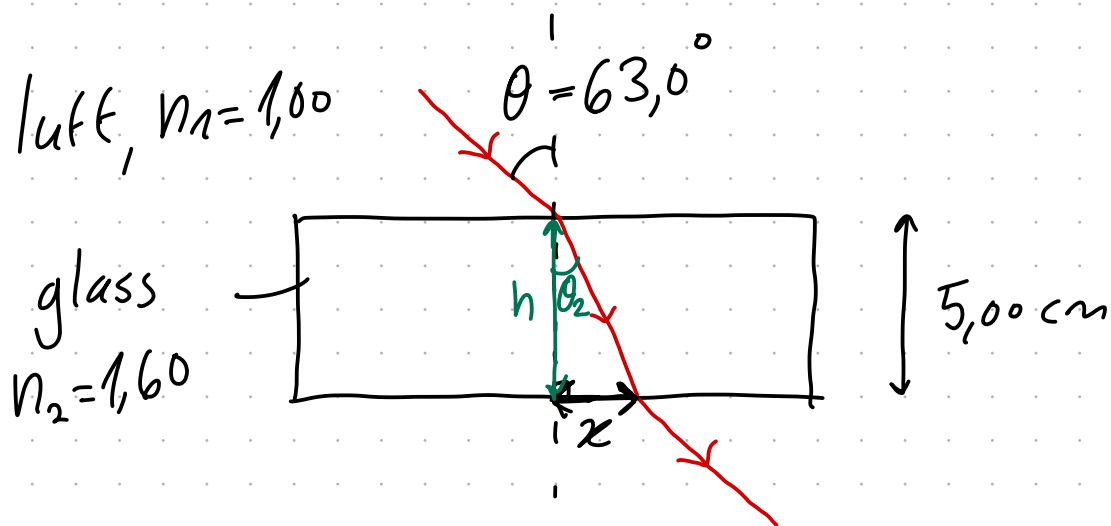
$$\tan \alpha_{gr} = \frac{r}{h} \Rightarrow r = h \cdot \tan \alpha_{gr}$$

$$r = 0,50 \text{ m} \cdot \tan 48,753^\circ = 0,57 \text{ m}$$

$$\underline{\text{Radiusen} = 0,57 \text{ m}}$$



# Eksamen vår 2018



a) Finn  $x$   $\tan \theta_2 = \frac{x}{h} \Rightarrow x = h \cdot \tan \theta_2$

Vi finner  $\theta_2$  med Snells lov.

$$\underbrace{n_1}_{=1} \frac{\sin \theta}{n_2} = \frac{n_2}{n_2} \sin \theta_2$$

$$\sin \theta_2 = \frac{\sin \theta}{n_2}$$

$$\theta_2 = \sin^{-1} \left( \frac{\sin \theta}{n_2} \right) = \sin^{-1} \left( \frac{\sin 63^\circ}{1,60} \right)$$

$$\theta_2 = 33,84^\circ$$

$$x = h \cdot \tan \theta_2 = 5,00 \text{ cm} \cdot \tan 33,84^\circ$$

$$\underline{x = 3,35 \text{ cm}}$$

b) Hvor lang tid bruker lyset gjennom prismet?

strekning = fart · tid

$$s = v \cdot t \quad \rightarrow \quad t = \frac{s}{v}$$

↑ ?

1. Strekning

$$s \cdot \frac{\cos \theta_2}{\cos \theta_2} = \frac{h}{s} \cdot s$$

$$s = \frac{h}{\cos \theta_2} = \frac{5,00 \text{ cm}}{\cos(33,84^\circ)} = 6,020 \text{ cm} = 6,020 \cdot 10^{-2} \text{ m}$$

2. Fart

$$n_2 = \frac{c_0}{v}$$

$$v = \frac{c_0}{n_2} = \frac{3,00 \cdot 10^8 \frac{\text{m}}{\text{s}}}{1,60} = 1,875 \cdot 10^8 \frac{\text{m}}{\text{s}}$$

$$t = \frac{6,020 \cdot 10^{-2} \text{ m} \cdot s \cdot 10^{-8}}{1,875 \cdot 10^8 \frac{\text{m}}{\text{s}} \cdot s \cdot 10^{-8}} = \frac{6,020}{1,875} \cdot \underbrace{10^{-2} \cdot 10^{-8}}_{10^{-10}} \text{ s}$$

↑ = 1

$$\underline{t = 3,21 \cdot 10^{-10} \text{ s}}$$