a)
$$\frac{1}{30^{\circ}}$$
 $\frac{30^{\circ}}{1}$ $\frac{1}{4}$ \frac

$$S_{x} = F_{\mu}$$

$$S = \frac{90N}{\sin 30^{\circ}} = 180N = 0.18 \text{ kN}$$

$$\leq F_y = 0$$

$$S_y = G$$

$$5 \cdot \cos 30^\circ = G$$

13.02

a)
$$\Sigma F_y = 0$$

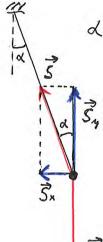
$$\frac{F_1 \cdot \sin 30^\circ}{\sin 60^\circ} = F_2$$

EF = 0, Ux = konsh

$$R = F_{1x} + F_{2x}$$

$$R = F_1 \cdot \cos 30^\circ + F_2 \cdot \cos 60^\circ = 6.0 \, \text{k N} \cdot \cos 30^\circ + 3.464 \, \text{k N} \cdot \cos 60^\circ = 6.9 \, \text{k N}$$

13.04



$$\lambda = 18^{\circ}$$
 a) $\sum F_{y} = 0$
 $S_{y} = G$

$$S_{y} = G$$

$$S \cdot \cos \alpha = mg$$
 $S \cdot \sin \alpha = ma$

$$a = \frac{5 \cdot \sin \alpha}{m}$$

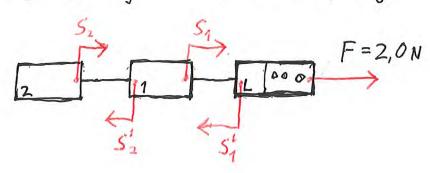
$$a = \frac{mq}{\cos d} \cdot \frac{\sin d}{m}$$

$$a = g \cdot fan d = 9.81 \frac{m}{52} \cdot fan 18^{\circ}$$

a er wanhengig av masse.

$$13.05$$
 $m_L = 0.20 kg$

$$m_1 = m_2 = 0,15 \, \text{kg}$$



$$F = (m_1 + m_1 + m_2) \cdot a$$

$$a = \frac{F}{(m_1 + m_1 + m_2)}$$

$$a = \frac{2,0N}{(0,20+0,15+0,15)kg} = 4,0\frac{m}{5^2}$$

De to voghene:

$$S_1 = (m_1 + m_2) \cdot a$$

$$S_1 = (0,15 + 0,15) kg \cdot 4,0 \frac{m}{52} = 1,2 N$$

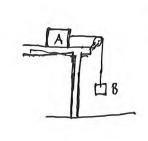
Bakerste Vogn: er systemet

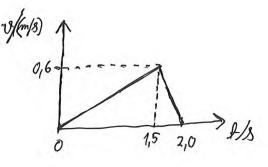
$$S_2 = 0.15 \, \text{kg} \cdot 4.0 \, \frac{\text{m}}{5^2} = 0.60 \, \text{N}$$

13.06
$$m_A = 2.6 \text{kg}$$

$$f_B = 1.5 \text{s}$$

$$a = \frac{\Delta v}{\Delta t}$$





a)
$$a_1 = \frac{(0,6-0)\frac{m}{3}}{(1,5-0)\frac{m}{3}} = \frac{0.40\frac{m}{3^2}}{(1,5-0)\frac{m}{3}} = \frac{0.40\frac{m}{3^2}}{(2.0-1.5)\frac{m}{3}} = \frac{-1.2\frac{m}{3^2}}{(2.0-1.5)\frac{m}{3}}$$

$$\frac{1}{R} = \frac{1}{R} \left(\frac{3}{4} \right)$$

$$\mu = \frac{R}{N} = \frac{R}{6}$$

$$\frac{R}{R} = \frac{1}{4}$$

$$\Delta E_{k} = W_{t}$$

$$W_{t} = R.8$$

$$2as = b^{2} - v_{o}^{2}$$

$$8 = \frac{-v_{o}^{2}}{2a}$$

$$8 = \frac{-(0.6 \frac{m}{s})^{2}}{2 \cdot (-1.2 \frac{m}{s^{2}})} = 0.15 \text{ m}$$

$$\frac{1}{2}mv^2 = R.8$$

$$R = \frac{mv^2}{2s}$$

$$\mu = \frac{R}{6} = \frac{mv}{\frac{28}{mg}} = \frac{v^2}{2s \cdot g} = \frac{(0.60 \, \text{m})^2}{2 \cdot 0.15 \, \text{m} \cdot 9.81 \, \text{m}} = 0.1223 = 0.12$$

$$S-R=ma_1$$

$$5 = ma_1 + R$$

$$5 = ma_1 + \mu G = ma_1 + \mu mg = m \cdot (a_1 + \mu g)$$

$$= 2,6 kg \cdot (0,40 \frac{m}{3^2} + 0,1223 \cdot 9,81 \frac{m}{3^2})$$

$$=4,159_N=4,2_N$$

Kule A vinner. De la banene er omtrent like lange, men bane A er klart braffene i første halvdel. Delle gir større akselerasjon i første halvdel av banen, noe som gjør at

kula der har maks, fart lenge for kulæiß-banen, Siden vil maksfarten holde seg til C mens kula i Bikke når samme maksfart for den er framme. Begge kuler har samme sluft-fart grunnet lik Epot ved start i forhold til punkt C.

$$\vec{R}=0$$
 på tegninga n:normalr
Dette gir $\sum F_p = ma_p$ i forhold
 $G_p = ma_p$ skråplan
 $mg \cdot sin d = ma_p$
 $a_p = 9.81 \frac{m}{52} \cdot sin 32^\circ = 5.2 \frac{m}{52}$

Sin
$$\alpha = \frac{G_p}{G}$$
 Cos $\alpha = \frac{G_n}{G}$
 $G_p = G \cdot \sin \alpha$ $G_n = G \cdot \cos \alpha$
 $G_p = mg \cdot \sin \alpha$ $G_n = mg \cdot \cos \alpha$

$$|R = \mu N| \text{ fordi } \mu = \frac{R}{N}$$

$$og \quad \sum F_n = 0$$

$$N - G_n = 0$$

$$N = G_n = mg \cdot cos \propto N$$

$$m = 2.0 kg$$

$$d = 32^{\circ}$$

$$\vec{R} = 0$$

i forhold til skråplanet n:normalretningen i forhold til skråplanet

p: parallell retning

$$\sum F_{p} = m a_{p}$$

$$G_{p} - R = m a_{p}$$

$$mg \cdot sin \alpha - \mu \cdot mg \cdot cos \alpha = m a_{p}$$

$$g \cdot sin \alpha - \mu g \cdot cos \alpha = a_{p}$$

$$a_{p} = g \cdot (sin \alpha - \mu \cdot cos \alpha)$$

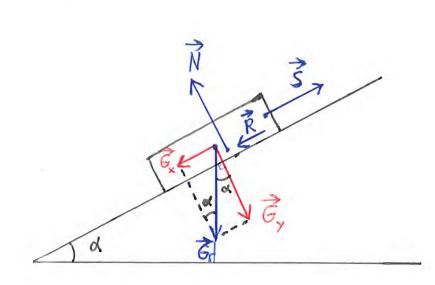
$$a_{p} = 9.81 \frac{m}{52} \cdot (sin 32^{\circ} - 0.20 \cdot cos 32^{\circ})$$

$$a_{p} = 3.5 \frac{m}{52}$$

c) mer en faktor i alle ledd i Newtons 2, (ov og kan dermed strykes ved at videler alle ledd på massen.

13.08 $\mu = 0,20 \quad \chi = 32^{\circ}$ a) EF = ma $-G_p - R = ma$ -6. sind - 4N = ma SF =0 -mg·sina-umgcosx = ma N-G,=0 $-g(\sin\alpha + \mu\cos\alpha) = a$ N=G-cosa $a = -9.81 \frac{m}{52} \cdot (\sin 32^{\circ} + 0.20 \cdot \cos 32^{\circ})$ N=mg.cosx $a = -6.9 \frac{m}{5^2} \left(-6.862 \frac{m}{5^2} \right)$ $2as = V^2 - V_0^2$ og V = 0b) $2as = -V_o^2$ $5 = \frac{-V_0^2}{2a} = \frac{-(3.4 \frac{m}{s})^2}{2.(6.862 \frac{m}{s^2})} = 0.84 \frac{m}{s}$ m = 2,0 kg Gp = mgslnd = 2,0kg . 9,81 kg . 5/n32° =10,39NR= uN = uGn = umg cos & = 0,20.2,0 kg. 9,81 kg. cos32° $= 3.32 \, \text{N}$ Rgli < G, glidefriksjon. Klossen glir ned

13,10 a)



$$S = 78,4.10^{3}N$$

$$A = 28^{\circ}$$

$$M = 9,2.10^{\circ}kg$$

$$G = Mg = 9,2.10^{\circ}kg \cdot 9,81^{\circ}kg$$

$$= 9,0.10^{\circ}N$$

$$(9,025.10^{\circ}N)$$

$$\sum F_{y} = 0$$

$$N - G_{y} = 0$$

$$N = G_{y}$$

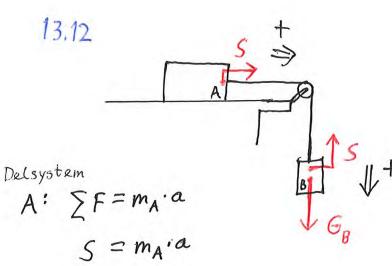
 $N = G_{y} = G \cdot \cos \alpha$ $N = 9,025 \cdot 10^{4} \text{N} \cdot \cos 28^{\circ} = 8,0 \cdot 10^{4} \text{N} \left(7,968 \cdot 10^{4} \text{N}\right)$

$$\Sigma F_{x} = 0$$

 $S - R - G_{x} = 0$
 $R = S - G_{x} = S - G \cdot \sin \alpha$
 $R = 78,4 \cdot 10^{3} N - 9,025 \cdot 10^{4} N \cdot \sin 28^{6}$
 $R = 3,6 \cdot 10^{4} N \quad (3,603 \cdot 10^{4} N)$

b)
$$\mu = \frac{R}{N}$$

$$\mu = \frac{3,603.10 \text{ N}}{7,968.10^4 \text{ N}} = 0.45$$



$$m_{A} = 7.8 kg$$
 $a = 2.0 \frac{m}{5^{2}}$
 $m_{B} = ?$
 $M_{B} = ?$
 $M_{B} = ?$
 $M_{B} = ?$
 $M_{B} = 9 - 8 = 8 = 8$
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 $M_{B} = 9 - 8$
 $M_{B} =$

13.14
$$v = 20 \frac{km}{h} = 20 \cdot \frac{1000m}{36008} = 5,555 \frac{m}{8}$$

 $h = 6,0m \qquad m = 1000 kg$

a)
$$= 5143 N = \frac{5,555 \%}{6,0m}$$

$$R = m \frac{v^{2}}{h} = 1000 \text{ kg} \cdot \frac{(5,535 \cdot 8)}{6,0m}$$

$$= 5143 \text{ N} = \frac{5,1 \text{ k N}}{6,0m}$$

$$= 5143 \text{ N} = \frac{5,1 \text{ k N}}{6,0m}$$

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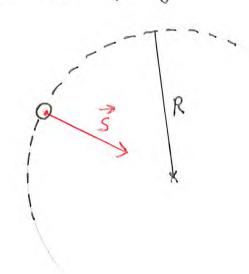
$$= 5143 \text{ N} = \frac{5,1 \text{ k N}}{6,0m}$$

$$= \frac{5,1 \text{ k N}}{6,0m}$$

$$= \frac{5,1 \text{ k N}}{6,0m}$$

$$= \frac{5,1 \text{ k N}}{6,0m}$$

13.15
$$m = 1.5 \text{ kg}$$
 $R = 1.2 \text{ m}$ $S = 40 \text{ N}$



$$\sum F = m a$$

$$S = m \frac{V^{2}}{R}$$

$$\frac{S \cdot R}{M} = V^{2}$$

$$V = \sqrt{\frac{5 \cdot R}{m}}$$

$$V = \sqrt{\frac{40N \cdot 1.2m}{1.5 \, kg}} = 5,656 \frac{m}{s}$$

$$= 5,7 \frac{m}{s}$$

$$S=v\cdot t$$

$$Tiden for ettom(op: t=\frac{5}{v}=\frac{2\pi R}{v}=\frac{2\pi r\cdot 1.2m}{5.656\frac{m}{s}}=1,3335$$

$$Antall omloppå ett minutt: n=\frac{60s}{1,333s}=\frac{45}{5}$$

13.17
$$v = 80 \frac{km}{R} = 22,22 \frac{cs}{8}$$
 $m = 0,20 \frac{kq}{q}$ $d = 22^{\circ}$

a) $200 \frac{km}{R} = 22,22 \frac{cs}{8}$ $m = 0,20 \frac{kq}{q}$ $d = 22^{\circ}$

3. $200 \frac{km}{R} = 22,22 \frac{cs}{8}$ $d = 22^{\circ}$

Shortdrag $d = 22,22 \frac{cs}{8}$ $d = 22,22 \frac{cs}{8}$

c)
$$x'$$
: $\sum F = ma$
 $S_x = m \frac{v^2}{r}$ $S_x = S \cdot \cos 45^\circ = 1248 \text{ N} \cdot \cos 45^\circ$
 $= 882,4 \text{ N}$
 $= 0,88 \text{ KN}$

= 1,2kN

$$\frac{1}{2}mv^2 = mgh$$

$$v^2 = 2gh$$

$$V = \sqrt{2gh}$$

$$V = \sqrt{2gh} = \frac{19.6 \frac{m}{5^2}}{V = \sqrt{2.9.81 \cdot 1.20^7 \frac{m}{5}}} = \frac{4.852 \frac{m}{5}}{V} = \frac{rett opp}{rett opp}$$

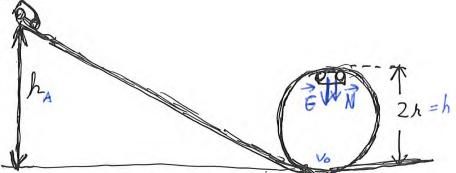
 $a = \frac{v^2}{r} = \frac{2gk}{k} = 2g$

$$V = 4,85 \frac{m}{5}$$

+11
$$S-G = m \frac{v^2}{r}$$

 $S = m(g + \frac{v^2}{r})$
 $S = 0.50 \text{ Kg}(9.81 + 19.6) \frac{m}{s^2} = 15 \text{ N. opp}$

13.20



m = 0.050 kg d = 0.24 m $v_0 = 3.1 \frac{\text{m}}{\text{s}} \text{ ved}$ bakkeniva

a)
$$E_p + E_k = F_{po} + E_{ko}$$

 $mgh + \frac{1}{2}mv^2 = \frac{1}{2}mv_o^2$
 $gh + \frac{1}{2}v^2 = \frac{1}{2}v_o^2$
 $v = v_o^2 - 2gh$

$$\sum F_{ig} = ma_{ig} \quad \text{toppen}$$

$$G + N = m \frac{v^{2}}{h}$$

$$M = m \left(\frac{v^{2}}{h} - q \right)$$

$$N = m \left(\frac{v^{2} - 2q \cdot 2h}{h} - q \right)$$

$$N = m \left(\frac{v^{2} - 2q \cdot 2h}{h} - q \right) = m \left(\frac{v^{2}}{h} - 5q \right)$$

$$N = \left(\frac{(3,1\%)^{2}}{0,12m} - 5 \cdot 9,81 \frac{N}{kg} \right) \cdot 0,050 \frac{N}{kg}$$

$$= 1,551 N = 16N \quad \text{nedover}$$

b)
$$N=0$$
 $v_0=2$.

 $\frac{v_0^2}{h}-5g=0$
 $\frac{v_0^2}{h}=5g$
 $v_0^2=5gh$
 $v_0=\sqrt{5gh}=\sqrt{5.9,81\frac{m}{32}\cdot0,12m}=2,426\frac{m}{3}=\frac{2.4\frac{m}{32}}{2}$

C)
$$E_p = E_{k0}$$
 $\lambda mgh = \frac{1}{2}mv_0^2$
 $gh = \frac{1}{2}v_0^2$
 $gh = \frac{1}{2}\cdot 5gh$
 $h = \frac{5}{2}h = \frac{5}{2}\cdot 0.12 m = \frac{0.30m}{0.30m}$

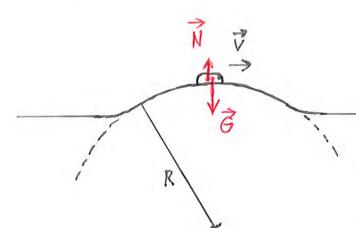
a)
$$\overrightarrow{N}$$

Under akselerasjon virker
friksjonskrafta i samme
retning som akselerasjonen.
Hvis R var null ville hjulene
spinne. Motkrafta til R virker
på veien og fører til at grus
og småstein skvetter bakover
når du trykker på gassen
på en grusvei.

$$\Sigma F_{y} = 0$$
 $N - G = 0$
 $N = G = 13.10N$

b)
$$\Sigma F = ma$$

 $\Sigma F = R = ma = \frac{G}{g} \cdot \left(\frac{V - V_0}{t}\right) = \frac{13 \cdot 10N}{9.81 \frac{m}{5^2}} \cdot \left(\frac{16 - 0}{12}\right) \frac{m}{5^2} = 1766N$
 $\left(\frac{G}{g} = 1325 \text{ kg}\right)$



$$\Sigma F = ma$$

 $G - N = m \frac{\chi^2}{R}$
 $G - m \frac{\chi^2}{R} = N$
 $N = 13 \cdot 10^3 N - 1325 \cdot \frac{16^2}{100} N$
 $= 9608N = \frac{966}{100} N$

N=0 hvis bilen svever.

$$\sum F = ma$$

$$G = m \frac{V^2}{R^2}$$

$$mg = m \frac{V^2}{R^2}$$

$$g = \frac{V^2}{R}$$

$$gR = V^2$$

$$V = \sqrt{gR} = \sqrt{9,81.100} \frac{m}{s}$$

$$V = 31 \frac{m}{s}$$

 $\sum F_{R} = mR^{2}$ $N-G_{n} = mR^{2}$ $N-G_{n} = mR$ $N-G_{n} = m$

R>G, fordi kjelken bremser normalt på radiell retning.
R<N fordi u normalt er mindre enn 1,0.

13.23
$$m = 0.300 \, \text{kg} \quad k = 3.0 \, \frac{N}{m}$$

 $f = \frac{1}{2\pi} \sqrt{\frac{K}{m}} = \frac{1}{2\pi} \sqrt{\frac{3.0 \, \text{kg}}{0.300 \, \text{kg}}} = 0.5032 \, \text{s}^{-1} = 0.50 \, \text{Hz}$
 $T = \frac{1}{5} = \frac{1}{0.5032 \, \text{s}^{-1}} = 1.987 \, \text{s} = 2.0 \, \text{s}$

13.24
$$\times (t) = 0.070 \text{ m} \cdot \cos(2\pi \cdot 0.60 \, \hat{s}^{\, 1} \cdot t)$$

 $A = 0.070 \text{ m}$ $f = 0.60 \, \hat{s}^{\, 1} \Rightarrow T = \frac{1}{5} = \frac{1}{0.60 \, \hat{s}^{\, -1}} = \frac{1.75}{0.60 \, \hat{s}^{\, -1}}$

13.25

$$A = 0.10 \text{ m}$$
 $A = 0.10 \text{ m}$
 $T = (2.24 - 0.00) \text{ s}$
 $= 2.24 \text{ s}$

13.26
$$m = 0.150 \text{kg}$$
 $k = 2.0 \frac{\text{M}}{\text{m}}$ $A = 0.060 \text{m}$
a) $f = \frac{1}{2\pi} \sqrt{\frac{\text{K}}{\text{m}}} = \frac{1}{2\pi} \sqrt{\frac{2.0 \frac{\text{M}}{\text{m}}}{0.150 \text{kg}}} = 0.5811 \frac{5}{5}^{1} = 0.58 \text{Hz}$
 $T = \frac{1}{5} = \frac{1}{0.58115^{1}} = \frac{1.75}{0.58115^{1}} = \frac{1.75}{0.58115^{1}}$

b)
$$x(t) = A\cos(2\pi ft) = 0.060 \text{m} \cdot \cos(2\pi \cdot 0.5811 \text{s}^{-1} \cdot t)$$

 $= 6.0 \text{cm} \cdot \cos(3.7 \text{s}^{-1} \cdot t)$
 $V(t) = -2\pi f A \cdot \sin(2\pi ft) = -2\pi \cdot 0.5811 \text{s}^{-1} \cdot 0.060 \text{m} \cdot \sin(2\pi \cdot 0.581 \text{s}^{-1} t)$
 $= -0.22 \frac{\text{m}}{\text{s}} \cdot \sin(3.7 \text{s}^{-1} \cdot t)$
 $a(t) = -4\pi^2 f^2 A \cdot \cos(2\pi ft) = -0.80 \frac{\text{m}}{\text{s}^{-2}} \cdot \cos(3.7 \text{s}^{-1} \cdot t)$

c)
$$x(0) = 6.0 \text{ cm}$$
 $x(1.2s) = -1.6 \text{ cm}$ $y(0) = 0$ $y(1.2s) = 0.21 \frac{\text{cm}}{s}$ $y(1.2s) = 0.22 \frac{\text{cm}}{s^2}$ $y(1.2s) = 0.22 \frac{\text{cm}}{s^2}$

13,26 d)
$$X = 0,060 \text{m} \cdot \cos(3,75^{1},t)$$

Casio $Y1 = 0.06 \times \cos(3.7 \times X)$
 $V = \frac{2\pi}{3,75^{1}} = 1.75$

(ca 2)

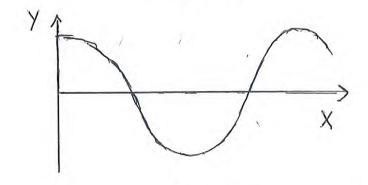
max ! 2.

 $Scale : 1$

Ymin : -0.06

max : 0.06

 $Scale : 1$



2)
$$T = (1,698 - 0,0)s = 1,7s$$
 Trace (shift) (F1)
 $t = 1,206s$ gir $x = -0,01478$ m $\approx -0,015$ m $= -1,5$ cm

$$V = konst. \Rightarrow \sum F_p = 0$$

$$G_p - R = 0$$

$$G_p = R$$

$$G \cdot sin\alpha = R$$

$$R = mg \cdot sin\alpha$$

$$\overrightarrow{R}$$
 \overrightarrow{F}_{K}
 \overrightarrow{G}
 \overrightarrow{G}
 \overrightarrow{G}

1.
$$P = \frac{W}{t} = \frac{F_k \cdot s}{t} = F_k \cdot v$$

2. $\sum F_p = 0$

$$2. \geq F_p = 0$$

$$F_k = mg \cdot sind$$

1. og 2. gin at P=mg(sind). V

$$\left(N\frac{m}{s} = \frac{N \cdot m}{s} = \frac{J}{s} = w\right)$$

$$P = 70 \, kg \cdot 9.81 \, \frac{N}{kg} \left(\sin 4.0^{\circ} \right) \cdot 6.944 \, \frac{m}{s}$$
$$= 332.6 \, N \, \frac{m}{s} = 0.33 \, kW$$