Attention Mechanism, Transformers, BERT, and GPT

Deep Learning (ENGG*6600*07)

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Introduction

- When looking at a scene or picture, our visual system, so as a machine learning model [1], focuses on or attends to some specific parts of the scene/image with more information and importance and ignores the less informative or less important parts.
- Moreover, when reading a **text**, especially when we want to try fast reading, one technique is skimming [2] in which our visual system or a model skims the data with high pacing and only attends to more informative words of sentences [3].
- The concept of attention can be modeled in machine learning where attention is a simple weighting of data. In the attention mechanism, the more informative or more important parts of data are given larger weights for the sake of more attention.





(a)

Mona Lisa is a portrait painted by Leonardo da Vinci.

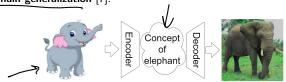
Mona Lisa is a portrait painted by Leonardo da Vinci.

(b)

Autoencoder and the Context Vector

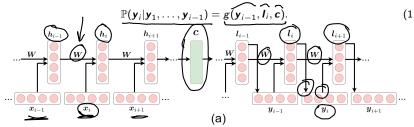


- Consider an autoencoder with encoder and decoder parts where the encoder gets an input
 and converts it to a context vector and the decoder gets the context vector and converts
 to an output.
- The output is related to the input through the context vector in the so-called <u>hidden</u> space.
- An autoencoder has an encoder (left part of autoencoder), a hidden space (in the middle), and a decoder (right part of autoencoder).
- For example, the input can be a sentence or a word in English and the output is the same sentence or word but in French. Assume the word "elephant" in English is fed to the encoder and the word "l'éléphant" in French is output. The context vector models the concept of elephant which also exists in the mind of human when thinking to elephant. This context is abstract in mind and can be referred to any fat, thin, huge, or small elephant [4].
- Another example for transformer is transforming a cartoon image of elephant to picture
 of a real elephant.
- As the autoencoder is transforming data from a domain to a hidden space and then to another domain, it can be used for domain transformation [5], domain adaptation [6], and domain generalization [7].



The Sequence-to-Sequence Model

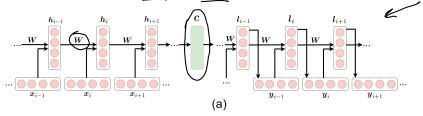
- The context is modeled as a vector in the hidden space. Let the context vector be denoted by $c \in \mathbb{R}^p$ in the <u>p-dimensional hidden space</u>.
- Consider a sequence of ordered tokens, e.g., a sequence of words which make a sentence. We want to transform this sequence to another related sequence. For example, we want to take a sentence in English and translate it to the same sentence in French. This model which transforms a sequence to another related sequence is named the sequence-to-sequence model [8].
- Suppose the number of words in a document or considered sentence be n. Let the ordered input tokens or words of the sequence be denoted by $\{x_1, x_2, \dots, x_{i-1}, \overline{x_i}, \dots, x_n\}$ and the output sequence be denoted by $\{y_1, y_2, \dots, y_{i-1}, \overline{y_i}, \dots, y_n\}$. As this figure illustrates, there exist latent vectors, denoted by $\{I_i\}_{i=1}^n$, in the decoder part for every word.
- In the sequence-to-sequence model, the probability of generation of the *i*-th word conditioning on all the previous words is determined by a function g(.) whose inputs are the immediate previous word y_{i-1}, the *i*-th latent vector f_i, and the context vector c:



The Sequence-to-Sequence Model

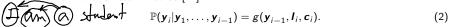
- In the sequence-to-sequence model, every word x_i produces a hidden vector h_i in the encoder part of the autoencoder. The hidden vector of every word, h_i , is fed to the next hidden vector, h_{i+1} , by a projection matrix W.
- In this model, for the whole sequence, there is only one context vector c which is equal to the last hidden vector of the encoder, i.e., $c = h_n$.

 Note that the encoder and decoder in the sequence-to-sequence model can be any sequential model such as RNN [9] or LSTM [10].



The Sequence-to-Sequence Model with Attention

• In the sequence-to-sequence model with attention [11, 12], the probability of generation of the i-th word is determined as [11]:

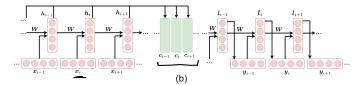


- In this model, in contrast to the sequence-to-sequence model which has only one context vector for the whole sequence, this model has a context vector for every word.
- The context vector of every word is a linear combination, or weighted sum, of all the hidden vectors; hence, the i-th context vector is:

$$c_i = \sum_{j=1}^n a_{ij} \mathbf{h}_j,$$
 (3)

where $a_{ij} \geq 0$ is the weight of h_i for the i-th context vector.

• This weighted sum for a specific word in the sequence determines which words in the sequence have more effect on that word. In other words, it determines which words this specific word "attends" to more. This notion of weighted impact, to see which parts have more impact, is called "attention".

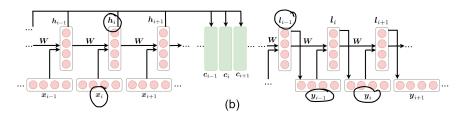


The Sequence-to-Sequence Model with Attention

- The original idea of arithmetic linear combination of vectors for the purpose of word embedding, similar to Eq. (3), was in the Word2Vec method [13, 14].
- The sequence-to-sequence model with attention considers a notion of similarity between the latent vector I_{i-1} of the decoder and the hidden vector h_i of the encoder [8]:

$$\mathbb{R}\ni (s_{ij}) = \text{similarity}(I_{i-1}, h_j). \tag{4}$$

• Intuition: The output word y_i depends on the previous latent vector I_{i-1} and the hidden vector h_j depends on the input word x_j . Hence, this similarity score relates to the impact of the input x_j on the output y_i . In this way, the score s_{ij} shows the impact of the j-th word to generate the i-th word in the sequence. This similarity notion can be a neural network learned by backpropagation [15].



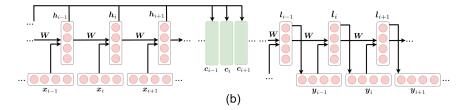
The Sequence-to-Sequence Model with Attention

 To make this score a probability, these scores should sum to one; hence, we make its softmax form as [11]:

$$\mathbb{R}\ni a_{ij}:=\frac{e^{s_{ij}}}{\sum_{k=1}^{n}e^{s_{ik}}}.$$
 (5)

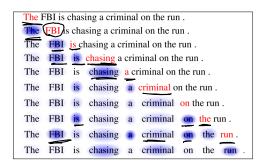
In this way, the score vector $[a_{i1}, a_{i2}, \dots, a_{in}]^{\top}$ behaves as a discrete probability distribution

• Therefore, In Eq. (3), $c_i = \sum_{i=1}^n a_{ij} h_j$, the weights sum to one and the weights with higher values attend more to their corresponding hidden vectors.

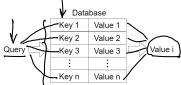


The Need for Composite Embedding

- Many of the previous methods for NLP, such as word2vec [13, 14, 16, 17] and GloVe [18], used to learn a representation for every word.
- However, for understanding how the words relate to each other, we can have a composite embedding where the compositions of words also have some embedding representation [19].
- For example, this figure shows a sentence which highlights the <u>relation of words</u>. This
 figure shows, when reading a word in a sentence, which previous words in the sentence we
 remember more. This relation of words shows that we need to have a composite
 embedding for natural language embedding.



 Consider a <u>database</u> with keys and values where a query is searched through the keys to retrieve a value [20].



• We can generalize this hard definition of query-retrieval to a <u>soft query-retrieval</u> where several keys, rather than only one key, can be corresponded to the query. For this, we calculate the <u>similarity of the query with all the keys</u> to see which keys are more similar to the query:

$$\underline{\operatorname{attention}(\boldsymbol{q}, \{\boldsymbol{k}_i\}_{i=1}^n, \{\boldsymbol{v}_i\}_{i=1}^n)} := \sum_{i=1}^n \boldsymbol{a}_i \boldsymbol{v}_i, \tag{6}$$

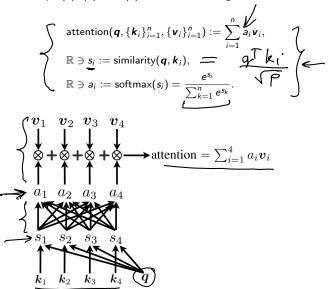
where:

$$\mathbb{R}\ni\underline{s_i}:=\text{similarity}(\mathbf{q},\mathbf{k}_i),\tag{7}$$

$$\mathbb{R} \ni \overline{a_i} := \operatorname{softmax}(s_i) = \frac{e^{s_i}}{\sum_{k=1}^n e^{s_k}},\tag{8}$$

and q, $\{k_i\}_{i=1}^n$, and $\{v_i\}_{i=1}^n$ denote the query, keys, and values, respectively.

• An illustration of Eqs. (6), (7), and (8) is shown in this figure.





• The <u>similarity</u> s_i can be any notion of <u>similarity</u>. Some of the well-known similarity measures are [21]:

$$\underline{\text{inner product:}} \ \underline{s_i} = \mathbf{q}^\top \mathbf{k}_i, \tag{9}$$

$$\underline{\text{general inner product:}} \ s_i = \boldsymbol{q}^\top \mathcal{N} \boldsymbol{k}_i, \tag{11}$$

additive similarity:
$$s_i = \boldsymbol{w}_q^{\top} \boldsymbol{q} + \boldsymbol{w}_k^{\top} \boldsymbol{k}_i$$
, (12)

where $\underline{W} \in \mathbb{R}^{p \times p}$, $w_q \in \mathbb{R}^p$, and $w_k \in \mathbb{R}^p$ are some learnable matrices and vectors.

• Among these similarity measures, the scaled inner product is used most often.

- The Eq. (6), attention $(q, \{k_i\}_{i=1}^n, \{v_i\}_{i=1}^n) := \sum_{i=1}^n a_i v_i$, calculates the attention of a target word (or query) with respect to every other input word (or keys) which are the previous and forthcoming words.
- Using Eq. (6), we see how similar the other words of the sequence are to that word. In other words, we see how impactful the other previous and forthcoming words are for generating a missing word in the sequence.
- Example:
 - Sentence: "I am a student".
 - We are processing the word "student".
 - ▶ Query: "student"
 - Values: "I", "am", "a"
 - Normalized similarity of the query and the values: weights 0.7, 0.2, and 0.1 for "I", "am", and "a", respectively.
 - The attention value for the word "student": $0.7 v_1 + 0.2 v_{am} + 0.1 v_a$.

Attention Formulation

-7 Word 2 Vee

- Let the words of a sequence of words be in a <u>d-dimensional space</u>, i.e., the sequence is $\{x_i \in \mathbb{R}^d\}_{i=1}^n$. This *d*-dimensional representation of words can be taken from any word-embedding NLP method such as <u>word2vec</u> [13, 14, 16, 17] or <u>GloVe</u> [18].
- The query, key, and value are projection of the words into <u>p-dimensional</u>, <u>p-dimensional</u>, and *r*-dimensional subspaces, respectively:

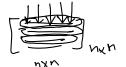
$$\begin{array}{c}
\mathbb{R} \stackrel{\longrightarrow}{\mathcal{P}} \stackrel{\longrightarrow}{\mathbf{k}}_i = \stackrel{\longrightarrow}{\mathbf{W}}_k^{\top} \mathbf{x}_i, & \\
\mathbb{R}^r \stackrel{\longrightarrow}{\mathcal{P}} \mathbf{w}_i = \stackrel{\longrightarrow}{\mathbf{W}}^{\top} \mathbf{x}_i, & \\
\end{array} \tag{14}$$

$$\longrightarrow \underline{\mathbb{R}'} \ni \underline{\mathbf{v}_i} = \underline{\mathbf{W}_V^\top} \mathbf{x}_i, \tag{15}$$

where $W_Q \in \mathbb{R}^{d \times p}$, $W_K \in \mathbb{R}^{d \times p}$, and $W_V \in \mathbb{R}^{d \times r}$ are the projection matrices into the low-dimensional query, key, and value subspaces, respectively.

- Consider the words, queries, keys, and values in matrix forms as $\boldsymbol{X} := [\boldsymbol{x}_1, \dots, \boldsymbol{x}_n] \in \mathbb{R}^{d \times n}, \; \boldsymbol{Q} := [\boldsymbol{q}_1, \dots, \boldsymbol{q}_n] \in \mathbb{R}^{p \times n}, \; \underline{\boldsymbol{K}} := [\boldsymbol{k}_1, \dots, \boldsymbol{k}_n] \in \mathbb{R}^{p \times n}, \; \text{and} \; \underline{\boldsymbol{V}} := [\boldsymbol{v}_1, \dots, \boldsymbol{v}_n] \in \mathbb{R}^{r \times n}, \; \text{respectively.}$
- In the similarity measures, such as the scaled inner product, we have the inner product $q^{\top}k_i$. Hence, the similarity measures contain $q^{\top}k_i = x_i^{\top}w_Q w_K^{\top}x_i$. This is like a kernel matrix so its behaviour is similar to the kappel for measuring similarity.

Attention Formulation



• Considering Eqs. (7), and (8) and the above definitions, the Eq. (6) can be written in matrix form, for the whole sequence of *n* words, as:

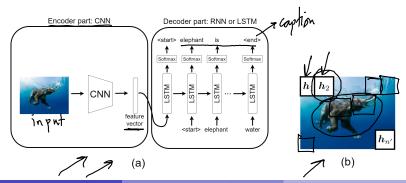
$$\underline{\mathbb{R}^{r \times n}} \ni \underline{Z} := \operatorname{attention}(Q, K, V) = \underbrace{V \operatorname{softmax}(\frac{1}{\sqrt{\rho}}Q^{\top}K)}_{\text{1}}$$
(16)

where $Z = [z_1, \ldots, z_n]$ is the attention values, for all the words, which shows how much every word attends to its previous and forthcoming words. In Eq. (16), the softmax operator applies the softmax function on every row of its input matrix so that every row sums to one.

 As the <u>queries</u>, <u>keys</u>, <u>and values</u> are all from the same words in the sequence, this attention is referred to as the "self-attention" [19].

Attention in Other Fields Such as Vision and Speech

- The attention concept has widely been used in NLP [11, 12]. Attention can be used in the field of computer vision [22]. Attention in computer vision means attending to specific parts of image which are more important and informative.
- We can consider the extracted low-layer features, which are different parts of image, as the hidden vectors {h_j}_{j=1}^{n'} in Eq. (4), where n' is the number of features for extracted image partitions. Similarity with latent vectors of decoder (LSTM) is computed by Eq. (4) and the query-retrieval model of attention mechanism, introduced before, is used to learn a self-attention on the images. Note that, as the partitions of image are considered to be the hidden variables used for attention, the model attends to important parts of input image.

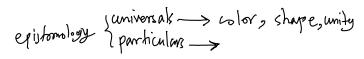


Attention in Other Fields Such as Vision and Speech

- Using attention in different fields of science is usually referred to as "attend, tell, and do something...".
- Some examples of applications of attention are caption generation for images (show, attend and tell) [22], caption generation for images with ownership protection (protect, show, attend and tell) [23], text reading from images containing a text (show, attend and read) [24], translation of one image to another related image (show, attend and translate) [25, 26], visual question answering (show, ask, attend, and answer) [27], human-robot social interaction (show, attend and interact) [28], and speech recognition (listen, attend and spell) [29, 30].

Transformer

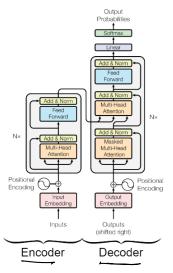
The Concept of Transformation



- As explained before, we can have an autoencoder which takes an input data, embeds data to a context vector which simulates a concept in human's mind [4], and generates an output. The input and output are related to each other through the context vector. In other words, the autoencoder transforms the input to a related output.
- An example for transformation is <u>translating</u> a sentence from a language to the same sentence in another language. Another example for transformer is <u>image captioning</u> in which the image is transformed to its caption explaining the content of image.
- An autoencoder, named "<u>transformer</u>", is proposed in the literature for the task for transformation [21].

Transformer Structure

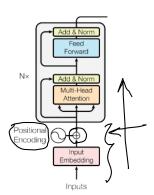
 The structure of transformer is depicted in this figure. A transformer is an autoencoder consisting of an encoder and a decoder.



Encoder of Transformer

Encoder of Transformer: Positional Encoding

- The <u>encoder part</u> of transformer embeds the <u>input sequence</u> of n words $X \in \mathbb{R}^{d \times n}$ into context vectors with the attention mechanism.
- We will explain later that transformer does <u>not have any recurrence and RNN or LSTM</u> module. As there is <u>no recurrence</u> and <u>no convolution</u>, the model has no sense of <u>order in sequence</u>. As the order of words is important for meaning of sentences, we need a way to account for the order of tokens or words in the sequence. For this, we can <u>add a vector accounting for the position to each input word embedding</u>.



Encoder of Transformer: Positional Encoding

• Consider the embedding of the *i*-th word in the sequence, denoted by $x_i \in \mathbb{R}^d$. For encoding the position of the *i*-th word in the sequence, the **position vector** $p_i \in \mathbb{R}^d$ can be set as:

$$p_{i}(2j+1) := \underline{\cos}\left(\frac{i}{10000^{\frac{2j}{p}}}\right),$$

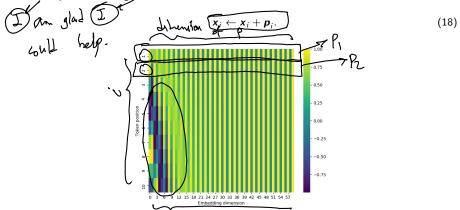
$$p_{i}(2j) := \underline{\sin}\left(\frac{i}{10000^{\frac{2j}{p}}}\right),$$

$$(17)$$

for all $j \in \{0,1,\ldots,\lfloor d/2 \rfloor\}$, where $\boldsymbol{p}_i(2j+1)$ and $\boldsymbol{p}_i(2j)$ denote the odd and even elements of \boldsymbol{p}_i , respectively.

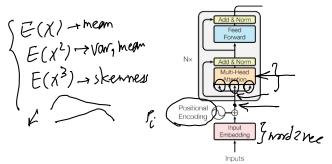
Encoder of Transformer: Positional Encoding

- This figure illustrates the dimensions of the position vectors across different positions.
 The position vectors for different positions of words are different as expected. Moreover, this figure shows that the difference of position vectors concentrate more on the initial dimensions of vectors.
- For incorporating the information of position with data, we add the positional encoding to the input embedding:



Multihead Attention with Self-Attention

- After positional encoding, data are fed to a <u>multihead attention</u> module with self-attention.
- This module applies the attention mechanism for h times.
- This several repeats of attention is for the reason explained here. The first attention determines how much every word attends to other words. The second repeat of attention calculates how much every pair of words attends to other pairs of words. Likewise, the third repeat of attention sees how much every pair of pairs of words attends to other pairs of pairs of words; and so on.
- This measure of attention or similarity between hierarchical pairs of words reminds us of the maximum mean discrepancy [31, 32] which measures similarity between different moments of data distributions.



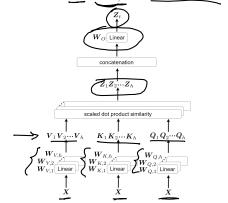
Multihead Attention with Self-Attention

 The data, which include positional encoding, are passed from linear layers for obtaining the gueries, values, and keys. These linear layers model linear projections introduced in Eqs. (13), (15), and (14), respectively. We have h of these linear layers to generate h set of queries, values, and keys as:

$$\longrightarrow \mathbb{R}^{p \times n} \ni \mathbf{Q}_i = \mathbf{W}_{Q,i}^{\top} \mathbf{X}, \quad \forall i \in \{1, \dots, h\},$$
 (19)

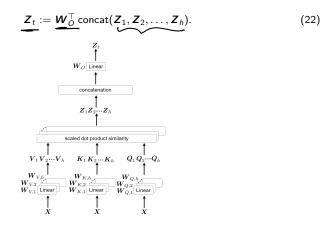
$$\longrightarrow \mathbb{R}^{p \times n} \ni Q_{i} = W_{Q,i}^{\top} X, \quad \forall i \in \{1, \dots, h\},
\longrightarrow \mathbb{R}^{p \times n} \ni V_{i} = W_{V,i}^{\top} X, \quad \forall i \in \{1, \dots, h\},
\longrightarrow \mathbb{R}^{r \times n} \ni K_{i} = W_{K,i}^{\top} X, \quad \forall i \in \{1, \dots, h\}.$$
(20)

$$\longrightarrow \mathbb{R}^{r \times n} \ni K_i = W_{K,i}^{\top} X, \quad \forall i \in \{1, \dots, h\}.$$
(21)



Multihead Attention with Self-Attention

• Then, the scaled dot product similarity, defined in Eq. (10) or (16), is used to generate the h attention values $\{Z_i\}_{i=1}^h$. These h attention values are concatenated to make a new long flattened vector. Then, by a linear layer, which is a linear projection, the total attention value, Z_t , is obtained:



Layer Normalization

• The data (containing positional encoding) and the total attention value are added:

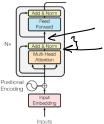
- This addition is inspired by the concept of residual introduced by <u>ResNet</u> [33].
- lacktriangle After this addition, a layer normalization is applied where for each hidden unit h_i we have:

$$h_i \leftarrow g(h_i - \mu),$$
 (24)

where μ and σ are the empirical mean and standard deviation over H hidden units:

$$\mu := \frac{1}{H} \sum_{i=1}^{H} h_i, \quad \sigma := \sqrt{\sum_{i=1}^{H} (h_i - \mu)^2}.$$
 (25)

 This is a standardization which makes the mean zero and the variance one; it is closely related to batch normalization and reduces the covariate shift [34].



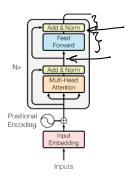
Feedforward Layer

- \bullet Henceforth, let Z'_t denote the total attention after both addition and layer normalization.
- We feed Z_t' to a feedforward network, having nonlinear activation functions, and then like before, we add the input of feedforward network to its output:

$$\mathbf{Z}_{t}^{\prime\prime} \leftarrow \mathbf{R} + \mathbf{Z}_{t}^{\prime},\tag{26}$$

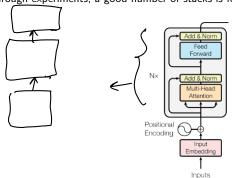
where R denotes the output of feedforward network.

- Again, layer normalization is applied and we, henceforth, denote the output of encoder by $\mathbf{Z}_{t}^{\prime\prime}$.
- This is the encoding for the whole input sequence or sentence having the information of attention of words and hierarchical pairs of words to each other.



Stacking

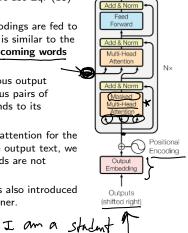
- The encoder is a **stack** of *N* identical layers.
- This stacking is for having **more learnable parameters** to have enough degree of freedom to learn the whole dictionary of words.
- Through experiments, a good number of stacks is found to be N = 6 [21].



Decoder of Transformer Masked Multihead Attention with Self-Attention



- A part of decoder is the masked multihead attention module whose input is the output embeddings $\{y_i\}_{i=1}^n$ shifted one word to the right.
- Positional encoding is also added to the output embeddings for including the information of their positions. For this, we use Eq. (18) where x_i is replaced by y_i .
- The output embeddings added with the positional encodings are fed to the masked multihead attention module. This module is similar to the multihead attention module but masks away the forthcoming words after a word.
- Therefore, every output word only attends to its previous output words, every pair of output words attends to its previous pairs of output words, every pair of pairs of output words attends to its previous pairs of pairs of output words, and so on.
- The reason for using the masked version of multihead attention for the output embeddings is that when we are generating the output text, we do not have the next words yet because the next words are not generated vet.
- This masking imposes some idea of sparsity which was also introduced by the **dropout** technique [35] but in a stochastic manner.

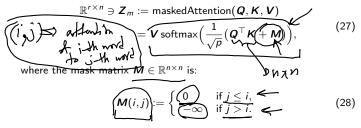


Output

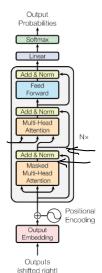
Probabilities

Masked Multihead Attention with Self-Attention

 Recall Eq. (16) which was used for multihead attention. The masked multihead attention is defined as:

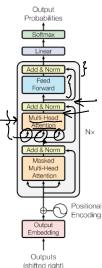


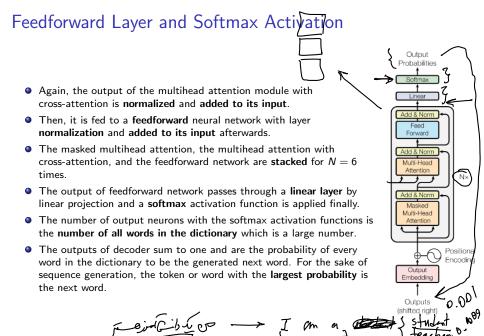
- As the softmax function has exponential operator, the mask does not have any impact for $j \leq i$ (because it is multiplied by $e^0 = 1$) and masks away for j > i (because it is multiplied by $e^{-\infty} = 0$). Note that $j \leq i$ and j > i correspond to the previous and next words, respectively, in terms of position in the sequence.
- Similar to before, the output of masked multihead attention is normalized and then is added to its input.



Multihead Attention with Cross-Attention

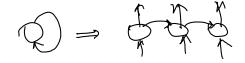
- The output of masked multihead attention module is fed to a multihead attention module with cross-attention.
- This module is not self-attention because all its values, keys, and queries are not from the same sequence but its values and keys are from the output of encoder and the queries are from the output of the masked multihead attention module in the decoder.
- In other words, the values and keys come from the processed input embeddings and the queries are from the processed output embeddings.
- The calculated multihead attention determines how much every output embedding attends to the input embeddings, how much every pair of output embeddings attends to the pairs of input embeddings, how much every pair of pairs of output embeddings attends to the pairs of pairs of input embeddings, and so on.
- This shows the connection between input sequence and the generated output sequence.





Complexity of Attention

Attention is All We Need!



- The <u>output of decoder</u> is fed to the masked multihead attention module of decoder with some shift.
- This is not a notion of recurrence. Hence, we see that there is not any recurrent module like RNN [9] and LSTM [10] in transformer. Therefore, attention is all we need to learn a sequence and there is no need to any recurrence module.
- The proposal of transformers [21] was a <u>breakthrough in NLP</u>; the state-of-the-art NLP methods are all based on transformers nowadays.

Complexity Comparison

- In self-attention, we learn attention of every word to every other word in the sequence of n words. Also, we learn a p-dimensional embedding for every word. Hence, the complexity of operations per layer is $O(n^2p)$. This is while the complexity per layer in recurrence is $O(np^2)$.
- Although, the complexity per layer in self-attention is worse than recurrence, many of its operations can be performed in **parallel** because all the words of sequence are processed simultaneously, as also explained in the following. Hence, the $\mathcal{O}(n^2p)$ is not very bad for being able to parallelize it. That is while the recurrence cannot be parallelized for its sequential nature.
- As for the <u>number of sequential operations</u>, the self-attention mechanism <u>processes all</u> the *n* words simultaneously so its sequential operations is in the order of $\mathcal{O}(1)$. As recurrence should process the words <u>sequentially</u>, the number of its sequential operations is of order $\mathcal{O}(n)$.
- As for the maximum path length between every two words, self-attention learns attention between every two words; hence, its maximum path length is of the order $\mathcal{O}(1)$. However, in recurrence, as every word requires a path with a length of a fraction of sequence (a length of n in the worst case) to reach the process of another word, its maximum path length is $\mathcal{O}(n)$.

Table 1. Comparison of complexities between self-attention and recurrence (Vaswani et al., 2017).

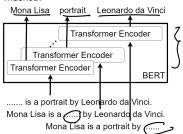
	Complexity per layer	Sequential operations	Maximum path length
Self-Attention	$\mathcal{O}(n^2p)$	$\mathcal{O}(1)$	$\mathcal{O}(1)$
Recurrence	$\mathcal{O}(np^2)$	$\mathcal{O}(n)$	$\mathcal{O}(n)$

BERT

BERT



- BERT (Bidirectional Encoder Representations from Transformers) [36] is one of the state-of-the-art methods for NLP. It is a stack of encoders of transformer. In other words, it is built using transformer encoder blocks.
- Although some NLP methods such as XLNet [37] have slightly outperformed it, BERT is still one of the best models for different NLP tasks such as question answering [38], natural language understanding [39], sentiment analysis, and language inference [40].
- BERT uses the technique of masked language modeling. It masks 15% of words in the input document/corpus and asks the model to predict the missing words. A sentence with a missing word is given to every transformer encoding block in the stack and the block is supposed to predict the missing word.
- It is an <u>unsupervised</u> manner because any word can be masked in a sentence and the
 output is supposed to be that word. As it is unsupervised and does not require labels, the
 huge text data of Internet can be used for training the BERT model where words are
 randomly selected to be masked.



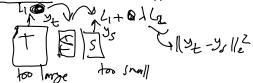
BFRT



- BERT learns to predict the missing word based on attention to its previous and forthcoming words so it is bidirectional. Hence, BERT jointly conditions on both left (previous) and right (forthcoming) context of every word.
- Moreover, as the missing word is predicted based on the other words of sentence, BERT embeddings for words are context-aware embeddings. Therefore, in contrast to word2vec [13, 14, 16, 17] and GloVe [18] which provide a single embedding per each word, every word has different BERT embeddings in various sentences.
- The BERT embeddings of words differ in different sentences based on their context. For example, the word "bank" has different meanings and therefore different embeddings in the sentences "Money is in the bank" and "Some plants grow in bank of rivers".
- It is also noteworthy that, for an input sentence, BERT outputs an embedding for the whole sentence in addition to giving embeddings for every word of the sentence. This sentence embedding is not perfect but works well enough in applications. One can use the BERT sentence embeddings and train a classifier on them for the task of spam detection or sentiment analysis.
- The BERT model is usually not trained from the scratch as its training has been done in a long time on huge amount of Internet data. For using it in different NLP applications, such as sentiment analysis, researchers usually do transfer learning and add one or several neural network layers on top of a pre-trained BERT model and train the network for their own task. During training, one can either freeze the weights of the BERT model and just train the added layers or also fine tune BERT weights by backpropagation.

BERT

- The parameters of encoder in transformer [21] are $\underline{6}$ encoder layers, $\underline{512}$ hidden layer units in the fully connected network and $\underline{8}$ attention heads (h=8).
- This is while BERT [36] has 24 encoder layers, 1024 hidden layer units in the fully connected network and 16 attention heads (h = 16).
- Usually, when we say BERT, we mean the <u>large BERT</u> [36] with the above-mentioned parameters.
- As the BERT model is huge and requires a lot of memory for saving the model, it cannot easily be used in embedded systems. Hence, many commercial smaller versions of BERT are proposed with less number of parameters and number of stacks. Some of these smaller versions of BERT are small BERT [41], tiny BERT [42], DistilBERT [43], and Roberta BERT [44].
- Some BERT models, such as clinical BERT [45] and BioBERT [46], have also been trained on medical texts for the biomedical applications.



- GPT (Generative Pre-trained Transformer), or GPT-1, [47] is another state-of-the-art method for NLP.
- It is a stack of <u>decoders of transformer</u>. In other words, it is built using <u>transformer</u> <u>decoder blocks</u>.
- In GPT, the multihead attention module with cross-attention is removed from the decoder of transformer because there is no encoder in GPT.
- Hence, the decoder blocks used in GPT have only positional encoding, masked multihead self-attention module and feedforward network with their adding, layer normalization, and activation functions.
- As GPT uses the masked multihead self-attention, it considers attention of word, pairs of words, pairs of pairs of words, and so on, only on the previous (left) words, pairs of words, pairs of pairs of words, and so on. In other words, GPT is not bidirectional and conditions only on the previous words and not the forthcoming words.
- The objective of BERT was to <u>predict a masked word</u> in a sentence. However, GPT model is used for <u>language model</u> [48, 49, 50] whose objective is to <u>predict the next word</u>, in an <u>incomplete sentence</u>, given all of the previous words.
- The predicted new word is then added to the sequence and is fed to the GPT as input
 again and the other next word is predicted. This goes on until the sentences get complete
 with their next coming words.
- In other words, GPT model takes some document and continues the text in the best and related way. For example, if the input sentences are about psychology, the trained GPT model generates the next words and sentences also about psychology to complete the document.
- As any text without label can be used for predicting the next words in sentences, GPT is an unsupervised method making it possible to be trained on huge amount of Internet

- The successors of GPT-1 [47] are GPT-2 [51] and GPT-3 [52]. GPT-2 and GPT-3 are extension of GPT-1 with more number of stacks of transformer decoder. Hence, they have more learnable parameters and can be trained with more data for better language modeling and inference.
- For example, **GPT-2** has **1.5** billion parameters.
- GPT-2 and especially GPT-3 have been trained with <u>much more Internet data</u> with various <u>general and academic subjects</u> to be able to <u>generate text in any subject</u> and <u>style</u> of interest. For example, GPT-2 has been trained on <u>8 million web pages</u> which contain 40GB of Internet text data.
- GPT-2 is a quite large model and cannot be easily used in <u>embedded systems</u> because of requiring large memory. Hence, different sizes of GPT-2, like <u>small, medium, large, Xlarge, and DistilGPT-2</u>, are provided for usage in embedded systems, where the number of stacks and learnable parameters differ in these versions. These versions of GPT-2 can be found and used in the <u>HuggingFace transformer Python package [53]</u>.
- GPT-2 has been used in many different applications such as <u>dialogue systems</u> [54], patent claim generation [55], and <u>medical text simplification</u> [56]. A combination of GPT-2 and BERT has been used for <u>question answering</u> [57].
- It is noteworthy that GPT can be seen as few shot learning [52]. A comparison of GPT and BERT can also be found in [58].

 meta learning

- GPT-3 is a very huge version of GPT with so many number of stacks and learnable parameters. For comparison, note that GPT-2, NVIDIA Megatron [59], Microsoft Turing-NLG [60], and GPT-3 [52] have 1.5 billion, 8 billion, 17 billion, and 175 billion learnable parameters, respectively.
- This huge number of parameters allows GPT-3 to be trained on very huge amount of Internet text data with various subjects and topics.
- Hence, GPT-3 has been able to learn almost all topics of documents and even some people are discussing whether it can pass the Turing's writer's test [61, 62].
- Note that GPT-3 has <u>kind of memorized</u> the texts of all subjects but **not in a bad way**, i.e., overfitting, rather in a good way. This memorization is because of the <u>complexity of huge number of learnable parameters</u> [63] and not <u>being overfitted is because of being trained by big enough Internet data</u>.
- GPT-3 has had many different interesting applications such as <u>fiction and poetry</u> generation [64].

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