

Do your eyes see a trend?

\*R.W. =  
random  
walk

Yes

No

$$\Delta y_t = \alpha + \rho y_{t-1} + \beta \cdot t + \text{other covariates} + \text{lags of } \Delta y_{t-s} + a_t$$

phi2 statistic from ur.df type=trend

$$H_0: \alpha = \rho = \beta = 0$$

$H_a: \alpha \neq 0$  or  $\rho \neq 0$  or  $\beta \neq 0$  or some combination

reject

accept

check tau3  
statistic

$$H_0: \rho = 0, H_a: \rho \neq 0$$

reject

accept

stationary ARMA  
use OLS or MLE  
to test coefficients

R.W. w/ drift  
where is the drift  
coming from?  
drift rate (intercept)  
or deterministic trend?  
phi3 statistic can  
give some insight

$$H_0: \rho = \beta = 0$$

$H_a: \beta \neq 0$  or  $\rho \neq 0$

reject

accept

Deterministic  
trend could  
exist w/in the  
R.W. along  
w/ drift

R.W. w/  
drift and  
no trend

Case 2:

$$\Delta y_t = \alpha + \rho y_{t-1} + \text{other covariates} + \text{lags of } \Delta y_{t-s} + a_t$$

Notice  $y_t = \alpha + (1+\rho)y_{t-1} + \text{other covariate} + \text{lags of } \Delta y_{t-s} + a_t$

(testing  $\rho < 0$  implies stationary)

phi1 statistic from ur.df type=drift

$$H_0: \alpha = \rho = 0 \text{ R.W., no drift}$$

$H_a: \alpha \neq 0$  or  $\rho \neq 0$  stationary AR

reject

accept

check tau2  
statistic

$$H_0: \rho = 0, H_a: \rho \neq 0$$

reject

accept

stationary  
ARMA

R.W. w/ drift  
GO TO CASE 4

Probably  
R.W. no drift  
check tau2

reject

accept

stationary  
ARMA

R.W.  
no  
drift

Difficult to distinguish  
these. Typically choose  
between stationary ARMA,  
R.W. w/ no drift,  
R.W. w/ drift.