

## 4 HARMONY 2018 proposal

**This section is a work-in-progress that is based on discussion that took place on the FBC PWG mailing list and HARMONY 2018 meeting in Oxford.**

Note that where text (or UML) defined in previous FBC specifications has been changed it has been colored red.

The proposed Flux Balance Constraints package version 3 extends the definition of the **FluxObjective**, extends the definition of the **chemicalFormula**, defines a **UserConstraint** and adds a generic **KeyValuePair** annotation.

### 4.1 The extended Model class

The **SBML Model** class is extended by a **listOfUserConstraints** of which it may contain at most one, see also Figure 12.

#### 4.1.1 Type FbcVariableType

The Flux Balance Constraints package defines a new enumerated type **FbcVariableType** which represents the index of a variable that occurs in either the **FluxObjective** or **UserConstraintComponent**. It contains the following two values, “linear” or “quadratic”.

#### 4.1.2 The FBC listOfUserConstraints

As shown in Figure 12 the **ListOfUserConstraints** is derived from **SBase** and inherits the attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. The **ListOfUserConstraints** must contain at least one **UserConstraint** (defined in Section 4.4).

### 4.2 The extended Species class

#### The chemicalFormula attribute

The optional attribute **chemicalFormula** containing a **string** that represents the **Species** objects elemental composition.

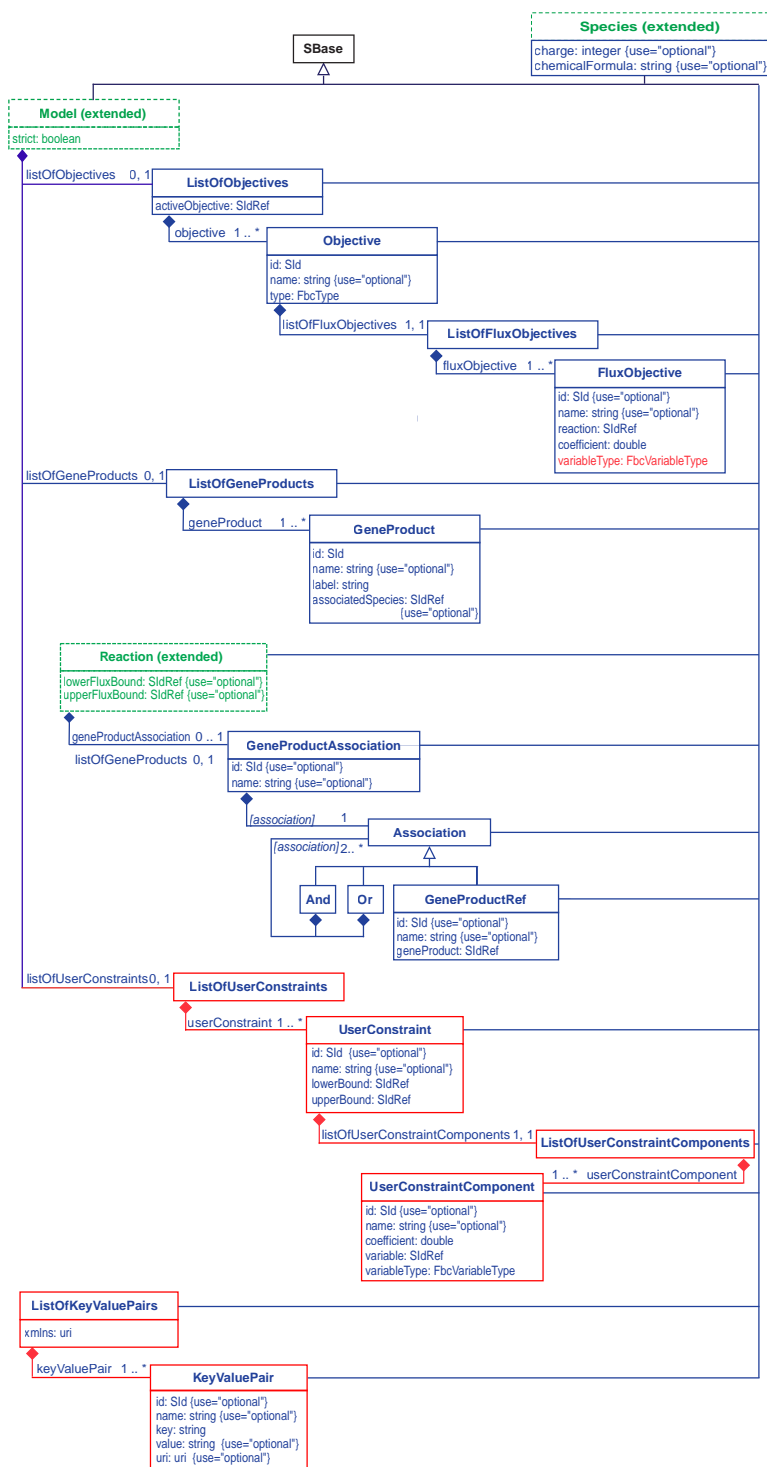
```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP" compartment="Cytosol"
  boundaryCondition="false" initialConcentration="0" hasOnlySubstanceUnits="false"
  fbc:charge="-4" fbc:chemicalFormula="C10H12N5O13P3"/>

<species metaid="meta_M1" id="M1" compartment="C" boundaryCondition="false"
  initialConcentration="0" hasOnlySubstanceUnits="false" fbc:charge="0"
  fbc:chemicalFormula="RCONH2"/>

<species metaid="meta_M2" id="M2" compartment="c" boundaryCondition="false"
  initialConcentration="0" hasOnlySubstanceUnits="false" fbc:charge="0"
  fbc:chemicalFormula="C2H4O2(CH2)n"/>
```

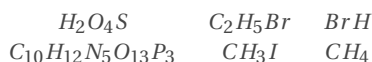
While there are many ways of referring to an elemental composition, the purpose of the **chemicalFormula** attribute is to enable reaction balancing and validation, something of particular importance in constraint-based models.

The format of the **chemicalFormula** should, whenever possible, consist only of atomic names (as in the Periodic Table). Similarly, for enhanced inter-operability, the element order should be arranged according to the Hill system (see Table 2) (Hill, 1900, 2012). Using this notation the number of carbon atoms in a molecule is indicated first, followed by the number of hydrogen atoms and then the number of all other chemical elements in alphabetical order. When the formula contains no carbon; all elements, including hydrogen, are listed alphabetically. Where there is more than a single atom present, this is indicated with an integer that follows the element symbol.



**Figure 10:** A UML representation of the Flux Balance Constraints package version three. Derived from **SBase**, most **FBC** classes inherit support for constructs such as **SBML Notes** and **Annotation**'s. The `[association]` element name is the name of the class, de-capitalized. In this case, the possible values are "and", "or", or "geneProductRef". See [Section 1.4](#) for conventions related to this figure. The individual classes are further discussed in the text.

However, in certain situations it does become necessary to use a generic symbol in a user defined compound. For example, such symbols can include R and X and have the general form of a single capital letter followed by zero or



**Table 2:** Examples of chemical formulas written using the Hill System. As described in [Section 4.2](#)

more lowercase letters. In addition, the undefined parenthesised group index  $(\dots)_n$  may also be used. Note that



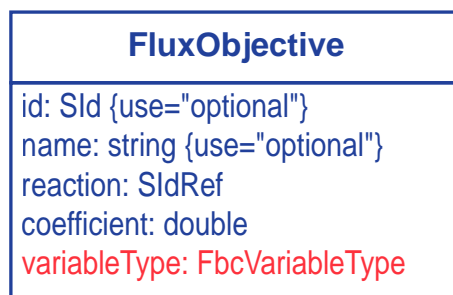
**Table 3:** Examples of chemical formulas written using allowed non-Hill symbols, as described in [Section 4.2](#).

in this case only the subscript  $n$  is allowed, integer values  $(\dots)_2$  and expressions such as  $(\dots)_{n-1}$  are considered invalid.

However, the use of R, X and  $(\dots)_n$  is not advised, as any **Reaction** in which such a **Species** occurs cannot necessarily be balanced. Therefore, any **chemicalFormula** that contains any of the aforementioned, non-Hill compatible symbols will raise a ‘best practices’ warning on model validation.

### 4.3 The FBC **FluxObjective** class

The FBC **FluxObjective** class is derived from **SBML SBBase** and inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. The **FluxObjective** class is a relatively simple container for a model variable that



**Figure 11:** A UML representation of the Flux Balance Constraints package **FluxObjective** class. For a complete description see [Figure 1](#) as well as [Section 1.4](#) for conventions related to this figure.

can be expressed as a ‘linear’ or ‘quadratic’, weighted by a signed linear coefficient.

#### The **id** and **name** attributes

A **FluxObjective** has two optional attributes: **id** an attribute of type **SId** and **name** an attribute of type **string**.

#### The **reaction** and **coefficient** attributes

The required **reaction** is of type **SIdRef** and is restricted to refer only to a **Reaction** while the **coefficient** attribute holds a **double** referring to the coefficient that this **FluxObjective** takes in the enclosing **Objective**.

#### The **variableType** attribute

The required **variableType** attribute contains a **FbcVariableType** that represents the index to which a variable is raised in a **FluxObjective**. For example, where  $J_x$  represents a steady-state flux the **FbcVariableType** defines either a “linear”,  $J_x^1$  or “quadratic”,  $J_x^2$  term.

**Flux objectives: example code**

An objective with purely linear terms in LP format: Maximize: 1 R1 + 2 R2

```
<fbc:listOfObjectives fbc:activeObjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
    <fbc:listOfFluxObjectives>
      <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1" fbc:variableType="linear"/>
      <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2" fbc:variableType="linear"/>
    </fbc:listOfFluxObjectives>
  </fbc:objective>
</fbc:listOfObjectives>
```

Similarly, an objective with a quadratic term in LP format: Minimize: 1 R1 + [4 R2<sup>2</sup>]/2

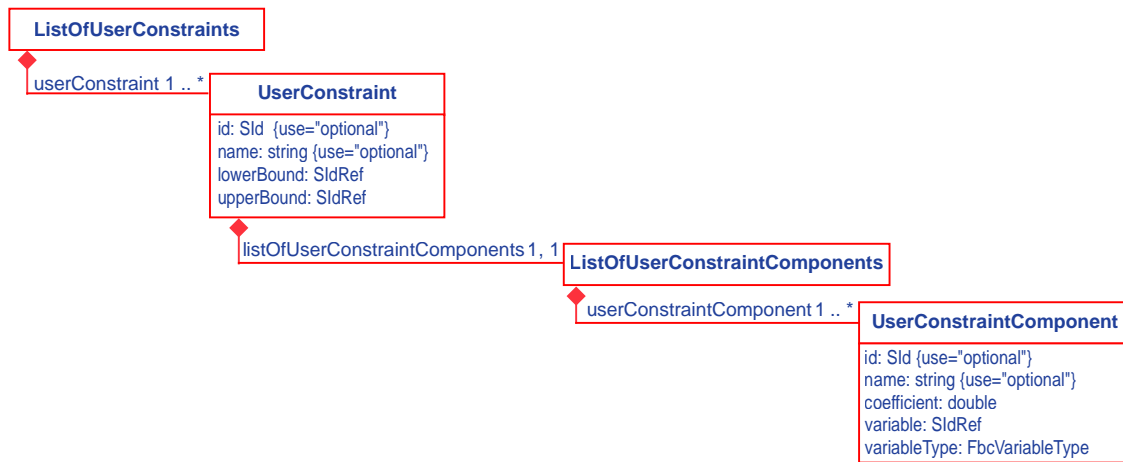
```
<fbc:listOfObjectives fbc:activeObjective="obj2">
  <fbc:objective fbc:id="obj2" fbc:type="minimize">
    <fbc:listOfFluxObjectives>
      <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1" fbc:variableType="linear"/>
      <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2" fbc:variableType="quadratic"/>
    </fbc:listOfFluxObjectives>
  </fbc:objective>
</fbc:listOfObjectives>
```

**Units**

As described above the linear **FluxObjective** defined here as  $n \cdot J$  where the **coefficient** ( $n$ ) is dimensionless and the **value** ( $J$ ) takes the units of the **reaction** flux i.e., “extent per time”. Therefore, the linear **FluxObjective**, ( $n \cdot J$ ) has the unit  $\frac{\text{extent}}{\text{time}}$  where the units of reaction “extent” and “time” are defined globally. Analogously, in the case of a quadratic **FluxObjective**,  $n \cdot J^2$  this would be  $\frac{\text{extent}^2}{\text{time}^2}$ .

**4.4 The FBC UserConstraint class**

The FBC **UserConstraint** class is derived from **SBML SBase** and inherits **metaid** and **sboTerm**, as well as the sub-components for **Annotation** and **Notes**. Its purpose is to define non-stoichiometric constraints, that is constraints that are not necessarily defined by the stoichiometrically coupled reaction network. In order to achieve we defined a new type of linear constraint, the **UserConstraint**.



**Figure 12:** A UML representation of the **SBML Model** class extended in the Flux Balance Constraints package by the **ListOfUserConstraints**. See Section 1.4 for conventions related to this figure.

Analogous to the attributes described in [Section 3.8](#) the `lowerBound` and `upperBound` form the boundaries of the `UserConstraint`.

$$\text{UserConstraint} = \text{value} \quad (4)$$

$$\text{UserConstraint} \geq \text{lowerBound value} \quad (5)$$

$$\text{UserConstraint} \leq \text{upperBound value} \quad (6)$$

Defining either an equality if both `lowerBound` and `upperBound` refer to the same parameter (Equation 4) or set of inequalities (Equations 4 and 5).

The `UserConstraint` contains a `ListOfUserConstraintComponents` representing a linear combination of `UserConstraintComponents`. Similar to a `FluxObjective` each `UserConstraintComponent` contains a coefficient-variable pair where the `coefficient` refers to a `Parameter`. In addition to a `Reaction` a `UserConstraintComponent` allows the `variable` to refer to non-constant `Parameter` thus allowing the definition of non-reaction, artificial, variables.

#### *The id and name attributes*

A `UserConstraint` has an optional `id` of type `SId` and an optional attribute `name` of type `string`.

#### *The lowerBound attribute*

The required `lowerBound` attribute contains an `SIdRef` that references a `Parameter` which contains the lower boundary value of the `UserConstraint`.

#### *The upperBound attribute*

The required `upperBound` attribute contains an `SIdRef` that references a `Parameter` which contains the upper boundary value of the `UserConstraint`.

#### *The listOfUserConstraintComponents element*

The element `listOfUserConstraintComponents` which contains a `ListOfUserConstraintComponents` is derived from and functions like a typical `SBML ListOf__` class with the restriction that it must contain one or more elements of type `UserConstraintComponent` (see [Section 4.5](#)). This implies that if a `UserConstraint` is defined there should be at least one `UserConstraintComponent` contained in a `ListOfUserConstraintComponents`.

## 4.5 The FBC `UserConstraintComponent` class

The FBC `UserConstraintComponent` class is derived from `SBML SBBase` and inherits `metaid` and `sboTerm`, as well as the subcomponents for `Annotation` and `Notes`. The `UserConstraintComponent` class is a relatively simple container for a variable and a variable type specifier which is weighted by a signed coefficient.

#### *The id and name attributes*

An `UserConstraintComponent` has an optional `id` of type `SId` and an optional attribute `name` of type `string`.

#### *The coefficient attribute*

The required `coefficient` attribute contains an `SIdRef` that is restricted to reference only a constant `Parameter` which holds the coefficient value. In `strict` mode a `Parameter` whose `SId` is referenced by a `coefficient`, as in the case of a `FluxObjective` coefficient, has to be constant and not take the value `NaN` or  $\pm\text{inf}$ .

#### *The variable attribute*

The required `variable` attribute contains an `SIdRef` that is restricted to reference the `SId` of either a `Reaction` or a non-constant `Parameter`. Conversely, if such non-constant `Parameter`'s `SId` is referenced by a `UserConstraintComponent`'s `variable` attribute it may not be referenced by any `coefficient`, `lowerFluxBound` or `upperFluxBound`.

attribute.

### The variableType attribute

The required `variableType` attribute contains a `FbcVariableType` that indicates whether a variable should be considered as 'linear' or 'quadratic'.

### User constraints: example code

The following example illustrates the encoding of the following two `UserConstraints`:

$$RGLX - RXLG = 5 \quad (7)$$

$$2 \cdot Avar - RGDP \geq 2 \quad (8)$$

```
<listOfParameters>
  <parameter id="uc1" value="5" constant="True"/>
  <parameter id="uc2lb" value="2" constant="True"/>
  <parameter id="uc2ub" value="INF" constant="True"/>
  <parameter id="ucco1a" value="1" constant="True"/>
  <parameter id="ucco1b" value="-1" constant="True"/>
  <parameter id="ucco2a" value="2" constant="True"/>
  <parameter id="ucco2b" value="-1" constant="True"/>
  <parameter id="Avar" value="NaN" constant="False"/>
</listOfParameters>

<fbc:listOfUserConstraints>
  <fbc:userConstraint fbc:id="uc1" fbc:lowerBound="uc1" fbc:upperBound="uc1">
    <fbc:listOfUserConstraintComponents>
      <fbc:userConstraintComponent fbc:coefficient="ucco1a" fbc:variable="RGLX"
        variableType="linear"/>
      <fbc:userConstraintComponent fbc:coefficient="ucco1b" fbc:variable="RXLG"
        variableType="linear"/>
    </fbc:listOfUserConstraintComponents>
  </fbc:userConstraint>
  <fbc:userConstraint fbc:id="uc2" fbc:lowerBound="uc2lb" fbc:upperBound="uc2ub">
    <fbc:listOfUserConstraintComponents>
      <fbc:userConstraintComponent fbc:coefficient="ucco2a" fbc:variable="Avar"
        variableType="linear"/>
      <fbc:userConstraintComponent fbc:coefficient="ucco2b" fbc:variable="RGLX"
        variableType="linear"/>
    </fbc:listOfUserConstraintComponents>
  </fbc:userConstraint>
</fbc:listOfUserConstraints>
```

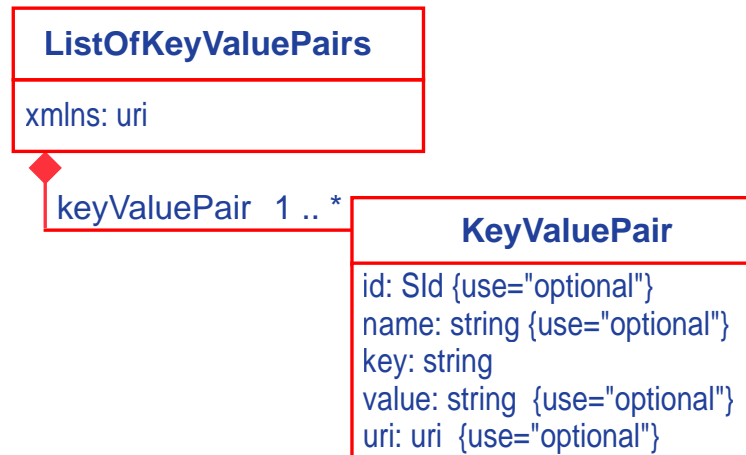
## 4.6 The FBC ListOfKeyValuePairs class

The `ListOfKeyValuePairs`, see Figure 13 for details, forms the basis of a controlled annotation defined by the Flux Balance Constraints package. This element defines a 'structured note' or 'descriptive list' of keys and associated values.

```
<annotation>
  <listOfKeyValuePairs xmlns="http://sbml.org/fbc/keyvaluepair">
    <keyValuePair key="keyX" uri="http://bgoli.net/kvp/spec_example.html" value="47"/>
    <keyValuePair key="ZZkey" uri="urn:sbml:fbc:kvp:html:spec_example" value="level_5"/>
    <keyValuePair key="x-factor" uri="http://bgoli.net/kvp/spec_example.html"
      value="intangible_metaphysical_property"/>
  </listOfKeyValuePairs>
</annotation>
```

As such it is analogous to the official **SBML** RDF annotation used to support MIRIAM annotations, as defined in the **SBML** specification documents. When an annotation that declares the `xmlns http://sbml.org/fbc/keyvaluepair`

then it must have the format specified here. Tools may chose to support reading and interpreting the content as described, but may optionally ignore the annotation and merely round trip it with any other third party annotations. As is the case with the RDF/MIRIAM annotations, support for **ListOfKeyValuePair**s will be included in the **SBML** support libraries. The **ListOfKeyValuePair**s functions like a typical **SBML ListOf\_\_** class with the restriction



**Figure 13:** A UML representation of the **SBML SBase** class extended in the Flux Balance Constraints package by the **ListOfKeyValuePair**. See [Section 1.4](#) for conventions related to this figure.

that it must contain one or more elements of type **KeyValuePair** (see [Section 4.7](#)). In addition it defines a single mandatory attribute, **xmlns**, which identifies the annotation as belonging to the Flux Balance Constraints package.

#### The **xmlns** attribute

The **xmlns** is a mandatory component of the **ListOfKeyValuePair**, is of the type **uri** and must have the value <http://sbml.org/fbc/keyvaluepair>.

## 4.7 The FBC **KeyValuePair** class

The FBC **KeyValuePair** class is derived from **SBase** and inherits the attribute **metaid**, **sboTerm** as well as the sub-components needed for **Notes**. It's sole purpose is to define a key–value pair with an extended key definition.

The **KeyValuePair** defines a single mandatory attribute the **key** as well as two optional attributes: **value** and **uri**.

#### The **id** and **name** attributes

A **KeyValuePair** has two optional attributes: **id** an attribute of type **SId** and **name**, an attribute of type **string**.

#### The **key** attribute

The **key** is the mandatory component of the **KeyValuePair** pair and is of type **string**. It has the special property that every **key** in an enclosing **ListOfKeyValuePair** must be unique.

#### The **value** attribute

The optional **value** attribute is of **string** and contains the value associated with a particular **key**. If not present, the **KeyValuePair** is defined as having no value.

#### The **uri** attribute

The optional attribute **uri** is of type **uri**. This attribute identifies a resource that defines the associated **key** component of the **KeyValuePair**, see [Table 4](#) for examples. As a best practice, it is highly recommended that all tools

Type	Example	Description
<b>urn</b>	urn:bgoli.net:example:kvp	a tool specific namespace declaration
<b>url</b>	<a href="http://bgoli.net/kvp/spec_example.html">http://bgoli.net/kvp/spec_example.html</a>	a url identifying a set of <b>key</b> definitions

**Table 4:** Examples of how the **uri** attribute can be used to identify **key** definitions by **urn** or **url**.

implementing a **KeyValuePair** also implement support for the **uri** attribute.

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