4 Proposal for FBC version 3: HARMONY 2018

The proposed Flux Balance Constraints package version 3 extends the definition of the **FluxObjective**, extends the definition of the `chemicalFormula`, redefines `charge` as a double, defines a **UserConstraint** and adds a generic **KeyValuePair** annotation.

> **The extensions and modifications contained in this document are proposed as version 3 of the Flux Balance Constraints package. This proposal is been formulated through open discussions on the FBC PWG mailing list and intense discussion during HARMONY 2018.**

Please note that where specification text (or UML) has been modified and diverges from the Flux Balance Constraints package version 2 specification, it has been colored red.

4.1 The extended Model class (updates specification Section 3.3)

The **SBML Model** class is extended by a `listOfUserConstraints` of which it may contain at most one, see Figure 13.

4.1.1 Type `FbcVariableType`

The Flux Balance Constraints package defines a new enumerated type `FbcVariableType` which represents the index of a variable that occurs in either the **FluxObjective** or **UserConstraintComponent**. It contains the following two values, "`linear`" or "`quadratic`".

4.1.2 The FBC listOfUserConstraints

As shown in Figure 13 the **ListOfUserConstraints** is derived from ***SBase*** and inherits the attributes `metaid` and `sboTerm`, as well as the subcomponents for **Annotation** and **Notes**. The **ListOfUserConstraints** must contain at least one **UserConstraint** (defined in Section 4.4).

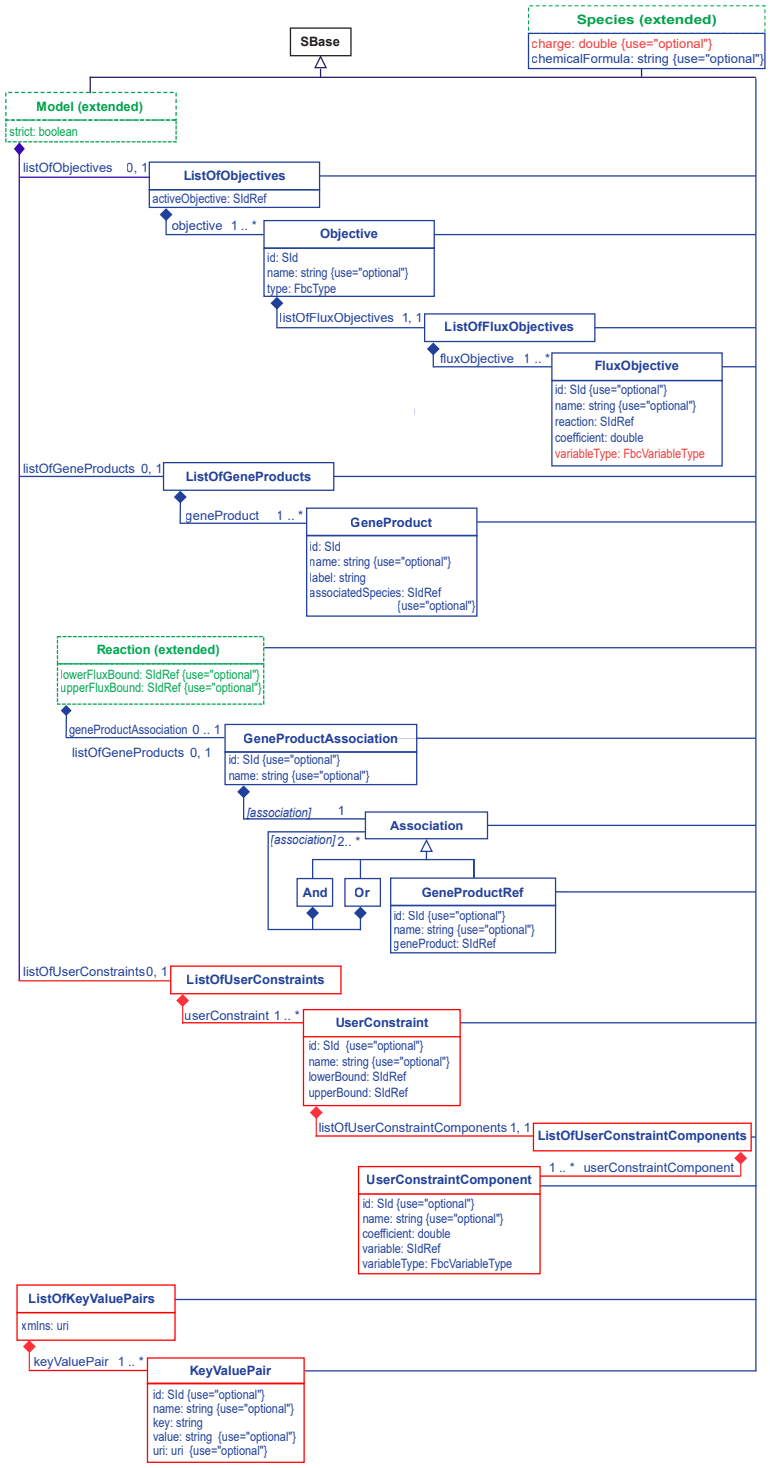

Figure 10: *A UML representation of the Flux Balance Constraints package version three. Derived from* ***SBase****, mostFBC classes inherit support for constructs such as SBML* ***Notes*** *and* ***Annotation****'s. The [association] element name is the name of the class, de-capitalized. In this case, the possible values are "and", "or", or "geneProductRef". See Section 1.4 for conventions related to this figure. The individual classes are further discussed in the text.*

4.2 The extended Species class (updates specification Section 3.4)

The Flux Balance Constraints package extends the SBML Level 3 Version 1 Core **Species** class with the addition of two attributes `charge` and `chemicalFormula`.

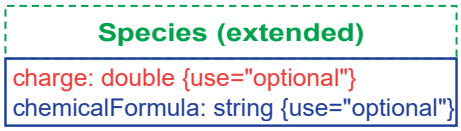

Figure 11: *A UML representation of the extended **SBML Species** class used in the Flux Balance Constraints package. See Section 1.4 for conventions related to this figure.*

The `charge` *attribute*

The optional attribute charge contains a signed double referring to the Species object's charge (in terms of electrons, not the SI unit coulombs). Note, that unlike FBC versions one and two a **Species** may, for the purposes of charge, be interpreted as a pseudoisomer or aggregate molecule and may assume a non-integer value. Non-integer charges should be used with caution as their use may have unintended side-effects, for example, with respect to the accuracy of reaction balancing.

The `chemicalFormula` *attribute*

The optional attribute `chemicalFormula` containing a `string` that represents the **Species** objects elemental composition.

```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP" compartment="Cytosol"
 boundaryCondition="false" initialConcentration="0" hasOnlySubstanceUnits="false"
 fbc:charge="-4" fbc:chemicalFormula="C10H12N5O13P3"/>

<species metaid="meta_M1" id="M1" compartment="C" boundaryCondition="false"
 initialConcentration="0" hasOnlySubstanceUnits="false" fbc:charge="0"
 fbc:chemicalFormula="RCONH2"/>

<species metaid="meta_M2" id="M2" compartment="c" boundaryCondition="false"
 initialConcentration="0" hasOnlySubstanceUnits="false" fbc:charge="0"
 fbc:chemicalFormula="C2H4O2(CH2)n"/>
```

While there are many ways of referring to an elemental composition, the purpose of the `chemicalFormula` attribute is to enable reaction balancing and validation, something of particular importance in constraint-based models.

The format of the `chemicalFormula` should, whenever possible, consist only of atomic names (as in the Periodic Table). Similarly, for enhanced inter-operability, the element order should be arranged according to the Hill system (see Table 2) (Hill, 1900, 2012). Using this notation the number of carbon atoms in a molecule is indicated first,

H_2O_4S	C_2H_5Br	BrH
$C_{10}H_{12}N_5O_{13}P_3$	CH_3I	CH_4

Table 2: *Examples of chemical formulas written using the Hill System. As described in Section 4.2*

followed by the number of hydrogen atoms and then the number of all other chemical elements in alphabetical order. When the formula contains no carbon; all elements, including hydrogen, are listed alphabetically. Where there is more than a single atom present, this is indicated with an integer that follows the element symbol.

However, in certain situations it does become necessary to use a generic symbol in a user defined compound. For example, such symbols can include R and X and have the general form of a single capital letter followed by zero or more lowercase letters. In addition, the undefined parenthesised group index $(\ldots)_n$ may also be used. Note that

$$RCONH_2 \quad RCOX \quad C_2H_4O_2(CH_2)_n$$

Table 3: *Examples of chemical formulas written using allowed non-Hill symbols, as described in Section 4.2.*

in this case only the subscript n is allowed, integer values $(\ldots)_2$ and expressions such as $(\ldots)_{n-1}$ are considered invalid.

However, the use of R, X and $(\ldots)_n$ is not advised, as any **Reaction** in which such a **Species** occurs cannot necessarily be balanced. Therefore, any `chemicalFormula` that contains any of the aforementioned, non-Hill compatible symbols will raise a 'best practices' warning on model validation.

4.3 The FBC FluxObjective class

The FBC **FluxObjective** class is derived from **SBML** ***SBase*** and inherits `metaid` and `sboTerm`, as well as the subcomponents for **Annotation** and **Notes**. The **FluxObjective** class is a relatively simple container for a model variable that

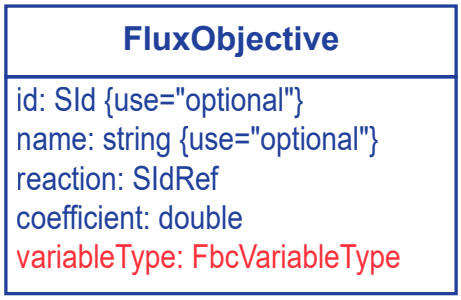

Figure 12: *A UML representation of the Flux Balance Constraints package* ***FluxObjective*** *class. For a complete description see Figure 1 as well as Section 1.4 for conventions related to this figure.*

can be expressed as a 'linear' or 'quadratic', weighted by a signed linear coefficient.

The `id` *and* `name` *attributes*

A **FluxObjective** has two optional attributes: `id` an attribute of type `SId` and `name` an attribute of type `string`.

The `reaction` *and* `coefficient` *attributes*

The required `reaction` is of type `SIdRef` and is restricted to refer only to a **Reaction** while the `coefficient` attribute holds a `double` referring to the coefficient that this **FluxObjective** takes in the enclosing **Objective**.

The `variableType` *attribute*

The required `variableType` attribute contains a `FbcVariableType` that represents the index to which a variable is raised in a **FluxObjective**. For example, where J_x represents a steady-state flux the `FbcVariableType` defines either a "`linear`", J_x^1 or "`quadratic`", J_x^2 term.

Flux objectives: example code

An objective with purely linear terms in LP format: `Maximize: 1 R1 + 2 R2`

```
<fbc:listOfObjectives fbc:activeObjective="obj1">
 <fbc:objective fbc:id="obj1" fbc:type="maximize">
  <fbc:listOfFluxObjectives>
   <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1" fbc:variableType="linear"/>
   <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2" fbc:variableType="linear"/>
  </fbc:listOfFluxObjectives>
 </fbc:objective>
</fbc:listOfObjectives>
```

Similarly, an objective with a quadratic term in LP format: `Minimize: 1 R1 + [4 R2^2]/2`

```
<fbc:listOfObjectives fbc:activeObjective="obj2">
 <fbc:objective fbc:id="obj2" fbc:type="minimize">
  <fbc:listOfFluxObjectives>
   <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1" fbc:variableType="linear"/>
   <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2" fbc:variableType="quadratic"/>
  </fbc:listOfFluxObjectives>
 </fbc:objective>
</fbc:listOfObjectives>
```

Units

As described above the linear **FluxObjective** defined here as $n \cdot J$ where the `coefficient` (n) is dimensionless and the `value` (J) takes the units of the `reaction` flux i.e., "extent per time". Therefore, the `linear` **FluxObjective**, $(n \cdot J)$ has the unit $\frac{extent}{time}$ where the units of reaction "extent" and "time" are defined globally. Analogously, in the case of a `quadratic` **FluxObjective**, $n \cdot J^2$ this would be $\frac{extent^2}{time^2}$.

4.4 The FBC UserConstraint class

The FBC **UserConstraint** class is derived from **SBML *SBase*** and inherits `metaid` and `sboTerm`, as well as the sub-components for **Annotation** and **Notes**. It's purpose is to define non-stoichiometric constraints, that is constraints that are not necessarily defined by the stoichiometrically coupled reaction network. In order to achieve we defined a new type of linear constraint, the **UserConstraint**.

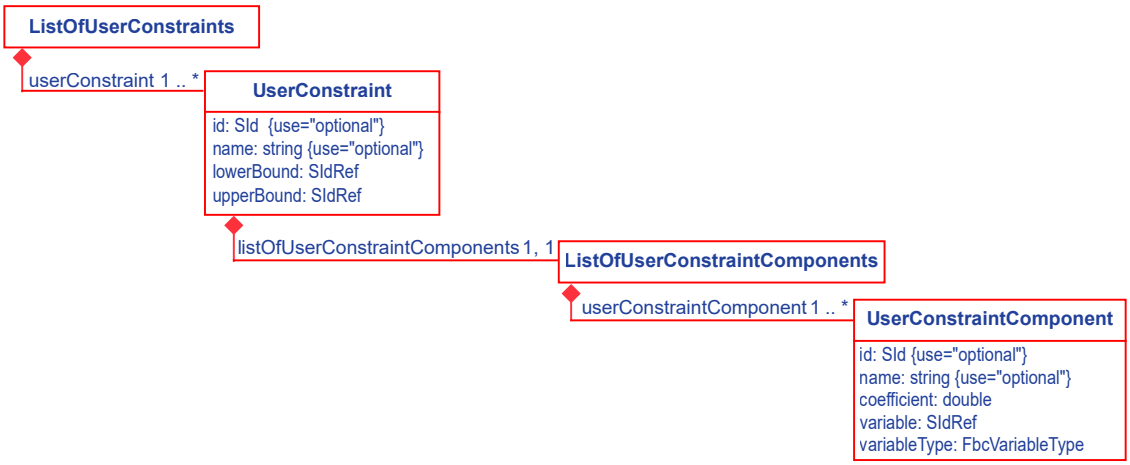

Figure 13: *A UML representation of the* ***SBML Model*** *class extended in the Flux Balance Constraints package by the* ***ListOfUserConstraints****. See Section 1.4 for conventions related to this figure.*

Analogous to the attributes described in Section 3.8 the `lowerBound` and `upperBound` form the boundaries of the

UserConstraint.

$$\textbf{UserConstraint} = \texttt{value} \tag{4}$$

$$\textbf{UserConstraint} \geq \texttt{lowerBound value} \tag{5}$$

$$\textbf{UserConstraint} \leq \texttt{upperBound value} \tag{6}$$

Defining either an equality if both `lowerBound` and `upperBound` refere to the same parameter (Equation 4) or set of inequalities (Equations 4 and 5).

The **UserConstraint** contains a **ListOfUserConstraintComponents** representing a linear combination of **UserConstraintComponent**s. Similar to a **FluxObjective** each **UserConstraintComponent** contains a coefficient–variable pair where the `coefficient` refers to a **Parameter**. In addition to a **Reaction** a **UserConstraintComponent** allows the `variable` to refer to non-constant **Parameter** thus allowing the definition of non-reaction, artificial, variables.

The `id` *and* `name` *attributes*

A **UserConstraint** has an optional `id` of type `SId` and an optional attribute `name` of type `string`.

The `lowerBound` *attribute*

The required `lowerBound` attribute contains an `SIdRef` that references a **Parameter** which contains the lower boundary value of the **UserConstraint**.

The `upperBound` *attribute*

The required `upperBound` attribute contains an `SIdRef` that references a **Parameter** which contains the upper boundary value of the **UserConstraint**.

The `listOfUserConstraintComponents` *element*

The element `listOfUserConstraintComponents` which contains a **ListOfUserConstraintComponents** is derived from and functions like a typical **SBML ListOf**__ class with the restriction that it must contain one or more elements of type **UserConstraintComponent** (see Section 4.5). This implies that if a **UserConstraint** is defined there should be at least one **UserConstraintComponent** contained in a **ListOfUserConstraintComponents**.

4.5 The FBC UserConstraintComponent class

The FBC **UserConstraintComponent** class is derived from **SBML *SBase*** and inherits `metaid` and `sboTerm`, as well as the subcomponents for **Annotation** and **Notes**. The **UserConstraintComponent** class is a relatively simple container for a variable and a variable type specifier which is weighted by a signed coefficient.

The `id` *and* `name` *attributes*

An **UserConstraintComponent** has an optional `id` of type `SId` and an optional attribute `name` of type `string`.

The `coefficient` *attribute*

The required `coefficient` attribute contains an `SIdRef` that is restricted to reference only a constant **Parameter** which holds the coefficient value. In **strict** mode a **Parameter** whose `SId` is referenced by a `coefficient`, as in the case of a **FluxObjective** `coefficient`, has to be constant and not take the value NaN or ±inf.

The `variable` *attribute*

The required `variable` attribute contains an `SIdRef` that is restricted to reference the `SId` of either a **Reaction** or a non-constant **Parameter**. Conversely, if such non-constant **Parameter**'s `SId` is referenced by a **UserConstraintComponent**'s `variable` attribute it may not be referenced by any `coefficient`, `lowerFluxBound` or `upperFluxBound` attribute.

The `variableType` *attribute*

The required `variableType` attribute contains a `FbcVariableType` that indicates whether a variable should be considered as 'linear' or 'quadratic'.

User constraints: example code

The following example illustrates the encoding of the following two **UserConstraint**s:

$$RGLX - RXLG = 5 \quad (7)$$

$$2 \cdot Avar - RGDP \geq 2 \quad (8)$$

```
<listOfParameters>
 <parameter id="uc1" value="5" constant="True"/>
 <parameter id="uc2lb" value="2" constant="True"/>
 <parameter id="uc2ub" value="INF" constant="True"/>
 <parameter id="ucco1a" value="1" constant="True"/>
 <parameter id="ucco1b" value="-1" constant="True"/>
 <parameter id="ucco2a" value="2" constant="True"/>
 <parameter id="ucco2b" value="-1" constant="True"/>
 <parameter id="Avar" value="NaN" constant="False"/>
</listOfParameters>

<fbc:listOfUserConstraints>
 <fbc:userContraint fbc:id="uc1" fbc:lowerBound="uc1" fbc:upperBound="uc1">
  <fbc:listOfUserConstraintComponents>
   <fbc:userConstraintComponent fbc:coefficient="ucco1a" fbc:variable="RGLX"
    variableType="linear"/>
   <fbc:userConstraintComponent fbc:coefficient="ucco1b" fbc:variable="RXLG"
    variableType="linear"/>
  </fbc:listOfUserConstraintComponents>
 </fbc:userContraint>
 <fbc:userContraint fbc:id="uc2" fbc:lowerBound="uc2lb" fbc:upperBound="uc2ub">
  <fbc:listOfUserConstraintComponents>
   <fbc:userConstraintComponent fbc:coefficient="ucco2a" fbc:variable="Avar"
    variableType="linear"/>
   <fbc:userConstraintComponent fbc:coefficient="ucco2b" fbc:variable="RGLX"
    variableType="linear"/>
  </fbc:listOfUserConstraintComponents>
 </fbc:userContraint>
</fbc:listOfUserConstraints>
```

4.6 The FBC ListOfKeyValuePairs class

The **ListOfKeyValuePairs**, see Figure 14 for details, forms the basis of a controlled annotation defined by the Flux Balance Constraints package. This element defines a 'structured note' or 'descriptive list' of keys and associated values.

```
 <annotation>
  <listOfKeyValuePairs xmlns="http://sbml.org/fbc/keyvaluepair">
   <keyValuePair key="keyX" uri="https://tinyurl.com/ybyr7b62" value="47"/>
   <keyValuePair key="ZZkey" uri="urn:tinyurl.com:example:kvp" value="level␣5"/>
   <keyValuePair key="x-factor" uri="https://tinyurl.com/ybyr7b62"
                              value="intangible␣metaphysical␣property"/>
  </listOfKeyValuePairs>
 </annotation>
```

As such it is analogous to the official **SBML** RDF annotation used to support MIRIAM annotations, as defined in the **SBML** specification documents. When an annotation that declares the `xmlns` `http://sbml.org/fbc/keyvaluepair` then it must have the format specified here. Tools may chose to support reading and interpreting the content as

described, but may optionally ignore the annotation and merely round trip it with any other third party annotations. As is the case with the RDF/MIRIAM annotations, support for **ListOfKeyValuePairs** will be included in the **SBML** support libraries. The **ListOfKeyValuePairs** functions like a typical **SBML ListOf__** class with the restriction

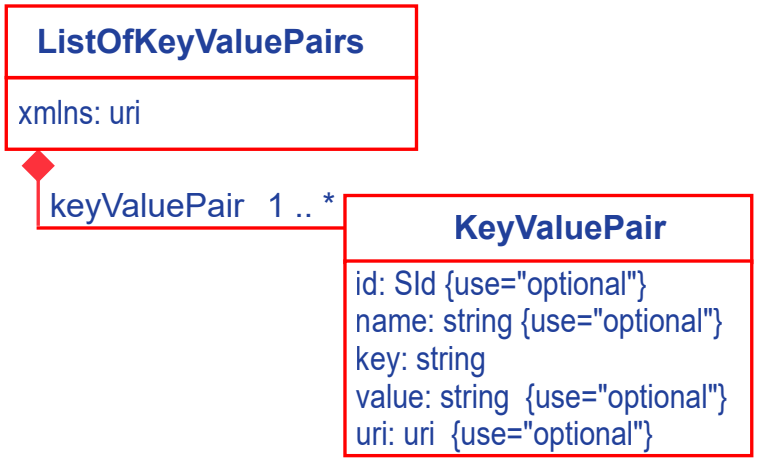

Figure 14: *A UML representation of the **SBML SBase** class extended in the Flux Balance Constraints package by the **ListOfKeyValuePairs**. See Section 1.4 for conventions related to this figure.*

that it must contain one or more elements of type **KeyValuePair** (see Section 4.7). In addition it defines a single mandatory attribute, `xmlns`, which identifies the annotation as belonging to the Flux Balance Constraints package.

The `xmlns` *attribute*

The `xmlns` is a mandatory component of the **ListOfKeyValuePairs**, is of the type `uri` and must have the value `http://sbml.org/fbc/keyvaluepair`.

4.7 The FBC KeyValuePair class

The FBC **KeyValuePair** class is derived from ***SBase*** and inherits the attribute `metaid`, `sboTerm` as well as the subcomponents needed for **Notes**. It's sole purpose is to define a key–value pair with an extended key definition.

The **KeyValuePair** defines a single mandatory attribute the `key` as well as two optional attributes: `value` and `uri`.

The `id` *and* `name` *attributes*

A **KeyValuePair** has two optional attributes: `id` an attribute of type `SId` and `name`, an attribute of type `string`.

The `key` *attribute*

The `key` is the mandatory component of the **KeyValuePair** pair and is of type `string`. It has the special property that every `key` in an enclosing **ListOfKeyValuePairs** must be unique.

The `value` *attribute*

The optional `value` attribute is of `string` and contains the value associated with a particular `key`. If not present, the **KeyValuePair** is defined as having no value.

The `uri` *attribute*

The optional attribute `uri` is of type `uri`. This attribute identifies a resource that defines the associated `key` component of the **KeyValuePair**, see Table 4 for examples. As a best practice, it is highly recommended that all tools implementing a **KeyValuePair** also implement support for the `uri` attribute.

Type	Example	Description
urn	urn:tinyurl.com:example:kvp	a tool specific namespace declaration
url	`https://tinyurl.com/ybyr7b62`	a url identifying a set of `key` definitions

Table 4: *Examples of how the* `uri` *attrbitue can be used to identify* `key` *definitions by* ***urn*** *or* ***url****.*