SBML Level 3 Package Specification

SBML Level 3 Package: Flux Balance Constraints ('fbc')

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This is a Release Candidate of the "fbc" package Version 2, Release 1 and not a normative document. Please send feedback to the Package Working Group mailing list at sbml-flux@lists.sourceforge.net. The official version 1 release 1 specification can be found here: http://identifiers.org/combine.specifications/sbml.level-3.version-1.fbc.version-1.release-1

The latest release, past releases, and other materials related to this specification are available at http://sbml.org/Documents/Specifications/SBML_Level_3/Packages/Flux_Balance_Constraints_(flux)

This release of the specification is available at



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1 Introduction and motivation

Constraint based modeling is a widely accepted methodology used to analyze and study biological networks on both a small and whole organism (genome) scale. Due to their large size these models are generally underdetermined and constraint based optimization methods (such as linear or mixed integer convex optimization) are used to analyze them. Optimization is assumed to occur within a defined set of constraints (e.g. stoichiometric, metabolic) and bounds (e.g. thermodynamic, experimental and environmental) on the values that the solution fluxes can obtain.

Perhaps the most well known (and widely used) analysis method is Flux Balance Analysis (FBA) which is performed on Genome Scale Metabolic Reconstructions (GSR's; Oberhardt et al. 2009). Using FBA a target flux is optimized (e.g. maximizing a flux to biomass or minimizing ATP production) while other fluxes can be bounded to simulate a selected growth environment or specific metabolic state.

As constraint based models are generally underdetermined and few or none of the kinetic rate equations, flux capacity constraints and related parameters are known it is crucial that a model definition includes the ability to define optimization parameters such as objective functions, flux bounds and constraints. Currently this is not possible in the Systems Biology Markup Language (SBML) Level 2 or Level 3 core specification (Hucka et al., 2011, 2003).

The question of how to encode constraint based (also referred to as steady state or FBA) models in SBML is not new. However, advances in the methods used to construct genome scale constraint based models and the wider adoption of constraint based modeling in biotechnological/medical applications have led to a rapid increase in both the number of models being constructed and the tools used to analyze them.

Faced with such growth, both in number and diversity, the need for a standardized data format for the definition, exchange and annotation of constraint based models has become critical. As the core model components (e.g. species, reactions, stoichiometry) can already be efficiently described in SBML (with its associated active community, software and tool support) the Flux Balance Constraints package aims to extend SBML Level 3 core by adding the elements necessary to encode current and future constraint based models.

1.1 Proposal corresponding to this package specification

This specification for Flux Balance Constraints in SBML Level 3 Version 1 is based on the proposal, by this documents authors, located at the following URL:

```
http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Balance_Constraints_Proposal_(2012)
```

The tracking number in the SBML issue tracking system (SBML Team, 2010) for Flux Balance Constraints package activities is 3154219. The version of the proposal used as the starting point for this specification is the version of March 2012. Previous versions of the current proposal are:

Version 3 (March 2012)

```
http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Balance_Constraints_Proposal_(2012)
```

Version 2 (March 2011)

 $http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Constraints_Pr$

Version 1 (February 2010)

http://precedings.nature.com/documents/4236/version/1

Details of related, earlier, independent proposals are provided in Section 2.

1.2 Tracking number

As initially listed in the SBML issue tracking system under:

http://sourceforge.net/tracker/?func=detail&aid=3154219&group_id=71971&atid=894711.

1.3 Package dependencies

The Flux Balance Constraints package adds additional classes to SBML Level 3 Version 1 Core and has no dependency on any other SBML Level 3 package.

1.4 Document conventions

Following the precedent set by the SBML Level 3 Core specification document, we use UML 1.0 (Unified Modeling Language; Eriksson and Penker 1998; Oestereich 1999) class diagram notation to define the constructs provided by this package. We also use color in the diagrams to carry additional information for the benefit of those viewing the document on media that can display color. The following are the colors we use and what they represent:

- *Black*: Items colored black in the UML diagrams are components taken unchanged from their definition in the SBML Level 3 Core specification document.
- *Green*: Items colored green are components that exist in SBML Level 3 Core, but are extended by this package. Class boxes are also drawn with dashed lines to further distinguish them.
- *Blue*: Items colored blue are new components introduced in this package specification. They have no equivalent in the SBML Level 3 Core specification.

We also use the following typographical conventions to distinguish the names of objects and data types from other entities; these conventions are identical to the conventions used in the SBML Level 3 Core specification document:

AbstractClass: Abstract classes are classes that are never instantiated directly, but rather serve as parents of other object classes. Their names begin with a capital letter and they are printed in a slanted, bold, sans-serif type-face. In electronic document formats, the class names defined within this document are also hyperlinked to their definitions; clicking on these items will, given appropriate software, switch the view to the section in this document containing the definition of that class. (However, for classes that are unchanged from their definitions in SBML Level 3 Core, the class names are not hyperlinked because they are not defined within this document.)

Class: Names of ordinary (concrete) classes begin with a capital letter and are printed in an upright, bold, sansserif typeface. In electronic document formats, the class names are also hyperlinked to their definitions in this specification document. (However, as in the previous case, class names are not hyperlinked if they are for classes that are unchanged from their definitions in the SBML Level 3 Core specification.)

SomeThing: Attributes of classes, data type names, literal XML, and generally all tokens *other* than SBML UML class names, are printed in an upright typewriter typeface. Primitive types defined by SBML begin with a capital letter; SBML also makes use of primitive types defined by XML Schema 1.0 (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000), but unfortunately, XML Schema does not follow any capitalization convention and primitive types drawn from the XML Schema language may or may not start with a capital letter.

For other matters involving the use of UML and XML, we follow the conventions used in the SBML Level 3 Core specification document.

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2 Background

V2

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V2

2.1 Problems with current SBML approaches

While there is currently no official way of encoding constraint based models in SBML L2 there have been pragmatic approaches used by a variety of groups and applications. Arguably the most comprehensive and widely used format is that used by the COBRA toolbox (Becker et al., 2007) where the metabolic reaction network is well defined using SBML's Reaction and Species classes. However, other FBA specific model components such as flux bounds and the reactions that take part in the objective function are less well defined. In this case LocalParameter elements are used which (implicitly) rely on e.g. all tools knowing and using the same naming convention for the parameter ID's. Furthermore, reaction annotations are generally stored as tool specific HTML key-value pairs in a Notes element which has routinely led to different research groups and software using in-house and/or tool specific ways to describe the same information. An example of such an annotation is the widely used 'gene protein association'. While a step in the right direction, this encoding is not suitable for direct translation into SBML Level 3.

It is, perhaps worth noting that while SBML Level 2 does have a construct known as **Constraint**, its function traditionally limited to measuring and reporting a model variables behavior in time. In contrast, the Flux Balance Constraints package considers a model at steady state and therefore time invariant. Instead it makes use of **Parameter** elements to define the allowable range that a steady-state flux may attain. Therefore 'flux bounds' and **Constraint** elements should be considered complementary to one another. Furthermore, certain attributes that were widely used by the constraint-based modeling community such as the **Species** attribute **charge** were removed in later versions of SBML. This has had the effect that a significant number of cosntraint-based modelling and metabolic flux analysis software still make use of SBML Level 2 Version 1.

2.2 Past work on this problem or similar topics

The problem of describing and annotating FBA models in SBML has been raised at various times in the past few years. In this regard there are two known putative proposals one by Karthik Raman and the other by the Church Laboratory. As far as we are aware these proposals never developed beyond their initial presentation at SBML forums/hackathons. In 2009 the discussion was reopened at the SBML Forum held in Stanford, an initiative which has subsequently developed into the current active package proposal and this document. In reverse chronological order these are:

Brett Olivier (2009) SBML Level 3 FBA package discussion

http://sbml.org/images/4/4a/Olivier_sbml_forum_2009_09_04.pdf

Karthik Raman (2005) Flux annotations in SBML

http://sbml.org/images/d/d9/Raman-flux-annotations.pdf

Church laboratory (pre 2005) Metabolic flux model annotations

http://sbml.org/Community/Wiki/Old_known_SBML_annotations_list

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3 Proposed syntax and semantics

In this section, we define the syntax and semantics of the Flux Balance Constraints package for SBML Level 3 Version 1. We expound on the various data types and constructs defined in this package, then in Section 4 on page 18, we provide complete examples of using the constructs in an example SBML model.

3.1 Namespace URI and other declarations necessary for using this package

Every SBML Level 3 package is identified uniquely by an XML namespace URI. For an SBML document to be able to use a given SBML Level 3 package, it must declare the use of that package by referencing its URI. The following is the namespace URI for this version of the Flux Balance Constraints package for SBML Level 3 Version 1:

```
"http://www.sbml.org/sbml/level3/version1/fbc/version2"
```

In addition, SBML documents using a given package must indicate whether understanding the package is required for complete mathematical interpretation of a model, or whether the package is optional. This is done using the attribute **required** on the **<sbml>** element in the SBML document. For the Flux Balance Constraints package, the value of this attribute must be set to "false".

The following fragment illustrates the beginning of a typical SBML model using SBML Level 3 Version 1 and this version of the Flux Balance Constraints package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core" level="3" version="1"
    xmlns:fbc="http://www.sbml.org/sbml/level3/version1/fbc/version2" fbc:required="false">
```

3.2 Primitive data types

Section 3.1 of the SBML Level 3 Version 1 Core specification defines a number of primitive data types and also uses a number of XML Schema 1.0 data types (Biron and Malhotra, 2000). More specifically we make use of integer, double, string, SId and SIdRef. In addition we make use of a new primitive: the enumeration FbcType, see Figure 1 for the interrelation between these entities.

The SId type is used as the data type for the identifiers of **GeneProduct** (Section 3.5), **GeneProductRef** (Section 3.11), **GeneProteinAssociation** (Section 3.9), **FluxObjective** (Section 3.7) and **Objective** (Section 3.6) classes. In the FBC package the **ListOfObjectives** has an attribute of type **SIdRef** that is used to refer to an 'active' **Objective**.

3.2.1 Type FbcType

The Flux Balance Constraints package defines a new enumerated type **FbcType** which represents the optimization sense of the objective function. It can have one of the following two values "maximize" or "minimize".

bgoli

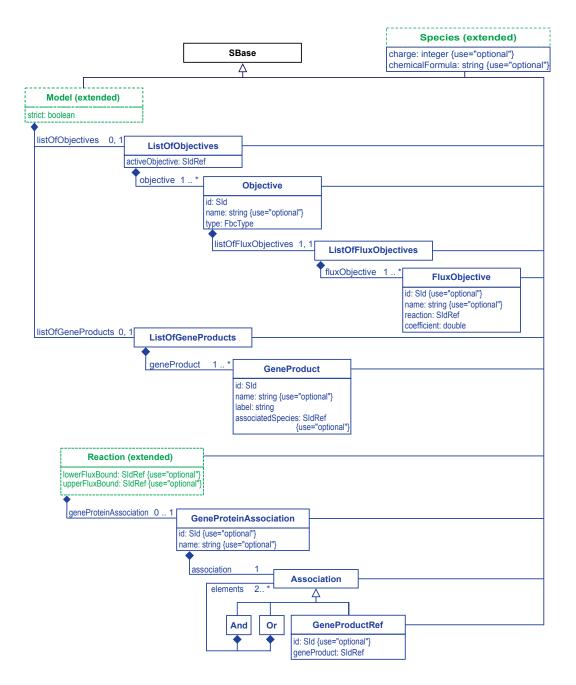


Figure 1: A UML representation of the Flux Balance Constraints package. Derived from **SBase**, the FBC classes inherit support for constructs such as SBML **Notes** and **Annotation**'s. See Section 1.4 for conventions related to this figure. The individual classes are further discussed in the text.

3.3 The extended Model class

The **SBML Model** class is extended by adding a mandatory boolean attribute **strict** as well as optional lists: **listOfObjectives** and **listOfGeneProducts**. A **Model** may contain at most one of each of these lists.

The attribute strict

The mandatory attribute strict of type boolean is used to apply an additional set of restrictions to the model. The strict attribute ensures that the Flux Balance Constraints package can be used to encode legacy FBA models

Model (extended) strict: boolean

Figure 2: A UML representation of the extended SBML Model class used in the Flux Balance Constraints package. See Section 1.4 for conventions related to this figure.

expressible as Linear Programs (LP's) with software that is unable to analyze arbitrary mathematical expressions. In addition it ensures that a 'strict' model is fully described and mathematically consistent, for example, by ensuring that all fluxes have a valid upper or lower bound.

This is accomplished by defining a set of restrictions which come into effect if strict is set to "true":

- Each Reaction in a Model must define attributes lowerFluxBound and upperFluxBound with each pointing to a valid Parameter object defined in the current Model.
- Each **Parameter** object referred to by the **Reaction** attributes lowerFluxBound and upperFluxBound must have their constant attribute set to "true" and its value attribute set to a double value which may not be "NaN".
- **SpeciesReference** elements of **Reaction**s must have their stoichiometry attribute set to a double value that is neither "NaN" nor "-INF" nor "INF". In addition their constant attribute must be set to "true".
- InitialAssignment elements may neither target the Parameter elements referenced by the Reaction attributes lowerFluxBound and upperFluxBound nor any SpeciesReference.
- All defined FluxObjective elements must have their coefficient attribute set to a double value that is neither "NaN" nor "-INF" nor "INF".
- A Reaction lowerFluxBound attribute may not have a value of "INF".
- A Reaction upperFluxBound attribute may not have a value of "-INF".
- For all reactions, the value of a lowerFluxBound must be less than or equal to the value of the upperFluxBound.

While it is not compulsory for a 'strict' FBC model to define an **Objective**, doing so does does allow it to be formulated as an LP and optimized, however, this decision is left to the modeler / creator.

Alternatively, if the value of the strict attribute is "false" then none of these restrictions apply. That means that, for example, the InitialAssignment construct may be used to determine the value of the Parameter elements used as flux bounds. It also means that, if so desired, flux bounds can be updated dynamically.

3.3.1 The FBC listOfObjectives

As shown in Figure 1 the **ListOfObjectives** is derived from **SBase** and inherits the attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. Unlike most other **SBML ListOf** classes, **ListOfObjectives** introduces an additional required attribute **activeObjective**. The **ListOfObjectives** must contain at least one **Objective** (defined in Section 3.6).

The activeObjective attribute

This attribute is of type **SIdRef** and can only refer to the **id** of an existing **Objective**. This required attribute exists so that when multiple **Objective**'s are included in a single model, the model will always be well described i.e., there is a single, primary objective function which defines a single optimum and its associated solution space.

3.3.2 The FBC listOfGeneProducts

As shown in Figure 1 the **ListOfGeneProducts** is derived from **SBase** and inherits the attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. The **ListOfGeneProducts** must contain at least one **Gene-Product** (defined in Section 3.5).

3.3.3 A note on units

The main unit definitions that should be considered when using the Flux Balance Constraints package are the global model definitions of "extent" and "time" as all FBC flux related classes (i.e., FluxObjective implicitly attain the same unit as the **Reaction** that they reference). More details on units can be found in their respective class definitions.

3.4 The extended Species class

The Flux Balance Constraints package extends the SBML Level 3 Version 1 Core **Species** class with the addition of two attributes **charge** and **chemicalFormula**.

Species (extended)

charge: integer {use="optional"}
chemicalFormula: string {use="optional"}

Figure 3: A UML representation of the extended SBML Species class used in the Flux Balance Constraints package. See Section 1.4 for conventions related to this figure.

The charge attribute

The optional attribute **charge** which contains a signed **integer** referring to the **Species** object's charge and is defined as it was in the **SBML** Level 2 Version 1 specification: "The optional field charge takes an integer indicating the charge on the species (in terms of electrons, not the SI unit coulombs)."

The chemicalFormula attribute

The optional attribute **chemicalFormula** containing a **string** that represents the **Species** objects elemental composition.

```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP" compartment="Cytosol"
boundaryCondition="false" initialConcentration="0" hasOnlySubstanceUnits="false"
fbc:charge="-4" fbc:chemicalFormula="C10H12N5013P3"/>
```

While there are many ways of referring to an elemental composition the purpose of the **chemicalFormula** attribute is to allow reaction balancing and validation which is particularly important in constraint based models.

The format of **chemicalFormula** must consist only of atomic names (as in the Periodic Table) or user defined compounds either of which take the form of a single capital letter followed by zero or more lowercase letters. Where there is more than a single atom present, this is indicated with an integer. With regards to order (and enhance inter-operability) it is recommended to use the Hill system order (Hill, 1900, 2012).

H2O4S C2H5Br BrH C10H12N5O13P3 CH3I

Table 1: Examples of chemical formulas written using the Hill System. As described in Section 3.4

Using this notation the number of carbon atoms in a molecule is indicated first, followed by the number of hydrogen atoms and then the number of all other chemical elements in alphabetical order. When the formula contains no carbon; all elements, including hydrogen, are listed alphabetically.

3.5 The FBC GeneProduct class

GeneProduct is a new FBC class derived from **SBML** *SBase* that inherits metaid and sboTerm, as well as the subcomponents for **Annotation** and **Notes**. The purpose of this class is to define a single gene product. It implements two required attributes id and label as well as two optional attributes name and associatedSpecies.

GeneProduct

id: SId
name: string {use="optional"}
label: string
associatedSpecies: SIdRef
{use="optional"}

Figure 4: A UML representation of the Flux Balance Constraints package GeneProduct class. See Section 1.4 for conventions related to this figure.

The id and name attributes

A **GeneProduct** has a required attribute id of type SId and an optional attribute name of type string. The unique id attribute is required to enable a **GeneProduct** to be referenced from a **GeneProductRef** used in a **GeneProteinAssociation**.

The label attribute

The primary purpose of a **GeneProduct** is to uniquely reference a gene or implied gene product (e.g. a peptide). As there is, currently, no restriction on the format of these these references they cannot be assumed to conform to an **SBML** SId syntax. Therefore the Flux Balance Constraints package defines the required attribute **label**, of type **string**, for this purpose.

While ideally some form of restriction should be placed on the value of label, at this point it is only possible to suggest that this attribute's value should conform to the definition of an SId. For example, take an existing GPR annotation:

```
GENE_ASSOCIATION: (Rv0649)
```

this can now be formally (and unambiguously) encoded as:

```
<fbc:geneProduct metaid="meta_gene_1" fbc:id="gene1" fbc:label="Rv0649"
fbc:associatedSpecies="s_Rv0649">
<annotation>
  <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
    xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
    xmlns:vCard="http://www.w3.org/2001/vcard-rdf/3.0#"
    xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
    xmlns:bqmodel="http://biomodels.net/model-qualifiers/">
    <rdf:Description rdf:about="#meta_gene_1">
    <bqbiol:is>
    <rdf:Bag>
    <rdf:li rdf:resource="http://identifiers.org/kegg.genes/mtu:Rv0649"/>
    </rdf:Bag>
    </bqbiol:is>
  </bde>
```

Furthermore, it is a highly recommended 'best practice' suggestion that a **GeneProduct** be annotated using the inherited MIRIAM compliant **SBML Annotation** mechanism. Doing so will help reduce the dependence and ambiguity of using an overloaded, semantically meaningful **label** attribute and enhance interoperability. For an example of this approach see Section 5.1.

The associatedSpecies attribute

A **GeneProduct** may, optionally, refer to a **Species** so as to provide compatibility with the Manchester style encoding of gene-protein associations. In this case the attribute **associatedSpecies** is of type **SIdRef** and, if defined, should point to an existing **Species** in the model.

3.6 The FBC Objective class

The FBC **Objective** class is derived from **SBML SBase** and inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. An integral component in a complete description of a steady-state model is the so-called 'objective function' which generally consist of a linear combination of model variables (fluxes) and a sense (direction). In the FBC package this concept is succinctly captured in the **Objective** class.

The id and name attributes

An **Objective** has a required attribute id of type SId and an optional attribute name of type string.

The type attribute

The required **type** attribute contains an **FbcType** type which represents the sense of the optimality constraint and can take one of two values:

```
maximize \mapsto "maximize"
minimize \mapsto "minimize"
```

The listOfFluxObjectives element

The element listOfFluxObjectives which contains a ListOfFluxObjectives is derived from and functions like a typical SBML ListOf_ class with the restriction that it must contain one or more elements of type FluxObjective (see Section 3.7). This implies that if an Objective is defined there should be at least one FluxObjective contained in a ListOfFluxObjectives.

Objective

id: SId

name: string {use="optional"} type: FbcType

Figure 5: A UML representation of the Flux Balance Constraints package Objective class. See Section 1.4 for conventions related to this figure.

Encoding the Objective

The Flux Balance Constraints package allows for the definition of multiple model objectives with one being designated as active (see Section 3.6) as illustrated in this example:

Note how both **Objective** instances differ in **type** and each contains different set of **FluxObjectives** (see Section 3.7). For an example of how the **Objective** relates to the description of the underlying mathematical model please see Section 4.1.3.

3.7 The FBC FluxObjective class

The FBC **FluxObjective** class is derived from **SBML SBase** and inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**.

The FluxObjective class is a relatively simple container for a model variable weighted by a signed linear coefficient.

FluxObjective

id: SId {use="optional"}
name: string {use="optional"}
reaction: SIdRef
coefficient: double

Figure 6: A UML representation of the Flux Balance Constraints package FluxObjective class. See Section 1.4 for conventions related to this figure.

The id and name attributes

A FluxObjective has two optional attributes: id an attribute of type SId and name an attribute of type string.

The reaction and coefficient attributes

The required **reaction** is of type **SIdRef** and is restricted to refer only to a **Reaction** while the **coefficient** attribute holds a **double** referring to the coefficient that this **FluxObjective** takes in the enclosing **Objective**. For example the objective **Maximize:** 1 R1 + 2 R2 would be encoded as

```
<fbc:listOfObjectives fbc:activeObjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
    <fbc:listOfFluxObjectives>
    <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1"/>
    <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2"/>
    </fbc:listOfFluxObjectives>
  </fbc:listOfObjective></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fi>
```

Units 15

As described above the **FluxObjective** defined here as $n \cdot J$ where the **coefficient** (n) is dimensionless and the **value** (J) takes the units of the **reaction** flux i.e., "extent per time". Therefore, the **FluxObjective** ($n \cdot J$) has the unit "extent per time" where the units of reaction "extent" and "time" are defined globally.

3.8 The extended Reaction class

The Flux Balance Constraints package extends the SBML Level 3 Version 1 Core **Reaction** class with the addition of a new optional element **GeneProteinAssociation** as well as two optional attributes **lowerFluxBound** and **upperFluxBound**.

Reaction (extended) lowerFluxBound: SldRef {use="optional"} upperFluxBound: SldRef {use="optional"}

Figure 7: A UML representation of the extended SBML Reaction class used in the Flux Balance Constraints package. See Section 1.4 for conventions related to this figure.

The attributes lowerFluxBound and upperFluxBound

The optional attributes lowerFluxBound and upperFluxBound of type SIdRef are used to specify the lower and upper flux bounds for the **Reaction**. (In the case that equal bounds are to be used on the reaction, both attributes should point to the same SBML element).

The attributes have to refer to an existing **Parameter** in the model. This makes it possible for other SBML elements to interact with these parameters depending on the value of the **fbc:strict** attribute of the **Model** (see also Section 3.3 on page 7).

For example, if the value of the strict attribute is "false", the value of a flux bound could be calculated based on InitialAssignment objects in the case of a constant Parameter (i.e. SBML parameters that have its constant attribute set to "true"). Should the parameter not be constant, then its value can be additionally updated by all SBML Level 3 Version 1 Core constructs (i.e.: EventAssignment, AssignmentRule, and AlgebraicRule).

Encoding the flux bounds

To generate a list of (in)equalities for each reaction, out of the references in upperFluxBound and lowerFluxBounds, one first resolves the reference to the underlying **Parameter**. If they point to the same element, the equality will be of the form:

otherwise two inequalities are to be derived:

<reaction> = <value>

```
<reaction>>=<lowerFluxBound value><reaction><=<upre>cupperFluxBound value>
```

In SBML Level 3 Version 1 with FBC Version 2 this is encoded as:

additionally the InitialAssignment construct can be used to change the value of the Parameter elements. If in the example above constant="false" then the elements can be set additionally by EventAssignment, AssignmentRule, and AlgebraicRule.

3.9 The FBC GeneProteinAssociation class

The Flux Balance Constraints package defines a **GeneProteinAssociation** class that derives from **SBase** and inherits the attributes metaid and sboTerm as well as the subcomponents for **Annotation** and **Notes**. As shown in Figure 1 the **GeneProteinAssociation** class extends **Reaction** with one or more genes (or gene products). Where more than one gene is present in an association they are then expressed as a logical expression where genes are related to one another using logical 'and' and 'or' operators.

The id attribute

The GeneProteinAssociation class defines an optional attribute: id of type SId

The name attribute

The GeneProteinAssociation class defines an optional attribute: name of type string

The association element

Each **GeneProteinAssociation** contains a single **Association**, however, as described in Section 3.10 an **Association** is an abstract class that implies that an **association** will always contain an instance of one of its sub-classes: **And**, **Or** or **GeneProductRef**.

GeneProteinAssociation

id: Sld {use="optional"}

name: string {use="optional"}

Figure 8: A UML representation of the Flux Balance Constraints package GeneProteinAssociation class. See Section 1.4 for conventions related to this figure.

Encoding the GeneProteinAssociation

As described in Section 3.9 the **GeneProteinAssociation** is simply a container that contains one of three types of **Association** either holding a single **GeneProductRef** or two or more **Association** elements in an **And** or **Or** relationship. For example, the following typical gene–protein association expression from the BiGG database *E. coli* reconstruction (iJR904; Reed et al. 2003; Schellenberger et al. 2010)

```
((B3670 and B3671) or (B0077 and B0078) or (B3768 and B3769 and B3767))
```

is now encoded in the Flux Balance Constraints package as:

```
<fbc:listOfGeneProducts>
 <fbc:geneProduct fbc:id="g_b3670" label="b3670" />
  <fbc:geneProduct fbc:id="g_b3671" label="b3671" />
  <fbc:geneProduct fbc:id="g_b0077" label="b0077" />
 <fbc:geneProduct fbc:id="g_b0078" label="b0078" /> <fbc:geneProduct fbc:id="g_b3768" label="b3768" />
 <fbc:geneProduct fbc:id="g_b3769" label="b3769" />
  <fbc:geneProduct fbc:id="g_b3767" label="b3767" />
</fbc:listOfGeneProducts>
<reaction id = "R_ACHBS" ... >
<fbc:geneProteinAssociation fbc:id="ga_29">
 <fbc:or>
  <fbc:and>
   <fbc:geneProductRef fbc:geneProduct="g_b3670"/>
   <fbc:geneProductRef fbc:geneProduct="g_b3671"/>
  </fbc:and>
  <fbc:and>
   <fbc:geneProductRef fbc:geneProduct="g_b0077"/>
   <fbc:geneProductRef fbc:geneProduct="g_b0078"/>
  </fbc:and>
  <fbc:and>
   <fbc:geneProductRef fbc:geneProduct="g_b3768"/>
   <fbc:geneProductRef fbc:geneProduct="g_b3769"/>
   <fbc:geneProductRef fbc:geneProduct="g_b3767"/>
  </fbc:and>
 </fbc:or>
</fbc:geneProteinAssociation>
</reaction>
```

3.10 The FBC Association class

V2

V2

The Flux Balance Constraints package defines an abstract *Association* class that is derived from *SBase* and inherits the attributes metaid and sboTerm, as well as the subcomponents for **Annotation** and **Notes**. It represents either a single gene, or a collection of genes in a logical expression and is only ever instantiated as one of its subclasses: **GeneProductRef** (Section 3.11), **And** (Section 3.12) and **Or** (Section 3.13).

3.11 The FBC GeneProductRef class

The Flux Balance Constraints package defines a **GeneProductRef** class that references a gene (or gene product) declared in **ListOfGeneProducts**, a child of **Model**. It is derived from an **Association** and thereby inherits the **SBase** attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes** as described in Figure 9.

The id attribute

The **GeneProductRef** class defines an optional attribute **id** of type **SId**.

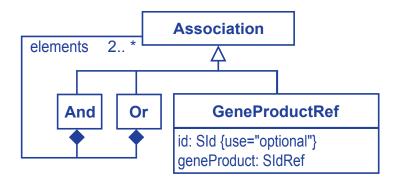


Figure 9: A UML representation of the Flux Balance Constraints package Association and derived classes. See Section 1.4 for conventions related to this figure.

The geneProduct attribute

The required **geneProduct** attribute of type **FbcSIdRef** references a **GeneProduct** element declared in the **ListOf-GeneProducts**.

3.12 The FBC And class

The Flux Balance Constraints package defines an **And** class that is derived from an **Association** and thereby inherits the **SBase** attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes** as described in Figure 9. This class represents a set of two or more associations that are related in an order independent 'and' relationship.

The elements element

Each **And** must contain two or more instances (not necessarily of the same type) of any **Association** subclass (**And**, **Or**, **GeneProductRef**).

```
<reaction id = "R_ACACCT" ... >
  <fbc:geneProteinAssociation fbc:id="ga_18">
        <fbc:and>
        <fbc:geneProductRef fbc:geneProduct="g_b3670"/>
        <fbc:geneProductRef fbc:geneProduct="g_b3671"/>
        </fbc:and>
        </fbc:geneProteinAssociation>
        </reaction>
```

3.13 The FBC Or class

The Flux Balance Constraints package defines an **Or** class that represents a gene (or gene product) and is derived from an **Association** and thereby inherits the **SBase** attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes** as described in Figure 9. This class represents a set of two or more **Association** elements related in an order independent 'or' relationship.

The elements element

Each **Or** must contain two or more instances (not necessarily of the same type) of any **Association** subclass (**And**, **Or**, **GeneProductRef**).

```
<reaction id = "R_ABTA" ... >
  <fbc:geneProteinAssociation fbc:id="ga_16">
    <fbc:or>
    <fbc:geneProductRef fbc:geneProduct="g_b2662"/>
    <fbc:geneProductRef fbc:geneProduct="g_b1302"/>
    </fbc:or>
    </fbc:or>
    </fbc:geneProteinAssociation>
</reaction>
```

V2

V2

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4 Illustrative examples of the FBC syntax

This section contains a worked example showing the encoding of a model suitable for Flux Balance Analysis using the Flux Balance Constraints package.

4.1 Example one: the basic FBC syntax

4.1.1 Kinetic model description



Figure 10: FBC syntax example: a simple four reaction pathway. The reactions are R1, R2, X1, X2 with fixed species IN, OUT, ATP, NADH and variable species A, B.

As shown in Figure 10 this example is a simple four reaction pathway that transforms metabolite *IN* to *OUT*. The model was created and analyzed using the SBW Flux Balance FBC implementation (Bergmann, 2012; Bergmann and Sauro, 2006). In **SBML** each reaction is represented as a chemical process transforming reactants to products, e.g. reaction *R1* is encoded in XML as (see also the complete example provided at the end of this section):

```
<reaction id="R1" reversible="false" fast="false">
  <list0fReactants>
    <speciesReference species="IN" stoichiometry="1" constant="true"/>
    </list0fReactants>
    list0fProducts>
        <speciesReference species="A" stoichiometry="1" constant="true"/>
        </list0fProducts>
    </reaction>
```

Using the reagent identity and stoichiometry it is possible to compactly describe this network in terms of its reaction stoichiometry as shown in Table 2 where each reaction is represented as a column.

Table 2: Example one: stoichiometric matrix, N

While the stoichiometry contains the structural properties of the reaction network the full description of a biological model can be described as a set of ordinary differential equations (ODE's). Of course other formalisms do exist,

but here we will concentrate exclusively on kinetic models where the change in concentration of each variable component in the system $(\frac{ds}{dt})$ is a non-linear function of the rates of the reactions which either create or consume it (the product of the stoichiometric matrix, **N** and the vector of reaction rates, **v**).

$$\frac{ds}{dt} = \mathbf{N}\mathbf{v} \tag{1}$$

The formulation of the kinetic model, as shown in Equation 1 is typical of the kind that can already be described using SBML Level 3 Version 1 Core where the vector **v** would contain rate equations as a function of parameters and variable species. In a steady-state, constraint based model these rates are considered unknowns and the system of equations can be rewritten as a set of linear constraints (see Equation 2):

$$NI = 0 (2)$$

Note that the rate vector \mathbf{v} is now represented as the steady-state flux vector \mathbf{J} . However, in order to perform a typical steady-state analysis such as flux balance analysis (FBA) we need to include more information into the model description. SBML Level 3 Version 1 Core does not have an unambiguous way of encoding either a capacity constraint or an objective target and for this we need to use the additional constructs provided by the Flux Balance Constraints package. In the following sections the same model data is shown encoded as XML and as a Linear Program (LP) in the common format used by IBM CPLEX.

4.1.2 Capacity constraints

A capacity constraint: in this example the maximum limit (upper bound) of the flux through reaction *R1* is set to be one (with an arbitrary unit of flux). In LP format this can be written as:

```
Bounds
R1 <= 1.0
```

the same information encoded as XML:

4.1.3 Objective function

This described a target which can be maximized or minimized: in this example the flux through reaction *R2* will be *maximized*.

```
Maximize objective1_objf: + 1.0 R2
```

the same information encoded as XML:

```
<fbc:list0f0bjectives fbc:active0bjective="objective1">
  <fbc:objective fbc:id="objective1" fbc:type="maximize">
        <fbc:list0fFlux0bjectives>
        <fbc:flux0bjective fbc:reaction="R2" fbc:coefficient="1"/>
        </fbc:list0fFlux0bjectives>
        </fbc:objective>
        </fbc:list0fObjectives></fbc:list0fObjectives></fbc:list0fObjectives></fbc:list0fObjectives></fbc:list0fObjectives>
```

4.1.4 Complete worked example

To conclude we show how the complete model described in Figure 10 encoded as both an LP and as XML. Formulated as an LP the problem can be written as:

```
Maximize
objective1_objf: + 1.0 R2

Subject To
    A: + R1 - X1 - X2 = 0.0
    B: - R2 + X1 + X2 = 0.0

Bounds
R1 <= 1.0
0.0 <= R2 <= +inf
0.0 <= X1 <= +inf
0.0 <= X2 <= +inf
END</pre>
```

Solving this we find that maximization of flux through R2 gives an optimal solution R2 = 1, shown in Equation 3, with one possible solution for **J**.

$$\begin{pmatrix}
1 & 0 & -1 & -1 \\
0 & -1 & 1 & 1
\end{pmatrix}
\begin{pmatrix}
1.0 \\
1.0 \\
0.0 \\
1.0
\end{pmatrix} = \mathbf{0}$$
(3)

Finally we provide the complete model, described above, encoded using the Flux Balance Constraints package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core"</pre>
 xmlns:fbc="http://www.sbml.org/sbml/level3/version1/fbc/version2"
 level="3" version="1" fbc:required="false">
<model id="fbcSpecExample1" timeUnits="time">
 <listOfUnitDefinitions>
  <unitDefinition id="volume">
    tofUnits>
    <unit kind="litre" exponent="1" scale="0" multiplier="1"/>
   </listOfUnits>
   </unitDefinition>
   <unitDefinition id="substance">
   tofUnits>
    <unit kind="mole" exponent="1" scale="0" multiplier="1"/>
   </listOfUnits>
  </unitDefinition>
   <unitDefinition id="time">
   tofUnits>
    <unit kind="second" exponent="1" scale="0" multiplier="1"/>
    </listOfUnits>
   </unitDefinition>
  </listOfUnitDefinitions>
```

```
<listOfCompartments>
 <compartment id="compartment" spatialDimensions="3" size="1" units="volume" constant="true"/>
</listOfCompartments>
Species>
 <species id="IN" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
 hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
 <species id="OUT" compartment="compartment" initialConcentration="0" substanceUnits="substance"
hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
 <species id="A" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
 hasOnlySubstanceUnits="false" boundaryCondition="false" constant="false"/>
 <species id="B" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
 hasOnlySubstanceUnits="false" boundaryCondition="false" constant="false"/>
 <species id="ATP" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
 hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
 <species id="NADH" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
  hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
</listOfSpecies>
<listOfParameters>
 <parameter id="R11" constant="true" value="0"/>
<parameter id="R1u" constant="true" value="1"/>
<parameter id="R21" constant="true" value="0"/>
 <parameter id="R2u" constant="true" value="INF"/>
 <parameter id="X11" constant="true" value="0"/>
 <parameter id="X1u" constant="true" value="INF"/>
 <parameter id="X21" constant="true" value="0"/>
<parameter id="X2u" constant="true" value="INF"/>
</listOfParameters>
<listOfReactions>
 <reaction id="R1" reversible="false" fast="false"</pre>
  fbc:lowerFluxBound="R11" fbc:upperFluxBound="R1u" >
  <speciesReference species="IN" stoichiometry="1" constant="true"/>
  </list0fReactants>
  tofProducts>
   <speciesReference species="A" stoichiometry="1" constant="true"/>
  </listOfProducts>
 </reaction>
 <reaction id="R2" reversible="false" fast="false"</pre>
  fbc:lowerFluxBound="R21" fbc:upperFluxBound="R2u" >
  <listOfReactants>
   <speciesReference species="B" stoichiometry="1" constant="true"/>
  </listOfReactants>
  t0fProducts>
   <speciesReference species="OUT" stoichiometry="1" constant="true"/>
  </listOfProducts>
 </reaction>
 <reaction id="X1" reversible="false" fast="false"</pre>
  fbc:lowerFluxBound="X11" fbc:upperFluxBound="X1u" >
  <listOfReactants>
   <speciesReference species="A" stoichiometry="1" constant="true"/>
  </list0fReactants>
  listOfProducts>
   <speciesReference species="ATP" stoichiometry="1" constant="true"/>
   <speciesReference species="B" stoichiometry="1" constant="true"/>
  </listOfProducts>
 </reaction>
 <reaction id="X2" reversible="false" fast="false"</pre>
  fbc:lowerFluxBound="X21" fbc:upperFluxBound="X2u" >
  <listOfReactants>
   <speciesReference species="A" stoichiometry="1" constant="true"/>
  </listOfReactants>
  <listOfProducts>
   <speciesReference species="B" stoichiometry="1" constant="true"/>
   <speciesReference species="NADH" stoichiometry="1" constant="true"/>
  </listOfProducts>
 </reaction>
```

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```
</listOfReactions>
<fbc:listOfObjectives fbc:activeObjective="objective1">
    <fbc:listOfObjective fbc:id="objective1" fbc:type="maximize">
        <fbc:listOfFluxObjectives>
        <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="1"/>
        </fbc:listOfFluxObjectives>
        </fbc:objective>
        </fbc:listOfObjectives>
        </model>
        </sbml>
```

5 Best practices

In this section, we illustrate a number of practices for using and interpreting various constructs in the Flux Balance Constraints package. These recommendations are non-normative, ignoring them will not render a model invalid, but may reduce inter-operability.

5.1 Examples contrasting the current SBML L2 encoding with L3 and FBC

These examples contrast some elements of an existing model, iJR904 from the BiGG Database encoded in the COBRA SBML Level 2 Version 1 format (Becker et al., 2007; Reed et al., 2003; Schellenberger et al., 2010) that have been translated into SBML Level 3 Version 1 FBC Version 2.

Objective function definition

SBML Level 2 objective function

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The SBML Level 3 objective function

```
<fbc:list0f0bjectives fbc:active0bjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
  <fbc:list0fFlux0bjectives>
  <fbc:flux0bjective fbc:reaction="R_BiomassEcoli" fbc:coefficient="1"/>
  </fbc:list0fFlux0bjectives>
  </fbc:objective>
  </fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjectives></fbc:list0bjec
```

Species definition

SBML Level 2 Species annotation version 1

Examine the **SBML** Level 2 Version 1 **Species** definition. Note how the **name** attribute is overloaded with the chemical formula in a tool specific way.

```
<species id="M_atp_c" name="ATP_C10H12N5013P3"
compartment="Cytosol" charge="-4" />
```

SBML Level 2 Species annotation version 2

A variation of the previous syntax that appeared in later models.

```
<species id="M_atp_c" name="ATP" compartment="c">
<notes>
  <body xmlns="http://www.w3.org/1999/xhtml">
```

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```
FORMULA: C10H12N5013P3
CHARGE: -4
</body>
</notes>
</species>
```

The SBML Level 3 FBC Species attributes

With the adoption of **SBML** FBC these **Species** properties can now be unified into a common format.

```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP" compartment="Cytosol"
boundaryCondition="false" initialConcentration="0" hasOnlySubstanceUnits="false"
fbc:charge="-4" fbc:chemicalFormula="C10H12N5013P3"/>
```

Reaction definition and flux bounds

SBML Level 2 Reaction

```
<reaction id="R_GTHS" name="glutathione_synthetase" reversible="false">
 <notes>
 <html:p>Abbreviation: R_GTHS</html:p>
 <html:p>EC Number: 6.3.2.3</html:p>
 <html:p>SUBSYSTEM: Cofactor and Prosthetic Group Biosynthesis</html:p>
 <html:p>Equation: [c] : atp + glucys + gly --&gt; adp + gthrd + h + pi</html:p>
 <html:p>Confidence Level: 0</html:p>
 <html:p>LOCUS:b2947#ABBREVIATION:gshB#ECNUMBERS:6.3.2.3#</html:p>
 <html:p>NAME:glutathione synthase#ABBREVIATION:GshB#</html:p>
 <html:p>GENE ASSOCIATION: (b2947)</html:p>
 </notes>
 <speciesReference species="M_atp_c" stoichiometry="1"/>
 <speciesReference species="M_glucys_c" stoichiometry="1"/>
 <speciesReference species="M_gly_c" stoichiometry="1"/>
 </listOfReactants>
 <speciesReference species="M_adp_c" stoichiometry="1"/>
 <speciesReference species="M_gthrd_c" stoichiometry="1"/>
 <speciesReference species="M_h_c" stoichiometry="1"/>
 <speciesReference species="M_pi_c" stoichiometry="1"/>
 </listOfProducts>
 <kineticLaw>
 <math xmlns="http://www.w3.org/1998/Math/MathML">
  <ci>FLUX_VALUE</ci>
 <listOfParameters>
  <parameter id="LOWER_BOUND" value="0" units="mmol_per_gDW_per_hr"/>
  <parameter id="UPPER_BOUND" value="999999" units="mmol_per_gDW_per_hr"/>
  <parameter id="OBJECTIVE_COEFFICIENT" value="0" />
  <parameter id="FLUX_VALUE" value="0" units="mmol_per_gDW_per_hr"/>
 </listOfParameters>
 </kineticLaw>
</reaction>
```

The SBML Level 3 FBC Reaction

As an example of a good annotation practice the EC number stored in the **Notes** element has been converted into MIRIAM compliant RDF. The Flux Balance Constraints package also facilitates the structured definition and use of gene protein associations and flux capacity constraints.

```
<reaction metaid="meta_R_GTHS" id="R_GTHS" name="glutathione_synthetase" reversible="false"
fbc:lowerFluxBound="R_GTHS_1" fbc:upperFluxBound="R_GTHS_u">
```

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```
<annotation>
  <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
    xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
    xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
   <rdf:Description rdf:about="#meta_R_GTHS">
    <bqbiol:is>
     <rdf:Bag>
      <rdf:li rdf:resource="http://identifiers.org/ec-code/6.3.2.3"/>
     </rdf:Bag>
    </bqbiol:is>
   </rdf:Description>
 </rdf:RDF>
 </annotation>
 <fbc:geneProteinAssociation fbc:id="gpr_GTHS">
 <fbc:geneProductRef fbc:geneProduct="g_b2947"/>
 </fbc:geneProteinAssociation>
 listOfReactants>
  <speciesReference constant="true" species="M_atp_c" stoichiometry="1"/>
 <speciesReference constant="true" species="M_glucys_c" stoichiometry="1"/>
<speciesReference constant="true" species="M_gly_c" stoichiometry="1"/>
  </listOfReactants>
 <speciesReference constant="true" species="M_adp_c" stoichiometry="1"/>
 <speciesReference constant="true" species="M_gthrd_c" stoichiometry="1"/>
<speciesReference constant="true" species="M_h_c" stoichiometry="1"/>
  <speciesReference constant="true" species="M_pi_c" stoichiometry="1"/>
 </listOfProducts>
</reaction>
<fbc:listOfGeneProducts>
  <fbc:geneProduct metaid="meta_g_b2947" fbc:id="g_b2947" fbc:label="b2947">
    <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"</pre>
     xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
     xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
     <rdf:Description rdf:about="#meta_g_b2947">
      <bgbiol:isEncodedBy>
       <rdf:Bag>
        <rdf:li rdf:resource="http://identifiers.org/ncbigene/947445"/>
       </rdf:Bag>
      </bgbiol:isEncodedBy>
     </rdf:Description>
    </rdf:RDF>
   </annotation>
  </fbc:geneProduct>
</fbc:listOfGeneProducts>
<listOfParameters>
 <parameter id="R_GTHS_1" constant="true" value="0"/>
 <parameter metaid="meta_R_GTHS_u" id="R_GTHS_u" constant="true" value="inf">
   <annotation>
    <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
     xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
     xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
     <rdf:Description rdf:about="#meta_R_GTHS_u">
      <bgbiol:isDescribedBy><rdf:Bag>
       <rdf:li rdf:resource="http://identifiers.org/pmc/PMC193654"/>
      </rdf:Bag></bqbiol:isDescribedBy>
     </rdf:Description>
    </rdf:RDF>
   </annotation>
 </parameter>
</list0fParameters>
```

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5.2 An example of a strict FBC model (XML)

This section highlights the best practices for a complete FBC Version 2 model. To improve readability detailed annotations, as described in Section 5.1 and unit definitions have been omitted.

```
<?xml version="1.0" encoding="UTF-8"?> <sbml</pre>
xmlns="http://www.sbml.org/sbml/level3/version1/core"
 xmlns:fbc="http://www.sbml.org/sbml/level3/version1/fbc/version2"
  level="3" version="1" fbc:required="false">
 <model id="fbcSpecExample1" timeUnits="time" fbc:strict="true">
  <listOfCompartments>
   <compartment id="compartment" spatialDimensions="3" size="1" units="volume" constant="true"/>
  </listOfCompartments>
  st0fSpecies>
   <species id="IN" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
   hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
   <species id="OUT" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
   hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
   <species id="A" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
   hasOnlySubstanceUnits="false" boundaryCondition="false" constant="false"/>
   <species id="B" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
   hasOnlySubstanceUnits="false" boundaryCondition="false" constant="false"/>
   <species id="ATP" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
   hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
   <species id="NADH" compartment="compartment" initialConcentration="0" substanceUnits="substance"</pre>
    hasOnlySubstanceUnits="false" boundaryCondition="true" constant="false"/>
  </listOfSpecies>
  <listOfParameters>
   <parameter id="lb" name="arbitrary_lower_bound" constant="true" value="-INF"/>
   <parameter id="ub" name="arbitrary_upper_bound" constant="true" value="INF"/>
   <parameter id="R11" name="lower___bound" constant="true" value="0"/>
   <parameter id="R1u" name="uptake_upper_bound" constant="true" value="1"/>
<parameter id="X21" name="export_only_lower_bound" constant="true" value="0"/>
  </listOfParameters>
  <fbc:listOfGeneProducts>
   <fbc:geneProduct fbc:id="g1" fbc:name="dog_gene" fbc:label="PetGeneDB1">
  <fbc:geneProduct fbc:id="g2" fbc:name="cat_gene" fbc:label="PetGeneDB2">
<fbc:geneProduct fbc:id="g3" fbc:name="mouse_gene" fbc:label="PetGeneDB3">
<fbc:geneProduct fbc:id="g4" fbc:name="bird_gene" fbc:label="PetGeneDB4">
  </fbc:listOfGeneProducts>
  <listOfReactions>
   <reaction id="R1" reversible="false" fast="false"</pre>
     fbc:lowerFluxBound="R11" fbc:upperFluxBound="R1u" >
    <fbc:geneProteinAssociation>
     <fbc:geneProductRef fbc:geneProduct="g1"/>
    </fbc:geneProteinAssociation>
    <listOfReactants>
     <speciesReference species="IN" stoichiometry="1" constant="true"/>
    </listOfReactants>
    t0fProducts>
     <speciesReference species="A" stoichiometry="1" constant="true"/>
   <reaction id="R2" reversible="true" fast="false"</pre>
     fbc:lowerFluxBound="lb" fbc:upperFluxBound="ub">
    <fbc:geneProteinAssociation fbc:id="andGPR">
      <fbc:geneProductRef fbc:geneProduct="g1"/>
      <fbc:geneProductRef fbc:geneProduct="g4"/>
     </fbc:and>
    </fbc:geneProteinAssociation>
    <listOfReactants>
     <speciesReference species="B" stoichiometry="1" constant="true"/>
    </listOfReactants>
    tofProducts>
     <speciesReference species="OUT" stoichiometry="1" constant="true"/>
```

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```
</listOfProducts>
   </reaction>
   <reaction id="X1" reversible="true" fast="false"</pre>
     fbc:lowerFluxBound="lb" fbc:upperFluxBound="ub" >
    <fbc:geneProteinAssociation fbc:id="orGPR">
     <fbc:or>
      <fbc:geneProductRef fbc:geneProduct="g2"/>
      <fbc:geneProductRef fbc:geneProduct="g3"/>
     </fbc:or>
    </fbc:geneProteinAssociation>
    <listOfReactants>
    <speciesReference species="A" stoichiometry="1" constant="true"/>
    </list0fReactants>
    listOfProducts>
     <speciesReference species="ATP" stoichiometry="1" constant="true"/>
     <speciesReference species="B" stoichiometry="1" constant="true"/>
    </listOfProducts>
   </reaction>
   <reaction id="X2" reversible="true" fast="false"</pre>
     fbc:lowerFluxBound="X21" fbc:upperFluxBound="ub" >
    <fbc:geneProteinAssociation fbc:id="allGPR">
     <fbc:or>
      <fbc:and>
       <fbc:geneProductRef fbc:geneProduct="g1"/>
       <fbc:geneProductRef fbc:geneProduct="g4"/>
      </fbc:and>
      <fbc:and>
       <fbc:geneProductRef fbc:geneProduct="g1"/>
       <fbc:geneProductRef fbc:geneProduct="g3"/>
      </fbc:and>
     </fbc:or>
    </fbc:geneProteinAssociation>
    <listOfReactants>
    <speciesReference species="A" stoichiometry="1" constant="true"/>
    </list0fReactants>
    tofProducts>
     <speciesReference species="B" stoichiometry="1" constant="true"/>
     <speciesReference species="NADH" stoichiometry="1" constant="true"/>
    </listOfProducts>
   </reaction>
  </listOfReactions>
  <fbc:list0f0bjectives fbc:active0bjective="objective1">
   <fbc:objective fbc:id="objective1" fbc:type="maximize">
    <fbc:listOfFluxObjectives>
    <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="1"/>
    </fbc:listOfFluxObjectives>
  </fbc:objective>
 </fbc:listOfObjectives>
 </model>
</sbml>
```

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A Validation of SBML documents

A.1 Validation and consistency rules

This section summarizes all the conditions that must (or in some cases, at least *should*) be true of an SBML Level 3 Version 1 model that uses the Flux Balance Constraints package. We use the same conventions as are used in the SBML Level 3 Version 1 Core specification document. In particular, there are different degrees of rule strictness. Formally, the differences are expressed in the statement of a rule: either a rule states that a condition *must* be true, or a rule states that it *should* be true. Rules of the former kind are strict SBML validation rules—a model encoded in SBML must conform to all of them in order to be considered valid. Rules of the latter kind are consistency rules. To help highlight these differences, we use the following three symbols next to the rule numbers:

- ✓ A checked box indicates a *requirement* for SBML conformance. If a model does not follow this rule, it does not conform to the Flux Balance Constraints specification. (Mnemonic intention behind the choice of symbol: "This must be checked.")
- A triangle indicates a *recommendation* for model consistency. If a model does not follow this rule, it is not considered strictly invalid as far as the Flux Balance Constraints specification is concerned; however, it indicates that the model contains a physical or conceptual inconsistency. (Mnemonic intention behind the choice of symbol: "This is a cause for warning.")
- ★ A star indicates a strong recommendation for good modeling practice. This rule is not strictly a matter of SBML encoding, but the recommendation comes from logical reasoning. As in the previous case, if a model does not follow this rule, it is not strictly considered an invalid SBML encoding. (Mnemonic intention behind the choice of symbol: "You're a star if you heed this.")

The validation rules listed in the following subsections are all stated or implied in the rest of this specification document. They are enumerated here for convenience. Unless explicitly stated, all validation rules concern objects and attributes specifically defined in the Flux Balance Constraints package.

For convenience and brevity, we use the shorthand "fbc:x" to stand for an attribute or element name x in the namespace for the Flux Balance Constraints package, using the namespace prefix fbc. In reality, the prefix string may be different from the literal "fbc" used here (and indeed, it can be any valid XML namespace prefix that the modeler or software chooses). We use "fbc:x" because it is shorter than to write a full explanation everywhere we refer to an attribute or element in the Flux Balance Constraints package namespace.

General rules about this package

- To conform to the Flux Balance Constraints package specification for SBML Level 3 Version 1, an SBML document must declare the use of the following XML Namespace: "http://www.sbml.org/sbml/level3/version1/fbc/version2".

 (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.1 on page 6.)
- Wherever they appear in an SBML document, elements and attributes from the Flux Balance Constraints package must be declared either implicitly or explicitly to be in the XML namespace "http://www.sbml.org/sbml/level3/version1/fbc/version2". (References: SBML Level 3 Package Specification for Flux Balance Constraints , Version 1, Section 3.1 on page 6.)

General rules about identifiers

(Extends validation rule #10301 in the SBML Level 3 Version 1 Core specification.) Within a Model the values of the attributes id and fbc:id on every instance of the following classes of objects must be unique across the set of all id and fbc:id attribute values of all such objects in a model: the Model itself, plus all contained FunctionDefinition, Compartment, Species,

Reaction, SpeciesReference, ModifierSpeciesReference, Event, and Parameter objects, plus the GeneProduct, Objective, FluxObjective and GeneProteinAssociation objects defined by the Flux Balance Constraints package. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.2 on page 6.)

fbc-10302
✓ The value of a fbc:id attribute must always conform to the syntax of the SBML data type SId. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.2 on page 6.)

Rules for the extended SBML class

- fbc-20101 ✓ In all SBML documents using the Flux Balance Constraints package, the SBML object must include a value for the attribute fbc:required attribute. (References: SBML Level 3 Version 1 Core, Section 4.1.2.)
- fbc-20102

 ✓ The value of attribute fbc:required on the SBML object must be of the data type boolean. (References: SBML Level 3 Version 1 Core, Section 4.1.2.)
- fbc-20103

 ✓ The value of attribute fbc:required on the SBML object must be set to "false". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.1 on page 6.)

Rules for extended Model object

- There may be at most one instance of each of the following kinds of objects within a **Model** object using Flux Balance Constraints: **ListOfGeneProducts** and **ListOfObjectives**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.)
- The various ListOf __ subobjects with an Model object are optional, but if present, these container object must not be empty. Specifically, if any of the following classes of objects are present on the Model, it must not be empty: ListOfObjectives. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.)
- fbc-20204 ✓ Apart from the general notes and annotation subobjects permitted on all SBML objects, a ListOfObjectives container object may only contain Objective objects. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.)
- fbc-20206 ✓ A ListOfObjectives object may have the optional attributes metaid and sboTerm defined by SBML Level 3 Core. Additionally the ListOfObjectives must contain the attribute active—Objective. No other attributes from the SBML Level 3 Core namespace or the Flux Balance Constraints namespace are permitted on a ListOfObjectives object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.)
- The value of attribute fbc:activeObjective on the ListOfObjectives object must be of the data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3.1 on page 8).
- The value of attribute fbc:activeObjective on the ListOfObjectives object must be the identifier of an existing Objective. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3.1 on page 8.)

Rules for extended Species object

fbc-20301 ✓ A SBML Species object may have the optional attributes fbc:charge and fbc:chemicalFormula. No other attributes from the Flux Balance Constraints namespaces

	Constraints, Version 1, Section 3.4 on page 9)		
fbc-20302	The value of attribute fbc:charge on the SBML Species object must be of the data type integer . (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.4 on page 9).		
fbc-20303	The value of attribute fbc:chemicalFormula on the SBML Species object must be set to a string consisting only of atomic names or user defined compounds and their occurrence. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.4 on page 9.)		
Rules for Object	ive object		
fbc-20501 🗹	A Objective object may have the optional SBML Level 3 Core attributes metaid and sboTerm . No other attributes from the SBML Level 3 Core namespace are permitted on a Objective . (References: SBML Level 3 Version 1 Core, Section 3.2.)		
fbc-20502 🗹	A Objective object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on a Objective . (References: SBML Level 3 Version 1 Core, Section 3.2.)		
fbc-20503	A Objective object must have the required attributes fbc:id and fbc:type and may have the optional attribute fbc:name . No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a Objective object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20504 ✓	The attribute fbc:name on a Objective must be of the data type string . (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20505	The attribute fbc:type on a Objective must be of the data type FbcType and thus its value must be one of "minimize" or "maximize". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20506 ✓	A Objective object must have one and only one instance of the ListOfFluxObjectives object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20507 ☑	The ListOfFluxObjectives subobject within a Objective object must not be empty. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20508	Apart from the general notes and annotation subobjects permitted on all SBML objects, a ListOfFluxObjectives container object may only contain FluxObjective objects. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
fbc-20509	A ListOfFluxObjectives object may have the optional metaid and sboTerm defined by SBML Level 3 Core. No other attributes from the SBML Level 3 Core namespace or the Flux Balance Constraints namespace are permitted on a ListOfFluxObjectives object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.6 on page 11.)		
Rules for FluxObjective object			
fbc-20601	A FluxObjective object may have the optional SBML Level 3 Core attributes metaid and shoTerm . No other attributes from the SBML Level 3 Core namespace are permitted on a		

FluxObjective. (References: SBML Level 3 Version 1 Core, Section 3.2.)

fbc-20602

✓ A FluxObjective object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on a FluxObjective. (References: SBML Level 3 Version 1 Core, Section 3.2.) A FluxObjective object must have the required attributes fbc:reaction and fbc-20603 V fbc:coefficient, and may have the optional attributes fbc:id and fbc:name. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a FluxObjective object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.7 on page 12.) fbc-20604 **☑** The attribute **fbc:name** on a **FluxObjective** must be of the data type **string**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.7 on page 12.) The value of the attribute **fbc:reaction** of a **FluxObjective** object must conform to the syntax of the SBML data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.7 on page 12.) fbc-20606 ✓ The value of the attribute **fbc:reaction** of a **FluxObjective** object must be the identifier of an existing Reaction object defined in the enclosing Model object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 12.) The value of the attribute fbc:coefficient of a FluxObjective object must conform to the fbc-20607 **☑** syntax of the SBML data type double. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.7 on page 12.) When the value of the Models fbc: strict attribute is "true", the value of the attribute fbc:fbc-20608 ✓ coefficient of a FluxObjective object must not be set to "NaN", "-INF" or "INF". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) Rules for extended Reaction object fbc-20701

✓ There may be at most one instance of a GeneProteinAssociation within a Reaction object using Flux Balance Constraints. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.8 on page 13.) fbc-20702

✓ A SBML Reaction object may have the optional attributes fbc:lowerFluxBound and fbc:upperFluxBound. No other attributes from the Flux Balance Constraints namespaces are permitted on a Reaction. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.8 on page 13) The attribute fbc:lowerFluxBound of a Reaction must be of the data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.8 on page 13.) The attribute fbc:upperFluxBound of a Reaction must be of the data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.8 on page 13.) fbc-20705 V The attribute fbc:lowerFluxBound of a Reaction must point to an existing Parameter in the model. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.8 on page 13.) fbc-20706 **☑** The attribute fbc:upperFluxBound of a Reaction must point to an existing Parameter in the model. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.8 on page 13.)

When the value of the Models fbc:strict attribute is "true", a Reaction must define the atfbc-20707

✓ tributes fbc:lowerFluxBound and fbc:upperFluxBound. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the Parameter objects refered to fbc-20708 **☑** by the attributes fbc:lowerFluxBound and fbc:upperFluxBound must have their constant attribute set to "true". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the Parameter objects referred to by the attributes fbc:lowerFluxBound and fbc:upperFluxBound must have their value attribute set to a value other than "Nan". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the Parameter objects refered to by the attributes fbc:lowerFluxBound and fbc:upperFluxBound may not be targeted by an Initial Assignment. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) fbc-20711 **☑** When the value of the Models fbc:strict attribute is "true", the value of the Parameter object refered to by the attribute fbc:lowerFluxBound may not have the value "INF". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) fbc-20712

✓ When the value of the Models fbc:strict attribute is "true", the value of the Parameter object refered to by the attribute fbc:upperFluxBound may not have the value "-INF". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the value of the Parameter fbc-20713 ✓ object referred to by the attribute fbc:lowerFluxBound must be less than or equal to the value of the Parameter object refered to by the attribute fbc:upperFluxBound. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the constant attribute of fbc-20714 **☑** SpeciesReference elements of a Reaction must be set to "true". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) fbc-20715

✓ When the value of the Models fbc:strict attribute is "true", the value of a SpeciesReference's stoichiometry attribute must not be set to "NaN", "-INF" or "INF". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) When the value of the Models fbc:strict attribute is "true", the SpeciesReference elements of a **Reaction** may not be targeted by an **InitialAssignment**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.3 on page 7.) Rules for GeneProteinAssociation object fbc-20801 V A GeneProteinAssociation object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespace are permitted on a **GeneProteinAssociation**. (References: SBML Level 3 Version 1 Core, Section 3.2.)

A **GeneProteinAssociation** object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on a **GeneProteinAssociation**. (References: SBML Level 3 Version 1 Core, Section 3.2.)

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fbc-20803 **√** A GeneProteinAssociation object may have the optional attributes fbc:id fbc:name. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a GeneProteinAssociation object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.9 on page 14.) The attribute **fbc:id** on a **GeneProteinAssociation** must be of the data type **SId**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.9 on page 14.) fbc-20805 V A GeneProteinAssociation object must have one and only one of the concrete Association objects: GeneProductRef, And or Or. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.9 on page 14.) fbc-20806 **☑** The attribute fbc:name on a GeneProteinAssociation must be of the data type string. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.9 on page 14.) Rules for GeneProductRef object fbc-20901 V A GeneProductRef object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespace are permitted on a GeneProductRef. (References: SBML Level 3 Version 1 Core, Section 3.2.) A GeneProductRef object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on a GeneProductRef. (References: SBML Level 3 Version 1 Core, Section 3.2.) A GeneProductRef object must have the required attribute fbc:geneProduct and may have the optional attribute fbc:id. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a GeneProductRef object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.11 on page 15.) fbc-20904 V The attribute fbc:geneProduct on a GeneProductRef must be of the data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.11 on page 15.) fbc-20905 V The attribute **fbc:id** on a **GeneProductRef** must be of the data type **SId**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.11 on page 15.) The attribute fbc:geneProduct on a GeneProductRef if set, must refer to id of a GeneProduct in the Model. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.11 on page 15.) Rules for And object An **And** object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespace are permitted on an And. (References: SBML Level 3 Version 1 Core, Section 3.2.) fbc-20102

✓ An And object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on an And. (References: SBML Level 3 Version 1 Core, Section 3.2.) fbc-20103 **☑** An And object must have two or more concrete Association objects: GeneProductRef, And, or Or. No other elements from the SBML Level 3 Flux Balance Constraints namespace are permitted on an And object. (References: SBML Level 3 Package Specification for Flux Balance

Constraints, Version 2, Section 3.12 on page 17.)

Rules for Or object

fbc-20111 ✓ An Or object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespace are permitted on an Or. (References: SBML Level 3 Version 1 Core, Section 3.2.)

- fbc-20112 ✓ An Or object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespace are permitted on an Or. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- fbc-20113 ✓ An Or object must have two or more concrete *Association* objects: GeneProductRef, And, or Or. No other elements from the SBML Level 3 Flux Balance Constraints namespace are permitted on an Or object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 2, Section 3.13 on page 17.)

B Summary of changes between versions

B.1 Version 1 to version 2

Awaiting confirmation.

V2

Section B Summary of changes between versions

V2

V2

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If you feel you should be mentioned in this section please contact the authors and ask to be included.

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