Systems Biology Markup Language (SBML) Level 2: Structures and Facilities for Model Definitions

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Updates to this SBML language specification may appear over time.
The latest revision of the SBML Level 2 Version 2 specification is available at
http://sbml.org/specifications/sbml-level-2/version-2/

This revision of the SBML Level 2 Version 2 specification is available at
http://sbml.org/specifications/sbml-level-2/version-2/revision-1/

The list of errata for all revisions of the SBML Level 2 Version 2 specification is available at
http://sbml.org/specifications/sbml-level-2/version-2/errata/

The XML Schema for SBML Level 2 Version 2 is available at
http://sbml.org/xml-schemas/

SBML Systems Biology Markup Language

Contents

1 Introduction

We present the **S**ystems **B**iology **M**arkup **L**anguage (SBML) Level 2, a model representation formalism for systems biology. SBML is oriented towards describing systems of biochemical reactions of the sort common in research on a number of topics, including cell signaling pathways, metabolic pathways, biochemical reactions, gene regulation, and many others. SBML is defined in a neutral fashion with respect to programming languages and software encoding; however, it is primarily oriented towards allowing models to be encoded using XML, the eXtensible Markup Language (Bosak and Bray, 1999; Bray et al., 2000). This document contains many examples of SBML models written in XML, as well as an XML Schema (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000) that defines SBML Level 2 Version 2. A downloadable copy of the XML Schema and other related documents and software are also available from the SBML project web site, `http://sbml.org/`.

The SBML project is not an attempt to define a universal language for representing quantitative models; the rapidly evolving views of biological function, coupled with the vigorous rates at which new computational techniques and individual tools are being developed today, are incompatible with a one-size-fits-all idea of a universal language. A more realistic alternative is to acknowledge the diversity of approaches and methods being explored by different software tool developers, and seek a common intermediate format—a *lingua franca*—enabling communication of the most essential aspects of the models.

1.1 Developments, Discussions, and Notifications of Updates

SBML has been, and continues to be, developed in collaboration with an international community of researchers and software developers. As in many projects, the primary mode of interaction between members is electronic mail, with discussions taking place on the mailing list `sbml-discuss@caltech.edu`. The mailing list archives and a Web browser-based interface to the list are available at `http://sbml.org/forums/`. It is *vitally important that all users of SBML stay informed about developments and revisions* by monitoring the mailing list or periodically visiting the SBML project web site, `http://sbml.org/`.

In Section 8.1, we attempt to acknowledge as many contributors to SBML's development as we can, but as SBML evolves, it becomes increasingly difficult to detail the individual contributions on a project that has truly become an international community effort.

1.2 SBML Levels, Versions, and Revisions

Major releases of SBML are termed *levels* and represent substantial changes to the composition and structure of the language. The release of SBML defined in this document, SBML Level 2, represents an incremental evolution of the language resulting from the practical experiences of many users and developers working with SBML Level 1 since its introduction in the year 2001 (Hucka et al., 2001, 2003). All of the structures of Level 1 can be mapped in a straightforward fashion to Level 2. In addition, a subset of the structures in Level 2 can be mapped to Level 1. However, the levels remain distinct; a valid SBML Level 1 document is not a valid SBML Level 2 document, and likewise, a valid SBML Level 2 document is not a valid SBML Level 1 document.

Minor releases of SBML are termed *versions* and constitute changes within an SBML Level to correct, adjust and refine language features. The present document defines SBML Level 2 Version 2. Appendix A lists the differences between SBML Level 2 Version 2 and Level 1 Version 2. Differences in the specifications of Version 1 and Version 2 of SBML Level 2 are highlighted in red in the body of this specification and are also listed in Appendix B.

Language specification documents inevitably require minor editorial changes as its communities of users discover errors and ambiguities. As a practical reality, these discoveries occur over time. In the context of SBML, such problems are formally announced publicly as *errata* in a given specification document. Borrowing concepts and processes from the World Wide Web consortium (Jacobs, 2004), we define SBML errata as changes of the following types: (a) formatting changes that do not result in changes to textual content; (b) corrections that do not affect conformance of software implementing support for a given combination of

SBML Level and Version; and (c) corrections that *may* affect such software conformance, but add no new language features. A change that affects conformance is one that either turns conforming data, processors, or other conforming software into non-conforming software, or turns non-conforming software into conforming software, or clears up an ambiguity or insufficiently documented part of the specification in such a way that software whose conformance was once unclear now becomes clearly conforming or non-conforming (Jacobs, 2004). In short, errata do not change the fundamental semantics or syntax of SBML, but rather clarify and disambiguate the specification and correct errors. (New syntax and semantics are only introduced in SBML Versions and Levels.)

Errata result in new *Revisions* of the SBML specification. Each revision is numbered with an integer, with the first revision of the specification being given the number 1. Subsequent revisions of an SBML specification document contain a section listing the accumulated errata issued since the first revision. A complete list of the errata for SBML Level 2 Version 2 since the publication of Revision 1 is made publicly available at http://sbml.org/specifications/sbml-level-2/version-2/errata/.

1.3 Deprecated Features

For the first time, a language feature of previous SBML levels and versions is deprecated in SBML Level 2 Version 2. The interpretation of a *deprecated feature* of SBML is the following:

> If a given feature is marked as deprecated, software implementations may chose to ignore that feature and still be considered compliant with the SBML specification. Beginning with the Level and Version in which a given feature is deprecated, software tools should not generate models containing the deprecated feature.

The feature deprecated in Level 2 Version 2 is the `charge` field on Species. This field does not appear to have been supported by any existing software, so the impact of this change is expected to be small.

The need for removing features from a language, whether SBML or other, is largely inevitable. SBML must by necessity continue evolving through the experiences of its users and implementors. Eventually, some features will be deemed unhelpful despite the best intentions of the language editors.

1.4 Backwards Compatibility Between Level 2 Version 2 and Level 2 Version 1

SBML Level 2 Version 2 is designed to be maximally backward compatible with SBML Level 2 Version 1 in the following sense: an XML document defining a valid model in SBML Level 2 Version 1, after changing the XML namespace and `version` attribute values on the `sbml` container element (see Section 4.1), can become a valid SBML Level 2 Version 2 document, subject to the following provisions:

1. UnitDefinition in SBML Level 2 Version 2 does not contain an `offset` field, and the interpretation of unit definitions has been defined and clarified more explicitly in this specification document. As a result of the changes, previous models containing `offset` on UnitDefinition objects are incompatible syntactically with Level 2 Version 2. See Section 4.4 for more explanation of SBML unit definitions and the implications of this change.

2. SBML Level 2 Version 2 is somewhat stricter about how the content of `annotation` elements must be organized. Previously valid SBML Level 2 Version 1 documents *may* need changes to their `annotation` elements to comply with the new specification. See Section 3.3.3 for more details.

3. SBML Level 2 Version 2 corrects numerous errata discovered in SBML Level 2 Version 1 since the time of the latter's introduction. These errata are listed in Section 1.2. As a result of changes to SBML Level 2 implied by these errata, some existing SBML Level 2 Version 1 models, even when modified as explained above, may still not be compliant with Version 2. The ultimate impact of the changes depends on the specific features used by a given model and the assumptions under which the model was created.

1.5 Scope and Limitations

SBML is designed to encode quantitative and qualitative models of biochemical reaction networks. The model representation scheme is designed to capture the data required by simulation and analysis tools that operate on these models. Although the focus of SBML is on models of biochemical reaction networks, SBML is also capable of encoding more general models composed of first-order ordinary differential equations and algebraic equations. Future software tools will undoubtedly require further evolution of SBML, and we expect that higher SBML levels will add structures and facilities on top of Level 2 after the simulation community has had time to gain experience with the current language definition. In Section 8.1, we discuss extensions that will likely be included in SBML Level 3.

The definition of the model description language presented here does not specify *how* programs should communicate or read/write SBML. We assume that for a simulation program to communicate a model encoded in SBML, the program will have to translate its internal data structures to and from SBML, use a suitable transmission medium and protocol, etc., but these issues are outside of the scope of this document.

1.6 Notational Conventions

We define SBML using a graphical notation based upon UML, the Unified Modeling Language (Eriksson and Penker, 1998; Oestereich, 1999). This UML-based definition in turn is used to define an XML Schema (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000) for SBML. The XML Schema defines the encoding of SBML documents in XML. In this section, we briefly summarize this UML-based approach and notation and its mapping to XML Schema 1.0. More details are available in a separate document (Hucka, 2000).

There are three main advantages to using UML as a basis for defining SBML data structures. First, compared to using other notations or a programming language, the UML visual representations are generally easier to grasp by readers who are not computer scientists. Second, the notation is implementation-neutral: the defined structures can be encoded in any concrete implementation language—not just XML, but C, Java and other languages as well. Third, UML is a de facto industry standard that is documented in many resources. Readers are therefore more likely to be familiar with it than other notations.

1.6.1 Typographical Conventions for Names

The following typographical notations are used in this document to distinguish object classes from other kinds of entities:

AbstractClass: Abstract classes are classes that are never instantiated directly, but rather serve as parents of other classes. Their names begin with a capital letter and they are printed in a slanted sans-serif typeface. In electronic document formats, the class names are also hyperlinked to their definitions in the specification. For example, in the PDF and HTML versions of this document, clicking on the word *Sbase* will send the reader to the figure showing the definition of this class.

Class: Names of ordinary (concrete) classes begin with a capital letter and are printed in an upright sans-serif typeface. In electronic document formats, the class names are also hyperlinked to their definitions in the specification. For example, in the PDF and HTML versions of this document, clicking on the word Species will send the reader to the figure showing the definition of this class.

`SomeThing`, `otherThing`: Fields within classes, primitive data type names, literal XML strings, and generally all tokens *other* than SBML UML class names, are printed in an upright typewriter typeface. Primitive types defined in SBML begin with a capital letter, but unfortunately, XML Schema 1.0 does not follow any convention and primitive XML types may either start with a capital letter (e.g,. `ID`) or not (e.g., `double`).

1.6.2 Notational Conventions for Object Fields

The basis of this UML-to-XML Schema approach is to translate object classes such as *Sbase* into XML Schema 1.0 complex types. When instances of these classes are expressed in XML, they are implemented as

XML *elements* and their fields are implemented either as *attributes* on the elements, or as subelements. The following example class definition illustrates the notation used for different types of fields in this specification document:

ExampleClass
field1: integer
field2: Species[0..*]
field3: double { use="optional" default="0.0" }
math: Math { namespace="http://www.w3.org/1998/Math/MathML" }
field4: (math : Math { namespace="http://www.w3.org/1998/Math/MathML" })

The symbols `field1`, `field2`, etc., represent fields in an object class. The colon immediately after the name separates the name of the field (on the left) from the type of data that it stores (on the right).

The order fields `field1`, `field2`, etc., in the XML encoding *is* significant and *must* follow the order given in the corresponding UML diagram. This ordering constraint also holds true when a subclass inherits fields from a base class: the base class field elements must occur before those introduced by the subclass. This ordering constraint is introduced by aspects of XML Schema beyond SBML's control. (Software developers should beware that the ordering requirement is a frequent cause of compatibility problems; validating XML parsers will generate errors if the field ordering of an XML element does not correspond to the SBML object class definition.)

Expressions in curly braces ({}) shown after a field type indicate additional constraints placed on the field. We express constraints using the XML Schema language. In the examples above, the text {`use="optional" default="0.0"`} indicates that the field `field3` is optional and that it has a default value of 0.0. A constraint of the form {`namespace="`*X*`"`} indicates that the field is not in the SBML Level 2 XML namespace but resides in the given XML namespace *X*. If a field is in a different namespace, then the type of the field will not be defined by the SBML UML but rather by another source. In the examples above, the `math` field and its content is defined in the MathML namespace.

Simple Attribute Fields

In the example above, `field1` is a field that would be translated into an XML attribute. Its value can be a simple scalar type such as `string`, `SId` and `double`, as well as enumeration types. All of the other fields shown in the example above are implemented as XML subelements—elements contained within the element that represents an instance of the class. They can represents lists and substructures.

Lists

Square brackets (`[]`) just after a type name indicate that the field contains a list of elements each having the same type. Specifically, the notation `[0..*]` signifies a list containing zero or more elements, the notation `[1..*]` signifies a list containing at least one element, and so on, with the asterix character indicating an unbounded upper limit.

The approach used here to translate from a list form into XML is, first, to create a subelement named `listOf_____s`, where the blank indicates the capitalized name of the field. (For example, `listOfField2s`.) Within this sublement are placed elements each of which has the name of the type, beginning with a lowercase letter. Here is an example:

```
<listOfCompartments>
    <compartment id="cytosol" size="2.5"/>
    <compartment id="mitochondria" size="0.3"/>
</listOfCompartments>
```

When list fields can have zero elements (i.e., the type name is followed by `[0..*]`), the `listOf_____s` element is optional. That is, a missing `listOf_____` element in an SBML XML instance document indicates that the list is empty. The `listOf_____` elements, when present, should always have content.

Substructures

A field definition of the form `X : (A : B)` defines an element X that contains a field A with type B. If A is the string `ANY` then the element X contains an arbitrary sequence of elements. A field definition of the form `X : ( A : B )` { `C` } is similar except that the field X and its content is constrained by constraint C. A field definition of the form `X : ( A : B` { `C` } `)` is similar except that the field A and its content is constrained by constraint C. In the examples above the field `field4` is an element which contains a `math` field. The `math` field is in the MathML namespace but `field4` is in the SBML namespace.

Additional Notes about the Translation to XML Schema

The class definitions are mapped to XML Schema 1.0 `complexType` elements. A class inheriting fields from a base class is constructed in XML Schema using a `extension` element. The fields that are implemented as XML attributes are represented in XML Schema as `attribute` elements. The fields that are implemented as XML elements are represented in XML Schema as `element` elements within a `sequence` element. See Appendix C for a mapping of this SBML specification to XML schema. Not all of the constraints on SBML documents described in this document can be practically expressed in XML Schema 1.0. Appendix E defines additional rules, beyond what is encoded in the XML Schema for SBML, that must followed to produce a valid SBML document. See Walmsley (2002) for more information on XML Schema.

1.7 Guide to the Rest of this SBML Specification Document

In the rest of this document, we describe in detail SBML's various constructs and their uses, provide examples and guidelines, and describe the differences compared to previous releases of SBML. More specifically:

- Section 2 provides a high-level overview of SBML Level 2 Version 2 and is constructs;
- Section 3 introduces concepts, definitions and principles that are used throughout SBML;
- Section 4 describes in detail each of the main components of SBML Level 2 Version 2;
- Section 6 describes a recommend format for certain kinds of annotations on SBML components;
- Section 7 provides a number of complete examples of models encoded in XML;
- Section 8 contains a list of changes that are anticipated for Level 3;
- Appendix A describes the differences between SBML Level 1 Version 2 and SBML Level 2 Version 1;
- Appendix B describes the differences between SBML Level 2 Version 1 and SBML Level 2 Version 2;
- Appendix C provides the complete XML Schema for SBML Level 2 Version 2;
- Appendix D provides the XML schema for the subset of MathML 2.0 used in SBML; and
- Appendix E lists the validation rules that are required to determine the correctness of an SBML document beyond simple XML Schema conformance.

2 Overview of SBML

The following is an example of a simple network of biochemical reactions that can be represented in SBML:

$$S_1 \xrightarrow{k_1[S_1]/([S_1]+k_2)} S_2$$

$$S_2 \xrightarrow{k_3[S_2]} S_3 + S_4$$

In this particular set of chemical equations above, the symbols in square brackets (e.g., "$[S_1]$") represent concentrations of molecular species, the k's represent constants, and the arrows represent reactions taking place at rates determined by the formulas above them. (And while this example uses concentrations, it could equally have used other measures such as molecular counts.) Broken down into its constituents, this model contains a number of components: reactant species, product species, reactions, rate laws, and parameters in the rate laws. To analyze or simulate this network, additional components must be made explicit, including compartments for the species, and units on the various quantities.

The top level of an SBML model definition simply consists of lists of these components, with every list being optional:

beginning of model definition
- *list of function definitions (optional)*
- *list of unit definitions (optional)*
- *list of compartment types (optional)*
- *list of species types (optional)*
- *list of compartments (optional)*
- *list of species (optional)*
- *list of parameters (optional)*
- *list of initial assignments (optional)*
- *list of rules (optional)*
- *list of constraints (optional)*
- *list of reactions (optional)*
- *list of events (optional)*

end of model definition

The meaning of each component is as follows:

Function definition: A named mathematical function that may be used throughout the rest of a model.

Unit definition: A named definition of a new unit of measure, or a redefinition of an existing SBML default unit. Named units can be used in the expression of quantities in a model.

Compartment Type: A type of location where reacting entities such as chemical substances may be located.

Species type: A type of entity that can participate in reactions. Examples of species types include ions such as Ca^{2+}, molecules such as glucose or ATP, binding sites on a protein, and more.

Compartment: A well-stirred container of a particular type and finite size where species may be located. A model may contain multiple compartments of the same compartment type. Every species in a model must be located in a compartment.

Species: A pool of entities of the same *species type* located in a specific *compartment*.

Parameter: A quantity with a symbolic name. In SBML, the term *parameter* is used in a generic sense to refer to named quantities regardless of whether they are constants or variables in a model. SBML Level 2 provides the ability to define parameters that are global to a model as well as parameters that are local to a single reaction.

Initial Assignment: A mathematical expression used to determine the initial conditions of a model. This type of structure can only be used to define how the value of a variable can be calculated from other values and variables at the start of simulated time.

Rule: A mathematical expression used in combination with the differential equations constructed based on the set of reactions in a model. It can be used to define how a variable's value can be calculated from other variables, or used to define the rate of change of a variable. The set of rules in a model can be used with the reaction rate equations to determine the behavior of the model with respect to time. The set of rules constrains the model for the entire duration of simulated time.

Constraint: A mathematical expression that defines a constraint on the values of model variables. The constraint applies at all instants of simulated time. The set of constraints in model should not be used to determine the behavior of the model with respect to time.

Reaction: A statement describing some transformation, transport or binding process that can change the amount of one or more species. For example, a reaction may describe how certain entities (reactants) are transformed into certain other entities (products). Reactions have associated kinetic rate expressions describing how quickly they take place.

Event: A statement describing an instantaneous, discontinuous change in a set of variables of any type (species concentration, compartment size or parameter value) when a triggering condition is satisfied.

Table 1 provides a summary of the sections in this document where each of these components is described in more detail.

A software package can read an SBML model description and translate it into its own internal format for model analysis. For example, a package might provide the ability to simulate the model by constructing differential equations representing the network and then perform numerical time integration on the equations to explore the model's dynamic behavior.

SBML allows models of arbitrary complexity to be represented. Each type of component in a model is described using a specific type of data structure that organizes the relevant information. The data structures determine how the resulting model is encoded in XML.

Component	Section	Starting page	New in Version 2?
Function definition	4.3	24	
Unit definition	4.4	26	
Compartment type	4.5	32	Yes
Species type	4.6	33	Yes
Compartment	4.7	34	
Species	4.8	36	
Parameter	4.9	39	
Initial assignment	4.10	40	Yes
Rule	4.11	43	
Constraint	4.12	48	Yes
Reaction	4.13	50	
Event	4.14	57	

Table 1: *A guide to the sections, and their starting page numbers, where each major SBML component is described in this specification document. The "New?" column indicates whether a given component is new as of SBML Level 2 Version 2.*

3 Preliminary Definitions and Principles

This section covers certain concepts and constructs that are used repeatedly in the rest of SBML Level 2.

3.1 Primitive Data Types

Many primitive types in SBML are taken from the data types defined in XML Schema 1.0 (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000). A few other primitive types are defined by SBML itself. What follows is a summary of the XML Schema types and the definitions of the SBML-specific types. Note that while we have tried to provide accurate and complete summaries of the XML Schema types, the following should not be taken to be normative definitions of these types. Readers should consult the XML Schema 1.0 specification for the normative definitions of the XML types used by SBML.

3.1.1 Type `string`

The XML Schema 1.0 type `string` is used to represent finite-length strings of characters. The characters permitted to appear in XML Schema `string` include all Unicode characters (Unicode Consortium, 1996) except for two delimiter characters, 0xFFFE and 0xFFFF (Biron and Malhotra, 2000). In addition, the following quoting rules specified by XML for character data (Bray et al., 2000, Section 2.4) must be obeyed:

- The ampersand (`&`) character must be escaped using the entity `&`.
- The apostrophe (`'`) and quotation mark (`"`) characters must be escaped using the entities `&apos;` and `&quot;`, respectively, when those characters are used to delimit a string attribute value.

Other XML built-in character or entity references, e.g., `<` and `&x1A;`, are permitted in strings.

3.1.2 Type `boolean`

The XML Schema 1.0 type `boolean` is used to represent the mathematical concept of binary-valued logic. The permitted literal values of a data field having type `boolean` are the following: "`true`", "`false`", "`1`", and "`0`". The value "`1`" maps to "`true`" and the value "`0`" maps to "`false`".

3.1.3 Type `integer`

The XML Schema 1.0 type `integer` is used to represent decimal integer numbers. The literal representation of an integer is a finite-length sequence of decimal digit characters with an optional leading sign ("+" or "-"). If the sign is omitted, "+" is assumed. There is no restriction on the absolute size of integer values in object fields in the SBML XML namespace; this matches the MathML 2.0 definition of integers.

3.1.4 Type `positiveInteger`

The XML Schema 1.0 type `positiveInteger` is used to represent nonzero, nonnegative, decimal integers: i.e., 1, 2, 3, ... The literal representation of an integer is a finite-length sequence of decimal digit characters, optionally preceded by a positive sign ("+"). There is no restriction on the absolute size of integer values in object fields in the SBML XML namespace; this matches the MathML 2.0 definition of integers.

3.1.5 Type `double`

The XML Schema 1.0 type `double` is the data type of floating point fields in SBML objects. It is restricted to IEEE double-precision 64-bit floating point type IEEE 754-1985.

The restriction on floating point fields in the SBML XML namespace differs from the restriction on floating point numbers in the MathML XML namespace. The values of the content of MathML `cn` elements do not necessarily conform to any specific floating point or integer representations designed for CPU implementation. For example the value of a `cn` element may exceed the maximum value that can be stored in a IEEE 64 bit floating point number (IEEE 754). We elaborate on this issue further in Section 3.5.3 and discuss additional important considerations.

3.1.6 Type ID

The XML Schema 1.0 type `ID` is identical to the XML 1.0 type `ID`. The lexical representation of this type consists of strings of characters restricted as shown in Figure 1.

```
letter      ::=  'a'..'z','A'..'Z'
digit       ::=  '0'..'9'
NCNameChar  ::=  letter | digit | '.'  | '-' | '_' | CombiningChar | Extender
ID          ::=  ( letter | '_' ) NCNameChar*
```

Figure 1: *The definition of the XML Schema type `ID` expressed in the variant of BNF used by the XML 1.0 specification (Bray et al., 2000). The characters (and) are used for grouping, the character * indicates "zero or more times", and the character | indicates "or". The `CombiningChar` production is a list of characters that add such things as accents to the preceding character. (For example, the Unicode character `#x030A` when combined with 'a' produces 'å'.) The `Extender` production is a list of characters that extend the shape of the preceding character. Please consult the XML 1.0 specification (Bray et al., 2000) for the complete definition of these last two productions.*

An important aspect of `ID` is the XML requirement that a given value of `ID` must be unique throughout an XML document. All data values of type `ID` are considered to reside in a single common global namespace spanning the entire XML document, regardless of the data fields (or XML attributes) where type `ID` is used and regardless of the level of nesting of the object structures (or XML elements).

3.1.7 Type SId

The type `SId` is the type of the `id` field found on the majority of SBML components. `SId` is a data type derived from the basic XML type `string`, but with restrictions about the characters permitted and the sequences in which those characters may appear. The definition of the type is shown in Figure 2.

```
letter   ::=  'a'..'z','A'..'Z'
digit    ::=  '0'..'9'
idChar   ::=  letter | digit | '_'
SId      ::=  ( letter | '_' ) idChar*
```

Figure 2: *The definition of the type `SId`. (Please see the caption of Figure 1 for an explanation of the notation.)*

The equality of `SId` values is determined by an exact character sequence match; i.e., comparisons of these identifiers must be performed in a case-sensitive manner. This applies to all uses of `SId` including the identifiers of unit definitions.

The `SId` is purposefully not derived from the XML `ID` type (Section 3.1.6). Using XML's `ID` would force all SBML identifiers to exist in a single global namespace, which would affect not only the form of local parameter definitions but also future SBML extensions for supporting model/submodel composition. Further, the use of the `ID` type for SBML identifiers would have limited utility because MathML 2.0 `ci` elements are not of the type `IDREF` (see Section 3.5). Since the `IDREF`/`ID` linkage cannot be exploited in MathML constructs, the utility of the XML `ID` type is greatly reduced.

3.1.8 Type SBOTerm

The type `SBOTerm` is used as the data type of a field called `sboTerm` available in many SBML objects. The type consists of strings of characters matching the restricted pattern described in Figure 3.

```
SBOTerm ::= SBO:[0-9][0-9][0-9][0-9][0-9][0-9][0-9]
```

Figure 3: *The definition of `SBOTerm`. The `SBOTerm` type consists of strings beginning with `SBO:` and followed by seven decimal digits. (Please see the caption of Figure 1 for an explanation of the notation.)*

Examples of valid string values of type `SBOTerm` are "`SBO:0000014`" and "`SBO:0003204`". These values are meant to be the identifiers of terms from an ontology whose vocabulary describes entities and processes in

computational models. Section 5 provides more information about the ontology and principles for the use of these terms in SBML models.

3.2 The SBML Object Inheritance Hierarchy

As explained above, the base data types in SBML are taken directly from XML Schema (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000). SBML defines additional object classes beyond this. The overall SBML inheritance hierarchy is depicted in Figure 4.

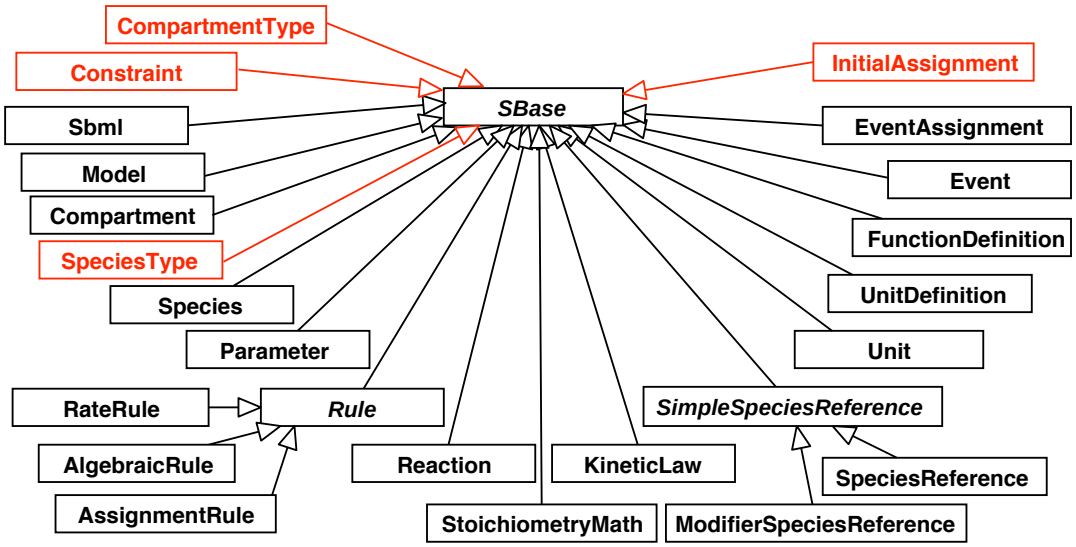

Figure 4: *A UML diagram of the inheritance hierarchy of major data types in SBML. Open arrows indicate inheritance, pointing from inheritors to their parents (Eriksson and Penker, 1998; Oestereich, 1999). In addition to these types, all substructures in SBML (including, for example, all the* `listOf` *lists) are also derived from Sbase. See text for details.*

3.3 Type SBase

Every structure composing an SBML Level 2 model definition has a specific data type that is derived directly or indirectly from a single abstract type called *Sbase*. In addition to serving as the parent class for most other classes of objects in SBML, this base type is designed to allow a modeler or a software package to attach arbitrary information to each major structure or list in an SBML model. The definition of *Sbase* is presented in Figure 5 on the following page.

In addition, the `listOf`_____ lists and all substructures such as `trigger` on Event (Section 4.14) are also derived from *Sbase*. (However, the `notes` and `annotation` fields in *Sbase*, discussed below, are not derived from *Sbase*.)

Sbase contains three fields, all of which are optional: `metaid`, `notes` and `annotation`. These fields are discussed separately in the following subsections.

3.3.1 The `metaid` Field

The `metaid` field is present for supporting metadata annotations using RDF (Resource Description Format; Lassila and Swick, 1999). It has a data type of XML `ID` (the XML identifier type), which means each `metaid` value must be globally unique within an SBML file. The `metaid` value serves to identify the element so that it can be referenced by metadata placed within `annotation` structures (see Section 3.3.3). Such metadata can use RDF `description` elements in which the RDF `describes` attributes contain the values of the `metaid`'s of objects in the SBML model.

SBase
metaid: ID { use="optional" }
notes: (ANY : { namespace="http://www.w3.org/1999/xhtml" }) { minOccurs="0" maxOccurs="1" }
annotation: (ANY) { minOccurs="0" maxOccurs="1" }

Figure 5: *The definition of Sbase. Text enclosed in braces next to field types (e.g., {`minOccurs="0"`}) indicates constraints on the possible field values. We use the XML Schema language to express constraints because we are primarily interested in the XML encoding of SBML. The constraint expression {`use="optional"`} means that the indicated field is optional and may be omitted in a particular instance in a model. The constraint expression `minOccurs="0"` likewise means the indicated field is optional; this alternate form of expression must be used for those fields that are containers (i.e., fields encoded as subelements in XML).*

3.3.2 The `notes` Field

The field `notes` in *Sbase* is a container for XHTML 1.0 (Pemberton et al., 2002) content. It is intended to serve as a place for storing optional information intended to be seen by humans. An example use of the `notes` field would be to contain formatted user comments about the structure in which the `notes` field is enclosed. Every data object derived directly or indirectly from type *Sbase* can have a separate value for `notes`, allowing users considerable freedom when adding comments to their models.

The content of `notes` must declare the use of the XHTML namespace. The proper namespace URI is `http://www.w3.org/1999/xhtml`. There are multiple ways in which this can be done. One way is to place the namespace declaration on the top-level Sbml object (see Section 4.1) and then reference the namespace in the `notes` content. The following example illustrates this approach:

```
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2"
      xmlns:xhtml="http://www.w3.org/1999/xhtml">
  ...
  <notes>
    <xhtml:body>
      <xhtml:center><xhtml:h2>A Simple Mitotic Oscillator</xhtml:h2></xhtml:center>
      <xhtml:p>A minimal cascade model for the mitotic oscillator
      involving cyclin and cdc2 kinase</xhtml:p>
    </xhtml:body>
  </notes>
  ...
```

Another approach is to declare the XHTML namespace within the `notes` content itself. The following is an example of this approach:

```
...
<notes>
  <body xmlns="http://www.w3.org/1999/xhtml">
    <center><h2>A Simple Mitotic Oscillator</h2></center>
    <p>A minimal cascade model for the mitotic oscillator
    involving cyclin and cdc2 kinase</p>
  </body>
</notes>
...
```

Still other approaches are possible. Section 7 provides additional examples of using `notes` in different models.

XHTML 1.0 is simply a formulation of HTML 4 in XML 1.0. This means the full power of HTML formatting is available for use in `notes` content. The intention behind requiring XHTML for `notes` content is to regulate the format of notes in a way that software developers will hopefully find easy to support, yet at the same time, to provide enough regulation on the format that users can predict to some degree how their notes will be displayed in different tools and environments. Libraries for displaying and editing HTML content are commonly available in contemporary software programming environments, and software developers may wish to avail themselves of these facilities rather than implementing their own XHTML support systems.

3.3.3 The annotation Field

Whereas the **notes** field described above is a container for content to be shown directly to humans, the **annotation** field is a container for optional software-generated content *not* meant to be shown to humans. Every data object derived from *Sbase* can have its own value for **annotation**. The field's data type is XML type **any**, allowing essentially arbitrary data content. SBML places only a few restrictions on the organization of the content; these are intended help software tools read and write the data as well as help reduce conflicts between annotations added by different tools.

The Use of XML Namespaces in annotation

At the outset, software developers should keep in mind that multiple software tools may attempt to read and write annotation content. To reduce the potential for collisions between annotations written by different applications, SBML Level 2 Version 2 stipulates that tools must use XML namespaces (Bray et al., 1999) to specify the intended vocabulary of every annotation. The application's developers must choose a URI (*Universal Resource Identifier*; Harold and Means 2001; W3C 2000a) reference that uniquely identifies the vocabulary the application will use, and a prefix string for the annotations. Here is an example. Suppose an application uses the URI **http://www.mysim.org/ns** and the prefix **mysim** when writing annotations related to screen layout. The content of an annotation might look like the following:

```
<annotation>
    <mysim:nodecolors xmlns:mysim="http://www.mysim.org/ns"
         mysim:bgcolor="green"
         mysim:fgcolor="white"/>
</annotation>
```

In this particularly simple case, the content consists of a single XML element (**nodecolors**) with two attributes (**bgcolor**, **fgcolor**), all of which are prefixed by the string **mysim**. (Presumably this particular content would have meaning to the hypothetical application in question.) The content in this particular example is small, but it should be clear that there could easily have been an arbitrarily large amount of data placed inside the **mysim:nodecolors** element.

The key point of the example above is that application-specific annotation data is entirely contained inside a single *top-level element* within the SBML **annotation** container. SBML Level 2 Version 2 places the following restrictions on annotations:

- Within a given SBML **annotation** element, there can only be one top-level element using a given namespace.
- No top-level element in an **annotation** may use an SBML XML namespace, either explicitly by referencing one of the SBML XML namespace URIs or implicitly by failing to specify any namespace on the annotation. (As of SBML Level 2 Version 2, the defined SBML namespaces are the following URIs: **http://www.sbml.org/sbml/level1**, **http://www.sbml.org/sbml/level2**, as well as **http://www.sbml.org/sbml/level2/version2**.)
- The ordering of top-level elements within a given **annotation** element is *not* significant. An application should not expect that its annotation content appears first in the **annotation** element, nor in any other particular location.

The use of XML namespaces in this manner is intended to improve the ability of multiple applications to place annotations on SBML model structures with reduced risks of interference or name collisions. Annotations stored by different simulation packages can therefore coexist in the same model definition. The rules governing the content of **annotation** elements are designed to enable applications to easily add, change, and remove their annotations from SBML elements while simultaneously preserving annotations inserted by other applications when mapping SBML from input to output.

Some more examples hopefully will make this more clear. The next example is invalid because it contains a top-level element in the SBML XML namespace—this happens because no namespace is declared for the **<cytoplasm>** element, which means by default it falls into the SBML namespace:

```
<annotation>
    <cytoplasm/>
</annotation>
```

The following example is invalid because it contains two top-level elements using the same XML namespace. Note that it does not matter that these are two different top-level elements (<nodecolors> and <textcolors>); what matters is that these separate elements are both in the same namespace rather than having been collected and placed inside one overall container element for that namespace.

```
<annotation>
    <mysim:nodecolors xmlns:mysim="http://www.mysim.org/ns"
        mysim:bgcolor="green"
        mysim:fgcolor="white"/>
    <mysim:textcolors xmlns:mysim="http://www.mysim.org/ns"
        mysim:bgcolor="green"
        mysim:fgcolor="white"/>
</annotation>
```

On the other hand, the following example is valid:

```
<annotation>
    <mysim:geometry xmlns:mysim="http://www.mysim.org/ns"
         mysim:bgcolor="green" mysim:fgcolor="white">
        <graph:node xmlns:graph="http://www.graph.org/ns" graph:x="4" graph:y="5" />
    </mysim:geometry>
    <othersim:icon xmlns:othersim="http://www.othersim.com/">
        WS2002
    </othersim:icon>
</annotation>
```

It is worth keeping in mind that although XML namespace names must be URI references, they are (like all XML namespace names) *not required* to be directly usable in the sense of identifying an actual, retrieval document or resource on the Internet (Bray et al., 1999). URIs such as `http://www.mysim.org/` may appear as though they are (e.g.,) Internet addresses, but there are not the same thing. This style of URI strings, using a domain name and other parts, is only a simple and commonly-used way of creating a unique name string.

Finally, note that the namespaces being referred to here are XML namespaces specifically in the context of the `annotation` field on *Sbase*. The namespace issue here is unrelated to the namespaces discussed in Section 3.4.1 in the context of component identifiers in SBML.

Content of Annotations and Implications for Software Tools

The `annotation` field in the definition of *Sbase* exists in order that software developers may attach optional application-specific data to the structures in an SBML model. However, it is important that this facility not be misused. In particular, it is *critical* that data essential to a model definition or that can be encoded in existing SBML structures is *not* stored in `annotation`. Parameter values, functional dependencies between model structures, etc., should not be recorded as annotations. It is crucial to keep in mind the fact that data placed in annotations can be freely ignored by software applications. If such data affects the interpretation of a model, then software interoperability is greatly impeded.

Here are examples of the kinds of data that may be appropriately stored in `annotation`: (a) information about the graphical layout of model components; (b) application-specific processing instructions that do not change the essential meaning of a model; (c) identification information for cross-referencing components in a model with items in a data resource such as a database.

Standardized Format for Certain Classes of Annotations

For case (c) above (i.e., information for cross-referencing components in a model to data resources), SBML Level 2 Version 2 recommends a standard format for use within an `annotation` field. This format should be used in preference to proprietary syntaxes to maximize the likelihood that multiple software tools will converge on the same syntax for this kind of information. The SBML Level 2 Version 2 recommended scheme is described in Section 6.

3.4 The `id` and `name` Fields on SBML Components

As will become apparent below, most structures in SBML include two common fields: `id` and `name`. These fields are not defined on *Sbase* (as explained in Section 3.4.3 below), but where they do appear, the common rules of usage described below apply.

3.4.1 The `id` Field and Identifier Scoping

The `id` field is a mandatory field on most structures in SBML. It is used to identify a component within the model definition. Other SBML structures can refer to the component using this identifier. Section 3.1.7 provides a definition of the data type `SId` used for the `id` field.

A biochemical network model can contain a large number of components representing different parts of a model. This leads to a problem in deciding the scope of an identifer: in what contexts does a given identifier X represent the same thing? The approaches used in existing simulation packages tend to fall into two categories which we may call global and local. The *global* approach places all identifiers into a single global namespace, so that an identifier X represents the same thing wherever it appears in a given model definition. The *local* approach places symbols in different namespaces depending on the context, where the context may be, for example, individual reaction rate expressions. The latter approach means that a user may use the same identifer X in different rate expressions and have each instance represent a different quantity.

The fact that different simulation programs may use different rules for identifier resolution poses a problem for the exchange of models between simulation tools. Without careful consideration, a model written out in SBML format by one program may be misinterpreted by another program. SBML Level 2 must therefore include a specific set of rules for treating identifers and their scopes.

The scoping rules in SBML Level 2 are relatively straightforward and are intended to avoid this problem with a minimum of requirements on the implementation of software tools:

- The identifiers (i.e., the values of the field `id`) of functions, compartment types, compartments, species types, species, reactions, species references, modifier species references, events, global parameters, and the model object, must be unique across the set of all such identifiers in the model. This means, for example, that a reaction and a species definition cannot both have the same identifier.
- Each Reaction instance (see Section 4.13) establishes a private local namespace for local parameter identifiers. Within the definition of a given reaction, local parameter identifiers introduced in that reaction override (shadow) identical identifers outside of that reaction. Of course, the corollary of this is that local parameters inside a Reaction object instance are not visible to other objects outside of that reaction.
- Unit identifiers (the values of the field `id` in the UnitDefinition structure) exist in a separate global namespace distinct from other identifiers.

The set of rules above can enable software packages using either local or global namespaces for parameters to exchange SBML model definitions. In particular, software environments using local namespaces for parameters internally should, in principle, be able to accept SBML model definitions without needing to change component identifiers. Environments using a global namespace for parameters internally can perform manipulations of the identifiers of local parameter elements within reaction definitions to avoid name collisions.

The namespace rules described here will hopefully provide a clean transition path to future levels of SBML, when submodels are introduced (Section 8.1). Submodels will provide the ability to compose one model from a collection of other models. This capability will have to be built on top of SBML Level 2's namespace organization. A straightforward approach to handling namespaces is to make each submodel's space be private. The rules governing namespaces within a submodel can simply be the Level 2 namespace rule described here, with each submodel having its own (to itself, global) namespace.

3.4.2 The name Field

In contrast to the **id** field, the **name** field is optional and is not intended to be used for cross-referencing purposes within a model. Its purpose instead is to provide a human-readable label for the component. The data type of the **name** field is the type **string** defined in XML Schema (Biron and Malhotra, 2000; Thompson et al., 2000) and discussed further in Section 3.1. SBML imposes no restrictions as to the content of **name** fields beyond those restrictions defined by the **string** type in XML Schema.

The recommended practice for handling **name** is as follows. If a software tool has the capability for displaying the content of **name** fields, it should display this content to the user as a component's label instead of the component's **id** field. If the user interface does not have this capability (e.g., because it cannot display or use special characters in symbol names), or if the **name** field is missing on a given component, then the user interface should display the value of the **id** field instead. (Script language interpreters are especially likely to display **id** fields instead of **name** fields.)

As a consequence of the above, authors of systems that automatically generate the values of **id** fields should be aware some systems may display the **id**'s to the user. Authors therefore may wish to take some care to have their software create **id** values that are reasonably easy for humans to type and read.

An additional point worth mentioning is although there are restrictions on the uniqueness of **id** values (see Section 3.4.1 below), there are no restrictions on the uniqueness of **name** values in a model. This allows software packages leeway in assigning component identifiers.

3.4.3 Identifiers, Names, and SBase

Although many SBML components also feature two other fields named **id** and **name**, these fields are purposefully not defined on *Sbase*. There are several reasons for this.

- The identifier field is optional on some SBML components and required on others. Putting **id** on *Sbase* would make it impossible to accommodate both cases—it would force identifiers to be mandatory on all components.
- The *Sbase* abstract type is used as the base type for certain structures such as Unit, AssignmentRule, AlgebraicRule, etc., which do not have identifiers at all because these structures do not need to be referenced by other structures. If instead *Sbase* had an **id** field, all objects of these other types in a model would then need to be assigned unique identifiers. This would be a needless burden on software developers, given that these objects do not need identifiers.
- The presence of an SBML identifier field (**id**) necessarily requires specifying scoping rules for the corresponding identifiers. However, the *Sbase* abstract type is used as the basis for defining components whose scoping rules are in some cases different from each other. (See Section 3.4.1 for more details). If *Sbase* where to have an **id** field, then the specification of *Sbase* would need a default scoping rule and this would then have to be overloaded on derived classes that needed different scoping. This would make the SBML specification needlessly complex.
- Because *Sbase* is the base type of the **listOf**_____ lists (see Section 3.2), putting **id** on *Sbase* would require all of these lists in a model to be given identifers. This would again be pointless because these lists are only syntactic constructs; they cannot carry a value or be referenced by the rest of an SBML model.
- Because the Sbml top-level object is derived from *Sbase*, it too would have to be assigned a mandatory identifier. Again, there is no functional reason to have an identifier on this object (it is outside the model!). With respect to the **name** field, *Sbase* does not have a **name** simply because such a field is paired with an **id** field.

3.5 Mathematical Formulas in SBML Level 2

Mathematical expressions in SBML Level 2 are represented using MathML 2.0 (W3C, 2000b), the XML standard for describing mathematics in machine-readable format. It is used in the definitions of functions

(Section 4.3), rules (Section 4.11), initial assignments (Section 4.10), constraints (Section 4.12), reaction kinetics (Section 4.13.9), stoichiometries (Section 4.13.7) and events (Section 4.14). The FunctionDefinition, KineticLaw, StoichiometryMath, EventAssignment, InitialAssignment, Constraint, and *Rule* structures each have a single MathML `math` subelement. The Event structure has two `math` elements, one inside a subelement named `trigger` and the other inside a subelement named `delay`. The FunctionDefinition's single `math` element is limited to containing only a single MathML `lambda` element.

The XML namespace URI for all MathML elements is `http://www.w3.org/1998/Math/MathML`. [See the W3C document by Bray et al. (1999) for more information about using XML namespaces.] The examples throughout this specification illustrate the use of this namespace and MathML in SBML.

The semantic interpretation of MathML in the context of SBML follows the MathML 2.0 standard. In particular, the semantics of MathML functions follow the definitions laid out by Abramowitz and Stegun (1977) and Zwillinger (1996). Readers are directed to these sources and the MathML specification for information about such things as which principle values of the inverse trigonometric functions to use.

3.5.1 Subset of MathML Used in SBML Level 2

The subset of MathML 2.0 elements used in SBML Level 2 is similar to that used by CellML (Hedley et al., 2001), another model definition language with similar goals as SBML. The MathML elements permitted in SBML are itemized below:

- *token*: `cn`, `ci`, `csymbol`, `sep`
- *basic content*: `apply`, `piecewise`, `piece`, `otherwise`
- *relational operators*: `eq`, `neq`, `gt`, `lt`, `geq`, `leq`
- *arithmetic operators*: `plus`, `minus`, `times`, `divide`, `power`, `root`, `abs`, `exp`, `ln`, `log`, `floor`, `ceiling`, `factorial`
- *logical operators*: `and`, `or`, `xor`, `not`
- *qualifiers*: `degree`, `bvar`, `logbase`
- *trigonometric operators*: `sin`, `cos`, `tan`, `sec`, `csc`, `cot`, `sinh`, `cosh`, `tanh`, `sech`, `csch`, `coth`, `arcsin`, `arccos`, `arctan`, `arcsec`, `arccsc`, `arccot`, `arcsinh`, `arccosh`, `arctanh`, `arcsech`, `arccsch`, `arccoth`
- *constants*: `true`, `false`, `notanumber`, `pi`, `infinity`, `exponentiale`
- *annotation*: `semantics`, `annotation`, `annotation-xml`

The inclusion of logical operators, relational operators, `piecewise`, `piece`, and `otherwise` elements facilitates the encoding of discontinuous expressions. Elements for representing partial differential calculus are not included. We anticipate that the requirements for partial differential calculus will be addressed in proposals for SBML Level 3 geometry representations (see Section 8.1).

Parsers should take particular note of the MathML semantics of the N-ary operators `plus`, `times`, `and`, `or` and `xor`, when they are used with different numbers of arguments. The MathML specification (W3C, 2000b) appendix C.2.3 describes the semantics for these operators with zero, one, and more arguments.

The following are the only attributes permitted on MathML elements in SBML:

- `style`, `class` and `id` on any element;
- `encoding` and `definitionURL` on `csymbol` elements; and
- `type` on `cn` elements.

Missing values for these attributes are to be treated in the same way as defined by MathML. These restrictions on attributes are designed to confine the MathML elements to their default semantics and to avoid conflicts in the interpretation of the type of token elements.

3.5.2 Handling of Whitespace

MathML 2.0 defines "whitespace" in the same way as XML does, i.e., the space character (Unicode hexadecimal code 0020), horizontal tab (code 0009), newline or line feed (code 000A), and carriage return (code 000D). In MathML, the content of elements such as `cn` and `ci` (described below) can be surrounded by whitespace characters. Prior to using the content, this whitespace is "trimmed" from both ends: all whitespace at the beginning and end of the content is removed Ausbrooks et al. (2003).

For example, in a MathML element `<cn> 42 </cn>`, the amount of white space on either side of the "`42`" inside the `<cn>` ... `</cn>` container does not matter. Prior to interpreting the content, the whitespace is removed altogether.

3.5.3 Use of cn Elements in MathML Expressions in SBML

The content of a `cn` element must be a number. The number can be preceded and succeeded by whitespace.

The following are the only permissible values for the `type` attribute on MathML `cn` elements: "`e-notation`", "`real`", "`integer`", and "`rational`". The value of the `type` attribute defaults to "`real`".

The values of the content of `cn` elements do not necessarily conform to any specific floating point or integer representations designed for CPU implementation. For example the value of a `cn` element may exceed the maximum value that can be stored in a IEEE 64 bit floating point number (IEEE 754). This is different from the XML Schema type `double` that is used in the definition floating point fields of structures in the SBML namespace which *is* restricted to IEEE double-precision 64-bit floating point type IEEE 754-1985. (Integer fields in the SBML namespace are only restricted by sign in some cases. The absolute size of field integer values is not restricted.)

It is important to note that MathML uses a style of scientific notation that differs from what is defined in XML Schema. The MathML 2.0 "`e-notation`" requires the mantissa and exponent to be separated by one `<sep/>` element. The mantissa must be a real number and the exponent part must be a signed integer. This leads to expressions such as

```
<cn type="e-notation"> 2 <sep/> -5 </cn>
```

for the number 2×10^{-5}. It is especially important to note that the expression

```
<cn type="e-notation"> 2e-5 </cn>
```

is *not valid* in MathML 2.0. In the SBML XML namespace, when an attribute value is declared to have type `double` (a type taken from XML Schema), the compact notation "`2e-5`" is in fact allowed, but not inside the MathML XML namespace. (This is a regrettable difference between two standards that SBML replies upon, but it is not feasible to redefine these types within SBML because the result would be incompatible with parser libraries written to conform with the MathML and XML Schema standards. It is also not possible to use XML Schema to define a data type for SBML attribute values permitting the use of the `<sep/>` notation, because XML attribute values cannot contain XML elements: `<sep/>` cannot appear in an XML attribute value.)

3.5.4 Use of ci Elements in MathML Expressions in SBML

The content of a `ci` element must be an SBML identifier that is declared elsewhere in the model. The identifier can be preceded and succeeded by whitespace. The set of possible identifiers that can appear in a `ci` element depends on the containing structure in which the `ci` is used:

- If a `ci` element appears in the body of a function definition (Section 4.3), the referenced identifier must be either (i) one of the declared arguments to that function, or (ii) the identifier of a previously defined function.
- In all other situations, the referenced identifier must be the identifier of a species, compartment, parameter, function or reaction declared in the model. The following are the only possible interpretations of using such an identifier in SBML:

- *Species identifier*: When a species identifier occurs in a `ci` element, it represents the quantity (*amount of substance* or *concentration*) of that species. The units associated with a species identifier are *the units of the species*, defined in Section 4.8.5.
- *Compartment identifier*: When a compartment identifier occurs in a `ci` element, it represents the size of the compartment. The units associated with the size of the compartment are those given on the Compartment structure that declares the identifier; see Section 4.7.5.
- *Parameter identifier*: When a parameter identifier occurs in a `ci` element, it represents the numerical value assigned to that parameter. The units associated with the parameter value are the units assigned in its instance of a Parameter structure; see Section 4.9.3.
- *Function identifier*: When a function identifier occurs in a `ci` element, it represents a call to that function. Function references in MathML occur in the context of using MathML's `apply` and often involve supplying arguments to the function; see Section 4.3.
- *Reaction identifier*: When a reaction identifier occurs in a `ci` element, it represents the rate of the reaction, which is given by the kinetic law of the reaction if present. The units associated with the reaction value are the units assigned to the KineticLaw structure contained within the Reaction structure; see Section 4.13.9. (The units of the reaction identifier follow the defaults described in Section 4.13.9 when the KineticLaw structure is not present.)

The content of `ci` elements outside a KineticLaw and FunctionDefinition structures always refer to objects declared in the top level global namespace; i.e., SBML uses "early binding" semantics. The only `ci` elements that can represent parameters listed in a KineticLaw structure are those `ci` elements contained in the KineticLaw structure (see Section 4.13.9).

3.5.5 Use of `csymbol` Elements in MathML Expressions in SBML

SBML Level 2 uses the MathML `csymbol` element to denote certain built-in mathematical entities without introducing reserved names into the component identifier namespace. The `encoding` field of `csymbol` should be set to "`text`". The `definitionURL` should be set to one of the following predefined SBML symbol URIs:

- `http://www.sbml.org/sbml/symbols/time`. This represents the current simulation time. The units of the current time entity are determined from the built-in `time` of Table 3 on page 31.
- `http://www.sbml.org/sbml/symbols/delay`. This represents a delay function. The delay function has the form $delay(x, d)$, taking two MathML expressions as arguments. Its value is the value of argument x at d time units before the current time. There are no restrictions on the form of x. The units of the d parameter are determined from the built-in `time`. The value of the d parameter, when evaluated, must be numerical and be greater than or equal to 0. The `delay` function is useful for representing biological processes having a delayed response, but where the detail of the processes and delay mechanism is not relevant to the operation of a given model.

The following examples demonstrate these concepts. The XML fragment below encodes the formula $x + t$, where t stands for time.

```
<math xmlns="http://www.w3.org/1998/Math/MathML">
    <apply>
        <plus/>
        <ci> x </ci>
        <csymbol encoding="text" definitionURL="http://www.sbml.org/sbml/symbols/time">
            t
        </csymbol>
    </apply>
</math>
```

In the fragment above, the use of the token `t` is mostly a convenience for human readers—the string inside the `csymbol` could have been almost anything, because it is essentially ignored by MathML parsers and SBML. Some MathML and SBML processors will take note of the token and use it when presenting the

mathematical formula to users, but the token used has no impact on the interpretation of the model and it does not enter into the SBML component identifier namespace. In other words, the content of the `csymbol` element is for rendering purposes only and can be ignored by the parser.

As a further example, the following XML fragment encodes the equation $k + delay(x, 0.1)$ or alternatively $k_t + x_{t-0.1}$:

```
<math xmlns="http://www.w3.org/1998/Math/MathML">
    <apply>
        <plus/>
        <ci> k </ci>
        <apply>
            <csymbol encoding="text" definitionURL="http://www.sbml.org/sbml/symbols/delay">
                delay
            </csymbol>
            <ci> x </ci>
            <cn> 0.1 </cn>
        </apply>
    </apply>
</math>
```

Note that the URI in the value of "`definitionURL`", as all URIs, are intended to serve as unique identifiers and are not intended to be dereferenced as Internet addresses.

3.5.6 Math Expression Types

MathML operators in SBML each return results in one of two possible types: boolean and numeric. The following guidelines summarize the different possible cases.

The relational operators (`eq`, `neq`, `gt`, `lt`, `geq`, `leq`), the logical operators (`and`, `or`, `xor`, `not`), and the boolean constants (`false`, `true`) always return boolean values.

The type of an operator referring to an SBML FunctionDefinition is determined by the type of the top-level operator of the MathML expression in the `math` field of the function definition. This type may be boolean or numeric.

All other operators, values and symbols return numeric results.

The roots of the expression trees used in the following contexts must yield boolean values:

- the arguments of the MathML logical operators (`and`, `or`, `xor`, `not`);
- the second argument of a MathML `piece` operator;
- the `trigger` field of an SBML Event structure; and
- the `math` field of an SBML Constraint structure.

The roots of the expression trees used in the following contexts can optionally yield boolean values:

- the arguments to the `eq` and `neq` operators;
- the first arguments of MathML `piece` and `otherwise` operators; and
- the top level expression of a function definition.

The roots of expression trees in other contexts must yield numeric values.

The type of expressions should be used consistently. The set of expressions that make up the first arguments of the `piece` and `otherwise` operators within the same `piecewise` operator should all return values of the same type. The arguments of the `eq` and `neq` operators should return the same type.

4 SBML Components

In this section, we define each of the major data structures in SBML. To provide illustrations of their use, we give partial model definitions in XML. Section 7 provides many full examples of SBML in XML.

In type definitions presented throughout this section section, we follow the UML convention of hiding the attributes derived from a parent type such as *Sbase*. It should be kept in mind that these attributes are always available.

4.1 The SBML Container

The outermost portion of an SBML Level 2 model definition consists of a single Sbml structure enclosing a single Model structure (see next Section). The definition of Sbml is shown in Figure 6.

Sbml
level: positiveInteger { use="required" fixed="2" } version: positiveInteger { use="required" fixed="2" }

Figure 6: *The definition of Sbml for SBML Level 2 Version 2. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

The XML namespace URI for SBML Level 2 Version 2 is `http://www.sbml.org/sbml/level2/version2`. All SBML Level 2 Version 2 elements should be encoded using this URI by assigning it to either the default XML namespace or a tag prefix. The character encoding for SBML is UTF-8. SBML documents should include the `encoding` attribute with the value `UTF-8` in the XML prologue.

In the transformation of UML to XML used in this document, the Sbml structure is turned into an element named `sbml`. The element has two required attributes: `level` and `version`. For SBML Level 2 Version 2, these attributes must be set to "2" and "2", respectively.

The following is an abbreviated example of the outermost content of an SBML model definition in XML:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
  ...
</sbml>
```

Readers may wonder why the SBML top-level XML element uses both a namespace URI identifying the SBML level and version, as well as separate XML attributes encoding the level and version. Why is the information duplicated? There are several reasons. First, XML is only one possible serialization of SBML (albeit an extremely popular one at this time). Though most of this document is written with XML in mind, it is the intention behind the design of SBML that its object structure should be implementable in other languages and software systems. Programmatic access is easier if the level and version information are accessible directly as data rather than have to be extracted from a string. Second, generic high-level XML parsers may give their calling programs access to the value of the `xmlns` attribute. Providing the information via separate attributes is a good backup measure. And finally, earlier in the history of SBML, it was expected that only the level needed to be encoded as part of the namespace URI (e.g., `http://www.sbml.org/sbml/level1`) because it was hoped that changes within levels would not require XML Schema changes. This has proven to be false, but SBML Level 1 (both versions) and the first version of SBML Level 2 still subscribe to this principle. This means that for these variants of SBML, software tools must look for a `version` attribute on the top-level element. For backwards compatibility with software that expects this, it makes more sense to keep the version and level attributes.

4.2 Models

The Model structure is the highest-level construct in an SBML data stream or document. Its definition is shown in Figure 7 on the following page. Only one component of type Model is allowed per instance of an

SBML Level 2 Version 2 document or data stream, although it does not necessarily need to represent a single biological entity.

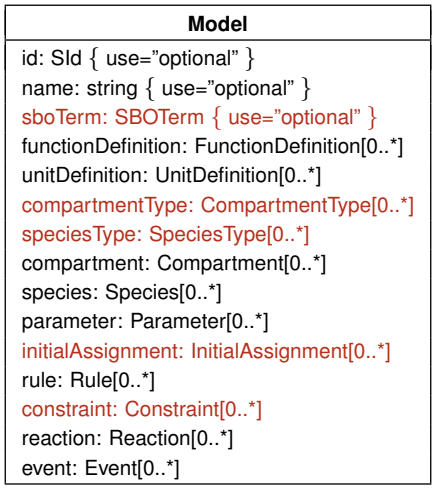

Figure 7: *The definition of Model. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

Model serves as a container for components of object classes FunctionDefinition, UnitDefinition, CompartmentType, SpeciesType, Compartment, Species, Parameter, InitialAssignment, *Rule*, Constraint, Reaction and Event. All of these components are optional; that is, the lists in each of the respective fields are permitted to have zero length. (However, there are dependencies between components, such that defining some requires defining others. For example, as explained in other sections below, defining a species requires defining a compartment, and defining a reaction requires defining a species.)

The Model structure has an optional field, `id`, used to give the model an identifier. The identifier must be a text string conforming to the syntax permitted by the `SId` data type described in Section 3.1.7. Model also has an optional `name` field, of type `string`. The `name` and `id` fields must be used as described in Section 3.4.

In the XML encoding of an SBML model, the lists of compartment types, compartments, species types, species, unit definitions, parameters, initial assignments, reactions, function definitions, constraints, rules and events are translated into lists of XML elements enclosed within elements of the form `listOf_____s`, where the blank is replaced by the name of the component type. If the word already ends in "s", such as "species", then the extra letter is omitted from the end, leading to `listOfSpecies`. The resulting XML data object has the form illustrated by the following skeletal model:

```
<model id="My_Model">
    <listOfFunctionDefinitions>
        ...
    </listOfFunctionDefintions>
    <listOfUnitDefinitions>
        ...
    </listOfUnitDefinitions>
    <listOfCompartmentTypes>
        ...
    </listOfCompartmentTypes>
    <listOfSpeciesTypes>
        ...
    </listOfSpeciesTypes>
    <listOfCompartments>
        ...
    </listOfCompartments>
    <listOfSpecies>
        ...
    </listOfSpecies>
```

```
        <listOfParameters>
            ...
        </listOfParameters>
        <listOfInitialAssignments>
            ...
        </listOfInitialAssignments>
        <listOfRules>
            ...
        </listOfRules>
        <listOfConstraints>
            ...
        </listOfConstraints>
        <listOfReactions>
            ...
        </listOfReactions>
        <listOfEvents>
            ...
        </listOfEvents>
    </model>
```

Readers may wonder about the motivations for the `listOf_____s` notation. A simpler approach to creating the lists of components would be to place them all directly at the top level under `<model> ... </model>`. We chose instead to group them within XML elements named after `listOf_____s`, because we believe this helps organize the components and makes visual reading of model definitions easier. These `listOf_____s` elements are derived from *Sbase* which enables each list to contain its own `metaid`, `notes` and `annotation` fields. Further details of how `listOf_____s` elements implement UML lists is described in Section 1.6.

4.2.1 The sboTerm Field

The Model structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). When a value is given to this field in a model, the value must be an SBO (`http://www.biomodels.net/SBO/`) identifier referring to a modeling framework defined in SBO (i.e., terms derived from `SBO:0000004`, "modeling framework"). The SBO term chosen should be the most precise (narrow) term that defines the mathematical framework assumed by the *entire* model. An example framework might be "discrete stochastic", which would mean the *entire* model was created under the assumption it will be simulated in a tool that turns substance quantities into discrete numbers and applies a stochastic stimulation algorithm (e.g., Gillespie, 1977) to the model. Other frameworks are possible.

The value given to `sboTerm` on a Model interacts with the SBO labels on the model's Reaction elements in the following way. The label on Model should apply to the model as a whole, meaning that *all* reactions in the model assume the same framework. In that case, the `sboTerm` values on individual Reaction elements may be omitted, but only the Reaction SBO labels can be thus omitted; the SBO labels on KineticLaw within Reaction must still be supplied, as must the terms on other components of the model, in order to characterize the model completely.

The absence of a `sboTerm` value means that either the model has not been labeled with SBO terms at all, or there was no available SBO modeling framework term at the time the model was created that was deemed suitable for characterizing the model as a whole. If Model has no value for `sboTerm`, the `sboTerm` fields on each Reaction in a model may still indicate the framework assumed for each reaction separately.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values, and a model must be interpretable without the benefit of SBO labels.

4.3 Function Definitions

The FunctionDefinition structure associates an identifier with a function definition. This identifier can then be used as the function called in subsequent MathML `apply` elements. FunctionDefinition is shown in Figure 8.

Function definitions in SBML (also informally known as "user-defined functions") have relatively limited capabilities. As is made more clear below, a function cannot reference parameters or other model quantities outside of itself; values must be passed as parameters to the function. Moreover, recursive and mutually-

FunctionDefinition
id: SId
name: string { use="optional" }
math: (lambda:Lambda) { namespace="http://www.w3.org/1998/Math/MathML" }

Figure 8: *The definition of FunctionDefinition. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

recursive functions are not permitted. The purpose of these limitations is to balance power against complexity of implementation. With the restrictions as they are, function definitions could be implemented as textual substitutions—they are simply macros. Software implementations may therefore not need the full function-definition machinery typically associated with programming languages.

The FunctionDefinition structure has three fields: `id`, `name` and `math`. Their purposes are explained in the following subsections.

4.3.1 The `id` and `name` Fields

The `id` and `name` fields have types `SId` and `string`, respectively, and operate in the manner described in Section 3.4. MathML `ci` elements in an SBML model can refer to the function defined by a FunctionDefinition using the value of its `id` field.

4.3.2 The `math` Field

The `math` field is a container for MathML content that defines the function. The content of this field can only be a MathML `lambda` element. The `lambda` element must begin with zero or more `bvar` elements, followed by any other of the elements in the MathML subset listed in Section 3.5.1 *except* `lambda` (i.e., a `lambda` element cannot contain another `lambda` element). This is the only place in SBML where a `lambda` element can be used. The function defined by a FunctionDefinition is only available for use in other MathML elements that *follow* the FunctionDefinition definition in the model. (These restrictions prevent recursive and mutually-recursive functions from being expressed.)

A further restriction on the content of the `math` field is that it cannot contain references to variables other than the variables declared to the `lambda` itself. That is, the contents of MathML `ci` elements inside the body of the `lambda` can only be the variables declared by its `bvar` elements, or the identifiers of other FunctionDefinitions defined earlier in the model. This implies that functions must be written so that all variables or parameters they may need are passed to them via their function parameters.

4.3.3 Examples

The following abbreviated SBML example shows a FunctionDefinition structure defining `pow3` as the name of a function computing the mathematical expression x^3, and after that, the invocation of that function in the mathematical formula of a rate law. Note how the invocation of the function uses its identifier

```
<model>
    ...
    <functionDefinition id="pow3">
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <lambda>
                <bvar><ci> x </ci></bvar>
                <apply>
                    <power/>
                    <ci> x </ci>
                    <cn> 3 </cn>
                </apply>
            </lambda>
        </math>
    </functionDefinition>
    ...
    <listOfReactions>
```

```
            <reaction id="reaction_1">
                ...
                <kineticLaw>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <ci> pow3 </ci>
                            <ci> S1 </ci>
                         </apply>
                    </math>
                </kineticLaw>
                ...
            </reaction>
        </listOfReactions>
        ...
    </model>
```

4.4 Unit Definitions

Units of measurement may be supplied in a number of contexts in an SBML model. The units of the following mathematical entities can be specified explicitly: the size of a compartment, the initial amount of a species, the units of constant and variable parameter values, the units of time and of substance in which a reaction rate is expressed, the units of time in an event's execution delay, and the results of mathematical formulas. Rather than requiring a complete unit definition on every structure, SBML provides a facility for defining named units that can be referenced throughout a model. In addition, every kind of SBML mathematical entity has units assigned to it from a set of built-in defaults (see Section 4.4.3 below, and also Sections 4.7.5, 4.8.5 and 4.13.9). By redefining these built-in default units, it is possible to change the units used throughout a model in a simple and consistent manner.

The SBML unit definition facility uses two classes of objects, UnitDefinition and Unit. Their definitions are shown in Figure 9 and explained in more detail in Sections 4.4.1 and 4.4.2 below.

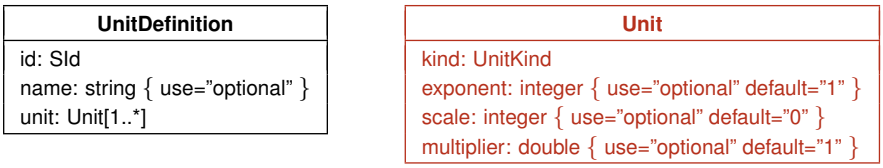

Figure 9: *The definition of UnitDefinition and Unit. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

The approach to defining units in SBML is compositional; for example, $meter\ second^{-2}$ is constructed by combining a Unit object representing $meter$ with another Unit object representing $second^{-2}$. The combination is wrapped inside a UnitDefinition, which provides for assigning an identifier and optional name to the combination. The identifier can then be referenced from elsewhere in a model.

The vast majority of modeling situations requiring new SBML unit definitions involve simple multiplicative combinations of base units and factors. An example of this might be "moles per litre per second". What distinguishes these sorts of simpler unit definitions from more complex ones is that they may be expressed without the use of an additive offset from a zero point. The use of offsets complicates all unit definition system, yet in the domain of SBML the real-life cases requiring offsets are few (and in fact, to the best of our knowledge, only involve temperature). Consequently, the SBML unit system has been consciously designed in a way that attempts to simplify implementation of unit support for the most common cases in systems biology, at the cost of an asymmetry in unit calculations introduced when offsets are used.

4.4.1 The UnitDefinition Structure

A unit definition in SBML consists of an instance of a UnitDefinition object, shown in Figure 9.

The `id` and `name` Fields

The `id` and `name` fields have types `SId` and `string`, respectively, and operate in the manner summarized in Section 3.4. There are three crucial differences between unit identifiers and most other identifiers in SBML:

1. The `id` of a Unit definition must not contain a value from Table 2 (i.e., the enumeration of predefined `UnitKind` values). This constraint simply prevents the redefinition of the base units.

2. Unit identifiers defined by the `id` field reside in a separate global namespace distinct from the namespace of other identifiers in a model; thus, unit identifiers cannot collide with the identifiers of species, compartments, reactions, etc.

3. There is a set of predefined identifiers for the built-in default units in SBML; these identifiers are "`substance`", "`volume`", "`area`", "`length`", and "`time`". Using one of these values for `id` in a UnitDefinition has the effect of redefining the model-wide default units for the corresponding quantities. We discuss this in more detail in Section 4.4.3.

The List of Units

A UnitDefinition object must contain one or more Unit objects within the `unit` container. In the XML form of SBML, this container becomes a `listOfUnits` element. Section 4.4.2 explains the meaning and use of Unit.

Example

The following skeleton of a unit definition illustrates an example use of UnitDefinition:

```
<listOfUnitDefinitions>
    <unitDefinition id="unit1">
        ...
    </unitDefinition>
    <unitDefinition id="unit2">
        ...
    </unitDefinition>
</listOfUnitDefinitions>
```

4.4.2 The Unit Structure

A Unit structure represents a (possibly transformed) reference to a base unit chosen from `UnitKind` (Table 2). The field `kind` indicates the chosen base unit, whereas the three fields `exponent`, `scale`, and `multiplier` define how the base unit is being transformed. These various fields are described in detail below.

Compatibility note: in SBML Level 2 Version 1, UnitDefinition had an additional field called `offset`. This field has been removed entirely from SBML Level 2 Version 2. Modelers and software authors are instead directed to use other methods of encoding units requiring offsets. The reasons for this change, and some suggestions for how to achieve equivalent effects of unit offsets, are discussed in more detail below.

The `kind` Field

The Unit data structure has one required field, `kind`, whose value must be taken from `UnitKind`, an enumeration of base units. The possible values of `UnitKind` are given in Table 2 on the following page.

Note that the set of acceptable values for the field `kind` does *not* include units defined by UnitDefinition structures. This means that the units definition system in SBML is not hierarchial: user-defined units cannot be built on top of other user-defined units, only on top of base units. SBML differs from CellML Hedley et al. (2001) in this respect; CellML allows the construction of hierarchial unit definitions.

The `exponent`, `scale` and `multiplier` Fields

The optional `exponent` field on Unit represents an exponent on the unit. Its default value is "`1`" (one). A Unit structure also has an optional `scale` field; its value must be an integer exponent for a power-of-ten multiplier used to set the scale of the unit. For example, a unit having a `kind` value of "`gram`" and a `scale` value of

ampere	farad	joule	lux	radian	volt
becquerel	gram	katal	metre	second	watt
candela	gray	kelvin	mole	siemens	weber
Celsius	henry	kilogram	newton	sievert	
coulomb	hertz	litre	ohm	steradian	
dimensionless	item	lumen	pascal	tesla	

Table 2: *The possible values of* `kind` *in a* `UnitKind` *structure. All are names of base or derived SI units (Bureau International des Poids et Mesures, 2000), except for "*`dimensionless`*" and "*`item`*", which are SBML additions important for handling certain common situations. "*`Dimensionless`*" is intended for cases where a quantity does not have units, and "*`item`*" for expressing such things as "N items" (e.g., "100 molecules"). Also, note that the gram and litre are not strictly part of SI; however, they are so commonly used in SBML's areas of application that they are included as predefined unit names. (The standard SI unit of mass is in fact the kilogram, and volume is defined in terms of cubic metres.)*

"-3" signifies $10^{-3} * gram$, or milligrams. The default value of **scale** is "0" (zero), because $10^0 = 1$. Lastly, the optional **multiplier** field can be used to multiply the **kind** unit by a real-numbered factor; this enables the definition of units that are not power-of-ten multiples of SI units. For instance, a **multiplier** of 0.3048 could be used to define "**foot**" as a measure of length in terms of a metre. The **multiplier** field has a default value of "1" (one).

The unit system allows model quantities to be expressed in units other than the base units of Table 2. For analyses and computations, the consumer of the model (be it a software tool or a human) will want to convert all model quantities to base SI units for purposes such as verifying the consistency of units throughout the model. Suppose we begin with a quantity having numerical value y when expressed in units $\{u\}$. The relationship between y and a quantity y_b expressed in base units $\{u_b\}$ is

$$y_b\,\{u_b\} = y\,\{u\}\left(\frac{w\,\{u_b\}}{\{u\}}\right) \tag{1}$$

The term in the parentheses on the right-hand side is a factor for converting a quantity in units $\{u\}$ to another quantity in units $\{u_b\}$. The ratio of units leads to canceling of $\{u\}$ in the equation above and leaves a quantity in units $\{u_b\}$. It remains to define this factor. In terms of the SBML unit system, it is:

$$\{u\} = (\texttt{multiplier} \cdot 10^{\texttt{scale}}\,\{u_b\})^{\texttt{exponent}} \tag{2}$$

where the dot $(\cdot)$ represents simple scalar multiplication. The variables **multiplier**, **scale**, and **exponent** in the equation above correspond to the fields with the same names in the Unit structure defined in Figure 9. The exponent in the equation above may make it more difficult to grasp the relationship immediately; so let us suppose for the moment that **exponent**="1". Then, it is easy to see that

$$\{u\} = \texttt{multiplier} \cdot 10^{\texttt{scale}}\,\{u_b\}$$

Dividing both sides by $\{u\}$ produces the ratio in the parenthesized portion of Equation 1, which means that $w = \texttt{multiplier} \cdot 10^{\texttt{scale}}$. To take a concrete example, one foot expressed in terms of the metre (a base unit) requires **multiplier**="0.3048", **exponent**="1", and **scale**="0":

$$\text{foot} = 0.3048 \cdot 10^0 \cdot \text{metre}$$

leading to a conversion between quantities of

$$y_b\,\text{metres} = 0.3048 \cdot y\,\text{feet}$$

Given a quantity of, say, $y = 2$, the conversion results in $y_b = 0.6096$. To relate this to SBML terms more concretely, the following fragment of SBML illustrates how this is represented using the Unit and UnitDefinition constructs:

```
<listOfUnitDefinitions>
    <unitDefinition id="foot">
        <listOfUnits>
            <unit kind="metre" multiplier="0.3048"/>
        </listOfUnits>
    </unitDefinition>
</listOfUnitDefinitions>
```

The case above is the simplest possible situation, involving the transformation of quantities from a single defined unit $\{u\}$ into a quantity expressed in a single base unit $\{u_b\}$. If, instead, multiple base units $\{u_{b_1}\}, \{u_{b_2}\}, \ldots, \{u_{b_n}\}$ are involved, the following equation holds (where the m_i terms are the `multiplier` values, the s_i terms are the `scale` values, and the x_i terms are the `exponent` values):

$$\begin{aligned}\{u\} &= (m_1 \cdot 10^{s_1}\{u_{b_1}\})^{x_1} \cdot (m_2 \cdot 10^{s_2}\{u_{b_2}\})^{x_2} \cdot \ldots \cdot (m_n \cdot 10^{s_n}\{u_{b_n}\})^{x_n} \\ &= m_1^{x_1} \cdot m_2^{x_2} \cdot \ldots \cdot m_n^{x_n} \cdot 10^{(s_1x_1+s_2x_2+\ldots+s_nx_n)}\{u_{b_1}\}^{x_1}\{u_{b_2}\}^{x_2}\ldots\{u_{b_n}\}^{x_n} \end{aligned} \quad (3)$$

Software developers should take care to track the exponents carefully because they can be negative integers. The overall use of Equation 3 is analogous to that of Equation 2, and leads to the following final expression. First, to simplify, let

$$\begin{aligned} m &= m_1^{x_1} \cdot m_2^{x_2} \cdot \ldots \cdot m_n^{x_n} \\ p &= s_1x_1 + s_2x_2 + \ldots + s_nx_n \end{aligned}$$

then,

$$y_b\,\{u_{b_1}\}\{u_{b_2}\}\ldots\{u_{b_n}\} = y\,\{u\}\left(\frac{m \cdot 10^p\{u_{b_1}\}^{x_1}\{u_{b_2}\}^{x_2}\ldots\{u_{b_n}\}^{x_n}}{\{u\}}\right) \quad (4)$$

Some additional points are worth discussing about the unit scheme introduced so far. First, and most importantly, the equations above are formulated with the assumption that the base units do not require an additive offset as part of their definition. *When temperature values in units other than kelvin are being considered, then a different interpretation must be made*, as discussed below.

A second point, related to the first, is that care is needed to avoid seemingly-obvious but incorrect translations of units described in textbooks. The scheme above makes it easy to formulate statements such as "1 foot = 0.3048 metres" in the most natural way. However, the most common expression of the relationship between Fahrenheit and Celsius temperatures, "(T in Fahrenheit) = 1.8 · (T in Celsius) + 32" might lead one to believe that defining Fahrenheit degrees in terms of Celsius degrees involves using `multiplier`="`1.8`". *Not so*, when degree changes are being considered and not temperature values. Converting *temperature values* is different from expressing a relationship between degree measurements. The proper value for the multiplier in the latter case is 5/9, i.e., `multiplier`="`0.555556`" (where we picked an arbitrary decimal precision). If, on the other hand, the actual temperature is relevant to a quantity (e.g., if a model uses a quantity that has particular values at particular temperatures), then offsets must be included in unit calculations as described below.

Handling Units Requiring the Use of Offsets in SBML Level 2 Version 2

Unit definitions and conversions requiring offsets cannot be done using the simple approach above. The most general case, involving offsets, multipliers and exponents, requires a completely different approach to defining units than what has been presented up to this point.

In previous versions of SBML, not only was the general case incorrectly presented (i.e., in the same terms described above, when in reality a different approach is required), but few if any developers even attempted to support offset-based units in their software. In the development of SBML Level 2 Version 2, a consensus among SBML developers has emerged that a fully generalized unit scheme is so confusing and complicated that it actually impedes interoperability. Level 2 Version 2 acknowledges this reality by reducing and simplifying the unit system, specifically by removing the `offset` field on UnitDefinition and describing recommended

approaches for handling Celsius and other temperature units. This is a backwards-incompatible change relative to SBML Level 2 Version 1 and SBML Level 1 Version 2, but it is believed to have limited real-life impact because so few tools and models appeared to have employed this feature anyway. By simplifying the unit system to the point that it only involves multiplicative factors as described above, we expect that more software tools will be able to support the SBML unit system from this point forward, ultimately improving interoperability.

We first address the question of how to handle units that *do* require offsets. In the SBML unit system, there are two situations to explore: handling the predefined Celsius unit (which has an implicit offset relative to the base SI unit kelvin), and handling user-defined units that require offsets (e.g., temperature reported in Fahrenheit).

- *Handling Celsius.* A model in which certain quantities are temperatures measured in degrees Celsius can be converted straightforwardly to a model in which those temperatures are in kelvin. A software tool could do this by performing a straightforward substitution using the following formula:

$$T_{kelvin} = T_{Celsius} + 273.15 \tag{5}$$

  In every mathematical formula of the model where a quantity (call it x) in degrees Celsius appears, replace x with $x_k + 273.15$ where x_k is now in kelvin.

  Of course, this transformation only needs to be performed if a tool must convert the model to one using kelvin for some purpose (such as verifying the units consistency of the whole model).

- *Handling other units requiring offsets.* The only known units (other than Celsius) requiring offsets in SBML's domain of common applications are other temperature units such as Fahrenheit. Few modern scientists would employ Fahrenheit degrees; therefore, this is an unusual situation. The complication inherent in converting between degrees Fahrenheit and degrees Celsius or kelvin is that both a multiplier and an offset are required:

$$T_{kelvin} = \frac{T_F + 459.67}{1.8} \tag{6}$$

  One approach to handling this is to use a FunctionDefinition to define a function encapsulating the relationship above, then to substitute a call to this function wherever the original temperature in Fahrenheit appears in the model's mathematical formulas. Here is a candidate definition as an example:

```
<functionDefinition id="Fahrenheit_to_kelvin">
    <math xmlns="http://www.w3.org/1998/Math/MathML">
        <lambda>
            <bvar><ci> temp_in_fahrenheit </ci></bvar>
            <apply>
                <divide/>
                <apply>
                    <plus/>
                    <ci> temp_in_fahrenheit </ci>
                    <cn> 459.67 </cn>
                </apply>
                <cn> 1.8 </cn>
            </apply>
        </lambda>
    </math>
</functionDefinition>
```

  An alternative approach not requiring the use of function definitions is to use an InitialAssignment to compute the conversion from Fahrenheit to (say) kelvin, assign its value to a variable, and then use that variable elsewhere in the model. Still another approach is to rewrite the mathematical formulas of a model to directly incorporate the conversion Equation 6 wherever the quantity appears.

  All of these approaches provide general solutions to the problem of supporting any units requiring offsets in the unit system of SBML Level 2 Version 2. It can be used for other temperature units requiring an offset (e.g., degrees Rankine, degrees Réaumur), although the likelihood of a real-life model requiring such other temperature units seems exceedingly small.

In summary, the removal of `offset` in SBML Level 2 Version 2 does not impede the creation of models using alternative units. If conversions are needed, then converting between temperature in degrees Celsius and thermodynamic temperature can be handled rather easily by the simple substitution described above. For the rarer case of Fahrenheit and other units requiring combinations of multipliers and offsets, users are encouraged to employ the power of FunctionDefinition, InitialAssignment, or other constructs in SBML.

Examples

The following example illustrates the definition of an abbreviation named "`mmls`" for the units $mmol\ l^{-1}\ s^{-1}$:

```
<listOfUnitDefinitions>
    <unitDefinition id="mmls">
        <listOfUnits>
            <unit kind="mole"   scale="-3"/>
            <unit kind="litre"  exponent="-1"/>
            <unit kind="second" exponent="-1"/>
        </listOfUnits>
    </unitDefinition>
</listOfUnitDefinitions>
```

4.4.3 Built-in Units

There are five special unit names in SBML, listed in Table 3, corresponding to the five types of quantities or that play roles in biochemical reactions: substance, volume, area, length and time. All SBML mathematical entities apart from parameters have default units drawn from these predefined values. Table 3 lists the default values; all of the defaults have `multiplier`="`1`" and `scale`="`0`".

Name	Possible Scalable Units	Default Units
`substance`	dimensionless, mole, item	mole
`volume`	dimensionless, litre, cubic metre	litre
`area`	dimensionless, square metre	square metre
`length`	dimensionless, metre	metre
`time`	dimensionless, second	second

Table 3: *SBML's built-in units.*

Redefinition of Built-In Units

Table 3 also lists alternative base units that are allowed as the basis of redefined values. For example, a redefinition of the built-in unit of time must be based on units of seconds. Within certain limits, a model may change the built-in units by reassigning the keywords `substance`, `length`, `area`, `time`, and `volume` in a UnitDefinition. The limitations on redefinitions of base units are the following:

1. The UnitDefinition of a redefined built-in unit can only contain a single Unit object within it.
2. The value of the `unitKind` field in the Unit object must be drawn from one of the values in the second column of the appropriate row of Table 3.
3. The value of the `exponent` field in the Unit object must be "`1`".

4.4.4 References to Units

A field that defines the units for a mathematical entity (e.g., the field `units` on Parameter) can refer to a named unit chosen from among the following:

- A new unit defined in a UnitDefinition as described at the start of Section 4.4;
- The predefined units from Table 2 on page 28; and

- The predefined units defined in Section 4.4.3 and listed in Table 3. (These are "`substance`", "`volume`", "`area`", "`length`", and "`time`".)

Examples

The following example illustrates how to change the built-in units of volume to be millilitres. If this definition appeared in a model, the units of volume on all components that did not explicitly specify different units would be changed to millilitres.

```
<model>
    ...
    <listOfUnitDefinitions>
        <unitDefinition id="volume">
            <listOfUnits>
                <unit kind="litre" scale="-3"/>
            </listOfUnits>
        </unitDefinition>
    </listOfUnitDefinitions>
    ...
</model>
```

Software developers are asked to pay special attention to the units used in an SBML model. Different users and developers sometimes make different assumptions about units, and these assumptions may not correspond to what is defined in SBML. Sections 3.5.4, 4.8.5 and 4.13.9 have particularly important notes about the usage of units in SBML.

4.5 Compartment Types

A *compartment type* in SBML is a grouping construct used to establish a relationship between multiple *compartments* (Section 4.7). A compartment type is represented by the CompartmentType data structure, defined in Figure 10.

Figure 10: *The definition of CompartmentType. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

In SBML Level 2 Version 2, a compartment type only has an identity, and this identity can only be used to indicate that particular compartments belong to this type. This may be useful for conveying a modeling intention, such as when a model contains many similar compartments, either by their biological function or the reactions they carry; without a compartment type construct, it would be impossible in the language of SBML to indicate that all of the compartments share an underlying conceptual relationship because each SBML compartment must be given a unique and separate identity.

Compartment types have no mathematical meaning in SBML Level 2 Version 2—they have no effect on a model's mathematical interpretation. Simulators and other numerical analysis software may ignore CompartmentType structures and references to them in a model.

There is no mechanism in SBML for representing hierarchies of compartment types. One CompartmentType structure cannot be the subtype of another CompartmentType structure; SBML provides no means of defining such relationships.

4.5.1 The `id` and `name` Fields

As with other major structures in SBML, CompartmentType has a mandatory field, `id`, used to give the species type an identifier. The identifier must be a text string conforming to the syntax permitted by the `SId` data type described in Section 3.1.7. CompartmentType also has an optional `name` field, of type `string`. The `name` and `id` fields must be used as described in Section 3.4.

4.5.2 Examples

The following partial SBML example illustrates a compartment type used to relate together many individual compartments in a hypothetical model.

```
<model>
    ...
    <listOfCompartmentTypes>
        <compartmentType id="mitochondria"/>
    </listOfCompartmentTypes>
    <listOfCompartments>
        <compartment id="m1" size="0.013" compartmentType="mitochondria" outside="cell"/>
        <compartment id="m2" size="0.013" compartmentType="mitochondria" outside="cell"/>
        <compartment id="m3" size="0.013" compartmentType="mitochondria" outside="cell"/>
        <compartment id="m4" size="0.013" compartmentType="mitochondria" outside="cell"/>
        <compartment id="cell" size="190.0"/>
    </listOfCompartments>
    ...
</model>
```

4.6 Species Types

The term *species type* refers to reacting entities independent of location. These include simple ions (e.g., protons, calcium), simple molecules (e.g., glucose, ATP), large molecules (e.g., RNA, polysaccharides, and proteins), and others. The SpeciesType data structure is intended to represent these entities. Its definition is shown in Figure 11.

Figure 11: *The definition of SpeciesType. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

SpeciesType structures are included in SBML to enable Species (Section 4.8) of the same type to be related together. It is a conceptual construct; the existence of SpeciesType structures in a model has no effect on the model's numerical interpretation. Except for the requirement for uniqueness of species/species type combinations located in compartments (described in Section 4.8.2), simulators and other numerical analysis software may ignore SpeciesType structures and references to them in a model.

There is no mechanism in SBML for representing hierarchies of species types. One SpeciesType structure cannot be the subtype of another SpeciesType structure; SBML provides no means of defining such relationships.

4.6.1 The `id` and `name` Fields

As with other major structures in SBML, SpeciesType has a mandatory field, `id`, used to give the species type an identifier. The identifier must be a text string conforming to the syntax permitted by the `SId` data type described in Section 3.1.7. SpeciesType also has an optional `name` field, of type `string`. The `name` and `id` fields must be used as described in Section 3.4.

4.6.2 Example

The following XML fragment is an example of two SpeciesType structures embedded in an SBML model.

```
<listOfSpeciesTypes>
    <speciesType id="Glucose"/>
    <speciesType id="Glucose_6_P"/>
</listOfSpeciesTypes>
```

4.7 Compartments

A *compartment* in SBML represents a bounded space in which species are located. Compartments do not necessarily have to correspond to actual structures inside or outside of a cell, although models are often designed that way. The definition of Compartment is shown in Figure 12.

Compartment
id: SId
name: string { use="optional" }
compartmentType: SId { use="optional" }
spatialDimensions: integer { maxInclusive="3" minInclusive="0" use="optional" default="3" }
size: double { use="optional" }
units: SId { use="optional" }
outside: SId { use="optional" }
constant: boolean { use="optional" default="true" }

Figure 12: *The definition of Compartment. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

It is worth pointing out that, although compartments are optional in the overall definition of Model (see Section 4.2), every species in an SBML model must be located in a compartment. This in turn means that if a model declares any species, the model must also declare at least one compartment.

4.7.1 The `id` and `name` Fields

Compartment has one required field, `id`, of type `SId`, to give the compartment a unique identifier by which other parts of an SBML model definition can refer to it. A compartment can also have an optional `name` field of type `string`. Identifiers and names must be used according to the guidelines described in Section 3.4.

4.7.2 The `compartmentType` Field

Each compartment in a model may optionally be designated as belonging to a particular compartment type. The optional field `compartmentType` of type `SId` is used identify the compartment type represented by the Compartment structure. The field's value must be the identifier of an existing CompartmentType structure. If the `compartmentType` field is not present on a particular compartment definition, a unique virtual compartment type is assumed for that compartment, and no other compartment can belong to that compartment type.

The values of `compartmentType` attributes on compartments have no effect on the numerical interpretation of a model. Simulators and other numerical analysis software may ignore `compartmentType` attributes.

4.7.3 The `spatialDimensions` Field

A Compartment structure has an optional field `spatialDimensions`, whose value must be a positive integer indicating the number of spatial dimensions possessed by the compartment. The maximum value is "`3`", meaning a three-dimensional structure (a volume). Other permissible values are "`2`" (for a two-dimensional area), "`1`" (for a one-dimensional curve), and "`0`" (for a point). The default value is "`3`".

4.7.4 The `size` Field

Each compartment has an optional floating-point field named `size`, representing the total size of the compartment. The `size` field enables concentrations of species to be calculated in the absence of geometry information. Note in particular that in SBML Level 2, a missing `size` value does *not* imply that the compartment size is 1. (This is unlike the definition of compartment `volume` in SBML Level 1.)

The `size` field must not be present if the `spatialDimensions` field is has a value of "`0`". This simply follows from the fact that a zero-dimensional object cannot have a size in the ordinary meaning of the word. When the `spatialDimensions` field does not have a value of "`0`", a missing value for `size` for a given compartment

signifies that the value is either unknown, determined by an AssignmentRule or InitialAssignment structure, not required for analysis, or is available from an external data source.

4.7.5 The `units` Field

The units associated with the compartment's `size` value may be explicitly set using the optional field `units`. The value chosen for this field must be either one of the base units from Table 2 on page 28, or the built-in units "`volume`", "`area`", "`length`" or "`dimensionless`", or a new unit defined by a unit definition in the enclosing model. The type of units assigned to the `units` field must also agree with the number of spatial dimensions of the compartment; that is, if the chosen units are not "`dimensionless`", they must be either units of volume if the value of `spatialDimensions` is "`3`", units of area if the value of `spatialDimensions` is "`2`", or units of length if the value of `spatialDimensions` is "`1`". If `spatialDimensions` is "`0`", the units associated with the compartment's `size` can only be "`dimensionless`".

The default units depends on the value of the compartment's `spatialDimensions` field according to the following rule: for spatial dimensions of 3, 2, 1 or 0, the compartment has the default units of `volume`, `area`, `length` and `dimensionless`, respectively. (See Table 3 on page 31 and Table 2 on page 28.)

The units of the compartment size, as defined by the `units` field, are used in the following ways:

- The value of the `units` field is used as the units of the `size` field of the compartment structure (see Section 4.7.4).
- The value of the `units` field is used as the units of the compartment identifier when it appears as a numerical quantity in a mathematical formula expressed in MathML (discussed in Section 3.5.4).
- The value of the `units` field is used as the units of the `math` field provided on AssignmentRule and InitialAssignment structures for setting a compartment's size (see Section 4.11.3).
- In a RateRule structure that sets the rate of change of the compartment's size (Section 4.11.4), the units on the rule's `math` field are those in the compartment's `units` field divided by the default *time* units. (In other words, the units for the rate of change of compartment size are *compartment size*/*time* units.)

4.7.6 The `constant` Field

A Compartment also has an optional boolean field called `constant` that indicates whether the compartment's size stays constant or can vary during a simulation. A value of "`false`" indicates the compartment's size can be determined by rules (see Section 4.11), and the value of the `size` field should be taken as being the initial size of the compartment. The default value for the `constant` field is "`true`" because in the most common modeling scenarios at the time of this writing, compartment sizes remain constant. The `constant` field must default to or be set to "`true`" if the `spatialDimensions` field is 0.

4.7.7 The `outside` Field

The optional field `outside` of type `SId` can be used to express containment relationships between compartments. If present, the value of `outside` for a given compartment must be the `id` field value of another compartment which encloses it, or in other words, the compartment that is "outside" of it. This enables the representation of simple topological relationships between compartments, for those simulation systems that can make use of the information (e.g., for drawing simple diagrams of compartments).

The directed graph formed by representing Compartment structures as vertexes and the `outside` attribute values as edges must be acyclic. If this condition were not imposed, a model could contain a Compartment that was contained inside itself.

Although containment relationships are partly taken into account by the compartmental localization of reactants and products, it is not always possible to determine purely from the reaction equations whether one compartment is meant to be located within another. In the absence of a value for `outside`, compartment definitions in SBML Level 2 do not have any implied spatial relationships between each other. For many

modeling applications, the transfer of substances described by the reactions in a model sufficiently express the relationships between the compartments. (As discussed in Section 8.1, we expect that SBML Level 3 will introduce the ability to define geometries and spatial qualities.)

4.7.8 Examples

The following example illustrates two compartments in an abbreviated SBML example of a model definition:

```
<model>
    ...
    <listOfCompartments>
        <compartment id="cytosol" size="2.5"/>
        <compartment id="mitochondria" size="0.3"/>
    </listOfCompartments>
    ...
</model>
```

The following is an example of using `outside` to model a cell membrane. To express that a compartment named B has a membrane that is modeled as another compartment M, which in turn is located within another compartment A, one would write:

```
<model>
    ...
    <listOfCompartments>
        <compartment id="A"/>
        <compartment id="M" spatialDimensions="2" outside="A"/>
        <compartment id="B" outside="M"/>
    </listOfCompartments>
    ...
</model>
```

4.8 Species

A *species* refers to a pool of reacting entities of a specific *species type* that take part in reactions and are located in a specific *compartment*. The Species data structure is intended to represent these pools. Its definition is shown in Figure 13.

Species
id: SId
name: string { use="optional" }
speciesType: SId { use="optional" }
compartment: SId
initialAmount: double { use="optional" }
inintialConcentration: double { use="optional" }
substanceUnits: SId { use="optional" }
spatialSizeUnits: SId { use="optional" }
hasOnlySubstanceUnits: boolean { use="optional" default="false" }
boundaryCondition: boolean { use="optional" default="false" }
charge: integer { use="optional" } *deprecated*
constant: boolean { use="optional" default="false" }

Figure 13: *The definition of Species. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

Although the exact definition of Species given here has changed from the definition in the specification of SBML Level 2 Version 1 (e.g., through the introduction of species types), the concept represented by Species remains the same.

4.8.1 The id and name Fields

As with other major structures in SBML, Species has a mandatory field, `id`, used to give the species an identifier. The identifier must be a text string conforming to the syntax permitted by the `SId` data type described in Section 3.1.7. Species also has an optional `name` field, of type `string`. The `name` and `id` fields must be used as described in Section 3.4.

4.8.2 The speciesType Field

Each species in a model may optionally be designated as belonging to a particular species type. The optional field `speciesType` of type `SId` is used identify the species type of the chemical entities that make up the pool represented by the Species structure. The field's value must be the identifier of an existing SpeciesType structure. If the `speciesType` field is not present on a particular species definition, it means the pool contains chemical entities of a type unique to that pool; in effect, a virtual species type is assumed for that species, and no other species can belong to that species type.

There can be only one species of a given species type in any given compartment of a model. More specifically, for all Species structures having a value for the `speciesType` field, the pair

(`speciesType` field value, `compartment` field value)

must be unique across the set of all Species structures in a model.

The value of `speciesType` attributes on species have no effect on the numerical interpretation of a model. Simulators and other numerical analysis software may ignore `speciesType` attributes.

4.8.3 The compartment Field

The required field `compartment`, also of type `SId`, is used to identify the compartment in which the species is located. The field's value must be the identifier of an existing Compartment structure. It is important to note that there is no default value for the `compartment` field on Species; every species in an SBML model must be assigned a compartment, and consequently, a model must define at least one compartment if that model contains any species.

4.8.4 The initialAmount and initialConcentration Fields

The optional fields `initialAmount` and `initialConcentration`, both having a data type of `double`, are used to set the initial quantity of the species in the named compartment. These fields are mutually exclusive; i.e., *only one* can have a value on any given instance of a Species structure. Also, `initialConcentration` must not have a value if the species' compartment has a `spatialDimensions` value of "`0`". Missing `initialAmount` or `initialConcentration` values implies that their values are either unknown, set by an AssignmentRule or InitialAssignment structure, not required for analysis, or available from an external data source.

The units of the value in the `initialAmount` field are set by the `substanceUnits` field of the species structure. The units of the value in the `initialConcentration` field are *substance*/*size* units (i.e., *concentration*). The units of *substance* are those defined in the `substanceUnits`, and the *size* units are those given in the `spatialSizeUnits` field as described in the next subsection.

4.8.5 The substanceUnits, spatialSizeUnits and hasOnlySubstanceUnits Fields

The units associated with a species' quantity, referred to as the *units of the species*, are determined via the optional fields `substanceUnits`, `spatialSizeUnits` and `hasOnlySubstanceUnits`.

`hasOnlySubstanceUnits` is a boolean field which defaults to "`false`". The *units of the species* are of the form *substance*/*size* units (i.e., *concentration* units, using a broad definition of concentration) if the compartment's `spatialDimensions` is non-zero and `hasOnlySubstanceUnits` has the value "`false`". The *units of the species* are of the form *substance* if `spatialDimensions` is zero or `hasOnlySubstanceUnits` has the value "`true`". The possible values of *units of the species* are summarized in Table 4. The units of *substance* are those defined in the `substanceUnits`, and the *size* units are those given in the `spatialSizeUnits` field.

value of `hasOnlySubstanceUnits`	*units of the species* when Spatial Dimensions is greater than 0	*units of the species* when Spatial Dimensions is 0
`false` (default)	*substance/size*	*substance*
`true`	*substance*	*substance*

Table 4: *How to interpret the value the `hasOnlySubstanceUnits` field of the Species structure.*

For both `substanceUnits` and `spatialSizeUnits`, the value chosen must be either a base unit from Table 2 on page 28, a built-in unit from Table 3 on page 31, or a new unit defined by a unit definition in the enclosing model. The chosen units for `substanceUnits` must be be `dimensionless`, `mole`, `item`, or units derived from these. The `substanceUnits` field defaults to the the built-in unit "`substance`" shown in Table 3 on page 31.

The type of units assigned to the `spatialSizeUnits` field must agree with the number of spatial dimensions of the species' compartment. Specifically, they must be units of volume or "`dimensionless`" if the value of the compartment's `spatialDimensions` is "`3`"; they must be units of area or "`dimensionless`" if the value of `spatialDimensions` is "`2`"; and they must be units of length or "`dimensionless`" if the value of `spatialDimensions` is "`1`". The `spatialSizeUnits` field must not have a value if `spatialDimensions` on the compartment has a value of "`0`", or if the species' `hasOnlySubstanceUnits` field has a value of "`true`". The default value of the `spatialSizeUnits` is the value of the `units` field of the species' compartment.

The *units of the species* are used in the following ways:

- The species identifier has these units when it appears as a numerical quantity in a mathematical formula expressed in MathML (discussed in Section 3.5.4).
- The `math` field of AssignmentRule and InitialAssignment structures determining the species' quantity (see Section 4.11.3) has these units.
- In RateRule structures that set the rate of change of the species' quantity (Section 4.11.4), the units on the rule's `math` field are the *units of the species* divided by the built-in *time* units.

4.8.6 The `constant` and `boundaryCondition` Fields

The Species structure has an optional boolean field named `constant` used to indicate whether the concentration of that species can vary during a simulation. The default value is "`false`", indicating that the species' concentration can be determined by reactions and rules.

Another optional field defined for Species is `boundaryCondition`. By default, when a species is a product or reactant of one or more reactions, its concentration is determined by those reactions. In SBML, it is possible to indicate that a given species' concentration is *not* determined by the set of reactions even when that species occurs as a product or reactant; i.e., the species is on the *boundary* of the reaction system but is a component of the rest of the model. The boolean field `boundaryCondition` can be used to indicate this. The value of the field defaults to "`false`", indicating the species *is* part of the reaction system. Table 5 shows how to interpret the combined values of the `boundaryCondition` and `constant` fields. In practice, a `boundaryCondition` value of "`true`" means a differential equation derived from the reaction definitions should not be generated for the species. A model must not contain an AssignmentRule or RateRule structure that determines the value of a species if the Species structure has `boundaryCondition` set to (or defaulting to) "`false`" and the species is a reactant and product of a reaction. The example model in section 7.5 contains all four possible combinations of the `boundaryCondition` and `constant` fields on `species` elements. Section 7.6 contains a translation into ODEs of a model which uses `boundaryCondition` and `constant` fields.

4.8.7 The `charge` Field

The optional field `charge` takes an integer indicating the charge on the species (in terms of electrons, not the SI unit coulombs). This may be useful when the species is a charged ion such as calcium (Ca^{2+}). The `charge` field is deprecated in SBML Level 2 Version 2: parsers are free to ignore this field and generators do not need to create this field.

constant value	boundaryCondition value	can have assignment or rate rule	can be reactant or product	concentration is changed by
true	true	no	yes	never changes
false	true	yes	yes	rule
true	false	no	no	never changes
false	false	yes	yes	reactions or rule but not both

Table 5: *How to interpret the values of the* `constant` *and* `boundaryCondition` *fields of the Species structure.*

4.8.8 Example

The following example shows two species definitions within an abbreviated SBML model definition. The example shows that species are listed under the heading `listOfSpecies` in the model:

```
<model>
    ...
    <listOfSpecies>
        <species id="Glucose" compartment="cell" initialConcentration="4"/>
        <species id="Glucose_6_P" compartment="cell" initialConcentration="0.75"/>
    </listOfSpecies>
    ...
</model>
```

4.9 Parameters

A Parameter structure is used to declare a variable for use in mathematical formulas in an SBML model definition. By default, parameters have constant value for the duration of a simulation and for this reason are called "parameters" instead of variables in SBML. The definition of Parameter is shown in Figure 14.

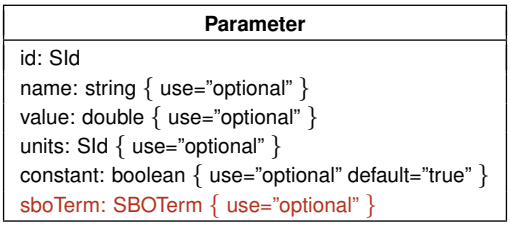

Figure 14: *The definition of Parameter. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

Parameters can be defined in two places in SBML: in lists of parameters defined at the top level in a Model structure, and within individual reaction definitions (as described in Section 4.13). Parameters defined at the top level are *global* to the whole model; parameters that are defined within a reaction are local to the particular reaction and (within that reaction) *override* any global parameters having the same identifiers (See Section 3.4.1 for further details).

4.9.1 The `id` and `name` Fields

Parameter has one required field, `id`, of type `SId`, to give the parameter a unique identifier by which other parts of an SBML model definition can refer to it. A parameter can also have an optional `name` field of type `string`. Identifiers and names must be used according to the guidelines described in Section 3.4.

4.9.2 The `value` Field

The optional field `value` determines the value (of type `double`) assigned to the identifer. A missing `value` implies that the `value` is either (a) unknown; (b) determined by an AssignmentRule or InitialAssignment struc-

ture; (c) not required for analysis; or (d) available from an external data source. If the parameter is not constant then the `value` field contains the initial value.

4.9.3 The `units` Field

The units associated with the value of the parameter are specified by the field `units`. These units are relevant when the parameter identifier appears in: (a) RateRule, AssignmentRule and InitialAssignment structures setting the value of the parameter; and (b) MathML expressions. A RateRule structure that may determine the value of the parameter has units *parameter units*/*time*, where *parameter units* are the units assigned to the parameter and *time* is the built-in `time` units. The value assigned to the parameter's `units` field must be chosen from one of the following possibilities: one of the base unit names from Table 2 on page 28; one of the built-in unit names appearing in first column of Table 3 on page 31; or the name of a new unit defined in the list of unit definitions in the enclosing Model structure. There are no constraints on which units can be chosen from these sets. There are no default units for parameters.

4.9.4 The `constant` Field

The Parameter structure has an optional boolean field named `constant` which indicates whether the parameter's value can vary during a simulation. The field's default value is "`true`"; a value of "`false`" indicates the parameter's value can be changed by rules (see Section 4.11) and the `value` is actually intended to be the initial value of the parameter.

Parameters local to a reaction (i.e., those defined within a Reaction's KineticLaw structure, as described in Section 4.13.9) cannot be changed by rules and therefore are implicitly always constant; thus, parameter definitions within Reaction structures should *not* have their `constant` field set to "`false`";

4.9.5 The `sboTerm` Field

The Parameter structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). When a value is given to this field in a parameter definition, the value must be an SBO identifier referring to a quantitative parameter defined in SBO (i.e., terms derived from `SBO:0000002`, "quantitative parameter"). The relationship is of the form "the SBML parameter *is a* X", where X is the SBO term. The term chosen should be the most precise (narrow) one that captures the role of the parameter in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

4.9.6 Example

The following is an example of parameters defined at the Model level:

```
<model>
    ...
    <listOfParameters>
        <parameter id="tau1" value="2.3" units="second"/>
        <parameter id="Km1" value="10.7" units="moleperlitre"/>
    </listOfParameters>
    ...
</model>
```

4.10 Initial Assignments

SBML Level 2 Version 2 provides two ways of assigning initial values to entities in a model. The simplest and most basic is to set the values of the appropriate fields in the relevant components; for example, the initial value of a model parameter (whether it is a constant or a variable) can be assigned by setting its `value` field directly in the model definition (Section 4.9). However, this approach is not suitable when the value must be calculated, because the initial value fields on different components such as species, compartments, and parameters are single values and not mathematical expressions. This is the reason for the introduction of InitialAssignment: to permit calculating the value of a constant or the initial value of a variable from the

values of *other* quantities in a model. The definition of InitialAssignment is shown in Figure 15.

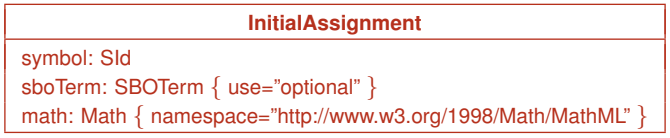

Figure 15: *The definition of InitialAssignment. Following UML notation fields that are inherited from a base class are not shown.*

As explained below, the provision of InitialAssignment does not mean that models necessarily must use this construct when defining initial values of quantities in a model. If a value can be set directly using the relevant field of a component in a model, then that approach may be more efficient and more portable to other software tools. InitialAssignment should be used when the other mechanism is insufficient for the needs of a particular model.

Initial assignments have some similarities to assignment rules (Section 4.11.3). The main differences are that unlike AssignmentRule, an InitialAssignment definition only applies at the beginning of simulated time (the former apply at all times), and InitialAssignment can set the value of a constant whereas an AssignmentRule cannot.

4.10.1 The `symbol` Field

InitialAssignment contains the field `symbol`, of type `SId`. The value of this field in an InitialAssignment object can be the identifier (i.e., the value of the `id` field) of a Compartment, Species or Parameter elsewhere in the model. The purpose of the InitialAssignment is to define the initial value of the constant or variable referred to by the `symbol` field.

An initial assignment cannot be made to reaction identifiers, that is, the `symbol` field value of an InitialAssignment cannot be an identifier that is the `id` field value of a Reaction object in the model. This is identical to a restriction placed on rules (see Section 4.11.5).

4.10.2 The `math` Field

The `math` field contains a MathML expression that is used to calculate the value of the constant or the initial value of the variable. The units of the value computed by the formula in the `math` field are taken to be the units associated with the identifier given in the `symbol` field. (That is, the units are the units of the species, compartment, or parameter, as appropriate for the kind of object identified by the value of `symbol`.)

4.10.3 The `sboTerm` Field

InitialAssignment has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). When a value is given to this field in an initial assignment definition, the value must be a valid SBO identifier referring to a mathematical expression (i.e., terms derived from `SBO:0000064`, "mathematical expression"). The InitialAssignment object should have a "is a" relationship with the SBO term, and the term should be the most precise (narrow) term that captures the role of the InitialAssignment in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

4.10.4 Semantics of Initial Assignments

The value calculated by an InitialAssignment object overrides the value assigned to the given symbol by the object defining that symbol. For example, if a Compartment's `size` is set in its definition, and the model also contains an InitialAssignment having that compartment's `id` as its `symbol` value, then the interpretation is that the `size` assigned in the Compartment definition should be ignored and the value assigned based on the computation defined in the InitialAssignment.

This does not mean that a definition of a symbol can be omitted if there is an InitialAssignment object for that symbol; the symbols must always be defined even if they are assigned a value separately. For example, there must be a Parameter definition for a given parameter if there is an InitialAssignment for that parameter.

The effects of all InitialAssignment objects are in general terms the same, but differ in the precise details depending on the type of variable being set:

- *In the case of a species*, an InitialAssignment sets the referenced species' initial quantity (*concentration* or *amount of substance*) to the value determined by the formula in `math`. (See Section 4.8.5 for an explanation of how the units of the species' quantity are determined.)
- *In the case of a compartment*, an InitialAssignment sets the referenced compartment's initial size to the size determined by the formula in `math`. The overall units of the formula are the units specified for the size of the compartment. (See Section 4.7.5 for an explanation of how the units of the compartment's size are determined.)
- *In the case of a parameter*, an InitialAssignment sets the referenced parameter's initial value to that determined by the formula in `math`. The overall units of the formula are the units defined for the parameter. (See Section 4.9.3 for an explanation of how the units of the parameter are determined.)

There cannot be two initial assignments for the same symbol in a model; that is, a model must not contain two or more InitialAssignment objects that both have the same identifier as their `symbol` field value. A model must also not define initial assignments *and* assignment rules simultaneously for the same entity. That is, there cannot be *both* an InitialAssignment and an AssignmentRule for the same symbol in a model, because both kinds of constructs apply at the start of simulated time and allowing both to exist for a given symbol would result in indeterminism. (See also Section 4.11.5.)

The ordering of InitialAssignment objects is not significant. The combined set of InitialAssignment, AssignmentRule and KineticLaw objects form a set of assignment statements that must be considered as a whole. The combined set of assignment statements should not contain algebraic loops: a chain of dependency between these statements should terminate. (More formally, consider the directed graph of assignment statements where nodes are a model's AssignmentRule objects and directed arcs exist for each occurrence of a symbol in an assignment statement `math` field. The directed arcs in this graph start from the statement assigning the symbol and end at the statement that contains the symbol in their math fields. Such a graph must be acyclic.) Examples of valid and invalid set of assignment statements are given in Section 4.11.5.

Finally, it is worth being explicit about the expected behavior in the following situation. Suppose (1) a given symbol has a value x assigned to it in its definition, and (2) there is an initial assignment having the identifier as its `symbol` value and reassigning the value to y, *and* (3) the identifier is also used in the mathematical formula of a second initial assignment. What value should the second initial assignment use? It is the value assigned to the symbol by the first initial assignment, not whatever value was given in the symbol's definition. This follows directly from the behavior at the beginning of this section: if an InitialAssignment object exists for a given symbol, then the symbol's value is overriden by that initial assignment.

4.10.5 Example

The following example shows how the species "`x`" can assigned the initial value $2 \times y$, where "`y`" is an identifier defined elsewhere in the model:

```
<model>
    ...
    <listOfSpecies>
        <species id="x" initialConcentration="5"/>
    </listOfSpecies>
    ...
    <listOfInitialAssignments>
        <initialAssignment symbol="x">
            <math xmlns="http://www.w3.org/1998/Math/MathML">
                <apply>
                    <times/>
```

```
                    <ci> y </ci>
                    <cn> 2 </cn>
                </apply>
            </math>
        </initialAssignment>
    </listOfInitialAssignments>
    ...
</model>
```

The next example illustrates the more complex behavior discussed above, when a symbol has a value assigned in its definition but there also exists an InitialAssignment for it *and* another InitialAssignment uses its value in its mathematical formula.

```
<model>
    ...
    <listOfSpecies>
        <species id="x" initialConcentration="5"/>
    </listOfSpecies>
    ...
    <listOfInitialAssignments>
        <initialAssignment symbol="x">
            <math xmlns="http://www.w3.org/1998/Math/MathML">
                <cn> 2 </cn>
            </math>
        </initialAssignment>
        <initialAssignment symbol="othersymbol">
            <math xmlns="http://www.w3.org/1998/Math/MathML">
                <apply>
                    <times/>
                    <ci> x </ci>
                    <cn> 2 </cn>
                </apply>
            </math>
        </initialAssignment>
    </listOfInitialAssignments>
    ...
</model>
```

The value of "`othersymbol`" in the SBML excerpt above will be "`4`". The case is somewhat pathological, but helps illustrate the rule of thumb: if there is an initial assignment for a symbol, the value assigned to the symbol in its definition must be ignored and the value created by the initial assignment used instead.

4.11 Rules

Rules provide a way to create constraints on variables for cases in which the constraints cannot be expressed using reactions (Section 4.13) nor by the assignment of an initial value to a component in a model. There are two orthogonal dimensions by which rules can be described. First, there are three different possible functional forms, corresponding to the following three general cases (where x is a variable, f is some arbitrary function returning a numeric result, V is a vector of variables that does not include x, and W is a vector of variables that may include x):

Algebraic	left-hand side is zero:	$0 = f(W)$
Assignment	left-hand side is a scalar:	$x = f(V)$
Rate	left-hand side is a rate-of-change:	$dx/dt = f(W)$

The second dimension concerns the role of variable x in the equations above: x can be the identifier of a compartment (to set its size), a species (to set its concentration), or a parameter (to set its value).

In their general form given above, there is little to distinguish between *assignment* and *algebraic* rules however there are restrictions on assignment rules that are described in Section 4.11.5 (the set of assignment rules cannot contain algebraic loops). They are treated as separate cases for the following reasons:

- *Assignment* rules can simply be evaluated to calculate intermediate values for use in numerical methods;

- Some simulators do not contain numerical solvers capable of solving unconstrained *algebraic* equations;
- Those simulators that *can* solve these *algebraic* equations make a distinction between the different categories listed above; and
- Some specialized numerical analyses of models may only be applicable to models that do not contain *algebraic* rules.

The approach taken to covering these cases in SBML is to define an abstract *Rule* structure containing only one field, `math`, to hold the right-hand side expression, then to derive subtypes of *Rule* that add fields to distinguish the cases of algebraic, assignment and rate rules. Figure 16 gives the definitions of *Rule* and the subtypes derived from it. The figure shows there are four subtypes, AlgebraicRule, AssignmentRule and RateRule derived directly from *Rule*. These correspond to the cases *Algebraic*, *Assignment*, and *Rate* described above respectively.

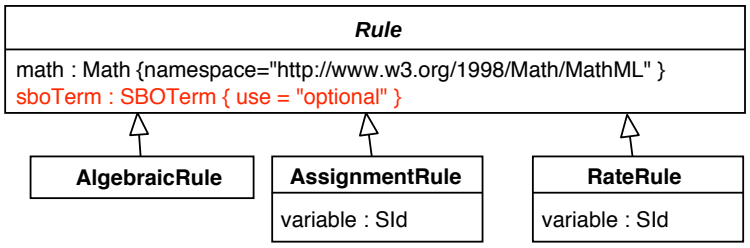

Figure 16: *The definition of Rule and derived types. Following UML notation fields that are inherited from a base class are not shown.*

4.11.1 The `sboTerm` Field

The *Rule* structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). This means that the object classes derived from *Rule*, namely AlgebraicRule, AssignmentRule, and RateRule, all have `sboTerm` fields. When a value is given to this field, it must be a valid SBO identifier referring to a mathematical expression defined in SBO (i.e., terms derived from `SBO:0000064`, "mathematical expression"). The AlgebraicRule, AssignmentRule, or RateRule object should have a "is a" relationship with the SBO term, and the term should be the most precise (narrow) term that captures the role of that rule in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

4.11.2 AlgebraicRule

The rule type AlgebraicRule is used to express equations that are neither assignments of model variables nor rates of change. AlgebraicRule does not add any fields to the basic *Rule*; its role is simply to distinguish this case from the other cases. An example of the use of AlgebraicRule structures is given in Section 7.4.

4.11.3 AssignmentRule

The rule type AssignmentRule is used to express equations that set the values of variables. The left-hand side (the `variable` field) of an assignment rule can refer to the identifier of a species, compartment, or parameter (but not a reaction). Two or more RateRule or AssignmentRule structures cannot have the same left-hand side or `variable` field value in an SBML model definition. In all cases, as would be expected, the units of the formula representing the right hand side, the `math` field, are identical to the units associated with the left hand side, the `variable` field, when that variable appears in other formulas.

The effects of an AssignmentRule structure are in general terms the same, but differ in the precise details depending on the type of variable being set:

- *In the case of a species*, an AssignmentRule sets the referenced species' quantity (*concentration* or *amount of substance*) to the value determined by the formula in `math`. The units of the formula are the *units of the species* as defined in Section 4.8.5.

  Restrictions: In a given SBML Level 2 model, there cannot be both a AssignmentRule `variable` field and a SpeciesReference `species` field having the same value. (See Section 4.13 for the definition of SpeciesReference.) This means an assignment rule cannot be defined for a species that is created or destroyed in a reaction. The only exception is when the given species is a boundary condition; i.e., on the Species structure the `boundaryCondition` field is set to "`true`".

- *In the case of a compartment*, an AssignmentRule sets the referenced compartment's size to the size determined by the formula in `math`. The overall units of the formula are the units specified for the size of the compartment identified by the value of the AssignmentRule's `variable` field. (See Section 4.7.5 for an explanation of how the units of the compartment's size are determined.)

- *In the case of a parameter*, an AssignmentRule sets the referenced parameter's value to that determined by the formula in `math`. The overall units of the formula are the units defined for the parameter identified by the value of the AssignmentRule's `variable` field. (See Section 4.9.3 for an explanation of how the units of the parameter are determined.)

4.11.4 RateRule

The rule type RateRule is used to express equations that determine the rates of change of variables. The left-hand side (the `variable` of a rate rule) can refer to the identifier of a species, compartment, or parameter (but not a reaction). Two or more RateRule or AssignmentRule structures cannot have the same left-hand side or `variable` field value in an SBML model definition. In all cases, as would be expected, the units of the formula representing the right hand side, in the `math` field, are of the form $x/time$ where x are the same units as associated with the symbol in the `variable` field, when that variable appears in other formulas. *time* is a built-in unit (see Section 4.4). The effects of a RateRule are in general terms the same, but differ in the precise details depending on which variable is being set:

- *In the case of a species*, a RateRule sets the rate of change of the species' quantity to the value determined by the formula in `math`. The overall units of the formula must be *species quantity*/*time*, where the *time* units are the built-in units of time described in Section 4.4 and the *species quantity* units are the *units of the species* as defined in Section 4.8.5.

  Restrictions: In a given model, there cannot be both a SpeciesReference `species` field and a RateRule `variable` field having the same value. (See Section 4.13 for the definition of SpeciesReference.) This means an rate rule cannot be defined for a species that is created or destroyed in a reaction. The only exception is when the given species is a boundary condition; i.e., on the Species structure that defines the species the `boundaryCondition` field is set to "`true`".

- *In the case of a compartment*, a RateRule sets the rate of change of the compartment's size to the value determined by the formula in `math`. The overall units of the formula are *size*/*time*, where the *time* units are the built-in units of time described in Section 4.4 and the *size* units are the units of size on the compartment identified by the value of the RateRule's `variable` field. (See Section 4.7.5 for an explanation of how the units of the compartment's size are determined.)

- *In the case of a parameter*, a RateRule sets the rate of change of the parameter's value to that determined by the formula in `math`. The overall units of the formula are of the form $x/time$ where x are the units defined for the parameter identified by the value of the AssignmentRule's `variable` field and the *time* units are the built-in units of time described in Section 4.4. (See Section 4.9.3 for an explanation of how the units of the parameter are determined.)

4.11.5 Restrictions on Rules

SBML specifically does not stipulate the form of the algorithms that can be applied to rules and reactions. For example, SBML does not specify when or how often rules should be evaluated. The constraints described

by rules and kinetic rate laws are meant to apply collectively to the set of variable values for a specific instant in time.

No more than one assignment or rate rule can be defined for a given identifier. No assignment or rate rule can be defined for an identifier whose corresponding structure has the field `constant` set to `true`.

A rule cannot be used to set the value of a reaction rate; that is, the value of a `variable` field in an AssignmentRule or RateRule cannot be the value of any Reaction's `id` field.

The value calculated by an AssignmentRule object overrides the value assigned to the given symbol by the object defining that symbol. For example, if a Compartment's `size` is set in its definition, and the model also contains an AssignmentRule having that compartment's `id` as its `variable` value, then the interpretation is that the `size` assigned in the Compartment definition should be ignored and the value assigned based on the computation defined in the AssignmentRule.

This does not mean that a definition of a symbol can be omitted if there is an AssignmentRule object for that symbol. For example, there must be a Parameter definition for a given parameter if there is an AssignmentRule for that parameter.

A model must also not define initial assignments *and* assignment rules simultaneously for the same entity. That is, there cannot be *both* an AssignmentRule and an InitialAssignment for the same symbol in a model, because both kinds of constructs apply at the start of simulated time and allowing both to exist for a given symbol would result in indeterminism. (See also Section 4.10.4.)

The combined set of InitialAssignment, AssignmentRule and KineticLaw structures form a set of assignment statements that should be considered as a whole. The combined set of assignment statements should not contain algebraic loops: a chain of dependency between these statements should terminate. Formally consider the directed graph of assignment statements where nodes are statements and directed arcs exist for each occurrence of a symbol in an assignment statement `math` field. The directed arcs start from the statement assigning the symbol to the statements that contain the symbol in their math fields. Such a graph must be acyclic. (A KineticLaw structure assigns to the symbol contained in the `id` field of the containing Reaction structure). Eliminating algebraic loops ensures that assignment statements can be evaluated any number of times without the result of those evaluations changing. As an example, consider the following equations:

$$x = x + 1, \quad y = z + 200, \quad z = y + 100$$

If this set of equations were interpreted as a set of assignment statements, it would be invalid because the rule for x refers to x and the rule for y refers to z whilst the rule for z refers to y.

The following set of equations if interpreted as assignment statements would be valid:

$$x = 10, \quad y = z + 200, \quad z = x + 100$$

A SBML model must not be overdetermined. A SBML model that does not contain AlgebraicRule structures is not over determined.

To determine whether a continuous deterministic mathematical model is overdetermined we form a bipartite graph in which one set of vertices represent the variables and the other the set of vertices represent the equations. Edges in the graph link equation vertexes to the variable vertices so that the variables are linked to the equations that determine them. Edges connect each algebraic equation vertex to all the vertices representing variables occurring in the equation. For each an ordinary differential equation (ODE) a single edge connects the vertex representing the equation to the vertex representing the variable determined by the equation.

A mathematical model is overdetermined if the maximal matchings of the bipartite graph contain disconnected vertexes representing equations. (If one maximal matching has this property then all the maximal matchings will have this property i.e. it is only necessary to find one maximal matching.) A efficient algorithm for finding a maximal matching is described in Hopcroft and Karp (1973).)

We can define the application of the above general statement to SBML by defining the mapping of SBML

structures to components of the bipartite graph representing the model structure. In this mapping we consider assignment rules to be algebraic equations and we consider the assignment of kinetic laws to reaction variables to be algebraic equations. We assume the construction of an ODE for each species determined by one or more reaction rate laws. The following mapping assumes that the model is valid in all respects but may be overdetermined e.g. equations cannot refer to undeclared variables.

The bipartite graph is formed as follows:

- Create equation vertexes for each of the following:
  1. a Species structure that has the `boundaryCondition` field set to false and `constant` field set to false and which is referenced by one or more reactant or product lists of a Reaction structure containing a KineticLaw structure
  2. a *Rule* structure
  3. a KineticLaw structure
- Create variable vertexes for (a) every Species, Compartment and Parameter structure which has the `Constant` field set to false; and (b) for every Reaction structure.
- Create an edge for each case of the following:
  1. *a Species structure that has the* `boundaryCondition` *field set to false and* `constant` *field set to false and which is referenced by the reactant or product lists of a Reaction structure containing a KineticLaw structure.* The edge connects the vertex representing the species to the vertex representing the species' equation (see (1) above)
  2. *an AssignmentRule or RateRule.* The edge connects the vertex representing the *Rule* to the vertex representing the variable referenced by the `variable` field of the rule.
  3. *a KineticLaw.* The edge connects the vertex representing the KineticLaw equation to the variable vertex representing the Reaction containing the KineticLaw.
  4. *the occurrence of a MathML* `ci` *symbol referencing a variable (that is referencing a Species,* `compartment`*,* `parameter` *structure which has the* `constant` *field set to false) within an AssignmentRule or AlgebraicRule.* The edge connects the vertex representing the rule to the vertex representing the variable.
  5. *the occurrence of a MathML* `ci` *symbol referencing a Reaction within an AssignmentRule or AlgebraicRule.* The edge connects the vertex representing the rule to the vertex representing the reaction variable.
  6. *the occurrence of a MathML* `ci` *symbol referencing a variable within an AssignmentRule or AlgebraicRule.* The edge connects the vertex representing the rule to the vertex representing the variable. The `ci` element must either reference: (a) a Species, `compartment` or `parameter` structure which has the `constant` field set to false; or (b) reference a Reaction structure)
  7. *the occurrence of a MathML* `ci` *symbol referencing a variable within an KineticLaw.* The edge connects the vertex representing the kinetic law to the vertex representing the variable. The `ci` element must either reference a Species, `compartment` or `parameter` structure which has the `constant` field set to false. In this context a `ci` element cannot refer to a Reaction structure.

4.11.6 Example of Rule Use

This section contains an example set of rules. Consider the following set of equations:

$$k = \frac{k_3}{k_2}, \quad s_2 = \frac{k\,x}{1 + k_2}, \quad A = 0.10\,x$$

This can be encoded by the following scalar rule set (where the definitions of `x`, `s`, `k`, `k2`, `k3` and `A` are assumed to be located elsewhere in the model and not shown in this abbreviated example):

```
<listOfRules>
    <assignmentRule variable="k">
        <notes>
            <xhtml:p>
                k = k3/k2
            </xhtml:p>
        </notes>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
                <divide/>
                <ci> k3 </ci>
                <ci> k2 </ci>
            </apply>
        </math>
    </assignmentRule>
    <assignmentRule variable="s2">
        <notes>
            <xhtml:p>
                s2 = (k * x)/(1 + k2)
            </xhtml:p>
        </notes>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
                <divide/>
                <apply>
                    <times/>
                    <ci> k </ci>
                    <ci> x </ci>
                </apply>
                <apply>
                    <plus/>
                    <cn> 1 </cn>
                    <ci> k2 </ci>
                </apply>
            </apply>
        </math>
    </assignmentRule>
    <assignmentRule variable="A">
        <notes>
            <xhtml:p>
                A = 0.10 * x
            </xhtml:p>
        </notes>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
                <times/>
                <cn> 0.10 </cn>
                <ci> x </ci>
            </apply>
        </math>
    </assignmentRule>
</listOfRules>
```

4.12 Constraints

The Constraint structure is a mechanism for stating the assumptions under which a model is designed to operate. The *constraints* are statements about permissible values of different quantities in a model. Figure 17 shows the definition of the Constraint data structure.

Constraint
sboTerm: SBOTerm { use="optional" }
math: Math { namespace="http://www.w3.org/1998/Math/MathML" }
message: (ANY: { namespace="http://www.w3.org/1999/xhtml" }) { minOccurs="0" maxOccurs="1" }

Figure 17: *The definition of Constraint. Following UML notation fields that are inherited from a base class are not shown.*

A Constraint structure consists of two fields: `math`, which contains a MathML formula, and the optional field `message`, which contains a message in XHTML format that may be displayed to the user. The formula contained in the `math` field should be an arbitrary function of the variables and parameters of the SBML model. The formula must return a boolean value of `true` when the model is a *valid* state. Constraint structures have effect at all times, i.e, $t >= 0$.

Constraint structures *cannot and should not* be used to compute the dynamical behavior of a model as part of, for example, simulation. They simply provide a mechanism allowing a modeler to express the validity of a model's state during numerical analysis. Constraints may be used as a key input to non-dynamical analysis, for example by expressing flux constraints for flux balance analysis.

The results of a simulation of a model containing a constraint are invalid from any simulation time at and after a point when the function given by the `math` returns a value of "`false`". (Invalid simulation results do not make a prediction of the behavior of the biochemical reaction network represented by the model.) The precise behavior of simulation tools is left undefined with respect to constraints. If invalid results are detected with respect to a given constraint, the `message` field may optionally be displayed to the user. Software tools are not required to display the message, but it is recommended as a matter of best practice. The simulation tool may also halt the simulation or clearly delimit in output data the simulation time point at which the simulation results become invalid.

4.12.1 The sboTerm Field

The Constraint structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). When a value is given to this field in a constraint definition, the value must be a valid SBO identifier referring to a mathematical expression (i.e., terms derived from `SBO:0000064`, "mathematical expression"). The Constraint should have an "is a" relationship with the SBO term, and the term should be the most precise (narrow) term that captures the role of the Constraint in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

4.12.2 Example

As an example, the following SBML fragment demonstrates the constraint that species S_1 should only have values between 1 and 100:

```
<listOfConstraints>
    <constraint>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
                <and/>
                <apply>
                    <lt/>
                    <cn> 1 </cn>
                    <ci> S1 </ci>
                </apply>
                <apply>
                    <lt/>
                    <ci> S1 </ci>
                    <cn> 100 </cn>
                </apply>
            </apply>
        </math>
        <message>
            <p xmlns="http://www.w3.org/1999/xhtml">
                Species S1 is out of range
            </p>
        </message>
    </constraint>
</listOfConstraints>
```

4.13 Reactions

A *reaction* represents any transformation, transport or binding process, typically a chemical reaction, that can change the amount of one or more species. In SBML, a reaction is defined primarily in terms of the participating reactants and products (and their corresponding stoichiometries), along with optional modifier species, an optional kinetic law describing the rate at which the reaction takes place, and optional parameters entering into the kinetic law. These various parts of a reaction are recorded in the SBML Reaction type defined in Figure 18.

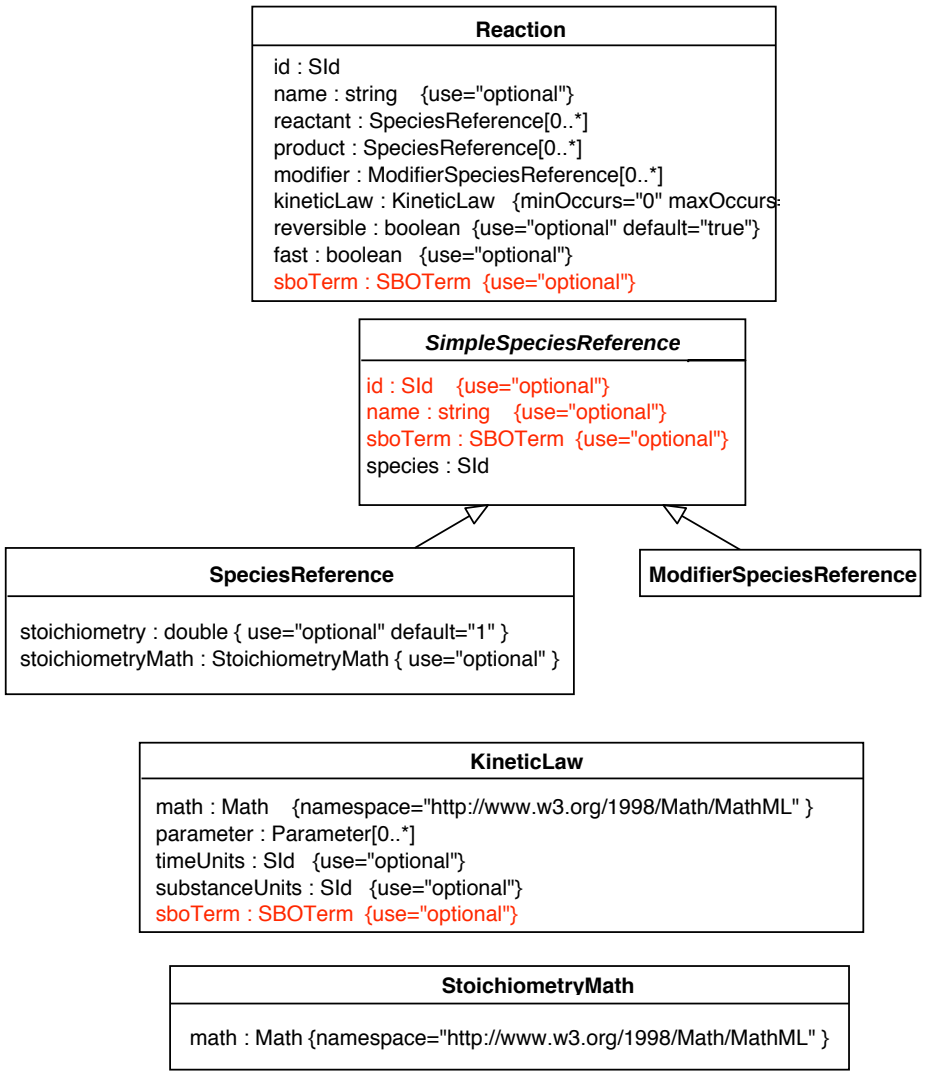

Figure 18: *The definitions of Reaction, KineticLaw, SpeciesReference and ModifierSpeciesReference. Following UML notation fields that are inherited from a base class are not shown.*

4.13.1 The `id` and `name` Fields

As with most other main structures in SBML, the Reaction data structure includes a required `id`, of type `SId`, and an optional `name`, of type `string`. These must be used according to the guidelines described in Section 3.4.

The identifier of a Reaction structure can be used in mathematical formulas in an SBML model to represent the rate of the reaction. This usage is explained in detail in Section 4.13.10 below.

4.13.2 The `reactant`, `product` and `modifier` Fields

The reactant species, product species and modifier species in a reaction are described using the fields `reactant`, `product` and `modifiers`, respectively. These fields are optional lists of SpeciesReference and ModifierSpeciesReference structures, as shown in Figure 18 on the page before. They are described in more detail in Sections 4.13.7 and 4.13.8 below.

4.13.3 The `reversible` Field

The optional boolean field `reversible` indicates whether the reaction is reversible. The field is optional, and if left unspecified in a model, it defaults to a value of "`true`". Although the reversibility of a reaction is determined by its rate law, the need to allow rate expressions in SBML to be optional leads to the need for a separate flag indicating reversibility. Information about reversibility in the absence of a `KineticLaw` in a Reaction is useful in certain kinds of structural analyses such as elementary mode analysis. It is true that the presence of this information in two places (i.e., the rate expression and the flag `reversible`) leaves open the possibility of a model containing contradictory information, but the creation of such a model would indicate an error on the part of the software generating it. Software developers must take care to guard against logical contradictions in the definitions of reactions.

4.13.4 The `fast` Field

The optional boolean field `fast` is another optional boolean field in the Reaction data structure. The field has no default value.

Previous definitions of SBML indicated that software tools could ignore this field if they did not implement support for the corresponding concept; however, further research has revealed that this is incorrect and `fast` cannot be ignored. SBML Level 2 Version 2 stipulates that if a model has values for `fast`, a software tool must be able to respect the field or else indicate to the user that it does not have the capacity to do so.

When a model contains values for `fast` on any of its reactions, it is an indication that the creator of the model is distinguishing different time scales of reactions. The model's reaction definitions are divided into two sets by the values of the `fast` fields. The set of reactions which have values of "`true`" (known as *fast reactions*) should be assumed to be operating on a time scale significantly faster than the other reactions (the *slow reactions*). Fast reactions are considered to be instantaneous relative to the slow reactions. Software tools must use a pseudo steady-state approximation for the set of fast reactions when constructing the system of equations for the model.

Modelers should take care to note that the correctness of the approximation requires a significant separation of time scales between the fast reactions and other proceses. This is not trivial to estimate a priori, and may even change over the course of a simulation, but can be reasonably assessed a posteriori in most cases.

Care must be taken when interpreting values on the `fast` field. The absence of a default value means that if a there are *no* values for `fast` anywhere in a model, the field itself cannot be used to make assumptions about fast or slow reactions; it only means the creator of the model is not using the field to make time scale distinctions. If the model does in fact constain fast reactions, they may be represented in another way. Conversely, if a model *does* contain a value for `fast` on any reaction, then the model's creator is making explicit statements about time scale separations and software reading the model must take appropriate steps or risk misinterpreting the model. Since there is no default value, the best-practice recommendation is to label all reactions in a model (either "`true`" or "`false`") if any one of the reactions needs to be given a value.

Analysis software cannot ignore the value of the `fast` attribute because doing so may lead to different results when compared to a software system that makes use of `fast`. For maximal interoperability, we recommend that SBML models are not generated with the `fast` attribute set to "`true`"; instead, any approximation required by the model should be made explicit through the use of rules (see Section 4.11).

4.13.5 The sboTerm Field

The Reaction structure has an optional **sboTerm** field of type **SBOTerm** (see Sections 3.1.8 and 5). When a value is given to this field in a reaction definition, the value must be a valid SBO identifier referring to a modeling framework (i.e., terms derived from **SBO:0000004**, "modeling framework"). The Reaction structure should have an "is a" relationship with the SBO term. The SBO term chosen should be the most precise (narrow) term that defines the mathematical framework used in the reaction.

As discussed in Section 4.2.1, the value given to **sboTerm** on a model's Reaction objects interacts with the SBO labels on the Model element. If the Model's **sboTerm** field has a value, it should be interpreted to mean that all the reactions in a model assume the same modeling framework. In that case, the **sboTerm** labels on individual reactions may be omitted, but only the Reaction SBO labels can be thus omitted; the SBO labels on KineticLaw within Reaction must still be supplied, as must the terms on other components of the model, in order to characterize the model completely. (See Section 4.2.1 for more discussion about this topic.)

SBO labels are optional information on a model. Applications are free to ignore **sboTerm** values, and a model must be interpretable without the benefit of SBO labels. Section 5 gives more information about this principle and the use of SBO.

4.13.6 SimpleSpeciesReference

Every species that enters into a given reaction must appear in that reaction's lists of reactants, products and/or modifiers. In an SBML model, all species that may participate in any reaction are listed in the **listOfSpecies** field of the top-level Model data structure (see Section 4.2). Lists of products, reactants and modifiers in Reaction structures do not introduce new species, but rather, they refer back to those listed in the model's top-level **listOfSpecies**. For reactants and products, the connection is made using the SpeciesReference data structure; for modifiers, it is made using the ModifierSpeciesReference data structure.

SimpleSpeciesReference, defined in Figure 18 on page 50, is an abstract type that serves as the parent class of both SpeciesReference and ModifierSpeciesReference. It is used simply to hold the fields **species**, **id**, **name**, and **sboTerm** that are common to the latter structures.

The id and name Fields

The optional identifier stored in the **id** field allows the *SimpleSpeciesReference* structure to be referenced from other structures. There are as yet no SBML structures that do this; however, such structures are anticipated in future levels of SBML. The identifier must be a text string conforming to the syntax permitted by the **SId** data type described in Section 3.1.7. The **id** value (whether it is in a SpeciesReference or ModifierSpeciesReference object) exists in the global namespace of the model, as described in Section 3.4. *SimpleSpeciesReference* also has an optional **name** field, of type **string**. The **name** and **id** fields must be used as described in Section 3.4.

The sboTerm Field

The *SimpleSpeciesReference* structure has an optional **sboTerm** field of type **SBOTerm** (see Sections 3.1.8 and 5). This means that the object classes derived from *SimpleSpeciesReference*, namely SpeciesReference and ModifierSpeciesReference, all have **sboTerm** fields. When a value is given to this field, it must be a valid SBO referring to a participant role. The appropriate term depends on whether the object is a reactant, product or species. If a reactant, then it should be a term in the **SBO:0000010**, "reactant" hierarchy; if a product, then it should be a term in the **SBO:0000011**, "product" hierarchy; and if a modifier, then it should be a term in the **SBO:0000019**, "modifier" hierarchy. The SpeciesReference and ModifierSpeciesReference structures should have an "is a" relationship to the term identified by the SBO term identifier. The SBO terms chosen should be the most precise (narrow) one that defines the role of the species in the reaction.

A product term must only be used when the SpeciesReference structure is contained in the **product** field of the containing Reaction structure. Similarly, a reactant term must only be used when the SpeciesReference structure is contained in the **reactant** field of the containing Reaction structure.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

4.13.7 SpeciesReference

In a given reaction, references to a model's species that act as reactants and/or products are made using SpeciesReference data objects.

The `species` field

The mandatory field `species`, inherited from *SimpleSpeciesReference* (Section 4.13.6), must refer to the name of an existing species defined in the enclosing Model structure.

The `stoichiometry` and `stoichiometryMath` fields

Product and reactant stoichiometries can be specified using *either* `stoichiometry` or `stoichiometryMath` in the SpeciesReference structure. The `stoichiometry` field is of type double and should contain values greater than 0. The `stoichiometryMath` field is implemented as an element containing a MathML math expression in dimensionless units. Only one of the `stoichiometry` and `stoichiometryMath` fields should be used on a given SpeciesReference structure. When neither field is present then the stoichiometry associated with the SpeciesReference structure is "1".

For maximum interoperability between models and software tools, we recommend that when generating SBML Level 2 models, the `stoichiometry` field be used in preference to the `stoichiometryMath` field and that the `stoichiometry` field contains integer values. Parsing software should expect and handle appropriately all possible values of the `stoichiometry` and `stoichiometryMath` fields including, for example, non-integer values for `stoichiometry`. The expression in `stoichiometryMath` may refer to species identifiers, as discussed in Section 3.5.4. The only species identifiers that can be used in `stoichiometryMath` are those listed in the `reactant`, `product` and `modifier` fields of the containing Reaction structure.

The following is a simple example of a species reference for species "X0", with stoichiometry 2, in a list of reactants within a reaction named "J1":

```
<model>
    ...
    <listOfReactions>
        <reaction id="J1">
            <listOfReactants>
                <speciesReference species="X0" stoichiometry="2">
            </listOfReactants>
            ...
        </reaction>
        ...
    </listOfReactions>
    ...
</model>
```

The following is a more complex example of a species reference for species "X0", with a stoichiometry expression consisting of the parameter `x`:

```
<model>
    ...
    <listOfReactions>
        <reaction id="J1">
            <listOfReactants>
                <speciesReference species="X0">
                    <stoichiometryMath>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <ci>x</ci>
                        </math>
                    </stoichiometryMath>
                </speciesReference>
            </listOfReactants>
            ...
```

```
            </reaction>
            ...
        </listOfReactions>
        ...
    </model>
```

A species can occur more than once in the lists of reactants and products of a given reaction. The effective stoichiometry for a species in a reaction is the sum of the stoichiometry values given on the SpeciesReference structures in the list of products minus the sum of stoichiometry values given on the SpeciesReference structures in the list of reactants. A positive value indicates the species is effectively a product and a negative value indicates the species is effectively a reactant. SBML places no restrictions on the effective stoichiometry of a species in a reaction; for example, it can be zero. In the following SBML fragment, the two reactions have the same effective stoichiometry for all their species:

```
<reaction id="x">
    <listOfReactants>
        <speciesReference species="a"/>
        <speciesReference species="a"/>
        <speciesReference species="b"/>
    </listOfReactants>
    <listOfProducts>
        <speciesReference species="c"/>
        <speciesReference species="b"/>
    </listProducts>
</reaction>
<reaction id="y">
    <listOfReactants>
        <speciesReference species="a" stoichiometry="2"/>
    </listOfReactants>
    <listOfProducts>
        <speciesReference species="c"/>
    </listProducts>
</reaction>
```

Constraints on the use of SpeciesReference structures

A reaction can contain an empty list of reactants or an empty list of products but must have at least one reactant or product. Also note that whether a given species is allowed to appear as a reactant or product is dictated by certain flags on the structure defining the species in the model; see Section 4.8.6 for more information.

4.13.8 ModifierSpeciesReference

Sometimes a species appears in the kinetic rate formula of a reaction but is itself neither created nor destroyed in that reaction (for example, because it acts as a catalyst or inhibitor). In SBML, all such species are simply called *modifiers* without regard to the detailed role of those species in the model. The Reaction structure provides a way to express which species act as modifiers in a given reaction. This is the purpose of the `modifier` field in Reaction; this field is a list of ModifierSpeciesReference structures defined in Figure 18 on page 50.

The ModifierSpeciesReference structure has a mandatory field, `species`, of type `SId`, inherited from *SimpleSpeciesReference*; its value must be the identifier of a species defined in the enclosing Model. This species is designated as a modifier for the current reaction. A reaction may have any number of modifiers. The ModifierSpeciesReference structure also has an optional field named `id`, used to give the reference an identifier. The identifier must be a text string conforming to the syntax permitted by the `SId` data type described in Section 3.1.7. The `id` value exists in the global namespace of the model as described in Section 3.4. ModifierSpeciesReference also has an optional `name` field, of type `string`. The `name` and `id` fields must be used as described in Section 3.4.

It is permissible for a modifier species to simultaneously appear in the list of reactants and products of the same reaction where it is designated as a modifier, as well as to appear in the list of reactants, products and modifiers of other reactions in the model.

4.13.9 KineticLaw

A `kineticLaw` structure, enclosed in a Reaction structure, describes the rate at which the reaction takes place. The inclusion of a KineticLaw structure in an instance of a Reaction component is optional; however, in general there is no useful default that can be substituted in place of a missing rate law definition in a reaction.

The `math` field

As shown in Figure 18 on page 50, the KineticLaw structure has a field called `math`; this is a MathML expression defining the rate of the reaction.

It is important to make clear at the outset that a "kinetic law" in SBML is *not* equivalent to a traditional rate law. The reason is that SBML must support multi-compartment models, and the units used in textbook rate laws as well as some conventional single-compartment modeling packages are problematic when used for defining reactions between multiple compartments. Rate expressions in SBML are expressed in terms of *substance/time*, rather than the more typical *concentration/time*. Converting between these two conventions is a simple matter of dividing the *substance/time* expression by the size of the compartment where a given species is located. To put this in slightly more precise terms, suppose there are two species S and P in a reaction $S \rightarrow P$, where S is located in a compartment A having volume V_A, P is located in a compartment B having volume V_B, and the kinetic law expression gives the rate of the reaction as being R. Then the rate of change in the concentration of S is given by $d[S]_A/dt = -R/V_A$ and the rate of change in the concentration of P is $d[P]_B/dt = R/V_B$. The translation of a complete multi-compartmental model into ODEs is given in Section 7.6.

The expression in `math` may refer to species identifiers, as discussed in Section 3.5.4. The only species identifiers that can be used in `math` are those listed in the `species` fields of the `reactant`, `product` and `modifier` structures contained in the Reaction structure.

The `substanceUnits` and `timeUnits` fields

As previously stated, the overall rate expression in the `math` field must have the units of *substance/time*. The optional fields `substanceUnits` and `timeUnits` determine the units of substance and time for the reaction, respectively. The values of these fields must be chosen from one of the following possibilities: one of the base unit names from Table 2 on page 28; one of the built-in unit names appearing in the first column of Table 3 on page 31); or the name of a new unit defined in the list of unit definitions in the enclosing Model structure. In the case of `substanceUnits`, the value chosen must be a scaled and/or multiplied variant of `dimensionless`, `moles`, or `item`. In the case of `timeUnits`, the value chosen must be a scaled and/or multiplied variant of `seconds` or `dimensionless`, with an `exponent` field value of "`1`".. If these fields are not set in a given KineticLaw instance, the units are taken from the defaults defined by the built-in "`substance`" and "`time`" of Table 3 on page 31.

The `Parameter` field

An instance of a KineticLaw type structure can contain zero or more `parameter` structures (Section 4.9) which define symbols that can be used in the `math` field. As discussed in Section 3.4.1, reactions introduce local namespaces for parameter identifiers. Within a KineticLaw structure inside a reaction definition, a local parameter whose identifier is identical to a global parameter defined in the enclosing Model-type structure takes precedence over that global parameter.

The `sboTerm` field

The KineticLaw structure has an optional `SBOTerm` field, `sboTerm` (see Section 5). This field when present must contain a Systems Biology Ontology (SBO; `http://www.biomodels.net/SBO/`) term identifier referring to a kinetic law SBO term, that is a term derived from `SBO:0000001`, "rate law". The KineticLaw structure should have a 'is a' relationship with the SBO term. The SBO term chosen should be the most precise (narrow) term that defines the type of kinetic law encoded by the structure.

Example

The following is an example of a Reaction structure that defines a reaction named J_1, in which $X_0 \rightarrow S_1$ at a rate given by kX_0S_2, in conventional units, where S_2 is a catalyst and k is a parameter. It demonstrates the use of species references and the KineticLaw structure. The units on the species here are the defaults of *substance/volume* (see Section 4.8), and so the conventional rate expression is multiplied by the compartment volume so that the encoded rate expression has the final units of *substance/time*.

```
<model>
    ...
    <listOfUnitDefinitions>
        <unitDefinition id="concent_per_time">
            <listOfUnits>
                <unit kind="litre"/>
                <unit kind="mole"   exponent="-1"/>
                <unit kind="second" exponent="-1"/>
            </listOfUnits>
        </unitDefinition>
    </listOfUnitDefinitions>
    ...
    <listOfSpecies>
        <species id="S1" compartment="c1" initialConcentration="2.0"/>
        <species id="S2" compartment="c1" initialConcentration="0.5"/>
        <species id="X0" compartment="c1" initialConcentration="1.0"/>
    </listOfSpecies>
        ...
    <listOfReactions>
        <reaction id="J1">
            <listOfReactants>
                <speciesReference species="X0"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="S1"/>
            </listOfProducts>
            <listOfModifiers>
                <modifierSpeciesReference species="S2"/>
            </listOfModifiers>
            <kineticLaw>
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <ci> k </ci>
                        <ci> S2 </ci>
                        <ci> X0 </ci>
                        <ci> c1 </ci>
                    </apply>
                </math>
                <listOfParameters>
                    <parameter id="k" value="0.1" units="concent_per_time"/>
                </listOfParameters>
            </kineticLaw>
        </reaction>
    </listOfReactions>
    ...
</model>
```

4.13.10 Reaction Identifiers Used in Mathematical Expressions

The value of the `id` field of a Reaction structure can be used as the content of a MathML `ci` element. Such a `ci` element or symbol represents the rate of the given reaction as given by the KineticLaw structure of the reaction. The symbol has the units of the KineticLaw as described in Section 4.13.9 or *substance/time* units if the KineticLaw is not present.

A KineticLaw structure forms an assignment statement assigning the evaluated value of the `math` field to the symbol value contained in the Reaction `id` field. No other structure can assign a value to such a reaction

symbol; i.e., the `variable` fields of InitialAssignment, RateRule, AssignmentRule and EventAssignment structures cannot contain the value of a Reaction `id` field.

The combined set of InitialAssignment, AssignmentRule and KineticLaw structures form a set of assignment statements that should be considered as a whole. The combined set of assignment rules should not contain algebraic loops: a chain of dependency between these statements should terminate. (More formally, consider the directed graph of assignment statements where nodes are statements and directed arcs exist for each occurrence of a symbol in a assignment statement `math` field. The directed arcs start from the statement defining the symbol to the statements that contain the symbol in their math fields. Such a graph must be acyclic.) Examples of valid and invalid set of assignment statements are given in Section 4.11.5.

4.14 Events

Model has an optional list of Event structures that describe the time and form of explicit instantaneous discontinuous state changes in the model. For example, an event may describe that one species concentration is halved when another species concentration exceeds a given threshold value.

An Event structure defines when the event can occur, the variables that are affected by the event, and how the variables are affected. The effect of the event can optionally be delayed after the occurrence of the condition which invokes it. The operation of an Event structure is divided into two phases (even when the event is not delayed): one when the event is *fired* and the other when the event is *executed*. The Event type is defined in Figure 19. Both Event and EventAssignment are derived from *Sbase* (see Section 3.3). An example of a model which uses events is given below.

Event
id: SId
name: string { use="optional" }
trigger: (math : Math { namespace="http://www.w3.org/1998/Math/MathML" })
delay: (math : Math { namespace="http://www.w3.org/1998/Math/MathML" }) { minOccurs="0" maxoccurs="1" }
timeUnits: SId { use="optional" }
sboTerm: SBOTerm { use="optional" }
eventAssignment: EventAssignment[1..*]

EventAssignment
variable: SId
sboTerm: SBOTerm { use="optional" }
math: Math { namespace="http://www.w3.org/1998/Math/MathML" }

Figure 19: *The definitions of Event and EventAssignment. Following UML notation, additional fields that are inherited from a base class, in this case Sbase, are not shown.*

4.14.1 Event

An Event definition has three required parts: an identifier, a trigger condition and at least one EventAssignment. In addition there is an optional delay expression. These are described below.

The `id` and `name` Fields

These optional fields are available to support external references to event structures. These fields operate in the manner described in Section 3.4 except that the `id` field is optional.

The `trigger` Field

The `trigger` field defines when the Event structure has an effect on the model. The `trigger` field contains a MathML boolean expression. The exact instant that the expression evaluates to true is the time point when the Event is *fired*. The event only fires when the `trigger` makes the transition from false to true. The event

will fire at any further time points when the `trigger` make this transition.

The `delay` Field

The optional `delay` field defines the length of time after the event has *fired* that the event is *executed*. The `delay` field is another MathML expression. This expression should be evaluated when the rule is *fired*. The default value for the `delay` field is 0. The value of the `delay` field should always be positive. The units of the `delay` field are those given on the `timeUnits` field.

The `timeUnits` Field

The optional field `timeUnits` determines the units of time that apply to the `delay` field. The value of the `timeUnits` field must be either "`second`" or "`dimensionless`" from Table 2 on page 28, "`time`" from Table 3 on page 31, or a new unit defined by a unit definition in the enclosing model which must be a variant of "`second`" units. The default value of the `timeUnits` field is "`time`".

The `sboTerm` Field

The Event structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). The term is associated with the trigger condition on the event. When a value is given to this field, it must be a valid SBO referring to a mathematical expression (i.e., terms derived from `SBO:0000064`, "mathematical expression"). The Event's trigger should have a "is a" relationship with the SBO term, and the term should be the most precise (narrow) term that captures the form of the trigger formula in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore `sboTerm` values. A model must be interpretable without the benefit of SBO labels.

The `eventAssignment` Field

The `eventAssignment` field consists of a non-empty list of EventAssignment structures. This field is implemented as a `listOfEventAssignments` element containing one or more `eventAssignment` elements. The EventAssignment structures represent variable assignments that have effect when the event is *executed*.

4.14.2 EventAssignment

The EventAssignment structure is shown in Figure 19.

The `variable` Field

The `variable` field is of type `SId` and contains the identifier of a variable i.e. a compartment, species or parameter. The `variable` field must not contain the identifier of a reaction. The values of the `variable` field must be unique among the set of EventAssignment structures within an Event structure. The structures referenced by the `variable` field must have their `constant` fields set to "`false`".

A variable cannot be assigned a value in an EventAssignment structure and be assigned a value by an AssignmentRule structure i.e. the value of a `variable` attribute on a EventAssignment structure cannot be the same as the value of a `variable` attribute on a AssignmentRule structure. This restriction is imposed because in the invalid case the EventAssignment is redundant because the variable would assume the value of given by the AssignmentRule.

The `sboTerm` Field

The EventAssignment structure has an optional `sboTerm` field of type `SBOTerm` (see Sections 3.1.8 and 5). When a value is given to this field, it must be a valid SBO term identifier referring to a mathematical expression (i.e., terms derived from `SBO:0000064`, "mathematical expression"). The EventAssignment should have an "is a" relationship with the SBO term, and the term should be the most precise (narrow) term that captures the form of the assignment formula in the model.

As discussed in Section 5, SBO labels are optional information on a model. Applications are free to ignore

`sboTerm` values. A model must be interpretable without the benefit of SBO labels.

The `math` Field

The `math` field contains a MathML expression that defines the new value of the variable. This expression is evaluated when the Event is *fired* but the variable only acquires the result or new value when the Event is *executed*. The order of the EventAssignment structures is not significant; the effect of one assignment cannot affect the result of another assignment. The identifiers occurring in the MathML `ci` fields of the EventAssignment structures represent the value of the identifier at the point when the Event is *fired*.

In all cases, as would be expected, the units of the formula in an EventAssignment are identical to the units associated with the `variable` field, when that variable appears in other formulas. However, the precise details, which are identical to those of AssignmentRule structures, depend on the variable that is being set:

- *In the case of a species*, an EventAssignment sets the referenced species' quantity (*concentration* or *amount of substance*) to the value determined by the formula in `math`. The units of the formula are the *units of the species* as defined in Section 4.8.5.
- *In the case of a compartment*, an EventAssignment sets the referenced compartment's size to the size determined by the formula in `math`. The overall units of the formula are the units specified for the size of the compartment identified by the value of the EventAssignment's `variable` field. (See Section 4.7.5 for an explanation of how the units of the compartment's size are determined.)
- *In the case of a parameter*, an EventAssignment sets the referenced parameter's value to that determined by the formula in `math`. The overall units of the formula are the units defined for the parameter identified by the value of the EventAssignment's `variable` field. (See Section 4.9.3 for an explanation of how the units of the parameter are determined.)

4.14.3 Example Event Structure

A example of an Event structure follows. This structure makes the assignment $k_2 = 0$ at the point when $P_1 \leq t$:

```
<event>
    <trigger>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
                <leq/>
                <ci> P1 </ci>
                <ci> t </ci>
            </apply>
        </math>
    </trigger>
    <listOfEventAssignments>
        <eventAssignment variable="k2">
            <math xmlns="http://www.w3.org/1998/Math/MathML">
                <cn> 0 </cn>
            </math>
        </eventAssignment>
    <listOfEventAssignments>
</event>
```

A complete example of a model using events is given in Section 7.9.

4.14.4 Detailed Semantics of Events

The description of events above describes the action of events in isolation from each other. This section describes how events interact. Events whose `trigger` expression is true at the start of a simulation do not *fire* at the start of the simulation. Events *fire* only when the trigger *becomes* true, i.e. the trigger expression transitions from false to true. It is possible for events to *fire* other events, i.e. an event assignment can cause an event to *fire*, therefore it is possible for model to be entirely encoded in Event structures.

Any transition of a `trigger` expression from false to true will cause an `event` to *fire*. Consider an `event` E with delay d where the `trigger` expression makes a transition from false to true at times t_1 and t_2. The EventAssignment structure will have effect at $t_1 + d$ and $t_2 + d$ irrespective of the relative times of t_1 and t_2. For example events can "overlap" so that $t_1 < t_2 < t_1 + d$ still causes an event assignments to occur at $t_1 + d$ and $t_2 + d$.

It is entirely possible for two events to be *executed* simultaneously in simulated time. It is assumed that, although the precise time at which these events are *executed* is not resolved beyond the given point in simulated time, the order in which the events occur is resolved. This order can be significant in determining the overall outcome of a given simulation. SBML Level 2 does not define the algorithm for determining this order (the tie-breaking algorithm). As a result, the results of simulations involving events may vary when simultaneous events occur during simulation. It is anticipated that future versions or levels of SBML will define a specific set of tie-breaking algorithms and a mechanism for models to indicate which algorithm should be applied during simulation.

Despite the absence of a specific tie-breaking algorithm, SBML event simulation is constrained as follows. When an event X *fires* another event Y and event Y has zero delay then event Y is added to the existing set of simultaneous events that are pending *execution*. Events such as Y do not have a special priority or ordering within the tie-breaking algorithm. Events X and Y form a cascade of events at the same point in simulation time. All events in a model are open to being in a cascade. The position of an event in the event list does not affect whether it can be in the cascade: Y can be triggered whether it is before or after X in the list of events. A cascade of events can be infinite (never terminate). When this occurs a simulator should indicate this has occurred, i.e. it is incorrect for the simulator to arbitrarily break the cascade and continue the simulation without at least indicating the infinite cascade occurred. A variable can change more than once when processing simultaneous events at simulation time t. The model behavior (output) for such a variable is the value of the variable at the end of processing all the simultaneous events at time t.

It is not possible for an event to be triggered when simulation time is zero ($t = 0$). All variables are nominally assumed to have their initial conditions at any time before $t = 0$ (to do otherwise assumes simulation before $t = 0$). The time symbol can never have a negative value. As result no transition in variable values or expressions can occur at $t = 0$ and thus no events can be triggered at that point in simulation time.

5 The Systems Biology Ontology and the sboTerm Field

The values of `id` fields on SBML components allow the components to be cross-referenced within a model. The values of `name` fields on SBML components provide meaningful labels suitable for display to humans (Section 3.4). The specific identifiers and labels used in a model necessarily must be unrestricted by SBML, so that software and users are free to pick whatever they need. However, this freedom makes it more difficult for software tools to interpret models without additional human intervention. For example, there is nothing inherent in a parameter with identifier "`k`" that would indicate to a software tool it is a first-order rate constant (if that's what "`k`" happened to be in some given model). An advanced software tool *might* be able to deduce the purposes of some model components by detailed analysis of the kinetic rate expressions and other parts of the model, but this quickly becomes infeasible for any but the simplest of models.

An approach to solving this problem is to associate model components with terms from a regulated, controlled vocabulary (CV). This is the purpose of the optional `sboTerm` field provided on the SBML classes Model, Parameter, InitialAssignment, AlgebraicRule, AssignmentRule, RateRule, Constraint, Reaction, KineticLaw, SpeciesReference, ModifierSpeciesReference, Event, and EventAssignment . In this section, we discuss the `sboTerm` field, the motivations and theory behind its introduction, and guidelines for its use.

The Systems Biology Ontology is not part of SBML; it is being developed separately, to allow the modeling community to evolve the ontology independently of SBML. However, the terms in the ontology are being designed with SBML components in mind, and are classified into subsets that can be related one-to-one with SBML components such as reaction rate expressions, parameters, and a few others.

5.1 Principles

Labeling model components with terms from a shared controlled vocabulary allows a software tool to identify each component using identifiers that are not tool-specific. An example of where this is useful is the desire by many software developers to provide users with meaningful names for reaction rate equations. Software tools with model editing interfaces frequently provide these names in menus or lists of choices for users. However, without a standardized set of names or identifiers shared between developers, a given software package cannot reliably interpret the names or identifiers of reactions in models written by other tools.

The first solution that might come to mind is to stipulate that certain common reactions always have the same name (e.g., "Michaelis-Menten"), but this is simply impossible to do: not only do humans often disagree on the names themselves, but it would not allow for correction of errors or updates to the list of predefined names except by issuing new revisions of the SBML specification—to say nothing of many other limitations with this approach. Moreover, the parameters and variables that appear in rate expressions also need to be identified in a way that software tools can interpret mechanically, implying that the names of these entities would also need to be regulated.

The Systems Biology Ontology (SBO) provides vocabularies for identifying common reaction rate expressions, common reactant/product/modifier roles in reactions, common parameter types and their roles in rate expressions, and common modeling frameworks (e.g., "continuous", "discrete", etc.). The relationship implied by an `sboTerm` value on an SBML model component is "is a": the thing defined by that SBML component "is a" instance of the thing defined in SBO having the identifier given by the `sboTerm` field value. By adding SBO term references on the components of a model, a software tool can provide additional details using an independent, shared vocabulary that can enable *other* software tools to recognize precisely what the component is meant to be. Those tools can then act on that information. For example, if the SBO identifier `SBO:0000049` is assigned to the concept of "first-order irreversible mass-action kinetics, continuous framework", and a given KineticLaw object in a model has an `sboTerm` field with this value, then regardless of the identifier and name given to the reaction itself, a software tool could use this to inform users that the reaction is a first-order irreversible mass-action reaction. This kind of reverse engineering of the meaning of reactions in a model would be difficult to do otherwise, especially for more complex reaction types.

The presence of the label on a kinetic expression can also allow software tools to make more intelligent decisions about rate laws. For example, an application could recognize certain identifiers as being ones it knows how to solve with optimized procedures. The application could then use internal, optimized code

implementing the rate laws indexed by identifiers such as `SBO:0000049` appearing in SBML models.

Although the use of SBO labels can be beneficial, it is critical to keep in mind that the presence of an `sboTerm` value on an object *must not change the fundamental mathematical meaning* of the model. An SBML model must be defined such that it stands on its own and does not depend on additional information added by SBO terms for a correct mathematical interpretation. SBO term definitions will not imply any alternative mathematical semantics for any SBML structure labeled with that term. Two important reasons motivate this principle. First, it would be too limiting to require that all software tools be able to understand the SBO vocabularies in addition to understanding SBML Level 2 Version 2. Supporting SBO is not only additional work for the software developer; for some kinds of applications, it may not make sense. If the SBO terms on a model are optional, it follows that the SBML model *must* remain unambiguous and fully interpretable without them, because an application reading the model may ignore the terms. Second, we believe allowing the use of `sboTerm` to alter the mathematical meaning of a model would give software authors too much leeway to shoehorn inconsistent concepts into SBML structures, ultimately reducing the interoperability of the models.

5.2 Using SBO and `sboTerm`

The `sboTerm` field data type is always `SBOTerm`, defined in Section 3.1.8. When present in a given model object instance, the field's value must be an identifier taken from the Systems Biology Ontology (SBO; `http://www.biomodels.net/SBO/`). This identifier must refer to a single SBO term that best defines the entity encoded by the SBML object in question. An example of the type of relationship intended is: *the KineticLaw in reaction R1 is a first-order irreversible mass action rate law.*

Note the careful use of the words "defines" and "entity encoded by the SBML object" in the paragraph above. As mentioned, the relationship between the SBML object and the URI is:

> The "thing" encoded by this SBML object *is an* instance of the "thing" represented by the referenced SBO term.

5.2.1 The Structure of the Systems Biology Ontology

The goal of SBO labeling for SBML is to clarify to the fullest extent possible the nature of each reaction rate equation in a model. The approach taken in SBO begins with a hierarchically-structured set of controlled vocabularies with four main divisions: (1) modeling framework, (2) participant role, (3) quantitative parameter, and (4) mathematical expression. Figure 20 illustrates the highest level of SBO.

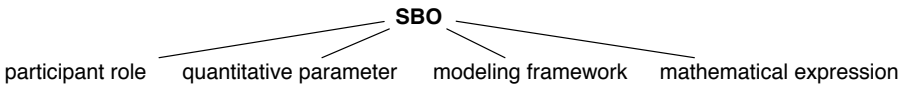

Figure 20: *The four controlled vocabularies (CVs) that make up the main branches of SBO. (Other CVs in SBO may evolve in time, but are not discussed here.)*

Each of the four branches of Figure 20 have a hierarchy of terms underneath them. At this time, we can only begin to list some initial concepts and terms in SBO; what follows is not meant to be complete, comprehensive or even necessarily consistent with future versions of SBO. The web site for SBO (`http://www.biomodels.net/SBO/`) should be consulted for the current version of the ontology. Section 5.4.1 describes how the impact of SBO changes on software applications is minimized.

Figure 21 shows the anticipated structure for the *participant role* CV which reflects the hierarchical conceptual groupings of the concepts. For example, in reaction rate expressions, there are a variety of possible modifiers. Some classes of modifiers can be further subdivided and grouped. All of this is easy to capture in the CV. As more agreement is reached in the modeling community about how to define and name modifiers for different cases, the CV can grow to accommodate it.

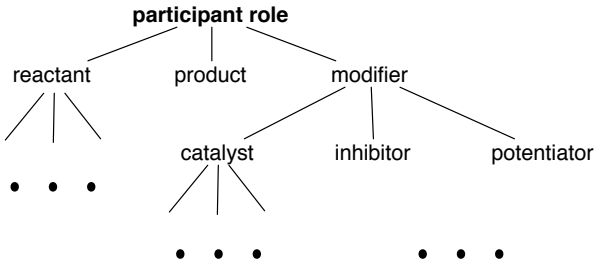

Figure 21: *Partial expansion of some of the terms in the* participant role *CV of SBO.*

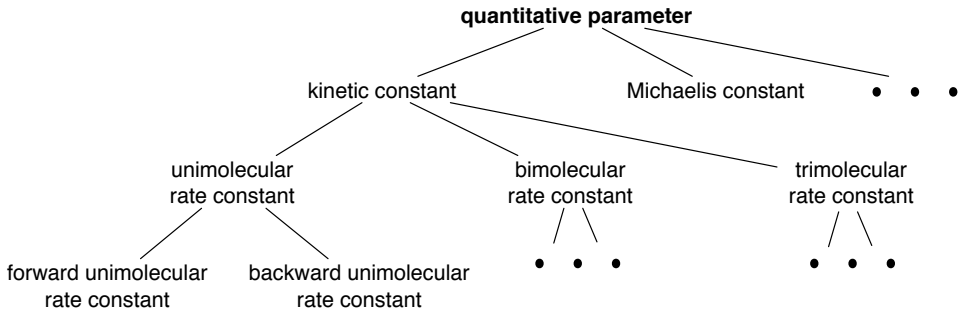

Figure 22: *Partial expansion of some of the terms in the* quantitative parameter *CV.*

Similar to the above, the controlled vocabulary for quantitative parameters also has a hierarhical structure, as illustrated in Figure 22. Note the separation of *kinetic constant* into separate terms for unimolecular, bimolecular, etc. reactions, as well as for for forward and reverse reactions. The need to have separate terms for forward and reverse rate constants arises in reversible mass-action reactions. This distinction is not always necessary for all quantitative parameters; for example, there is no comparable concept for the Michaelis constant. Another distinction for some quantitative parameters is a decomposition into different versions based on the modeling framework being assumed. For example, different terms for continuous and discrete formulations of kinetic constants represent specializations of the constants for particular simulation frameworks. Not all quantitative parameters will need to be distinguished along this dimension.

The *modeling framework* controlled vocabulary is needed to support labeling models and reactions with the framework for which they are designed. Figure 23 illustrates the structure of this CV, which is at this point extremely simple, but we expect that more terms will evolve in the future.

Figure 23: *Partial expansion of some of the terms in the* modeling framework *CV.*

Finally, there is the *mathematical expression* framework. This controlled vocabulary encompasses the various mathematical expressions that constitute a model. Figure 24 illustrates a portion of the hierarchy. Rate law formulas are part of the mathematical expression hierarchy, and subdivided by successively more refined distinctions until the leaf terms represent precise statements of common reaction types. Other types of mathematical expressions are likely to be included in order to be able to characterize other mathematical components of a model, namely initial assignments, assignment rules, rate rules, algebraic rules, constraints, and event triggers and assignments.

The leaf terms of the rate law portion of the SBO mathematical expression framework contain the mathematical formulas for the rate laws encoded using MathML 2.0. There are many potential uses for this. One is to allow a software application to obtain the formula and insert it into a model. In effect, the formulas given in the CV act as templates for what to put into an SBML KineticLaw definition. The MathML definition also acts as a precise statement about the rate law in question.

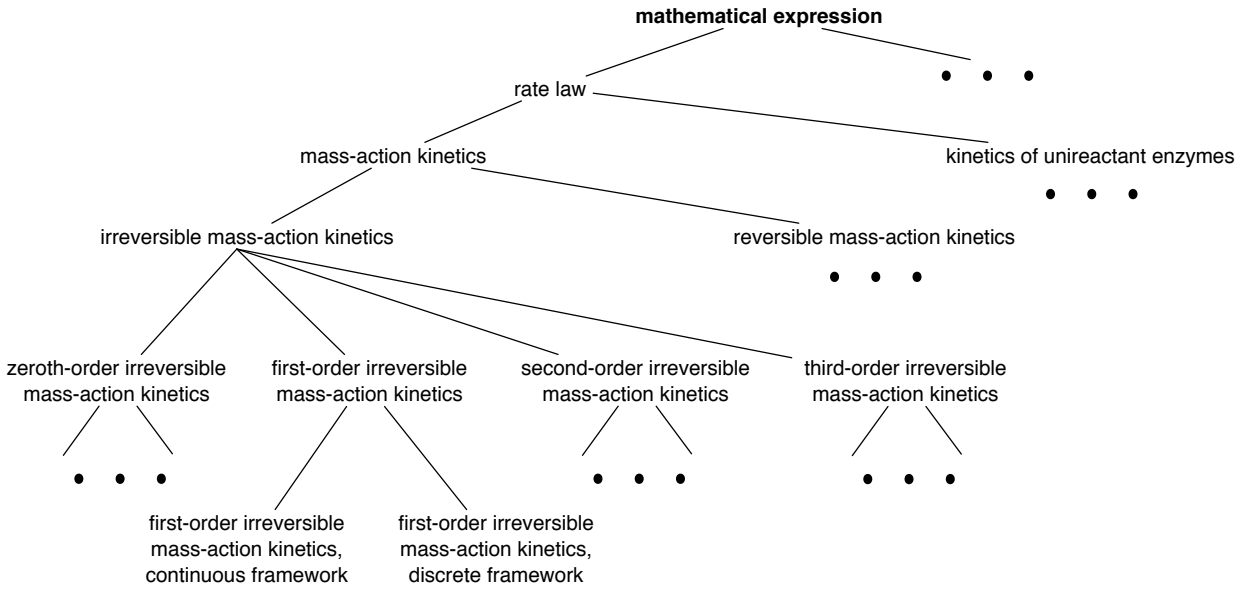

Figure 24: *Partial expansion of some of the terms in the* mathematical expression *CV.*

To make this discussion concrete, here is an example definition of an entry in the SBO rate law hierarchy at the time of this writing. This term represents second-order, irreversible, mass-action kinetics with one reactant, formulated for use in a continuous modeling framework:

> *ID*: SBO:0000052
>
> *Name*: second order irreversible mass action kinetics, one reactant, continuous scheme
>
> *Definition*: Reaction scheme where the products are created from the reactants and the change of a product quantity is proportional to the product of reactant activities. The reaction scheme does not include any reverse process that creates the reactants from the products, and the change of a product quantity is proportional to the square of one reactant quantity. It is to be used in a reaction modelled using a continuous framework.
>
> *Parent(s)*: SBO:0000052, first-order irreversible mass-action kinetics (is a)
>
> *MathML*:

```
<math xmlns="http://www.w3.org/1998/Math/MathML">
   <lambda>
     <bvar><ci definitionURL="http://biomodels.net/SBO/SBO:0000036">k</ci></bvar>
     <bvar><ci definitionURL="http://biomodels.net/SBO/SBO:0000010">R</ci></bvar>
     <apply>
         <times/>
         <ci>k</ci>
         <ci>R</ci>
         <ci>R</ci>
     </apply>
   </lambda>
</math>
```

In the MathML definition of the term shown above, the bound variables in the `lambda` expression are tagged with references to terms in the SBO quantitative parameter (for `k`) and SBO participant role (for `R`) vocabularies. This makes it possible for software applications to interpret the intended meanings of the parameters in the expression.

One of the goals of SBO is to permit a tool to traverse up and down the hierarchy in order to find equivalent terms in different frameworks. The hope is that when a software tool encounters a given rate formula in a

model, the formula will be a specific form (say, "mass-action kinetics, second order, one reactant, for discrete simulation"), but by virtue of the consistent organization of the reaction rate CV into framework-specific definitions, the tool should in principle be able to determine the definitions for other frameworks (say, "mass-action kinetics, second order, one reactant for *continuous* simulation"). If the software tool is designed for continuous simulation and it encounters an SBML model with rate laws formulated for discrete simulation, it could in principle look up the rate laws' identifiers in the CV and search for alternative definitions intended for discrete simulation. And of course, the converse is true, for when a tool designed for discrete simulation encounters a model with rate laws formulated for continuous simulation.

5.2.2 Relationships Between Individual SBML Components and SBO Terms

The availability of `sboTerm` fields on various SBML components is limited to those for which an SBO label is appropriate given the goals and principles of SBO's use in SBML (Section 5.1). Table 6 summarizes the relationship between SBML components having `sboTerm` fields and the vocabularies within SBO that apply to that component.

SBML Component	SBO Vocabulary	Parent SBO Identifier
Model	modeling framework	SBO:0000004
Reaction	modeling framework	SBO:0000004
Parameter	quantitative parameter	SBO:0000002
SpeciesReference	participant role	SBO:0000003
ModifierSpeciesReference	participant role	SBO:0000003
KineticLaw	mathematical expression	SBO:0000064
InitialAssignment	mathematical expression	SBO:0000064
AlgebraicRule	mathematical expression	SBO:0000064
AssignmentRule	mathematical expression	SBO:0000064
RateRule	mathematical expression	SBO:0000064
Constraint	mathematical expression	SBO:0000064
Event	mathematical expression	SBO:0000064
EventAssignment	mathematical expression	SBO:0000064

Table 6: *SBML components and the main types of SBO terms that may be assigned to them. The parent identifiers are provided for guidance, but actual annotations should use more specific child terms. See text for explanation.*

The parent identifiers shown in Table 6 are provided for reference. They are the highest-level terms in their respective vocabularies; however, these are *not* the terms that would be used to annotate an element in SBML, because there are more specific terms underneath the parents shown here. A software tool should use the most specific SBO term available for a given concept rather than using the top-level identifier acting as the root of that particular vocabulary.

5.3 Relationships to the SBML `annotation` Field

Another means of providing this kind of information would be to place it inside the `annotation` field (Sections 3.3 and 6). Although `sboTerm` is just another kind of optional annotation in SBML, the SBO references are separated out and given a separate field on SBML components, both to simplify their use for software tools and because they assert a slightly stronger and more focused connection in a more regimented fashion. SBO term references are intended to allow a modeler to make a statement of the form "this object is identical to meaning and intention to the definition of X in the SBO vocabulary" and do so in a way that a *software tool can interpret unambiguously.*

5.3.1 Tradeoffs in Using SBO Terms

The SBO-based approach to annotating SBML components with controlled terms has the following strengths:

1. The syntax is minimally intrusive and maximally simple, requiring only one string-valued attribute.

2. It supports a significant fraction of what SBML users have wanted to do with controlled vocabularies.

3. It does not interfere with any other scheme. The more general annotation-based approach described in Section 6 can still be used simultaneously in the same model.

The scheme has the following weaknesses:

1. An object can only have one `sboTerm` field, therefore, it can only be related to a single term in SBO. (This also impacts the design of SBO: it must be structured such that a class of SBML elements can logically only be associated with one class of terms in the ontology.)

2. The only relationship that can be expressed by `sboTerm` is "is a". It is not possible to represent different relationships (known as *verbs* in ontology-speak). This limits what can be expressed.

The weaknesses are not shared by the annotation scheme described in Section 6. If an application's needs cannot be met using SBO terms, software developers should examine the approach described in Section 6.

5.3.2 When to Use SBO and When to Use Other Annotations

The general annotation guidelines described in Section 6 could also be used to make references to SBO terms. However, in the interest of making the use of SBO in SBML maximally interoperable between software tools, the best-practice recommendation is to place SBO references in the `sboTerm` field rather than in the `annotation` field of an object.

Some software applications may have their own vocabulary of terms similar in purpose to SBO. For maximal software interoperability, the best-practice recommendation in SBML is nonetheless to use SBO terms in preference to using application-specific annotation schemes. Software applications should therefore attempt to translate their private terms to and from SBO terms when writing and reading SBML, respectively.

5.4 Additional Discussion

Here we discuss some additional points about the SBO-based approach.

5.4.1 Frequency of Change in the Ontology

The SBO development approach follows conventional ontology development approaches in bioinformatics. One of the principles being followed is that identifiers and meanings of terms in the CVs never change and the terms are never deleted. Where some terms are deemed obsolete, the introduction of new terms refine or supercede existing terms, but the existing identifiers are left in the CV. Thus, references never end up pointing to nonexistent entries. In the case where synonymous terms are merged after agreement that multiple terms are identical, the term identifiers are again left in the CV and they still refer to the same concept as before. Out-of-date terms cached or hard-coded by an application remain usable in all cases. (Also, with machine-readable CV encodings and appropriate software design, it should be possible to develop API libraries that automatically map older terms to newer terms as the CVs evolve.)

Therefore, a model is never in danger of ending up with SBO identifiers that cannot be dereferenced. If an application finds an old model with a term `SBO:0000065`, it can be assured that it will be able to find this term in SBO, even if it has been superceded by other, more preferred terms.

5.4.2 Consistency of Information

If you have a means of linking (say) a reaction rate formula to a term in a CV, is it possible to have an inconsistency between the formula in the SBML model and the one defined for the CV term? Yes, but this is not a new problem; it arises in other situations involving SBML models already. The guideline for these situations is that the model must be self-contained and stand on its own. Therefore, in cases where they differ, the definitions in the SBML model take precedence over the definitions referenced by the CV. In other words, the model (and its MathML) is authoritative.

5.4.3 Implications for Network Access

Must a software tool have the ability to access the network or read the CV every time it encounters a model or otherwise works with SBML? No. Since the SBO will likely stabilize and change infrequently once a core set of terms is defined, applications can cache the controlled vocabulary and not make network accesses to the master SBO copy unless something forces them to (e.g., detecting a reference in a model to an SBO term that the application does not recognize). In addition, applications could have user preference settings indicating how often the CV definitions should be refreshed (similar to how modern applications provide a setting dictating how often they should check for new versions of themselves). Simple applications may go further and hard code references to terms in SBO that have reached stability and community consensus.

5.4.4 Implications for Software Tools

What if a software tool does not pay attention to the SBO annotations described here? Then one is faced with exactly the situation that exists today: the SBML model must be interpreted as-is, without benefit of the information added by the SBO terms. The purpose of introducing an ontology scheme and guidelines for its use is to give tools enough information that they *could* perform added processing, if they were designed to take advantage of that information.

5.4.5 Is Another Ontology Really Needed?

It may seem that developing a new, separate ontology is overkill for the intended purpose. However, it turns out that no existing ontology contains the necessary details for this role in SBML. In particular, none of the existing ontologies provide mathematical formulas for rate laws.

6 A Standard Format for the annotation Field

This section describes the standard non-proprietary format for `annotation` elements when (a) referring to controlled vocabulary terms and database identifiers which define and describe biological and biochemical entities; and (b) describing the creator of a model and its modification history. Such a structured format should facilitate the generation of models compliant with the MIRIAM standard of model curation (Le Novère et al., 2005).

This format should *not* be used to refer to SBO terms (Section 5), because SBO defines terms about mathematical modelling constructs and not the biological and biochemical entities that the mathematics represent.

This format uses a restricted form of Dublin Core (Dublin Core Metadata Initiative, 2005) and BioModels qualifier elements (see `http://sbml.org/wiki/Biomodels_Qualifiers`) embedded in RDF (W3C, 2004b). It uses a number of external XML standards and associated XML namespaces. Table 7 lists these namespaces and relevant documentation on those namespaces. The format constrains the order of elements in these namespaces beyond the constraints defined in the standard definitions for those namespaces. For each standard listed, the format only uses a subset of the possible syntax defined by the given standard. Thus it is possible for an `annotation` element to include XML that is compliant with those external standards but is not compliant with the format described here. Parsers wishing to support this format should be aware that a valid `annotation` element may contain an `rdf:RDF` element which is not compliant with the format described here. A parser should check that all aspects of the syntax defined here before assuming that the contained data is encoded in the format.

Namespace Prefix	Namespace URI	Definition Document
`dc`	`http://purl.org/dc/elements/1.1/`	(Powell and Johnston, 2003)
`rdf`	`http://www.w3.org/1999/02/22-rdf-syntax-ns#`	(W3C, 2004a)
`dcterms`	`http://purl.org/dc/terms/`	(Kokkelink and Schwnzl, 2002) (DCMI Usage Board, 2005)
`vcard`	`http://www.w3.org/2001/vcard-rdf/3.0#`	(Iannella, 2001)
`bqbiol`	`http://biomodels.net/biology-qualifiers/`	
`bqmodel`	`http://biomodels.net/model-qualifiers/`	

Table 7: *The XML standards used in the SBML standard format for annotation. The namespace prefix are shown to indicate only the prefix used in the main text.*

6.1 General Syntax fo the standard annotation

An outline of the format syntax is shown below.

```
<SBML_ELEMENT +++ metaid="SBML_META_ID" +++ >
  +++
  <annotation>
    +++
    <rdf:RDF
      xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
      xmlns:dc="http://purl.org/dc/elements/1.1/"
      xmlns:dcterm="http://purl.org/dc/terms/"
      xmlns:vcard="http://www.w3.org/2001/vcard-rdf/3.0#"
      xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"

      xmlns:bqmodel="http://biomodels.net/model-qualifiers/"

    >
      <rdf:Description rdf:about="#SBML_META_ID">
        [MODEL_HISTORY]
        <RELATION_ELEMENT>
          <rdf:Bag>
            <rdf:li rdf:resource="URI" />
```

```
                ...
              </rdf:Bag>
            </RELATION_ELEMENT>
            ...
          </rdf:Description>
          +++
        </rdf:RDF>
        +++
      </annotation>
      +++
    </SBML_ELEMENT>
```

The above outline shows the order of the elements. The capitalized identifiers refer to generic strings of a particular type: `SBML_ELEMENT` refers to any SBML element name that can contain an `annotation` element; `SBML_META_ID` is a XML `ID` string; `RELATION_ELEMENT` refers to a element names in either the namespace `http://biomodels.net/biology-qualifiers/` or `http://biomodels.net/model-qualifiers/`; and `URI` is a URI. `[MODEL_HISTORY]` refers to an optional section described in Section 6.4 which can only be present within SBML model elements. '`+++`' is a placeholder for either no content or valid XML syntax that is not defined by the standard annotation scheme but is consistent with the relevant standards for the enclosing elements. '`...`' is a placeholder for zero or more elements of the same form as the immediately preceding element. The precise form of whitespace and the XML namespace prefix definitions is not constrained. The rest of this section describes the format formally in English.

In this format the annotation of an element is located in a single `rdf:RDF` element contained within an SBML `annotation` element. The annotation element can contain other elements in any order as described in Section *3.3.3*. The format described in this section only defines the form of the `rdf:RDF` element. The containing SBML *Sbase* element must have a `metaid` field value. (As this attribute is of the type `ID` its value must unique to the entire SBML document.)

The first element of the `rdf:RDF` element must be an `rdf:Description` element with an `rdf:about` attribute. (This format doesn't define the form of subsequent elements of the `rdf:RDF` element.) The value of the `rdf:about` attribute must be of the form `#<string>` where the string component is equal to the value of the `metaid` field of the containing SBML element.

The `rdf:Description` element can contain only an optional model history section (see Section 6.4 followed by a sequence of zero or more BioModels relation elements. The optional model history section can only be present within an SBML Model element. The specific type of the relation elements will vary depending on the relationship between the SBML component and referenced information or resource.

Whilst Section 6.3 describes the detailed semantics of each of the relation element types the content of these elements follows exactly the same form. The Biomodels qualifiers relation elements must only contain a single `rdf:Bag` element which in turn must only contain one or more `rdf:li` elements. The `rdf:li` elements must only have a `rdf:resource` attribute containing a URI referring to an information resource (See Section 6.2).

Annotations in this format can be located at different depths within a model component as is appropriate.

6.2 Use of URIs

The format represents a set of relationships between the SBML element and the resources referred to by the contained `rdf:resource` attribute values. The BioModels relation elements simply define the type of the relationship.

For instance a Species element representing a protein could be annotated with a reference to the database UniProt by the `http://www.uniprot.org/#P12999` resource identifier, identifying exactly the protein described by the Species element. This identifier maps to a unique entry in UniProt which is never deleted from the database. In the case of UniProt, this is the "accession" of the entry. When the entry is merged with another one, both "accession" are conserved. Similarly in a controlled vocabulary resource, each term is associated with a perenial identifier. The UniProt entry also possess an "entry name" (the Swiss-Prot "identifier"), a "protein name", "synonyms" etc. Only the "accession" is perennial and should be used.

The value of the rdf:resource attribute is a URI that both uniquely identifies the resource, and the data in the resource. In this case the resource constraining the identifier precedes the '#' symbol and the term or database identifier follows the '#' symbol. In the present example, the resource http://www.uniprot.org/ includes the entry P12999.

The value of the rdf:resource attribute is a URI, not a URL; as such, a URI does not have to reference a physical web object but simply identifies a controlled vocabulary term or database object (a URI is a label that, in this case, just happens to look like a URL). For instance, a true URL for an Internet resource such as http://www.uniprot.org/entry/P12999 might correspond to the URI http://www.uniprot.org/#P12999.

SBML does not specify how a parser is to interpret a URI. In the case of a transformation into a physical URL, there could be several solutions. For instance, the URI http://www.geneontology.org/#GO:0007268 can be translated into:

http://www.ebi.ac.uk/ego/DisplayGoTerm?selected=GO:0007268
http://www.godatabase.org/cgi-bin/amigo/go.cgi?view=details&query=GO:0007268
http://www.informatics.jax.org/searches/GO.cgi?id=GO:0007268

Similarly the URI http://www.ebi.ac.uk/intenz/#EC 3.5.4.4 can refer to:

http://www.ebi.ac.uk/intenz/query?cmd=SearchEC&ec=3.5.4.4
http://www.expasy.org/cgi-bin/nicezyme.pl?3.5.4.4
http://www.chem.qmul.ac.uk/iubmb/enzyme/EC3/5/4/4.html
http://www.genome.jp/dbget-bin/www_bget?ec:3.5.4.4
etc.

To enable interoperability, the community has agreed on an initial set of standardized valid URI syntax rules which may be used within the standard annotation format. This set of rules is not part of the SBML standard but will grow independently from specific SBML Levels and Versions. As the set changes a given URI syntax rule will not be modified although the physical resource associated with the rule may change. These URIs will always be composed as resource#id. The web page http://sbml.org/wiki/MIRIAM_URI_Set lists URI syntaxes and possible physical links to controlled vocabulary and databases. Each entry contains a list of SBML and relation elements in which the given URI can be appropriately embedded. To enable consistent and thus useful links to external resources, the URI syntax rule set must have a consistent view of the concepts represented by the different SBML elements for the purposes of this format. For example as the rule set is designed to link SBML biological and biochemical resources the rule set assumes that a Species element represents the concept of a biochemical entity type rather than mathematical symbol. The URI rule list will evolve with the evolution of databases and resources. The annotation format described in this section does not require software to access this list to operate.

6.3 Relation Elements

To enable the format to encode different types of relationships between SBML elements and resources, different Biomodel qualifier elements are used to enclose a set of rdf:li elements. The relation elements imply a specific relationship between the enclosing SBML element and the resources referenced by the rdf:li elements.

The detailed semantics (i.e. from the perspective of automatic parser) of the relation elements is defined by the URI list at http://sbml.org/wiki/MIRIAM_URI_Set, and thus is outside the scope of SBML. The URI list generally assumes that the biological entity represented by the element is the concept linked to the reference resource.

Several relation elements with a given tag, enclosed in the same SBML element, each represent an alternative annotation to the SBML element. For example two bqbiol:hasPart elements within a Species SBML element represent two different sets of references to the parts making up the the chemical entity represented by the species. (The species is not made up of all the entities represented by all the references combined).

The complete list of the qualifier elements in the Biomodels qualifier namespaces is documented at http://sbml.org/wiki/Biomodels_Qualifiers. The list is divided into two namespaces one for model qualifiers

`http://biomodels.net/biology-qualifiers/` (prefix used here `bqbiol`) and the other for biological qualifiers `http://biomodels.net/model-qualifiers/`) (prefix used here `bqmodel`. This list will only grow i.e no element will be removed from the list. The following is the list of elements at the time of writing:

- `bqmodel:is` The object encoded by the SBML component is the subject of the referenced resource. For instance, this qualifier should be used to link the model to a model database.
- `bqmodel:isDescribedBy` The object encoded by the SBML component is described by the referenced resource. This relation should be used to link SBML components to literature that describes the component.
- `bqbiol:is` The object encoded by the SBML component is the subject of the referenced resource. This relation could be used to link a reaction to its exact counterpart in KEGG or Reactome for instance.
- `bqbiol:hasPart` The object encoded by the SBML component includes the subject of the referenced resource, either physically or logically.
- `bqbiol:isPartOf` The object encoded by the SBML component is a physical or logical part of the subject of the referenced resource.
- `bqbiol:isVersionOf` The object encoded by the SBML component is a version or an instance of the subject of the referenced resource.
- `bqbiol:hasVersion` The subject of the referenced resource is a version or an instance of the object encoded by the SBML component.
- `bqbiol:isHomologTo` The object encoded by the SBML component is a homolog to the referenced resource.

In all cases using the biology qualifiers, the 'object' of the relation is the biological or biochemical object represented by the enclosing SBML element. In the cases of the model qualifiers, the 'object' of the relation is the model component encoded by the enclosing SBML element. The resources referenced by the rdf:li elements contained within the relation element are the 'object' of the relation.

6.4 Model History

When enclosed in an SBML Model element, the format described in previous sections can include additional elements to describe the history of the model. This history data must occur immediately before the first BioModels relation elements. These additional elements encode information on the model creator and a sequence of dates recording changes to the model. The syntax for this section is outlined below.

```
<dc:creator rdf:parseType="Resource">
  <rdf:Bag>
    <rdf:li rdf:parseType="Resource">
      [[
      +++
      <vCard:N rdf:parseType="Resource">
        <vCard:Family>FAMILY_NAME</vCard:Family>
        <vCard:Given>GIVEN_NAME</vCard:Given>
      </vCard:N>
      +++
      [<vCard:EMAIL>EMAIL_ADDRESS</vCard:EMAIL>]
      +++
      [<vCard:ORG>
        <vCard:Orgname>ORGANIZATION_NAME</vCard:Orgname>
      </vCard:ORG>]
      +++
      ]]
    </rdf:li>
    ...
  </rdf:Bag>
</dc:creator>
```

```
<dcterms:created rdf:parseType="Resource">
  <dcterms:W3CDTF>DATE<dcterms:W3CDTF>
</dcterms:created>
<dcterms:modified rdf:parseType="Resource">
  <dcterms:W3CDTF>DATE<dcterms:W3CDTF>
</dcterms:modified>
```

The order of elements is as shown above except that elements of the format contained between `[[` and `]]` can occur in any order. The capitalized identifiers refer to generic strings of a particular type: `FAMILY_NAME` is the family name of a person who created the model; `GIVEN_NAME` is the first name of the same person who created the model; `EMAIL_ADDRESS` is the email address of the same person who created the model; and `ORGANIZATION_NAME` is the name of the organization with which the same person who created the model is affiliated `DATE` is a date in W3C date format (Wolf and Wicksteed, 1998). `W3CDTF`, `N`, `ORG` and `EMAIL` are literal strings. The elements of the format contained between `[` and `]` are optional. '+++' is a placeholder for either no content or valid XML syntax that is not defined by the standard annotation scheme but is consistent with the relevant standards for the enclosing elements. '`...`' is a placeholder for zero or more elements of the same form as the immediately preceding element. The precise form of whitespace and the XML namespace prefix definitions is not constrained. The remaining text in this section describes the syntax formally in English.

The additional elements of the model history sub-format consist in sequence of a `dc:creator` element, a `dcterms:created` element and zero or more `dcterms:modified` elements. All these elements must have the attribute `rdf:parseType` set to `Resource`.

The `dc:creator` element describes the person who created the SBML encoding of the model and contains a single `rdf:Bag` element. The `rdf:Bag` element can contain any number of elements however the first element must be a `rdf:li` element. The `rdf:li` element can contain any number of elements in any order. The set of elements contained with the `rdf:li` element can include the following informative elements: `vCard:N`, `vCard:EMAIL` and `vCard:ORG`. The `vCard:N` contains the name of the creator and must consist of a sequence of two elements: `vCard:Family` and the `vCard:Given` whose content is the family (surname) and given (first) names of the creator respectively. The `vCard:N` must have the attribute `rdf:parseType` set to `Resource`. The content of the `vCard:EMAIL` element must be the email address of the creator. The content of the `vCard:ORG` element must contain a single `vCard:Orgname` element. The `vCard:Orgname` element must contain the name of an organization to which the creator is affiliated.

The `dcterms:created` and `dcterms:modified` elements must each contain a single `dcterms:W3CDTF` element whose content is a date in W3C date format (Wolf and Wicksteed, 1998) which is a a profile of (restricted form of) ISO 8601.

6.5 Examples

The following shows the annotation of a model with model creation data and links to external resources:

```
<model metaid="_180340" id="GMO" name="Goldbeter1991_MinMitOscil">
    <annotation>
        <rdf:RDF
                xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
                xmlns:dc="http://purl.org/dc/elements/1.1/"
                xmlns:dcterms="http://purl.org/dc/terms/"
                xmlns:vCard="http://www.w3.org/2001/vcard-rdf/3.0#"
                xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
                xmlns:bqmodel="http://biomodels.net/model-qualifiers/"
        >
            <rdf:Description rdf:about="#_180340">
                <dc:creator rdf:parseType="Resource">
                    <rdf:Bag>
                        <rdf:li rdf:parseType="Resource">
                            <vCard:N rdf:parseType="Resource">
                                <vCard:Family>Shapiro</vCard:Family>
                                <vCard:Given>Bruce</vCard:Given>
                            </vCard:N>
                            <vCard:EMAIL>bshapiro@jpl.nasa.gov</vCard:EMAIL>
```

```
                                <vCard:ORG>
                                    <vCard:Orgname>NASA Jet Propulsion Laboratory</vCard:Orgname>
                                </vCard:ORG>
                            </rdf:li>
                        </rdf:Bag>
                    </dc:creator>
                    <dcterms:created rdf:parseType="Resource">
                        <dcterms:W3CDTF>2005-02-06T23:39:40</dcterms:W3CDTF>
                    </dcterms:created>
                    <dcterms:modified rdf:parseType="Resource">
                        <dcterms:W3CDTF>2005-09-13T13:24:56</dcterms:W3CDTF>
                    </dcterms:modified>
                    <bqmodel:is>
                        <rdf:Bag>
                            <rdf:li rdf:resource="http://www.ebi.ac.uk/biomodels/#BIOMD0000000003"/>
                        </rdf:Bag>
                    </bqmodel:is>
                    <bqmodel:isDescribedBy>
                         <rdf:Bag>
                             <rdf:li rdf:resource="http://www.ncbi.nlm.nih.gov/PubMed/#1833774"/>
                         </rdf:Bag>
                    <bqmodel:isDescribedBy>
                    <bqbiol:isVersionOf>
                        <rdf:Bag>
                            <rdf:li rdf:resource="http://www.genome.jp/kegg/pathway/#hsa04110"/>
                            <rdf:li rdf:resource="http://www.reactome.org/#69278"/>
                        </rdf:Bag>
                    </bqbiol:isVersionOf>
            </rdf:Description>
        </rdf:RDF>
    </annotation>
```

The following example shows a Reaction structure annotated with a reference to its exact Reactome counterpart.

```
<reaction id="cdc2Phospho" metaid="jb007">
  <annotation>
    <rdf:RDF
      xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
      xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
    >
      <rdf:Description rdf:about="#jb007">
        <bqbiol:is>
          <rdf:Bag>
            <rdf:li rdf:resource="http://www.reactome.org/#170156"/>
          </rdf:Bag>
        </bqbiol:is>
      </rdf:Description>
    </rdf:RDF>
  </annotation>
  <listOfReactants>
    <speciesReference species="cdc2"/>
  </listOfReactants>
  <listOfProducts>
    <speciesReference species="cdc2-Y15P"/>
  </listOfProducts>
  <listOfModifiers>
    <modifierSpeciesReference species="wee1"/>
  </listOfModifiers>
</reaction>
```

The following example describes a species that represents a complex between the protein calmodulin and calcium ions:

```
<species id="Ca_calmodulin" metaid="cacam">
  <annotation>
    <rdf:RDF
      xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
```

```
        xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
      >
        <rdf:Description rdf:about="#cacam">
          <bqbiol:hasPart>
            <rdf:Bag>
              <rdf:li rdf:resource="http://www.uniprot.org/#P62158"/>
              <rdf:li rdf:resource="http://www.genome.jp/kegg/compound/#C00076"/>
            </rdf:Bag>
          </bqbiol:hasPart>
        </rdf:Description>
      </rdf:RDF>
    </annotation>
  </species>
```

The following example describes a species that represents either "Calcium/calmodulin-dependent protein kinase type II alpha chain" or "Calcium/calmodulin-dependent protein kinase type II beta chain". This is the case for instance in the somatic cytoplasm of striatal medium-size spiny neurons, where both are present but they cannot be functionally differentiated.

```
  <species id="calcium_calmodulin" metaid="cacam">
    <annotation>
      <rdf:RDF
        xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
        xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
      >
        <rdf:Description rdf:about="#cacam">
          <bqbiol:hasVersion>
            <rdf:Bag>
              <rdf:li rdf:resource="http://www.uniprot.org/#Q9UQM7"/>
              <rdf:li rdf:resource="http://www.uniprot.org/#Q13554"/>
            </rdf:Bag>
          </bqbiol:hasVersion>
        </rdf:Description>
      </rdf:RDF>
    </annotation>
  </species>
```

The above approach should not be used to describe "any Calcium/calmodulin-dependent protein kinase type II chain" because such an annotation requires references to the products of other genes such as gamma or delta. All the known proteins could be enumerated but such an approach would almost surely lead to inaccuracies due to the evolution of biological knowledge. Instead the annotation should refer to a generic information such as Ensembl family ENSF00000000194 "CALCIUM/CALMODULIN DEPENDENT KINASE TYPE II CHAIN" or PIR superfamily PIRSF000594 "Calcium/calmodulin-dependent protein kinase type II".

The following two examples show how to use the qualifier `is Version Of`. The first example is the relationship between a reaction and an EC code. An EC code describes an enzymatic activity and an enzymatic reaction involving a particular enzyme can be seen as an instance of this activity. For instance the following reaction represents the phosphorylation of a glutamate receptor by a complex calcium/calmodulin kinase II.

```
  <reaction id="NMDAR_phosphorylation" metaid="thx1138">
    <annotation>
      <rdf:RDF
        xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
        xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
      >
        <rdf:Description rdf:about="#thx1138">
          <bqbiol:isVersionOf>
            <rdf:Bag>
              <rdf:li rdf:resource="http://www.ebi.ac.uk/intenz/#EC 2.7.1.17"/>
            </rdf:Bag>
          </bqbiol:isVersionOf>
        </rdf:Description>
      </rdf:RDF>
    </annotation>
    <listOfReactants>
```

```
        <speciesReference species="NMDAR"/>
      </listOfReactants>
      <listOfProducts>
        <speciesReference species="P-NMDAR"/>
      </listOfProducts>
      <listOfModifiers>
        <modifierSpeciesReference species="CaMKII"/>
      </listOfModifiers>
      <kineticLaw>
        <math xmlns="http://www.w3.org/1998/Math/MathML">
          <apply>
            <times/>
            <ci>CaMKII</ci>
            <ci>kcat</ci>
            <apply>
              <divide/>
              <ci>NMDAR</ci>
              <apply>
                </times>
                <ci>NMDAR</ci>
                <ci>Km</ci>
              </apply>
            </apply>
          </apply>
        </math>
        <listOfParameters>
          <parameter id="kcat" value="1"/>
          <parameter id="Km" value="5e-10"/>
        </listOfParameters>
      </kineticLaw>
    </reaction>
```

The second example of the use of isVersionOf is the complex between Calcium/calmodulin-dependent protein kinase type II alpha chain and Calcium/calmodulin, that is only one of the "calcium- and calmodulin-dependent protein kinase complexes" described by the Gene Ontology term GO:0005954.

```
    <species id="CaCaMKII" metaid="C8H10N4O2">
      <annotation>
        <rdf:RDF
          xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
          xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
        >
          <rdf:Description rdf:about="#C8H10N4O2">
            <bqbiol:isVersionOf>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.geneontology.org/#GO:0005954"/>
              </rdf:Bag>
            </bqbiol:isVersionOf>
          </rdf:Description>
        </rdf:RDF>
      </annotation>
    </species>
```

The previous case is different form the following one, although they could seem similar at first sight. The "Calcium/calmodulin-dependent protein kinase type II alpha chain" is a part of the above mentioned "calcium- and calmodulin-dependent protein kinase complex".

```
    <species id="CaMKIIalpha" metaid="C10H14N2">
      <annotation>
        <rdf:RDF
          xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
          xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
        >
          <rdf:Description rdf:about="#C10H14N2">
            <bqbiol:isPartOf>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.geneontology.org/#GO:0005954"/>
              </rdf:Bag>
```

```
            </bqbiol:isPartOf>
          </rdf:Description>
        </rdf:RDF>
      </annotation>
    </species>
```

It is possible describe a component with several alternative sets of qualified annotations. For instance, the following species represents a pool of GMP, GDP and GDP. We annotate it with the three corresponding KEGG compound identifiers but also with the three corresponding ChEBI identifiers.

```
    <species id="GXP" metaid="GXP">
      <annotation>
        <rdf:RDF
          xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
          xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
        >
          <rdf:Description rdf:about="#GXP">
            <bqbiol:hasVersion>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/#CHEBI:17345"/>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/#CHEBI:17552"/>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/#CHEBI:17627"/>
              </rdf:Bag>
            </bqbiol:hasVersion>
            <bqbiol:hasVersion>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/compound/#C00035"/>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/compound/#C00044"/>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/compound/#C00144"/>
              </rdf:Bag>
            </bqbiol:hasVersion>
          </rdf:Description>
        </rdf:RDF>
      </annotation>
    </species>
```

The following example presents a reaction being actually the combination of three different elementary molecular reactions. We annotate it with the three corresponding KEGG reaction, but also with the three corresponding enzymatic activities. It is important to note that the two hasPart elements represent two alternative annotations. The process represented by the Reaction structure is composed of three parts, and not six parts.

```
    <reaction id="adenineProd" metaid="adeprod">
      <annotation>
        <rdf:RDF
          xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
          xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
        >
          <rdf:Description rdf:about="#adeprod">
            <bqbiol:hasPart>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/intenz/#EC 2.5.1.22"/>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/intenz/#EC 3.2.2.16"/>
                <rdf:li rdf:resource="http://www.ebi.ac.uk/intenz/#EC 4.1.1.50"/>
              </rdf:Bag>
            </bqbiol:hasPart>
            <bqbiol:hasPart>
              <rdf:Bag>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/reaction/#R00178"/>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/reaction/#R01401"/>
                <rdf:li rdf:resource="http://www.genome.jp/kegg/reaction/#R02869"/>
              </rdf:Bag>
            </bqbiol:hasPart>
          </rdf:Description>
        </rdf:RDF>
      </annotation>
    </reaction>
```

It is possible to mix different URIs in a given set. The following example presents two alternative annotations of the human hemoglobine, the first with ChEBI heme and the second with KEGG heme.

```
<species id="heme" metaid="heme">
  <annotation>
    <rdf:RDF
      xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
      xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
    >
     <rdf:Description rdf:about="#heme">
       <bqbiol:hasPart>
         <rdf:Bag>
           <rdf:li rdf:resource="http://www.uniprot.org/#P69905"/>
           <rdf:li rdf:resource="http://www.uniprot.org/#P68871"/>
           <rdf:li rdf:resource="http://www.ebi.ac.uk/#CHEBI:17627">
         </rdf:Bag>
       </bqbiol:hasPart>
       <bqbiol:hasPart>
         <rdf:Bag>
          <rdf:li rdf:resource="http://www.uniprot.org/#P69905"/>
           <rdf:li rdf:resource="http://www.uniprot.org/#P68871"/>
           <rdf:li rdf:resource="http://www.genome.jp/kegg/compound/#C00032"/>
         </rdf:Bag>
       </bqbiol:hasPart>
     </rdf:Description>
   </rdf:RDF>
  </annotation>
</species>
```

It is possible to mix different qualified sets in the same annotation element. The following phosphorylation is annotated by its exact KEGG counterpart and by the generic GO term “phosphorylation”.

```
<reaction id="phosphorylation" metaid="phosphorylation">
  <annotation>
    <rdf:RDF
      xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
      xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
    >
      <rdf:Description rdf:about="#phosphorylation">
        <bqbiol:is>
          <rdf:Bag>
            <rdf:li rdf:resource="http://www.genome.jp/kegg/reaction/#R03313" />
          </rdf:Bag>
        </bqbiol:is>
        <bqbiol:isVersionOf>
          <rdf:Bag>
            <rdf:li rdf:resource="http://www.geneontology.org/#GO:0016310" />
          </rdf:Bag>
        </bqbiol:isVersionOf>
      </rdf:Description>
    </rdf:RDF>
  </annotation>
</reaction>
```

7 Example Models Expressed in XML Using SBML

In this section, we present several examples of complete models encoded in XML using SBML Level 2.

7.1 A Simple Example Application of SBML

Consider the following representation of an enzymatic reaction:

$$E + S \underset{k_{\mathrm{off}}}{\overset{k_{\mathrm{on}}}{\rightleftharpoons}} ES \xrightarrow{k_{\mathrm{cat}}} E + P$$

The following is the minimal SBML document encoding the model shown above:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="2" xmlns="http://www.sbml.org/sbml/level2/version2">
    <model name="EnzymaticReaction">
        <listOfCompartments>
            <compartment id="cytosol" size="1e-14"/>
        </listOfCompartments>
        <listOfSpecies>
            <species compartment="cytosol" id="ES" initialAmount="0" name="ES" />
            <species compartment="cytosol" id="P" initialAmount="0" name="P" />
            <species compartment="cytosol" id="S" initialAmount="1e-20" name="S" />
            <species compartment="cytosol" id="E" initialAmount="5e-21" name="E" />
        </listOfSpecies>
        <listOfReactions>
            <reaction id="veq">
                <listOfReactants>
                    <speciesReference species="E"/>
                    <speciesReference species="S"/>
                </listOfReactants>
                <listOfProducts>
                    <speciesReference species="ES"/>
                </listOfProducts>
                <kineticLaw>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <times/>
                            <ci>cytosol</ci>
                            <apply>
                                <minus/>
                                <apply>
                                    <times/>
                                    <ci>kon</ci>
                                    <ci>E</ci>
                                    <ci>S</ci>
                                </apply>
                                <apply>
                                    <times/>
                                    <ci>koff</ci>
                                    <ci>ES</ci>
                                </apply>
                            </apply>
                        </apply>
                    </math>
                    <listOfParameters>
                        <parameter id="kon" value="1000000"/>
                        <parameter id="koff" value="0.2"/>
                    </listOfParameters>
                </kineticLaw>
            </reaction>
            <reaction id="vcat" reversible="false" >
                <listOfReactants>
                    <speciesReference species="ES"/>
                </listOfReactants>
                <listOfProducts>
                    <speciesReference species="E"/>
                    <speciesReference species="P"/>
```

```
                    </listOfProducts>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci>cytosol</ci>
                                <ci>kcat</ci>
                                <ci>ES</ci>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="kcat" value="0.1"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

In this example, the model has the identifier "EnzymaticReaction". The model contains one compartment (with identifier "cytosol"), four species (with identifiers "ES", "P", "S", and "E"), and two reactions ("veq" and "vcat"). The elements in the <listOfReactants> and <listOfProducts> in each reaction refer to the names of elements listed in the <listOfSpecies>. The correspondences between the various elements is explicitly stated by the <speciesReference> elements.

The model also features local parameter definitions in each reaction. In this case, the three parameters ("kon", "koff", "kcat") all have unique identifiers and they could also have just as easily been declared global parameters in the model. Local parameters frequently become more useful in larger models, where it may become tedious to assign unique identifiers for all the different parameters.

7.2 Example Involving Units

The following model uses the units features of SBML Level 2. In this model, the default value of substance is changed to be mole units with a scale factor of -3, or millimoles. This sets the default substance units in the model. The size and time built-ins are left to their defaults, meaning size is in litres and time is in seconds. The result is that, in this model, kinetic law formulas define rates in millimoles per second and the species symbols in them represent concentration values in millimoles per litres. All the species elements set the initial amount of every given species to 1 millimole. The parameters Vm and Km are defined to be in millimoles per litres per second, and milliMoles per litres, respectively.

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2"
      xmlns:xhtml="http://www.w3.org/1999/xhtml">
    <model>
        <listOfUnitDefinitions>
            <unitDefinition id="substance">
                <listOfUnits>
                    <unit kind="mole" scale="-3"/>
                </listOfUnits>
            </unitDefinition>
            <unitDefinition id="mmls">
                <listOfUnits>
                    <unit kind="mole" scale="-3"/>
                    <unit kind="litre" exponent="-1"/>
                    <unit kind="second" exponent="-1"/>
                </listOfUnits>
            </unitDefinition>
            <unitDefinition id="mml">
                <listOfUnits>
                    <unit kind="mole" scale="-3"/>
                    <unit kind="litre" exponent="-1"/>
                </listOfUnits>
            </unitDefinition>
        </listOfUnitDefinitions>
        <listOfCompartments>
```

```
        <compartment id="cell" size="1"/>
    </listOfCompartments>
    <listOfSpecies>
        <species id="x0" compartment="cell" initialConcentration="1"/>
        <species id="x1" compartment="cell" initialConcentration="1"/>
        <species id="s1" compartment="cell" initialConcentration="1"/>
        <species id="s2" compartment="cell" initialConcentration="1"/>
    </listOfSpecies>
    <listOfParameters>
        <parameter id="vm" value="2" units="mmls"/>
        <parameter id="km" value="2" units="mml"/>
    </listOfParameters>
    <listOfReactions>
        <reaction id="v1">
            <listOfReactants>
                <speciesReference species="x0"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="s1"/>
            </listOfProducts>
            <kineticLaw>
                <notes>
                    <xhtml:p>((vm * s1)/(km + s1))*cell</xhtml:p>
                </notes>
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <apply>
                            <divide/>
                            <apply>
                                <times/>
                                <ci> vm </ci>
                                <ci> s1 </ci>
                            </apply>
                            <apply>
                                <plus/>
                                <ci> km </ci>
                                <ci> s1 </ci>
                            </apply>
                        </apply>
                        <ci> cell </ci>
                    </apply>
                </math>
            </kineticLaw>
        </reaction>
        <reaction id="v2">
            <listOfReactants>
                <speciesReference species="s1"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="s2"/>
            </listOfProducts>
            <kineticLaw>
                <notes>
                    <xhtml:p>((vm * s2)/(km + s2))*cell</xhtml:p>
                </notes>
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <apply>
                            <divide/>
                            <apply>
                                <times/>
                                <ci> vm </ci>
                                <ci> s2 </ci>
                            </apply>
                            <apply>
                                <plus/>
                                <ci> km </ci>
```

```
                                    <ci> s2 </ci>
                                </apply>
                            </apply>
                            <ci> cell </ci>
                        </apply>
                    </math>
                </kineticLaw>
            </reaction>
            <reaction id="v3">
                <listOfReactants>
                    <speciesReference species="s2"/>
                </listOfReactants>
                <listOfProducts>
                    <speciesReference species="x1"/>
                </listOfProducts>
                <kineticLaw>
                    <notes>
                        <xhtml:p>((vm * x1)/(km + x1))*cell</xhtml:p>
                    </notes>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <times/>
                            <apply>
                                <divide/>
                                <apply>
                                    <times/>
                                    <ci> vm </ci>
                                    <ci> x1 </ci>
                                </apply>
                                <apply>
                                    <plus/>
                                    <ci> km </ci>
                                    <ci> x1 </ci>
                                </apply>
                            </apply>
                            <ci> cell </ci>
                        </apply>
                    </math>
                </kineticLaw>
            </reaction>
        </listOfReactions>
    </model>
</sbml>
```

7.3 Example Involving Assignment Rules

This section contains a model that simulates a system containing a fast reaction. This model uses rules to express the mathematics of the fast reaction explicitly rather than using the implicit `fast` field on a reaction element.

The system modeled is

$$X_0 \xrightarrow{k_1 X_0} S_1$$

$$S_1 \xrightarrow{k_f S_1 - k_r S_2} S_2$$

$$S_2 \xrightarrow{k_2 S_2} X_1$$

$$k_1 = 0.1, \quad k_2 = 0.15, \quad k_f = K_{eq}10000, \quad k_r = 10000, \quad K_{eq} = 2.5.$$

This can be approximated with the following system:

$$X_0 \xrightarrow{k_1 X_0} T$$

$$T \xrightarrow{k_2 S_2} X_1$$

$$S_1 = \frac{T}{1 + K_{eq}}, \quad S_2 = K_{eq} S_1$$

The following example SBML model encodes the approximate form.

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2"
      xmlns:math="http://www.w3.org/1998/Math/MathML">
    <model>
        <listOfCompartments>
            <compartment id="cell" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="X0" compartment="cell" initialConcentration="1"/>
            <species id="X1" compartment="cell" initialConcentration="0"/>
            <species id="T" compartment="cell" initialConcentration="0"/>
            <species id="S1" compartment="cell" initialConcentration="0"/>
            <species id="S2" compartment="cell" initialConcentration="0"/>
        </listOfSpecies>
        <listOfParameters>
            <parameter id="Keq" value="2.5"/>
        </listOfParameters>
        <listOfRules>
            <assignmentRule variable="S1">
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <divide/>
                        <ci> T </ci>
                        <apply>
                            <plus/>
                            <cn> 1 </cn>
                            <ci> Keq </ci>
                        </apply>
                    </apply>
                </math>
            </assignmentRule>
            <assignmentRule variable="S2">
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <ci> Keq </ci>
                        <ci> S1 </ci>
                    </apply>
                </math>
            </assignmentRule>
        </listOfRules>
        <listOfReactions>
            <reaction id="in">
                <listOfReactants>
                    <speciesReference species="X0"/>
                </listOfReactants>
                <listOfProducts>
                    <speciesReference species="T"/>
                </listOfProducts>
                <kineticLaw>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <times/>
                            <ci> k1 </ci>
                            <ci> X0 </ci>
                        </apply>
                    </math>
                    <listOfParameters>
                        <parameter id="k1" value="0.1"/>
                    </listOfParameters>
                </kineticLaw>
            </reaction>
            <reaction id="out">
```

```
                    <listOfReactants>
                        <speciesReference species="T"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="X1"/>
                    </listOfProducts>
                    <listOfModifiers>
                        <modifierSpeciesReference species="S2"/>
                    </listOfModifiers>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci> k2 </ci>
                                <ci> S2 </ci>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="k2" value="0.15"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

7.4 Example Involving Algebraic Rules

This section contains an example model that contains an AlgebraicRule structure. The model contains a different formulation of the fast reaction described in Section 7.3.

The system described in Section 7.3 can be approximated with the following system:

$$X_0 \xrightarrow{k_1 X_0} T$$

$$T \xrightarrow{k_2 S_1} X_1$$

$$S_2 = K_{eq} S_1$$

with the constraint:

$$S_1 + S_2 - T = 0$$

The following example SBML model encodes this approximate form.

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
    <model>
        <listOfCompartments>
            <compartment id="cell" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="X0" compartment="cell" initialConcentration="1"/>
            <species id="X1" compartment="cell" initialConcentration="0"/>
            <species id="T" compartment="cell" initialConcentration="0"/>
            <species id="S1" compartment="cell" initialConcentration="0"/>
            <species id="S2" compartment="cell" initialConcentration="0"/>
        </listOfSpecies>
        <listOfParameters>
            <parameter id="Keq" value="2.5"/>
        </listOfParameters>
        <listOfRules>
            <assignmentRule variable="S2">
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
```

```
                            <times/>
                            <ci> Keq </ci>
                            <ci> S1 </ci>
                        </apply>
                    </math>
                </assignmentRule>
                <algebraicRule>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <minus/>
                            <apply>
                                <plus/>
                                <ci> S2 </ci>
                                <ci> S1 </ci>
                            </apply>
                            <ci> T </ci>
                        </apply>
                    </math>
                </algebraicRule>
            </listOfRules>
            <listOfReactions>
                <reaction id="in">
                    <listOfReactants>
                        <speciesReference species="X0"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="T"/>
                    </listOfProducts>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci> k1 </ci>
                                <ci> X0 </ci>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="k1" value="0.1"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
                <reaction id="out">
                    <listOfReactants>
                        <speciesReference species="T"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="X1"/>
                    </listOfProducts>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci> k2 </ci>
                                <ci> S2 </ci>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="k2" value="0.15"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

7.5 Example with Combinations of boundaryCondition and constant Values on Species with RateRule Structures

This section contains a model that includes four species each with a different combination of values of for the boundaryCondition and constant fields.

Consider the following hypothetical system:

$$S_1 + S_2 \xrightarrow{k_1 S_1 S_2 S_3} S_4$$

S_3 is a catalyst that catalyzes the conversion S_1 and S_2 into S_4. S_1 and S_2 are on the boundary of the system (S_1 and S_2 are reactants but their values are not determined by a kinetic law). The value of S_1 is determined over time by the rate rule:

$$\frac{dS_1}{dt} = k_2$$

Constant values are:

$$S_2 = 1$$

$$S_3 = 2$$

$$k_1 = 0.5$$

$$k_2 = 0.1$$

and initial values are:

$$S_1 = 0$$

$$S_4 = 0$$

The value of S_1 varies over time so in SBML S_1 has a constant field with a default value of "false". The values of S_2 and S_3 are fixed so in SBML they have a constant field values of "true". S_3 only occurs as a modifier so the value of its boundaryCondition field can default to false. S_4 is a product whose value is determined by a kinetic law and therefore in the SBML representation has false values, the default values, for both boundaryCondition and constant fields.

The following is the XML document that encodes the model shown above:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
    <model id="BoundaryCondExampleModel">
        <listOfCompartments>
            <compartment id="compartmentOne" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="S1" initialConcentration="0" compartment="compartmentOne"
                boundaryCondition="true" />
            <species id="S2" initialConcentration="1" compartment="compartmentOne"
                boundaryCondition="true" constant="true" />
            <species id="S3" initialConcentration="3" compartment="compartmentOne"
                constant="true"/>
            <species id="S4" initialConcentration="0" compartment="compartmentOne"/>
        </listOfSpecies>
        <listOfParameters>
            <parameter id="k1" value="0.5"/>
            <parameter id="k2" value="0.1"/>
        </listOfParameters>
        <listOfRules>
            <rateRule variable="S1">
```

```
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <ci> k2 </ci>
                     </math>
                </rateRule>
            </listOfRules>
            <listOfReactions>
                <reaction id="reaction_1" reversible="false">
                    <listOfReactants>
                        <speciesReference species="S1"/>
                        <speciesReference species="S2"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="S4"/>
                    </listOfProducts>
                    <listOfModifiers>
                        <modifierSpeciesReference species="S3"/>
                    </listOfModifiers>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci> k1 </ci>
                                <ci> S1 </ci>
                                <ci> S2 </ci>
                                <ci> S3 </ci>
                             </apply>
                        </math>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

7.6 Example of Translation from a Multi-Compartmental Model to ODEs

This section contains a model with 2 compartments and 4 reactions. The model is derived from Lotka-Volterra, with in addition a reversible transport step. When instantiated, this model displays dampened oscillations of three of the species.

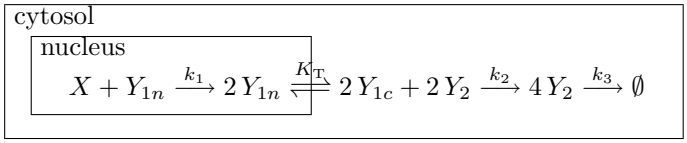

Figure 25: *A example multi-compartmental model.*

The model `LotkaVolterra_tranport` is illustrated in Figure 25. The SBML representation of the model is shown below, and is followed by its complete translation into ordinary differential equations. In this SBML model, the reaction equations are in substance per time units. The reactions have also been simplified to reduce common stoichiometric factors. The species variables are in concentration units; their initial quantities are declared using the attribute `initialAmount` on the `species` definitions, but since the attribute `hasOnlySubstanceUnits` is *not* set to true, the symbols of the species represent their concentrations. The species with identifier "`X`" is a boundary condition. Note the attribute `speciesType`="`Y`" that tells us species "`Y1n`" and "`Y1c`" are pools of the same participant, but located in different compartments.

```
    <?xml version="1.0" encoding="UTF-8"?>
    <sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
        <model name="LotkaVolterra_tranport">
            <listOfSpeciesTypes>
                <speciesType id="Y1" />
            </listOfSpeciesTypes>
            <listOfCompartments>
```

```
        <compartment id="cytoplasm" size="5"/>
        <compartment id="nucleus" outside="cytoplasm" size="1" />
    </listOfCompartments>
    <listOfSpecies>
        <species id="X" compartment="nucleus" initialAmount="1"
                        constant="true" boundaryCondition="true" />
        <species id="Y1n" compartment="nucleus" speciesType="Y1" initialAmount="1" />
        <species id="Y1c" compartment="nucleus" speciesType="Y1" initialAmount="0" />
        <species id="Y2" compartment="cytoplasm" initialAmount="1" />
    </listOfSpecies>
    <listOfParameters>
        <parameter id="k1" value="2500" />
        <parameter id="k2" value="2500" />
        <parameter id="kT" value="25000" />
        <parameter id="k3" value="2500" />
    </listOfParameters>
    <listOfReactions>
        <reaction id="production" reversible="false">
            <listOfReactants>
                <speciesReference species="X"/>
                <speciesReference species="Y1n"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="Y1n"/>
                <speciesReference species="Y1n"/>
            </listOfProducts>
            <kineticLaw>
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <ci>nucleus</ci>
                        <ci>k1</ci>
                        <ci>X</ci>
                        <ci>Y1n</ci>
                    </apply>
                </math>
            </kineticLaw>
        </reaction>
        <reaction id="transport" reversible="true">
            <listOfReactants>
                <speciesReference species="Y1n"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="Y1c"/>
            </listOfProducts>
            <kineticLaw>
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <apply>
                        <times/>
                        <ci>cytoplasm</ci>
                        <ci>kT</ci>
                        <apply>
                            <minus/>
                            <ci>Y1n</ci>
                            <ci>Y1c</ci>
                        </apply>
                    </apply>
                </math>
            </kineticLaw>
        </reaction>
        <reaction id="transformation" reversible="false">
            <listOfReactants>
                <speciesReference species="Y1c"/>
                <speciesReference species="Y2"/>
            </listOfReactants>
            <listOfProducts>
                <speciesReference species="Y2"/>
                <speciesReference species="Y2"/>
            </listOfProducts>
```

```
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci>cytoplasm</ci>
                                <ci>k2</ci>
                                <ci>Y1c</ci>
                                <ci>Y2</ci>
                            </apply>
                        </math>
                    </kineticLaw>
                </reaction>
                <reaction id="degradation" reversible="false">
                    <listOfReactants>
                        <speciesReference species="Y2"/>
                    </listOfReactants>
                    <kineticLaw>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <times/>
                                <ci>cytoplasm</ci>
                                <ci>k3</ci>
                                <ci>Y2</ci>
                            </apply>
                        </math>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

The ODE translation of this model is as follows. The species variables in the following equations are all in terms of concentrations. First, we give the values of the constant parameters:

$$
\begin{aligned}
k_1 &= 2500 \\
k_2 &= 2500 \\
K_3 &= 25000 \\
K_T &= 2500
\end{aligned}
$$

Initial conditions of variables:

$$
\begin{aligned}
V_n &= 1 \\
V_c &= 5 \\
X &= Y1_n = Y2 = 1
\end{aligned}
$$

And finally, the differential equations:

$$\frac{dX}{dt} = 0$$

$$\frac{dY1_n}{dt} = \frac{k_1 \times X \times Y1_n \times V_n - K_T \times (Y1_n - Y1_c) \times V_c}{V_n} \quad \text{reactions production and transport}$$

$$\frac{dY1_c}{dt} = \frac{K_T \times (Y1_n - Y1_c) \times V_c - k_2 \times Y1_c \times Y2 \times V_c}{V_c} \quad \text{reactions transport and transformation}$$

$$\frac{dY2}{dt} = \frac{k_2 \times Y1_c \times Y2 \times V_c - k_3 \times Y2 \times V_c}{V_c} \quad \text{reactions transformation and degradation}$$

7.7 Example Involving Function Definitions

This section contains a model that uses the function definition feature of SBML. Consider the following hypothetical system:

$$S_1 \xrightarrow{f(S_1)} S_2$$

where

$$f(x) = x * 2$$

The following is the XML document that encodes the model shown above:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
    <model id="Example">
        <listOfFunctionDefinitions>
            <functionDefinition id="f">
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                    <lambda>
                        <bvar><ci> x </ci></bvar>
                        <apply>
                            <times/>
                            <ci> x </ci>
                            <cn> 2 </cn>
                        </apply>
                    </lambda>
                </math>
            </functionDefinition>
        </listOfFunctionDefinitions>
        <listOfCompartments>
            <compartment id="compartmentOne" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="S1" initialConcentration="1" compartment="compartmentOne"/>
            <species id="S2" initialConcentration="0" compartment="compartmentOne"/>
        </listOfSpecies>
        <listOfReactions>
            <reaction id="reaction_1" reversible="false">
                <listOfReactants>
                    <speciesReference species="S1"/>
                </listOfReactants>
                <listOfProducts>
                    <speciesReference species="S2"/>
                </listOfProducts>
                <kineticLaw>
                    <math xmlns="http://www.w3.org/1998/Math/MathML">
                        <apply>
                            <ci> f </ci>
                            <ci> S1 </ci>
                         </apply>
                    </math>
                </kineticLaw>
            </reaction>
        </listOfReactions>
    </model>
</sbml>
```

7.8 Example Involving *delay* Functions

The following is a simple model illustrating the use of *delay* to represent a gene that suppresses its own expression. The model can be expressed in a single rule:

$$\frac{dP}{dt} = \frac{\frac{1}{1 + m(P_{delayed})^q} - P}{\tau}$$

where

$P_{delayed}$	is $delay(P, \Delta_t)$ or P at $t - \Delta_t$
P	is protein concentration
τ	is the response time
m	is a multiplier or equilibrium constant
q	is the Hill coefficient

The SBML form of this model is as follows:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
    <model>
        <listOfCompartments>
            <compartment id="cell" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="P" compartment="cell" initialConcentration="0"/>
        </listOfSpecies>
        <listOfParameters>
            <parameter id="tau" value="1"/>
            <parameter id="m" value="0.5"/>
            <parameter id="q" value="1"/>
            <parameter id="delta_t" value="1"/>
        </listOfParameters>
        <listOfRules>
            <rateRule variable="P">
                <math xmlns="http://www.w3.org/1998/Math/MathML">
                 <apply>
                  <divide/>
                  <apply>
                   <minus/>
                   <apply>
                    <divide/>
                    <cn> 1 </cn>
                    <apply>
                     <plus/>
                     <cn> 1 </cn>
                     <apply>
                      <times/>
                      <ci> m </ci>
                      <apply>
                       <power/>
                       <apply>
                        <csymbol encoding="text"
                                 definitionURL="http://www.sbml.org/sbml/symbols/delay">
                            delay
                        </csymbol>
                        <ci> P </ci>
                        <ci> delta_t </ci>
                       </apply>
                       <ci> q </ci>
                      </apply>
                     </apply>
                    </apply>
                   </apply>
                   <ci> P </ci>
                  </apply>
                  <ci> tau </ci>
                 </apply>
                </math>
            </rateRule>
        </listOfRules>
    </model>
</sbml>
```

7.9 Example Involving Events

This section presents a simple model system that demonstrates the use of events in SBML. Consider a system with two genes, k_1 and k_2. k_1 is initially on and k_2 is initially off. When turned on, the two genes lead to the production of two products, P_1 and P_2, respectively, at a fixed rate. When P_1 reaches a given concentration, k_2 switches off. This system can be represented mathematically as follows:

$$\begin{aligned} \frac{dP_1}{dt} &= k_1 - P_1 \\ \frac{dP_2}{dt} &= k_2 - P_2 \\ k_2 &= \begin{cases} 0 & \text{when } P_1 \leq \tau, \\ 1 & \text{when } P_1 > \tau. \end{cases} \end{aligned}$$

The initial values are:

$$k_1 = 1 \quad k_2 = 0 \quad \tau = 0.25 \quad P_1 = 0 \quad P_2 = 0$$

The SBML Level 2 representation of this as follows:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2"
      xmlns:math="http://www.w3.org/1998/Math/MathML">
    <model>
        <listOfCompartments>
            <compartment id="cell" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species id="P1" compartment="cell" initialConcentration="0"/>
            <species id="P2" compartment="cell" initialConcentration="0"/>
        </listOfSpecies>
        <listOfParameters>
            <parameter id="k1" value="1" constant="false"/>
            <parameter id="k2" value="0" constant="false"/>
            <parameter id="tau" value="0.25"/>
        </listOfParameters>
        <listOfRules>
            <rateRule variable="P1">
                <math:math>
                    <math:apply>
                        <math:minus/>
                        <math:ci> k1 </math:ci>
                        <math:ci> P1 </math:ci>
                    </math:apply>
                </math:math>
            </rateRule>
            <rateRule variable="P2">
                <math:math>
                    <math:apply>
                        <math:minus/>
                        <math:ci> k2 </math:ci>
                        <math:ci> P2 </math:ci>
                    </math:apply>
                </math:math>
            </rateRule>
        </listOfRules>
        <listOfEvents>
            <event>
                <trigger>
                    <math:math>
                        <math:apply>
                            <math:gt/>
                            <math:ci> P1 </math:ci>
                            <math:ci> tau </math:ci>
                        </math:apply>
```

```
                    </math:math>
                </trigger>
                <listOfEventAssignments>
                    <eventAssignment variable="k2">
                        <math:math>
                            <math:cn> 1 </math:cn>
                        </math:math>
                    </eventAssignment>
                </listOfEventAssignments>
            </event>
            <event>
                <trigger>
                    <math:math>
                        <math:apply>
                            <math:leq/>
                            <math:ci> P1 </math:ci>
                            <math:ci> tau </math:ci>
                        </math:apply>
                    </math:math>
                </trigger>
                <listOfEventAssignments>
                    <eventAssignment variable="k2">
                        <math:math>
                            <math:cn> 0 </math:cn>
                        </math:math>
                    </eventAssignment>
                </listOfEventAssignments>
            </event>
        </listOfEvents>
    </model>
</sbml>
```

7.10 Example Involving Two-Dimensional Compartments

The following example is a model that uses a two-dimensional compartment. It is a fragment of a larger model of calcium regulation across the plasma membrane of a cell. The model includes a calcium influx channel, `Ca_channel`, and a calcium-extruding PMCA pump, `Ca_Pump`. The model also includes two cytosolic proteins that buffer calcium via the `CalciumCalbindin_gt_BoundCytosol` and `CalciumBuffer_gt_BoundCytosol` reactions.

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version2" level="2" version="2">
    <model id="facilitated_ca_diffusion">
        <listOfUnitDefinitions>
            <unitDefinition id="substance">
                <listOfUnits>
                    <unit kind="mole" scale="-6"/>
                </listOfUnits>
            </unitDefinition>
            <unitDefinition id="area">
                <listOfUnits>
                    <unit kind="metre" scale="-6" exponent="2" />
                </listOfUnits>
            </unitDefinition>
        </listOfUnitDefinitions>
        <listOfCompartments>
            <compartment id="Extracellular" spatialDimensions="3" size="1"/>
            <compartment id="PlasmaMembrane" outside="Extracellular" spatialDimensions="2" size="1"/>
            <compartment id="Cytosol" outside="PlasmaMembrane" spatialDimensions="3" size="1"/>
        </listOfCompartments>
        <listOfSpecies>
            <species
              id="CaBPB_C"
              compartment="Cytosol"
              initialConcentration="47.17"/>
            <species
              id="B_C"
```

```
      compartment="Cytosol"
      initialConcentration="396.04"/>
    <species
      id="CaB_C"
      compartment="Cytosol"
      initialConcentration="3.96"/>
    <species
      id="Ca_EC"
      compartment="Extracellular"
      initialConcentration="1000"/>
    <species
      id="Ca_C"
      compartment="Cytosol"
      initialConcentration="0.1"/>
    <species
      id="CaCh_PM"
      compartment="PlasmaMembrane"
      initialConcentration="1"/>
    <species
      id="CaPump_PM"
      compartment="PlasmaMembrane"
      initialConcentration="1"/>
    <species
      id="CaBP_C"
      compartment="Cytosol"
      initialConcentration="202.83"/>
</listOfSpecies>
<listOfReactions>
    <reaction id="CalciumCalbindin_gt_BoundCytosol" fast="true">
        <listOfReactants>
            <speciesReference species="CaBP_C"/>
            <speciesReference species="Ca_C"/>
        </listOfReactants>
        <listOfProducts>
            <speciesReference species="CaBPB_C"/>
        </listOfProducts>
        <kineticLaw>
                  <notes>
                  <p xmlns="http://www.w3.org/1999/xhtml">
                      (((Kf_CalciumCalbindin_BoundCytosol * CaBP_C) * Ca_C) -
                         (Kr_CalciumCalbindin_BoundCytosol * CaBPB_C))
                  </p>
                  </notes>
            <math xmlns="http://www.w3.org/1998/Math/MathML">
                <apply>
                    <minus/>
                    <apply>
                        <times/>
                        <ci> Kf_CalciumCalbindin_BoundCytosol </ci>
                        <ci> CaBP_C </ci>
                        <ci> Ca_C </ci>
                    </apply>
                    <apply>
                        <times/>
                        <ci> Kr_CalciumCalbindin_BoundCytosol </ci>
                        <ci> CaBPB_C </ci>
                    </apply>
                </apply>
            </math>
                 <listOfParameters>
                    <parameter id="Kf_CalciumCalbindin_BoundCytosol" value="20.0"/>
                    <parameter id="Kr_CalciumCalbindin_BoundCytosol" value="8.6"/>
                 </listOfParameters>
        </kineticLaw>
    </reaction>
    <reaction id="CalciumBuffer_gt_BoundCytosol" fast="true">
        <listOfReactants>
            <speciesReference species="Ca_C"/>
            <speciesReference species="B_C"/>
```

```
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="CaB_C"/>
                    </listOfProducts>
                    <kineticLaw>
                        <notes>
                          <p xmlns="http://www.w3.org/1999/xhtml">
                            (((Kf_CalciumBuffer_BoundCytosol * Ca_C) * B_C) -
                                (Kr_CalciumBuffer_BoundCytosol * CaB_C))
                          </p>
                        </notes>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <minus/>
                                <apply>
                                    <times/>
                                    <ci> Kf_CalciumBuffer_BoundCytosol </ci>
                                    <ci> Ca_C </ci>
                                    <ci> B_C </ci>
                                </apply>
                                <apply>
                                    <times/>
                                    <ci> Kr_CalciumBuffer_BoundCytosol </ci>
                                    <ci> CaB_C </ci>
                                </apply>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="Kf_CalciumBuffer_BoundCytosol" value="0.1"/>
                            <parameter id="Kr_CalciumBuffer_BoundCytosol" value="1.0"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
                <reaction id="Ca_Pump">
                    <listOfReactants>
                        <speciesReference species="Ca_C"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="Ca_EC"/>
                    </listOfProducts>
                    <listOfModifiers>
                        <modifierSpeciesReference species="CaPump_PM"/>
                    </listOfModifiers>
                    <kineticLaw>
                        <notes>
                          <p xmlns="http://www.w3.org/1999/xhtml">
                            ((Vmax * kP * ((Ca_C - Ca_Rest) / (Ca_C + kP)) / (Ca_Rest + kP)) *
                                CaPump_PM)
                          </p>
                        </notes>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <divide/>
                                <apply>
                                    <times/>
                                    <ci> Vmax </ci>
                                    <ci> kP </ci>
                                    <ci> CaPump_PM </ci>
                                    <apply>
                                        <minus/>
                                        <ci> Ca_C </ci>
                                        <ci> Ca_Rest </ci>
                                    </apply>
                                </apply>
                                <apply>
                                    <times/>
                                    <apply>
                                        <plus/>
                                        <ci> Ca_C </ci>
```

```
                                        <ci> kP </ci>
                                    </apply>
                                    <apply>
                                        <plus/>
                                        <ci> Ca_Rest </ci>
                                        <ci> kP </ci>
                                    </apply>
                                </apply>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="Vmax" value="-4000"/>
                            <parameter id="kP" value="0.25"/>
                            <parameter id="Ca_Rest" value="0.1"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
                <reaction id="Ca_channel">
                    <listOfReactants>
                        <speciesReference species="Ca_EC"/>
                    </listOfReactants>
                    <listOfProducts>
                        <speciesReference species="Ca_C"/>
                    </listOfProducts>
                    <listOfModifiers>
                        <modifierSpeciesReference species="CaCh_PM"/>
                    </listOfModifiers>
                    <kineticLaw>
                        <notes>
                          <p xmlns="http://www.w3.org/1999/xhtml">
                            (J0 * Kc * (Ca_EC - Ca_C) / (Kc + Ca_C) * CaCh_PM)
                          </p>
                        </notes>
                        <math xmlns="http://www.w3.org/1998/Math/MathML">
                            <apply>
                                <divide/>
                                <apply>
                                    <times/>
                                    <ci> CaCh_PM </ci>
                                    <ci> J0 </ci>
                                    <ci> Kc </ci>
                                    <apply>
                                        <minus/>
                                        <ci> Ca_EC </ci>
                                        <ci> Ca_C </ci>
                                    </apply>
                                </apply>
                                <apply>
                                    <plus/>
                                    <ci> Kc </ci>
                                    <ci> Ca_C </ci>
                                </apply>
                            </apply>
                        </math>
                        <listOfParameters>
                            <parameter id="J0" value="0.014"/>
                            <parameter id="Kc" value="0.5"/>
                        </listOfParameters>
                    </kineticLaw>
                </reaction>
            </listOfReactions>
        </model>
    </sbml>
```

8 Discussion

The volume of data now emerging from molecular biotechnology leave little doubt that extensive computer-based modeling, simulation and analysis will be critical to understanding and interpreting the data (Abbott, 1999; Gilman, 2000; Popel and Winslow, 1998; Smaglik, 2000). This has lead to an explosion in the development of computer tools by many research groups across the world. The explosive rate of progress is exciting, but the rapid growth of the field is accompanied by problems and pressing needs.

One problem is that simulation models and results often cannot be directly compared, shared or re-used, because the tools developed by different groups often are not compatible with each other. As the field of systems biology matures, researchers increasingly need to communicate their results as computational models rather than box-and-arrow diagrams. They also need to reuse published and curated models as library components in order to succeed with large-scale efforts (e.g., the Alliance for Cellular Signaling; Gilman, 2000; Smaglik, 2000). These needs require that models implemented in one software package be portable to other software packages, to maximize public understanding and to allow building up libraries of curated computational models.

We offer SBML to the systems biology community as a suggested format for exchanging models between simulation/analysis tools. SBML is an open model representation language oriented specifically towards representing systems of biochemical reactions.

Our vision for SBML is to create an open standard that will enable different software tools to exchange computational models. SBML is not static; we continue to develop and experiment with it, and we interact with other groups who seek to develop similar markup languages. We plan on continuing to evolve SBML with the help of the systems biology community to make SBML increasingly more powerful, flexible and useful.

8.1 Future Enhancements: SBML Level 3 and Beyond

As mentioned above, SBML Level 2 is intended to provide a foundation for modeling biochemical networks. Many people have expressed a desire to see additional capabilities added to SBML. The following summarizes additional features that are under consideration to be included in SBML Level 3:

- *Arrays.* This will enable the creation of arrays of components (species, reactions, compartments and submodels).
- *Connections.* This will be a mechanism for describing the connections between items in an array.
- *Geometry.* This will enable the encoding of the spatial characteristics of models including the geometry of compartments, the diffusion properties of species and the specification of different species concentrations across different regions of a cell.
- *Model Composition.* This will enable a large model to be built up out of instances of other models. It will also allow the reuse of model components and the creation of several instances of the same model.
- *Multi-state and Complex Species.* This will allow the straight-forward construction of models involving species with a large number of states or species composed of subcomponents. The representation scheme would be designed to contain the combinatorial explosion of objects that often results from these types of models.
- *Diagrams.* This feature will allow components to be annotated with data to enable the display of the model in a diagram.
- *Dynamic Structure.* This will enable model structure to vary during simulation. One aspect of aspect of this allowing rules and reactions to have their effect conditional on the state of the model system. For example in SBML Level 2 it is possible to create a rule with the effect:

$$\frac{ds}{dt} = \begin{cases} 0 & \text{if } s > 0 \\ y & \text{otherwise} \end{cases}$$

Dynamic restructuring would enable the expression of the following example:

$$\text{if } s > 0 \quad \frac{ds}{dt} = y$$

where s is not determined by the rule when $s \leq 0$.

- *Tie-breaking algorithm.* This will include a controlled vocabulary and associated fields on models to indicate the simultaneous event tie-breaking algorithm required to correctly simulate the model.

Acknowledgments

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The development of SBML was originally funded entirely by the Japan Science and Technology Agency (JST) under the ERATO Kitano Symbiotic Systems Project during the years 2000–2003. The principal investigators were Hiroaki Kitano and John C. Doyle. The original SBML Team was lead by Hamid Bolouri and consisted of Hamid, Andrew Finney, Herbert Sauro, and Michael Hucka.

We gratefully acknowledge sponsorship from many funding agencies. Support for the continued development of SBML and associated software, meetings and activities today comes from the following sources: the National Human Genome Research Institute (USA); grant number GM070923 from the National Institute of General Medical Sciences (USA); the International Joint Research Program of NEDO (Japan); the JST ERATO-SORST Program (Japan); the Japanese Ministry of Agriculture; the Japanese Ministry of Education, Culture, Sports, Science and Technology; the BBSRC e-Science Initiative (UK); the DARPA IPTO Bio-Computation Program (USA); and the Air Force Office of Scientific Research (USA). Additional support has been or continues to be provided by the California Institute of Technology (USA), the University of Hertfordshire (UK), the Molecular Sciences Institute (USA), and the Systems Biology Institute (Japan).

SBML was first conceived at the JST/ERATO-sponsored *First Workshop on Software Platforms for Systems Biology*, held in April, 2000, at the California Institute of Technology in Pasadena, California, USA. The participants collectively decided to begin developing a common XML-based declarative language for representing models. A draft version of the Systems Biology Markup Language was developed by the Caltech ERATO team and delivered to all collaborators in August, 2000. This draft version underwent extensive discussion over mailing lists and then again during the *Second Workshop on Software Platforms for Systems Biology* held in Tokyo, Japan, November 2000. A revised version of SBML was issued by the Caltech ERATO team in December, 2000, and after further discussions over mailing lists and in meetings, we produced a description of SBML Level 1 (Hucka et al., 2001). A journal publication (Hucka et al., 2003) was not produced until much later, on the occasion of the development of Version 2 of Level 1.

SBML Level 2 was conceived at the *5th Workshop on Software Platforms for Systems Biology*, held in July 2002, at the University of Hertfordshire, UK. The participants collectively decided to revise the form of SBML in Level 2. The first draft of the Level 2 Version 1 document was released in August 2002. The final set of features in SBML Level 2 Version 1 was finalized in May 2003 at the *7th Workshop on Software Platforms for Systems Biology* in Ft. Lauderdale, Florida.

SBML Level 2 Version 2 was developed with contributions from so many people constituting the worldwide *SBML Forum* that we regret it has become infeasible to list individuals by name. We are grateful to everyone on the `sbml-discuss` and `libsbml-discuss` mailing lists, the creators of CellML (Hedley et al., 2001), the members of the DARPA Bio-SPICE project, and the authors of the following software SBML-aware systems: BALSA, BASIS, BIOCHAM, BioCharon, biocyc2SBML, BioGrid, BioModels, BioNetGen, BioPathway Explorer, Bio Sketch Pad, BioSens, BioSPICE Dashboard, BioSpreadsheet, BioTapestry, BioUML, BSTLab, CADLIVE, CellDesigner, Cellerator, CellML2SBML, Cellware, CL-SBML, COPASI, Cytoscape, DBsolve, Dizzy, E-CELL, ecellJ, ESS, FluxAnalyzer, Fluxor, Gepasi, INSILICO discovery, JACOBIAN, Jarnac, JDesigner, JigCell, JWS Online, Karyote, KEGG2SBML, Kinsolver, libSBML, MathSBML, MesoRD, MetaboLogica, MetaFluxNet, MMT2, Modesto, Moleculizer, Monod, Narrator, NetBuilder, Oscill8, PANTHER Pathway, PathArt, PathScout, PathwayLab, Pathway Tools, PathwayBuilder, PATIKAweb, PaVESy, PET, PNK, Reactome, ProcessDB, PROTON, pysbml, PySCeS, runSBML, SABIO-RK, SBML ODE Solver, SBMLeditor, SBMLmerge, SBMLR, SBMLSim, SBMLToolbox, SBliD, SBToolbox, SBW, SCIpath, Sigmoid, SigPath, SigTran, SIMBA, SimBiology, Simpathica, SimWiz, SmartCell, SRS Pathway Editor, StochSim, STOCKS, TERANODE Suite, Trelis, Virtual Cell, WinSCAMP, and XPPAUT.

A Differences between SBML Level 1 Version 2 and Level 2 Version 1

Compared to SBML Level 1 Version 2, SBML Level 2 Version 1 introduces the following changes:

- SBML Level 2 supports the inclusion of metadata using the same approach as CellML (Cuellar et al., 2002). All structures in SBML can be annotated with optional content in RDF (Resource Description Format; Lassila and Swick, 1999) following the guidelines put forward by Cuellar et al.. (Section 3.3.)

- All data structures, including Sbml and `listOf`_____ elements, are now derived from the type *Sbase*. (Section 3.3.) This means all major structures in SBML can have separate annotations and metadata associated with them.

- A new field, **`id`**, replaces the **`name`** field previously defined for most SBML structures to identify each part of a model. (See Section 3.4.) The **`id`** field has a type of **`SId`**, whose definition is similar to **`SName`** in Level 1. In SBML Level 2, the **`name`** field is optional and is defined to allow any Unicode characters allowed by the **`string`** type of XML Schema (Biron and Malhotra, 2000).

- Formulas in Level 2 are expressed using MathML (W3C, 2000b) 2.0. The field named **`formula`** previously available on the KineticLaw and *Rule* structures has been replaced by a MathML element named **`math`** containing MathML content. In addition, stoichiometry numbers may now be expressed using MathML, allowing for more flexibility in defining reactions. (Sections 3.5, 4.11 and 4.13.)

- The namespace for identifiers in a model does not contain any built-in symbols; gone, for example, are the predefined rate laws of SBML Level 1. The approach taken in SBML Level 2 is that each model must itself define whatever functions it needs using the new FunctionDefinition mechanism. Although SBML Level 2 *does* define two built-in entities (a symbol representing time and another symbol representing delay functions), these are referenced using a feature of MathML and are not in the same namespace as identifiers defined by a model. (Section 3.5.5.)

- SBML Level 2 makes explicit a previously unstated assumption, that the XML encoding of a model uses UTF-8. SBML documents must refer to the UTF-8 encoding in their XML declaration. (Section 4.1.)

- The top-level Model structure can contain an optional list of global user-defined functions expressed in MathML and organized in new structures of type FunctionDefinition. (Sections 4.2 and 4.3.)

- The top-level Model structure can contain an optional list of event definitions organized in structures of type Event. Events define discrete changes in model behavior at specific times during a time simulation of the model. (Section 4.2 and 4.14.)

- Unlike in SBML Level 1, unit identifiers in Level 2 are in a separate namespace from the namespace used for models, functions, species, compartments, reactions and parameters. Also, the unit names "**`meter`**" and "**`liter`**" are not defined in Level 2 because the SBML user community deemed them unnecessary. Finally, Unit structures now have the additional fields **`multiplier`** and **`offset`** to enable the definition of non-SI units. (Section 4.4.)

- The Compartment structure has a new field, **`spatialDimensions`**, whose value is a positive integer specifying the number of dimensions in space the compartment possesses. This enables the definition of such things as two-dimensional membranes. As a side-effect, the units of species concentration in SBML Level 2 depend on the spatial dimensions of the compartment where the species is located. To support these new capabilities, **`Compartment`** now uses a field named **`size`** instead of **`volume`**, and there are two new built-in units for area and length. (Sections 4.4 and 4.7.)

- All fields representing initial conditions or parameter values, including compartment sizes and species concentrations, are optional in Level 2. A missing value for one of these fields implies that the value is either unknown, not required for analysis, or should be obtained from an external source. (Sections 4.7, 4.8 and 4.9.)

- The Compartment, Species and Parameter structures each have a new boolean field named `constant`. This field specifies whether the variables represented by these structures can be changed by rules and reactions. (Sections 4.7, 4.8 and 4.9.)

- The Species structure has a new field, `initialConcentration`, for setting the initial value of a species in terms of its concentration. This is in addition to the ability, carried over from Level 1, to set the values in terms of amounts. (Section 4.8.)

- The Species structure has two new fields, `spatialSizeUnits` and `substanceUnits`, which replace the `units` field in Level 1. These fields are composed to form the concentration units of the species symbol. (Section 4.8.)

- The rule structures are simpler compared to SBML Level 1. There is no longer a `type` field on AssignmentRule. A redesigned structure AssignmentRule and new RateRule structure replace SBML Level 1's `ParameterRule`, `SpeciesConcentrationRule` and `CompartmentVolumeRule`. (Section 4.11.)

- The Reaction structure has a new list of *modifiers* in addition to the list of reactants and products. The `listOfModifiers` enumerates species that affect a reaction but are neither created nor destroyed by the reaction. (Section 4.13.)

B Differences between SBML Level 2 Version 1 and Level 2 Version 2

The changes introduced by SBML Level 2 Version 2 over SBML Level 2 Version 1 as described by this specification are divided into 2 parts: (a) new and changed features and, (b) Version 1 errata corrected in Version 2.

B.1 Feature Changes Relative to Level 2 Version 1

The features introduced or changed in Version 2 are:

- *XML namespace.* Version 2 uses the XML namespace `http://www.sbml.org/sbml/level2/version2`.
- *Removal of predefined annotation namespaces.* In Section 3.3.3, previous Levels and Versions of SBML reserved a set of XML Namespace names corresponding to software tools known to exist at the time. Due to the explosion of SBML-compatible software tools in recent years, it has become infeasible to maintain such a list; moreover, informal discussions with SBML users revealed that no one paid much attention to the list anyway. Beginning with SBML Level 2 Version 2, no such namespaces are defined in the SBML specification.
- *One top level element per XML Namespace per* `annotation` *element and associated restrictions.* An `annotation` element cannot contain two or more top level elements in the same XML namespace. An `annotation` element cannot contain a top level element in the SBML namespace. The order of top level elements within an `annotation` element is not significant.
- *Introduction of* `sboTerm`. In Version 2, the Model, Parameter, InitialAssignment, AlgebraicRule, AssignmentRule, RateRule, Constraint, Reaction, KineticLaw, SpeciesReference, ModifierSpeciesReference, Event, and EventAssignment structures have an addition field named `sboTerm`. This field is of type `SBOTerm`. Its value is permitted to be only valid Systems Biology Ontology (SBO) identifiers. (Section 5.)
- *New format for linking external resources to SBML.* A new format for using RDF and Dublin Core within `annotation` elements to link SBML models to external resources and record model version history is introduced. Whilst CellML metadata can be included in SBML the specification does not make any specific mention of CellML metadata.
- *Built-in units can be dimensionless.* In Level 2 Version 2, the built-in units (e.g., `substance`, `volume` and others), can be assigned `dimensionless` units. This facilities the correct encoding of models based on dimensionless experimental data.
- *UnitDefinition no longer has an* `offset` *field.* In Version 2, the `offset` field on UnitDefinition has been removed because it was impossible to define consistently with the rest of the SBML unit system. Either a complicated set of special exceptions and rules would have had to be introduced to enable proper interpretation of units with offsets, or the offset field could be removed. Since the situations requiring offsets are so infrequent, removing the offsets was judged to be the lesser of evils. As a benefit, the unit system of SBML Level 2 Version 2 is streamlined and straightforward to implement, which may encourage more software developers to support it.
- *Compartment Type.* In Version 2 the Model structure has an addition list of CompartmentType structures. Each of these structures represents a type of compartment and consists of just `name` and `id` fields. The `id` field can optionally be referenced from an Compartment structure using a new `compartmentType` field.
- *Species Type.* In Version 2 the Model structure has an addition list of SpeciesType structures. A SpeciesType structure represents a type of chemical entity independent of location and consists of just `name` and `id` fields. The `id` field can optionally be referenced from an Species structure using a new `speciesType` field.
- `charge` *field deprecated.* In Version 2 the Species structure `charge` field is deprecated.

- *Constraints.* In Version 2, the Model structure has an addition list of Constraint structures. The `math` field of Constraint contains a boolean expression which is is function of the model state which returns whether the state is valid. Unlike the *Rule* structures Constraint should not be used to compute the dynamical behavior of the model.

- *`Id` on SimpleSpeciesReference .* Version 2 adds `id` and `name` fields to the *SimpleSpeciesReference* structure. The `id` field declares an identifier which is in the global namespace of objects.

- *Reaction identifier as a symbol in math expressions.* In Version 2 the value of the `id` of any reaction can appear in an expression within a MathML `ci` element. The symbol represents the rate of the reaction which is given by the KineticLaw structure of the Reaction. It is not possible to explicitly assign a value to the symbol using InitialAssignment, EventAssignment, AssignmentRule or RateRule structures.

- *Initial Assignment Structures.* In Version 2 the Model structure has an additional list of InitialAssignment structures. This list of structures is evaluated before an reactions or other rules to determine the values of constants and the initial values of variables. Assignment rules override the values calculated by the InitialAssignment structures.

- *The order of AssignmentRule structures is not significant.* In Version 2 the order of AssignmentRule is not significant however the set of assignment rules formed from KineticLaw, InitialAssignment and AssignmentRule structures as a whole must not contain algebraic loops.

- *Strong interpretation of `fast` on Reaction*

  Until Level 2 Version 2, it was assumed that the `fast` field on Reaction could be ignored by software tools that did not have the capacity to support it. Further research has shown that this is not true. SBML Level 2 Version 2 stipulates that if a model has values for `fast`, a software tool must be able to respect the field or else indicate to the user that it does not have the capacity to do so.

B.2 Incorporation of errata from SBML Level 2 Version 1

The errata in the SBML Level 2 Version 1 specification that corrected in this Version 2 specification are as follows. The page and section numbers refer to the final PDF version of the SBML Level 2 Version 1 specification.

- page 1: The specification should contain a link to the latest version of the specification and to this specific *issue* of the document.

- page 2: Each additional errata to the specification should result in an new issue of the specification each with a unique number. The first issue of the specification should be numbered 1. The errata on this specification should recorded in a new section starting in issue 2. Each errata will be numbered with the issue in which the errata is introduced. Errata should not change the fundamental semantics or syntax of SBML but merely clarify and disambiguate the specification.

- page 2: The specification should make explicit the features which are not backwards compatable between Level 2 Version 2 and Level 2 Version 1.

- page 3 Section 1.2: The specification should make explicit the differences in the numeric types of XML Schema and MathML.

- page 4 Section 3.1: This section should include an explanation of why `id` and `name` fields are not present on *Sbase*.

- page 8 Figure 3: Change `nameChar` and `name` to `idChar` and `SId` to indicate clearly the use of the BNF syntax definition.

- page 9 Section 3.6: The specification should reference existing documents to clarify the semantics of the MathML operators in the MathML subset.

- page 9 Section 3.6: The specification should constrain the use of MathML operators which return different types of result (numeric or boolean) appropriately.
- page 9 Section 3.6.1: The `encoding` attribute is permitted on `annotation` and `annotation-xml` elements in MathML, not only on `csymbol` as stated on that page.
- page 9 Section 3.6.1: The MathML 2.0 standard specifies the result of n-ary operators when the number of operands is critically small, for example for `times` and `add` elements, when the number of operands are zero or one. This is an obscure part of MathML and the specification should highlight the relevant sections of the MathML specification.
- page 9 Section 3.6.2: The specification should make explicit the differences in the numeric types of XML Schema and MathML.
- page 9 Section 3.6.2: The specification should describe the MathML whitespace rules for `cn` elements.
- page 10 Section 3.6.3: The specification should describe the MathML whitespace rules for `ci` elements.
- page 10 Section 3.6.3: The specification should state whether SBML has early or late binding semantics.
- page 10, Section 3.6.4: The delay function is not clearly defined. There is no explanation of what range of values is valid for the time. For example, can delay times be less than zero? Also, are there restrictions on the acceptable values of the argument x?
- page 13, Section 4.3.1: The 'can' in the second sentence should be replaced by 'should'.
- page 14, Section 4.4.2: The `id` field of a UnitDefinition structure must not contain a value from Table 2, the table of `UnitKind` values. This restriction is necessary because otherwise a unit definition could redefine one of the base unit kinds.
- page 14, Section 4.4.2: The first formula should be the following:

  $$u_{new} = (multiplier \times 10^{scale} \times u)^{exponent} + offset$$

  This equation is superseded by modifications to the Unit and UnitDefinition structures in this specification SBML Level 2 Version 2.
- page 16, Section 4.4.3: The example code redefining the built-in unit `volume` should replace `liters` with `litre`. `liters` is not a valid value for the `kind` attribute.
- page 18 section 4.5.6: the value of `outside` field for a given Compartment structure must be the value of an `id` field of another Compartment structure.
- page 18 Section 4.5.6: The graph formed where compartments are nodes and the arcs are implied by the values of `outside` attributes must be acyclic otherwise a compartment can be outside itself.
- page 19 Section 4.6.3: On Species elements the `initialConcentration` attribute can have a value even if the `hasOnlySubstanceUnits` attribute is "`true`".
- page 19 Section 4.6.4: This section should contain a table that shows how the units of a species is determined from the spatial dimensions of the species and the value of the `hasOnlySubstanceUnits` attribute.
- page 24 Section 4.8.4: This section should specify that the model should not be overdetermined as defined in Section 4.11.5 of the SBML Level 2 Version 2 specification (i.e. this document).
- page 24 Section 4.8.4: This section should not refer to assignment rules using the term 'scalar rule'.
- page 27 Section 4.9.5: If a species id occurs in any `ci` element MathML element including KineticLaw and StoichiometryMath elements it should appear in a *SimpleSpeciesReference* element in the reaction. The specification only applies this rule to the KineticLaw element. Such a species is at a minimum a modifier of the reaction.

- page 29 Section 4.9.5: The relationship of the abstract class *SimpleSpeciesReference* to the concrete classes SpeciesReference and ModifierSpeciesReference should be made explicit.

- page 29 Section 4.9.6: Despite being redundant it is possible for a species to be referenced from the `modifier` field whilst being referenced from the `product` and/or `reactant` fields of the same reaction.

- page 29 section 4.9.7: 3rd paragraph: The text is overly restrictive and contradictory with respect of the units of species symbols. Species symbols can be either amount or concentration units depending on the species declaration.

- page 29 section 4.9.7: Final paragraph: The kinetic law expression is composed so that the units are of the parameter are not those conventionally used. This is not good practice. The rate law expression should be changed to include the compartment volume so that the units of the parameter are those that would be measured by an experimentalist and used in practice by a modeler.

- page 31 Section 4.10.5: A `variable` attribute on a EventAssignment element should be unique among the set of assignments within an Event element if not the effect of event assignment is ambiguous.

- page 31 Section 4.10.5: A `variable` attribute on a EventAssignment element should not have the same value as a `variable` attribute on a AssignmentRule element.

- page 32 Section 4.10.7: *Any* transition of a `trigger` expression from false to true will cause an `event` to *fire*. Consider an `event` E with delay d where the `trigger` expression makes a transition from false to true at times t_1 and t_2. The EventAssignment structure will have effect at $t_1 + d$ and $t_2 + d$ irrespective of the relative times of t_1 and t_2. For example events can "overlap" so that $t_1 < t_2 < t_1 + d$ still causes event assignments to occur at $t_1 + d$ and $t_2 + d$.

- page 32 Section 4.10.7: Events cannot be triggered at $t = 0$.

- page 34 Section 5.2: The units of parameter `Km` should be moles per litre as the parameter is added to the concentration of a species.

- page 38 Example 5.3: The `out` reaction should have a `listOfModifiers` which refers to species `S2` since it is referenced in the reaction's KineticLaw.

- page 40 Example 5.5: The one rule in `listOfRules` should not use `<apply> ... </apply>`; these tags should be omitted.

- page 42 Example 5.6: The MathML in the two RateRule definitions should not use `<apply> ... </apply>`; these tags should be omitted.

- page 46 Example 5.8: The value of the `definitionURL` attribute on a `csymbol` delay should be `http://www.sbml.org/sbml/symbols/delay`, not `http://www.sbml.org/symbols/delay` (the incorrect form omitted "`sbml`").

- page 55 Appendix A: The appendix states that UML inheritance is mapped, in XML Schema, to the `extension` of `complexType` elements. This is by far the most natural interpretation and the one used in the schema available on the SBML web site and used by libSBML. However, this approach introduced a restriction: an ordering of elements is imposed on all extended types because the definition of XML Schema effectively requires the use of `sequence` ordering in order to be able to use type inheritance in this way. (A full explanation of the details can be found in Section 13.5 of Walmsley (2002)) The result is that the ordering of subelements in SBML XML is important. For example, `notes` and `annotation` elements must occur before `listOfReactants` elements within a Reaction element. Appendix A should state this restriction explicitly. Appendix A should be moved into the main text. The dependence on `sequence` is a result of using XML Schema.

- page 55 Appendix A: The SCHUCS document doesn't state what model group element should be used in the XML schema interpretation of UML. (Examples of XML schema are that `xs:element` elements should be enclosed in `xs:choice`, `xs:all` or `xs:sequence` elements; see p.488 table A-1 of Walmsley

(2002).) To be consistent with the previous errata item, `xs:sequence` elements should be used. (The SBML schemas use this interpretation).

- page 56, Appendix B: The last bullet, second sentence starts: "there is no longer a `type` field on *Rule*". Technically, this should read: "there is no longer a `type` field on AssignmentRule".

C XML Schema for SBML

The following is an XML Schema definition for the SBML Level 2 Version 1, using the W3C Recommendation for XML Schema version 1.0 of 2 May 2001 (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000). This schema does not define all aspects of SBML Level 2: a SBML document validated by this schema is not necessarily a valid SBML Level 2 document. Appendix D contains a a schema for the SBML MathML subset. Appendix E contains a list of the remaining checks required to validate a model that is already consistent with these two schemas.

```
<?xml version="1.0" encoding="UTF-8"?>
<xsd:schema
    targetNamespace="http://www.sbml.org/sbml/level2/version2"
    xmlns="http://www.sbml.org/sbml/level2/version2"
    xmlns:mml="http://www.w3.org/1998/Math/MathML"
    xmlns:xlink="http://www.w3.org/1999/xlink"
    xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
    xmlns:xsd="http://www.w3.org/2001/XMLSchema"
    elementFormDefault="qualified"
    attributeFormDefault="unqualified"
    version="SBML L2 V2">
    <xsd:import
        namespace="http://www.w3.org/1998/Math/MathML"
        schemaLocation="http://www.w3.org/Math/XMLSchema/mathml2/mathml2.xsd"/>
    <xsd:annotation>
        <xsd:documentation>
      File name : sbml.xsd
      Author : M. Hucka, A. Finney, D. Lucio
      Description : XML Schema for the Systems Biology Markup Language Level 2 Version 2
                    This is designed for XML Schema version 1.0.
      Version : 1

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      Inc., 59 Temple Place, Suite 330, Boston, MA 02111-1307 USA.
</xsd:documentation>
    </xsd:annotation>
    <!--The definition of SId follows.-->
    <xsd:simpleType name="SId">
        <xsd:annotation>
            <xsd:documentation>
                The type SId is used throughout SBML as the type of the 'id'
                attributes on model elements.
            </xsd:documentation>
        </xsd:annotation>
        <xsd:restriction base="xsd:string">
            <xsd:pattern value="(_|[a-z]|[A-Z])(_|[a-z]|[A-Z]|[0-9])*"/>
        </xsd:restriction>
    </xsd:simpleType>
    <xsd:simpleType name="SBOTerm">
        <xsd:annotation>
            <xsd:documentation>a string for referring to an SBO term</xsd:documentation>
        </xsd:annotation>
        <xsd:restriction base="xsd:string">
            <xsd:pattern value="(SBO:)([0-9]{7})"/>
```

```
            </xsd:restriction>
        </xsd:simpleType>
        <!--The definition of SBase follows.-->
        <xsd:complexType name="SBase" abstract="true">
            <xsd:annotation>
                <xsd:documentation>
                    The SBase type is the base type of all main components in SBML.
                    It supports attaching metadata, notes and annotations to components.
                </xsd:documentation>
            </xsd:annotation>
            <xsd:sequence>
                <xsd:element name="notes" minOccurs="0">
                    <xsd:complexType>
                        <xsd:sequence>
                            <xsd:any
                                namespace="http://www.w3.org/1999/xhtml"
                                processContents="skip"
                                minOccurs="0"
                                maxOccurs="unbounded"/>
                        </xsd:sequence>
                    </xsd:complexType>
                </xsd:element>
                <xsd:element name="annotation" minOccurs="0">
                    <xsd:complexType>
                        <xsd:sequence>
                            <xsd:any processContents="skip" minOccurs="0" maxOccurs="unbounded"/>
                        </xsd:sequence>
                    </xsd:complexType>
                </xsd:element>
            </xsd:sequence>
            <xsd:attribute name="metaid" type="xsd:ID" use="optional"/>
        </xsd:complexType>
        <!--The definition of FunctionDefinition follows.-->
        <xsd:complexType name="FunctionDefinition">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:sequence>
                        <xsd:element ref="mml:math"/>
                    </xsd:sequence>
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of UnitKind follows.-->
        <xsd:simpleType name="UnitKind">
            <xsd:restriction base="xsd:string">
                <xsd:enumeration value="ampere"/>
                <xsd:enumeration value="becquerel"/>
                <xsd:enumeration value="candela"/>
                <xsd:enumeration value="Celsius"/>
                <xsd:enumeration value="coulomb"/>
                <xsd:enumeration value="dimensionless"/>
                <xsd:enumeration value="farad"/>
                <xsd:enumeration value="gram"/>
                <xsd:enumeration value="gray"/>
                <xsd:enumeration value="henry"/>
                <xsd:enumeration value="hertz"/>
                <xsd:enumeration value="item"/>
                <xsd:enumeration value="joule"/>
                <xsd:enumeration value="katal"/>
                <xsd:enumeration value="kelvin"/>
                <xsd:enumeration value="kilogram"/>
                <xsd:enumeration value="litre"/>
                <xsd:enumeration value="lumen"/>
                <xsd:enumeration value="lux"/>
                <xsd:enumeration value="metre"/>
                <xsd:enumeration value="mole"/>
                <xsd:enumeration value="newton"/>
                <xsd:enumeration value="ohm"/>
                <xsd:enumeration value="pascal"/>
                <xsd:enumeration value="radian"/>
                <xsd:enumeration value="second"/>
                <xsd:enumeration value="siemens"/>
                <xsd:enumeration value="sievert"/>
                <xsd:enumeration value="steradian"/>
                <xsd:enumeration value="tesla"/>
                <xsd:enumeration value="volt"/>
                <xsd:enumeration value="watt"/>
                <xsd:enumeration value="weber"/>
```

```
            </xsd:restriction>
        </xsd:simpleType>
        <!--The definition of Unit follows.-->
        <xsd:complexType name="Unit">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:attribute name="kind" type="UnitKind" use="required"/>
                    <xsd:attribute name="exponent" type="xsd:integer" default="1"/>
                    <xsd:attribute name="scale" type="xsd:integer" default="0"/>
                    <xsd:attribute name="multiplier" type="xsd:double" default="1"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of UnitDefinition follows.-->
        <xsd:complexType name="ListOfUnits">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:sequence>
                        <xsd:element name="unit" type="Unit" maxOccurs="unbounded"/>
                    </xsd:sequence>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <xsd:complexType name="UnitDefinition">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:sequence>
                        <xsd:element name="listOfUnits" type="ListOfUnits"/>
                    </xsd:sequence>
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of CompartmentType follows.-->
        <xsd:complexType name="CompartmentType">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of SpeciesType follows.-->
        <xsd:complexType name="SpeciesType">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of Compartment follows.-->
        <xsd:complexType name="Compartment">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
                    <xsd:attribute name="compartmentType" type="SId" use="optional"/>
                    <xsd:attribute name="size" type="xsd:double" use="optional"/>
                    <xsd:attribute name="spatialDimensions" use="optional" default="3">
                        <xsd:simpleType>
                            <xsd:restriction base="xsd:integer">
                                <xsd:minInclusive value="0"/>
                                <xsd:maxInclusive value="3"/>
                            </xsd:restriction>
                        </xsd:simpleType>
                    </xsd:attribute>
                    <xsd:attribute name="units" type="SId" use="optional"/>
                    <xsd:attribute name="outside" type="SId" use="optional"/>
                    <xsd:attribute name="constant" type="xsd:boolean" use="optional" default="true"/>
                </xsd:extension>
            </xsd:complexContent>
        </xsd:complexType>
        <!--The definition of Species follows.-->
        <xsd:complexType name="Species">
            <xsd:complexContent>
                <xsd:extension base="SBase">
                    <xsd:attribute name="id" type="SId" use="required"/>
                    <xsd:attribute name="name" type="xsd:string" use="optional"/>
```

```
                <xsd:attribute name="speciesType" type="SId"  use="optional"/>
                <xsd:attribute name="compartment" type="SId"/>
                <xsd:attribute name="initialAmount" type="xsd:double" use="optional"/>
                <xsd:attribute name="initialConcentration" type="xsd:double" use="optional"/>
                <xsd:attribute name="substanceUnits" type="SId" use="optional"/>
                <xsd:attribute name="spatialSizeUnits" type="SId" use="optional"/>
                <xsd:attribute
                    name="hasOnlySubstanceUnits"
                    type="xsd:boolean"
                    use="optional"
                    default="false"/>
                <xsd:attribute
                    name="boundaryCondition" type="xsd:boolean" use="optional" default="false"/>
                <xsd:attribute name="charge" type="xsd:integer" use="optional"/>
                <xsd:attribute name="constant" type="xsd:boolean" use="optional" default="false"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Parameter follows.-->
    <xsd:complexType name="Parameter">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:attribute name="id" type="SId" use="required"/>
                <xsd:attribute name="name" type="xsd:string" use="optional"/>
                <xsd:attribute name="value" type="xsd:double" use="optional"/>
                <xsd:attribute name="units" type="SId" use="optional"/>
                <xsd:attribute name="constant" type="xsd:boolean" use="optional" default="true"/>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="ListOfParameters">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element name="parameter" type="Parameter" maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Constraint follows. -->
    <xsd:complexType name="Constraint" abstract="true">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                    <xsd:element name="message" minOccurs="0">
                        <xsd:complexType>
                            <xsd:sequence>
                                <xsd:any
                                    namespace="http://www.w3.org/1999/xhtml"
                                    processContents="skip"
                                    minOccurs="0"
                                    maxOccurs="unbounded"/>
                            </xsd:sequence>
                        </xsd:complexType>
                    </xsd:element>
                </xsd:sequence>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="Rule" abstract="true">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                </xsd:sequence>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="AlgebraicRule">
        <xsd:complexContent>
            <xsd:extension base="Rule"/>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="AssignmentRule">
        <xsd:complexContent>
            <xsd:extension base="Rule">
```

```
                <xsd:attribute name="variable" type="SId" use="required"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="RateRule">
        <xsd:complexContent>
            <xsd:extension base="Rule">
                <xsd:attribute name="variable" type="SId" use="required"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Initial Assignment follows.-->
    <xsd:complexType name="InitialAssignment">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                </xsd:sequence>
                <xsd:attribute name="symbol" type="SId" use="required"/>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Constraint follows.-->
    <xsd:complexType name="Constraint">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                    <xsd:element name="message" minOccurs="0">
                        <xsd:complexType>
                            <xsd:sequence>
                                <xsd:any
                                    namespace="http://www.w3.org/1999/xhtml"
                                    processContents="skip"
                                    minOccurs="0"
                                    maxOccurs="unbounded"/>
                            </xsd:sequence>
                        </xsd:complexType>
                    </xsd:element>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Reaction follows.-->
    <xsd:complexType name="KineticLaw">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                    <xsd:element name="listOfParameters" type="ListOfParameters" minOccurs="0"/>
                </xsd:sequence>
                <xsd:attribute name="timeUnits" type="SId" use="optional"/>
                <xsd:attribute name="substanceUnits" type="SId" use="optional"/>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="SimpleSpeciesReference" abstract="true">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:attribute name="id" type="SId" use="optional"/>
                <xsd:attribute name="name" type="xsd:string" use="optional"/>
                <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
                <xsd:attribute name="species" type="SId" use="required"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="ModifierSpeciesReference">
        <xsd:complexContent>
            <xsd:extension base="SimpleSpeciesReference"/>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="ListOfModifierSpeciesReferences">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="modifierSpeciesReference"
                        type="ModifierSpeciesReference"
```

```
                        maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="StoichiometryMath">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="SpeciesReference">
        <xsd:complexContent>
            <xsd:extension base="SimpleSpeciesReference">
                <xsd:sequence>
                    <xsd:element name="stoichiometryMath" type="StoichiometryMath" minOccurs="0"/>
                </xsd:sequence>
                <xsd:attribute name="stoichiometry" type="xsd:double" use="optional" default="1"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="ListOfSpeciesReferences">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="speciesReference" type="SpeciesReference" maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="Reaction">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="listOfReactants" type="ListOfSpeciesReferences" minOccurs="0"/>
                    <xsd:element
                        name="listOfProducts" type="ListOfSpeciesReferences" minOccurs="0"/>
                    <xsd:element
                        name="listOfModifiers"
                        type="ListOfModifierSpeciesReferences"
                        minOccurs="0"/>
                    <xsd:element name="kineticLaw" type="KineticLaw" minOccurs="0"/>
                </xsd:sequence>
                <xsd:attribute name="id" type="SId" use="required"/>
                <xsd:attribute name="name" type="xsd:string" use="optional"/>
                <xsd:attribute name="reversible" type="xsd:boolean" use="optional" default="true"/>
                <xsd:attribute name="fast" type="xsd:boolean" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!--The definition of Event follows.-->
    <xsd:complexType name="EventAssignment">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element ref="mml:math"/>
                </xsd:sequence>
                <xsd:attribute name="variable" type="SId" use="required"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="ListOfEventAssignments">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="eventAssignment" type="EventAssignment" maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="MathField">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
```

```
                    <xsd:element ref="mml:math"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <xsd:complexType name="Event">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element name="trigger" type="MathField"/>
                    <xsd:element name="delay" type="MathField" minOccurs="0"/>
                    <xsd:element name="listOfEventAssignments" type="ListOfEventAssignments"/>
                </xsd:sequence>
                <xsd:attribute name="id" type="SId" use="optional"/>
                <xsd:attribute name="name" type="xsd:string" use="optional"/>
                <xsd:attribute name="timeUnits" type="SId" use="optional"/>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
    <!-- The definition of Model follows.-->
    <xsd:complexType name="Model">
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element name="listOfFunctionDefinitions" minOccurs="0">
                        <xsd:complexType>
                            <xsd:complexContent>
                                <xsd:extension base="SBase">
                                    <xsd:sequence>
                                        <xsd:element
                                            name="functionDefinition"
                                            type="FunctionDefinition"
                                            maxOccurs="unbounded"/>
                                    </xsd:sequence>
                                </xsd:extension>
                            </xsd:complexContent>
                        </xsd:complexType>
                    </xsd:element>
                    <xsd:element name="listOfUnitDefinitions" minOccurs="0">
                        <xsd:complexType>
                            <xsd:complexContent>
                                <xsd:extension base="SBase">
                                    <xsd:sequence>
                                        <xsd:element
                                            name="unitDefinition"
                                            type="UnitDefinition"
                                            maxOccurs="unbounded"/>
                                    </xsd:sequence>
                                </xsd:extension>
                            </xsd:complexContent>
                        </xsd:complexType>
                    </xsd:element>
                    <xsd:element name="listOfCompartmentTypes" minOccurs="0">
                        <xsd:complexType>
                            <xsd:complexContent>
                                <xsd:extension base="SBase">
                                    <xsd:sequence>
                                        <xsd:element
                                            name="compartmentType"
                                            type="CompartmentType"
                                            maxOccurs="unbounded"/>
                                    </xsd:sequence>
                                </xsd:extension>
                            </xsd:complexContent>
                        </xsd:complexType>
                    </xsd:element>
                    <xsd:element name="listOfSpeciesTypes" minOccurs="0">
                        <xsd:complexType>
                            <xsd:complexContent>
                                <xsd:extension base="SBase">
                                    <xsd:sequence>
                                        <xsd:element
                                            name="speciesType"
                                            type="SpeciesType"
                                            maxOccurs="unbounded"/>
                                    </xsd:sequence>
                                </xsd:extension>
                            </xsd:complexContent>
                        </xsd:complexType>
                    <xsd:element name="listOfCompartments" minOccurs="xsd">
```

```
    <0:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="compartment"
                        type="Compartment"
                        maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
</xsd:element>
</xsd:element>
<xsd:element name="listOfSpecies" minOccurs="0">
    <xsd:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="species" type="Species" maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
</xsd:element>
<xsd:element name="listOfParameters" minOccurs="0">
    <xsd:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="parameter"
                        type="Parameter"
                        maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
</xsd:element>
<xsd:element name="listOfInitialAssignments" minOccurs="0">
    <xsd:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
                        name="initialAssignment"
                        type="InitialAssignment"
                        maxOccurs="unbounded"/>
                </xsd:sequence>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
</xsd:element>
<xsd:element name="listOfRules" minOccurs="0">
    <xsd:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:choice maxOccurs="unbounded">
                    <xsd:element
                        name="algebraicRule"
                        type="AlgebraicRule"
                        minOccurs="0"/>
                     <xsd:element
                        name="assignmentRule"
                        type="AssignmentRule"
                        minOccurs="0"/>
                    <xsd:element
                        name="rateRule" type="RateRule" minOccurs="0"/>
                </xsd:choice>
            </xsd:extension>
        </xsd:complexContent>
    </xsd:complexType>
</xsd:element>
<xsd:element name="listOfConstraints" minOccurs="0">
    <xsd:complexType>
        <xsd:complexContent>
            <xsd:extension base="SBase">
                <xsd:sequence>
                    <xsd:element
```

```
                                        name="constraint"
                                        type="Constraint"
                                        maxOccurs="unbounded"/>
                                </xsd:sequence>
                            </xsd:extension>
                        </xsd:complexContent>
                    </xsd:complexType>
                </xsd:element>
                <xsd:element name="listOfReactions" minOccurs="0">
                    <xsd:complexType>
                        <xsd:complexContent>
                            <xsd:extension base="SBase">
                                <xsd:sequence>
                                    <xsd:element
                                        name="reaction" type="Reaction" maxOccurs="unbounded"/>
                                </xsd:sequence>
                            </xsd:extension>
                        </xsd:complexContent>
                    </xsd:complexType>
                </xsd:element>
                <xsd:element name="listOfEvents" minOccurs="0">
                    <xsd:complexType>
                        <xsd:complexContent>
                            <xsd:extension base="SBase">
                                <xsd:sequence>
                                    <xsd:element
                                        name="event" type="Event" maxOccurs="unbounded"/>
                                </xsd:sequence>
                            </xsd:extension>
                        </xsd:complexContent>
                    </xsd:complexType>
                </xsd:element>
            </xsd:sequence>
            <xsd:attribute name="id" type="SId" use="optional"/>
            <xsd:attribute name="name" type="xsd:string" use="optional"/>
            <xsd:attribute name="sboTerm" type="SBOTerm" use="optional"/>
        </xsd:extension>
    </xsd:complexContent>
</xsd:complexType>
<!-- The following is the type definition for the top-level element in an SBML document.-->
<xsd:complexType name="Sbml">
    <xsd:complexContent>
        <xsd:extension base="SBase">
            <xsd:sequence>
                <xsd:element name="model" type="Model"/>
            </xsd:sequence>
            <xsd:attribute name="level" type="xsd:positiveInteger" use="required" fixed="2"/>
            <xsd:attribute name="version" type="xsd:positiveInteger" use="required" fixed="2"/>
        </xsd:extension>
    </xsd:complexContent>
</xsd:complexType>
<!--The following is the (only) top-level element allowed in an SBML document.-->
<xsd:element name="sbml" type="Sbml"/>
<!--The end.-->
</xsd:schema>
```

D XML Schema for MathML subset

The following XML schema defines the syntax of the MathML syntax that is used in SBML Level 2 version 1 and 2.

```
<?xml version="1.0" encoding="UTF-8"?>
<!-- edited with XMLSPY v5 rel. 3 U (http://www.xmlspy.com)
by Andrew Finney (University of Hertfordshire Biocomputation Research Group, STRC) -->
<!--/**
 * Filename    : restricted-math.xsd
 * Description : schema for the MathML subset used by SBML L2
 * Author(s)   : SBML Development Group <sbml-team@caltech.edu>
 * Organization: University of Hertfordshire STRC
 *
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 *
 * The original code contained here was initially developed by:
 *
 *     Andrew Finney
 *     Science and Technology Research Centre
 *     University of Hertfordshire
 *     Hatfield, AL10 9AB
 *     United Kingdom
 *
 *     http://www.sbml.org
 *     mailto:sbml-team@caltech.edu
 *
 * Contributor(s):
 */
--> <xs:schema
targetNamespace="http://www.w3.org/1998/Math/MathML"
xmlns="http://www.w3.org/1998/Math/MathML"
xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
xmlns:xs="http://www.w3.org/2001/XMLSchema"
elementFormDefault="qualified" attributeFormDefault="unqualified">
    <xs:attributeGroup name="MathAttributes">
        <xs:attribute name="class" type="xs:NMTOKENS" use="optional"/>
        <xs:attribute name="style" type="xs:string" use="optional"/>
        <xs:attribute name="id" type="xs:ID" use="optional"/>
    </xs:attributeGroup>
    <xs:complexType name="MathBase">
        <xs:attributeGroup ref="MathAttributes"/>
    </xs:complexType>
    <xs:complexType name="Ci">
        <xs:simpleContent>
            <xs:extension base="xs:string">
                <xs:attributeGroup ref="MathAttributes"/>
            </xs:extension>
        </xs:simpleContent>
    </xs:complexType>
    <xs:simpleType name="CnType">
        <xs:restriction base="xs:string">
            <xs:enumeration value="e-notation"/>
```

```
            <xs:enumeration value="real"/>
            <xs:enumeration value="integer"/>
            <xs:enumeration value="rational"/>
        </xs:restriction>
    </xs:simpleType>
    <xs:complexType name="Cn" mixed="true">
        <xs:sequence>
            <xs:element name="sep" type="MathBase"/>
        </xs:sequence>
        <xs:attribute name="type" type="CnType" use="optional" default="real"/>
        <xs:attributeGroup ref="MathAttributes"/>
    </xs:complexType>
    <xs:simpleType name="CsymbolURI">
        <xs:restriction base="xs:string">
            <xs:enumeration value="http://www.sbml.org/sbml/symbols/time"/>
            <xs:enumeration value="http://www.sbml.org/sbml/symbols/delay"/>
        </xs:restriction>
    </xs:simpleType>
    <xs:complexType name="Csymbol">
        <xs:simpleContent>
            <xs:extension base="xs:string">
                <xs:attribute name="encoding" use="required" fixed="text"/>
                <xs:attribute name="definitionURL" type="CsymbolURI" use="required"/>
                <xs:attributeGroup ref="MathAttributes"/>
            </xs:extension>
        </xs:simpleContent>
    </xs:complexType>
    <xs:complexType name="NodeContainer">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:sequence>
                    <xs:group ref="Node"/>
                </xs:sequence>
            </xs:extension>
        </xs:complexContent>
    </xs:complexType>
    <xs:complexType name="Apply">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:sequence>
                    <xs:choice>
                        <xs:element name="ci" type="Ci"/>
                        <xs:element name="csymbol" type="Csymbol"/>
                        <xs:element name="eq" type="MathBase"/>
                        <xs:element name="neq" type="MathBase"/>
                        <xs:element name="gt" type="MathBase"/>
                        <xs:element name="lt" type="MathBase"/>
                        <xs:element name="geq" type="MathBase"/>
                        <xs:element name="leq" type="MathBase"/>
                        <xs:element name="plus" type="MathBase"/>
                        <xs:element name="minus" type="MathBase"/>
                        <xs:element name="times" type="MathBase"/>
                        <xs:element name="divide" type="MathBase"/>
                        <xs:element name="power" type="MathBase"/>
                        <xs:sequence>
                            <xs:element name="root" type="MathBase"/>
                            <xs:element name="degree" type="NodeContainer" minOccurs="0"/>
                        </xs:sequence>
                        <xs:element name="abs" type="MathBase"/>
                        <xs:element name="exp" type="MathBase"/>
                        <xs:element name="ln" type="MathBase"/>
                        <xs:sequence>
                            <xs:element name="log" type="MathBase"/>
                            <xs:element name="logbase" type="NodeContainer" minOccurs="0"/>
                        </xs:sequence>
                        <xs:element name="floor" type="MathBase"/>
                        <xs:element name="ceiling" type="MathBase"/>
                        <xs:element name="factorial" type="MathBase"/>
                        <xs:element name="and" type="MathBase"/>
                        <xs:element name="or" type="MathBase"/>
                        <xs:element name="xor" type="MathBase"/>
                        <xs:element name="not" type="MathBase"/>
                        <xs:element name="sin" type="MathBase"/>
                        <xs:element name="cos" type="MathBase"/>
                        <xs:element name="tan" type="MathBase"/>
                        <xs:element name="sec" type="MathBase"/>
                        <xs:element name="csc" type="MathBase"/>
                        <xs:element name="cot" type="MathBase"/>
                        <xs:element name="sinh" type="MathBase"/>
                        <xs:element name="cosh" type="MathBase"/>
```

```
                        <xs:element name="tanh" type="MathBase"/>
                        <xs:element name="sech" type="MathBase"/>
                        <xs:element name="csch" type="MathBase"/>
                        <xs:element name="coth" type="MathBase"/>
                        <xs:element name="arcsin" type="MathBase"/>
                        <xs:element name="arccos" type="MathBase"/>
                        <xs:element name="arctan" type="MathBase"/>
                        <xs:element name="arcsec" type="MathBase"/>
                        <xs:element name="arccsc" type="MathBase"/>
                        <xs:element name="arccot" type="MathBase"/>
                        <xs:element name="arcsinh" type="MathBase"/>
                        <xs:element name="arccosh" type="MathBase"/>
                        <xs:element name="arctanh" type="MathBase"/>
                        <xs:element name="arcsech" type="MathBase"/>
                        <xs:element name="arccsch" type="MathBase"/>
                        <xs:element name="arccoth" type="MathBase"/>
                    </xs:choice>
                    <xs:sequence maxOccurs="unbounded">
                        <xs:group ref="Node"/>
                    </xs:sequence>
                </xs:sequence>
            </xs:extension>
        </xs:complexContent>
    </xs:complexType>
    <xs:complexType name="Otherwise">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:group ref="Node"/>
            </xs:extension>
        </xs:complexContent>
    </xs:complexType>
    <xs:complexType name="Piece">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:sequence minOccurs="2" maxOccurs="2">
                    <xs:group ref="Node"/>
                </xs:sequence>
            </xs:extension>
        </xs:complexContent>
    </xs:complexType>
    <xs:complexType name="Piecewise">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:choice maxOccurs="unbounded">
                    <xs:element name="piece" type="Piece"/>
                    <xs:element name="otherwise" type="Otherwise"/>
                </xs:choice>
            </xs:extension>
        </xs:complexContent>
    </xs:complexType>
    <xs:attributeGroup name="AnnotationAttributes">
        <xs:attributeGroup ref="MathAttributes"/>
        <xs:attribute name="encoding" type="xs:string" use="required"/>
    </xs:attributeGroup>
    <xs:complexType name="Annotation">
        <xs:simpleContent>
            <xs:extension base="xs:string">
                <xs:attributeGroup ref="AnnotationAttributes"/>
            </xs:extension>
        </xs:simpleContent>
    </xs:complexType>
    <xs:complexType name="Annotation-xml">
        <xs:sequence maxOccurs="unbounded">
            <xs:any processContents="skip"/>
        </xs:sequence>
        <xs:attributeGroup ref="AnnotationAttributes"/>
    </xs:complexType>
    <xs:complexType name="Semantics">
        <xs:complexContent>
            <xs:extension base="MathBase">
                <xs:sequence>
                    <xs:group ref="Node"/>
                    <xs:sequence maxOccurs="unbounded">
                        <xs:choice>
                            <xs:element name="annotation" type="Annotation"/>
                            <xs:element name="annotation-xml" type="Annotation-xml"/>
                        </xs:choice>
                    </xs:sequence>
                </xs:sequence>
            </xs:extension>
```

```
            </xs:complexContent>
        </xs:complexType>
        <xs:group name="Node">
            <xs:choice>
                <xs:element name="apply" type="Apply"/>
                <xs:element name="cn" type="Cn"/>
                <xs:element name="ci" type="Ci"/>
                <xs:element name="csymbol" type="Csymbol"/>
                <xs:element name="true" type="MathBase"/>
                <xs:element name="false" type="MathBase"/>
                <xs:element name="notanumber" type="MathBase"/>
                <xs:element name="pi" type="MathBase"/>
                <xs:element name="infinity" type="MathBase"/>
                <xs:element name="exponentiale" type="MathBase"/>
                <xs:element name="semantics" type="Semantics"/>
                <xs:element name="piecewise" type="Piecewise"/>
            </xs:choice>
        </xs:group>
        <xs:complexType name="Bvar">
            <xs:complexContent>
                <xs:extension base="MathBase">
                    <xs:sequence>
                        <xs:element name="ci" type="Ci"/>
                    </xs:sequence>
                </xs:extension>
            </xs:complexContent>
        </xs:complexType>
        <xs:complexType name="Lambda">
            <xs:complexContent>
                <xs:extension base="MathBase">
                    <xs:sequence>
                        <xs:sequence maxOccurs="unbounded">
                            <xs:element name="bvar" type="Bvar"/>
                        </xs:sequence>
                        <xs:group ref="Node"/>
                    </xs:sequence>
                </xs:extension>
            </xs:complexContent>
        </xs:complexType>
        <xs:complexType name="Math">
            <xs:sequence>
                <xs:choice>
                    <xs:group ref="Node"/>
                    <xs:element name="lambda" type="Lambda"/>
                </xs:choice>
            </xs:sequence>
        </xs:complexType>
        <xs:element name="math" type="Math"/>
    </xs:schema>
```

E Validation Rules for SBML

This section contains a summary of all the conditions that should be true of a model, in addition to consistency with the XML Schemas given in Appendixes C and D, for that model to considered valid SBML.

General Identifier Validation

900. The value of the `id` field on every instance of the following in a model must be unique: Model, FunctionDefinition, CompartmentType, Compartment, SpeciesType, Species, Reaction, SpeciesReference, ModifierSpeciesReference, Event, and model-wide Parameters. Note that UnitDefinition and parameters defined inside a reaction are treated separately. (References: L2V1 Section 3.5; L2V2 Section 3.4.1.)

901. The value of the `id` field of every UnitDefinition must be unique across the set of all UnitDefinitions in the entire model. (References: L2V2 Section 4.4; L2V1 Section 3.4.1 and 4.4.1.)

902. The value of the `id` field of each parameter defined locally within a KineticLaw must be unique across the set of all such parameter definitions in that KineticLaw. (References: L2V2 Sections 3.4.1 and 4.13.9; L2V1 Sections 3.4.1 and 4.13.9.)

903. The value of the `variable` field in all AssignmentRule and RateRule definitions must be unique across the set of all such rule definitions in a model. (References: L2V1 Section 4.8.4; L2V2 Section 4.11.3.)

904. In each Event, the value of the `variable` field within every EventAssignment definition must be unique across the set of all EventAssignments within that Event. (References: L2V1 erratum 17; L2V2 Section 4.14.)

905. An identifier used as the value of `variable` in an EventAssignment cannot also appear as the value of `variable` in an AssignmentRule. (References: L2V1 Section 4.10.5; L2V2 Section 4.14.)

906. The value of a `sboTerm` attribute must have the data type `SBOTerm`, which is a string consisting of the characters 'S', 'B', 'O', ':', followed by exactly seven digits. (References: L2V2 Section 3.1.8.)

907. Every `metaid` field value must be unique across the set of all `metaid` values in a model. (References: L2V2 Sections 3.3.1 and 3.1.6.)

General MathML Validation

2000. All MathML content in SBML must appear within a `math` element with a namespace declaration of "`http://www.w3.org/1998/Math/MathML`". (References: L2V2 Section 3.5.)

2001. The only permitted MathML 2.0 elements in SBML Level 2 are the following: `cn`, `ci`, `csymbol`, `sep`, `apply`, `piecewise`, `piece`, `otherwise`, `eq`, `neq`, `gt`, `lt`, `geq`, `leq`, `plus`, `minus`, `times`, `divide`, `power`, `root`, `abs`, `exp`, `ln`, `log`, `floor`, `ceiling`, `factorial`, `and`, `or`, `xor`, `not`, `degree`, `bvar`, `logbase`, `sin`, `cos`, `tan`, `sec`, `csc`, `cot`, `sinh`, `cosh`, `tanh`, `sech`, `csch`, `coth`, `arcsin`, `arccos`, `arctan`, `arcsec`, `arccsc`, `arccot`, `arcsinh`, `arccosh`, `arctanh`, `arcsech`, `arccsch`, `arccoth`, `true`, `false`, `notanumber`, `pi`, `infinity`, `exponentiale`, `semantics`, `annotation`, and `annotation-xml`. (References: L2V2 Section 3.5.1.)

2002. In the SBML subset of MathML 2.0, the MathML attribute `encoding` is only permitted on `csymbol`. No other MathML elements may have a `encoding` attribute. (References: L2V2 Section 3.5.1.)

2003. In the SBML subset of MathML 2.0, the MathML attribute `definitionURL` is only permitted on `csymbol`. No other MathML elements may have a `definitionURL` attribute. (References: L2V2 Section 3.5.1.)

2004. In the SBML subset of MathML 2.0, the MathML attribute `type` is only permitted on the `cn` construct. No other MathML elements may have a `type` attribute. (References: L2V2 Section 3.5.1.)

2005. The only permitted values for the `type` attribute on MathML `cn` elements are "`e-notation`", "`real`", "`integer`", and "`rational`". (References: L2V2 Section 3.5.3.)

2006. MathML `lambda` elements are only permitted as the first element inside the `math` element of a FunctionDefinition; they may not be used elsewhere in an SBML model. (References: L2V2 Section 4.3.2.)

2007. Outside of a FunctionDefinition, if a `ci` element is the first element within a MathML `apply`, then the `ci`'s value can only be chosen from the set of identifiers of FunctionDefinitions defined in the SBML model. (References: L2V2 Section 4.3.2.)

2008. Outside of a FunctionDefinition, if a `ci` element is not the first element within a MathML `apply`, then the `ci`'s value can only be chosen from the set of identifiers of Species, Compartment, Parameter or Reaction objects defined in the SBML model. (References: L2V2 Section 3.5.4.)

2009. The `id` value of a Parameter defined within a KineticLaw can only be used in `ci` elements within the MathML content of that same KineticLaw; the identifier is not visible to other parts of the model. (References: L2V2 Section 3.5.4.)

2010. In SBML Level 2 Versions 1 and Version 2, the only values permitted for `definitionURL` on a `csymbol` are "`http://www.sbml.org/sbml/symbols/time`" and "`http://www.sbml.org/sbml/symbols/delay`". (References: L2V2 Section 3.5.5.)

2011. The arguments of the MathML logical operators `and`, `or`, `xor`, and `not` must have boolean values. (References: L2V2 Section 3.5.6.)

2012. The second argument of a MathML `piece` operator must have a boolean value. (References: L2V2 Section 3.5.6.)

2013. The `trigger` expression of an SBML Event must produce a boolean value. (References: L2V2 Section 3.5.6.)

2014. The `math` expression of an SBML Constraint must produce a boolean value. (References: L2V2 Section 3.5.6.)

2015. The arguments to the following MathML constructs must have a numeric type: `plus`, `minus`, `times`, `divide`, `power`, `root`, `abs`, `exp`, `ln`, `log`, `floor`, `ceiling`, `factorial`, `sin`, `cos`, `tan`, `sec`, `csc`, `cot`, `sinh`, `cosh`, `tanh`, `sech`, `csch`, `coth`, `arcsin`, `arccos`, `arctan`, `arcsec`, `arccsc`, `arccot`, `arcsinh`, `arccosh`, `arctanh`, `arcsech`, `arccsch`, `arccoth`. (References: L2V2 Section 3.5.6.)

2017. The types of values within `piecewise` operators should all be consistent: the set of expressions that make up the first arguments of the `piece` and `otherwise` operators within the same `piecewise` operator should all return values of the same type. (References: L2V2 Section 3.5.6.)

2018. The values of all arguments to `eq` and `neq` operators should have the same type (either all boolean or all numeric). (References: L2V2 Section 3.5.6.)

2019. The following MathML elements must yield numeric expressions: `math` in KineticLaw, `stoichiometryMath` in SpeciesReference, `math` in InitialAssignment, `math` in AssignmentRule, `math` in RateRule, `math` in AlgebraicRule, `trigger` and `delay` in Event, and `math` in EventAssignment.

General Unit Validation

3000. When the `variable` in an AssignmentRule refers to a Compartment, the units of the rule's right-hand side must be consistent with either the `units` in that Compartment definition, or (in the absence of explicit units declared for the compartment size) the default units for that compartment. (References: L2V2 Section 4.11.3.)

3001. When the `variable` in an AssignmentRule refers to a Species, the units of the rule's right-hand side must be consistent with either the `units` in that Species definition, or (in the absence of explicit units declared for the species quantity) the default units for that species. (References: L2V2 Section 4.11.3.)

3002. When the `variable` in an AssignmentRule refers to a Parameter, the units of the rule's right-hand side must be consistent with the `units` in that Parameter definition. (References: L2V2 Section 4.11.3.)

3003. When the `variable` in an InitialAssignment refers to a Compartment, the units of the InitialAssignment's `math` expression must be consistent with either the `units` in that Compartment definition, or (in the absence of explicit units declared for the compartment size) the default units for that compartment. (References: L2V2 Section 4.10.)

3004. When the `variable` in an InitialAssignment refers to a Species, the units of the InitialAssignment's `math` expression must be consistent with either the `units` in that Species definition, or (in the absence of explicit units declared for the species' quantity) the default units for that species. (References: L2V2 Section 4.11.3.)

3005. When the `variable` in an InitialAssignment refers to a Parameter, the units of the InitialAssignment's `math` expression must be consistent with the `units` in that Parameter definition. (References: L2V2 Section 4.11.3.)

3100. When the `variable` in a RateRule definition refers to a Compartment, the units of the rule's right-hand side must be of the form *x per time*, where *x* is either the `units` in that Compartment definition, or (in the absence of explicit units declared for the compartment size) the default units for that compartment, and *time* refers to the units of time for the model. (References: L2V2 Section 4.11.4.)

3101. When the `variable` in a RateRule definition refers to a Species, the units of the rule's right-hand side must be of the form *x per time*, where *x* is either the `units` in that Species definition, or (in the absence of explicit units declared for the species' quantity) the default units for that species, and *time* refers to the units of time for the model. (References: L2V2 Section 4.11.4.)

3102. When the `variable` in a RateRule definition refers to a Parameter, the units of the rule's right-hand side must be of the form *x per time*, where *x* is the `units` in that Parameter definition, and *time* refers to the units of time for the model. (References: L2V2 Section 4.11.4.)

3200. The units of the `math` formula in a KineticLaw definition must be the equivalent of *substance per time*. The optional KineticLaw fields `substanceUnits` and `timeUnits` determine the units of substance and time, respectively. In the absence of values for these, the units are taken from the model's defaults. (References: L2V2 Section 4.13.9.)

3301. The content of a `math` field must conform to MathML 2.0 syntax, otherwise the consistency of the units cannot be established.

3302. A mathematical expression using `power` with non-integer exponents may result in incorrect units.

3303. The use of non-integer exponents may result in incorrect units.

3304. The units of the expressions used as arguments to a function call must match the units expected for the arguments of that function.

3400. When a value for `delay` is given in a Event definition, the units of the delay formula must correspond to either the value of `timeUnits` in the Event or (if no `timeUnits` are given), the model's default units of time. (References: L2V2 Section 4.14.)

General Annotation Validation

2200. Every top-level element within an `annotation` element must have a namespace declared. (References: L2V2 Section 3.3.3.)

2201. There cannot be more than one top-level element using a given namespace inside a given `annotation` element. (References: L2V2 Section 3.3.3.)

2202. Top-level elements within an `annotation` element cannot use any SBML namespace, whether explicitly (by declaring the namespace to be one of the URIs `http://www.sbml.org/sbml/level1`, `http://www.sbml.org/sbml/level2`, or `http://www.sbml.org/sbml/level2/version2`), or implicitly (by failing to declare any namespace). (References: L2V2 Section 3.3.3.)

Model

1000. An SBML document must contain a Model definition. (References: SBML L2V1 and L2V2 Section 4).

1001. If a model defines any Species, then the model must also define at least one Compartment. This is an implication of the fact that the `compartment` field on Species is not optional. (References: L2V1 Section 4.5; Section 4.8.3.)

1002. The order of subelements within Model must be the following (where any one may be optional, but the ordering must be maintained): `listOfFunctionDefinitions`, `listOfUnitDefinitions`, `listOfCompartmentTypes`, `listOfSpeciesTypes`, `listOfCompartments`, `listOfSpecies`, `listOfParameters`, `listOfInitialAssignments`, `listOfRules`, `listOfConstraints`, `listOfReactions` and `listOfEvents`. (References: L2V2 Section 4.2.)

FunctionDefinition

1100. The top-level element within `math` in a FunctionDefinition must be `lambda`. (References: L2V1 Section 4.3.2; L2V2 Section 4.3.2.)

1101. Inside the `lambda` of a FunctionDefinition, if a `ci` element is the first element within a MathML `apply`, then the `ci`'s value can only be chosen from the set of identifiers of other SBML FunctionDefinitions defined prior to that point in the SBML model. (References: L2V2 Section 4.3.2.)

1102. Inside the `lambda` of a FunctionDefinition, the identifier of that FunctionDefinition cannot appear as the value of a `ci` element. SBML functions are not permitted to be recursive. (References: L2V2 Section 4.3.2.)

1103. Inside the `lambda` of a FunctionDefinition, if a `ci` element is not the first element within a MathML `apply`, then the `ci`'s value can only be the value of a `bvar` element declared in that `lambda`. (References: L2V2 Section 4.3.2.)

1104. The value type returned by a FunctionDefinition's `lambda` must be either boolean or numeric. (References: L2V2 Section 3.5.6.)

Unit and UnitDefinition

1201. The value of the `id` field in a UnitDefinition must not be identical to any unit predefined in SBML. That is, the identifier must not be the same as a value from the `UnitKind` enumeration (e.g., "`litre`", "`mole`", "`metre`", etc.). (References: L2V1 erratum 14; L2V2 Section 4.4.2.)

1202. Redefinitions of the built-in unit `substance` must be based on the units `mole` or `item`. More formally, a UnitDefinition for `substance` must simplify to a single Unit whose `kind` field has a value of either "`mole`" or "`item`" and whose `exponent` field has a value of "`1`". (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1203. Redefinitions of the built-in unit `length` must be based on the unit `metre` or `dimensionless`. More formally, a UnitDefinition for `length` must simplify to a single Unit in which either (a) the `kind` field has a value of "`metre`" and the `exponent` field has a value of "`1`", or (b) the `kind` field has a value of "`dimensionless`" with any `exponent` value. (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1204. Redefinitions of the built-in unit `area` must be based on squared `metre`s or `dimensionless`. More formally, a UnitDefinition for `area` must simplify to a single Unit in which either (a) the `kind` field has a value of "`metre`" and the `exponent` field has a value of "`2`", or (b) the `kind` field has a value of "`dimensionless`" with any `exponent` value. (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1205. Redefinitions of the built-in unit `volume` must be based on `litre`, `metre` or `dimensionless`. More formally, a UnitDefinition for `volume` must simplify to a single Unit in which the `kind` field value is either "`litre`", "`metre`", or "`dimensionless`". Additional constraints apply if the kind is "`litre`" or "`metre`". (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1206. If a UnitDefinition for `volume` simplifies to a Unit in which the `kind` field value is "`litre`", then its `exponent` field value must be "`1`". (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1207. If a UnitDefinition for `volume` simplifies to a Unit in which the `kind` field value is "`metre`", then its `exponent` field value must be "`3`". (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1208. Redefinitions of the built-in unit `time` must be based on `second`. More formally, a UnitDefinition for `time` must simplify to a single Unit in which either (a) the `kind` field has a value of "`second`" and the `exponent` field has a value of "`1`", or (b) the `kind` field has a value of "`dimensionless`" with any `exponent` value. (References: L2V1 Section 4.4.3; L2V2 Section 4.4.3.)

1209. The `offset` field in Unit is deprecated as of SBML Level 2 Version 2. Software tools should not generate models containing deprecated features. (References: L2V2 Section 4.4.)

Compartment

1300. The size of a Compartment must not be set if the compartment's `spatialDimensions` field has value `0`. (References: L2V1 Section 4.5.3; L2V2 Section 4.7.5.)

1301. If a Compartment definition has a `spatialDimensions` value of "`0`", then its `units` must be set to "`dimensionless`" or else to the identifier of a UnitDefinition based on `dimensionless`. (References: L2V1 Section 4.5.4; Section 4.7.5.)

1302. If a Compartment definition has a `spatialDimensions` value of "`0`", then its `constant` field value must either default to or be set to "`true`". (References: L2V1 Section 4.5.5; L2V2 Section 4.7.6.)

1303. The `outside` field value of a Compartment must be the identifier of another Compartment defined in the model. (References: L2V1 Section 4.5.6; Section 4.7.7.)

1304. A Compartment may not enclose itself through a chain of references involving the `outside` field. This means that a compartment cannot have its own identifier as the value of `outside`, nor can it point to another compartment whose `outside` field points directly or indirectly to the compartment. (References: L2V1 erratum 11; L2V2 Section 4.7.7.)

1305. The value of the `units` field on a Compartment having `spatialDimensions` of "`1`" must be either "`length`", "`metre`", "`dimensionless`", or the identifier of a UnitDefinition based on either `metre` (with `exponent` equal to "`1`") or `dimensionless`. (References: L2V1 Section 4.5.4; L2V2 Section 4.7.5.)

1306. The value of the `units` field on a Compartment having `spatialDimensions` of "`2`" must be either "`area`", "`dimensionless`", or the identifier of a UnitDefinition based on either `metre` (with `exponent` equal to "`2`") or `dimensionless`. (References: L2V1 Section 4.5.4; L2V2 Section 4.7.5.)

1307. The value of the `units` field on a Compartment having `spatialDimensions` of "`3`" must be either "`volume`", "`litre`", or the identifier of a UnitDefinition based on either `litre`, `metre` (with `exponent` equal to "`3`"), or `dimensionless`. (References: L2V1 Section 4.5.4; L2V2 Section 4.7.5.)

1308. If the `compartmentType` field is given a value in a Compartment definition, it must contain the identifier of an existing CompartmentType. (References: L2V2 Section 4.7.2.)

Species

1400. The value of `compartment` in a Species definition must be the identifier of an existing Compartment defined in the model. (References: L2V1 Section 4.6.2; Section 4.8.3.)

1401. If a Species definition sets `hasOnlySubstanceUnits` to "`true`", then it must not have a value for `spatialSizeUnits`. (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1402. A Species definition must not set `spatialSizeUnits` if the Compartment in which it is located has a `spatialDimensions` value of "`0`". (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1404. If a Species located in a Compartment whose `spatialDimensions` is set to "`0`", then that Species definition cannot set `initialConcentration`. (References: L2V1 Section 4.6.3; L2V2 Section 4.8.4.)

1405. If a Species is located in a Compartment whose `spatialDimensions` has value "`1`", then that Species definition can only set `spatialSizeUnits` to a value of "`length`", "`metre`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `metre` (with an `exponent` value of "`1`") or "`dimensionless`". (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1406. If a Species is located in a Compartment whose `spatialDimensions` has value "`2`", then that Species definition can only set `spatialSizeUnits` to a value of "`area`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `metre` (with an `exponent` value of "`2`") or "`dimensionless`". (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1407. If a Species is located in a Compartment whose `spatialDimensions` has value "`3`", then that Species definition can only set `spatialSizeUnits` to a value of "`volume`", "`litre`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `litre`, `metre` (with an `exponent` value of "`3`") or `dimensionless`. (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1408. The value of a Species's `substanceUnits` field can only be one of the following: "`substance`", "`mole`", "`item`", "`dimensionless`", or the identifier of a UnitDefinition derived from "`mole`" (with an `exponent` of "`1`"), "`item`" (with an `exponent` of "`1`"), or "`dimensionless`". (References: L2V1 Section 4.6.4; L2V2 Section 4.8.5.)

1409. A Species cannot set values for both `initialConcentration` and `initialAmount` because they are mutually exclusive. (References: L2V1 Section 4.6.3; L2V2 Section 4.8.4.)

1410. Unless a species is a boundary species in a model, its concentration or amount cannot be set by both reactions and rules simultaneously. More formally, if the identifier of a Species definition having a `boundaryCondition` value of "`false`" is referenced by a SpeciesReference anywhere in a model, then this identifier cannot also appear as the value of a `variable` in an AssignmentRule or a RateRule definition. (References: implicit in L2V1 Section 4.6.5; L2V2 Section 4.8.6.)

1411. The value of `speciesType` in a Species definition must be the identifier of an existing SpeciesType. (References: L2V2 Section 4.8.2.)

1412. There cannot be more than one species of a given SpeciesType in the same compartment of a model. More formally, for any given compartment, there cannot be more than one Species definition in which both of the following hold simultaneously: (i) the Species' `compartment` value is set to that compartment's identifier and (ii) the Species' `speciesType` is set the same value as the `speciesType` of another Species that also sets its `compartment` to that compartment identifier. (References: L2V2 Section 4.8.2.)

Parameter

1500. The `units` in a Parameter definition must be a value chosen from among the following: a value from the `UnitKind` enumeration (e.g., "`litre`", "`mole`", "`metre`", etc.), a built-in unit (e.g., "`substance`", "`time`", etc.), or the identifier of a UnitDefinition in the model. (References: L2V1 Section 4.7.3; L2V2 Section 4.9.3.)

InitialAssignment

1900. The value of `symbol` in an InitialAssignment definition must be the identifier of an existing Compartment, Species, or Parameter defined in the model. (References: L2V2 Section 4.10.)

1901. A given identifier cannot appear as the value of more than one `symbol` field across the set of InitialAssignments in a model. (References: L2V2 Section 4.10.)

1902. The value of a `symbol` field in any InitialAssignment definition cannot also appear as the value of a `variable` field in an AssignmentRule. (References: L2V2 Section 4.10.)

Reaction

1600. A Reaction definition must contain at least one SpeciesReference, either in its `listOfReactants` or its `listOfProducts`. (References: L2V2 Section 4.13.7.)

1608. The order of subelements within Reaction must be the following: `listOfReactants` (optional), `listOfProducts` (optional), `listOfModifiers` (optional), `kineticLaw`. (References: L2V2 Section 4.13.)

SpeciesReference and ModifierSpeciesReference

1601. The value of a SpeciesReference `species` field must be the identifier of an existing Species in the model. (References: L2V1 Section 4.9.5; L2V2 Section 4.13.7.)

1602. The value of a SpeciesReference's `species` field must not be the identifier of a Species having both a `constant` field value of "`true`" and a `boundaryCondition` field value of "`false`". (References: L2V1 Section 4.6.5; L2V2 Section 4.8.6.)

1603. A SpeciesReference must not have a value for both `stoichiometry` and `stoichiometryMath`; they are mutually exclusive. (References: L2V1 Section 4.9.5; L2V2 Section 4.13.7.)

KineticLaw

1604. The value of a KineticLaw's `substanceUnits` can only be one of the following: "`moles`", "`substance`", "`item`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `mole` (with an `exponent` value of "`1`"), `item` (with an `exponent` value of "`1`"), or "`dimensionless`". (References: L2V1 Section 4.9.7; L2V2 Section 4.13.9.)

1605. The value of a KineticLaw's `timeUnits` must be either "`second`", "`time`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `second` (with an `exponent` value of "`1`") or "`dimensionless`". (References: L2V1 Section 4.9.7; L2V2 Section 4.13.9.)

1606. All species referenced in the KineticLaw formula of a given reaction must first be declared using SpeciesReference or ModifierSpeciesReference. More formally, if a Species identifier appears in a `ci` element of a Reaction's KineticLaw formula, that same identifier must also appear in at least one SpeciesReference or ModifierSpeciesReference in the Reaction definition. (References: L2V2 Section 4.13.9.)

1609. The order of subelements within KineticLaw must be the following: `math`, `listOfParameters`. The `listOfParameters` is optional, but if present, must follow `math`. (References: L2V2 Section 4.13.9.)

StoichiometryMath

1607. All species referenced in the StoichiometryMath formula of a given reaction must first be declared using SpeciesReference or ModifierSpeciesReference. More formally, if a Species identifier appears in a `ci` element of a Reaction's StoichiometryMath formula, that same identifier must also appear in at least one SpeciesReference or ModifierSpeciesReference in the Reaction definition. (References: L2V2 Section 4.13.9.)

AssignmentRule and RateRule

1700. The value of an AssignmentRule's `variable` must be the identifier of an existing Compartment, Species, or globally-defined Parameter. (References: L2V1 Section 4.8.2; L2V2 Section 4.11.3.)

1701. The value of a RateRule's `variable` must be the identifier of an existing Compartment, Species, or globally-defined Parameter. (References: L2V1 Section 4.8.3; L2V2 Section 4.11.4.)

1702. Any Compartment, Species or Parameter whose identifier is the value of a `variable` field in an AssignmentRule, must have a value of "`false`" for `constant`. (References: L2V1 Section 4.8.4; L2V2 Section 4.11.3.)

1703. Any Compartment, Species or Parameter whose identifier is the value of a `variable` field in an RateRule, must have a value of "`false`" for `constant`. (References: L2V1 Section 4.8.4; L2V2 Section 4.11.4.)

1704. A given identifier cannot appear as the value of more than one `variable` field across the combined set of AssignmentRules and RateRules in a model. (References: L2V2 Section 4.11.5.)

1705. There must not be circular dependencies in the combined set of InitialAssignment, AssignmentRule and KineticLaw definitions in a model. Each of these constructs has the effect of assigning a value to an identifier (i.e., the identifier given in the field `symbol` in InitialAssignment, the field `variable` in AssignmentRule, and the field `id` on the KineticLaw's enclosing Reaction). Each of these constructs computes the value using a mathematical formula. The formula for a given identifier cannot make reference to a second identifier whose own definition depends directly or indirectly on the first identifier. (References: L2V2 Section 4.11.5.)

AlgebraicRule

9999. SBML models cannot be overdetermined as defined in the specification. See the detailed exposition of this rule in Section 4.11.5.

Constraint

2100. A Constraint `math` expression must evaluate to a value of type `boolean`. (References: L2V2 Section 4.12.)

2101. The order of subelements within Constraint must be the following: `math`, `message`. The `message` element is optional, but if present, must follow the `math` element. (References: L2V2 Section 4.12.)

Event

1800. The value of an Event's `timeUnits` must be "`time`", "`second`", "`dimensionless`", or the identifier of a UnitDefinition derived from either `second` (with an `exponent` value of "1") or "`dimensionless`". (References: L2V1 Section 4.10.4; L2V2 Section 4.14.)

1801. An Event `trigger` expression must evaluate to a value of type `boolean`. (References: L2V1 Section 4.10.2; L2V2 Section 4.14.)

1802. The value of `variable` in an EventAssignment can only be the identifier of a Compartment, Species, or model-wide Parameter definition. (References: L2V1 Section 4.10.5; L2V2 Section 4.14.)

1804. The order of subelements within Event must be the following: `trigger`, `delay`, `listOfEventAssignments`. The `delay` element is optional, but if present, must follow `trigger`. (References: L2V2 Section 4.14.)

EventAssignment

1802. The value of `variable` in an EventAssignment can only be the identifier of a Compartment, Species, or model-wide Parameter definition. (References: L2V1 Section 4.10.5; L2V2 Section 4.14.)

1803. Any Compartment, Species or Parameter definition whose identifier is used as the value of `variable` in an EventAssignment must have a value of "`false`" for its `constant` field. (References: L2V1 Section 4.10.5; L2V2 Section 4.14.)

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