SBML Level 3 Package Specification

SBML Level 3 Package: Flux Balance Constraints ('fbc')

Brett G. Olivier

b.g.olivier@vu.nl

Systems Bioinformatics VU University Amsterdam Amstedam, NH, The Netherlands Frank T. Bergmann

fbergmann@caltech.edu

Computing and Mathematical Sciences California Institute of Technology Pasadena, CA, US

Version 1, Release Candidate 1

December 11, 2012

This is a draft specification for the package "fbc" and not a normative document. Please send feedback to the Package Working Group mailing list at sbml-flux@lists.sourceforge.net

The latest release, past releases, and other materials related to this specification are available at http://sbml.org/Documents/Specifications/SBML_Level_3/Packages/Flux_Balance_Constraints_(flux)

This release of the specification is available at http://sbml.org/Documents/Specifications/Fbc_Level_1_Version_1



Contents

| 1 | Intr | oduction and motivation 3 | | | | |
|---------------------------------|--------------|---|------------------------------------|--|--|--|
| | 1.1 | Proposal corresponding to this package specification | 3 | | | |
| | 1.2 | Tracking number | 4 | | | |
| | 1.3 | Package dependencies | 4 | | | |
| | 1.4 | Document conventions | 4 | | | |
| 2 | Bac | ackground | | | | |
| | 2.1 | Problems with current SBML approaches | 5 | | | |
| | 2.2 | Past work on this problem or similar topics | 5 | | | |
| 3 Proposed syntax and semantics | | | | | | |
| | 3.1 | Namespace URI and other declarations necessary for using this package | | | | |
| | 3.2 | Primitive data types | 6 | | | |
| | | 3.2.1 Type FbcSId | 6 | | | |
| | | 3.2.2 Type FbcSIdRef | 6 | | | |
| | | 3.2.3 Type FbcType | 6 | | | |
| | | 3.2.4 Type FbcOperation | 7 | | | |
| | 3.3 | The extended Model class | 7 | | | |
| | | 3.3.1 The FBC listOfFluxBounds | 7 | | | |
| | | 3.3.2 The FBC listOfObjectives | 7 | | | |
| | 3.4 | The extended Species class | 8 | | | |
| | 3.5 | The FBC FluxBound class | 8 | | | |
| | 3.6 | The FBC Objective class | 9 | | | |
| | 3.7 | The FBC FluxObjective class | 11 | | | |
| 4 | Exa | mples | 12 | | | |
| | | Example of the FBC syntax | 12 | | | |
| | | | 12 | | | |
| | | 4.1.2 Capacity constraints | 13 | | | |
| | | | 13 | | | |
| | | | 13 | | | |
| 5 | Bes | st practices | 16 | | | |
| | | | 16 | | | |
| 6 | | ure development | 13 16 16 19 | | | |
| Ŭ | 6.1 | | 19 | | | |
| | 0.1 | | 19 | | | |
| | | | 19 | | | |
| Δ | Vali | dation of SBML documents | 22 | | | |
| | | Validation and consistency rules | 22 | | | |
| ۸۵ | | wledgments | 27 | | | |
| | | | | | | |
| ne | eferences 28 | | | | | |

1 Introduction and motivation

Constraint based modelling is a widely accepted methodology used to analyze and study biological networks on both a small and whole organism (genome) scale. Typically these models are underdetermined and constraint based methods (e.g. linear, quadratic optimization) are used to optimize specific model properties. This is assumed to occur under a defined set of constraints (e.g. stoichiometric, metabolic) and bounds (e.g. thermodynamic, experimental and environmental) on the values that the solution fluxes can obtain.

Perhaps the most well known (and widely used) analysis method is Flux Balance Analysis (FBA; Orth et al., 2010) which is performed on Genome Scale Reconstructions (GSR's; Oberhardt et al., 2009). Using FBA a target flux is optimized (e.g. maximizing a flux to biomass or minimizing ATP production) while other fluxes can be bounded to simulate a selected growth environment or specific metabolic state.

As constraint based models are generally underdetermined, i.e. few or none of the kinetic rate equations and related parameters are known, it is crucial that a model definition includes the ability to define optimization parameters such as objective functions, flux bounds and constraints ... currently this is not possible in the Systems Biology Markup Language (SBML) Level 2 or Level 3 core specification (Hucka et al., 2011, 2003).

The question of how to encode constraint based (a.k.a. 'FBA') models in SBML is not new. However, advances in the methods used to construct GSR scale models and the wider adoption of constraint based modelling in biotechnological/medical applications have led to a rapid increase in both the number of models being constructed and the tools used to analyze them.

Faced with such growth, both in number and diversity, the need for a standardized data format for the definition, exchange and annotation of constraint based models has become critical. As the core model components (e.g. species, reactions, stoichiometry) can already be efficiently described in SBML (with its significant community, software and tool support) the Flux Balance Constraints Package aims to extend SBML core by adding the elements necessary to describe current and future constraint based models.

1.1 Proposal corresponding to this package specification

This specification for Flux Balance Constraints in SBML Level 3 Version 1 is based on the proposal by the same authors, located at the following URL:

```
http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Balance_Constraints_Proposal_(2012)
```

The tracking number in the SBML issue tracking system (SBML Team, 2010) for Flux Balance Constraints package activities is 3154219. The version of the proposal used as the starting point for this specification is the version of March 2012. Previous versions of the current proposal are:

Version 3 (March 2012)

http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Balance_Constraints_Proposal_(2012)

Version 2 (March 2011)

 $http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Flux_Constraints_Pr$

Version 1 (February 2010)

http://precedings.nature.com/documents/4236/version/1

Details of earlier independent proposals are provided in Section 2.

13

20

21

23

16

23

27

29

31

33

34

38

1.2 Tracking number

As initially listed in the SBML issue tracking system under: http://sourceforge.net/tracker/?func=detail&aid= 3154219&group_id=71971&atid=894711.

1.3 Package dependencies

The Flux Balance Constraints package adds additional classes to SBML Level 3 Version 1 Core and has no dependency on any other SBML Level 3 package.

1.4 Document conventions

Following the precedent set by the SBML Level 3 Core specification document, we use UML 1.0 (Unified Modeling Language; Eriksson and Penker 1998; Oestereich 1999) class diagram notation to define the constructs provided by this package. We also use color in the diagrams to carry additional information for the benefit of those viewing the document on media that can display color. The following are the colors we use and what they represent:

- *Black*: Items colored black in the UML diagrams are components taken unchanged from their definition in the SBML Level 3 Core specification document.
- *Green*: Items colored green are components that exist in SBML Level 3 Core, but are extended by this package. Class boxes are also drawn with dashed lines to further distinguish them.
- *Blue*: Items colored blue are new components introduced in this package specification. They have no equivalent in the SBML Level 3 Core specification.

We also use the following typographical conventions to distinguish the names of objects and data types from other entities; these conventions are identical to the conventions used in the SBML Level 3 Core specification document:

AbstractClass: Abstract classes are classes that are never instantiated directly, but rather serve as parents of other object classes. Their names begin with a capital letter and they are printed in a slanted, bold, sans-serif type-face. In electronic document formats, the class names defined within this document are also hyperlinked to their definitions; clicking on these items will, given appropriate software, switch the view to the section in this document containing the definition of that class. (However, for classes that are unchanged from their definitions in SBML Level 3 Core, the class names are not hyperlinked because they are not defined within this document.)

Class: Names of ordinary (concrete) classes begin with a capital letter and are printed in an upright, bold, sansserif typeface. In electronic document formats, the class names are also hyperlinked to their definitions in this specification document. (However, as in the previous case, class names are not hyperlinked if they are for classes that are unchanged from their definitions in the SBML Level 3 Core specification.)

SomeThing: Attributes of classes, data type names, literal XML, and generally all tokens *other* than SBML UML class names, are printed in an upright typewriter typeface. Primitive types defined by SBML begin with a capital letter; SBML also makes use of primitive types defined by XML Schema 1.0 (Biron and Malhotra, 2000; Fallside, 2000; Thompson et al., 2000), but unfortunately, XML Schema does not follow any capitalization convention and primitive types drawn from the XML Schema language may or may not start with a capital letter.

For other matters involving the use of UML and XML, we follow the conventions used in the SBML Level 3 Core specification document.

Section 1 Introduction and motivation Page 4 of 29

2 Background

2.1 Problems with current SBML approaches

While there is currently no official way of encoding constraint based models in SBML L2 there have been pragmatic approaches used by a variety of groups and applications. Arguably the best and most widely used format is that used by the COBRA toolbox (Becker et al., 2007) where the metabolic network is well defined using SBML Reaction and Species classes. However, flux bounds and reactions that take part in the objective function are defined as LocalParameter objects and (implicitly) rely on all tools using the same naming convention. Similarly, reaction annotations are generally stored as key-value pairs in HTML Notes objects which has routinely led to different groups and software using in-house key definitions describing the same entity. While a step in the right direction this format is not suitable for implementation in SBML Level 3.

2.2 Past work on this problem or similar topics

The problem of describing and annotating 'FBA' models in SBML has been raised at various times in the past few years. In this regard there are two known putative proposals one by Karthik Raman and the other by the Church Laboratory. As far as we are aware these proposals never developed beyond their initial presentation at SBML forum/hackathons. In 2009 the discussion was reopened at the SBML Forum held in Stanford and has subsequently developed into the current active package proposal and this document (see Section 1).

Brett Olivier (2009) SBML Level 3 FBA package discussion

http://sbml.org/images/4/4a/Olivier_sbml_forum_2009_09_04.pdf

Karthik Raman (2005) Flux annotations in SBML

http://sbml.org/images/d/d9/Raman-flux-annotations.pdf

Church laboratory (pre 2005) Metabolic flux model annotations

http://sbml.org/Community/Wiki/Old_known_SBML_annotations_list

Section 2 Background Page 5 of 29

3 Proposed syntax and semantics

In this section, we define the syntax and semantics of the Flux Balance Constraints package for SBML Level 3 Version 1. We expound on the various data types and constructs defined in this package, then in Section 4 on page 12, we provide complete examples of using the constructs in example SBML models.

3.1 Namespace URI and other declarations necessary for using this package

Every SBML Level 3 package is identified uniquely by an XML namespace URI. For an SBML document to be able to use a given SBML Level 3 package, it must declare the use of that package by referencing its URI. The following is the namespace URI for this version of the Flux Balance Constraints package for SBML Level 3 Version 1:

```
"http://www.sbml.org/sbml/level3/version1/fbc/version1"
```

In addition, SBML documents using a given package must indicate whether understanding the package is required for complete mathematical interpretation of a model, or whether the package is optional. This is done using the attribute **required** on the **<sbml>** element in the SBML document. For the Flux Balance Constraints package, the value of this attribute must be set to "true".

The following fragment illustrates the beginning of a typical SBML model using SBML Level 3 Version 1 and this version of the Flux Balance Constraints package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core" level="3"
version="1"
    xmlns:fbc="http://www.sbml.org/sbml/level3/version1/fbc/version1"
    fbc:required="true">
```

3.2 Primitive data types

Section 3.1 of the SBML Level 3 Version 1 Core specification defines a number of primitive data types and also uses a number of XML Schema 1.0 data types (Biron and Malhotra, 2000). More specifically we make use of integer, double, string and SIdRef. In addition we make use of four new primitives FbcSId, FbcSIdRef as well as the enumerations FbcType and FbcOperation, see Figure 1 for the interrelation between these entities.

3.2.1 Type FbcSId

The type FbcSId is derived from SId (SBML Level 3 Version 1 Core specification Section 3.1.7) and has identical syntax. The FbcSId type is used as the data type for the identifiers of FluxBound (Section 3.5) and Objective (Section 3.6) classes. By using a separate identifier type we differentiate them from others defined in the SBML model and thus ensuring data encapsulation.

3.2.2 Type FbcSIdRef

Type FbcSIdRef is used for all attributes that refer to identifiers of type FbcSId. Derived from FbcSId it has the restriction that the value of an attribute having type FbcSIdRef must match the value of a FbcSId attribute in the current model. In the FBC package the ListOfObjectives has an attribute of this type that is used to refer to an 'active' Objective .

3.2.3 Type FbcType

The Flux Balance Constraints package defines a new enumerated type **FbcType** which represents the optimization sense of the objective function. It can have one of the following two values "maximize" or "minimize".

18

20

21 22

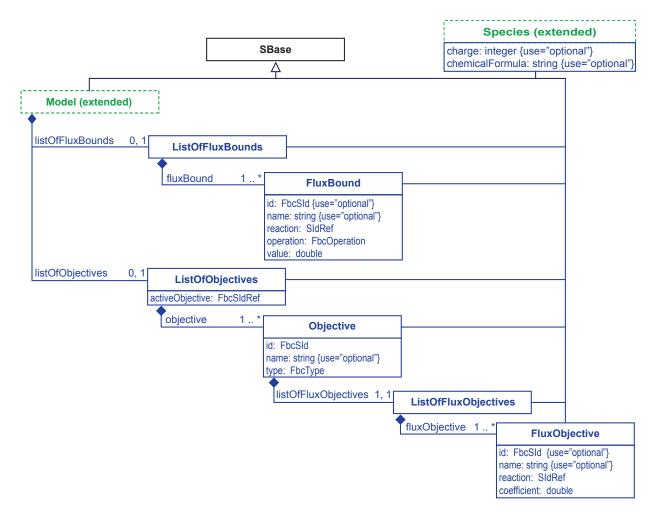


Figure 1: A UML representation of the Flux Balance Constraints package classes. See Section 1.4 for conventions related to this figure. The individual classes are further discussed in the text.

3.2.4 Type FbcOperation

The Flux Balance Constraints package defines a new enumerated type FbcOperation which represents a boolean operator. It can take only one of the following values: "lessEqual", "greaterEqual", "less", "greater" or "equal".

3.3 The extended Model class

The **SBML Model** class is extended with the addition of two children, i.e. a **listOfFluxBounds** and a **listOfObjectives**. 5 The **Model** may contain at most one of these lists.

3.3.1 The FBC listOfFluxBounds

As shown in Figure 1 the **ListOfFluxBounds** is derived from **SBase** and inherits the attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. **ListOfFluxBounds** must contain at least one **FluxBound** (defined in Section 3.5).

3.3.2 The FBC listOfObjectives

As shown in Figure 1 the **ListOfObjectives** is derived from **SBase** and inherits the attributes **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. Unlike most other **SBML ListOf** classes, **ListOfObjec**-

tives introduces an additional required attribute activeObjective. The ListOfObjectives must contain at least one Objective (defined in Section 3.6).

The activeObjective attribute

This attribute is of type FbcSIdRef and can only refer to an existing **Objective** (FbcSId). This required attribute exists so that when multiple **Objective** 's are included in a single model, the model will always be well described i.e. there is a single, primary objective function which defines a single optimum and its associated solution space.

3.4 The extended Species class

The Flux Balance Constraints package extends the SBML Level 3 Version 1 Core **Species** class with the addition of two attributes:

The charge attribute

The optional attribute **charge** which contains a signed **integer** referring to the **Species** object's charge and is defined as it was in the **SBML** Level 2 Version 1 specification: "The optional field charge takes an integer indicating the charge on the species (in terms of electrons, not the SI unit coulombs)."

The chemicalFormula attribute

The optional attribute **chemicalFormula** containing a **string** that represents the **Species** objects elemental composition.

```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP"
  compartment="Cytosol" boundaryCondition="false"
  fbc:charge="-4" fbc:chemicalFormula="C10H12N5013P3"
  initialConcentration="0" hasOnlySubstanceUnits="false"
/>
```

While there are many ways of referring to an elemental composition the purpose of the chemicalFormula attribute is to allow reaction balancing and validation which is particularly important in constraint based models. To this end it is recommended that the format of chemicalFormula should follow the Hill system (or notation). Here the number of carbon atoms in a molecule is indicated first, followed by the number of hydrogen atoms and then the number of all other chemical elements in alphabetical order. When the formula contains no carbon; all elements, including hydrogen, are listed alphabetically.

Species (extended) charge: integer {use="optional"} chemicalFormula: string {use="optional"}

Figure 2: A UML representation of the extended SBML Species class used in the Flux Balance Constraints package. See Section 1.4 for conventions related to this figure.

3.5 The FBC FluxBound class

FluxBound is a new FBC class derived from **SBML** *SBase* that inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. The purpose of this class is to hold a single (in)equality that provides the maximum or minimum value that a reaction flux can obtain at steady state. It implements four attributes.

Section 3 Proposed syntax and semantics

12

19

20

21 23

The id and name attributes

A **FluxBound** has two optional attributes: **id** an attribute of type **FbcSId** and **name** an attribute of type **string**.

The reaction attribute

The required **reaction** attribute of type **SIdRef**. This attribute must refer to a **Reaction** element defined within the enclosing model.

The operation attribute

The operation attribute contains a value of type FbcOperation that can take a limited set of boolean operators as defined in Section 3.2.4. The operation attribute represents a mathematical (in)equality of the form <reaction> <perator> <value> e.g. $R_5 >= 0$, $R_5 < \infty$ and $R_7 = 1.0$. The mapping between traditional mathematical symbols and FbcOperation values is as follows:

```
<= → "lessEqual"

>= → "greaterEqual"

< → "less"

> → "greater"

= → "equal"
```

The value attribute

The **value** attribute holds a **double** value representing the numerical value of the flux bound. This may include an explicitly defined $\pm \infty$ encoded as a value, e.g. "INF".

Encoding the FluxBound

As described in Section 3.5 the flux bound represents a mathematical (in)equality of the form <reaction><operator><value>.

In SBML Level 3 Version 1 with FBC this is encoded as:

This example illustrates two things: the encoding of ∞ and that care should be used when selecting inequalities such as "less" or "greater". While mathematically there is a difference, this difference is only practically relevant when working with rational arithmetic (solvers).

3.6 The FBC Objective class

The FBC **Objective** class is derived from **SBML SBase** and inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**. An integral component in a complete description of a steady-state model is the so-called 'objective function' which generally consist of a linear combination of model variables (fluxes) and a sense (direction). In the FBC package this concept is succinctly captured in the **Objective** class.

The id and name attributes

An **Objective** has a required attribute **id** of type **FbcSId** and an optional attribute **name** of type **string**.

21

25

26

28

29

30

31

32 33

FluxBound

id: FbcSId {use="optional"}
name: string {use="optional"}

reaction: SIdRef

operation: FbcOperation

value: double

Figure 3: A UML representation of the Flux Balance Constraints package FluxBound class. See Section 1.4 for conventions related to this figure.

The type attribute

The required **type** attribute contains an **FbcType** type which represents the sense of the optimality constraint and can take one of two values:

```
maximize \mapsto \text{``maximize''}
minimize \mapsto \text{``minimize''}
```

The listOfFluxObjectives element

The element listOfFluxObjectives which contains a ListOfFluxObjectives is derived from and functions like a typical SBML ListOf_ class with the restriction that it must contain one or more elements of type FluxObjective (see Section 3.7). This implies that if an Objective is defined there should be at least one FluxObjective contained in a ListOfFluxObjectives.

Objective

id: FbcSld

name: string {use="optional"}

type: FbcType

Figure 4: A UML representation of the Flux Balance Constraints package Objective class. See Section 1.4 for conventions related to this figure.

Encoding the Objective

The Flux Balance Constraints package allows for the definition of multiple model objectives with one being designated as active (see Section 3.6) as illustrated in this example:

```
<fbc:list0f0bjectives fbc:active0bjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
        <fbc:list0fFlux0bjectives>
        <fbc:flux0bjective fbc:reaction="R101" fbc:coefficient="1"/>
        </fbc:list0fFlux0bjectives>
        <fbc:objective>
        <fbc:objective fbc:id="obj2" fbc:type="minimize">
              <fbc:list0fFlux0bjectives>
              <fbc:list0fFlux0bjectives>
              <fbc:flux0bjective fbc:reaction="R102" fbc:coefficient="-2.5"/>
                    <fbc:flux0bjective fbc:reaction="R103" fbc:coefficient="1"/>
                   </fbc:list0fFlux0bjectives>
        </fbc:list0fObjective>
        </fbc:list0fObjectives>
```

16

19

20

22

23

25

26

Note how both **Objective** instances differ in **type** and each contains different set of **FluxObjectives** (see Section 3.7).

3.7 The FBC FluxObjective class

The FBC **FluxObjective** class is derived from **SBML SBase** and inherits **metaid** and **sboTerm**, as well as the subcomponents for **Annotation** and **Notes**.

The FluxObjective class is a relatively simple container for a model variable weighted by a signed linear coefficient.

The id and name attributes

A FluxObjective has two optional attributes: id an attribute of type FbcSId and name an attribute of type string.

The reaction and coefficient attributes

The required reaction is of type SIdRef and is restricted to refer only to an SBML Reaction while the coefficient attribute holds a double referring to the coefficient that this FluxObjective takes in the enclosing Objective. For example the objective Maximize: 1 R1 + 2 R2 would be encoded as

```
<fbc:listOfObjectives fbc:activeObjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
        <fbc:listOfFluxObjectives>
        <fbc:fluxObjective fbc:reaction="R1" fbc:coefficient="1"/>
        <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="2"/>
        </fbc:listOfFluxObjectives>
        </fbc:listOfObjective></fbc:listOfObjectives>
```

FluxObjective

id: FbcSId {use="optional"}
name: string {use="optional"}

reaction: SldRef coefficient: double

Figure 5: A UML representation of the Flux Balance Constraints package FluxObjective class. See Section 1.4 for conventions related to this figure.

15

19

20

4 Examples

This section contains a worked example showing the encoding of a model suitable for Flux Balance Analysis using the Flux Balance Constraints package.

4.1 Example of the FBC syntax

4.1.1 Kinetic model description



Figure 6: FBC syntax example: a simple four reaction pathway. The reactions are R1, R2, X1, X2 with fixed species IN, OUT, ATP, NADH and variable species A, B.

As shown in Figure 6 this example is a simple four reaction pathway that transforms metabolite *IN* to *OUT*. The model was created and analyzed using the SBW Flux Balance FBC implementation Bergmann (2012); Bergmann and Sauro (2006). In **SBML** each reaction is represented as a chemical process transforming reactants to products, e.g. reaction *R1* is encoded in XML as (see also the complete example provided at the end of this section):

```
<reaction id="R1" reversible="false" fast="false">
  <list0fReactants>
    <speciesReference species="IN" stoichiometry="1" constant="true"/>
    </list0fReactants>
    stoifProducts>
        <speciesReference species="A" stoichiometry="1" constant="true"/>
        </list0fProducts>
    </reaction>
```

13

18

Using the reagent identity and stoichiometry it is possible to compactly describe this network in terms of its reaction stoichiometry as shown in Table 1 where each reaction is represented as a column. While the stoichiometry

Table 1: Example one: stoichiometric matrix, N

contains the structural properties of the reaction network the full description of a biological model can be described as a set of ordinary differential equations (ODE's). Of course other formalisms do exist, but here we will

Section 4 Examples Page 12 of 29

18

25

30

31

32

33

34

35 36

concentrate exclusively on kinetic models where the change in concentration of each variable component in the system $(\frac{ds}{dt})$ is a non-linear function of the rates of the reactions which either create or consume it (the product of the stoichiometric matrix, **N** and the vector of reaction rates, **v**).

$$\frac{ds}{dt} = \mathbf{N}\mathbf{v} \tag{1}$$

The formulation of the kinetic model, as shown in Equation 1 is typical of the kind that can already be described using SBML Level 3 Version 1 Core where the vector **v** would contain rate equations as a function of parameters and variable species. In a steady-state, constraint based model these rates are considered unknowns and the system of equations can be rewritten as a set of linear constraints (see Equation 2):

$$NJ = 0 (2)$$

Note that the rate vector \mathbf{v} is now represented as the steady-state flux vector \mathbf{J} . However, in order to perform a typical steady-state analysis such as flux balance analysis (FBA) we need to include more information into the model description. SBML Level 3 Version 1 Core does not have an unambiguous way of encoding either a capacity constraint or an objective target and for this we need to use the additional constructs provided by the Flux Balance Constraints package. In the following sections the same model data is shown encoded as both XML and in the LP format (as used by IBM CPLEX).

4.1.2 Capacity constraints

A capacity constraint: in this example the maximum limit (upper bound) of the flux through reaction *R1* is set to be one (with an arbitrary unit of flux). In LP format this can be written as:

```
Bounds
R1 <= 1.0
```

the same information encoded as XML:

```
<fbc:listOfFluxBounds>
  <fbc:fluxBound fbc:reaction="R1" fbc:operation="lessEqual" fbc:value="1"/>
  </fbc:listOfFluxBounds>
```

4.1.3 Objective function

This described a target which can be maximized or minimized: in this example the flux through reaction *R2* will be *maximized*.

```
Maximize objective1_objf: + 1.0 R2
```

the same information encoded as XML:

```
<fbc:listOfObjectives fbc:activeObjective="objective1">
  <fbc:objective fbc:id="objective1" fbc:type="maximize">
  <fbc:listOfFluxObjectives>
  <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="1"/>
  </fbc:listOfFluxObjectives>
  </fbc:objective>
  </fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fbc:listOfObjectives></fi>
```

4.1.4 Complete worked example

To conclude we show how the complete model described in Figure 6 encoded as both an LP and as XML. Formulated as an LP the problem can be written as:

Section 4 Examples Page 13 of 29

35

41

52

53

54

55

```
Naximize
objective1_objf: + 1.0 R2

Subject To
    A: + R1 - X1 - X2 = 0.0
    B: - R2 + X1 + X2 = 0.0

Bounds
R1 <= 1.0
0.0 <= R2 <= +inf
0.0 <= X1 <= +inf
0.0 <= X2 <= +inf
END</pre>
```

Solving this we find that maximization of flux through *R2* gives an optimal solution of *one* shown with one possible solution for **J** (see Equation 3).

$$\begin{pmatrix} 1 & 0 & -1 & -1 \\ 0 & -1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1.0 \\ 1.0 \\ 0.0 \\ 1.0 \end{pmatrix} = \mathbf{0}$$
 (3)

Finally we provide the complete model, described above, encoded using the Flux Balance Constraints package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core"</pre>
      xmlns:fbc="http://www.sbml.org/sbml/level3/version1/fbc/version1"
      level="3" version="1" fbc:required="false">
 <model id="fbcSpecExample1" timeUnits="time">
    <listOfUnitDefinitions>
      <unitDefinition id="volume">
        tofUnits>
          <unit kind="litre" exponent="1" scale="0" multiplier="1"/>
        </listOfUnits>
      </unitDefinition>
      <unitDefinition id="substance">
          <unit kind="mole" exponent="1" scale="0" multiplier="1"/>
        </listOfUnits>
      </unitDefinition>
      <unitDefinition id="time">
          <unit kind="second" exponent="1" scale="0" multiplier="1"/>
        </listOfUnits>
      </unitDefinition>
    </listOfUnitDefinitions>
    <listOfCompartments>
      <compartment id="compartment" spatialDimensions="3" size="1"</pre>
       units="volume" constant="true"/>
    </list0fCompartments>
    <listOfSpecies>
      <species id="IN" compartment="compartment" initialConcentration="0"</pre>
       substanceUnits="substance" hasOnlySubstanceUnits="false"
       boundaryCondition="true" constant="false"/>
      <species id="OUT" compartment="compartment" initialConcentration="0"</pre>
       substanceUnits="substance" hasOnlySubstanceUnits="false"
       boundaryCondition="true" constant="false"/>
      <species id="A" compartment="compartment" initialConcentration="0"</pre>
       substanceUnits="substance" hasOnlySubstanceUnits="false"
       boundaryCondition="false" constant="false"/>
      <species id="B" compartment="compartment" initialConcentration="0"</pre>
```

Section 4 Examples Page 14 of 29

14

15

16

18

19

20

21

22

23

24

27

29

30

32

33

34

35

36

37

38

39

41

42

43

44

47

50

51

52

53

55

56

57

```
substanceUnits="substance" hasOnlySubstanceUnits="false"
      boundaryCondition="false" constant="false"/>
     <species id="ATP" compartment="compartment" initialConcentration="0"</pre>
      substanceUnits="substance" hasOnlySubstanceUnits="false"
      boundaryCondition="true" constant="false"/>
      <species id="NADH" compartment="compartment" initialConcentration="0"</pre>
      substanceUnits="substance" hasOnlySubstanceUnits="false"
      boundaryCondition="true" constant="false"/>
   </listOfSpecies>
   <reaction id="R1" reversible="false" fast="false">
       <listOfReactants>
          <speciesReference species="IN" stoichiometry="1" constant="true"/>
       </list0fReactants>
       1 istOfProducts>
          <speciesReference species="A" stoichiometry="1" constant="true"/>
       </listOfProducts>
     </reaction>
     <reaction id="R2" reversible="false" fast="false">
       <listOfReactants>
         <speciesReference species="B" stoichiometry="1" constant="true"/>
       </listOfReactants>
       tofProducts>
          <speciesReference species="OUT" stoichiometry="1" constant="true"/>
       </list0fProducts>
     </reaction>
     <reaction id="X1" reversible="false" fast="false">
       <listOfReactants>
         <speciesReference species="A" stoichiometry="1" constant="true"/>
       </listOfReactants>
       tofProducts>
         <speciesReference species="ATP" stoichiometry="1" constant="true"/>
         <speciesReference species="B" stoichiometry="1" constant="true"/>
       </listOfProducts>
     </reaction>
     <reaction id="X2" reversible="false" fast="false">
       tofReactants>
          <speciesReference species="A" stoichiometry="1" constant="true"/>
       </list0fReactants>
       tofProducts>
         <speciesReference species="B" stoichiometry="1" constant="true"/>
          <speciesReference species="NADH" stoichiometry="1" constant="true"/>
       </listOfProducts>
     </reaction>
   </listOfReactions>
   <fbc:listOfFluxBounds>
      <fbc:fluxBound fbc:reaction="R1" fbc:operation="lessEqual" fbc:value="1"/>
   </fbc:listOfFluxBounds>
   <fbc:list0f0bjectives fbc:active0bjective="objective1">
     <fbc:objective fbc:id="objective1" fbc:type="maximize">
       <fbc:listOfFluxObjectives>
         <fbc:fluxObjective fbc:reaction="R2" fbc:coefficient="1"/>
       </fbc:listOfFluxObjectives>
      </fbc:objective>
   </fbc:list0f0bjectives>
 </model>
</sbml>
```

Section 4 Examples Page 15 of 29

5 Best practices

In this section, we recommend a number of practices for using and interpreting various constructs in the Flux Balance Constraints package. These recommendations are non-normative, but we advocate them strongly; ignoring them will not render a model invalid, but may reduce inter-operability between software and models.

5.1 Examples contrasting the current SBML L2 encoding with L3 and FBC

These examples contrast some elements of an existing model, iJR904 from the BiGG Database encoded in the COBRA format Becker et al. (2007); Reed et al. (2003); Schellenberger et al. (2010) that have been translated into SBML Level 3 Version 1 using the CBMPy implementation of the FBC package Olivier (2012); Olivier et al. (2005) and libSBML experimental ver. 5.6.0 Bornstein et al. (2008).

Objective function definition

SBML Level 2 objective function

15

18

19

22

24

25 26

30

32

33

34

35

42

44

45

The SBML Level 3 objective function

```
<fbc:list0f0bjectives fbc:active0bjective="obj1">
  <fbc:objective fbc:id="obj1" fbc:type="maximize">
    <fbc:list0fFlux0bjectives>
    <fbc:flux0bjective fbc:reaction="R_BiomassEcoli" fbc:coefficient="1"/>
    </fbc:list0fFlux0bjectives>
  </fbc:objective>
  </fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0bjectives></fbc:list0f0b
```

Species definition

It is particularly useful to contrast the differences in the **Species** definition as it is used in genome scale models.

SBML Level 2 Species annotation version 1

To begin with we let's examine the **SBML** Level 2 Version 1 species definition used by the BiGG database and COBRA Becker et al. (2007); Schellenberger et al. (2010). Note how the name attribute is overloaded with the chemical formula.

```
<species id="M_atp_c" name="ATP_C10H12N5013P3"
compartment="Cytosol" charge="-4" />
```

Section 5 Best practices Page 16 of 29

18

19

20 21 22

27

29

30

32

33

34

35

36

37

38

40

41

43

44

46

47

50

52

53

55

56

57

58

SBML Level 2 Species annotation version 2

A newer variation of the above, probably necessitated by the discontinuation of the **charge** attribute in **SBML** and libSBML

```
<species id="M_atp_c" name="ATP" compartment="c">
  <notes>
    <body xmlns="http://www.w3.org/1999/xhtml">
        FORMULA: C10H12N5013P3
        CHARGE: -4
        </body>
        </notes>
        </species>
```

The SBML Level 3 Species attributes

Hopefully, with the adoption of SBML FBC these species properties can be unified into a common format.

```
<species metaid="meta_M_atp_c" id="M_atp_c" name="ATP"
  compartment="Cytosol" boundaryCondition="false"
  fbc:charge="-4" fbc:chemicalFormula="C10H12N5013P3"
  initialConcentration="0" hasOnlySubstanceUnits="false"
/>
```

Reaction definition and flux bounds

SBML Level 2 Reaction

```
<reaction id="R_GTHS" name="glutathione_synthetase" reversible="false">
 <html:p>Abbreviation: R_GTHS</html:p>
 <html:p>Synonyms: _0</html:p>
 <html:p>EC Number: 6.3.2.3</html:p>
 <html:p>SUBSYSTEM: Cofactor and Prosthetic Group Biosynthesis</html:p>
 <html:p>Equation: [c] : atp + glucys + gly --&gt; adp + gthrd + h + pi</html:p>
 <html:p>Confidence Level: 0</html:p>
 <html:p>NCD</html:p>
 <html:p>genes:</html:p>
 <html:p>LOCUS:b2947#ABBREVIATION:gshB#ECNUMBERS:6.3.2.3#</html:p>
  <html:p>proteins:</html:p>
 <html:p>NAME:glutathione synthase#ABBREVIATION:GshB#</html:p>
 <html:p>GENE ASSOCIATION: (b2947)</html:p>
 </notes>
 <listOfReactants>
 <speciesReference species="M_atp_c" stoichiometry="1"/>
 <speciesReference species="M_glucys_c" stoichiometry="1"/>
 <speciesReference species="M_gly_c" stoichiometry="1"/>
 </listOfReactants>
 <listOfProducts>
 <speciesReference species="M_adp_c" stoichiometry="1"/>
 <speciesReference species="M_gthrd_c" stoichiometry="1"/>
 <speciesReference species="M_h_c" stoichiometry="1"/>
 <speciesReference species="M_pi_c" stoichiometry="1"/>
 </listOfProducts>
 <kineticLaw>
 <math xmlns="http://www.w3.org/1998/Math/MathML">
  <ci>FLUX_VALUE</ci>
 <listOfParameters>
  <parameter id="LOWER_BOUND" value="0" units="mmol_per_gDW_per_hr"/>
  <parameter id="UPPER_BOUND" value="999999" units="mmol_per_gDW_per_hr"/>
  <parameter id="OBJECTIVE_COEFFICIENT" value="0" />
```

Section 5 Best practices Page 17 of 29

15

16

17

18

21

23

24

26

27

28

29

30

32

33

35

36

38

39

49

43

45

46

47

48

```
<parameter id="FLUX_VALUE" value="0" units="mmol_per_gDW_per_hr"/>
  </listOfParameters>
  </kineticLaw>
  </reaction>
```

The SBML Level 3 Reaction and FluxBound

As an example and where (unambiguously) possible the **SBML** Level 2 annotation has been converted into MIRIAM compliant RDF, in this case the *EC number*. In addition this example highlights an open issue, namely, how to deal with the information currently encoded in the **Notes** element. Currently this information is not completely encodable using the current **SBML** annotation mechanism, however, for an example of an alternative mechanism, implemented as a tool specific annotation please see Section 6.

```
<reaction metaid="meta_R_GTHS" id="R_GTHS" name="glutathione_synthetase" reversible="false">
<annotation>
 <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
   xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
    xmlns:vCard="http://www.w3.org/2001/vcard-rdf/3.0#"
   xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
   xmlns:bqmodel="http://biomodels.net/model-qualifiers/">
   <rdf:Description rdf:about="#meta_R_GTHS">
   <bqbiol:is>
    <rdf:Bag>
     <rdf:li rdf:resource="http://identifiers.org/ec-code/6.3.2.3"/>
    </rdf:Bag>
   </bqbiol:is>
  </rdf:Description>
 </rdf:RDF>
</annotation>
 <listOfReactants>
 <speciesReference species="M_atp_c" stoichiometry="1"/>
 <speciesReference species="M_glucys_c" stoichiometry="1"/>
 <speciesReference species="M_gly_c" stoichiometry="1"/>
 </listOfReactants>
 tofProducts>
 <speciesReference species="M_adp_c" stoichiometry="1"/>
 <speciesReference species="M_gthrd_c" stoichiometry="1"/>
 <speciesReference species="M_h_c" stoichiometry="1"/>
 <speciesReference species="M_pi_c" stoichiometry="1"/>
</list0fProducts>
</reaction>
```

```
<fbc:listOfFluxBounds>
  <fbc:fluxBound fbc:id="R_GTHS_lower_bnd" fbc:reaction="R_GTHS" fbc:operation="greaterEqual"
    fbc:value="0"/>
  <fbc:fluxBound fbc:id="R_GTHS_upper_bnd" fbc:reaction="R_GTHS" fbc:operation="lessEqual"
    fbc:value="999999"/>
  </fbc:listOfFluxBounds>
```

Section 5 Best practices Page 18 of 29

6 Future development

In this section we highlight some open issues not addressed in this version of the FBC specification.

6.1 Model annotation

While the Flux Balance Constraints package address the basic constraint based model structure the effective annotation of individual model components is critical to its efficient (re)use. Here two examples of custom annotations are provided as an example of how this could be achieved.

6.1.1 Gene association annotation

An example of an annotation currently encoded in the **Notes** element that is not encodable using the **SBML Annotation** mechanism is the so called "Gene Association".

In order to capture this information we propose the following mechanism which can be used to represent a logical expression containing "genes" in this case the final (transcribed/translated) protein product of a gene which forms a sub-component of a protein.

```
<fbc:listOfGeneAssociations>
 <fbc:geneAssociation fbc:id="ga1" fbc:reaction="R_ACGAptspp">
  <fbc:or>
   <fbc:and>
    <fbc:gene>b2415</fbc:gene>
    <fbc:gene>b2417</fbc:gene>
    <fbc:gene>b2416</fbc:gene>
    <fbc:gene>b1101</fbc:gene>
   </fbc:and>
   <fbc:and>
    <fbc:gene>b2415</fbc:gene>
    <fbc:gene>b0679</fbc:gene>
    <fbc:gene>b2416</fbc:gene>
   </fbc:and>
  </fbc:or>
 </fbc:geneAssociation>
</fbc:listOfGeneAssociations>
```

6.1.2 Generic annotation mechanism

An annotation issue previously introduced in the example shown in Section 4 where a **SBML** Level 2 **Reaction** is encoded using the Flux Balance Constraints package.

SBML Level 2 Reaction

```
<reaction id="R_GTHS" name="glutathione_synthetase" reversible="false">
<notes>
  <html:p>Abbreviation: R_GTHS</html:p>
  <html:p>Synonyms: _0</html:p>
  <html:p>Synonyms: _0</html:p>
  <html:p>EC Number: 6.3.2.3</html:p>
  <html:p>SUBSYSTEM: Cofactor and Prosthetic Group Biosynthesis</html:p>
  <html:p>Equation: [c]: atp + glucys + gly --&gt; adp + gthrd + h + pi</html:p>
  <html:p>Confidence Level: 0</html:p>
  <html:p>NCD</html:p>
  <html:p>NCD</html:p>
  <html:p>LOCUS:b2947#ABBREVIATION:gshB#ECNUMBERS:6.3.2.3#</html:p>
  <html:p>Proteins:</html:p>
  <html:p>NAME:glutathione synthase#ABBREVIATION:GshB#</html:p>
  <html:p>SAME:glutathione synthase#ABBREVIATION:GshB#</html:p>
  </notes>
```

15

18

21

26

29

30

33

38

43

44

49

18

19

20

21

22

23

32

33

35

36

38

39

41

42

44

47

52

53

58

59

```
<listOfReactants>
 <speciesReference species="M_atp_c" stoichiometry="1"/>
 <speciesReference species="M_glucys_c" stoichiometry="1"/>
 <speciesReference species="M_gly_c" stoichiometry="1"/>
<speciesReference species="M_adp_c" stoichiometry="1"/>
 <speciesReference species="M_gthrd_c" stoichiometry="1"/>
 <speciesReference species="M_h_c" stoichiometry="1"/>
 <speciesReference species="M_pi_c" stoichiometry="1"/>
</listOfProducts>
<kineticLaw>
 <math xmlns="http://www.w3.org/1998/Math/MathML">
  <ci>FLUX_VALUE</ci>
 <listOfParameters>
  <parameter id="LOWER_BOUND" value="0" units="mmol_per_gDW_per_hr"/>
  <parameter id="UPPER_BOUND" value="999999" units="mmol_per_gDW_per_hr"/>
  <parameter id="OBJECTIVE_COEFFICIENT" value="0" />
  <parameter id="FLUX_VALUE" value="0" units="mmol_per_gDW_per_hr"/>
 </listOfParameters>
</kineticLaw>
</reaction>
```

SBML Level 3 Reaction

Note how that in order to maintain all the annotations encoded in the **SBML** Level 2 **Reaction notes** a custom annotation is introduced i.e. the KeyValueData class¹.

In general this example highlights the need for a community supported annotation mechanism for genome scale, constraint based models.

```
<reaction metaid="meta_R_GTHS" id="R_GTHS" name="glutathione_synthetase" reversible="false">
 <listOfKeyValueData xmlns="http://pysces.sourceforge.net/KeyValueData">
  <data id="subsystem" type="string" value="Cofactor_and_Prosthetic_Group_Biosynthesis"/>
   <data id="name" type="string" value="glutathione_synthase#ABBREVIATION:GshB#"/>
  <data id="gene_association" type="string" value="(b2947)"/>
<data id="equation" type="string" value="[c]_:_atp_+_glucys_+_gly_--&gt;_adp_+_gthrd_+_h_+_pi"/>
  <data id="genes" type="string"/>
  <data id="proteins" type="string"/>
  <data id="locus" type="string" value="b2947#ABBREVIATION:gshB#ECNUMBERS:6.3.2.3#"/>
  <data id="abbreviation" type="string" value="R_GTHS"/>
  <data id="synonyms" type="string" value="_0"/>
  <data id="confidence_level" type="string" value="0"/>
  </listOfKeyValueData>
 <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
   xmlns:dc="http://purl.org/dc/elements/1.1/" xmlns:dcterms="http://purl.org/dc/terms/"
   xmlns:vCard="http://www.w3.org/2001/vcard-rdf/3.0#"
    xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
   xmlns:bqmodel="http://biomodels.net/model-qualifiers/">
   <rdf:Description rdf:about="#meta_R_GTHS">
   <bqbiol:is>
     <rdf:Bag>
     <rdf:li rdf:resource="http://identifiers.org/ec-code/6.3.2.3"/>
     </rdf:Bag>
   </bqbiol:is>
  </rdf:Description>
 </rdf:RDF>
 </annotation>
 <listOfReactants>
 <speciesReference species="M_atp_c" stoichiometry="1"/>
 <speciesReference species="M_glucys_c" stoichiometry="1"/>
```

 $^{^{}m l}$ More information about this annotation is available at http://pysces.sourceforge.net/KeyValueData

A Validation of SBML documents

A.1 Validation and consistency rules

This section summarizes all the conditions that must (or in some cases, at least *should*) be true of an SBML Level 3 Version 1 model that uses the Flux Balance Constraints package. We use the same conventions as are used in the SBML Level 3 Version 1 Core specification document. In particular, there are different degrees of rule strictness. Formally, the differences are expressed in the statement of a rule: either a rule states that a condition *must* be true, or a rule states that it *should* be true. Rules of the former kind are strict SBML validation rules—a model encoded in SBML must conform to all of them in order to be considered valid. Rules of the latter kind are consistency rules. To help highlight these differences, we use the following three symbols next to the rule numbers:

- ✓ A checked box indicates a *requirement* for SBML conformance. If a model does not follow this rule, it does not conform to the Flux Balance Constraints specification. (Mnemonic intention behind the choice of symbol: "This must be checked.")
- A triangle indicates a *recommendation* for model consistency. If a model does not follow this rule, it is not considered strictly invalid as far as the Flux Balance Constraints specification is concerned; however, it indicates that the model contains a physical or conceptual inconsistency. (Mnemonic intention behind the choice of symbol: "This is a cause for warning.")
- ★ A star indicates a strong recommendation for good modeling practice. This rule is not strictly a matter of SBML encoding, but the recommendation comes from logical reasoning. As in the previous case, if a model does not follow this rule, it is not strictly considered an invalid SBML encoding. (Mnemonic intention behind the choice of symbol: "You're a star if you heed this.")

The validation rules listed in the following subsections are all stated or implied in the rest of this specification document. They are enumerated here for convenience. Unless explicitly stated, all validation rules concern objects and attributes specifically defined in the Flux Balance Constraints package.

For convenience and brevity, we use the shorthand "fbc:x" to stand for an attribute or element name x in the namespace for the Flux Balance Constraints package, using the namespace prefix fbc. In reality, the prefix string may be different from the literal "fbc" used here (and indeed, it can be any valid XML namespace prefix that the modeler or software chooses). We use "fbc:x" because it is shorter than to write a full explanation everywhere we refer to an attribute or element in the Flux Balance Constraints package namespace.

General rules about this package

- To conform to the Flux Balance Constraints package specification for SBML Level 3 Version 1, an SBML document must declare the use of the following XML Namespace:

 [-25] "http://www.sbml.org/sbml/level3/version1/fbc/version1". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.1 on page 6.)
- Wherever they appear in an SBML document, elements and attributes from the Flux Balance Constraints package must be declared either implicitly or explicitly to be in the XML namespace "http://www.sbml.org/sbml/level3/version1/fbc/version1". (References: SBML Level 3 Package Specification for Flux Balance Constraints , Version 1, Section 3.1 on page 6.)

General rules about identifiers

(Extends validation rule #10301 in the SBML Level 3 Version 1 Core specification.) Within a Model the values of the attributes id and fbc:id on every instance of the following classes of objects must be unique across the set of all id and fbc:id attribute values of all such objects in a model: the Model itself, plus all contained FunctionDefinition, Compartment, Species, Reaction, SpeciesReference, ModifierSpeciesReference, Event, and Parameter objects, plus

14

19

22

27

28

| Rules for the ex | xtended SBML class | 4 |
|--------------------|---|------------------|
| fbc-20101 | In all SBML documents using the Flux Balance Constraints package, the SBML object must | 5 |
| | include a value for the attribute fbc:required attribute. (References: SBML Level 3 Version 1 | 6 |
| | Core, Section 4.1.2.) | 7 |
| fbc-20102 | The value of attribute fbc:required on the SBML object must be of the data type boolean. (References: SBML Level 3 Version 1 Core, Section 4.1.2.) | 8 |
| fbc-20103 ✓ | The value of attribute fbc:required on the SBML object must be set to "true". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.1 on page 6.) | 10 11 12 |
| Rules for exten | ded Model object | 13 |
| fbc-20201 ☑ | There may be at most one instance of each of the following kinds of objects within a Model | 14 |
| | object using Flux Balance Constraints: ListOfFluxBounds and ListOfObjectives . (References: | 15 |
| | SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.3 on | 16 |
| | page 7.) | 17 |
| fbc-20202 | The various ListOf subobjects with an Model object are optional, but if present, these con- | 18 |
| | tainer object must not be empty. Specifically, if any of the following classes of objects are | 19 |
| | present on the Model , it must not be empty: ListOfFluxBounds and ListOfObjectives . (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Sec- | 20 |
| | tion 3.3 on page 7.) | 22 |
| fbc-20203 🗹 | Apart from the general notes and annotation subobjects permitted on all SBML objects, a | 23 |
| | ListOfFluxBounds container object may only contain FluxBound objects. (References: SBML | 24 |
| | Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.3 on page 7.) | 25 |
| fbc-20204 | Apart from the general notes and annotation subobjects permitted on all SBML objects, a | 26 |
| | ListOfObjectives container object may only contain Objective objects. (References: SBML | 27 |
| | Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.3 on page 7.) | 28 |
| fbc-20205 ✓ | A ListOfFluxBounds object may have the optional metaid and sboTerm defined by SBML | 29 |
| | Level 3 Core. No other attributes from the SBML Level 3 Core namespace or the Flux Balance | 30 |
| | Constraints namespace are permitted on a ListOfFluxBounds object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.3 on page 7.) | 31 |
| | | |
| fbc-20206 | A ListOfObjectives object may have the optional attributes metaid and sboTerm defined by SBML Level 3 Core. Additionally the ListOfObjectives must contain the attribute activeObject | 33 |
| | No other attributes from the SBML Level 3 Core namespace or the Flux Balance Constraints | . 1 v e : |
| | namespace are permitted on a ListOfObjectives object. (References: SBML Level 3 Package | 36 |
| | Specification for Flux Balance Constraints, Version 1, Section 3.3 on page 7.) | 37 |
| fbc-20207 ✓ | The value of attribute fbc:activeObjective on the ListOfObjectives object must be of the | 38 |
| _ | data type FbcSIdRef. (References: SBML Level 3 Package Specification for Flux Balance Con- | 39 |
| | straints, Version 1, Section 3.2.2 on page 6). | 40 |
| fbc-20208 | The value of attribute fbc:activeObjective on the ListOfObjectives object must be set to | 41 |
| | the FbcSId of an existing Objective . (References: SBML Level 3 Package Specification for Flux | 42 |
| | Balance Constraints, Version 1, Section 3.2.2 on page 6.) | 43 |

the <code>FluxBound</code> , <code>Objective</code> and <code>FluxObjective</code> objects defined by the Flux Balance Constraints package. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Ver-

sion 1, Section 3.2 on page 6.)

Rules for extended Species object

- A SBML Species object may have the optional attributes fbc: charge and fbc: chemicalFormula.
 No other attributes from the Flux Balance Constraints namespaces are permitted on a Species.

 (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.4 on page 8)

 5
- The value of attribute fbc:charge on the SBML Species object must be of the data type integer. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.4 on page 8).
- The value of attribute fbc:chemicalFormula on the SBML Species object must be set to the string. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.4 on page 8.)

Rules for FluxBound object

- fbc-20401 ✓ A FluxBound object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespaces are permitted on a FluxBound. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- fbc-20402 ✓ A FluxBound object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespaces are permitted on a FluxBound . (References: SBML Level 3 Version 1 Core, Section 3.2.)
- fbc-20403 ✓ A FluxBound object must have the required attributes fbc:reaction, fbc:operation and fbc:value, and may have the optional attributes fbc:id and fbc:name. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a FluxBound object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- The attribute fbc:reaction in FluxBound must be of the data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- **fbc-20405** ✓ The attribute **fbc:name** in **FluxBound** must be of the data type **string**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- fbc-20406

 The attribute fbc:operation in FluxBound must be of the data type enum. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- **fbc-20407** ✓ The attribute **fbc:value** in **FluxBound** must be of the data type **double**. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- The value of the attribute fbc:reaction in a FluxBound object must be the identifier of an existing Reaction object defined in the enclosing Model object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- The value of the attribute fbc: operation in a FluxBound object must be one of "lessEqual", "greaterEqual", "less", "greater" or "equal". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)
- The combined set of all **FluxBound** 's with identical value for **fbc:reaction** must be consistent. That is while it is possible to define a lower and an upper bound for a reaction, it is not possible to define multiple lower or upper bounds. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.5 on page 8.)

14

24

31

33

35

38

39

41

14

16

23

26

27

29

34

44

Rules for Objective object

- fbc-20501 ✓ A Objective object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespaces are permitted on a Objective. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- **fbc-20502** ✓ A **Objective** object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespaces are permitted on a **Objective**. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- A Objective object may have the required attribute fbc:id and fbc:type and the optional attribute fbc:name. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a Objective object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- The attribute fbc:name in Objective must be of the data type string. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- fbc-20505

 ✓ The attribute fbc:type in Objective must be of the data type FbcType. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- fbc-20506

 ✓ The value of the attribute fbc:type in a Objective object must be one of "minimize" or "maximize". (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- **fbc-20507** ✓ A **Objective** must have one and only one instance of the **ListOfFluxObjectives** object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- The ListOfFluxObjectives subobject with a Objective object must not be empty. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- Apart from the general notes and annotation subobjects permitted on all SBML objects, a ListOfFluxObjectives container object may only contain Objective objects. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)
- fbc-20510
 ✓ A ListOfFluxObjectives object may have the optional metaid and sboTerm defined by SBML Level 3 Core. No other attributes from the SBML Level 3 Core namespace or the Flux Balance Constraints namespace are permitted on a ListOfFluxObjectives object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.6 on page 9.)

Rules for FluxObjective object

- fbc-20601
 ✓ A FluxObjective object may have the optional SBML Level 3 Core attributes metaid and sboTerm. No other attributes from the SBML Level 3 Core namespaces are permitted on a FluxObjective. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- **fbc-20602** ✓ A **FluxObjective** object may have the optional SBML Level 3 Core subobjects for notes and annotations. No other elements from the SBML Level 3 Core namespaces are permitted on a **FluxObjective**. (References: SBML Level 3 Version 1 Core, Section 3.2.)
- A FluxObjective object must have the required attributes fbc:reaction and fbc:coefficient, and may have the optional attributes fbc:id and fbc:name. No other attributes from the SBML Level 3 Flux Balance Constraints namespace are permitted on a FluxObjective object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 11.)

| fbc-20604 ✓ | The attribute fbc:name in FluxObjective must be of the data type string . (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 11.) | |
|----------------|--|---|
| fbc-20605 | The value of the attribute fbc:reaction of a FluxObjective object must conform to the syntax of the SBML data type SIdRef. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 11.) | 4 |
| fbc-20606 | The value of the attribute fbc:reaction of a FluxObjective object must be the identifier of an existing Reaction object defined in the enclosing Model object. (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 11.) | : |
| fbc-20607 ☑ | The value of the attribute fbc:coefficient of a FluxObjective object must conform to the syntax of the SBML data type double . (References: SBML Level 3 Package Specification for Flux Balance Constraints, Version 1, Section 3.7 on page 11.) | |

Acknowledgments

We would like to thank the following people who contributed in various ways to the development of both the original proposal and this document.

For financial/travel/technical/moral and general support we thank especially Herbert Sauro (University of Washington, USA), Ursula Kummer (Heidelberg University, Germany), Bas Teusink (VU University Amsterdam) and Michael Hucka (CalTech, USA).

A special work of thanks goes to Sarah Keating for her invaluable work with the libSBML and SBML Toolbox implementations and critical reading of this document.

We also would like to thank Neil Swainston, Keiran Smallbone, Daniel Hyduke, Nicolas Le Novère and all those who contributed ideas and held discussions with us on various occasions.

Section Acknowledgments Page 27 of 29

References

Becker, S. A., Feist, A. M., Mo, M. L., Hannum, G., Palsson, B. O., and Herrgard, M. J. (2007). Quantitative prediction of cellular metabolism with constraint-based models: the COBRA Toolbox. *Nat. Protocols*, 2(3):727–738. 1750-2799 10.1038/nprot.2007.99 10.1038/nprot.2007.99.

Bergmann, F. T. (2012). Sbw flux balance. Available via the World Wide Web at https://github.com/fbergmann/FluxBalance.

Bergmann, F. T. and Sauro, H. M. (2006). SBW - a modular framework for systems biology. In *Proceedings of the 38th conference on Winter simulation*, WSC '06, pages 1637–1645. Winter Simulation Conference.

Biron, P. V. and Malhotra, A. (2000). XML Schema part 2: Datatypes (W3C candidate recommendation 24 October 2000). Available via the World Wide Web at http://www.w3.org/TR/xmlschema-2/.

Bornstein, B. J., Keating, S. M., Jouraku, A., and Hucka, M. (2008). LibSBML: an API Library for SBML. *Bioinformatics*, 24(6):880–881.

Eriksson, H.-E. and Penker, M. (1998). UML Toolkit. John Wiley & Sons, New York.

Fallside, D. C. (2000). XML Schema part 0: Primer (W3C candidate recommendation 24 October 2000). Available via the World Wide Web at http://www.w3.org/TR/xmlschema-0/.

Hucka, M., Bergmann, F. T., Hoops, S., Keating, S. M., Sahle, S., and Wilkinson, D. J. (2011). Available via the World Wide Web at http://sbml.org/Documents/Specifications.

Hucka, M., Finney, A., Sauro, H., Bolouri, H., Doyle, J., Kitano, H., Arkin, A., Bornstein, B., Bray, D., Cornish-Bowden, A., Cuellar, A., Dronov, S., Gilles, E., Ginkel, M., Gor, V., Goryanin, I., Hedley, W., Hodgman, T., Hofmeyr, J., Hunter, P., Juty, N., Kasberger, J., Kremling, A., Kummer, U., Novère, N. L., Loew, L., Lucio, D., Mendes, P., Minch, E., Mjolsness, E., Nakayama, Y., Nelson, M., Nielsen, P., Sakurada, T., Schaff, J., Shapiro, B., shimizu, T., Spence, H., Stelling, J., Takahashi, K., Tomita, M., Wagner, J., and Wang, J. (2003). The Systems Biology Markup Language (SBML): a medium for representation and exchange of biochemical network models. *Bioinformatics*, 19(4):524–31.

19

23

Oberhardt, M. A., Palsson, B. Ø., and Papin, J. A. (2009). Applications of genome-scale metabolic reconstructions. *Molecular Systems Biology*, 5:320.

Oestereich, B. (1999). Developing Software with UML: Object-Oriented Analysis and Design in Practice. Addison-Wesley.

Olivier, B. G. (2012). CBMPy: Constraint Based Modelling in Python. Available via the World Wide Web at http://pysces.sf.net/cbm.

Olivier, B. G., Rohwer, J. M., and Hofmeyr, J.-H. S. (2005). Modelling cellular systems with PySCeS. *Bioinformatics*, 21(4):560–561.

Orth, J. D., Thiele, I., and Palsson, B. Ø. (2010). What is flux balance analysis? *Nature Biotechnology*, 28(3):245–248.

Reed, J. L., Vo, T. D., Schilling, C. H., and Palsson, B. O. (2003). An expanded genome-scale model of Escherichia coli K-12 (iJR904 GSM/GPR). *Genome Biol*, 4(9):R54.

SBML Team (2010). The SBML Issue Tracker. Available via the World Wide Web at http://sbml.org/issue-tracker.

Schellenberger, J., Park, J., Conrad, T., and Palsson, B. (2010). BiGG: a Biochemical Genetic and Genomic knowledgebase of large scale metabolic reconstructions. *BMC Bioinformatics*, 11(1):213.

Section Acknowledgments Page 28 of 29

Thompson, H. S., Beech, D., Maloney, M., and Mendelsohn, N. (2000). XML Schema part 1: Structures (W3C candidate recommendation 24 October 2000). Available online via the World Wide Web at the address http://www.w3.org/TR/xmlschema-1/.

Section Acknowledgments Page 29 of 29