Spatial Processes

James C. Schaff
schaff@neuron.uchc.edu
Center for Cell Analysis and Modeling
University of Connecticut
Farmington, Connecticut, US

Anu Lakshminarayana
anu@uchc.edu)
Center for Cell Analysis and Modeling
University of Connecticut
Farmington, Connecticut, US

Lucian P. Smith

lpsmith@u.washington.edu

Computing and Mathematical Sciences

California Institute of Technology

Seattle, Washington, US

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This is a draft specification for the SBML Level 3 package called "spatial". It is not a normative document. Please send feedback to the Package Working Group mailing list at sbml-spatial@lists.sourceforge.net.

The latest release, past releases, and other materials related to this specification are available at http://sbml.org/Documents/Specifications/SBML_Level_3/Packages/spatial

This release of the specification is available at



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1 Introduction

A set of biochemical process in cellular physiology may be modeled using different choices of spatial and temporal scales depending on the questions to be addressed. SBML Level 3 Core has explicit support for multi-compartmental modeling where cellular organization is approximated by a set of compartments (e.g. membrane-bound organelles) containing well-stirred populations of molecules. However, the coupling between localized biochemical reactions and diffusive molecular transport within the constraints of cellular geometry often results in important nonuniform molecular distributions. While it is often possible to approximate the influence of spatial organization and localization within a compartmental model using altered parameters and additional species, it is sometimes simpler and always more mechanistic to directly model these spatial processes.

An increasing number of modeling and simulation tools include direct support for modeling with explicitly defined cellular geometry. These models generally include heterogeneous molecular distributions, diffusive transport, and spatially localized reactions. These spatial models generally belong to two different mathematical frameworks, stochastic (where each molecule is tracked in space and time) and deterministic (where time varying species concentration fields are described by partial differential equations).

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There are a sufficient number of spatial modeling tools and spatial models to justify the effort of creating a spatial modeling extension of SBML. All such models must describe the cellular geometry, map molecular species to spatial locations, map reactions to spatial locations, and specify molecular transport within geometric compartments and at boundaries of these compartments.

It is the purpose of this SBML Level 3 extension to define a common representation for cellular geometry, spatial mappings of species and reactions, and explicit species transport.

1.1 Proposal corresponding to this package specification

This specification for Spatial in SBML Level 3 Version 1 is based on the proposal located at the following URL:

https://sbml.svn.sf.net/svnroot/sbml/trunk/specifications/sbml-level-3/version-1/spatial/proposal

The tracking number in the SBML issue tracking system (SBML Team, 2010) for Spatial package activities is 188 (http://sourceforge.net/p/sbml/sbml-specifications/188/).

1.2 Package dependencies

The Spatial package has no dependencies on other SBML Level 3 packages.

1.3 Document conventions

UML 1.0 (Unified Modeling Language; Eriksson and Penker 1998; Oestereich 1999) notation is used in this document to define the constructs provided by this package. Colors in the diagrams carry the following additional information for the benefit of those viewing the document on media that can display color:

- *Black*: Items colored black in the UML diagrams are components taken unchanged from their definition in the SBML Level 3 Core specification document.
- *Green*: Items colored green are components that exist in SBML Level 3 Core, but are extended by this package. Class boxes are also drawn with dashed lines to further distinguish them.
- *Blue*: Items colored blue are new components introduced in this package specification. They have no equivalent in the SBML Level 3 Core specification.

The following typographical conventions distinguish the names of objects and data types from other entities; these conventions are identical to the conventions used in the SBML Level 3 Core specification document:

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AbstractClass: Abstract classes are never instantiated directly, but rather serve as parents of other classes. Their names begin with a capital letter and they are printed in a slanted, bold, sans-serif typeface. In electronic document formats, the class names defined within this document are also hyperlinked to their definitions; clicking on these items will, given appropriate software, switch the view to the section in this document containing the definition of that class. (However, for classes that are unchanged from their definitions in SBML Level 3 Core, the class names are not hyperlinked because they are not defined within this document.)

Class: Names of ordinary (concrete) classes begin with a capital letter and are printed in an upright, bold, sans-serif typeface. In electronic document formats, the class names are also hyperlinked to their definitions in this specification document. (However, as in the previous case, class names are not hyperlinked if they are for classes that are unchanged from their definitions in the SBML Level 3 Core specification.)

- **SomeThing**. Attributes of classes, data type names, literal XML, and tokens *other* than SBML class names, are printed in an upright typewriter typeface.
- [elementName]: In some cases, an element may contain a child of any class inheriting from an abstract base class. In this case, the name of the element is indicated by giving the abstract base class name in brackets, meaning that the actual name of the element is the de-capitalized form of whichever subclass is used.

For other matters involving the use of UML and XML, this document follows the conventions used in the SBML Level 3 Core specification document.

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2 Background and context

2.1 Problems with current SBML approaches

There is no standard way of specifying spatial models in SBML short of introducing an explicit spatial discretization in the form of a large number of compartments with duplicate species and reactions and additional reactions for coupling due to transport. This approach hard-codes the numerical methods which destroys portability and is not practical beyond a few compartments. Tools have been forced to resort to proprietary extensions (e.g. MesoRD custom annotations) to encode geometry.

2.2 Past work on this problem or similar topics

There are many standards for the exchange of geometric information of engineered parts in Computer Aided Design and Manufacturing. These formats are designed for geometric shapes which are directly specified by a designer rather than the data driven, freeform biological structures encountered in cell biology.

There also exist standards for the representation of unstructured computational meshes that can encode these freeform biological structures more readily. However, it is important to note that while a computational mesh necessarily encodes an approximation to the shapes of geometric objects, the particular form will be algorithm dependent.

To ensure model interoperability, we must encode the geometric shapes in a way that is independent of the numerical methods and even the mathematical framework. The representation of a spatial model within SBML should be largely invariant of the particular encoding of the geometry definition within that model. For example, a spatial model represented in SBML that encodes geometry as a set of geometric primitives (e.g. spheres, cylinders) should be easily portable to a tool that only supports polygonal surface tessellation. It is expected that a geometry translation library will be very useful for interoperability the same way that libSBML greatly improved model interchange by solving similar implementation problems in a standard way.

2.3 Prior work

The first version of the Spatial proposal was written [fill in history]

Lucian: We probably do need something here.

3 Package syntax and semantics

This section contains a definition of the syntax and semantics of the Spatial package for SBML Level 3 Version 1 Core. The Spatial package involves several new object classes, and extends the existing **Model**, **Compartment**, **Species**, **Reaction**, and **Parameter** object class. Section 4 on page 36 contains complete examples of using the constructs in SBML models.

Lucian: Periodically when I have comments, I'll put them in sections that look like this-in red, with the pointy-hand icon off to the side. They tend to be design questions I had when creating this document for parts I thought were not clear, or are suggestions for changes that could be made.

3.1 Overview of spatial extension

The SBML Compartment, Reaction and Species, and molecular transport mechanisms (DiffusionCoefficient, AdvectionCoefficient, BoundaryCondition) are mapped to geometric domains to describe spatial models within SBML. The primary mechanism to accomplish this mapping is to simply map Compartments to collections of geometric Domains called DomainTypes. Each Domain is a contiguous patch of volumetric space or a contiguous surface patch that is ultimately described by a single system of equations (whichever mathematical framework is used). In analogy with initial conditions, the mathematical system defined within a domain often needs a definition of what happens at the domain boundary (e.g. boundary conditions) to complete the specification. Because of this, the boundaries between adjacent domains need to be identified so that appropriate boundary conditions can be specified. For compactness of representation, rather than map to each individual Domain, Compartments are mapped to DomainTypes, along with the corresponding Species and Reactions (with the new compartment attribute).

3.1.1 Geometry

The **Geometry** object within a model is completely modular and does not reference the rest of the model, promoting reuse of the same geometry in different models. The geometry separately defines a coordinate system, a list of domain types, a list of domains and their adjacency relationships, and a list of alternate geometric representations.

3.1.2 Alternative Geometry Definitions

Modeling and simulation tools will each natively support some subset (often just one) of the possible *Geometry-Definitions* (analytic, sampled field, constructive solid geometry, and parametric shapes). Interoperability will be enhanced if tools write as many geometry definitions as they are able. Upon reading the model, a tool will typically choose the most convenient geometry definition, i.e. the one that it natively supports. If a tool does not edit the geometry, it has the ability to preserve the alternate representations during model editing (because the mapping of the model to the geometry is not stored in the geometry).

There are two general classes of geometric representation specification: those that explicitly specify surfaces and those that implicitly specify surfaces. For example, a level set is a field where a specific isosurface of the field specifies a geometric surface. A geometry described using constructive solid geometry of geometric primitives (e.g. spheres, cylinders) specifies directly which points are "inside" an object. Alternatively, explicit surface representations explicitly declare the set of points belonging to surfaces (e.g. polygonal tessellations).

3.2 Namespace URI and other declarations necessary for using this package

Every SBML Level 3 package is identified uniquely by an XML namespace URI. For an SBML document to be able to use a given Level 3 package, it must declare the use of that package by referencing its URI. The following is the namespace URI for this version of the Spatial package for SBML Level 3 Version 1 Core:

"http://www.sbml.org/sbml/level3/version1/spatial/version1"

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In addition, SBML documents using a given package must indicate whether the package can be used to change the mathematical interpretation of a model. This is done using the attribute **required** on the **sbml** element in the SBML document. For the Spatial package, the value of this attribute must be "true", because the use of the Spatial package can change the mathematical meaning of a model.

The following fragment illustrates the beginning of a typical SBML model using SBML Level 3 Version 1 Core and this version of the Spatial package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core" level="3" version="1"
    xmlns:spatial="http://www.sbml.org/sbml/level3/version1/spatial/version1"
    spatial:required="true">
```

3.3 Primitive data types

The Spatial package uses a number of the primitive data types described in Section 3.1 of the SBML Level 3 Version 1 Core specification, and adds several additional primitive types described below.

3.3.1 Type SpId

The type SpId is derived from SId (SBML Level 3 Version 1 Core specification Section 3.1.7) and has identical syntax. The SpId type is used as the data type for the identifiers of various objects in the Spatial Processes package. The purpose of having a separate type for such identifiers is to enable the space of possible spatial identifier values to be separated from the space of all other identifier values in SBML. The equality of SpId values is determined by an exact character sequence match; i.e., comparisons of these identifiers must be performed in a case-sensitive manner.

3.3.2 Type SpIdRef

Type SpIdRef is used for all attributes that refer to identifiers of type SpId. This type is derived from SpId, but with the restriction that the value of an attribute having type SpIdRef must match the value of a SpId attribute in the relevant model; in other words, the value of the attribute must be an existing spatial identifier in the referenced model. As with SpId, the equality of SpIdRef values is determined by exact character sequence match; i.e., comparisons of these identifiers must be performed in a case-sensitive manner.

3.3.3 Type BoundaryConditionKind

The BoundaryConditionKind primitive data type is used in the definition of the BoundaryCondition class. The type BoundaryConditionKind is derived from type string and its values are restricted to being one of the following possibilities: "Robin_valueCoefficient", "Robin_inwardNormalGradientCoefficient", "Robin_sum", "inwardNormalFlux", and "value". Attributes of type BoundaryConditionKind cannot take on any other values. The meaning of these values is discussed in the context of the BoundaryCondition class's definition in Section 3.12 on page 16.

3.3.4 Type ComponentKind

The ComponentKind primitive data type is used in the definition of the CoordinateComponent class. ComponentKind is derived from type string and its values are restricted to being one of the following possibilities: "cartesianX", "cartesianY", and "cartesianZ". Attributes of type ComponentKind cannot take on any other values. The meaning of these values is discussed in the context of the CoordinateComponent class's definition in Section 3.15 on page 18.

Other ComponentKind types are held in reserve for future versions of this specification, and may include "spherical-Radius", "sphericalAzimuth", "sphericalElevation", "cylindricalRadius", "cylindricalAzimuth", "cylindricalHeight", "polarRadius", and "polarAzimuth".

The CoordinateKind type has been removed.

3.3.5 Type DiffusionKind

The DiffusionKind primitive data type is used in the definition of the DiffusionCoefficient class. DiffusionKind is derived from type string and its values are restricted to being one of the following possibilities: "isotropic" and "tensor". Attributes of type DiffusionKind cannot take on any other values. The meaning of these two values is discussed in the context of the DiffusionCoefficient class's definition in Section 3.10 on page 14.

3.3.6 Type FunctionKind

The FunctionKind primitive data type is used in the definition of the AnalyticVolume class. The type FunctionKind is derived from type string and its values are restricted to being one of the following possibilities: "layered" and "R-function". Attributes of type FunctionKind cannot take on any other values. The meaning of these values is discussed in the context of the AnalyticVolume class's definition in Section 3.23 on page 24.

3.3.7 Type GeometryKind

The GeometryKind primitive data type is used in the definition of the Geometry class. GeometryKind is derived from type string and its values are restricted to being the single possibility "cartesian". Other GeometryKind types are held in reserve for future versions of this specification, and may include "cylindrical", "spherical", and "polar". Attributes of type GeometryKind cannot take on any other values. The meaning of these values is discussed in the context of the Geometry class's definition in Section 3.14 on page 17.

3.3.8 Type SetOperation

The SetOperation primitive data type is used in the definition of the CSGSetOperator class. The type SetOperation is derived from type string and its values are restricted to being one of the following possibilities: "union", "intersection", and "difference". Attributes of type SetOperation cannot take on any other values. The meaning of these values is discussed in the context of the CSGSetOperator class's definition in Section 3.34 on page 30.

3.3.9 Type doubleArray

The doubleArray primitive data type is a space-delimited list of double values in a single string.

3.3.10 Type integerArray

The integerArray primitive data type is a space-delimited list of integer values in a single string.

3.4 The extended Model object

The **Model** object is extended in the spatial package to contain a new **Geometry** child, as seen in Figure 1. The **Geometry** element is contained in the Model element in the 'spatial' namespace. In order to specify a spatial geometry, some of the existing SBML elements need to be extended (**Compartment**, **Species**, **Parameter**, and **Reaction**). These extensions to the SBML elements are discussed in the sections that follow.

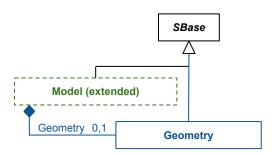


Figure 1: The definition of the extended Model object from the Spatial package. The Geometry object and its children are defined in their own sections.

3.5 The extended Compartment object

The **Compartment** in the SBML core is extended while defining a spatial model. An SBML model with spatial geometry defines domain types (classes of domains that are anatomically and physiologically similar). These domain types need to be mapped to a compartment in the SBML model. **Compartments** are extended to define **CompartmentMappings** that map compartments to **DomainTypes** such that each corresponding **DomainType** is assigned the same biological and mathematical function. Within SBML L3 Core, the compartment Sid refers to the size of that compartment and is specified by the size attribute or may be set by a rule. For spatial models, the compartment size is calculated as the product of the unit size specified in the compartment mapping and the size of the current domain. The definition for the extension of the Compartment element is shown in Figure 2.

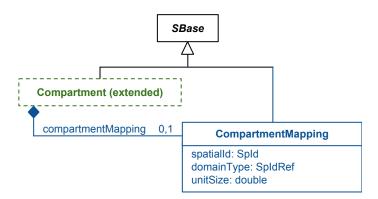


Figure 2: The definition of the extension to the Compartment element, and the definition of the CompartmentMapping class. The SBML core attributes of Compartment are not displayed.

The **Compartment** element has an optional **CompartmentMapping** child which indicates the **DomainType** to which the **Compartment** is mapped. If there is no **CompartmentMapping** for a **Compartment** in a spatial model, then that **Compartment** is excluded from the spatial version of the model. In the same way, if a **DomainType** is not mapped to one or more **Compartments**, then the corresponding **Domains** in the geometry have no assigned function.

3.6 The CompartmentMapping class

Each **Compartment** in a model that defines a spatial geometry may contain an optional **CompartmentMapping**. A **CompartmentMapping** is defined as part of the model rather than part of the geometry so that the geometry is modular and may be readily shared between models and reused. A **CompartmentMapping** maps a **Compartment** defined in the model to a **DomainType** defined in the geometry such that each corresponding **DomainType** is assigned the same biological and mathematical function described by the set of **Compartments** that are mapped to that **DomainType**.

This mapping need not be one-to-one. In fact, it is common to map er-lumen, er-membrane, and cytosol to the same cell interior volume or 3D **DomainType**. The **unitSize** attribute specifies the relative quantity of each **Compartment** that is mapped to the **DomainType**.

3.6.1 The spatialId attribute

The spatialId attribute is a mandatory attribute of type SpId that is used to uniquely identify a CompartmentMapping in the model. All identifiers of type SpId must be unique within the Geometry. The mathematical value of a CompartmentMapping is its unitSize attribute, and can be bound to a Parameter by using a SpatialSymbolReference.

3.6.2 The domainType attribute

The mandatory domainType attribute is of type SpIdRef that indicates a DomainType defined in the Geometry element.

3.6.3 The unitSize attribute

The unitSize attribute is of type double and represents the relative size of the Compartment with respect to the size of the Domains to which they are mapped. Thus for any infinitesimal subset of the Domain with size S, there exists an amount of Compartment; of size (S*unitSize;) for i=1..N compartments mapped to that DomainType. For example, a 3D Compartment (and DomainType) which is mapped to a 3D DomainType has a unitSize which is a volume fraction of dimensionless unit. The total set of all such volume fractions mapped to a particular DomainType will typically sum to one.

If the spatialDimensions attribute of the parent **Compartment** is different than the spatialDimension attribute of referenced **DomainType**, the unitSize attribute is a conversion factor between the two. The most common example of this would be a 2D **Compartment** being mapped to a 3D **DomainType**, such as an ER-membrane being mapped to a volumetric cell interior. In this case, the unitSize is a surface-to-volume ratio.

If connected to a **Parameter** via a **SpatialSymbolReference**, an **InitialAssignment** may override the value of the **unitSize** attribute. It is theoretically possible to have this value change in time through the use of a **Rule** or **Event**, but some (if not all) software tools may not support this setup. If the value is set to change, and the dimensionality of the parent **Compartment** and referenced **DomainType** is the same, the other **CompartmentMapping** elements for the same **DomainType** will typically change in concert, so that they continue to sum to one.

Any bound **Parameter**'s units should be equivalent to the units of the parent **Compartment** divided by the units of the referenced **DomainType**.

3.7 The extended Species object

The SBML core **Species** is extended when a spatial geometry is defined in the model with the addition of a single new required boolean "isSpatial" attribute. The extension to the **Species** element is shown in Figure 3 on the next page.

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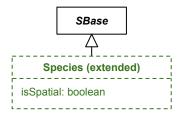


Figure 3: The extension to the Species element. The attributes of Species from SBML Level 3 Version 1 Core are not displayed.

3.7.1 The isSpatial attribute

The **isSpatial** attribute is of data type boolean. If it is set to true, the **Species** is spatially distributed in a possibly nonhomogeneous manner within the **Domains** of the same type as the mapped **DomainType**.

For continuous deterministic models (described by partial differential equations), a spatial **Species** will result in a concentration field described by a partial differential equation which incorporates contributions from **Reactions**, diffusion (**DiffusionCoefficient**) and advection (**AdvectionCoefficient**) and are subject to boundary conditions (**BoundaryCondition**) and initial conditions (**InitialAssignment** and **Rule**). All of these quantities can be explicit functions of the spatial coordinates as well as spatial and nonspatial **Parameters** and **Species**.

For stochastic models, the **Species** is represented as a collection of particles that are distributed throughout the **Domains** and are subject to reactions, diffusion and advection. Simulation algorithms either track individual particles (e.g. Particle-based methods) or use spatial discretization to track a large number of well stirred pools (e.g. Next-Subvolume Method).

The **compartment** of any **Species** set **isSpatial** = "true" must have a child **CompartmentMapping**: if it did not, its compartment would not actually be a part of the spatial model.

3.8 The extended Parameter object

When an SBML model defines a spatial geometry, the SBML core **Parameter** is used to define the diffusion coefficient, transport velocity (advection) and boundary conditions for species and the coordinate components defined in the **Geometry**. One **Parameter** is created for each quantity, by adding a child **DiffusionCoefficient**, **AdvectionCoefficient**, or **BoundaryCondition**. Conversely, some elements defined in the spatial package may need to be referenced by mathematics in core constructs, or even have their value set by core constructs such as **InitialAssignment** or **Rule**. These spatial elements can be semantically linked to a **Parameter** by giving it a child **SpatialSymbolReference** pointing to that element.

A **Parameter** that has been extended for the Spatial package can have only one of the above listed objects. For example, if a **Parameter** is extended to represent the diffusion coefficient of a species, the existing attributes of the **Parameter** (id, name, value, units, constant) are defined according to SBML core specifications, along with a **DiffusionCoefficient** child that contains the information about the species it represents. Figure 4 on the following page represents the extension to the **Parameter** element.

3.9 The SpatialSymbolReference class

A **Parameter** is extended with a **SpatialSymbolReference** element, when a symbol from the defined spatial geometry (**spatialId** of any element contained in **Geometry**) is required to be used in the SBML core model. Typically, the **SpatialSymbolReference** is used to represent the coordinate components defined in the **Geometry**'s listOfCoordinateComponents. For example, if the **Geometry** is defined in a 2-dimensional Cartesian coordinate system with X and Y defined as coordinate components, two **Parameters** (one each for **CoordinateComponents** X and Y) are created in the model. The value of the parameter is not required to be set. For each of these parameters, a **SpatialSymbolReference** object is created.

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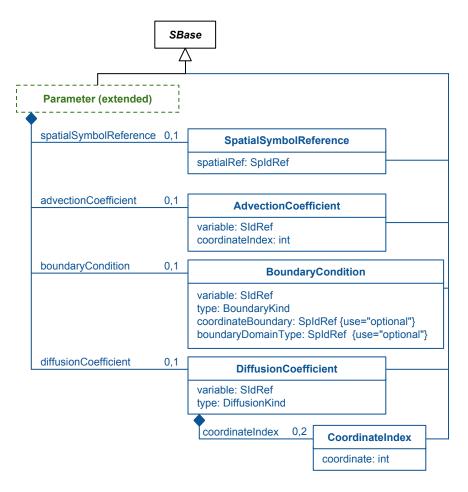


Figure 4: The Parameter element extension for spatial package. The SBML Level 3 Version 1 Core attributes for Parameter are not displayed in this figure.

3.9.1 The spatialRef attribute

The **spatialId** attribute of **SpatialSymbolReference**, is of type **SpIdRef** and refers to the **spatialId** of any element defined in the **Geometry** of the model.

3.10 The DiffusionCoefficient class

When a species in a spatial model has a diffusion rate constant, a **Parameter** for this diffusion constant is created in the SBML model with a **DiffusionCoefficient** child, which is used to identify the **Species** whose diffusion rate the **Parameter** represents. The diffusion coefficient can then be set like any other variable: its initial value can be set using the **Parameter**'s **value** attribute or through an **InitialAssignment**, and if the diffusion coefficient changes in time, this can be defined with a **Rule** or **Event**. If set, the units of this **Parameter** should be length²/time. If left unset, the **DiffusionCoefficient** will inherit the model units of length²/time (typically cm²s⁻¹ or um²s⁻¹).

It is possible to define both diffusion and advection for the same **Species**.

3.10.1 The variable attribute

The required variable attribute of **DiffusionCoefficient** is of type **SIdRef** and is the SId of the **Species** or **Parameter** in the model whose diffusion coefficient is being set.

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3.10.2 The type attribute

The required type attribute of DiffusionCoefficient is of type DiffusionKind and indicates whether the diffusion coefficient is "isotropic" (i.e. applies equally in all dimensions/directions) or "tensor" (i.e. applies only for a particular pair of coordinate indices). Coefficients of type "isotropic" may not have any child CoordinateIndex children, while coefficients of type "tensor" must have exactly two.

3.10.3 The CoordinateIndex class

The optional CoordinateIndex children of the DiffusionCoefficient object represent the index attributes of the CoordinateComponent (e.g. 0 for x, 1 for y, 2 for z), for specifying the diffusion coefficient for flux in the plane defined by the two CoordinateIndex axes. coordinateIndex direction due to a gradient in the coordinateIndex direction (diagonal term of the diffusion tensor). If the coordinateIndex is missing, the diffusion is considered to be Isotropic.

Lucian: I updated this some, but was also thinking: if we remove the 'index' value from the **CoordinateComponent**, it might make sense for the **coordinateIndex** attribute to be of type **SpIdRef** instead, and have it reference the actual coordinate component from the model. In other words, instead of 'coordinateIndex=0', you'd have 'coordinate="x"'. Does this seem reasonable? Also, we'll have to think about what to do with this if we ever add back in other coordinate systems.

3.10.4 DiffusionCoefficient uniqueness

Only one **DiffusionCoefficient** may be defined per **Species** per pair of valid axes in the **Compartment** in which it resides. Since isotropic diffusion is defined for all axes at once, this means that if an isotropic **DiffusionCoefficient** is defined for a **Species**, it may have no other diffusuion coefficients.

3.11 The AdvectionCoefficient class

The AdvectionCoefficient is the extension to Parameter in SBML core that is used to represent transport velocity of a species, if it exists. The transport velocity for the species is defined in a manner similar to the diffusion constant with a unit of length/time (regardless of the units of the corresponding Species' "compartment" attribute). A Parameter is created in SBML code for the velocity with an AdvectionCoefficient child to identify the Species whose velocity is represented by the Parameter; its initial value is set either through the value attribute or an InitialAssignment. If the advection coefficient changes in time or space, this can be modeled with a Rule or Event.

If defined, the units of the parent **Parameter** should be in length/time; if not defined, it inherits from the model-wide units of length divided by the model-wide units of time.

It is possible to define both diffusion and advection for the same **Species**.

3.11.1 The variable attribute

The variable attribute of **AdvectionCoefficient** is of type **SIdRef** and is the SId of the **Species** or **Parameter** in the model whose advection coefficient (transport velocity) is being set.

3.11.2 The coordinateIndex attribute

The **coordinateIndex** is of type **int** and represents the coordinate component of the velocity. For example, if the **Geometry** is defined in the Cartesian coordinate system and is 2-dimensional, the species can have velocity terms for both X and Y. If the **Parameter** represents the transport velocity of the species in the X-coordinate, the **coordinateIndex** attribute will take a value of 0, and if it represents the velocity in the Y-coordinate, the attribute will take a value of 1. Only one **AdvectionCoefficient** may be defined per **Species** per valid **coordinateIndex**.

Lucian: Again, this might be clearer as a 'coordinate' attribute of type 'SpIdRef' instead of linking things to indices.

Section 3 Package syntax and semantics

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3.12 The Boundary Condition class

A **Species** in a spatial model that has a diffusion rate or an advection velocity needs to have specified boundary conditions. A boundary condition is either the concentration of the species or the flux density of the species at a boundary. The boundary refers to either an internal membrane boundary or a face of the box defined by the minimum and maximum coordinates of the geometry (the geometries bounding box).

When creating a spatial SBML model, species boundary conditions are created as parameters, one for each boundary condition, by adding a child **BoundaryCondition** that points to the corresponding **Species** and boundary, depending on the coordinate system.

For Cartesian Geometries, there are two boundaries for every axis being modeled. For example, in a 2D cartesian geometry for the external boundaries, there could be up to four parameters or parameter sets created for each spatial **Species** whose **Compartments** abut the minimum and maximums of the X and Y axes).

The **Parameter**'s value is set either through the **value** attribute or an **InitialAssignment**. If the boundary condition changes in time, it can be set with a **Rule** or **Event**. If set, the **Parameter** unit must be equal to the appropriate unit for its type (see below). Only one **BoundaryCondition** may be defined per **Species** per boundary (regardless of type).

3.12.1 The variable attribute

The **variable** attribute of **BoundaryCondition** is of type **SIdRef** and is the SId of the **Species** or **Parameter** in the model whose boundary condition is being set.

3.12.2 The type attribute

The type attribute is of type BoundayConditionKind and indicates the type of boundary condition. The boundary condition types come in three groups: for Neumann boundaries, "inwardNormalFlux" is used. For Dirichlet boundaries, "value" is used. For Robin boundaries, three different Parameters must be defined, with BoundaryCondition elements of type "Robin_valueCoefficient", "Robin_inwardNormalGradientCoefficient", and "Robin_sum".

The unit of the boundary condition is determined by the type, and the unit for density and velocity. For "value", the unit would be the unit of concentration. For "inwardNormalFlux", the unit would be concentration*length/time. For Robin boundaries, for a variable "u" with an inward pointing normal vector "n", Robin value coefficient "a", Robin inward normal gradient coefficient "b", and Robin sum "g", the condition is defined by the equation "a*u + b*inner_product(grad(u),n) = g", with appropriate units.

Lucian: Does this explanation work?

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3.12.3 The coordinateBoundary attribute

The coordinateBoundary attribute is of type SpIdRef and refers to the spatialId of either the boundaryMin or boundaryMax object of the CoordinateComponent defined in Geometry. This spatialId indicates the boundary condition (minimum or maximum) in the CoordinateComponent. A Parameter that is extended with a BoundaryCondition object can only define the coordinateBoundary attribute or the boundaryDomainType attribute, but not both.

3.12.4 The boundaryDomainType attribute

The boundaryDomainType attribute is of type SpIdRef and refers to the spatialId of the DomainType of the location of the species whose boundary condition is being defined. A Parameter that is extended with a BoundaryCondition object can only define the coordinateBoundary attribute or the boundaryDomainType attribute, but not both.

3.13 The extended Reaction object

The SBML core **Reaction** is extended when a spatial geometry is defined in the model with the addition of a single new required boolean **isLocal** attribute. Figure 5 displays the definition of the extension of the **Reaction** element.

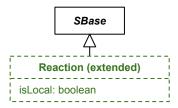


Figure 5: The extension to the **Reaction** element. The SBML Level 3 Version 1 Core attributes and children for **Reaction** are not displayed in the figure.

3.13.1 The isLocal attribute

The **isLocal** attribute for a **Reaction** is of type **Boolean**. The attribute is set to true if the reaction is to be considered a local description of the reaction in terms of concentration/time defined at each point in space rather than substance/time over an entire **Compartment** or "pool". Note that this means that the units of the **KineticLaw** are different depending on whether the **Reaction** is local or not.

3.14 The Geometry class

A single geometry must be defined within the model if the spatial extension is to be used. Figure 6 on the following page shows the definition of the **Geometry** element.

3.14.1 The spatialId attribute

The **spatialId** attribute is of type **SpId**, uniquely identifies the **Geometry** element, and is optional. It has no mathematical meaning.

3.14.2 The coordinateSystem attribute

The coordinateSystem attribute is a required attribute and is of type GeometryKind. It represents the coordinate system used by the Geometry. A value of "cartesian" indicates that the geometry is a cartesian coordinate system, with the coordinate components corresponding to the x, y, and z components of that system (which could be 1-, 2-, or 3-dimensional). This is the only coordinate system defined in this version of the specification—in the future, if necessary, "cylendrical", "spherical", and "polar" may be added as possibilities, along with n-dimensional cartesian modeling, should there be interest in the modeling community to exchange these types of models.

3.14.3 The listOf container classes

The Geometry has listOfCoordinateComponents, listOfDomainTypes, listOfDomains, and listOfAdjacentDomains, and listOfGeometryDefinitions that help define the geometry. The ListOfCoordinateComponents is a list of CoordinateComponent objects, the ListOfDomainTypes is a list of DomainType objects, the ListOfDomains is a list of Domain objects, ListOfAdjacentDomains is a list of AdjacentDomains objects, and the ListOfGeometryDefinitions is a list of alternative GeometryDefinitions (ParametricGeometry, CSGeometry, SampledFieldGeometry, AnalyticGeometry). None of these lists are technically required, but, if present, none of them may be empty.

Note that the children of the **ListOfGeometryDefinitions** object are not called **geometryDefinition** but rather take the name of the derived class, decapitalized. Thus, they may be called **parametricGeometry**, **sampledFieldGeometry**, **csGeometry**, or **analyticGeometry**.

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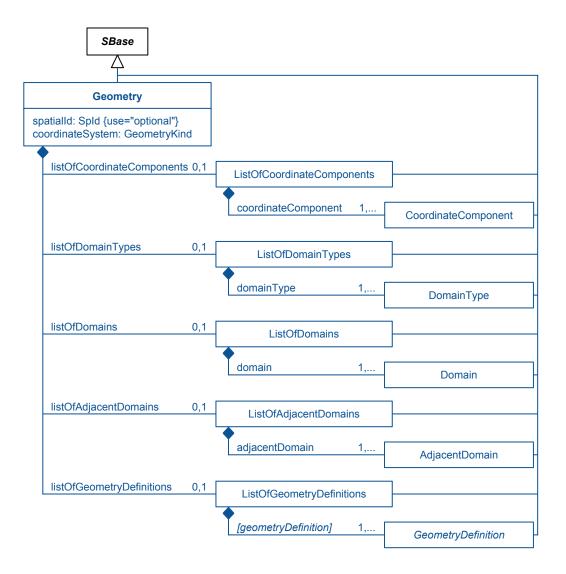


Figure 6: The definition of the Geometry, ListOfCoordinateComponents, ListOfDomainTypes, ListOfDomains, ListOfAdjacentDomains, and ListOfGeometryDefinitions classes from the Spatial package. The various children of the ListOfclasses are defined in their own sections.

3.15 The CoordinateComponent class

A **CoordinateComponent** object explicitly defines a coordinate component of the coordinate axes and gives them names, units, and formally associates them with a coordinate system. The **CoordinateComponent** also defines the minimum and maximum values of the coordinate axis it represents. The definition of **CoordinateComponent** is shown in Figure 7 on the next page.

3.15.1 The spatialId attribute

A **CoordinateComponent** is identified with the **spatialId** attribute which is of type **SpId**. When referenced (for example, via a **SpatialSymbolReference** extension of the SBML core **Parameter** object) and used within a mathematical expression, it represents the coordinate value for this **CoordinateComponent**.

Because a **CoordinateComponent** represents an entire axis, it is not appropriate, should it be connected to a **Parameter** via a **SpatialSymbolReference**, for that **Parameter** to be set via an **InitialAssignment** or **Rule**. Rather, it is treated like the SBML core **csymbol** "time", and can be used as an independent variable in other calculations.

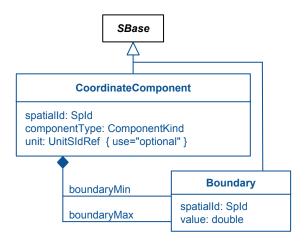


Figure 7: The CoordinateComponent object definition. One or more instances of CoordinateComponent objects in a ListOfCoordinateComponents can be present in Geometry.

3.15.2 The componentType attribute

The componentType attibute of type ComponentKind represents the type of the coordinate component, and may take one of a subset of all possible ComponentKind values depending on its parent Geometry, as defined in Table 1. For Cartesian geometries, one-dimensional geometries may be defined by having a single "cartesianX" CoordinateComponent; two-dimensional geometries may be defined by having two CoordinateComponent children with componentType values of "cartesianX" and "cartesianY", and three-dimensional geometries may be defined by having three CoordinateComponent children with componentType values of "cartesianX", "cartesianY", and "cartesianZ".

GeometryKind	Dimensions	ComponentKinds
cartesian	1	"cartesianX" (coord1)
cartesian	2	"cartesianX" (coord1) and "cartesianY" (coord2)
cartesian	3	"cartesianX" (coord1), "cartesianY" (coord2), and "cartesianZ" (coord3)

Table 1: Correspondance between the type of a Geometry and the possible component Types of it child Coordinate-Component elements. Also noted is the corresponding attribute (coord1, coord2, or coord3) corresponding to each axis when defining InteriorPoint elements (see Section 3.19 on page 22).

Lucian: coordinateType attribute removed.

3.15.3 The unit attribute

The unit of a **CoordinateComponent** is represented by the **unit** attribute, of type **UnitSIdRef**. If not specified, the unit of a **CoordinateComponent** inherits from the **lengthUnits** attribute of the **Model** object, and if that in turn is not specified, the **CoordinateComponent** units cannot be determined.

3.16 The Boundary class

The minimum and the maximum for a **CoordinateComponent** represent the bounds in each coordinate. For example, for three dimensional Cartesian coordinate system with x, y, and z coordinates, the minimum and maximum limits for each coordinates define planes orthogonal to each coordinate axis and passing through the minimum or maximum. If max-min is the same for each x,y,z then the bounds on the geometry is a cube. The **Boundary** class interacts with the **BoundaryCondition** class, allowing modelers to define how model elements behave at the

boundary of the model. For species defined within volumes adjacent to these surfaces, **BoundaryCondition** elements must be introduced.

Lucian: Just a note to coordinate the text here to sync with the text in the **BoundaryCondition** class, if that changes.

The minimum limit of a **CoordinateComponent** is represented by the **boundaryMin** object and the maximum limit is represented by the **boundaryMax** object, and apply to **CoordinateComponent** elements. Both are **Boundary** objects, and have the following attributes:

3.16.1 The spatialId attribute

The **spatialId** attribute of the **Boundary** object identifies the object. The attribute is required and is of type **SpId**. This attribute is used when specifying the **BoundaryCondition** for a species as an extension of an SBML core **Parameter**. When referenced (for example, via a **SpatialSymbolReference** extension of the SBML core **Parameter** object) and used within a mathematical expression, it represents the value of the **Boundary**. The units are the same as its parent **CoordinateComponent**, and are not set separately.

3.16.2 The value attribute

The value attribute is of type double. In a boundaryMin object, it represents the minimum limit of the Coordinate-Component. In a boundaryMax object, it represents the maximum limit of the CoordinateComponent.

If connected to a **Parameter** via a **SpatialSymbolReference**, this **value** may be overridden by an **InitialAssignment**. It is theoretically possible to have this value change in time through the use of a **Rule** or **Event**, but some (if not all) software tools may not support this setup.

3.17 The DomainType class

A **DomainType** is a class of domains that are identified as being anatomically and physiologically similar. For example, a **DomainType** "cytosol" may be defined in a **Geometry** as identifying the structure and function of the cell interior. If there is one cell, then there is one domain, if there are multiple cells, then there are multiple disjoint domains ("cytosol1", "cytosol2", etc.) identified with the **DomainType** "cytosol". **CompartmentMappings**, defined as an extension to an SBML core **Compartment**, map compartments to domain types such that each corresponding domain is assigned the same biological and mathematical function. Figure 8 shows the **DomainType** object.

Each SBML **Compartment** maps to a single **DomainType**, meaning that the initial condition of each **Species** in each **Compartment** will be the same across all **Domains** that map to a given **DomainType**. If those **Species** are spatially distributed, they will subsequently evolve independently from each other. However, if modeling two **Domains** that are similar but whose **Species** have different initial conditions, those **Domains** should be modeled as separate **DomainTypes**.

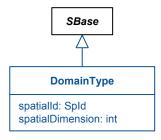


Figure 8: The DomainType object. One or more instances of DomainType in a ListOfDomainTypes instance can be present in a Geometry object.

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3.17.1 The spatialId attribute

Each **DomainType** is identified with a **spatialId** of type **SpId**. When referenced and used within a mathematical expression, it represents the sum of the sizes of all domains associated with this **DomainType**.

As a derived quantity, if connected to a **Parameter** via a **SpatialSymbolReference**, this value may *not* be overridden by an **InitialAssignment**, nor by the use of a **Rule** or **Event**. Its value is always connected to the size of its component **Domains** instead. The units of a **DomainType** are the units of the corresponding base units of the SBML **Model** for length (for one-dimensional domains), area (for two-dimensional domains), or volume (for three-dimensional domains). It is required to define the corresponding base units for every **DomainType** in the **Model**.

3.17.2 The spatialDimension attribute

The spatialDimension attribute of the **DomainType** is of type int and can take on a value of 0, 1, 2, or 3. The spatial dimension is specified for a **DomainType**, rather than being repeated for each **Domain** that is represented by the **DomainType**.

Lucian: The equivalent attribute of a **Compartment** is spatialDimensions, i.e. it has an 's' on the end. Can we change this to match?

3.18 The Domain class

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Domains represent contiguous regions identified by the same **DomainType**. One, two and three dimensional domains are contiguous linear regions, surface regions, and volume regions (respectively), bounded by the limits of the coordinate system (e.g. min/max of x,y,z) and adjacent domains corresponding to different domain types. **Domain** is shown in Figure 9.

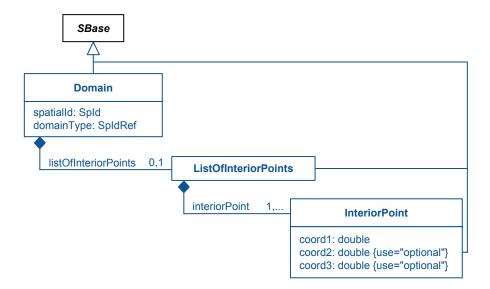


Figure 9: The definition of the **Domain**, **ListOfInteriorPoints**, and **InteriorPoint** classes. A **ListOfDomains** instance in **Geometry** can contain one or more **Domain** object instances.

3.18.1 The spatialId attribute

A **Domain** is identified with a spatialID attribute of type **SpId**. This **spatialId** may be used within a **SpatialSymbol-Reference** object that is extended from an SBML core **Parameter** and can be used in an expression. When referenced, the domain evaluates to the absolute size of that domain as used by the simulator (the meshed size).

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As a derived quantity, if connected to a **Parameter** via a **SpatialSymbolReference**, this value may *not* be overridden by an **InitialAssignment**, nor by the use of a **Rule** or **Event**. Its value is always connected to the size of the corresponding **Geometry** instead. The units of the **Domain** are the same as the units of the corresponding **DomainType**.

3.18.2 The domainType attribute

The domainTpe attribute refers to the spatialId of the DomainType that describes the anatomy and physiology of this domain. The attribute is of type SpIdRef. It is through this association that compartments, and hence the whole SBML model, gets mapped to the individual domains.

3.19 The InteriorPoint class

Each **Domain** can contain a **ListOfInteriorPoints**. The list of spatial points for a domain is interior to that domain. This list is optional for a **Domain** if it is the only **Domain** defined for its **DomainType**, but is required otherwise.

For those geometric descriptions that can describe multiple disjoint domains belonging to the same domainType, these interior points allow unambiguous identification of each domain. Formally, a single point would suffice, but in practice some tools (e.g. Smoldyn) require multiple points to handle non-convex volumes bounded by explicit surfaces. For discontinuous surfaces with the same domainType, the interior point identifies which domain is associated with which surface patch defined in the geometry definition.

Each InteriorPoint has three attributes: coord1, coord2, and coord3.

3.19.1 The coord1, coord2, and coord3 attributes

An InteriorPoint element represents a single point within the defined coordinate system and should be in the interior of the domain that contains it. It has three attributes, coord1, coord2, and coord3, of type double, representing the position along each of the up to three coordinate axes defined by the CoordinateComponents (with index 0, 1, and 2 respectively for a three dimensional geometry; see Table 1 on page 19).

Each InteriorPoint must define the same number of attributes as there are dimensions of the corresponding **Geometry** to which it belongs.

In the case of surfaces, interior points are sometimes required to make unambiguous identification of multiple surfaces (e.g multiple plasma membranes for multiple cells present in a geometry). Due to roundoff error and finite word lengths, it is difficult to find a three dimensional point that lies on a surface. In this case, the distance from the surface will be used to provide unambiguous identification.

3.20 The AdjacentDomains class

AdjacentDomains (or domain adjacencies) captures the topological relationships within the **Geometry**. Consider that the **Domains** are nodes in a graph. The **AdjacentDomains** objects are the edges that specify the spatial connectivity of these nodes. Armed with the topology and the domain sizes, one can readily perform a compartmental approximation. Figure 10 on the following page shows the definition of the **AdjacentDomains** object.

3.20.1 The spatialId attribute

This attribute identifies an AdjacentDomains object. The attribute is of type SpId. It has no mathematical meaning.

3.20.2 The domain1 and domain2 attributes

The domain1 and domain2 attributes, of type SpIdRef, are required attributes. They are the spatialIds of two domains that touch each other (spatially adjacent). These are typically surface-volume contacts.

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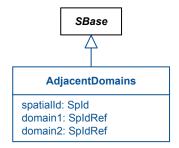


Figure 10: The definition of the AdjacentDomains class. Geometry can contain one instance of ListOfAdjacentDomains that can have one or more instances of AdjacentDomains objects.

3.21 The Geometry Definition class

A **Geometry** can specify a list of **GeometryDefinitions**. The **GeometryDefinition** is an abstract class that is the general term for the container which defines the concrete geometric constructs represented by the **Geometry**. Four types of **GeometryDefinitions** have been identified - **AnalyticGeometry**, **SampledFieldGeometry**, **ParametricGeometry**, **CSGeometry** (Constructed Solid Geometry) - and are elaborated in the following sections. The definition of the **GeometryDefinition** element is displayed in Figure 11. The spatial dimension of the **GeometryDefinition** must match the **spatialDimension** of the **DomainType** defined for the associated **Domain**.

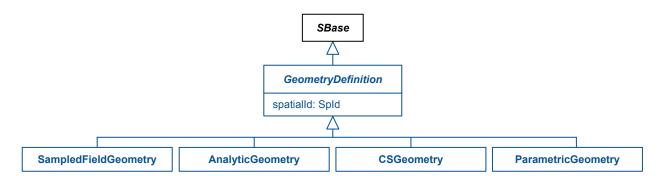


Figure 11: The Geometry Definition element. Geometry contains one instance of listOfGeometry Definitions that can contain one or more instances of Geometry Definition (one of AnalyticGeometry, SampledFieldGeometry, CSGeometry, ParametricGeometry, defined below).

3.21.1 The spatialId attribute

The **spatialId** attribute that is common to all the **GeometryDefinition** types is used to uniquely identify the **GeometryDefinition**. The attribute is of type **SpId**. A **GeometryDefinition** has no mathematical meaning.

3.22 The AnalyticGeometry class

The AnalyticGeometry is a class of *GeometryDefinition* where the geometry of each domain is defined by an analytic expression. An AnalyticGeometry is defined as a collection of AnalyticVolumes, one AnalyticVolume for each volumetric domain in the geometry. In this representation, the surfaces are treated as the boundaries between dissimilar AnalyticVolumes. The AnalyticGeometry object contains a ListOfAnalyticVolumes. Figure 12 on the following page shows the definition of the AnalyticGeometry object.

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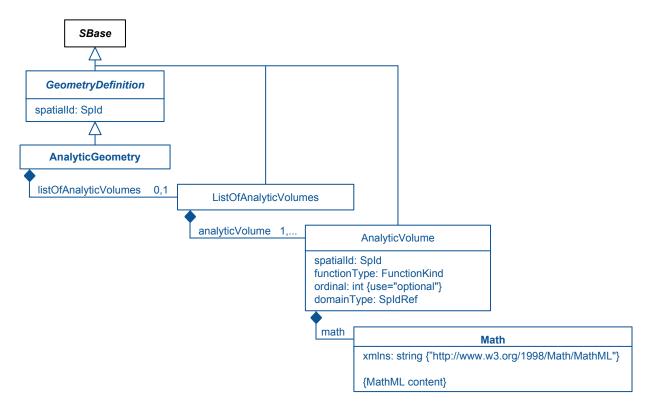


Figure 12: The definition of the AnalyticGeometry, ListOfAnalyticVolumes, and AnalyticVolume classes.

3.23 The Analytic Volume class

The **AnalyticVolume** is used to specify the analytic expression of a volumetric (3-dimensional) domain. The analytic expression for the **AnalyticVolume** is defined in the Math element.

3.23.1 The spatialId attribute

The **spatialId** attribute uniquely identifies the **AnalyticVolume**. The attribute is required and is of type **SpId**. It has no mathematical meaning.

3.23.2 The functionType attribute

The functionType attribute is of type FunctionKind and is currently limited to "layered" (to be renamed), or "R-function". A "layered" function type implies that the Math child element contains an inequality in the spatial dimensions (e.g. x,y,z) such that evaluation to "true" indicates that the point (x,y,z) is within that shape, and "false" indicates that it is not covered by that shape. The "R-function" functionType indicates that the shape is represented by a real-valued function whose sign indicates coverage by the shape.

Lucian: If you want to rename 'layered', now is the time to do it ;-)

3.23.3 The domainType attribute

R.

The domainType attribute of type SpIdRef is a required attribute. It represents the spatialId of the DomainType of the Domain that is represented by this AnalyticVolume.

3.23.4 The ordinal attribute

The **ordinal** attribute of type **int** is an optional attribute. It is used to represent the order of the **AnalyticVolume**. The **ordinal** is useful while reconstructing the geometry in the specific software tool - it represents the order in

which the **Analytic Volumes** representing geometric domains have to be evaluated.

Rather than struggle with the task of preventing overlapping regions of space from different **AnalyticVolumes**, the **AnalyticVolumes** are to be considered to be evaluated in the reverse order of their ordinals. In this way, any **AnalyticVolumes** that have already been processed will cover those with a smaller ordinal, thus resolving any ambiguities and removing the constraint that all **AnalyticVolumes** be disjoint and cover the entire geometric domain. The **AnalyticVolume** with **ordinal** 0 can be the "background" layer (typically the extracellular space).

No two **AnalyticVolumes** may have the same **ordinal** value, even if they should not overlap, because some tools may not calculate the geometries to the same level of precision as other tools, and may end up with overlap due to rounding errors, and will still need to resolve the ambiguity for their own purposes. Any **AnalyticVolume** without an **ordinal** value should also not overlap with any other **AnalyticVolume**, but if it does, the software tool may resolve the situation however it sees fit.

3.24 The Math class

The Math element is a required element for an **AnalyticVolume**. The Math element contains a MathML expression that defines the analytic expression for the **AnalyticVolume** referencing the coordinate components that are specified in the **ListOfCoordinateComponents** in the **Geometry**, according to the **functionType**.

3.25 The SampledFieldGeometry class

SampledFieldGeometry is a type of *GeometryDefinition* that defines a sampled image-based geometry or a geometry based on samples from a level set. **SampledFieldGeometry** is defined using a **SampledField** that specifies the sampled image and a list of **SampledVolumes** that represent the volumetric domains as sampled image regions. Figure 13 on the next page shows the definition of the **SampledFieldGeometry** object. It may be used for geometries of any dimension.

3.26 The SampledVolume class

A **SampledVolume** represents an interval of the sampled field that constitutes one or more contiguous regions. A **SampledVolume** is defined for each volumetric (3-dimensional) **Domain** in the **Geometry**. It has the following attributes.

3.26.1 The spatialId attribute

The **spatialId** attribute identifies a **SampledVolume** object. The attribute is of type **SpId** and is required when specifying a **SampledVolume**. It has no mathematical meaning.

3.26.2 The domainType attribute

The required domainType attribute is of type SpIdRef. It is the spatialId of the DomainType that represents this class of anatomical features. If there are more than one contiguous regions, then more than one domain will be defined corresponding to each SampledVolume.

3.26.3 The sampledValue attribute

The required sampledValue attribute is of type double. It represents the pixel value of a SampledVolume.

3.26.4 The minValue attribute

The optional minValue attribute is of type double. It represents the minimum of the pixel value (sampledValue) range.

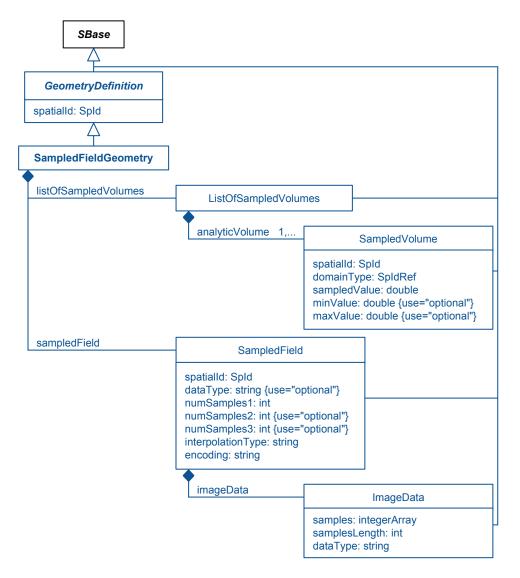


Figure 13: The definition of the SampledFieldGeometry, ListOfSampledVolumes, SampledVolume, SampledField, and ImageData classes.

3.26.5 The maxValue attribute

The optional maxValue attribute is of type double. It represents the maximum of the pixel value (sampledValue) range.

3.27 The SampledField class

A **SampledField** defined in a **SampledFieldGeometry** is a sampled scalar field such as an image or samples from a level set. Currently, the attributes of **SampledField** represent the specification of an image dataset (the number of samples in x, y, z coordinates, data type of the image representation, etc.) and the ImageData element of the **SampledField** specifies the actual image as integer sampled data.

3.27.1 The spatialId attribute

The **spatialId** attribute identifies a **SampledField**. It is of type **SpId** and is a required attribute. It has no mathematical meaning.

3.27.2 The numSamples1, numSamples2, numSamples3 attributes

The numSamples1, numSamples2, and numSamples3 attributes represent the number of samples in each of the coordinate components. (e.g. numX, numY, numZ) in an image dataset. These attributes are of type int and are required to specify the SampledField. The samples are assumed to be uniformly sampled.

3.27.3 The dataType attribute

This attribute represents the data type of each sample (e.g. int32). The attribute is of type string and is optional.

Lucian: This attribute seems a bit arbitrary, and unhelpful unless there's a standard list of possible values here. Is there one? If not, I say we drop the attribute entirely.

3.27.4 The interpolationType attribute

The **interpolationType** attribute is an optional attribute of type **string** and represents the interpolation type of the sampled data and is defined as "constant" for zeroth order, "linear" for first order, etc.

Lucian: Again, the list of possible values here needs to be explicitly stated. If it really can be any arbitrary order, switching this to a non-negative integer would make more sense.

3.27.5 The encoding attribute

The **encoding** attribute is an optional attribute of type **string**. It is used to specify text encoding and compression.

Lucian: Again, the list of possible values here needs to be explicitly stated, if it makes any difference to the model. Unless you really want people to be able to put in 'standard zip' or 'rot13' as their encoding type.

3.28 The ImageData class

The ImageData element represents the actual image data of the image-based geometry as encoded samples defined by the encoding and the data type. The ImageData element has the following attributes.

3.28.1 The samples attribute

The samples attribute is of type integerArray, whose values represent the image pixel values. This attribute is required.

3.28.2 The samplesLength attribute

The **samplesLength** attribute is of type **int** and is required. It represents the array length of the **samples** attribute (number of values in the image data array).

3.28.3 The dataType attribute

The dataType attribute is of type string and is required. Presently, this attribute indicates if the image data is 'compressed' or 'uncompressed'. Anu: (This attribute and the encoding attribute of SampledField have to be revisited.)

Lucian: I agree!

3.29 The CSGeometry class

CSGeometry (Constructed Solid Geometry) is a type of *GeometryDefinition* that defines a combined, solid, volumetric object from a number of primitive solid volumes by the application of set operations such as union, intersection and difference and affine transformations such as rotation, scaling, translation, etc. The **CSGeometry** element is defined by a listOfCSGObjects element that contains a collection of **CSGObjects**. Figure 14 on the following page shows the definition of the **CSGeometry** object.

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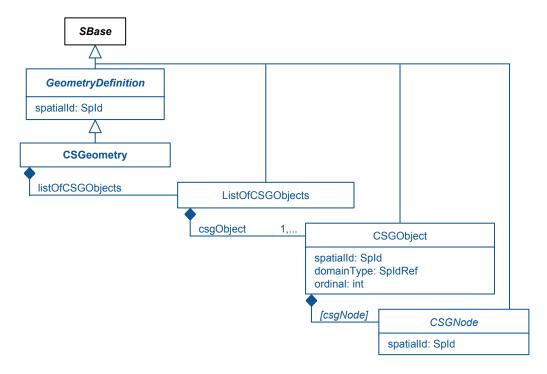


Figure 14: The definition of the CSGeometry, ListOfCSGObjects, and CSGObject classes.

3.30 The CSGObject class

Each CSGObject is a scene graph representing a particular geometric object using constructed solid geometry. A node in a tree (scene graph) is made up of CSGPrimitives, CSGSetOperators, and CSGTransformations. Note that the CSGPrimitives are always leaves in this tree. The CSGObject is analogous to an AnalyticVolume element in the sense that it is a constructed geometry (from primitives) used to specify a volumetric (3-dimensional) domain. The CSGObject element has three attributes: spatialId, domain and ordinal. The definition of the CSGObject is completed by defining a CSGNode which is the root of the CSGObject scene graph.

3.30.1 The spatialId attribute

The spatialId attribute uniquely identifies the CSGObject element. The attribute is required and is of type SpId.

Lucian: Does this element have mathematical meaning?

3.30.2 The domain attribute

The **domain** attribute is of type **SpIdRef** and is a required attribute. It is a reference to the **spatialId** of the **Domain** that this **CSGObject** represents.

Lucian: Am I correct in assuming that this information is redundant with the corresponding **Domain**'s interior points list? Is this information necessarily redundant? Is that OK? I'm going to assume that the following is a reasonable restriction:

All InteriorPoints of the corresponding Domain must be points inside the geometry this CSGObject describes.

3.30.3 The ordinal attribute

The **ordinal** attribute of type **int** is an optional attribute. It is used to represent the order of the **CSGObject**. The **ordinal** is useful while reconstructing the geometry in the specific software tool - it represents the order in which the **CSGObjects** representing geometric domains have to be placed.

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Lucian: We should probably be as explicit here as we were with the similar "ordinal" attribute of the AnalyticVolume class. Can I assume that the same rules apply and copy the text here? One oddness is that the "ordinal" attribute of the AnalyticVolume class is optional, while here it is required. If they do the same thing, we should probably either make them both optional, or both required.

3.30.4 The [csgNode] child

The child [csgNode] element represents the geometry that is to be linked to the domainType of the CSGObject. Note that the child of the CSGObject element is not called "csgNode" but rather takes the name of the derived class, decapitalized. Thus, a CSGObject may have a csgPrimitive, csgPseudoPrimitive, csgSetOperator, csgTranslation, csgRotation, csgScale, or csgHomogeneousTransformation child.

3.31 The CSGNode class

The operators and operands used to construct a constructed solid geometry are generalized as a *CSGNode*, defined in Figure 15 as an abstract base class. The classes that inherit from *CSGNode* can be one of the following: **CSGSet-Operator**, *CSGTransformation* (operators; itself another abstract base class), **CSGPrimitive**, or **CSGPseudoPrimitive** (operands). The *CSGNode* has one attribute: **spatialId**. The **CSGObject** contains a *CSGNode* object which is the root of the **CSGObject** scene graph (representing one constructed solid geometry domain).

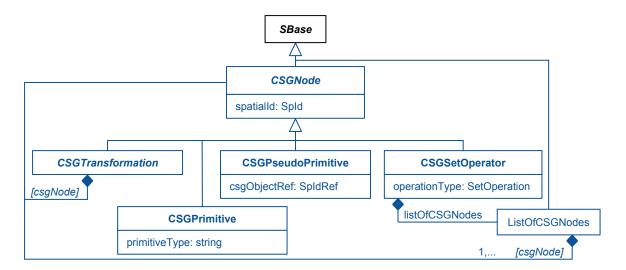


Figure 15: The definition of the abstract base class CSGNode, and its subclasses CSGPrimitive, CSGPseudoPrimitive, and CSGSetOperator. The abstract base class CSGTransformation (also a subclass of CSGNode) is defined in Section 3.36 on the next page.

3.31.1 The spatialId attribute

The spatialId attribute uniquely identifies the *CSGNode* element. The attribute is required and is of type SpId.

Lucian: Do any of these classes have mathematical meaning?

3.32 The CSGPrimitive class

CSGPrimitive element represents the primitive geometric shapes that can be represented by the **CSGeometry**. Some of the primitive shapes that can be used are "sphere", "cylinder", "cube", "cone", etc. These shapes are defined with a predefined orientation and fitting within the unit cube (+/- 1 in x, y, and z). This element has one required attribute: primitiveType of type string.

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3.32.1 The primitiveType attribute

The **primitiveType** attribute is a required attribute that is of type **string**. It represents one of the predefined primitive shapes.

Lucian: This list absolutely needs to be included in the spec!

3.33 The CSGPseudoPrimitive class

CSGPseudoPrimitive element is used to reference a pre-defined **CSGObject** object while defining a **CSGObject** (geometric domain). This allows the re-use of one constructed **CSGObject** in another. It has one attribute of type SpIdRef.

3.33.1 The csgObjectRef attribute

The csgObjectRef attribute identifies a pre-defined CSGObject in the CSGeometry The attribute is required and is of type SpId. A CSGObject may not reference itself, nor its parent, nor its parent's parent, etc.

3.34 The CSGSetOperator class

The **CSGSetOperator** element represents the set operations (union, intersection, difference) that can be performed on a set of primitive geometric shapes (**CSGPrimitives**) or on a set of **CSGNodes** (a transformation or set operation on one or a set of **CSGPrimitives**). This element has one attribute of type **string**. It also contains a required child **ListOfCSGNodes** that represents the set of nodes on which the set operation is performed.

3.34.1 The operationType attribute

The operationType attribute is of type SetOperation and represents an operation that can be performed on a set of *CSGNodes*. The possible values that the operationType attribute can take are "union", "intersection" or "difference".

Lucian: 'union' and 'intersection' are unordered, but 'difference' is order-dependent, which is tricky to accomplish in the order-agnostic XML of SBML. Either you have to say that order is important in this one case (something we've tried to avoid everywhere else), or we add an 'order' attribute somewhere, or we drop 'difference' as a possible set operator. Also, according to wikipedia, the more common term is 'complement', with 'relative complement' and 'absolute complement' both meaning different things.

3.35 The ListOfCSGNodes class

The **ListOfCSGNodes** must contain one or more **csgNode** children that are to be combined according to the set operation of the parent **CSGSetOperator**. While having a single child is legal, this is semantically equivalent to simply putting that child in the model instead of the **CSGSetOperator**, and therefore has limited modeling benefit. Note that the children of the **ListOfCSGNodes** object are not called **csgNode** but rather take the name of the derived class, decapitalized. Thus, they may be called **csgPrimitive**, **csgPseudoPrimitive**, **csgSetOperator**, **csgTranslation**, **csgRotation**, **csgScale**, or **csgHomogeneousTransformation**.

3.36 The CSGTransformation class

The *CSGTransformation* represents a generalization for the type of transformation that can be performed on a primitive geometric shape (*CSGPrimitive*) or on a *CSGNode* (a transformation or set operation on one or a set of *CSGPrimitives*). The types of possible transformations are 'rotation', 'translation', 'scaling', and 'homogeneous transformation', defined below. The *CSGTransformation* element contains a *CSGNode* element upon which the transformation is performed. It also has one attribute: transformationType of type string.

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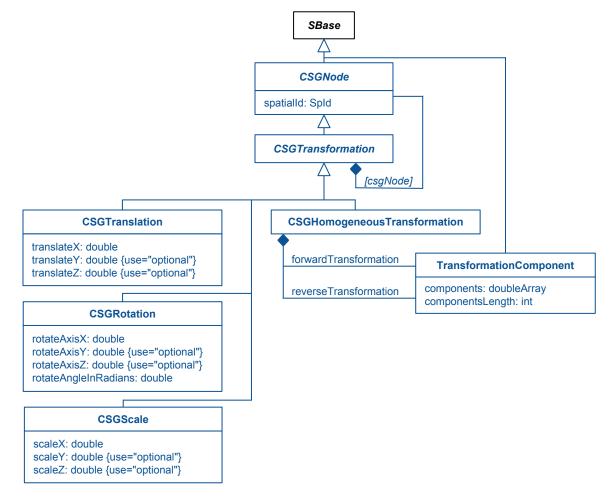


Figure 16: The definition of the abstract base class CSGTransformation, its subclasses, CSGRotation, CSGScale, and CSGHomogeneousTransformation, and the TransformationComponent class.

3.36.1 The transformationType attribute

The transformationType attribute is of type **string** and is a required attribute. It represents the type of transformation ('rotation', 'translation', 'scaling', and 'homogeneous transformation').

Lucian: This attribute didn't show up in the UML diagrams, and is redundant if the names of the elements are 'csgRotation', 'csgTranslation', etc. I would strongly recommend the naming approach, as you've done this already, and I in fact already assumed it would be done this way. If not... can we change it? I dunno.

3.36.2 The csgNode child

The child csgNode element represents the geometry that is to be transformed by the *CSGTransformation* element. Note that this child is not called csgNode but rather takes the name of the derived class, decapitalized. Thus, it may be called csgPrimitive, csgPseudoPrimitive, csgSetOperator, csgTranslation, csgRotation, csgScale, or csgHomogeneousTransformation.

3.37 The CSGTranslation class

The **CSGTranslation** element represents a translation transformation on a *CSGNode* (a transformation or set operation on one or a set of **CSGPrimitives**) or a **CSGPrimitive** along the axes defined in the **Geometry**. This element has 3 attributes:

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3.37.1 The translateX attribute

The translateX attribute is of type double. It represents the translation of the *CSGNode* along the x-axis (the CoordinateComponent with the componentType of "cartesianX").

3.37.2 The translateY attribute

The translateY attribute is of type double. It represents the translation of the *CSGNode* along the y-axis (the CoordinateComponent with the componentType of "cartesianY").

3.37.3 The translateZ attribute

The translateZ attribute is of type double. It represents the translation of the *CSGNode* along the z-axis (the CoordinateComponent with the componentType of "cartesianZ").

Lucian: I still think it's awkward to have attributes here that correspond to attribute *values* somewhere else, but it's at least not incorrect, like it was before we stripped everything but the cartesian coordinate system. Not sure what a good fix would be, though.

3.38 The CSGRotation class

The **CSGRotation** element represents a rotation transformation on a **CSGNode** (a transformation or set operation on one or a set of **CSGPrimitives**) or a **CSGPrimitive** about the axes defined in the **Geometry**. This element has 4 attributes:

3.38.1 The rotateX attribute

The rotateX attribute is of type double. It represents the rotation of the *CSGNode* along the x-axis (the Coordinate-Component with the componentType of "cartesianX").

Lucian: I don't know what 'the rotation' means, since there's already an angle attribute. Are we talking relative rotation of that angle on this axis? I think we need more semantics here.

3.38.2 The rotateY attribute

The rotateY attribute is of type double. It represents the rotation of the *CSGNode* along the y-axis (the Coordinate-Component with the componentType of "cartesianY").

3.38.3 The rotateZ attribute

The rotateZ attribute is of type double. It represents the rotation of the *CSGNode* along the z-axis (the Coordinate-Component with the componentType of "cartesianZ").

3.38.4 The rotationAngleInRadians attribute

The **rotationAngleInRadians** attribute is of type **double**. It represents the rotation angle of the **CSGNode**, in radians, along the defined axis.

3.39 The CSGScale class

The **CSGScale** element represents a scale transformation on a *CSGNode* (a transformation or set operation on one or a set of **CSGPrimitives**) or a **CSGPrimitive** along the axes defined in the **Geometry**. This element has 3 attributes:

Lucian: Does it make a difference if the object is scaled and remains centered where it was, or leaves its corner at the origin? If so, the version used should be explicitly stated here, I think.

3.39.1 The scaleX attribute

The scaleX attribute is of type double. It represents the amount of scaling of the *CSGNode* along the x-axis (the CoordinateComponent with the componentType of "cartesianX").

3.39.2 The scaleY attribute

The scaleY attribute is of type double. It represents the amount of scaling of the *CSGNode* along the y-axis (the CoordinateComponent with the componentType of "cartesianY").

3.39.3 The scaleZ attribute

The scaleZ attribute is of type double. It represents the amount of scaling of the *CSGNode* along the z-axis (the CoordinateComponent with the componentType of "cartesianZ").

3.40 The CSGHomogeneousTransformation class

The **CSGHomogeneousTransformation** element represents a homogeneous transformation on a **CSGNode**: a transformation or set operation on one or more **CSGPrimitives**. This element contains two TransformationComponent elements: a **forwardTransformation** and a **reverseTransformation**, both of type **TransformationComponent**.

Lucian: The difference between the forward and reverse transformations needs to be explained here, as well as why you need both.

3.41 The TransformationComponent class

The **TransformationComponent** element represents an affine transformation that can be applied to a *CSGNode*. This element has the following two attributes:

3.41.1 The components attribute

The **components** attribute is of type **doubleArray**, whose values represent the affine transformation. This attribute is required.

3.41.2 The componentsLength attribute

The componentsLength attribute is of type int and is required. It represents the array length of the components attribute (number of values in the components array).

3.42 The ParametricGeometry class

ParametricGeometry is a type of *GeometryDefinition* that parametrically defines geometric strucutures/domains. The ParametricGeometry element is defined with a listOfObjects that is a collection of ParametricObjects and a listOfSpatialPoints that is a collection of SpatialPoints. Figure 17 on the following page shows the definition of the ParametricGeometry object.

3.43 The ParametricObject class

The **ParametricObject** element represents a parametric geometry object.

3.43.1 The spatialId attribute

The spatialId attribute is a required attribute of type SpId. It uniquely identifies the ParametricObject element.

Lucian: Does this element have mathematical meaning?

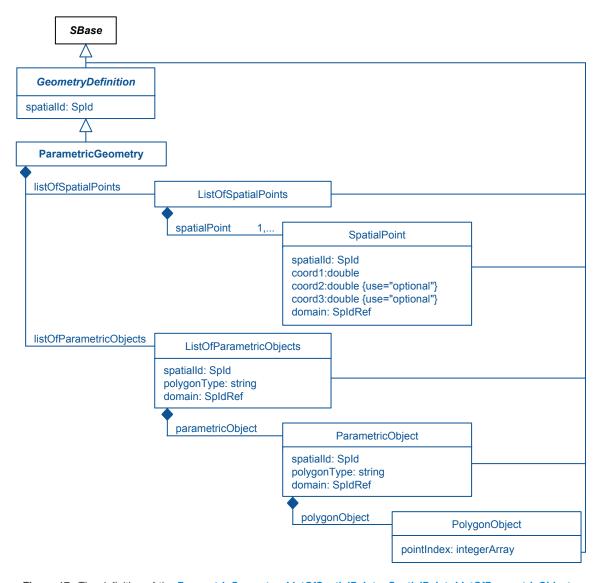


Figure 17: The definition of the ParametricGeometry, ListOfSpatialPoints, SpatialPoint, ListOfParametricObjects, ParametricObject, and PolygonObject classes.

3.43.2 The polygonType attribute

The polygonType attribute is of type string and is a required attribute. It represents the type of polygon that describes the ParametricObject.

Lucian: What options are there for this attribute?

3.43.3 The domain attribute

The **domain** attribute is of type **SpIdRef** and is a required attribute. It is a reference to the **spatialId** of the domain that this **ParametricObject** represents.

Lucian: As above: Am I correct in assuming that this information is redundant with the corresponding **Domain**'s interior points list? Is this information necessarily redundant? Is that OK? I'm going to assume that the following is a reasonable restriction:

All InteriorPoints of the corresponding Domain must be points inside the geometry this ParametricObject describes.

3.44 The PolygonObject class

The polygonObject represents an ordered list of indices that refer to elements in the SpatialPoints array and are interpreted by considering the **polygonType** attribute of the **ParametricObject**. For reference, we could consider using the VTK polydata convensions for shapes and vertex orderings.

Lucian: Wait, 'consider'? Are there other options? If so, how would the modeler know that a different conversion was being followed? Or does it not matter?

3.44.1 The pointIndex attribute

The pointIndex attribute is an array of integers holding the indices of the points in the SpatialPoints array.

3.45 The SpatialPoint class

The **SpatialPoint** element represents a point used as a vertex in the **ParametricGeometry**.

3.45.1 The spatialId attribute

The spatialId element uniquely identifies a SpatialPoint element. It is a required attribute and is of type SpId.

Lucian: Does this element have mathematical meaning?

3.45.2 The coord1, coord2, and coord3 attributes

The **coord1**, **coord2**, **coord3** attributes are of type **double**. They represent the 3-dimensional coordinate of the SpatialPoint. Depending on the dimension of the **Geometry**, one, two or all the three attributes are required.

3.45.3 The domain attribute

The **domain** attribute is of type **SpIdRef** and is a required attribute. It is a reference to the **spatialId** of the domain which contains this SpatialPoint.

Lucian: And once more:

All InteriorPoints of the corresponding Domain must be points inside the geometry this SpatialPoint describes.

4 Examples

This section will hopefully contain examples employing the Spatial package for SBML Level 3.

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5 Interaction with the Required Elements package

The Required Elements package is designed to create a way for a modeler to denote which specific elements of an SBML model have changed due to interactions with a package. The Spatial Processes package can change the mathematical meaning of the SBML core elements **Compartment**, **Species**, **Reaction**, and **Parameter**. If the Required Elements namespace and the Spatial Processes namespace are declared in the same SBML document, the following restrictions apply. Note that these do not apply in a document without the Required Elements namespace declared.

5.1 Compartments

When a spatial geometry is defined in the SBML model, the **Compartment** element may be extended for the spatial package to represent a spatially-defined area with particular boundaries whose mathematical value is defined as its unitSize multiplied by the size of the **DomainType** to which it maps. Any **Compartment** with a child **CompartmentMapping** element must therefore have a **ChangedMath** child pointing to the Spatial Processes namespace. Its viableWithoutChange attribute may be set to "true" if the compartment's size is set with the size attribute (setting it through a **Rule** or **InitialAssignment** is illegal for the purposes of the spatial package). For example, the modeling package may precalculate the compartment size and store it in the Compartment size attribute. However, due to slight differences in mesh generation between simulators, the domain size actually used within computations may vary slightly from simulator to simulator, and will thus introduce small errors that may break mass conservation.

A **Compartment** without a child **CompartmentMapping** element remains unaffected by the Spatial package, and must therefore not have a **ChangedMath** child that points to the Spatial Processes namespace.

5.2 Species

Any **Species** with the <code>isSpatial</code> attribute set to "true" must have a **ChangedMath** child that points to the Spatial Processes namespace, as the model assumes a spatially-distributed level of that **Species**, instead of considering it to be a well-mixed pool. Its <code>viableWithoutChange</code> attribute may be set to "true" if the model specifies the initialAmount or initialConcentration attributes of the Species or if the initial condition is specified by a Rule or an InitialAssignment.

A **Species** with the **isSpatial** attribute set to "**false**" remains unaffected by the Spatial package, and must therefore not have a **ChangedMath** child that points to the Spatial Processes namespace.

5.3 Reactions

Any **Reaction** with an <code>isLocal</code> attribute set to "true" must have a **ChangedMath** child that points to the Spatial Processes namespace, as the model treats such a **Reaction** as defining a change in local substrate concentrations over time, instead of as a change in global substrate amounts over time. Its <code>viableWithoutChange</code> attribute will therefore almost always be set to "false", as the units of the <code>KineticLaw</code> have been changed. However, concentration over time can be numerically identical to amount over time in <code>Compartments</code> of unit volume; in this situation, the value of that attribute may be set to "true". However, this practice is discouraged.

A **Reaction** with the **isLocal** attribute set to "**false**" remains unaffected by the Spatial package, and must therefore not have a **ChangedMath** child that points to the Spatial Processes namespace.

5.4 Parameters

A Parameter object with a SpatialSymbolReference child does not take its value from its value attribute, but rather from the Spatial object with which it is linked. Therefore, all Parameter objects with a SpatialSymbolReference child must have a ChangedMath child that points to the Spatial Processes namespace. Its viableWithoutChange attribute may be set to "true" if the Parameter's value is set, and/or if there is an InitialAssignment or Rule that sets

that value.

Parameter objects with DiffusionCoefficient, AdvectionCoefficient, or BoundaryCondition children, on the other hand, still take their values from the value attribute and/or other SBML Level 3 Version 1 Core elements, and remain unchanged by any Spatial construct. Therefore, these and any other Parameter elements without SpatialSymbolReference children may not be given a ChangedMath child that points to the Spatial Processes namespace.

5.5 General

No other SBML Level 3 Version 1 Core element is affected by the Spatial Processes package, and none may therefore not have a **ChangedMath** child that points to the Spatial Processes namespace.

A Validation of SBML documents using Spatial constructs

This section summarizes all the conditions that must (or in some cases, at least *should*) be true of an SBML Level 3 Version 1 model that uses the Spatial package. We use the same conventions that are used in the SBML Level 3 Version 1 Core specification document. In particular, there are different degrees of rule strictness. Formally, the differences are expressed in the statement of a rule: either a rule states that a condition *must* be true, or a rule states that it *should* be true. Rules of the former kind are strict SBML validation rules—a model encoded in SBML must conform to all of them in order to be considered valid. Rules of the latter kind are consistency rules. To help highlight these differences, we use the following three symbols next to the rule numbers:

- ✓ A checked box indicates a *requirement* for SBML conformance. If a model does not follow this rule, it does not conform to the Spatial package specification. (Mnemonic intention behind the choice of symbol: "This must be checked.")
- A triangle indicates a *recommendation* for model consistency. If a model does not follow this rule, it is not considered strictly invalid as far as the Spatial package specification is concerned; however, it indicates that the model contains a physical or conceptual inconsistency. (Mnemonic intention behind the choice of symbol: "This is a cause for warning.")
- ★ A star indicates a strong recommendation for good modeling practice. This rule is not strictly a matter of SBML encoding, but the recommendation comes from logical reasoning. As in the previous case, if a model does not follow this rule, it is not considered an invalid SBML encoding. (Mnemonic intention behind the choice of symbol: "You're a star if you heed this.")

The validation rules listed in the following subsections are all stated or implied in the rest of this specification document. They are enumerated here for convenience. Unless explicitly stated, all validation rules concern objects and attributes specifically defined in the Spatial package.

For convenience and brievity, we use the shorthand "spatial:x" to stand for an attribute or element name x in the namespace for the Spatial package, using the namespace prefix spatial. In reality, the prefix string may be different from the literal "spatial" used here (and indeed, it can be any valid XML namespace prefix that the modeler or software chooses). We use "spatial:x" because it is shorter than to write a full explanation everywhere we refer to an attribute or element in the Spatial package namespace.

General rules about the Spatial package

- spatial-10101 ☑ To conform to Version 1 of the Spatial package specification for SBML Level 3, an SBML document must declare the use of the following XML Namespace:

 "http://www.sbml.org/sbml/level3/version1/spatial/version1". (References: SBML Level 3 Package Specification for Spatial, Version 1, Section 3.2 on page 8.)
- spatial-10102

 ✓ Wherever they appear in an SBML document, elements and attributes from the Spatial package must be declared either implicitly or explicitly to be in the XML namespace

 "http://www.sbml.org/sbml/level3/version1/spatial/version1". (References: SBML Level 3 Package Specification for Spatial, Version 1, Section 3.2 on page 8.)

Rules for the extended SBML class

- spatial-10201 ✓ In all SBML documents using the Spatial package, the SBML object must include a value for the attribute spatial:required attribute. (References: SBML Level 3 Version 1 Core, Section 4.1.2.)
- spatial-10202

 ✓ The value of attribute spatial:required on the SBML object must be of the data type boolean. (References: SBML Level 3 Version 1 Core, Section 4.1.2.)

spatial-10203

✓ The value of attribute spatial:required on the SBML object must be set to "true" (References: SBML Level 3 Package Specification for Spatial, Version 1, Section 3.2 on page 8.)

General rules about attributes

Lucian: Obviously this will need to be filled out.

Acknowledgments

Work such as this does not take place in a vacuum; many people contributed ideas and discussions that shaped the Groups proposal that you see before you. We particularly thank Frank Bergmann, and the members of the *sbml-discuss* and *sbml-spatial* mailing lists for suggestions and comments.

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