# **Qualitative Models**

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This is a working draft of the specification for the SBML Level 3 package "qual". It is not a normative document. Please send comments and other feedback to the Package Working Group mailing list, sbml-qual@lists.sourceforge.net.

The latest release, past releases, and other materials related to this specification are available at  $\label{latest} $$ $$ http://sbml.org/Community/Wiki/SBML\_Level_3\_Proposals/Qualitative\_Models $$$ 

This release of the specification is available at http://sbml.org/images/a/a7/SBML-L3-qual-specification\_0.1.pdf



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# 1 Introduction

1.1 Motivation

Quantitative methods for modelling biological networks require an in-depth knowledge of the biochemical reactions and their stoichiometric and kinetic parameters. In many cases, this knowledge is missing. This has led to the development of several qualitative modelling methods using information such as gene expression data coming from functional genomic experiments. Qualitative models are typically based on the definition of *regulatory* or *influence graph*. The components of these models differ from species and reactions used in current SBML models. For example, qualitative models typically associate discrete levels of activities with entity pools; the processes involving them cannot be described as reactions per se but rather as transitions between states. Boolean networks, logical models and some Petri nets are the most used qualitative formalisms in biology. Despite differences from traditional SBML models, it is desirable to bring these classes of models under a common format scheme. The purpose of this Qualitative Models package for SBML Level 3 is to support qualitative models into SBML.

# 2 Background and context

After several attempts to use the existing SBML L2 format, a decision was made to develop an extension for SBML L3. A first proposal written in August 2008 by Duncan Berenguier and Nicolas Le Novère was discussed during a meeting on the 12th and 13th of August 2008<sup>1</sup>. This meeting led to the release of a document (L3F\_extention\_draft\_1.2.pdf) which is a revision of a previous proposal for this package. A summary of the meeting is available at http://www. bi.ac.uk/compneur/xwiki/bin/view/SBML/L3F, and a document A second meeting was held at in November

2010 (see http://compbio.igc.gulbenkian.pt/nmd/node/30, for the program and participants). A revised version of the proposal was discussed during this meeting. This document accounts for the outcomes of the meeting discussions and of following exchanges.

<sup>&</sup>lt;sup>1</sup>Nicolas Le Novère (SBML), Sarah Keating (SBML), Nicolas Rodriguez (SBML), Denis Thieffry (GINsim), Duncan Berenguier (GINsim), Aurélien Naldi (GINsim), Claudine Chaouiya (GINsim, Petri nets), Tomas Helikar (Chemchains), Ioannis Xenarios (SQUAD), Alessandro Di Cara (SQUAD), Mathias John (PiML), Dagmar Koehn (PiML)

# 3 Package syntax and semantics

In this section, we define the syntax and semantics of the Hierarchical Model Composition package for SBML Level 3 Version 1. We expound on the various data types and constructs defined in this package, then in Section 4, we provide complete examples of using the constructs in example SBML models.

# 3.1 Namespace URI and other declarations necessary for using this package

Every SBML Level 3 package is identified uniquely by an XML namespace URI. For an SBML document to be able to use a given SBML Level 3 package, it must declare the use of that package by referencing its URI. The following is the namespace URI for this version of the Qualitative Models package for SBML Level 3 Version 1:

```
"http://www.sbml.org/sbml/level3/version1/qual/version1"
```

In addition, SBML documents using a given package must indicate whether understanding the package is required for complete mathematical interpretation of a model, or whether the package is optional. This is done using the attribute required on the <sbml> element in the SBML document. For the Qualitative Models package, the value of this attribute must be set to "true".

The following fragment illustrates the beginning of a typical SBML model using SBML Level 3 Version 1 and this version of the Qualitative Models package:

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1/core" level="3" version="1"
    xmlns:qual="http://www.sbml.org/sbml/level3/version1/qual/version1" qual:required="true">
```

# 3.2 Primitive data types

Section 3.1 of the SBML Level 3 specification defines a number of primitive data types and also uses a number of XML Schema 1.0 data types NEED CITATION. We assume and use some of them in the rest of this specification, specifically boolean, ID, SId, SIdRef, UnitSId, UnitSIdRef, and string. The Qualitative Model package defines other primitive types; they are described below.

#### 3.2.1 Type temporisationType

The temporisationType is an enumeration of values used to indicate the updating policy used by a **Transition**. The possible values are timer, priority, sustain, proportion and rate.

# 3.2.2 Type sign

The **sign** is an enumeration of values used to indicate direction of an **Input** within the system. The possible values are positive, negative and dual.

#### 3.2.3 Type transitionInputEffect

The transitionInputEffect is an enumeration of values used to indicate the effect of an Input Transition within the system. The possible values are none and consumption.

## 3.2.4 Type transitionOutputEffect

The transitionOutputEffect is an enumeration of values used to indicate the effect of an Output Transition within the system. The possible values are production, assignmentLevel and assignmentSymbol.

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# 3.3 Qualitative modelling

Before describing the classes and their attributes that have been used by this Qualitative Models Specification it is worth clarifying the intended meaning of some of the terms used.

## 3.3.1 Levels and symbols

The entities being modelled have either a *level* or a *symbol* associated with them that indicate the current state of the entity.

A *level* may be a boolean but may also represent more than two states and thus is considered to be an integer. In the case of the entity being a boolean its allowed levels would be "0" or "1"; but in other cases it may have any number of levels i.e. integer values up to and including a maximum.

A *symbol* is intended to represent any value that might be appropriate in the model. A user can merely define the set of symbols that might be used and how the **symbolValue** associated with an entity might be altered by the model.

TODO: Some examples of symbols that might be used would be good

3.3.2 Transitions

Qualitative Models consider *transitions* between the levels/symbols of the entities involved in the model. This may involve the level of an entity being increased or decreased by a fixed amount; the level/symbol remaining unchanged; or the level/symbol being reassigned to an alternate value. Transitions occur when a set of conditions is met. These conditions may involve the levels/symbols falling above or below a given *threshold*. A simple example of this is the case where there are two entities A and B and the model states that when the level of A exceeds "1" (the threshold), the level of B is increased by "1".

3.3.3 FunctionTerms

The resulting value of an entity following a transition may have several possibilities that are governed by a number of conditions. Each transition can have a list of conditional functions *functionTerms*, each associated with a result that allow the user to specify sets of piecewise conditions. For example a model may wish to encode the following

$$B = \begin{cases} B+1 & \text{if } A < 1\\ B & \text{if } 1 <= A < 3\\ B+2 & \text{otherwise} \end{cases}$$

In this case the **Transition** would have a **FunctionTerm** for each of the first two conditions and a **DefaultTerm** for the otherwise component.

## 3.4 The extended Model class

The extension of SBML Level 3 Core's **Model** class is relatively straightforward: the Qualitative Models Package adds two lists, one for holding qualitativeSpecies (listOfQualitativeSpecies, of class **ListOfQualitativeSpecies**), and the other for holding transitions (listOfTransitions, of class **ListOfTransitions**). Figure 1 on the following page provides the UML diagram. The **Model** element may contain at most one **ListOfQualitativeSpecies**, which must contain at least one **QualitativeSpecies**. It may also contain at most one **ListOfTransitions** which must contain at least one **Transition**. The **QualitativeSpecies** class and the **Transition** class are defined in Section 3.5 and Section 3.6 respectively.

# 3.5 The QualitativeSpecies class

Similarly to the **Species** in SBML, the components of qualitative models refer to pools of entities that are considered indistinguishable and are each located in a specific **Compartment**. However, here components are characterised by their qualitative influences rather than by taking parts into reactions. Therefore, we define the **Qualita-**

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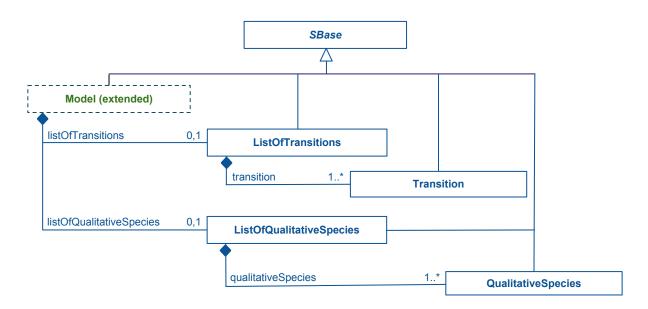


Figure 1: The definitions of the extended Model class. In other respects, Model remains defined as in the SBML Level 3 Core specification.

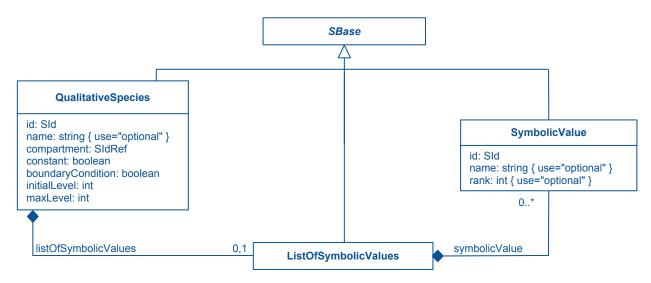


Figure 2: The definitions of the QualitativeSpecies class.

tiveSpecies element to represent such pools of entities.

A **QualitativeSpecies** describes a pool of indistinguishable entities in a **Compartment**. It is associated with either a **level** or a **symbolValue** from its **SymbolicValue**. These objects classes are defined in Figure 2.

The id attribute

The **id** attribute takes a required value of type **SId**. The **id** is used as an identifier for the particluar **QualitativeSpecies**. It can be used as a <ci> element within MathML, in which case it it interpreted as the *level* or *symbol* of this **QualitativeSpecies**.

The name attribute

A **QualitativeSpecies** also has an optional name attribute of type **string**. The name attribute should be used in the same manner as on SBML Level 3 Core objects; see Section 3.3.2 of the SBML Level 3 Version 1 Core specification for more information.

## The compartment attribute

The required attribute compartment, of type SIdRef, is used to identify the compartment in which the qualitativeSpecies is located. The attribute's value must be the identifier of an existing **Compartment** object in the model. This attribute is comparable with the compartment attribute on the **Species** element.

#### The constant and boundaryCondition attributes

These attributes are treated as in **Species** elements.

Question: Since a qualitativeSpecies cannot take part in a reaction what meaning does boundaryCondition have ??

Question: Does constant mean it cannot be changed by a transition?

The initialLevel attribute

The initialLevel is an integer that defines the initial *level* of the **QualitativeSpecies** in its **Compartment**. This attribute is optional.

The maxLevel attribute

The maxLevel is an integer that sets the maximal *level* of the QualitativeSpecies. This attribute is optional.

## 3.5.1 The Symbolic Value class

The **QualitativeSpecies** element may contain at most one **SymbolicValue** that contains zero or more **SymbolicValue** elements. An empty list is allowed, and useful for e.g. adding annotations.

The **SymbolicValue** element defines a non instantiated parameter that allows the model to associate undefined values with a particular **QualitativeSpecies**. Symbols can be considered as uninstantiated parameters. Such symbols may represent the different solutions of piecewise linear differential equations, along with different thresholds.

The id attribute

A **SymbolicValue** element has an **id** attribute that takes a required value of type **SId**. The **id** is used as an identifier for the particluar **SymbolicValue** and may be referenced by the **symbolicResult** attribute of a **FunctionTerm** within a **Transition** to indicate that this **SymbolicValue** is the resulting value for this **QualitativeSpecies** following a particular **Transition**.

The name attribute

There is an optional name attribute of type string that should be used in the same manner as on SBML Level 3 Core objects; see Section 3.3.2 of the SBML Level 3 Version 1 Core specification for more information.

The rank attribute

The **rank** is an **integer** that defines the position of the symbol in the **SymbolicValue**. This attribute is optional.

Question: What difference does the position make or does rank meaning ordering independent of physical position?

Question: Are symbols and levels exclusive?

# 3.6 The Transition class

A **Transition** element contains at most one **ListOfInputs** and exactly one **ListOfOutputs** and one **ListOfFunction-Terms**. These objects classes are defined in Figure 3 on the following page.

The id attribute

A **Transition** element has an optional id attribute of type SId.

The name attribute

There is an optional name attribute of type string that should be used in the same manner as on SBML Level 3 Core objects; see Section 3.3.2 of the SBML Level 3 Version 1 Core specification for more information.

## The temporisationType attribute

A **Transition** has an attribute **temporisationType** of type **temporisationType** used to indicate the updating policy associated with this **Transition** element. This attribute is optional. Table 1 describes the different updating policies.

TemporisationType	Interpretation
timer	TBD
priority	TBD
sustain	TBD
proportion	TBD
rate	TBD

Table 1: Interpretation of the temporisationType attribute on a Transition.

## TODO: need more explanation of this

## 3.6.1 The Input class

The **ListOfInputs** contains zero or more elements of type **Input**. A transition with zero inputs can be useful for defining an initial assignment, where the state of an output depends on a function but not on any input values. An empty list is allowed, and useful for e.g. adding annotations. Each **Input** refers to a **QualitativeSpecies** that participates in the corresponding **Transition**.

The id attribute

An **Input** element has an optional **id** attribute of type **SId**. The identifier of an **Input** can be used as a <ci> element within MathML, in which case it it interpreted as the **thresholdLevel** or **thresholdSymbol**.

The name attribute

There is an optional name attribute of type string that should be used in the same manner as on SBML Level 3 Core objects; see Section 3.3.2 of the SBML Level 3 Version 1 Core specification for more information.

#### The qualitativeSpecies attribute

The required attribute qualitativeSpecies, of type SIdRef, is used to identify the QualitativeSpecies that is the *input* of this Transition. The attribute's value must be the identifier of an existing QualitativeSpecies object in the model. This attribute is comparable with the species attribute on the SpeciesReference element.

#### The thresholdLevel and thresholdSymbol attributes

The thresholdLevel is a integer. The thresholdSymbol is a SIdRef that must refer to the identifier of a SymbolicValue. These attributes are optional and but mutually exclusive. It is invalid to define both.

Question: Must the thresholdSymbol refer to one of the listOfSymbolicValues in the QualitativeSpecies that is referenced by this In

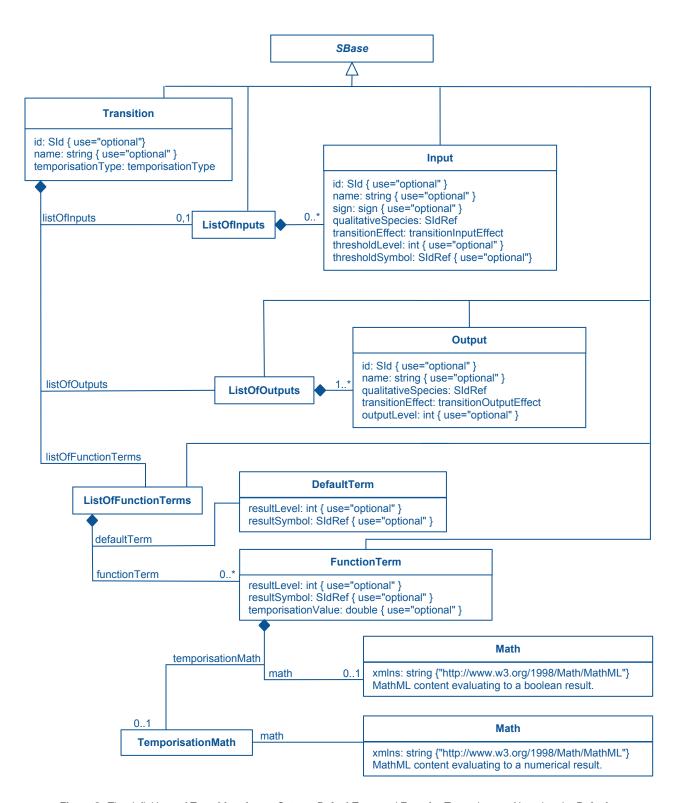


Figure 3: The definitions of Transition, Input, Output, DefaultTerm and FunctionTerm classes. Note that the DefaultTerm class is not derived from SBase.

## The transitionEffect attribute

Each Input has a required attribute transitionEffect of type transitionInputEffect which describes how the **QualitativeSpecies** referenced by the **Input** is affected by the **Transition**. Table 2 shows the possible values with the interpretation of each value.

TransitionInputEffect	Interpretation			
none consumption	Neither the level nor the symbol associated with the qualitativeSpecies is modified.  The level of the qualitativeSpecies is decreased by the resultLevel of the selected term possibly modified by the thresholdLevel of the Input.			

Table 2: Interpretation of the transitionEffect attribute on an Input.

The following example illustrate the interpretation of the transitionEffect attribute. In the case of qualitativeSpecies "A" the level is unaltered by the 'Transition. However the level of qualitativeSpecies "B" is reduced by resultLevel from the whichever FunctionTerm is applicable (see Section 3.6.5

## TODO: An example of a resultLevel modified by a thresholdLevel

#### The sign attribute

The **sign** of type **sign** can be used as an indication as to whether the contribution of this input is positive, negative, or both. The sign is usually used for visualization purposes only. This attribute is optional.

## 3.6.2 The Output class

The **ListOfOutputs** contains at least one **Output**. Each **Output** refers to a **QualitativeSpecies** that participates in the corresponding **Transition**.

The id attribute

An **Output** element has an optional **id** attribute of type **SId**.

The name attribute

There is an optional name attribute of type string that should be used in the same manner as on SBML Level 3 Core objects; see Section 3.3.2 of the SBML Level 3 Version 1 Core specification for more information.

#### The qualitativeSpecies attribute

The required attribute qualitativeSpecies, of type SIdRef, is used to identify the QualitativeSpecies that is the *output* of this Transition. The attribute's value must be the identifier of an existing QualitativeSpecies object in the model. This attribute is comparable with the species attribute on the SpeciesReference element.

#### The outputLevel attribute

The outputLevel is an integer used along with the transitionEffect set to production to specify the effect of the Transition on the corresponding QualitativeSpecies. This attribute is optional. Question: This contradicts the table

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#### The transitionEffect attribute

Each **Output** has a required attribute **transitionEffect** of type **transitionOutputEffect** which describes how the **QualitativeSpecies** referenced by the **Output** is affected by the **Transition**. Table 3 shows the possible values with the interpretation of each value.

TransitionInputEffect	Interpretation
production	The level of the qualitativeSpecies is increased by the resultLevel of the selected term possibly
	modified by the thresholdLevel of the Output.
assignmentLevel	The level of the qualitativeSpecies is set to the resultLevel of the selected term.
assignmentSymbol	The symbol of the qualitativeSpecies is set to the resultSymbol of the selected term.

Table 3: Interpretation of the transitionEffect attribute on an Output.

## 3.6.3 The ListOfFunctionTerms class

The **ListOfFunctionTerms** may contain any number of **FunctionTerm** elements, and exactly one **DefaultTerm**. Each **FunctionTerm** encodes the conditions under which this term is selected. The **DefaultTerm** describes the results of the **Transition** applied by default. The disjunction of the terms defines the *qualitative function* associated with a **Transition**.

#### 3.6.4 The DefaultTerm class

The **DefaultTerm** defines the default result of a **Transition**.

#### The resultLevel and resultSymbol attributes

The default result is described by a **resultLevel** or a **resultSymbol**. Both are optional, but one of them must be defined.

The resultLevel is an integer describing a level. The resultSymbol is a SIdRef referring to a Symbolic Value.

Question: Can both be defined?

Question: Again, should the symbol refer to a symbolic Value from the qualitative Species

#### 3.6.5 The FunctionTerm class

Each **FunctionTerm** is also associated with a result (symbolic or level) and in addition to a Boolean function inside a **Math** element that can be used to set the conditions under which this term is selected.

#### The resultLevel and resultSymbol attributes

The result of the term is described by a **resultLevel** or a **resultSymbol**. Both are optional, but one of them must be defined.

The resultLevel is an integer describing a level. The resultSymbol is a SIdRef referring to a SymbolicValue.

#### The Math element:

Each **FunctionTerm** holds a Boolean function encoded in a **Math** element, using the subset of MathML 2.0 as defined in SBML L3v1 Section 3.4.6. This element encodes the conditions under which the **FunctionTerm** is selected.

## The temporisationValue attribute and the TemporisationMath element:

The attribute temporisationValue and the element TemporisationMath allow the specification of the "temporisation" of the Transition under the corresponding FunctionTerm. Both are optional. Depending on the value of the temporisationType, either one or both could be used.

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# 4 Examples

# 4.1 Graphical and typographical conventions

As this proposal covers various formalisms, the examples are labeled with a token indicating the corresponding formalism: All all formalisms, PN Petri nets, LRG logical regulatory networks or SYM symbolic relationships.

# Simple Logical Regulatory Graph

**LRG** The following example shows a simple LRG with 3 regulators A, B and C, where A can take three values  $(A = \{0,1,2\})$ , and B,C are Boolean. The logical functions are the following: B := 1 if  $A \ge 1$ , C := 1 if  $B \ge 1$ , A := 2 if  $A \ge 1$  and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A < 1 and A < 2 or  $A \ge 1$ ; A := 1 if A < 1 and A <

Listing 1: Logical Regulatory Graph example

```
<?xml version="1.0" encoding="UTF8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1" level="3" version="1" xmlns:qual="http://www.sbml.org/sbml/level</pre>
 <model id="example">
    <listOfCompartments>
      <compartment id="cytosol" name="cytosol"/>
      <compartment id="nucleus" name="nucleus"/>
    </listOfCompartments>
    <qual:listOfQualitativeSpecies xmlns="http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Qualitative_Models">
      <qualitativeSpecies id="A" maxLevel="2" compartment="cytosol"/>
      <qualitativeSpecies id="B" maxLevel="1" compartment="cytosol"/>
      <qualitativeSpecies id="C" maxLevel="1" compartment="nucleus"/>
    </qual:listOfQualitativeSpecies>
    <qual:listOfTransitions xmlns="http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Qualitative_Models"
      <transition id="tr_B">
        t0fInputs>
          <input id="theta_B_A" qualitativeSpecies="A" thresholdLevel="1" transitionEffect="none" sboTerm="\SBO:0000170</pre>
        </listOfInputs>
        tofOutputs>
          <output qualitativeSpecies="B" transitionEffect="assignmentLevel"/>
        </list0f0utputs>
        <listOfFunctionTerms>
          <functionTerm resultLevel="1">
            <math> <!-- A >= 1-->
              <apply>
                <geq/>
                <ci>A</ci>
                <ci>theta_B_A</ci>
              </apply>
            </functionTerm>
          <defaultTerm resultLevel="0"/>
        </listOfFunctionTerms>
      </transition>
      <transition id="tr_A">
        t0fInputs>
          <input id="theta_A_A1" qualitativeSpecies="A" thresholdLevel="1" transitionEffect="none" sbdTerm=5'SB0:00001</pre>
          <input id="theta_A_A2" qualitativeSpecies="A" thresholdLevel="2" transitionEffect="none" sboTerm=%"SBO:00001</pre>
          <input id="theta_A_C" qualitativeSpecies="C" thresholdLevel="1" transitionEffect="none" sboTerm="4SBO:0000170"</pre>
        </listOfInputs>
        tofOutputs>
          <output qualitativeSpecies="A" transitionEffect="assignmentLevel"/>
```

```
<listOfFunctionTerms>
     <functionTerm resultLevel="2">
       <math> <! -- (A >= 1 and A < 2) or C < 1 -->
       <apply>
         <or/>
         <apply>
           <and/>
           <apply>
             <geq/>
             <ci>A</ci>
            <ci>theta_A_A1</ci>
           </apply>
           <apply>
             <lt/>
             <ci>A</ci>
             <ci>theta_A_A2</ci>
           </apply>
         </apply>
         <apply>
           <lt/>
           <ci><ci><</ci>
           <ci>theta_A_C</ci>
                                                                                                           22
         </apply>
                                                                                                           23
       </apply>
     </functionTerm>
   <functionTerm resultLevel="1">
     < math > < ! -- A < 1 and C >= 1 -->
       <apply>
         <and/>
         <apply>
          \langle lt/ \rangle
           <ci>A</ci>
           <ci>theta_A_A</ci>
         </apply>
         <apply>
           <geq/>
                                                                                                           37
           <ci><ci><</ci>
           <ci>theta_A_C</ci>
         </apply>
       </apply>
     </functionTerm>
                                                                                                           43
   <defaultTerm resultLevel="0"/>
 </listOfFunctionTerms>
                                                                                                           45
</transition>
<transition id="tr_C">
 <listOfInputs>
   <input id="theta_C_B" qualitativeSpecies="B" thresholdLevel="1" transitionEffect="none" sboTerm="SB0:0000169'</pre>
 </listOfInputs>
 tofOutputs>
   <output qualitativeSpecies="C" transitionEffect="assignmentLevel"/>
 </list0f0utputs>
 <listOfFunctionTerms>
   <functionTerm resultLevel="1">
     <math> <!-- B >= 1 -->
       <apply>
         <geq/>
         <ci>B</ci>
```

# Simple Petri net

**PN** The following example shows a simple Petri net, containing 4 places A, B, C and D with one transition t1.

Listing 2: Petri net example

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level3/version1" level="3" version="1" xmlns:qual="http://www.sbml.org/sbml/level</pre>
 <model id="PN_exemple">
                                                                                                            17
    <listOfCompartments>
                                                                                                            18
      <compartment id="default" />
                                                                                                            19
    </listOfCompartments>
    <qual:listOfQualitativeSpecies xmlns="http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Qualitative_Models">
      <qualitativeSpecies id="A" compartment="default" initialLevel="2" />
      <qualitativeSpecies id="B" compartment="default" initialLevel="4" />
                                                                                                            23
      <qualitativeSpecies id="C" compartment="default" initialLevel="2" />
                                                                                                            24
      <qualitativeSpecies id="D" compartment="default" initialLevel="3" />
                                                                                                            25
    </qual:listOfQualitativeSpecies>
    <qual:listOfTransitions xmlns="http://sbml.org/Community/Wiki/SBML_Level_3_Proposals/Qualitative_Models">
      <transition id="t1">
        listOfInputs>
          <input id="t1_A" qualitativeSpecies="A" thresholdLevel="2" transitionEffect="consumption" />
                                                                                                            30
          <input id="t1_B" qualitativeSpecies="B" thresholdLevel="1" transitionEffect="consumption" />
        </listOfInputs>
        tofOutputs>
          <output qualitativeSpecies="C" level="1" transitionEffect="production" />
          <output qualitativeSpecies="D" level="2" transitionEffect="production" />
        </list0f0utputs>
        <listOfFunctionTerms>
          <functionTerm result="1">
                                                                                                            38
            <math> <! -- A >= 2 and B >= 1 -->
              <apply>
                <and />
                <apply>
                  <geq />
                                                                                                            43
                  <ci>A</ci>
                  <ci>t1_A</ci>
                </apply>
                <apply>
                  <geq />
                  <ci>A</ci>
                  <ci>t1_B</ci>
                </apply>
              </apply>
            </functionTerm>
```

# 5 Best practices

All To be valid, the SBML root element must express the requirement of this package: <sbml ... qual:required="true" ... >.

**PN** In Petri nets the initial conditions are part of the model, the initialLevel must be defined. To represent unbounded places, the maxLevel should be not specified.

**LRG** Discussions are still ongoing about the possible (but some times convenient to avoid cumbersome descriptions) incoherency of the **FunctionTerm** elements. For the moment, here are the guidelines to ensure coherent definitions:

- The **FunctionTerm** elements of all the transitions targeting the same output should be "coherent": the conditions of two **FunctionTerm** elements, leading to different effects on the level/symbol of the output, should not be fulfilled at the same time (i.e. they should be exclusive).
- If several **FunctionTerm** elements lead to the same effect on the level/symbol of the same output, then the importing tool should consider the disjunction (OR) on the conditions of the terms.

**LRG** To declare external nodes (ones that have no Boolean expression/truth table associated with them), one should set the attribute boundaryCondition of the **QualitativeSpecies** to TRUE:

**LRG** To declare a "delay" node, which is specified to delay its state update for k iterations, one should set, for all the **Transition** elements having this node as their (unique) output, the attribute temporisation Type to the value timer and the temporisation Value to k.

**LRG** To declare a "sustain" node, which is specified to sustain (i.e., to remain in) its latest state for the next k iterations, one should set, for all the **Transition** elements having this node as their (unique) output, the attribute temporisationType to the value sustain and the temporisationValue to k.

# **Validation of SBML documents** Α

Acknowledgments			