In this lecture, we will present a powerful heuristic approach for deriving many of the exact results we have discussed so for

=> may seem slappy or arbitrary @ first, but w/ practice, can be done in way that teaps track of approximations in controlled manner, white highlighting trey physical intuition.

=> enables progress in more complicated settings where exact results are rol aboravailable.

Start by returning to Gaussian random walk: $d_{+} x = \mu + \sqrt{\sigma^{2}} \eta(4) \implies x(t) = \mu t + \sqrt{\sigma^{2}} + Z$

=> when are stochastic vs. deterministic effects dominant?

* since deterministic contribution at

stochastic contribution at

=> stochastic tem always dominant at short t.

deterministic tem always dominant @ long t.

(7)

. Now we return to our evolution problem:

$$\frac{4}{12} = 22 + \sqrt{\frac{h}{2}} N(1) \implies 2(++8+) = 2(++) + 22(+) + \sqrt{\frac{h}{24+}} + 57$$

=> can't apply same approach because det and stoch terms both depend on 5(4), which influenced by del and stoch terms, etc., etc.

=> need to integrate SDE (monent egs, gen fines, etc.) => Hard!

Heuristics = way to do this approximately = "poor man's integration" or "Euler's medial for analytical sol'ns"

Idea: if interested in logarithmic precision [i.e., $\log(x(t)) \pm O(1)$] short time approx contributed $f(\Delta t) = f(0) + 5f(0) \Delta t + \sqrt{5000} \approx 7$ works prelly well until $\log f(\Delta t) \simeq \log(f(0)) \pm O(1)$, since this is who $\Delta f_{sel} = \Delta f_{diff}$ short to donate by O(1) factors.

=> call this time Δt_{nset} occurs when $\log(\Delta x) = \log x \pm O(1)$ [" $\Delta x \sim x$ "]

At this point, set $f(0) = f(\Delta t_{resot})$ and repeal enline process,...

Therefore method for building up f(1) for $+ > \Delta t_{resot}$.

Question then becomes: Are deterministic forces (selection) or stochastic forces (drift) dominant on timescales ~ Atreset?

- Approach: gress & check (self-consistency)
- (1) if deterministic forces dominant ($\Delta f_{sel} \gg \Delta f_{drift}$),

 must have $f \sim |\Delta f_{sel}| \sim |shf\Delta f_{reset}| = \int \Delta f_{reset} \sim T_{sel} = \frac{1}{|s|}$ (really, $\Delta f_{reset} \approx \frac{c_1}{|s|}$ for O(1) const c_1)

on this timescale, contribution from drift is

| Affaitt | ~ [FAtroset ~ [F => | Affaitt | « | Affaitt | » | NISI |

| Selection diminunt

After k resets, have O(1) = O(1) =

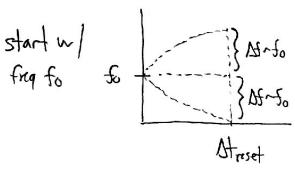
2) If stochastic forces dominant (Afaith) Afsel) then

for | Afaith| ~ (\frac{

So Afselec Afdrift when | fee /NISI (drill dominates)

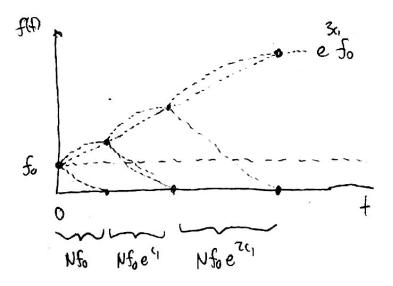
=) in this case, behavior is not as simple as so unbinsed random walk since diffusion coefficient depoids on f(+).

=> but can still understand behavior by gluing together serval iterated random walks.



After Atresed gens, f(t) = fo + fo =) decent & chance of going oxlind! w/ prob ≈ e - (1 - 0(1) factor [e.s. 1/2] mulation is not extinct and must have size 5 = 50/2-4= e 50

then process repeats itself starting from f(0) = e fo:



can see that after k iterations:

* probability of surinal 15 Pourinal = e cik

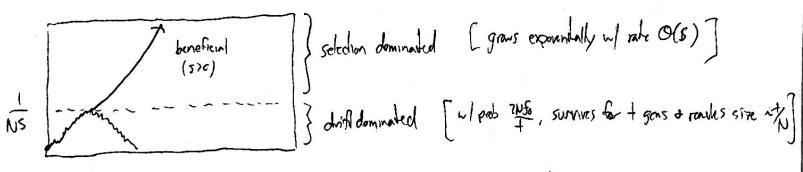
* size is f(+)≈freqk

* total time elapsed is + Nfo+ Nfe+ ... + Nfe (k = e -1) ~Hse (k>1)

Rewriting in terms of t: * survival probability is
$$\approx \frac{N50}{1} \cdot c$$

* size is $541 \approx \frac{c \cdot t}{N}$

- =) i.e. w/ probability ~ $\frac{VE}{T}$, survives for t gens a reaches size ~ tN
- =) attendirely, in toms of final size f(t)=f: w/ probability 50/f, dofts to size >f on timescale t-Nf gens.
- * Heuristic approach pretends that division between drift dominated & sel dominated is infinitely shap, and can part 2 regimes together (note: # asymptotic mertching) =) Incurs O(1) errors in log f(t) a +, but that's w/in our dolerance anyway.



- (1) For beneficial mut (570), dotts to size ~ \(\text{NS } \times \) prob ~ \(\frac{\tilde{k}}{\tilde{k}\tilde{S}} \) ~ 5, takes \(\tilde{S} \) gens to do 50.
- 2) deletions mul (sco), drills to size ~ Was w/ prob ~ IsI, but can't grow any higher =) prob of surviving another 151 gens is me =) psurvive(+)-151e -151e
- (3) Newlal mulations book like triangles ~ height to, width (+, ~ prob plt) = 42