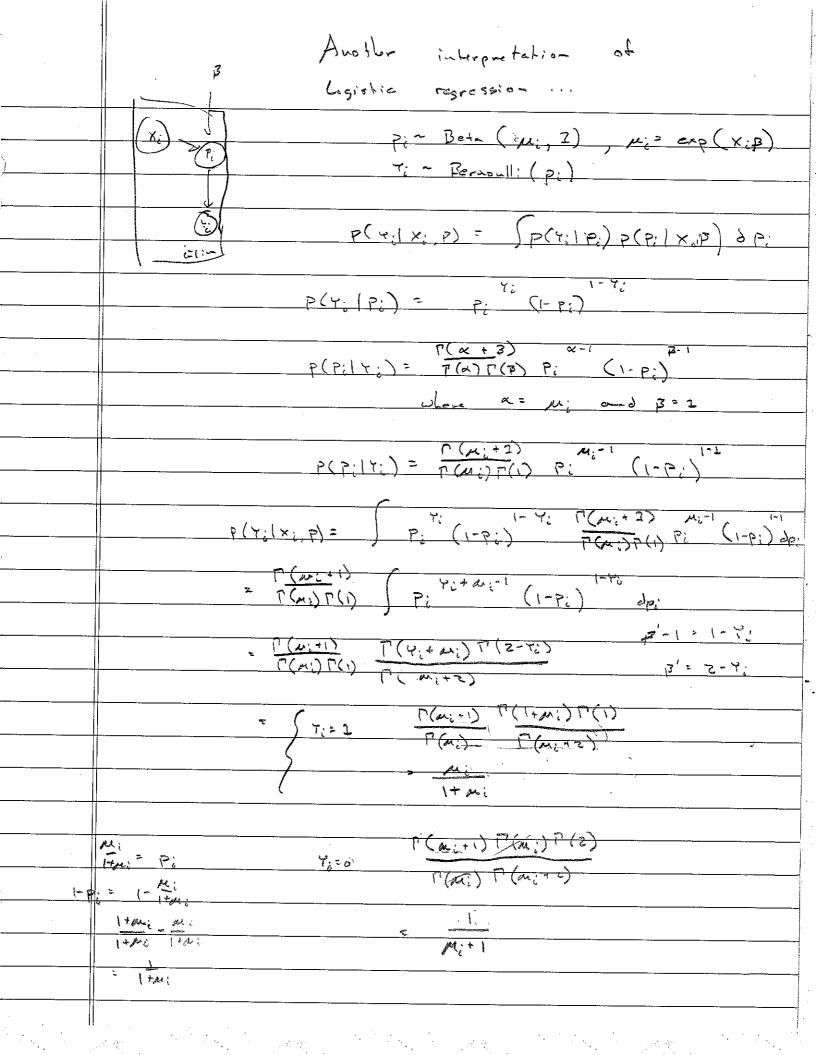
Generalized linear Models Main point: Y = X13 potentially in-appropriate - O Y not co-tinuoe) I not limearly irelated to X c-1/or 13 a) what about transformations b) GLM's -ove (lexible Ex-ples 11: probability of default lelection el: orteures of sae Another exemple log T = XB

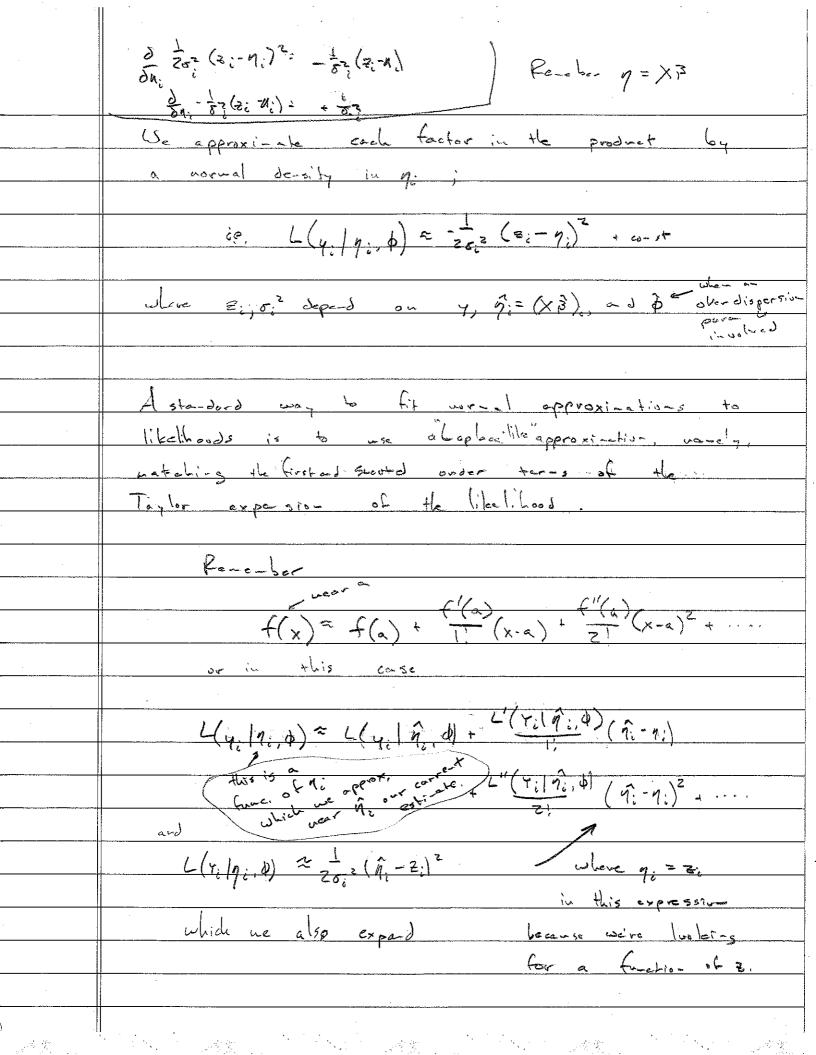
6LM recipe: 1) Linear predictor 7 = X13 2) Link Function g(.) that relates the linear prediction to the we of the ortcore voriable μ= 5 (η) = 5 (XB) 3) The rando- co-ponent specy fying the distribution of the ortcome voriable y with mean E (y | X) = m In general the dist of y way dependen a dispersion paran d I.E. E[Y|X] = 5"(XR) where X = u The likelihood of the data (XB): being the ith linear predictor is given by P(Y | X, B, a) = TT P(Y: | (XB); b) The most common likelihoods, Paisson and Binomial do not use dispersion parama

<u>Co-timers</u>	
1) Nor-	fune g(u) = u = g'(u).
vor	Il positive contact une can use the
05	Games or Weibull.
i I	data!
y Pois	ries celled the Poisson agression
- vo ele	
	Assue y m - Poisso- (m)
	ie. p(Y/w) = +1 / - / -
A link	Common (but not necessarily ideal)  function is log(), ie x
	1003 100 100 100 100 100 100 100 100 100
	likelihood of the data is the
	P(7/3) = TT +: 1 @ (exp(7:))
wle	re y:= (XB); is as before.
Ca- least-	de Boyes extination, ML of

Bi-any or Probability data  Suppose that you Bin (night) with ni larous
Then P(4/B) = TT (4:) Mi (1-Mi)
Where Mi west be between 0 and I.
Let g(mi) = log (mi/(1-mi)) = logit transfor-
Let $g(u_i) = log(m_i/(1-m_i)) \leftarrow logit transfor-$ the $g'(0) = exp(0)$ $logitie$ $logitie$ $logitie$ $logitie$
g-'(g(mi)): exp(log(mi)(-mi)))
- 1-mi - mi - mi - mi - mi - mi - mi - m
Pc-e-b-r u = g-1(y) = g-1(XB)
$e \times p(x \neq y)$ $(+e \times p(x, \neq y))$ $a = d$
 1-m; = 1+ exp(-xB)



5. P(T|X,P) = [[ P(T:|X:|B) = II (I+m;) (I+m;)  $= \underbrace{\frac{e^{x_i p}}{(e^{x_i p})^{T_i}}}_{E_i} \underbrace{\frac{e^{x_i p}}{(e^{x_i p})^{T_i}}}_{C_i}$ We am do gradient ascent directly on 13 by taking derivatives and doing gradient ascent. Since ordinary linear regression is very forst it makes sense to use related computational bols to fit the rodel (ie learn B). If we write the joint  $p(\hat{\gamma} \mid \gamma, \phi) = p(\gamma, \dots, \gamma_n \mid \gamma, \phi) = \frac{n}{11} p(\gamma_i \mid \gamma_i, \phi)$ = T) exp(L(yi/7i, d)) Where L is the log likelihood function for the judicidual observations.



$$z_{\sigma_{i}} = (\hat{q}_{i} - \hat{z}_{i})^{2} = z_{\sigma_{i}} = (\hat{q}_{i} - \hat{z}_{i})^{2} + z_{\sigma_{i}} = (\hat{z}_{i} - \hat{z}_{i})^{2} + z_{\sigma_{i}} = (\hat{z}_{i} - \hat{z}_{i})^{2} + z_{\sigma$$

Example - Bernoulli logistic L(4:14:) = 4: log (en:) + (1-4:) log (1+en:) = Y: N: - Y: (og (1+e "i) + (1-Y:) log 1 = Ti y: - log (1+e"i) Now L' as L' co- be comprted and used to solve for z; adogs And in turn to iteratively solve for model