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**Algorithm 1** Particle Filter

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1: Initialize  $K$  particles  $\{\{R^k = \emptyset, w^k = \frac{1}{K}\}\}_{k=1}^K$ 
2: Initialize  $\mathbf{u} = []$ 
3: while true do
4:    $x \leftarrow \text{NextObservation}()$ 
5:    $\mathbf{u} \leftarrow \mathbf{u}x$ 
6:   for all  $k = 1, \dots, K$  do
7:     if  $|R^k| > \text{maxRestaurants} - 2$  then
8:        $R_{\mathbf{d}}^k \leftarrow \text{ProposeRestaurantToDelete}()$ 
9:        $R^k \leftarrow R^k \setminus R_{\mathbf{d}}^k$ 
10:    end if
11:     $\{R_{\mathbf{u}}^k, R_{\pi(\mathbf{u})}^k, \dots, R_{[]}^k\} \leftarrow \text{FindRestaurant}(\mathbf{u})$ 
12:     $\mathbf{P}^k \leftarrow \{R_{\mathbf{u}}^k, R_{\pi(\mathbf{u})}^k, \dots, R_{[]}^k\}$ 
13:     $R^k \leftarrow R^k \cup \mathbf{P}^k$ 
14:     $v^k \leftarrow \text{Seat}(x, \mathbf{P}^k)$ 
15:     $w^k \leftarrow v^k w^k$ 
16:  end for
17:  # resample particles
18:  # predict
19: end while
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$$\begin{aligned}\mathcal{G}_1|d_1, c_1, \mathcal{G}_0 &\sim \mathcal{PY}(d_1, c_1, \mathcal{G}_0) \\ \mathcal{G}_2|d_2, c_2, \mathcal{G}_1 &\sim \mathcal{PY}(d_2, c_2, \mathcal{G}_1) \\ \theta_i|\mathcal{G}_2 &\sim \mathcal{G}_2 \quad i = 1, \dots, N.\end{aligned}$$

$$\begin{aligned}\mathcal{G}_1^t|d_1, c_1, \mathcal{G}_0 &\sim \mathcal{PY}(d_1, d_2, \mathcal{G}_0) \\ \mathcal{G}_2^t|d_2, c_2, \mathcal{G}_1^t &\sim \mathcal{PY}(d_2, c_2, \mathcal{G}_1^t), \quad t = 1, \dots, T \\ \theta_i^t|\mathcal{G}_2^t &\sim \mathcal{G}_2^t, \quad i = 1, \dots, N_t\end{aligned}$$

$$\begin{aligned}\mathcal{G}_{[]}^n|\mathcal{U}_{\Sigma}, d_0 &\sim \mathcal{PY}(d_0, 0, \mathcal{U}_{\Sigma}) \\ \mathcal{G}_{\mathbf{u}}^n|\mathcal{G}_{\sigma(\mathbf{u})}^n, d_{|\mathbf{u}|} &\sim \mathcal{PY}(d_{|\mathbf{u}|}, 0, \mathcal{G}_{\sigma(\mathbf{u})}^n) \quad \forall \mathbf{u} \in \Sigma^+ \\ \theta_n|\theta_{n-1} \dots \theta_1 = \mathbf{u} &\sim \mathcal{G}_{\mathbf{u}}^n\end{aligned}$$

where  $\mathcal{U}_{\Sigma}$  is a uniform distribution over the set of symbols,  $\mathbf{u}$  is a particular context,  $\Sigma^+$  is the set of all such contexts, and  $\sigma(\mathbf{u})$  is the context  $\mathbf{u}$  modified by removing the most distant symbol. We assume  $|\Sigma| < \infty$ .