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# Chapter 1

## Introduction

### 1.1 Drug Development

#### 1.1.1 Costs of Drug Development

The process of bringing new drugs to market is a long and expensive affair. Information about both the costs and time necessary to bring a drug to clinical trials are less available than statistics for drug molecules reaching clinical trials. There is much debate over the average cost and time investment needed to develop a new drug. At the least it is necessary to identify a possible target molecule, find a small molecule with promising binding characteristics to that target which is additionally not toxic nor a strong binder to the wide variety of other proteins necessary for regular cellular function. These small molecules are then varied to maximize binding affinity to the target molecule, while attempting to simultaneously minimize cross reactivity. Finally, after this process, these drug compounds are rigorously tested through clinical trials. The final costs necessary for this process range from 400 million per new chemical entity to as much as 2 billion. Estimates for the time required also vary significantly, but many estimates place the time required at around 10 years from target identification to an approved drug. One of the largest factors affecting the average cost of each new drug compound is the low success rate for compounds which have been under active research for a number of years. Effectively screening these compounds earlier in the pipeline has the potential to significantly decrease the average cost of each new drug molecule. [Adams and Brantner, 2006]

The average cost of identifying a new drug molecule and gaining approval for that molecule is actually growing at a rate greater than inflation. The number of new drugs introduced during the period 2005-2010 was actually 50% fewer than the number introduced during the time frame from 2000-2005. New drug compounds have been shown to have important impacts on both longevity and quality of life. In fact, during the 14 year period from 1986 to 2000, 40% of the two year increase in life expectancy can be accounted for by the effect of new drugs introduced during that period. [Paul et al., 2010]

The expected period of time that a candidate drug compound will spend in clinical trials is approximately nine to fourteen years[DiMasi et al., 2003; Paul et al., 2010]. During the period from 1981 to 1990 the rate of approval of potential drugs decreased, as did that of self-originated drugs, or those drugs which were originally identified by a pharmaceutical research company. Of potential drug compounds which reach clinical trials, only 10% will finally be approved as new drugs [DiMasi, 2001; Paul et al., 2010]. Of potential drug compounds entering clinical trials that fail to be approved as new drugs, approximately two thirds will be abandoned or fail during phase II clinical trials, which test the efficacy of a drug. This is generally viewed as a failure to find a small molecule with sufficiently high binding affinity to the target protein. Thirty percent of potential drug compounds entering clinical trials will fail in stage I, either because they are poorly tolerated, toxic to humans or cause side effects. Each of these is a potential indicator of cross reactivity with proteins other than the target molecule.

Computationally screening these compounds earlier in the process has the potential of reducing the attrition rate at this point in the process. Additionally, increasing the affinity for the target itself can allow for lower dosages which can increase survival through phase II clinical studies. Finally, approximately 20% of potential drug compounds entering clinical trials will fail in stage III. These drugs fail for a variety of reasons, though ineffectiveness is frequently cited as a reason. All told efficacy accounts for 37.6% of all drugs that are abandoned after reaching clinical trials, making it the single largest contributing factor to the failure of these compounds to eventually receive approval as new drugs. Other factors include saftey, and economics. [DiMasi, 2001]

For new chemical entities introduced in the 1990's the cost of research and development increasing at a rate 7.4% above inflation. Rates for the 2000's are not yet available or are only now becoming available due to the long lead time between introduction of a new chemical entity and that new chemical entity becoming an approved drug. During the period from 1985 to 2000 the rate of spending on research and development increased at approximately twice the rate of introduction of new chemical entities. Although the largest factors in determining this cost are the costs during clinical trials significant amounts are also spent earlier in the drug discovery pipeline, such as target identification, lead identification, and lead optimization. Improved computational techniques are generally viewed as possible means of decreasing costs or times associated with the earlier steps in the process. However, by increasing the fraction of leads which survive the screening process techniques which help identify and optimize lead molecules can have a very large effect on the cost of each new molecular entity. Clinical trials consist of six sometimes overlapping stages, denoted 0 to V, though stages I to III are where the majority of drug molecules are abandoned. Of the candidate compounds which enter clinical trials only approximately 20% will finally be approved as drugs. [DiMasi et al., 2003]

Since 1950, the number of new chemical entities introduced per billion dollars has decreased by 50% every 9 years. Possible problems cited as contributing to this decrease in efficiency include:

- 1. the ready availability of high quality and effective generic drugs as treatment options for many diseases,
- 2. decreased risk tolerance among regulatory agencies,
- 3. increased spending and personnel without understanding underlying relationships between spending and personnel and discovery of new compounds, and the long period of time between beginning research on a drug target and finally gaining approval for a new drug compound, and
- systematic overestimation of the efficacy of high throughput screening techniques relative more classical techniques such as clinical science, and animal screening [Scannell et al., 2012].

The high failure rates during clinical trials have been identified as one of the most critical factors in determining the overall costs of drug development. [Bleicher et al., 2003]

#### 1.1.2 Computer Assisted Drug Design

The ultimate goal of computer assisted drug design is to improve rational drug design by exploiting the continuously increasing processing power available both in high performance super computers, but also in single workstations. Seeking to supplement the ability of a researcher either by allowing examination of a large number of possible interactions quickly or providing some insight that might be much more difficult to obtain through biochemical experiments, both in terms of time and expense. Different classes of programs have been developed to help solve each of the distinct steps in the pre-clinical stages of drug development, namely:

- 1. Hit Identification the process of screening a large small molecule database (up to one million or more small molecules) database to identify small molecules which bind a given target protein, or hits. These hits are usually small molecules with a target binding affinity on the order of micromolar.
- 2. Hit to lead optimization the process of modifying these "hit" molecules either by substitution or addition of chemical moieties or mixing and matching substructures between given hits, to produce compounds with higher binding affinities than the initial hit compounds. Hit to lead optimization seeks to improve the micromolar binding affinity of hit compounds to nanomolar affinity or better.
- 3. Lead Optimization the final step of modifying lead compounds to increase "druglikeness" to ensure that the molecule is sufficiently soluble, well tolerated, and does not disrupt regular cellular function.

#### 1.1.2.1 Hit Identification

The earliest form of hit identification experiments were animal screens, where mutant animals were studied to find the specific gene or protein causing a specific phenotype. This type of experiment relies on careful genetic controls and breeding, but also some element of luck in observing a relevant phenotype in the first place. "Brute force" animal screens have since been improved with extensive mutation libraries and exhaustive non-lethal mutation libraries for organisms such as yeast and Escherichia coli. Even so, these screens are slow, often taking three years or longer, and error prone, as performing a large number of repetitive experiments causes even the most fastidious of scientists to lose focus. High-throughput screening seeks to supplement the human factor with robots, which are capable of performing similar experiments with greater speed and fewer errors. With the help of this automation it is possible to test the interactions of as many as 100 million different reactions per day [Agresti et al., 2010]. Though the high initial cost of high-throughput screening equipment as well as the cost of the small molecule libraries necessary for screening are often prohibitive even to large research institutions. In order to make this sort of experiment available to a larger number of institutions some research institutions have instituted means of sharing this equipment, through high-throughput screening as a service type arrangements [HTSRC, 2004; MSSR, 2006].

The direct computational equivalent to high-throughput screening is virtual screening, where a library of small molecules is computational "docked" into the active site of the target protein, and some scoring metric is used to identify possible binders. In this sort of computational screen, he problem of the cost of small molecule libraries is essentially a solved problem in virtual screening as there are readily available libraries of drug-like small molecules for use in virtual screening programs. For example, the ZINC database provides a library of over seven-hundred thousand commercially available small molecules in a number of different file formats for use in virtual screening [Irwin and Shoichet, 2005]. Another possibility for hit identification in silico is through fragment assembly methods.

The first published study using computational docking was published in 1982 by Irwin Kuntz describing a program which would later go on to become the well known DOCK program [Kuntz et al., 1982]. Generally docking consists of a method of quickly screening possible protein-small-molecule interaction conformations. An emphasis is placed on the computational cost of evaluating the energy function over accuracy, as the poses generated by this step are usually fed into structural refinement programs for further sampling and

more accurate estimation of energies. For example in the original Kuntz study, the system only only had six degrees of freedom on which to sample, three translational and three rotational degrees of freedom for the ligand with the protein held fixed. Along with a hard sphere collision model this provided a sufficiently selective screen to identify the native binding geometry of the heme group to myoglobin as well as thyroid hormone analogs to prealbumin [Kuntz et al., 1982].

The rate at which new structures are being deposited into the Protein Data Bank is increasing on an annual basis. But tools are necessary to draw meaningful insights from this data, hopefully leading to new drugs.

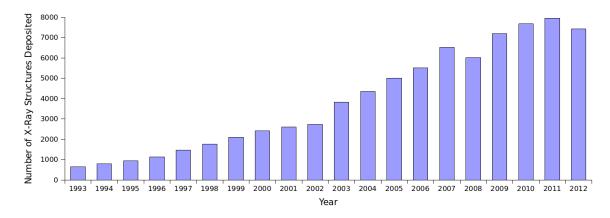


Figure 1.1: The rate at which new structures is deposited into the PDB over the last two decades. Due to a variety of improvements in the field of crystallography this rate has been steadily increasing.

For example a recent increase in the field of crystallography, is "crystal-less" crystallography in which small molecules are bound by a porous scaffold matrix. The regular structure of the matrix imparts a regular packing arrangement, necessary for interpreting diffraction patterns, onto the arrangement of small molecules. This has the potential to address one of the largest difficulties in obtaining quality structural data for proteins, which is that it is very difficult to purify and crystallize certain proteins [Inokuma et al., 2013].

The number of target molecules of the set of all drugs currently available on the market consists of only about 500 proteins. The bottleneck in introduction of new chemical entities

is not virtual screening, but rather optimizing these hits into higher affinity leads and eventually balancing the requirements across all characteristics to produce a new drug [Bleicher et al., 2003].

Of the total proteome only 30,000 are regulated by small molecule binding, making them reasonable targets of drug action. A large number of these possible drug targets are not implicated in any disease, due to this and a number of other factors, estimates of the total number of these proteins which are possible drug targets is much lower. Frequently cited numbers for the number of possible drug targets in humans are six-hundred to fifteen-hundred, still significantly higher than the total number of targets which are exploited by current drugs. The different families of cellular proteins are not equally likely to be targets of drugs. As of 2013 47% of current drug targets are enzymes, followed by 30% being GPCR's [Hopkins and Groom, 2002].

The consists of a number of characteristics which are generally true of drug like molecules:

- 1. Five or fewer hydrogen bond donors,
- 2. 500 Da or less total molecular mass
- 3. high liphophilicity
- 4. sum of nitrogen and oxygen atoms is not greater than 10 Lipinski et al., 1997

Through understanding the protein-ligand conformation and specific contacts they were able to modify a known substrate There is an advantage to flexible substrates, which is that they can flex in order to create better contacts with the protein structure increasing binding affinity. This is especially important as the location of heavy atoms in the target protein is frequently only known to an accuracy of 0.4 angstroms. Further specific knowledge of the binding geometry between the initial lead compound and the target makes it possible to computationally screen possible chemical group substituents, to maximize binding affinity, increase solubility or bioavailability. One of the earliest examples of the successful application of structure based drug design is the carbonic anhydrase inhibitor dorzolamide, in which most of these ideas were applied to find a drug with very high binding affinity [Greer et al., 1994].

Despite advantages in speed and cost due to limitations in accuracy computational screening has struggled to produce the same results as empirical screening. However, more recently virtual screening has succeeded in producing hit rates greater than those from empirical screening techniques. Virtual screening has been used to identified leads which were later developed into the human immunodeficiency virus (HIV) protease inhibitor Viracept, and the anti-influenza drug Relenza. A number of challenges which limit the utility of

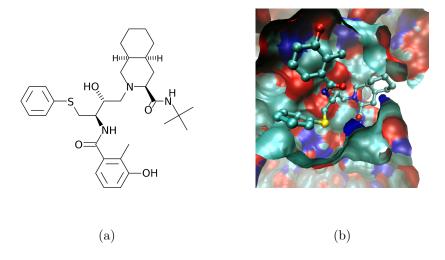


Figure 1.2: The HIV protease inhibitor, nelfinavir, marketed under the name Viracept was originally identified using a computational docking screen. It has a very high binding affinity for its target protein, 2 nM. Here it is shown crystallized with multidrug variant (ACT) (V82T/I84V) of HIV-1 protease, PDBID 3EL5. (b) generated with Visual Molecular Dynamics [Humphrey et al., 1996] and [POVRAY 3.6, 2004].

#### docking programs have been identified

- 1. The number of possible small molecules is essentially unbounded, however only a very small fraction of these ligands are potentially drug compounds. Limiting sampling to this subspace is a challenging problem.
- 2. The number of conformations of ligand molecules rises exponentially with the number of internal degrees of freedom of the ligand. Sampling the huge conformational space of the ligand becomes a computationally difficult problem on its own.
- 3. The difficulty of accurately assessing or comparing the energy of different protein-

ligand complexes or conformations [Shoichet, 2004].

It has been found that introduced drugs are often very chemically similar the "hit" compounds from which they were derived [Proudfoot, 2002]. So in order to increase the diversity of drugs and find drugs which are able to treat new diseases, or diseases which have evolved resistance to current drugs it may be necessary to either increase the size of the screened database or increase the possible diversity which might be increase through the hit-to-lead step.

#### 1.1.2.2 Hit-to-Lead Optimization

Hit compounds generally have a binding affinity for the target protein on the order of micromolar binding. The goals of hit-to-lead optimization are to further increase that affinity with the goal of eventually reaching binding affinities on the order of 10 nanomolar or better, find other molecules with similar chemical characteristics to increase the size and diversity of the set of lead compounds, and screening hit compounds for any obvious issues. At this stage for computational screening more accurate energy models are required than for the initial screen [Jorgensen, 2004; Gohlke and Klebe, 2002; Jorgensen, 2009].

Depending on the type of "hit" compounds identified in the initial screen, hits are either combined through molecular-growing and evolution techniques, or similar structures to the hit compounds can be sampled either by exploring the local chemical space or "mutation" of substituents. In either case, the potential lead compound is docked or grown in the known binding site.

A scoring function which is hopefully well correlated with the binding energy is then used to rank these possible compounds. Interestingly it is not necessarily the case that the scoring function is anchored in a physical force field, it is possible to use statistical or artificial intelligence approaches with success, so long as they are able to successfully solve the classification problem of distinguishing strong binders from weak binders. Docking as a means of converting hit compounds to lead compounds is very similar to docking as a means of hit generation, however in this case the small molecule library is much smaller and is generated to cover chemical space surrounding hit compounds. Additionally whereas for initial hit generation a coarse grained energy function might have been sufficient to

differentiate ligands which bind strongly from those which do not bind at all, to convert these "hits" to lead compounds it is necessary to use a more sensitive, and necessarily slower, energy model to accurately rank the binding affinity of different small molecules [Jorgensen, 2004; Gohlke and Klebe, 2002]. These energy models will be discussed briefly in 1.4.

A popular program for building, or mutating lead compounds is Biochemical and Organic Model Builder (BOMB) [Barreiro et al., 2007]. BOMB can operated as either a hit identification program or as a hit to lead optimization method. Working to identify new compounds BOMB starts with a number of different small "core" scaffolds and attempts to increase binding affinity by adding or replace substituents with favorable interactions while avoiding steric clashes. BOMB has been successfully used to evolve a hit compound which showed no inhibition of HIV reverse transcriptase into a potent non-nucleoside RT inhibitor with nanomolar level binding [Barreiro et al., 2007].

Whereas previously, lead compounds were evaluated almost exclusively on binding affinity to the target protein, more recently more weight is being placed on identifying hit compounds which satisfy other characterisites besides binding affinity [Bleicher et al., 2003]. It is important to begin to consider other characterisites of the potential drugs earlier in the pre-clinical process, because later it is difficult to make changes which affect characterisites such as solubility without significantly altering the binding affinity of an already highly modified hit compound. As "lead" compounds are rarely very chemically distinct from the hits from which they were derived, and increasing binding affinity is actually sometimes an easier problem than addressing some of the other characteristics in the "rule of five" it is reasonable to begin by first trying to optimize hit compounds to satisfy some other criteria and postpone maximizing binding affinity [Proudfoot, 2002].

#### 1.1.2.3 Lead Optimization

In lead optimization the compounds which have been identified by the earlier steps in the process are optimized to drug molecules. The largest differentiating factor between hit-to-lead optimization and lead optimization is the plausibility of the compound to act as a successful drug molecule. The goals of lead optimization overlap heavily with those of the

hit-to-lead stage. Although this can include increasing binding affinity to the target even further, usually the focus is on other characteristics including selectivity, ease of synthesis, pharmacokinetic properties and intellectual property concerns [Keserű and Makara, 2006]. Computational modelling can help not only identify hit compounds, and convert those initial hits into leads, but also to help estimate absorption, distribution, metabolism, elimination, toxicology, sometimes referred to as the ADME characteristics [Kerns and Di, 2008].

Computational models for ADME characteristics ususally use regression equations or neural networks to predict these characteristics [Jorgensen, 2004].

Up to one half of all drugs which do not survive clinical trials, fail to do so because of lack of efficacy, which is influenced both by binding, but also by the absorption characteristics of the molecule. The number of drugs which fail to make it through clinical trials due to toxcicity is similarly high, about 40% [Li, 2001]. Advancing a potential drug to clinical trials represents a very large financial investment, and effective computational screens of lead molecules at this point in the process can reduce the rate of failure in clinical trials, thereby having a very large impact on the final costs of new drugs brought to market.

### 1.2 Sampling Algorithms

#### 1.2.1 Minimization

Minimization techniques seek to find the lowest energy conformation in a given potential well. Generally, they make no attempt to sample outside of that well, and therefore are frequently implemented as a final stage in sampling, in order to relieve any unfavorable interactions in proposed structures. There are a large number of different minimization techniques, and they will not be covered in any real depth here, please see the original papers for more details, or [Schlick, 2010] for a review. As the basic terms of the general molecular mechanics potential energy function are differentiable, and discounting for the moment the significant effects of solvent, it is possible to solve for the energy gradient, or force on every atom for a given conformation. A few minimizations methods include:

1. "Steepest descent", conceptually the simplest minimization algorithm, in which the gradient is calculated at each step, and the size of the step is proportional to the

magnitude of the gradient [Levitt and Lifson, 1969; Bixon and Lifson, 1967].

- 2. "Newton" methods instead of approximating the gradient as a linear function in a small neighborhood, express the gradient, as a quadratic function. This has been shown to converge more quickly than steepest descent [Ponder and Richards, 1987]. Discrete Newton and Quasi-Newton methods use numeric estimation techniques instead of analytically solving for the gradient [Schlick, 2010].
- "Truncated Newton" methods find an approximate solution to Newton's equations, forcing the residual to approach zero as the series converges [Dembo and Steihaug, 1983].

#### 1.2.2 Monte-Carlo Sampling

Metropolis Monte-Carlo simulation was originally developed in the 1950's to provide rapid sampling of the solution space of many variable problems [Metropolis  $et\ al.$ , 1953; Hastings, 1970]. Monte-Carlo techniques generate a sequence of states from a distribution by proposing a new state based only on the current state If the ensemble average is the same as the sequence average, a Monte Carlo Markov chain can be used to estimate ensemble averages, this is known as ergodicicy [Schlick, 2010]. Another requirement is  $detailed\ balance$  that the probability of transition from a state  $X_i$  to a state  $X_{i+1}$  is the same as the probability of the reverse transition, i.e.  $X_{i+1}$  to  $X_i$ . By setting the probability of acceptance to

$$P(x \to x') = min\left(1, e^{-\frac{\Delta E}{k_B T}}\right) \tag{1.1}$$

these conditions are met.

In molecular mechanics, Metropolis Monte Carlo provides a very efficient means of sampling conformation space and a simple method of estimating the distribution of states. Modifications on this method, such as annealing, where the temperature is continuously decreased over the course of the simulation, or umbrella sampling, which attempts to achieve better sampling in cases where a potential energy barrier divides two or more states from each other [Torrie and Valleau, 1977]. While Monte Carlo sampling techniques are very fast to provide new states, the majority of these states reflect higher energy conformations.

Since it is of practical biological interest, Monte Carlo minimization has been developed to increase the rate at which minima are sampled [Li and Scheraga, 1987].

#### 1.2.3 Analytic Loop Closure

Subsequences with regular secondary structures,  $\alpha$ -helices and  $\beta$ -sheets are generally better conserved, and therefore likely to be well covered by simple homology models [Kolodny *et al.*, 2005]. The intervening "random coil" or loop regions often play a large role in determining protein specificity for a specific ligand as in antigen-antibody binding [Bajorath and Sheriff, 1996], small protein toxins to the receptors they target [Wu and Dean, 1996], or transcription factors to specific DNA sequences [Jones *et al.*, 1999].

Loop closure or prediction is a significant part of homology modeling, and building structures consistent with X-ray refraction data. Therefore in order to accurately predict three dimensional structure through homology models, infer the protein binding partners and function, or even build a three dimensional structure consistent with both X-ray data and physical constraints, accurately predicting these loop regions is critical [Fiser et al., 2000].

The question is, given two fixed endpoints and a flexible loop, or actuator, find a conformation of the loop which connects the two endpoints. Because of the similarities that this problem solves with robotics a number of algorithms have been adapted from that field [Kolodny et al., 2005]. The first of these is analytical loop closure, where a conformation which satisfies the closure criteria is solved for directly by solving a system of equations. Though this problem can be solved analytically for small loops [Wedemeyer and Scheraga, 1999; Go and Scheraga, 1970; Bruccoleri and Karplus, 1985; Palmer and Scheraga, 1991], the problem becomes more difficult as loop length grows and the number of degrees of freedom of the loop section increases. Additionally these closure constraints make sampling multiple different conformations more difficult [Cortés and Siméon, 2005], though it is possible to hierarchically solve sub-loops in order to generate conformations for possible loops [Wedemeyer and Scheraga, 1999].

#### 1.2.4 Random Tweak

Random tweak, like CCD is a method of producing and sampling closed loop conformations. It begins in much the same was as CCD, by randomizing  $\phi$  and  $\psi$  dihedral angles. Random tweak seeks to close the loop while retaining dihedral angles as close to the randomized starting structure as possible. By adjusting each dihedral only a small amount at a time and staying in the region where  $sin(\Theta) \approx \Theta$  it is possible to formulate a set of linear equations to solve for a set of  $\Delta\Theta_i$  which minimizes the distance between the crystal position of the atom to be closed and the random position. Because the assumption  $sin(\Theta) \approx \Theta$ , only holds for small  $\Theta$ , the maximum change in angle is limited, 10 degrees in the original implementation. Because almost all structures predicted using the random tweak or cyclic coordinate descent produce closed loops, a much smaller fraction of time is spent sampling loops which do not satisfy the closure criteria, and these algorithms can be very efficient [Fine et al., 1986; Shenkin et al., 1987].

#### 1.2.5 Cyclic Coordinate Descent

Another robotics algorithm which has been successfully applied to protein loop closure is Cyclic Coordinate Descent (CCD) [Canutescu and Dunbrack, 2003]. As the length of a flexible loop grows the number of degrees of freedom increases and the possible solution space grows exponentially. Cyclic coordinate descent seeks to close the loop by adjusting the degrees of freedom, in this case the  $\phi$  and  $\psi$  dihedral angles, sequentially and possibly iterating over each degree of freedom multiple times until the loop is closed. This method is able to solve for conformations very quickly, and the likelyhood of closing a loop increases as the number of degrees of freedom of the system increases. In cyclic coordinate descent the  $\phi$  and  $\psi$  angles of each loop backbone residue are first randomized. Then a loop dihedral is chosen at random, and varied to move the last atom of the loop as near as possible to its desired position. A new dihedral is chosen and optimized until the loop is closed. It is possible that this procedure does not converge to a closed state, however experiments have shown that this is very unlikely even for extended loops with few degrees of freedom, < 2% failure rate for 4 residue loops. Solving for the ideal dihedral angle at each step is a simple optimization problem making CCD a very fast algorithm [Wang and Chen, 1991;

Canutescu and Dunbrack, 2003]. In experiments CCD produces closed loop candidates in 1/6 the time of the random tweak method.

A variation on cyclic coordinate descent seeks to close the loop by not only requiring atom closure, but by requiring that the entire backbone of the closure residue is superimposed, within some geometric similarity tolerance, between the predicted and crystal structure. This constrainint ensures that the angles and dihedrals of the closure residue are reasonable [Canutescu and Dunbrack, 2003].

#### 1.2.6 Rotamer Assembly

Rotamer assembly or systematic search shares some similarity with fragment buildup techniques in that it uses a rotamer library to assemble possible loops. This rotamer library represents the common backbone dihedrals for each amino acid. This method operates by dividing the loop into two pieces, usually in half, and considering all possible half loops which can be built using rotamer library [Moult and James, 1986]. For each side of the loop a "tree" is considered in both a physical sense, that the hemi-loop branches as it grows away from its anchor, and a decision tree sense, in that every residue represents a decision where a single rotamer is selected from the rotamer library. When the hemi-trees for each side of the gap are fully constructed some closure criteria is applied.

In the case of the original systematic search geometric agreement is required of the entire mid-residue [Moult and James, 1986], however a more lax criteria is applied in the case of the PLOP where only one atom is required to be approximately superimposed [Jacobson et al., 2004]. By carefully pruning trees during the building process, and biasing the search towards occupied regions of  $\phi$ - $\psi$  space, systematic search can be quite efficient, spending little time sampling implausible regions of conformation space. Additionally, by building residue pairs, using a smaller possibly restricting the rotamer library by building multiple residues at a time this sort of procedure has been used to build loops of 20+ residues [Zhao et al., 2011].

### 1.3 Molecular Modeling

Molecular modeling seeks to gain new insights into the real world behavior of molecules by mimicking these molecules, usually using computer simulations. According to the theory of "minimal frustration" the protein native state is not only a low energy state, but is also stable [Bryngelson and Wolynes, 1987]. So the prediction of native or native-like conformations focuses on finding those conformations which have a low potential energy. As measuring the true potential energy of a system is very difficult or impossible computational models seek to reproduce the qualitative behavior of the energy surface. Quantum mechanics calculations are often viewed as the gold standard with respect to intramolecular energy calculations. However, despite the accuracy of quantum mechanics, its application to large systems such as proteins is currently limited due to the amount of time necessary to perform quantum mechanics calculations on a large number of atoms. Instead quantum mechanics calculations have been used to parameterize a majority of the most popular molecular mechanics force fields currently in use, including:

- 1. AMBER [Weiner *et al.*, 1984],
- 2. OPLS-AA [Kaminski *et al.*, 1994],
- 3. and CHARMM [MacKerell et al., ].

The earliest molecular mechanics force fields either modeled groups of atoms as a unit, hydrogens being grouped with their bound heavy atom [Jorgensen and Tirado-Rives, 1988], or even each residue as a unit [Lee et al., 1999], both to reduce the number of parameters in the model and to increase the speed of computations. Although ab initio folding experiments are theoretically interesting, they are generally not practical both because of the difficulty in simulating such a large system for the time-frame necessary to observe behaviors like folding, and also because structural models for many proteins are available either directly as X-ray structures, or indirectly through homology.

Because of the evolutionary cost of mis-folded proteins, proteins have been selected to minimize mis-folding, making the general shape of the potential energy surface roughly funnel shaped with the native structure at the minimum [Leopold *et al.*, 1992]. Despite this



Figure 1.3: To an extent it is always possible to either increase accuracy or decrease running time, or the cost of an experiment. New scientific methods should allow one to increase accuracy while not spending additional time.

shape, the energy landscape of proteins is a very "jagged" surface with a large number of local minima [Tsai et al., 1999].

Even the smallest enzyme contains 62 amino acids, and has thousands of degrees of freedom [Chen et al., 1992], and larger enzymes are regularly more than 1000 amino acids. The number of degrees of freedom of these systems make any attempt to analytically solve for a global minimum energy conformation impossible, and require other methods of generating plausible conformations. In order to compensate for this a number of different sampling methods have been developed.

### 1.4 Energy Functions

Some energy models do not seek to accurately rank potential conformations, fast "screening" functions attempt to quickly differentiate physically impossible conformations from plausible conformations without performing an expensive minimization or energy calculation step.

Application of these screening functions has the potential to greatly reduce the number of potential conformations that must be scored using the full detail energy function, greatly decreasing the overall cost of conformation prediction. These screening criteria can be applied either during the sampling procedure, potentially eliminating sampling of a large area of excluded conformation space, or after sampling before a more expensive energy function is applied to rank conformations. Effective screening criteria have a large impact on the total performance of a structure prediction method.

One of the earliest screening criteria was the hard sphere overlap collision detection [Levinthal, 1966], and this method is consistently included in screening scriteria. Other screens include:

- 1. bounds on bond lengths and angles, as a single bond which deviates significantly from equilibrium can dominate the energy of a conformation,
- 2. limitations on  $\phi$ - $\psi$  space occuped by backbone dihedrals corresponding to the Ramachandran plot of the residue,
- 3. limiting side chain dihedrals to staggered conformations, which correspond to the low energy well of side chain dihedral space [Moult and James, 1986],
- 4. excluding structuctures which present excessive solvent accessible surface area, as this conflicts with the hydrophobic effect, which has a large effect on the conformation of the native state [Chothia and Janin, 1975]
- 5. limitations on the number of "dry" cavities, and the number of internal charged residues [Moult and James, 1986]

#### 1.4.1 The General Form of the Energy Model

The general form of most molecular mechanics energy potentials is reasonably consistent, with bonds and angles being modeled as a spring, dihedrals as a Fourier series.

$$E(r^{N}) = E_{\text{bonds}} + E_{\text{angles}} + E_{\text{dihedrals}} + E_{\text{nonbonded}}$$
(1.2)

$$E_{\text{bonds}} = \sum_{\text{bonds}} K_r (r - r_0)^2 \tag{1.3}$$

$$E_{\text{angles}} = \sum_{\text{angles}} k_{\theta} (\theta - \theta_0)^2 \tag{1.4}$$

$$E_{\text{dihedrals}} = \sum_{i=1...4} \frac{V_i}{2} \left[ 1 + \cos \left( i * (\phi - \phi_0) \right) \right]$$
 (1.5)

The non-bonded terms are modeled as a Columbic potential between any point charges and a Lennard-Jones or 6-12 potential between any non-bonded atoms. These non-bonded atoms are phased in by a "fudge factor" for atoms in a 1-4 configuration.

$$E_{\text{nonbonded}} = \sum_{i>j} f_{ij} \left( \frac{q_i q_j e^2}{r_{ij}} + 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] \right)$$

$$f_{ij} = \begin{cases} 0 & \text{if } i \text{ and } j \text{ are separated by 2 or fewer bonds} \\ 0.5 & \text{if } i \text{ and } j \text{ are separated by 3 bonds} \\ 1.0 & \text{otherwise} \end{cases}$$

$$(1.6)$$

Where  $\sigma_{ij} = \sqrt{\sigma_{ii}\sigma_{jj}}$  and  $\epsilon_{ij} = \sqrt{\epsilon_{ii}\epsilon_{jj}}$  [Jorgensen *et al.*, 1996].

#### 1.4.2 Molecular Surfaces

Central to the discussion of solvent is a discussion of how to formulate the surface of a protein. The most frequently used formulations of surface area include:

- 1. The Van der Waals (VDW) surface is the surface formed by the VDW radius of each molecule, though sometimes differing parameters are used for the VDW radii, and the ideal radii may even vary by application.
- 2. The solvent accessible surface, which is defined as the surface traced by the center of a spherical probe "rolled" over the VDW surface [Richards, 1977]. This idea is very closely related to the idea of the solvent excluded volume, or the shape of the solvent cavity enforced by the VDW surface of the molecule [Richmond, 1984].
- 3. The molecular surface, or Connolly surface, is composed of the VDW surface in areas where the spherical probe touches the VDW surface, in union with all points on the probe "between" two points on the VDW surface when the probe is contacting multiple atoms [Connolly, 1983], put another way the surface of the volume which intersects no possible probe location.

Frequently these surfaces are approximated numerically, using the Shrake-Rupley algorithm [Shrake and Rupley, 1973], by considering a spherical mesh about every atom and including only points which satisfy the definition of the surface, or using these points to interpolate a surface.

The significance of surface area is determined by physical constraints but can be well illustrated by a number of observations about proteins. First the ratio of total area of a theoretical unfolded, i.e. linearly arranged, protein to its length is almost among proteins, only varying by  $\sim 3\%$  between different proteins.

#### 1.4.3 Solvent Models

Beyond covalent terms and electrostatic effects, solvation effects have a very large effect on protein structure, and the interactions between proteins and small molecules. Therefore it is critical to accurately model the effect of the solvent on the molecule. While explicitly modeling each water molecule and sampling over possible conformations is the most realistic possible model, doing so requires calculating both a large number of solute-solute interactions as well as sampling extensively different solvent configurations. In this case it is likely that more time will be spent determining the behavior of the solvent than that of the solute. Because of these complexities even with efficient methods of sampling explicit solvent models, these simulations are too expensive to use on systems the size of proteins [Figueirido et al., 1997; Zhang et al., 2001].

Therefore there is significant interest in continuum models which accurately describe the mean force of water, without requiring additional sampling or interactions as in explicit models [Zhang et al., 2001; Still et al., 1990; Qiu et al., 1997]. These methods have the potential to be three orders of magnitude, or even more, faster than explicit solvent experiments, and a number of different methods have been shown to accurately describe solvent effects [Zhang et al., 2001].

The total free energy of solvation can be separated into polar and non-polar components, which correspond to the work done inserting the uncharged solute molecule, or protein, into the solvent and then building the charges to their native values [Roux and Simonson, 1999].

$$E_{solvent} = \Delta W_{non-polar} + \Delta W_{electrostatic} \tag{1.7}$$

According to scaled particle theory the non-polar work done by inserting a sphere into a solvent can be approximated if the raidus of the sphere is neither too large nor to small as

$$\Delta W_{np}(s) = \gamma S A(X) \tag{1.8}$$

where  $\gamma$  is the surface tension of the solvent and the surface area corresponds most closely to the Connolly surface.

The electrostatic contribution to the solvent energy is the work necessary to add a charge to a hard sphere atom already in the solvent. The charge density in the solvent can be given by the Poisson-Boltzmann equation

$$\nabla \cdot [\epsilon(r)\nabla \psi(r)] = -4\pi \rho_u(r) \tag{1.9}$$

Though it is possible to solve this at every step of a simulation, it becomes rather expensive, therefore faster approximations are sought [Nicholls and Honig, 1991]. The total work can be approximated by the Born model

$$\Delta W_{electrostatic} = \frac{Q^2}{2R} \left( \frac{1}{\epsilon_v} - 1 \right) \tag{1.10}$$

However, this assumes that the induced charge in the solvent is entirely concentrated on the surface of the ion, which is impossible, therefore R, or the Born  $\alpha$  radius becomes a fit parameter, representing the effective radius of a charged sphere in the solvent.

The electrostatic solvation contribution can also be expressed as

$$\Delta W_{\text electrostatic} = \frac{1}{2} \sum_{i,j} q_i q_j f(x_i, x_j) = \frac{1}{2} \sum_i q_i^2 f(x_i, x_i) + \frac{1}{2} \sum_{i \neq j} q_i q_j f(x_i, x_j)$$
(1.11)

where f is a weighting function for the interaction between charges  $q_i$  and  $q_j$ . Historically there are a variety of methods of approximating this weighting function, however one of the most popular is the generalized Born (GB) [Still *et al.*, 1990]. In the generalized Born approch

$$f(x_i, x_j) = \sqrt{d(x_i, x_j) + R_i R_j e^{\frac{-d(x_i, x_j)^2}{4R_i R_j}}}$$
(1.12)

and one of the limiting factors to accuracy becomes obtaining proper estimates of the effective radii, since charges are not uniformly exposed to the solvent [Schaefer and Karplus, 1996].

Another approach is to estimate both the nonpolar and electrostatic contributions to solvation as proportional to the surface area, with different proportionality constants for different atoms.

$$\Delta W = \sum_{atoms} \gamma_{atom} SA(atom) \tag{1.13}$$

Although this method is very inexpensive to compute, it can be somewhat difficult to solve for the force on an atom, due to the way the surface changes as atoms move [Roux and Simonson, 1999].

# Chapter 2

# Prediction of P450 Sites of Metabolism

#### 2.1 Introduction

The most common method of drug clearance among currently prescribed drugs is metabolism, which is the primary method of clearance for approximately 75% of the top 200 most commonly prescribed drugs in the United States [Williams et al., 2004]. Cytochrome p450 is critical to drug metabolism, being active in approximately 75% of drugs which are cleared in this method [Guengerich, 2007]. As covered in 1.1.2.3, accurately predicting absorption, distribution, metabolism, and excretion, characteristics of drug compounds can be a critical determining factor in determining drug efficacy, performance in clinical development stages, and the overall costs of bringing new drugs to market. Because of the ubiquity of P450 in metabolic reactions of drugs, there is no other single enzyme family as significant to determining ADME as P450.

The general form of the reaction most frequently catalyzed by P450 is

$$RH + O_2 + NADPH + H^+ > ROH + H_2O + NADP^+$$
 (2.1)

The specific locations of sites of metabolism (SOM) on small molecules can have a profound effect on the ADME characteristics of a small molecule. Some cancer drugs such as epipodophyllotoxins, ifosphamide, tamoxifen, taxol and vinca alkaloids, are converted

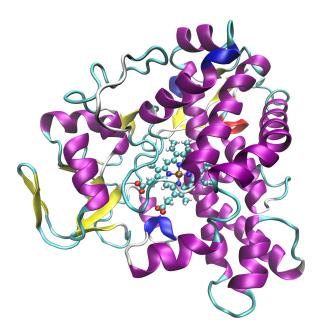


Figure 2.1: The structure of cytochrome P450, taken from PDBid 1JFB, shown in cartoon representation. The bonded heme group, shown as ball and stick model, is visible in the center. The brown iron atom is chelated by four deep blue nitrogen atoms.

into their active states by oxygenation at specific locations by P450 [Kivisto *et al.*, 1995]. P450 is the body's primary defense against toxicity, usually catalyzing the conversion of toxic compounds into harmless products [Gonzalez, 2005; Guengerich, 2001]. However in certain cases, such as acetaminophen, it is possible for P450 to convert a harmless reactant into a toxic product [Chen *et al.*, 1998].

#### 2.2 Methods

Prediction of sites of metabolism is a three stage procedure:

- 1. Initially the small molecule is docked using a rigid body grid search algorith GLIDE
- 2. The docked conformations are refined using a Monte Carlo Minimization (MMC) approach which samples degrees of freedom in both the ligand and protein
- 3. Refined conformations are classified into reactive site or non-reactive site on the basis of the energy of the refined conformations and the intrinsic reactivity of the site

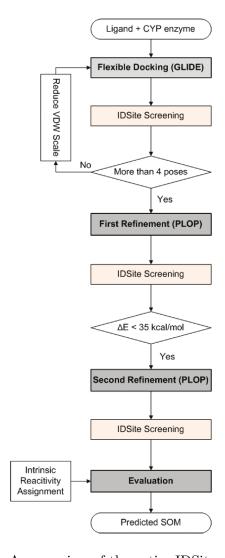


Figure 2.2: An overview of the entire IDSite procedure.

#### 2.2.1 Docking

#### 2.2.2 Monte Carlo Minimization Refinement

1. Hybrid Monte Carlo Moves: Hybrid Monte Carlo (HMC) is built on top of a molecular dynamics (MD) integrator. We implemented velocity verlet MD using the RESPA formalism [Tuckerman et al., 1991], with bonded and short range interactions evaluated every inner time step, with long range interactions evaluated every long time step. We also included in the including Andersen, Berendsen, and Langevin thermostats, as well as Brownian Dynamics. Short range interactions included all bonded inter-

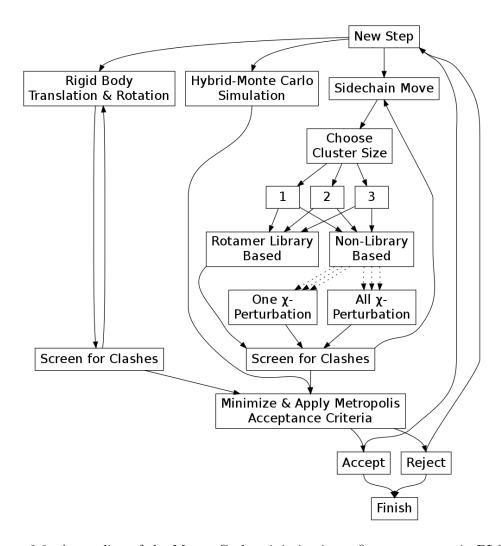


Figure 2.3: An outline of the Monte Carlo minimization refinement stages in PLOP.

actions and nonbonded interactions less than a user-specified cutoff. Both short and long range cutoffs are dipole-based as described in a previous paper [cite]. Energies are conserved in vacuum simulations if the long range cutoff extends to cover the entire molecule. With implicit solvent dynamics, energies are not conserved as there is no derivative of the Born alpha with respect to position, so a thermostat must be used to approximate realistic dynamics. One mode of action is to run HMC on top of normal RESPA dynamics, with acceptance and rejections done after a fixed number of steps of MD, as in typical HMC. Velocities are re-randomized after every Monte Carlo step from the Maxwell-Boltzmann distribution. However, HMC can also be

implemented in a multiple-time step Monte Carlo framework [Hetenyi et al., 2002]. In this case, molecular dynamics is run only using only the short range energies, which will conserve energy and thus yield proper Markov chain behavior while the cutoffs and Born alpha are not updated. Inner loop Monte Carlo steps are performed with only the short range dynamics, and outer loop Monte Carlo steps are performed with all interactions. In the case of implicit solvent simulations, the Born alpha are only reevaluated in the outer loop Monte Carlo steps. This allows for evaluation of the full surface integral relatively infrequently, and yields a properly weighted Boltzmann distribution of conformations without needing position derivatives of the Born alphas. The hybrid Monte Carlo (HMC)[Duane et al., 1987] move in PLOP performs simultaneous sampling for the selected residues in the protein side chains and backbone as well as the ligand. Each HMC move performs a 5 picosecond, constant energy molecular dynamic (MD) simulation (starting at 900K) on all the atoms in the selected residues. Taking up to 15 minutes per move, the HMC is the most expensive among all three types of moves in PLOP.

2. Rigid motion moves. Rigid body translation and rotation were also implemented for noncovalently linked moieties, such as ligands. Random rotations and translations were coupled together, allowing for more concerted movement. Rigid body move implemented in PLOP can optionally include a screening step, where atomic Lennard-Jones overlaps that would lead to energies much higher than would be observed in any conceivably long equilibrium simulation are rejected without further evaluation. A ratio of 0.7 between the distance between the two atoms and the sum of the Lennard-Jones radii of the two atoms yields energies on the order of 10's of thousands of kcal/mol, and is thus reasonable to maintain equilibrium sampling in a Monte Carlo simulation. Translations were implemented in a random direction, with a user-defined magnitude. Rotations were implemented by picking a random quarternion (a random angle around a random axis, through the geometric center of the rigid group) with a user specified maximum random angle centered around either the current angle, or 180 from the current angle, in the case of a flip. Multiple time scale Monte Carlo sampling was also implemented with rigid body moves, with short range and long

range interactions defined as above. In addition, an option to compute the inner Monte Carlo loops with reduced Lennard-Jones radii were also implemented, to increase the ability to escape from tight spacial bottlenecks. In this case, the long time step energies are the full energies with unscaled Lennard-Jones radii. This increases the conformational freedom and therefore sampling for the short, at a cost of decreasing the acceptance probability in the outer loop. Scaled Lennard-Jones radii were also implemented in multiple time dynamics, but yielded very little apparent improvement because of the lack of phase space overlap between dynamics with different scaled Lennard-Jones radii). Rigid body moves are used to sample the translational and rotational space of the ligand. Multiple attempts with reduced VDW radii are applied, as it is quite common to fail in searching for a clash-free conformation in a single rigid body moving attempt (especially when the ligand is large and flexible and the binding pocket is relatively small). Each rigid body move includes 1000 attempts, and each attempt performs a translation along a random vector and a rotation around a random axis, with less than 0.5 angstroms and 60 degree displacement, respectively. In addition, the VDW radii are reduced (scaling factor 0.8) to soften the Lennard-Jones potential, so that mild steric clashes are allowed, which are likely to be resolved by the subsequent minimization. The rigid body move usually takes 20 to 40 seconds per move.

3. Side chain moves. Several types of side chain motions were implemented in PLOP. In all cases, they are defined in a such a way that they can be applied to both ligands and proteins. The same atomic overlap screening function implemented with the rigid body Monte Carlo was implemented with the side chain torsional moves. a. Random torsion angle moves: The first type of move that was implemented is random movement of torsional chi angles. For small torsion moves, a random perturbation of the angle of +/- X is made, where X is a random number with user defined magnitude. For large torsion moves, for each torsion angle that is changed, a random angle is selected in the form 60\*Y +/- X, where Y = 1 through 5, and X is the same random number for the small torsion moves. The large move was introduced since positions at the top of rotamer barriers are relatively unlikely to be selected, and efficiency

thus can be improved by focusing on the more probable moves. The ratio of small to large torsion moves can be used-adjusted, as can the ratio of probabilities of changing all the torsions in a randomly selected side chain versus changing only one single (randomly selected) torsion among all the free torsions in the simulation can be set as a user-defined parameter. Rotamer side chain moves: A second type of torsional samples implemented is random selection of a new rotamer state for the entire side chain, plus an optional user defined small noise term for each torsion in the rotamer state. A database of protein rotamer states obtained from crystallographic data are already a part of PLOP [Xiang and Honig, 2001] Rotamer libraries for ligands are generated by examining all possible side chain conformations at 10 degree resolution and screening this set for steric clashes. A Monte Carlo move in this case represents a choice of a new torsional rotamer state for the entire side chain. Monte Carlo moves based on torsional states cannot lead to correct equilibrium distributions, as transitions from non-rotamer states to rotamer states are defined, but not reverse transitions, upsetting detailed balance. However, a pretabulated rotamer state is more likely to be low energy than a randomly generated torsional state, and thus allows for more diverse conformational searching. Correlated torsional moves: Most torsional rearrangements of the side chains in the core of proteins are highly correlated because of the density. In order to attempt to include correlated torsional motion, at each step we examine the distance between all pairs of beta carbons in the ligands that are free to move. At each step, for the set of side chains that are free to move, clusters where beta carbons are all mutually within a user-specified distance are identified. This process takes a trivial amount of time compared to an energy evaluation, so does not slow the simulation at all. Then, with user specified probabilities, clusters of different sizes are selected for the torsional moves, either with random side chain moves, or rotamer selection moves. By selecting only clusters where all residues are mutual neighbors, detailed balanced is observed for simulations where accurate equilibrium sampling is desired. By varying the dihedral angles of the rotatable bonds, IDSite uses side chain MC moves in PLOP to sample the selected side-chain conformations of the protein and of the ligand. Up to three close residues (C beta distance within 6 angstroms) are allowed to rotate collectively, but the moves of the protein residues and those of the ligand are separated. In each attempted movement, the conformations of the selected side chains (from the protein/ligand) are either changed by random perturbations or assigned by the randomly selected rotamers from a library. For an attempt with a random perturbation, the displacement of each dihedral angle is the sum of a large rotation (N times 60 degrees with N as a random integer between 0 and 5) and a random perturbation from 0 to 30 degrees. For a rotamer library attempt, a side-chain conformation is updated with a random rotamer from a high resolution side-chain library for protein residues [Xiang and Honig, 2001], and from a homogeneous library at 10 degree resolution for the ligand. If a structure with tolerable overlaps is generated in an attempt, it is minimized and sent to subsequent stages for judgment of acceptance. Each side-chain move takes less than 15 seconds and is the fastest among all the three move types.

#### 2.2.3 Evaluation

- 1. PLOP, designed for extensive sampling with protein loop optimization proteins has had recent success in correctly predicting protein structure such as short and medium loops and side chain configurations [cite]
- 2. It has also been useful in identifying and partially overcoming certain classes of errors in implicit model simulations, such as insufficiently compact structures [cite], and overstabilitzation of salt bridges [cite]
- 3. However, the sampling methods introduced in plop have been limited in the ability to sample the system. Although it can sample very diverse structures, it doesn't necessary locate nearby minima, especially those related by conformational rearrangement, and may therefore miss some decoy configurations.
- 4. We have introduced a framework for Monte Carlo sampling into PLOP, including
  1. hybrid Monte Carlo using molecular dynamics 2. torsional moves 3. translation and
  rotation moves for separated moieties, such as ligands bound in an active site.
- 5. We have used this Monte Carlo framework to extensively sample CDK2 ligands. Methods: We have introduced a framework into PLOP for both rigorous Monte Carlo

sampling and minimization Monte Carlo. Move sets including hybrid Monte Carlo, moves in torsional space, and translation and rotational rigid body moves.

Chains of Monte Carlo moves: Chains of Monte Carlo moves are performed serially. At the beginning of each sequence of steps, one of the possible Monte Carlo options (for these simulations HMC, rigid body MC, and side chain MC) is randomly selected according to the user specified probabilities, and a user specified number of outer loop MC moves are made. The process is then repeated for a user-specified number of steps. In many cases, thermodynamic sampling is not needed, and all that is required is exploration of representative low energy states. Many of the caveats that are required for equilibrium simulations can be ignored, and additional MC methods leading to significantly increased conformational sampling can be used. Low energy state sampling: In this paper we will focus on the minimization Monte Carlo (MinMC) as a tool to generate large numbers of low-energy configurations to test the underlying energy model. MinMC was implemented in the multiple level Monte Carlo framework as well, with minimization occurring only at the outer steps. This allows a number of very rapid moves to be made on the short range potentials at high temperature to maximize conformational exploration before minimization. By using a moderately high temperature, significant conformational motion can be introduced while still remaining somewhat close to the potential energy surface. Other Considerations: The Monte Carlo implementation in PLOP is very modular, allowing additional Monte Carlo move sets to be added in easily. Additional speedups were achieved by implementing storage and retrieval of the complete state of GB variables such that upon rejection, no additional calculation need be done. Other features that have been implemented that will not be further discussed in this paper are a simulated annealing protocol, allowing the temperature used either for strict or minimization Monte Carlo to be decreased throughout the simulation, and replica exchange using MPI. There are a very large number of possible parameters that have been introduced, and it is not feasible to directly optimize conformational searching over the entire parameter space. We performed limited optimization, first of the [fill in the sequence of optimizations and the rationale], looking for the most diverse clustering [Robert, fill in this discussion of the criteria]. This lead to the following set of parameters. We can decide how much of our intermediate results about useful parameters

to use here. I'd lean towards more mentions. It would help explain some of the screwy combinations we have (like the different MC acceptance criteria)]. For the simulations described in this paper, we used the following parameters: Short range energy dipole-dipole and Lennard-Jones cutoffs of 8 Angstroms were used, as well as 12 Angstrom cutoffs for the short range charge-dipole cutoff and 15 Angstroms for the short range dipole-dipole cutoff. All long range cutoffs were set to be effectively infinite. In this study, we compared four different functional forms of the potential function. In all cases, OPLS-2005 protein parameters were used for both the protein and ligand, as implemented in PLOP. Ligand parameters were generated with the hetgrp\_ffgen utility of Schrodinger software, using OPLS-2005 parameters. Surface Generalized Born implicit solvent was used, in the form described in [Ghosh et al., 1998]. In previous papers using structure prediction with PLOP, two separate correction terms were introduced which substantially improved side chain prediction. One was a hydrophobic attraction term, introduced by analogy with the ChemScore [cite]. The second was a variable dielectric treatment of charged side chains, accounting for the change of polarization around charged moieties [?]. Our four effective potential energy functions are four choices resulting from inclusion or exclusion of these correction terms. All atoms of all residues with any atom within 5 Angstroms of the ligand in the starting crystal structure were allowed to move during Monte Carlo moves, including the ligand itself. For each combination of force fields and for each structure, a sequence of 3100 repetitions of the overall serial MC sequence was carried out. The relative probabilities for HMC, rigid body MC, and side chain MC were 1, 7, and 14, respectively (the total probability is normalized to 1.0). For rigid body Monte Carlo, a steric screen with an overlap factor of 0.7 was used, with a translation size of 0.5 Angstroms and a rotation size of plus or minus 60 degrees. No flip moves were included, as flips were not anticipated with the geometry of the ligand system [Robert, check this is true?] A Lennard-Jones scaling parameter of 0.8 was used during the inner steps. Each rigid MC step consisted of 1000 inner steps, and only one outer step, meaning that only one minimization occurred each time rigid body Monte Carlo was selected as the move step. Minimized Monte Carlo acceptance was performed at 300 K. For side chain Monte Carlo, a steric screen with an overlap factor of 0.6 was used. Rotamer torsional moves were selected 75% of the time, with half of the remaining being of random torsions, and the other half random perturbations of all torsions within the randomly selected side chains. Clusters of size 1 (i.e. single side chains), size 2 and size three were selected in equal proportion, and all side chains in the cluster were perturbed with the selected torsion move. A mutual beta carbon distance of 6 Angstroms was used for the clustering size. Small torsion perturbations made +/- 60 degress from the current dihedral angle, and were performed 5% of the time; Large periodic moves were performed 95% of the time. Only outer steps were performed, and each side chain Monte Carlo series consisted in only one move. Minimization was performed after the single step, and acceptance was performed at 1 K. The underlying molecular dynamics for the hybrid Monte Carlo consisted of 500 5 ns RESPA [Tuckerman et al., 1991] steps, each with 5 1 ns short range steps. The dynamics were initialized from a Maxwell-Boltzmann distribution at 900 K, and then run without any thermostat the full 2. 5 ps run. Minimization was performed after the single HMC step, with acceptance/rejection performed at a Monte Carlo temperature of 900 K.

#### 2.3 Results

#### 2.4 Discussion

# Chapter 3

# Other Improvements in the Protein Local Optimization Program

### 3.1 Regression Testing

A number of common problems inherent in large programming projects are identifying bugs or regressions One of the largest problems [Evans, 2013; Atwood, 2009] Cathedral Bazaar [Raymond, 1999]

- 3.2 Small Molecule Library
- 3.3 Crystal Symmetry
- 3.4 Knowledge Based Backbone Dihedral Penalty

Dot (directed graphs) [Koutsofios et al., 1991]

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