

BootStrapping

```
# Example from  
# An Introduction to the Bootstrap  
# (Chapman & Hall/CRC Monographs on Statistics and Applied Probability) 1st Edition  
# by Bradley Efron (Author), R.J. Tibshirani (Author)
```

```
# Resampling Example for aspirin  
#  
#           strokes      subjects  
# aspirin group      119      11037  
# placebo group     98       11034  
#  
# ratio of rates, theta_hat
```

```
defaultW <- getOption("warn")
```

```
options(warn = -1)
```

```
theta_hat = (119/11037) / (98/11034)  
theta_hat
```

```
## [1] 1.213956
```

```
# We want to estimate the interval for true stroke ratio, theta, which is 0.93 to 1.59  
# with 95% confidence level
```

```
aspirin_stroke_cases = rep(1,119)  
#aspirin_stroke_cases
```

```
aspirin_no_stroke_cases = rep(0,11037-119)  
#aspirin_no_stroke_cases
```

```
aspirin_group = c(aspirin_stroke_cases,aspirin_no_stroke_cases)  
#aspirin_group
```

```
aspirin_group <- sample(aspirin_group)
```

```
placebo_stroke_cases = rep(1,98)  
#placebo_stroke_cases
```

```
placebo_no_stroke_cases = rep(0,11034-98)
```

```

#placebo_no_stroke_cases

placebo_group = c(placebo_stroke_cases,placebo_no_stroke_cases)
#placebo_group
placebo_group <- sample(placebo_group)

asp_bs_sample_case = sample(x= aspirin_group, size = 11037,replace = TRUE)
#asp_bs_sample_case

sum(asp_bs_sample_case)

```

```
## [1] 117
```

```

plb_bs_sample_case = sample(x= placebo_group, size = 11037,replace = TRUE)
#sum(plb_bs_sample_case)

# lets take 1000 bootstrap samples

library(purrr)
k <- seq(1,1000)
asp_bs <- map(k,function(k){
  set.seed(k, sample.kind = "Rounding")
  return(sample(x= aspirin_group, size = 11037,replace = TRUE))
})

plb_bs <- map(k,function(k){
  set.seed(k, sample.kind = "Rounding")
  return(sample(x= placebo_group, size = 11034,replace = TRUE))
})

#str(asp_bs)
#typeof(asp_bs)
#class(asp_bs)

#str(asp_bs)

asp_bs[[1000]][45]

```

```
## [1] 0
```

```

#summary(asp_bs)
k <- 1:1000
mean_asp <- map(k,function(k){
  numerator = sum(asp_bs[[k]])/11037
  denom = sum(plb_bs[[k]])/11034
  return(numerator/denom)
})

mean_asp1 <- unlist(mean_asp)
#mean_asp1
class(mean_asp1)

```

```
## [1] "numeric"

print("mean:")

## [1] "mean:"

mean(mean_asp1)

## [1] 1.226485

print("standard deviation:")

## [1] "standard deviation:"

sd(mean_asp1)

## [1] 0.1638905

# 95% confidence interval
print("95% confidence interval:")

## [1] "95% confidence interval:"

quantile(mean_asp1,c(25/1000,975/1000))

##      2.5%      97.5%
## 0.9372311 1.5691076

# Now we do the same analysis using bootstrap package boot

library(boot)

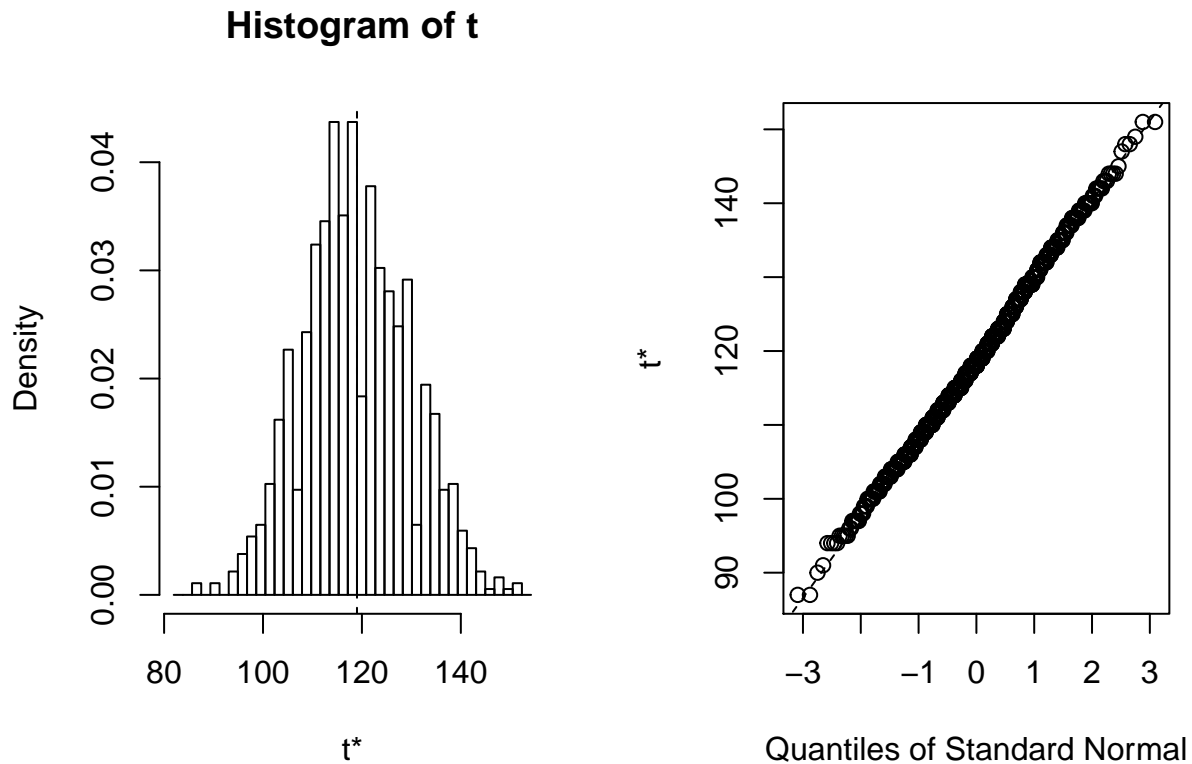
set.seed(100, sample.kind = "Rounding")

sum_ones_as <- function(data,indices){ return(sum(data[indices]))}

results_as <- boot(data = aspirin_group, statistic = sum_ones_as, R = 1000)
results_as

##
## ORDINARY NONPARAMETRIC BOOTSTRAP
##
##
## Call:
## boot(data = aspirin_group, statistic = sum_ones_as, R = 1000)
##
##
## Bootstrap Statistics :
##      original    bias    std. error
## t1*         119  -0.124    10.76255
```

```
plot(results_as)
```



```
#results_as$t

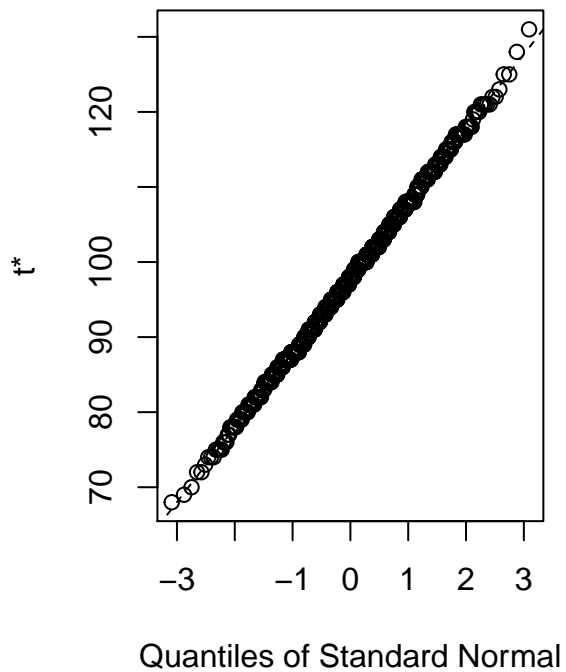
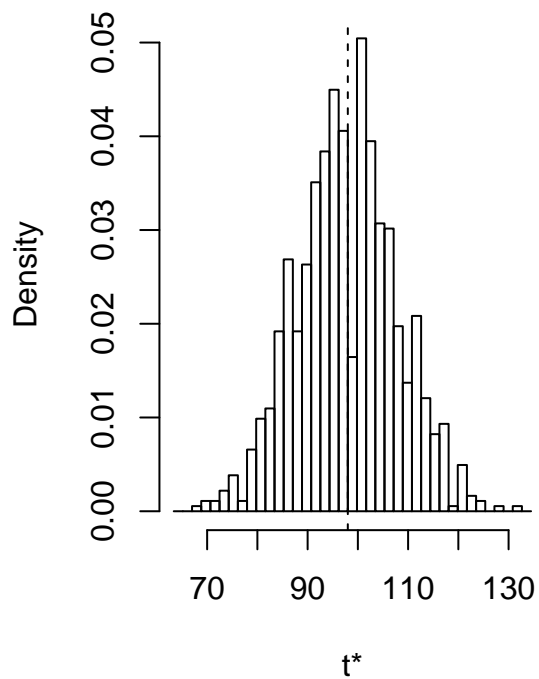
sum_ones_pl <- function(data,indices){ return(sum(data[indices]))}

results_pl <- boot(data = placebo_group, statistic = sum_ones_pl, R = 1000)
results_pl
```

```
##
## ORDINARY NONPARAMETRIC BOOTSTRAP
##
##
## Call:
## boot(data = placebo_group, statistic = sum_ones_pl, R = 1000)
##
##
## Bootstrap Statistics :
##      original    bias    std. error
## t1*          98  -0.161    9.939209
```

```
plot(results_pl)
```

Histogram of t



```
#results_pl$t
ratio <- (results_as$t/11037)/(results_pl$t/11034)
#ratio
print("mean:")
```

```
## [1] "mean:"
```

```
mean(ratio)
```

```
## [1] 1.226406
```

```
print("standard deviation:")
```

```
## [1] "standard deviation:"
```

```
sd(ratio)
```

```
## [1] 0.1607141
```

```

# 95% confidence interval
print("95% Confidence Interval:")

## [1] "95% Confidence Interval:"

quantile(ratio,c(25/1000,975/1000))

##      2.5%      97.5%
## 0.9396958 1.5671498

#Reference
# https://www.statmethods.net/advstats/bootstrapping.html

options(warn = defaultW)

```