

3.)

$$\alpha_p = 3\text{dB} ; \omega_c = \omega_p = 2000\pi \text{ rad/s}$$

$$\alpha_s = 10\text{dB} ; \omega_s = 700\pi \text{ rad/s}$$

$$T = \frac{1}{f} = \frac{1}{5000} = 2 \times 10^{-4} \text{ sec.}$$

Prewarping the digital frequencies we have

$$\Omega_p = \frac{2}{T} \tan \frac{\omega_p T}{2} = \frac{2}{2 \times 10^{-4}} \times \tan \left(\frac{2000\pi \times 2 \times 10^{-4}}{2} \right)$$

$$= 10^4 \tan(0.2\pi) = 7265 \text{ rad/s}$$

$$\Omega_s = \frac{2}{T} \tan \frac{\omega_s T}{2} = \frac{2}{2 \times 10^{-4}} \tan \left(\frac{700\pi \times 2 \times 10^{-4}}{2} \right)$$

$$= 10^4 \times \tan(0.07\pi)$$

$$= 2235 \text{ rad/s.}$$

The order of the filter

$$N = \frac{\log \sqrt{\frac{10^{0.1\alpha_s} - 1}{10^{0.1\alpha_p} - 1}}}{\log \frac{\Omega_s}{\Omega_p}} = \frac{\log \sqrt{\frac{10^1 - 1}{10^{0.3} - 1}}}{\log \frac{7265}{2235}} = \frac{\log 3}{\log 3.25} = 0.932$$

$$\therefore \underline{\underline{N=1}}$$

$$\Omega_c = 1 \text{ rad/s} \Rightarrow H(s) = \frac{1}{1+s}$$

$$\Omega_c = \Omega_p = 7265 \text{ rad/s.}$$

$$\boxed{\begin{array}{l} s \rightarrow \frac{\Omega_c}{s} \\ \text{ie.) } s \rightarrow \frac{7265}{s} \end{array}}$$

The transfer function of high pass filter

$$H(s) = \frac{1}{s+1} \bigg|_{s = \frac{7265}{s}}$$

Using ~~bilinear~~ bilinear transformation

$$H(z) = H(s) \bigg|_{s = \frac{2}{T} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$= \frac{s}{s+7265} \bigg|_{s = \frac{2}{2 \times 10^{-4}} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$\boxed{H(z) = \frac{0.5792(1-z^{-1})}{1-0.1584z^{-1}}}$$