Homework #13 AEP 3610 Due December 4

- 1. Griffiths 4.18
- 2. Griffiths 4.30
- 3. Griffiths 4.32
- 4. Griffiths 4.33
- 5. Griffiths 4.37

Bryant Har bjh 254 If first copy somehow disappeared or went into

b) Energy only dependent on principal quantum number. By textlook $E_{n} = -\left[\frac{m_{e}}{2\pi^{2}}\left(\frac{e^{2}}{4\pi\epsilon_{o}}\right)^{2}\right]\frac{1}{n^{2}} \Rightarrow \boxed{E_{\eta} = -\frac{m_{e}}{8\pi^{2}}\left(\frac{e^{2}}{4\pi\epsilon_{o}}\right)^{2} = -3.4 \text{ eV}}$

(Superposition of n=2 states)

Q430

a)
$$\chi^{t}\chi = 1 = A^{2}(9+16) = A = \frac{1}{5}$$

b) $(S_x) = \chi^+ S_x \chi = \frac{\pi}{50} [-3i \, 4] [0] [0] [0] = S_x = \frac{\pi}{50} (12i - 12i) = 0$ $(S_x) = \chi^+ S_x \chi = \frac{\pi}{50} [-3i \, 4] [0] [0] [0] = S_x = \frac{\pi}{50} (-12 - 12i) = 0$ $(S_y) = \chi^+ S_x \chi = \frac{\pi}{50} [-3i \, 4] [0] [0] [0] = S_x = \frac{\pi}{50} (-12 - 12i) = -\frac{12\pi}{25}$ $(S_y) = \chi^+ S_x \chi = \frac{\pi}{50} [-3i \, 4] [0] [0] [0] = S_x = \frac{\pi}{50} (-12i) = -\frac{\pi}{25} \pi$

C)
$$\langle S_{x}^{2} \rangle = \langle S_{y}^{2} \rangle = \langle S_{z}^{2} \rangle = \frac{k^{2}}{4}$$

 $\Rightarrow \sigma_{x}^{2} = \langle S_{x}^{2} \rangle - \langle S_{x} \rangle^{2} = \frac{k^{2}}{4} - 0 \Rightarrow \sqrt{\sigma_{x}^{2}} = \sigma_{y}^{2} = \langle S_{y}^{2} \rangle - \langle S_{y} \rangle^{2} = \frac{k^{2}}{4} - \frac{144k^{2}}{625} \Rightarrow \sqrt{\sigma_{y}^{2}} = \sigma_{y}^{2} = \langle S_{z}^{2} \rangle - \langle S_{z} \rangle^{2} = \frac{k^{2}}{4} - \frac{144k^{2}}{625} \Rightarrow \sqrt{\sigma_{z}^{2}} = \sigma_{y}^{2} = \frac{7}{50} \text{ h}$

$$\sigma_{z}^{2} = \langle S_{z}^{2} \rangle - \langle S_{z} \rangle^{2} = \frac{k^{2}}{4} - \frac{44k^{2}}{2500} \Rightarrow \sqrt{\sigma_{z}^{2}} = \sigma_{z}^{2} = \frac{12}{25} \text{ h}$$

 $\sigma_{S_{x}}\sigma_{S_{y}} \geq \frac{1}{2}|\langle S_{x}\rangle| \Rightarrow \frac{1}{2} \cdot \frac{7}{50} + 2 \cdot \frac{1}{2} \cdot \frac{7}{50} + 3 \cdot \frac{$

(24.32] a) $S_y = \frac{4}{2} \begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix} \Rightarrow \begin{bmatrix} -2 & -\frac{11}{2} \\ \frac{11}{2} & -2 \end{bmatrix} \Rightarrow 2^2 - \frac{11}{4} = 0 \Rightarrow 2 = \pm \frac{1}{2}$

$$\begin{bmatrix} -t_{1} & -t_{1} \\ -t_{1} & -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} 1 \\ -t_{1} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{1} \\ -t_{1} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} & t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1} & -t_{2} \\ -t_{2} \end{bmatrix} = \lambda \begin{bmatrix} t_{1}$$

b) Project onto eigenvectors...

$$\lambda = \frac{\pi}{2} : \chi_{+}^{+} \begin{bmatrix} a \\ b \end{bmatrix} = \frac{1}{\sqrt{2}} (a - ib) \Rightarrow + \frac{\pi}{2} , \text{ probability } \frac{1}{\sqrt{2}} |a - ib|^{2}$$
 $\lambda = -\frac{\pi}{2} : \chi_{-}^{+} \begin{bmatrix} a \\ b \end{bmatrix} = \frac{1}{\sqrt{2}} (a + ib) \Rightarrow -\frac{\pi}{2} , \text{ probability } \frac{1}{\sqrt{2}} |a + ib|^{2}$

C)
$$S_{y}^{2} = 50\% \cdot \left(\frac{\pi}{2}\right)^{2} + 50\% \left(-\frac{\pi}{2}\right)^{2} = S_{y}^{2} \rightarrow \frac{\pi^{2}}{4}$$
 Probability 1

$$\begin{array}{c} O(S_{1}^{2}) = (S_{1}^{0} + S_{2}^{0}) \frac{1}{\sqrt{2}} (f_{1}^{0} + I_{1}^{0}) = \frac{1}{\sqrt{2}} \left[(S_{1}^{0})_{1} + I_{1}^{0} S_{2}^{0}) + I_{2}^{0} S_{2}^{0} f_{1}^{0} + I_{2}^{0} S_{2}^{0} f_{1}^{0}) \right] \\ = \frac{1}{\sqrt{2}} \left[(S_{1}^{0})_{1} + I_{2}^{0} S_{2}^{0} f_{1}^{0} f_{1}^{0} f_{1}^{0} f_{2}^{0} f_{2}^{0} f_{1}^{0} f_{1}^{0} f_{2}^{0} f_$$