Project Final Paper:

"Analyzing Crime Rates in America: Data Analytics Approach"

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1. Problem Statement

With the development of modern machine learning techniques and their availability across the globe, researchers are trying to apply it to a lot of fields. Crime Forecasting is one of those fields in which use of machine learning has recently developed but it still remains a largely untouched problem. While there are numerable factors that affect the crime rate in various locations, it does come down to a few critical factors that can be predicted with the help of data available from government agencies.

The purpose of this project is to convert the reactive approach of Law Enforcement agencies to a rather proactive approach based on the forecasting model developed using multiple linear regression or regression trees based on the dataset used in the project for various locations across the US.

2. Dataset

The dataset being used is an agglomeration of data points collected from multiple sources, bounded by a common timeline and are combined via programming. The given socio-economic data includes the 1990 Law Enforcement Management and Admin Stats (LEMAS) survey and crime data from 1995 FBI UCR.

The variables included in the dataset involve the community, such as the percent of the population considered urban, the median family income, involving law enforcement, such as per capita number of police officers, and percent of officers assigned to drug units. The crime attributes that could be predicted are the 8 crimes considered 'Index Crimes' by the FBI (Murders, Rape, Robbery, etc.), per capita (actually per 100,000 population) versions of each, and Per Capita Violent Crimes and Per Capita Nonviolent Crimes. The potential goal is to reduce the number of attributes from a total of 129 of which 125 are predictive attributes and 4 are non-predictive.

3. Approach

3.1 Backward Subset Selection

First, all the other potential output variables except *violentPerPop*, were removed from the data set. Then the dataset was divided into 70% training and 30% test data. The code is shown below:

```
#remove other predictor variables
crimeViolence<-crimeNonNA[,c(-120,-118:-103)]
set.seed(1)
#create the training data and test data. Training:Test ratio is 70:30
train<-sample(nrow(crimeViolence),(0.7)*nrow(crimeViolence))
crime.train<-crimeViolence[train,]
crime.test<-crimeViolence[-train,]</pre>
```

Then tried to perform subset selection method on violentPerPop (violent crime per population) after removing characteristic variables and response variables with target number of 20 variables.

```
> library(leaps)
>
regfit.full = regsubsets(violentPerPop~.-State-communityname-murders-murder
erPop-rapes-rapesPerPop-robberies-robbbPerPop-assaults-assaultPerPop-burglar
ies-burglPerPop-larcenies-larcPerPop-autoTheft-autoTheftPerPop-arsons-arsons
PerPop-violentPerPop-nonViolPerPop, data=crimeNonNA, nvmax=20, really.big=T)
Reordering variables and trying again:
```

However, as it was 'big data' with more than 100 attributes and 1000 observations, even after over 24-hours of waiting in workstation condition, the RStudio still showed running for the results. So, it was to use the simple backward subset selection method based on linear regression.

```
> model.back=step(lm(violentPerPop..state-communityname-murders-murdPerPop-rapes-rapesPerPop-robberies-
robbberPop-assaults-assaultPerPop-burglaries-burglPerPop-larcenies-larcPerPop-autorheft-autorheftPerPop
arsons-aronsPerPop-violentPerpop-nonviolePrPop, data=training), direction="backward")

Start: AIC-15721.03
violentPerPop ~ (communityname + State + fold + pop + perHoush +
pctBlack + pctWhite + pctAsian + pctHisp + `pctI2-21' + `pctI2-29' +
pctI6-24' + pct65up + persurban + pctUrban + medIncome +
pctWwage + pctWfarm + pctWdiv + pctWsocsec + pctPubAsst +
pctRetire + medFamIncome + perCapInc + whitePerCap + blackPerCap +
NAperCap + asianPerCap + otherPerCap + hispPerCap + persPoverty +
pctEvoverty + pctLowEdu + pctNotHSgrad + pctCollard + pctUnemploy +
pctEmploy + pctEmployMfg + pctEmployProfServ + pctOccupManu +
pctOccupMgmt + pctWaleDivorc + pctWaleWeWar + pctFemplovorc +
pctLilvorc + persPerFam + pctVard + pctCidsPar + `pctKids-4w2Par` +
pctLilvorc + persPerFam + pctVard + pctCidsPar + `pctKids-4w2Par` +
pctLilvorar + pctWard + pctCidsPar + `pctKids-4w2Par` +
pctTopcIntmig-5 + pctFenImmig-8 + `pctFenImmig-3' +
pctFenImmig-5 + pctFenImmig-8 + `pctFenImmig-3' +
pctTopcPenseHous + pctLargHousFam + pctLargHous + persPerOccupHous +
perSperOwnOccup + pcrtHousOwnerOccup + pctPopDenseHous + pctSmallHousUnits + medNumBedrm + housevacant +
pctHousOccup + pctHousOwnerOccup + pctPoworOccup +
pctHousOwnerOccup + pctVacaantBoarded + pctVacantBoarded + pctVacant
```

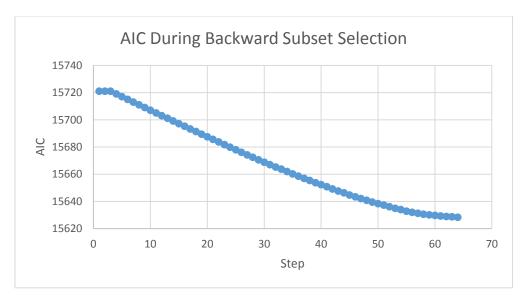
After running the code, system tested several selections and it came down to 40 variables.

```
Step: AIC=15628.35

violentPerPop ~ perHoush + pctBlack + persUrban + pctUrban + medIncome + pctwwage + pctwfarm + pctRetire + medFamIncome + percapInc + asianPerCap + otherPerCap + pctPoverty + pctLowEdu + pctEmployHg + pcttBelDivorc + pctFemblovHg + pctEmployHg + pctMalDivorc + pctKidsZPar + `pctWorkMom-18` + pctKidsBornNevrMarr + numForeignBorn + `pctImid-5' + pctLargHous + persPeroccupHous + persPerPenterOccup + pctPerSownOccup + pctPopDenseHous + houseVacant + pctHousOwnerOccup + pctVacantBoarded + pctVacant6up + rentLowQ + rentMed + medOwnCostpct + medOwnCostPctWo + persEmergShelt + pctForeignBorn + pctOfficDrugUnit
                                                                     Df Sum of Sq
                                                               158604072 15628
1 243502 158847574 15628
1 284132 158888205 15629
  `pctImmig-5`
perHoush
                                                                                      1076085 159680157 15635
1101295 159705367 15636
       medOwnCostPctWO
                                                                                     1101295 159705367 15636
1104748 159708820 15636
1246176 159850248 15637
1267800 159871872 15637
1329812 15993384 15638
1391914 159995986 15638
1407123 160011195 15638
1473115 160077188 15639
1552309 160156381 15639
        persPerRenterOccup 1
        pctAllDivorc
       rentLowQ
pctPersOwnOccup
pctUrban
persPerOccupHous
        numForeignBorn
        rentMed
                                                                                     1552399 1601156381 15639
1561018 160165990 15639
1638371 160242443 15640
1733253 160337325 15641
1888951 160443023 15642
1882624 160486696 15642
2155720 160759792 15644
2201689 160805762 15645
        pctHousOwnerOccup
      pctwwage
pctEmployMfg
`pctWorkMom-18`
pctMaleDivorc
        pctKids2Par 1
pctKidsBornNevrMarr 1
      pctRetire
persUrban
houseVacant
                                                                                      2236748 160840820 15645
2460671 161064743 15647
                                                               1 3491974 162096046 15655
1 4607057 163211130 15664
```

And the summary of linear regression model it obtained through backward subset selection method is provided on the next page.

```
> summary(model.back)
call:
lm(formula = violentPerPop ~ perHoush + pctBlack + persUrban +
    pctUrban + medIncome + pctWwage + pctWfarm + pctRetire +
    medFamIncome + perCapInc + asianPerCap + otherPerCap + pctPoverty +
    pctLowEdu + pctEmploy + pctEmployMfg + pctMaleDivorc + pctFemDivorc +
    pctAllDivorc + pctKids2Par + `pctWorkMom-18` + pctKidsBornNevrMarr
numForeignBorn + `pctImmig-5` + pctLargHous + persPerOccupHous +
    persPerRenterOccup + pctPersOwnOccup + pctPopDenseHous +
    houseVacant + pctHousOwnerOccup + pctVacantBoarded + pctVacant6up +
    rentLowQ + rentMed + medOwnCostpct + medOwnCostPctWO + persEmergShelt +
    pctForeignBorn + pctOfficDrugUnit, data = training)
Residuals:
     Min
               10
                    Median
                                          Max
-1456.77
         -177.02
                    -26.76
                             124.42 2341.13
Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
                     3.432e+03 5.767e+02 5.951 3.43e-09 ***
(Intercept)
perHoush
                    -1.545e+02 1.017e+02
                                            -1.520 0.128856
                     9.344e+00 1.527e+00
                                           6.119 1.25e-09 ***
pctBlack
                                 3.415e-04 -4.472 8.43e-06 ***
persUrban
                    -1.527e-03
                                3.058e-01 3.363 0.000793 ***
pctUrban
                    1.028e+00
medIncome
                    -2.159e-02
                                7.302e-03 -2.957 0.003160 **
                    -1.653e+01
                                4.531e+00 -3.649 0.000274 ***
pctWwage
pctWfarm
pctRetire
medFamIncome
ancapInc
                                1.794e+01
                                            1.905 0.057044
                     3.417e+01
                                 3.790e+00 -4.264 2.16e-05 ***
                    -1.616e+01
                                            2.290 0.022181 *
                    1.532e-02
                                6.688e-03
                    -1.285e-02
                                7.853e-03 -1.636 0.102052
                                            2.713 0.006752 **
2.690 0.007242 **
                    3.239e-03
                                1.194e-03
                     3.473e-03
                                1.291e-03
otherPerCap
pctPoverty
                    -1.004e+01
                                3.604e+00 -2.785 0.005423 **
                  -7.398e+00 3.221e+00
7.783e+00 4.779e+00
                                3.221e+00 -2.297 0.021772 *
pctLowEdu
pctEmploy
                                            1.629 0.103618
                  -5.627e+00 1.499e+00 -3.753 0.000182 ***
2.482e+02 6.346e+01 3.912 9.65e-05 ***
pctEmployMfg
pctMaleDivorc
                                            2.852 0.004413 **
pctFemDivorc
                     1.905e+02
                                6.678e+01
pctAllDivorc
                    -4.112e+02
                                1.292e+02 -3.182 0.001495 **
                                4.112e+00 -4.186 3.04e-05 ***
                    -1.721e+01
pctKids2Par
 pctWorkMom-18`
                    -9.548e+00
                                2.470e+00 -3.866 0.000116 ***
pctKidsBornNevrMarr 4.259e+01
                                1.007e+01 4.230 2.50e-05 ***
                                6.270e-04
numForeignBorn
                                            3.460 0.000558
                     2.170e-03
                                1.279e+01 -1.407 0.159739
`pctImmig-5`
                    -1.799e+01
                    -1.788e+01
                                9.846e+00 -1.816 0.069534
pctLargHous
persPerOccupHous
                                            3.382 0.000742 ***
                    7.068e+02
                                2.090e+02
                                1.191e+02 -2.996 0.002784 **
persPerRenterOccup -3.568e+02
pctPersOwnOccup
                     -3.266e+01
                                 9.936e+00 -3.287 0.001038 **
                                 6.082e+00
                    1.549e+01
                                            2.547 0.010985 *
pctPopDenseHous
                                             5.327 1.18e-07 ***
houseVacant
                     3.294e-02
                                 6.183e-03
                                            3.562 0.000382 ***
pctHousOwnerOccup
                    3.332e+01
                                9.355e+00
pctVacantBoarded
                     8.230e+00
                                3.704e+00
                                            2.222 0.026447
                    -2.281e+00
                                9.703e-01 -2.350 0.018899 *
pctVacant6up
                                3.047e-01 -3.210 0.001360 **
                    -9.779e-01
rentLowO
                                            3.552 0.000396 ***
                    1.097e+00
rentMed
                                 3.089e-01
medOwnCostpct
                    -8.507e+00
                                5.420e+00 -1.570 0.116751
medOwnCostPctWO
                    -2.683e+01
                                8.970e+00 -2.992 0.002827 **
persEmergShelt
                     7.340e-02
                                4.160e-02
                                            1.764 0.077910
pctForeignBorn
                     9.151e+00
                                4.195e+00
                                             2.181 0.029339
                                            2.423 0.015543 *
pctOfficDrugUnit
                     9.661e+00 3.988e+00
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 350.8 on 1289 degrees of freedom
Multiple R-squared: 0.6883,
                                 Adjusted R-squared: 0.6787
F-statistic: 71.17 on 40 and 1289 DF, p-value: < 2.2e-16
```



It can be seen from graph above that AIC decreased continuously each step during stepwise backward selection. Through cross-validation approach a RMSE value of 122,105.7 was obtained.

However, it would not be a good subset selection method as this selected variables' value is limited to when it is only used on building a linear regression model.

3.2 Lasso Regression

The output variable in focus is violentPerPop, which is the total number of violent crimes per 100K population. Ridge regression does have one obvious disadvantage. Unlike forward and backward stepwise selection, which will generally select models that involve just a subset of the variables, ridge regression will include all p predictors in the final model. Lasso regression is a great model that is similar to ridge regression, faster than the subset selection models, and in addition performs variable selection.

3.2.1 Methodology

After obtaining the training and test data, a model matrix x and vector y was created, since lasso regression expected the x to be a matrix and y to be a vector. These matrices contain the predictors and output variables respectively. The first variable in x is deleted because it consists of the intercept term. The code is as below:

```
#create a model matrix X and Y containing the predictors and outputs
x<-model.matrix (violentPerPop~.,crimeViolence)[,-1]
y<-crimeViolence$violentPerPop</pre>
```

To perform the lasso regression, **glmnet()** function from glmnet package is used.

```
#create a grid of values to iterate the lambda grid <- 10^{\land} seq (10,-2, length =100)
```

```
#run lasso regression using alpha = 1 and lambda = grid
lasso.mod =glmnet (x[train ,],y[train],alpha =1, lambda =grid)
```

The alpha value indicates the type regression: ridge (0) and lasso (1). Initially, a grid of values was created to iterate lambda (λ). In this case, *grid* is a variable consisting of sequence of power of 10. In the **glmnet**() function, the value of λ is assigned the variable *grid*.

```
> dim(coef(lasso.mod))
[1] 103 100
```

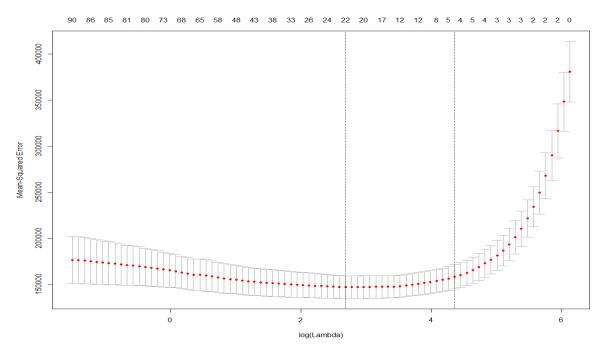
The resultant coefficients of *lasso.mod* is a 103×100 matrix. This means it has 103 rows with the number of variables including an intercept and 100 columns (one for each value of lambda). However, finding the best lambda is a cumbersome task, which leads to using cross validation has to be used to find the best lambda (λ). Function **cv.glmnet()** was used to run a cross validation. The code is as below:

```
#running cross validation using cv.glmnet
cv.crime.out<-cv.glmnet (x[train ,],y[train],alpha =1)</pre>
```

Once the cross validation ran, the output was plotted. The code is shown below:

```
#plot the cross validation output
plot(cv.crime.out)
```

The plot below gives the best value of λ that produces gives the least mean squared error. In this case, the best λ is the one corresponding to 22 degrees of freedom, which implies the variables have been reduced from 103 to 23 variables.



The best λ can be found out using the below code:

```
#get the best lambda
bestlam<-cv.crime.out$lambda.min
bestlam
14.6556082687358
```

The best λ value is approximately 14.6556. This λ value is used to predict the RMSE for the test data, which would correspond to the lowest amongst all the λ values. The test RMSE is around 127741.7, which is comparable to the test RMSE from the best subset selection. The code and output is shown below:

```
#using the bestlam predict the test MSE
lasso.pred<-predict (lasso.mod ,s=bestlam ,newx=x[-train,])
mean((lasso.pred - y[-train])^2)
> mean((lasso.pred - y[-train])^2)
[1] 127741.7
```

The model coefficients were evaluated using glmnet() function on the whole data with alpha = 1 and lambda = bestlam (14.6566). The code is shown below:

```
#predicting the coefficients |
out=glmnet (x,y,alpha =1, lambda =bestlam)
lasso.coef=predict (out ,type ="coefficients",s=bestlam)[1:103,]
lasso.coef[lasso.coef!=0]
```

The *lasso.coef* contains the coefficients of all the variables in the model.

```
> lasso, coef
        (Intercept)
                                                     perHoush
                                                                         pctBlack
                                                                                              pctWhite
                                                                                                                   pctAsian
                                                                                                                                         pctHisp
       1.843002e+03
                            0.000000e+00
                                                 0.000000e+00
                                                                     2.666860e+00
                                                                                         -4.166381e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
          pct12-21
                               pct12-29
                                                   pct16-24
                                                                          pct65up
                                                                                             persurban
                                                                                                                   pctUrban
                                                                                                                                       medIncome
       0.000000e+00
                           -2.101424e+00
                                                 0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                               5.043544e-01
                                                                                                                                    0.000000e+00
                                pctWfarm
           pctwwage
                                                                       pctWsocsec
                                                                                            pctPubAsst
                                                                                                                  pctRetire
                                                                                                                                    medFamIncome
                                                      pctWdiv
                                                0.000000e+00
       0.000000e+00
                            0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
          perCapInc
                            whitePerCap
                                                 blackPerCap
                                                                         NAperCap
                                                                                           asianPerCap
                                                                                                                otherPerCap
                                                                                                                                      hispPerCap
       0.000000e+00
                                                                     0.000000e+00
                                                                                          2.733715e-04
                            0.000000e+00
                                                0.000000e+00
                                                                                                                                    0.000000e+00
                                                                                                               1.100905e-03
                                                                     pctNotHSgrad
        persPoverty
                              pctPovertv
                                                    pctLowEdu
                                                                                           pctCollGrad
                                                                                                                pctUnemplov
                                                                                                                                       pctEmplov
                                                 0.000000e+00
       0.000000e+00
                            0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
                                                                                         pctMaleDivorc
       pctEmployMfg
                      pctEmployProfServ
                                                 pct0ccupManu
                                                                     pctOccupMgmt
                                                                                                              pctMaleNevMar
                                                                                                                                    pctFemDivorc
                                                 0.000000e+00
                                                                     0.000000e+00
                                                                                                               0.000000e+00
      -1.791161e+00
                            0.000000e+00
                                                                                          2.750502e+01
                                                                                                                                    0.000000e+00
       pctAllDivorc
                              persperFam
                                                                      pctKids2Par
                                                                                       pctKids-4w2Par
                                                                                                             pct12-17w2Par
                                                                                                                                   pctworkMom-6
                                                      pct2Par
       0.000000e+00
                            0.000000e+00
                                                0.000000e+00
                                                                     -9.636614e+00
                                                                                          0.000000e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
    pctworkMom-18
                                         pctKidsBornNevrMarr
                                                                                                             pctFanImmia-5
                                                                                                                                  pctFanImmia-8
                       kidsBornNevrMarr
                                                                   numForeianBorn
                                                                                        pctFanImmia-3
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
      -3.151782e+00
                            0.0000000e+00
                                                 5.514086e+01
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                          pctImmia-10
                                                                                                            pctSpeakOnlyEng
                                                                                                                                  pctNotSpeakEng
   `pctFgnImmig-10`
                            `pctImmia-3
                                                 `pctImmia-5
                                                                      pctImmia-8
       0.000000e+00
                            0.000000e+00
                                                0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
                                                                                                            pctPersOwnOccup
     pctLargHousFam
                            pctLargHous
                                            persPerOccupHous
                                                                  persPerOwnOccup
                                                                                    persPerRenterOccup
                                                                                                                                 pctPopDenseHous
       0.000000e+00
                                                                                                               0.000000e+00
                            0.000000e+00
                                                0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                                                    8.465181e+00
                                                                     pctHous0ccup
  pctSmallHousUnits
                            medNumBedrm
                                                 housevacant
                                                                                     pctHousOwnerOccup
                                                                                                           pctVacantBoarded
                                                                                                                                    pctVacant6up
       1.066477e-01
                            0.000000e+00
                                                 5.897551e-03
                                                                     -4.405190e+00
                                                                                          0.000000e+00
                                                                                                               7.643565e+00
                                                                                                                                    0.000000e+00
     medYrHousBuilt
                          pctHousWOphone
                                              pctHousWOplumb
                                                                       ownHousLow0
                                                                                            ownHousMed
                                                                                                               ownHousUper0
                                                                                                                                   ownHousOrange
       0.000000e+00
                            0.000000e+00
                                                0.000000e+00
                                                                     0.000000e+00
                                                                                          0.000000e+00
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
           rentLowO
                                 rentMed
                                                   rentUpperO
                                                                       rent0range
                                                                                          medGrossRent
                                                                                                          medRentpctHousInc
                                                                                                                                   medOwnCostpct
       0.000000e+00
                            0.000000e+00
                                                 0.000000e+00
                                                                                          0.000000e+00
                                                                                                                                    0.000000e+00
                                                                     1.488381e-01
                                                                                                               4.717190e-01
    medOwnCostPctWO
                         persEmergShelt
                                                persHomeless
                                                                   pctForeignBorn
                                                                                     pctBornStateResid
                                                                                                            pctSameHouse-5
                                                                                                                                `pctSameCounty-5
                            0.000000e+00
      -1.072224e+01
                                                 0.000000e+00
                                                                     7.427340e-01
                                                                                          -6.516433e-03
                                                                                                               0.000000e+00
                                                                                                                                    0.000000e+00
    pctSameState-5
                                landArea
                                                   popDensity
                                                                   pctUsePubTrans
                                                                                      pctOfficDrugUnit
       0.000000e+00
                            0.000000e+00
                                                 0.000000e+00
                                                                     0.000000e+00
                                                                                          7.598575e+00
```

This included the coefficients with value equal to zero. However, as mentioned at the beginning of this section, lasso regression's advantage over the ridge regression is its ability to perform variable selection and at the same time provide an accurate model with respect to the bias-variance trade-off. We can obtain the non-zero variables by sub-setting the *lasso.coef* variable. The final set of variables is shown below.

```
> lasso.coef[lasso.coef!=0]
        (Intercept)
                               pctBlack
                                                    pctWhite
                                                                       `pct12-29`
                                                                                             pctUrban
                                                                                                               asianPerCap
                                                                                                                                   otherPerCap
                           2.666860e+00
                                                                                                              2.733715e-04
                                                                                                                                  1.100905e-03
       1.843002e+03
                                               -4.166381e+00
                                                                    -2.101424e+00
                                                                                         5.043544e-01
       pctEmployMfg
                          pctMaleDivorc
                                                 pctKids2Par
                                                                   pctWorkMom-18` pctKidsBornNevrMarr
                                                                                                           pctPopDenseHous
                                                                                                                              pctSmallHousUnits
      -1.791161e+00
                           2.750502e+01
                                               -9.636614e+00
                                                                    -3.151782e+00
                                                                                          5.514086e+01
                                                                                                              8.465181e+00
                                                                                                                                   1.066477e-01
        houseVacant
                           pctHousOccup
                                            pctVacantBoarded
                                                                      rentQrange
                                                                                    medRentpctHousInc
                                                                                                           medOwnCostPctWO
                                                                                                                                 pctForeignBorn
                          -4.405190e+00
                                                                                                             -1.072224e+01
       5.897551e-03
                                                7.643565e+00
                                                                     1.488381e-01
                                                                                         4.717190e-01
                                                                                                                                  7.427340e-01
  pctBornStateResid
                       pctOfficDrugUnit
      -6.516433e-03
                           7.598575e+00
```

4. Final Model Selection for the crime dataset

For the final model, we have to edit the data to contain only the output variable and the predictor variables from the lasso regression since it is more efficient than the subset selection method, both backward and forward. In addition, ridge regression does not aid in variable selection although it is an accurate model.

```
#creating a vector with the new variables whose coefficients are not 0
newVariables<-names(lasso.coef[lasso.coef!=0][-1])
newVariables<-c("pctBlack","pctWhite","pct12-29","pctUrban","asianPerCap","otherPerCap","pctEmployMfg",
             pctMaleDivorc","pctKids2Par","pctWorkMom-18","pctKidsBornNevrMarr","pctPopDenseHous",
             pctSmallHousUnits","houseVacant","pctHousOccup","pctVacantBoarded","rentQrange","medRentpctHousInc","
            I'medOwnCostPctWO", "pctForeignBorn", "pctBornStateResid", "pctOfficDrugUnit", "violentPerPop")
crimeViolenceFinalData<-crimeViolence[newVariables]</pre>
> str(crimeViolenceFinalData)
'data.frame': 1901 obs. of 23 variables:
 $ pctBlack : num 1.37 0.8 0.74 2.51 1.6 ...
$ pctWhite : num 91.8 95.6 94.3 95.7 96.6 .
                      : num 91.8 95.6 94.3 95.7 96.6 ...
 $ pct12-29
                      : num 21.4 21.3 25.9 32.9 27.4 ...
 $ pctUrban
: num 100 100 100 100 100 100 100 100 100 ...
 $ pctKidsBornNevrMarr: num 0.36 0.24 0.88 1.58 1.18 4.66 1.64 4.71 2.47 7.44 ...
 $ pctPopDenseHous : num 0.39 1.01 2.03 2.11 1.47 ...
 $ pctSmallHousUnits : num 11.1 23.6 47.5 53.2 47.4 ...
 $ housevacant : int 64 240 544 5119 566 2051 1562 5606 1807 714 ...
 $ pctHousOccup : num 98.4 97.2 95.7 91.8 95.1 ...
 $ pctVacantBoarded : num 3.12 0 0.92 2.09 1.41 6.39 0.45 5.64 2.77 3.78 ...
 $ rentorange : int 316 205 150 134 361 139 146 177 142 190 ...
 $ medRentpctHousInc : num 23.8 27.6 24.1 26.4 24.4 26.3 25.2 29.6 23.8 33 ...
 $ medOwnCostPctWO : num 14 12.5 11.6 11.7 12.5 12.2 12.8 13 12.9 11.8 ...
$ pctForeignBorn : num 10.66 8.3 5 1.49 9.19 ...
 $ pctBornStateResid : num 53.7 77.2 44.8 64.3 77.3 ...
 $ pctOfficDrugUnit : num 0 0 0 0 0 0 6.57 0 0 ...
                  : num 41 128 219 443 227 ...
 $ violentPerPop
```

This dataset was used to perform linear regression and regression tree.

4.1 Linear Regression

The model was run against all the predictor variables on the training dataset. The code is shown below:

```
#linear regression model on the complete set of variables, performed on the training data lm.fit<-lm(violentPerPop~.,data=crimeViolenceFinalData[train,]) summary(lm.fit)
```

The summary gives the various summaries of the result of the linear regression.

```
> summary(1m.fit)
call:
lm(formula = violentPerPop ~ ., data = crimeViolenceFinalData[train,
Residuals:
    Min
               10 Median
                                  30
                                          Max
-1507.29 -190.93 -35.36
                             130.19 2455.02
Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
                     1.687e+03 4.468e+02 3.776 0.000166 ***
8.192e+00 2.378e+00 3.445 0.000590 ***
(Intercept)
                     8.192e+00 2.378e+00
                                            3.445 0.000590 ***
pctBlack
                    8.289e-01 2.118e+00 0.391 0.695656
pctWhite
                    -5.596e+00 2.159e+00 -2.592 0.009654 **
 pct12-29`
pct∪rban
                    5.385e-01 2.581e-01 2.086 0.037143 *
asianPerCap
                    2.137e-03 1.177e-03 1.815 0.069731
otherPerCap
                    3.307e-03 1.293e-03 2.557 0.010656 *
                  -4.245e+00 1.487e+00 -2.854 0.004379 **
pctEmployMfq
pctMaleDivorc
pctKids2Par
`pctWorkMom-18`
                    3.653e+01 6.775e+00 5.392 8.26e-08 ***
                    -9.023e+00 2.836e+00 -3.182 0.001498 **
                    -4.770e+00
                                1.835e+00 -2.599 0.009444 **
pctKidsBornNevrMarr 5.614e+01 8.873e+00 pctPopDenseHous 1.315e+01 3.803e+00
                                            6.327 3.43e-10 ***
                                            3.457 0.000565 ***
pctSmallHousUnits 4.519e-01 1.343e+00 0.336 0.736631
houseVacant 5.982e-03 1.391e-03 3.762 1.00682 *
nctHousOccup -6.612e+00 2.586e+00 -2.557 0.010682 *
                    5.982e-03 1.591e-03 3.761 0.000177 ***
pctVacantBoarded 6.732e+00 3.466e+00 1.942 0.052295 .
                    2.923e-01 1.555e-01 1.880 0.060329 .
rentQrange
medRentpctHousInc 6.134e+00 4.451e+00 1.378 0.168364
medownCostPctWO -3.313e+01 8.217e+00 -4.033 5.83e-05 ***
                                            1.013 0.311016
pctForeignBorn
                    2.771e+00 2.734e+00
pctBornStateResid 4.128e-01 8.239e-01
                                             0.501 0.616411
                    8.519e+00 4.040e+00 2.109 0.035144 *
pctOfficDrugUnit
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 361.5 on 1307 degrees of freedom
Multiple R-squared: 0.6644, Adjusted R-squared: 0.6587
F-statistic: 117.6 on 22 and 1307 DF, p-value: < 2.2e-16
> lm.pred<-predict(lm.fit,crimeViolenceFinalData[-train,])</pre>
> mean((lm.pred-crimeViolenceFinalData[-train,]$violentPerPop)^2)
[1] 127357
```

The above output gives significance values attached to each of the coefficients of the variables. The model's F-statistic is < 2.2e-16 which suggests the model is significant. The multiple R-square is 0.6644 and the adjusted R-square is 0.6587. The RMSE of the base model is 127,357. The endeavor of this analysis was to find a model that takes into consideration bias variance trade-off, multi-collinearity and improving adjusted R-square.

The first step was to check for correlation between the variables and variance inflation factor (VIF). This is useful in checking for multi-collinearity present in the model. The **cor**() function was used to create a correlation matrix between the variables of the dataset and **vif**() function was used to calculate the VIF values for each variable.

```
#correlation matrix cor(crimeViolenceFinalData)
```

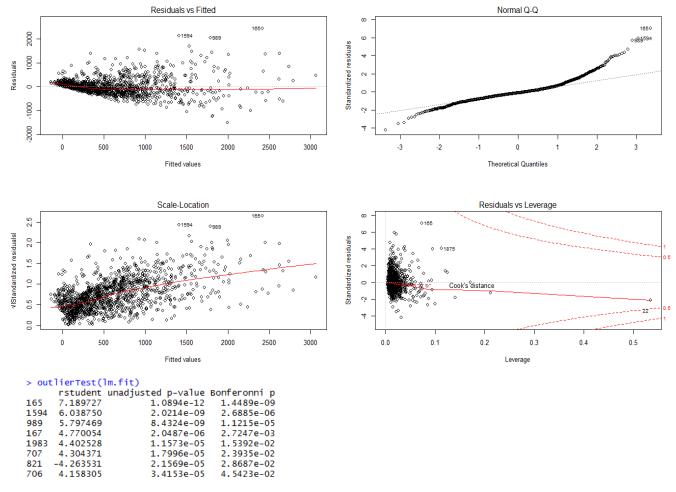
```
pctBlack
                                                     pctWhite
-0.79612281
                                                                            pct12-29
                                                                                                 pctUrban
                                                                                                                   asianPerCap
                                                                                                                                        otherPerCap
                                                                                                                                                           pctEmployMfg pctMaleDivorc pctKids2Par
-0.0167747211 0.39851223 -0.73022541
                                 1.000000000
pctBlack
                                                                         0.12170807
                                                                                           -0.001108497
                                                                                                                -0.1079634624
                                                                                                                                       -0.089816523
pctWhite
pct12-29
                                 -0.796122809
0.121708069
                                                         . 00000000
                                                                            22060335
                                                                                            -0.048983008
                                                                                                                 0.1421262378
                                                                                                                                        0.101630404
                                                                                                                                                            0.0330027766
                                                                                                                                                                                     -0.33658011
                                                                                                                                                                                                        0.69943035
                                                                                                                                                                                                         -0.21258113
                                                                                            -0.110376102
                                                                                                                 0.2867100401
                                                                                                                                          .132139504
                                                                                                                                                            0.1161581698
                                                                            00000000
                                                                                                                                                                                     -0.05865820
.
pcturban
                                 -0.001108497
                                                      0.04898301
                                                                         -0.11037610
                                                                                            1,000000000
                                                                                                                 0.0826915977
                                                                                                                                        0.136647402
                                                                                                                                                            -0.1027644712
                                                                                                                                                                                     -0.06292618
                                                                                                                                                                                                         0.10426066
asianPerCap
otherPerCap
                                -0.107963462
-0.089816523
                                                      0.14212624
0.10163040
                                                                        -0.28671004
-0.13213950
                                                                                               .082691598
.136647402
                                                                                                                                          .150449248
                                                                                                                                                            0.0008427735
-0.0398265231
                                                                                                                                                                                     -0.21571294
-0.17813689
                                                                                                                                                                                                         0.27059974
0.24801178
                                                                                                                    0000000000
                                                                                                                 0.1504492476
pctEmployMfg
pctMaleDivorc
                                 -0.016774721
                                                      0.03300278
                                                                        -0.11615817
                                                                                            -0.102764471
                                                                                                                 0.0008427735
                                                                                                                                          .039826523
                                                                                                                                                            1.0000000000
                                                                                                                                                                                      0.04880237
                                                                                                                                                                                                        -0.02425829
                                 0.398512233
                                                      0.33658011
                                                                        -0.05865820
                                                                                            -0.062926182
                                                                                                                 0. 21 571 294 32
                                                                                                                                          178136891
                                                                                                                                                               0488023678
                                                                                                                                                                                      1.00000000
                                                                                                                                                                                                        -0.71154415
pctKids2Par
pctworkMom-18
                                 0.093261430
                                                      0.15319060
                                                                         0.02467978
                                                                                            -0.063588039
                                                                                                                 -0.0982906320
                                                                                                                                          .009030479
                                                                                                                                                            0.0907257482
                                                                                                                                                                                      0.10590772
                                                                                                                                                                                                         0.02553232
nctKidsBornNevrMarr
                                 0.805987508
                                                      0 79869868
                                                                         0 24755725
                                                                                            0.012412963
                                                                                                                -0 1949514656
                                                                                                                                        0 160074201
                                                                                                                                                            0.0413104084
                                                                                                                                                                                      0.47703650
                                                                                                                                                                                                        -0.85907269
                                 0.106760074
0.230687625
                                                         59611933
                                                                                               046818216
                                                                                                                                                               0449163617
                                                                                                                                                                                      0.10595398
pctPopDenseHous
pctSmallHousUnits
                                                     -0.36829823
                                                                         0.28453013
                                                                                                                                                                                      0.57164732
                                                                                            -0.025579618
                                                                                                                -0.2484797130
                                                                                                                                       -0.190387391
                                                                                                                                                            -0.0627126101
                                                                                                                                                                                                        -0.63612379
.
housevacant
                                 0.178274385
                                                     -0.19405335
                                                                         0.02866199
                                                                                            0.120718521
                                                                                                                -0.0479523642
                                                                                                                                       -0.040598164
                                                                                                                                                            -0.1176446047
                                                                                                                                                                                      0.18287795
                                                                                                                                                                                                        -0.21789493
                                 -0.176977377
0.471390664
                                                      0.10976775
-0.44124639
                                                                                                                                                                                      0.31802374
                                                                            05426459
                                                                                               143687623
                                                                                                                 0.0702500609
                                                                                                                 -0.1246136282
                                                                                                                                        0.118070615
                                                                                                                                                            -0.0096422638
                                                                                                                                                                                      0.31807409
pctVacantBoarded
                                                                         0.06571658
                                                                                            0.018833126
                                                                                                                                                                                                        -0.51140007
rentorange
                                 -0.148904031
                                                      0.07771463
                                                                         -0.16395706
                                                                                            0.226358768
                                                                                                                 0.2556612917
                                                                                                                                        0.211353859
                                                                                                                                                           -0.1113090020
                                                                                                                                                                                     -0.39521112
                                                                                                                                                                                                        0.33055177
medRentpctHousInc
medOwnCostPctWO
                                 0.184448871
0.216758656
                                                                                                                                       -0.052407676
0.032855567
                                                      -0.33177946
                                                                            29995579
                                                                                               .023941261
                                                                                                                 0.1310458147
                                                                                                                                                           -0.2755652208
                                                                                                                                                                                      0.09422160
                                                                                                                                                                                                        -0.36317165
                                                     -0.05770524
                                                                         -0.08660812
                                                                                            -0.019351974
                                                                                                                 0.0229028198
                                                                                                                                                                                     -0.05822100
pctForeianBorn
                                 -0.092416524
                                                    -0.38803015
                                                                         0.07031523
                                                                                            0.275071971
                                                                                                                 0.0469447689
                                                                                                                                        0.065197471
                                                                                                                                                           -0.0296992810
                                                                                                                                                                                     -0.11492294
                                                                                                                                                                                                        -0.03369781
pctBornStateResid
pctOfficDrugUnit
                                                     0.11677719
-0.25849976
                                                                                                                                       -0.100206038
-0.022221617
                                 0.090748436
                                                                        -0.04831816
                                                                                            -0 226344705
                                                                                                                 -0 0523206557
                                                                                                                                                            0 3418906347
                                                                                                                                                                                     -0.05125950
                                                                                                                                                                                                        -0.06276262
                                                                                                                                                                                     0.22033626 -0.28928097
0.51663043 -0.72815910
                                 0.252640272
                                 0.625339003 -0.67719557
violentPerPop
                                                                         0.10993216
                                                                                            0.073954613
                                                                                                                -0.1331356171
                                                                                                                                      -0.100414879
                                                                                                                                                           -0.0576949244
                                pctWorkMom-18 pctKidsBornNevrMarr pct
0.093261430 0.80598751
                                                                                            onDenseHous
                                                                                                               pctSmallHousUnits
                                                                                                                                             houseVacant pctHousOccup
0.178274385 -0.17697738
                                                                                                                                                                                      pctVacantBoarded
                                                                                                                                                                                             0.471390664
-0.441246392
                                                                                                                          -0.36829823
                                                                                                                                                                    0.10976775
                                                                                                                                                                                                                  0.077714626
pctWhite
                                   0.153190599
                                                                   -0.79869868
                                                                                             -0.59611933
                                                                                                                                             -0.194053349
pct12-29
                                   0.024679778
                                                                    0.24755725
                                                                                              0.25574512
                                                                                                                           0.28453013
                                                                                                                                             0.028661994
                                                                                                                                                                    0.05426459
                                                                                                                                                                                              0.065716577
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                                  -0.063588039
-0.098290632
                                                                    0.01241296
                                                                                              0.04681822
                                                                                                                          -0.02557962
                                                                                                                                             0.120718521
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                                                                                                                                                                                              0.018833126
                                                                                                                                                                                                                  0.226358768
                                                                                                                          -0.24847971
                                                                                              -0.15569186
                                                                                                                                                                                             -0.124613628
asianPerCap
                                                                    -0.19495147
                                                                                                                                             -0.047952364
                                                                                                                                                                    0.07025006
                                                                                                                                                                                                                  0.255661292
otherPerCan
                                   0.009030479
                                                                    -0.16007420
                                                                                             -0.11637886
                                                                                                                          -0.19038739
                                                                                                                                             -0.040598164
                                                                                                                                                                    0.09609754
                                                                                                                                                                                             -0.118070615
                                                                                                                                                                                                                  0.211353859
pctEmployMfg
pctMaleDivorc
                                   0.090725748
0.105907721
                                                                    0.04131041
0.47703650
                                                                                              0.04491636
0.10595398
                                                                                                                          -0.06271261
0.57164732
                                                                                                                                             -0.117644605
0.182877953
                                                                                                                                                                                             -0.009642264
0.318074095
                                                                                                                                                                                                                 -0.111309002
-0.395211121
                                                                                                                                                                       30177818
                                                                                                                                                                    0.31802374
pctKids2Par
                                   0.025532317
                                                                    -0.85907269
                                                                                             -0.33138574
                                                                                                                          -0.63612379
                                                                                                                                             -0.217894932
                                                                                                                                                                    0.32512759
                                                                                                                                                                                             -0.511400072
                                                                                                                                                                                                                  0.330551766
pctWorkMom-18
pctKidsBornNevrMar
                                                                                                                          -0.02817173
0.46515535
                                   1.000000000
                                                                    -0.07798889
                                                                                             -0.38638258
                                                                                                                                             -0.070989669
                                                                                                                                                                    0.04356815
                                                                                                                                                                                             -0.175937801
                                                                                                                                                                                                                  -0 125645390
                                                                                                                                              0.242113540
                                                                                                                                                                                                                -0.145358721
-0.035763760
pctPopDenseHous
                                  -0.386382580
                                                                    0.39601169
                                                                                              1.00000000
                                                                                                                           0.42269478
                                                                                                                                              0.091344755
                                                                                                                                                                   -0.03062160
                                                                                                                                                                                              0.195483438
 octSmallHousUnits
                                  -0.028171735
                                                                    0.46515535
                                                                                              0.42269478
                                                                                                                           1.00000000
                                                                                                                                              0.189122644
                                                                                                                                                                   -0.31762911
                                                                                                                                                                                              0.168056075 -0.235016663
                                                                                             0.09134476
-0.03062160
                                   0.043568154
pctHousOccup
                                                                    -0.17647692
                                                                                                                          -0.31762911
                                                                                                                                             -0.190983491
                                                                                                                                                                    1.00000000
                                                                                                                                                                                             -0.159310997
                                                                                                                                                                                                                  0.133240348
nctVacantBoarded
                                  -0.175937801
                                                                    0.55580817
                                                                                              0.19548344
                                                                                                                           0.16805608
                                                                                                                                             0.222099655
                                                                                                                                                                    -0.15931100
                                                                                                                                                                                              1.000000000
                                                                                                                                                                                                                 -0.115316371
rentQrange
medRentpctHousInc
                                  -0.125645390
-0.201289041
                                                                    -0.14535872
0.34073451
                                                                                              -0.03576376
0.34459176
                                                                                                                          -0.23501666
0.33895331
                                                                                                                                             -0.001808993
0.081046531
                                                                                                                                                                    0.13324035
-0.21338804
                                                                                                                                                                                              0.115316371
                                                                                                                                                                                                                  1.000000000
0.150771779
                                                                                                                                                                                              0.155632784 0.177622287
medOwnCostPctwO
                                  -0.013441573
                                                                    0.20630820
                                                                                             -0.14367608
                                                                                                                           0.05736692
                                                                                                                                              0.014706191
                                                                                                                                                                    -0.14314070
                                                                                                                                                                                                                  0.159421108
                                  -0.351858095
0.133704735
                                                                                             0.72823854
-0.24781275
                                                                                                                          0.33393437
-0.21465234
                                                                                                                                             0.088702672
-0.097702619
                                                                                                                                                                    0.09253142
                                                                                                                                                                                             -0.046217517
0.158786006
                                                                                                                                                                                                                0.303191573
-0.218091613
pctForeignBorn
                                                                    0.15043728
                                                                    0.02592819
pctBornStateResid
pctOfficDrugUnit
violentPerPop
                                  -0.047004403
                                                                    0.31197280
                                                                                              0.11025193
                                                                                                                           0.22979470
                                                                                                                                             0.240768533
                                                                                                                                                                   -0.07297227
                                                                                                                                                                                              0.203275365 0.014780519
                                  -0.141478711
                                                         0.73961847

OWNCOSTPCTWO PETFOREIGNER
0.21675866 -0.092416
-0.03770524 -0.388031
-0.08660812 0.070311
-0.01935197 0.275073
-0.02590282 0.046944
0.03259240 -0.029699
-0.05822100 -0.114922
-0.12829139 -0.033699
-0.13829139 -0.33699
-0.13829139 -0.33699
-0.13829139 -0.33699
-0.1434157 0.0582603
-0.1766229 0.333934
-0.143457608 0.728233
-0.14344070 0.092531
-0.17762229 -0.04621,1
-0.15942111 0.308191
0.8866136 0.298866
-0.17130435 -0.475354
-0.05246134 0.201644
                                                                    0.73961847
                                                                                              0.40294564
                                                                                                                       0.46610650
pctofficorugunit
0.25264027
-0.2584907
0.07947460
0.22458477
-0.05912096
-0.02222162
-0.0799639
0.2203162
-0.88928097
-0.04700440
0.31197280
0.11025193
0.2297947
0.24076853
-0.07297227
0.20327536
0.01478052
0.1098229
0.05127715
0.12789469
0.11705261
1.0000000
0.31912127
                                                                                                                           0.46610650
                                                                                                                                             0.288353604
                                                                                                                                                                   -0.25561333
                                                                                                                                                                                              0.475130968 -0.115718678
                                  ntpctHousInc m
0.18444887
                                                                                          orn pctBornStateR
                                                                                                                                              violentPerPop
0.62533900
pctBlack
pctWhite
pct12-29
pctUrban
asianPerCap
otherPerCap
pctEmployMfg
pctMaleDivorc
pctKids2Par
pctWorkMom-18
pctKidsBornNevrMarr
pctPopDenseHous
pctSmall Housunits
housevacant
pctHousDocCup
pctVacantBoarded
rentQrange
medRentpctHousInc
medOwnCostPctWo
pctForeIgnBorn
pctBornStateResid
pctOfficDrugunit
                                                                                                       0.09074844
0.11677719
-0.04831816
-0.22634471
-0.05232066
-0.10020604
-0.05125950
0.06276262
0.13370474
0.02592819
-0.24781275
-0.24781275
-0.1465234
-0.09770262
0.17938707
0.15878601
-0.28887179
0.17190435
-0.47753475
                                                                               -0.38803015
0.07031523
0.27507197
0.04694477
0.06519747
-0.02969928
-0.11492294
-0.03369781
-0.35185810
0.15043728
0.7282384
0.33393437
0.08870267
0.09253142
-0.04621752
0.330319157
                                                                               0.02413511
                                       29886841
22887179
                                                                                                                                                    . 20164666
. 08666947
pctOfficDrugUnit
violentPerPop
                                    0.10982595
0.31135051
                                                                                                       -0.11705261
-0.08666947
                                                                                                                               0.31912127
```

In addition to this, the variance inflation factor (VIF) values can be calculated.

<pre>vif(lm.fit)</pre>					
pctBlack	pctWhite	`pct12-29`	pct∪rban	asianPerCap	otherPerCap
11.521016	12.633484	1.710365	1.341629	1.215820	1.125621
pctEmployMfg	pctMaleDivorc	pctKids2Par	`pctWorkMom-18`	pctKidsBornNevrMarr	pctPopDenseHous
1.447163	3.737126	11.767610	1.428727	7.980885	5.361674
pctSmallHousUnits	houseVacant	pctHousOccup	pctVacantBoarded	rentQrange	medRentpctHousInc
3.606784	1.169145	1.717957	1.704862	1.732170	1.693879
medOwnCostPctWO	pctForeignBorn	pctBornStateResid	pctOfficDrugUnit		
1.451586	5.900580	2.008470	1.283560		

From the data above, one can see that pctBlack, pctWhite, pctKids2Par, pctKidsBornNevrMarr have high VIF values. From the correlation matrix we can observe that pctBlack and pctWhite are highly correlated and pctWhite has a high p-value. Hence, pctWhite can be removed from the model. It is also observed that pctKidsBornNevrMarr and pctKids2Par have high VIF values and they are highly correlated. We can remove pctKids2Par. Similarly, any variable with high p-value were removed. Before performing the next iteration of the regression analysis, the model was tested for outliers and leverage points.



It can be observed that observations 165, 1594, and 989 are outliers and have influence in the OLS fit and observation 22 is a high leverage point. These points were deleted and the new model was run.

```
> summary(lm.fit2)
call:
lm(formula = violentPerPop ~ . - pctWhite - asianPerCap - medRentpctHousInc -
    pctSmallHousUnits - pctHousOccup - pctVacantBoarded - pctOfficorugUnit -
    pctForeignBorn - pctBornStateResid, data = crimeviolenceFinalData2[train,
])
                                               Median
-31.79
 Min 1Q
-1367.84 -172.34
                                                                    3Q Max
120.14 1729.53
Coefficients:
                                                   Estimate Std. Error t value Pr(>|t|)
1.627e+03 2.636e+02 6.173 8.91e-10 ***
8.374e+00 1.277e+00 6.557 7.89e-11 ***
4.962e+00 1.209e+00 -2.904 0.003748 **
2.348e-03 1.137e-03 2.065 0.039149 **
3.355e+00 1.215e+00 -2.927 0.003478 **
2.901e+01 5.581e+00 5.199 2.33e-07 ***
1.215e+01 2.240e+00 -5.423 6.97e-08 ***
6.061e+00 1.615e+00 5.423 6.98e-08 ***
4.371e+01 8.061e+00 5.423 6.98e-08 ***
1.581e+01 2.003e+00 7.893 6.18e-15 ***
(Intercept)
pctBlack
'pct12-29'
pctUrban
otherPerCap
pctEmployMfg
pctMaleDivorc
pctKids2Par
'pctWorkMom-18'
rctKids2pcnNewr
                                                 Estimate

1.627e+03

8.374e+00

-4.962e+00

6.567e-01

2.348e-03

-3.555e+00

2.901e+01

-1.215e+01

-6.061e+00

4.371e+01
                                                                           8.061e+00
2.003e+00
2.410e-03
 pctKidsBornNevrMarr
                                                   4.371e+01
1.581e+01
  pctPopDenseHous
                                                                                                         7.893 6.18e-15 ***
8.273 3.18e-16 ***
 houseVacant
                                                   1.994e-02
 rentQrange
medOwnCostPctWO
                                               4.174e-01 1.294e-01
-2.350e+01 6.965e+00
                                                                                                         3,226 0,001286
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 334.9 on 1313 degrees of freedom
(3 observations deleted due to missingness)
Multiple R-squared: 0.664, Adjusted R-squared: 0.6606
F-statistic: 199.6 on 13 and 1313 DF, p-value: < 2.2e-16
  > lm.pred2<-predict(lm.fit2,crimeViolenceFinalData2[-train,])</pre>
  > mean((lm.pred2-crimeViolenceFinalData2[-train,]$violentPerPop)^2)
   [1] 146042.6
```

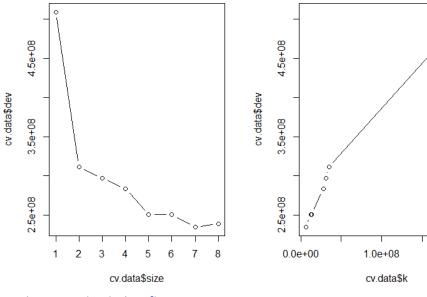
It can be observed that all the variables in the model are now significant and there has been an increase in the adjusted R-squared as well, which suggests that it is a better fit. However, there was also an increase in the RMSE for this model.

4.2 Regression Trees

Regression trees are easy to explain and are easily interpretable. Trees can be displayed graphically with the help of plot functions. In the analysis of the dataset, it is consider using a pruned tree using a cross-validation approach. The code is given below:

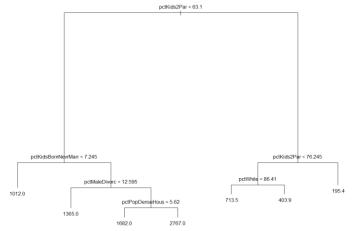
```
set.seed(10)
tree.data<-tree(violentPerPop~.,crimeViolenceFinalData1[train,])
cv.data =cv.tree[tree.data,FUN=prune.tree)|
par(mfrow =c(1,2))
plot(cv.data$size ,cv.data$dev ,type="b")
plot(cv.data$size ,cv.data$dev ,type="b")</pre>
```

The corresponding plot is shown below:



prune.data =prune.tree (tree.data,best = 7)
par(mfrow =c(1,1))
plot(prune.data)
text(prune.data,pretty=0,xpd=TRUE)
tree.pred1=predict(prune.data,crimeViolenceFinalData1[-train,])
mean((tree.pred1-crimeViolenceFinalData1[-train,]\$violentPerPop)^2)
> mean((tree.pred1-crimeViolenceFinalData1[-train,]\$violentPerPop)^2)
[1] 166975.5

The model was run for tree size 7 and the mean was calculated. The RMSE of this model was higher than that of the linear regression model. Next, the random forest model was applied to check model efficiency.



2.0e+08

4.3 Random Forests

Random forests give models that have low variance. Another model that was considered during this analysis was bagging. Though bagging improves the accuracy over using a single tree, it is hard to interpret the

model. Random forest on the other hand is a very efficient learning method. It builds on the idea of bagging, but it de-correlates the trees, thereby reducing the variance of the whole model. For each tree, each time a split in a tree is considered, a random sample of m predictors is chosen as split candidates from among the p predictors. We calculate the value of m through iteration using the code below:

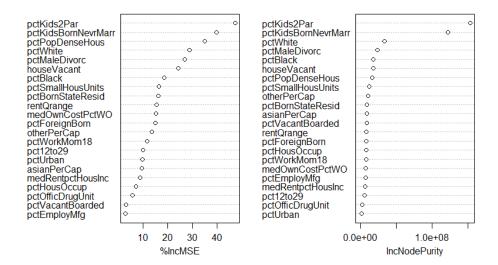
```
library(randomForest)
set.seed(5)
par(mfrow = c(1,1))
result<-NULL
for(k in 1:22){
  rf.model<-randomForest(violentPerPop~.,crimeViolenceFinalData1[train,],mtry=k,importance=TRUE,ntree=1501)
  pred.value<-predict(rf.model,crimeViolenceFinalData1[-train,]</pre>
  error<-mean((pred.value-crimeViolenceFinalData1[-train,]$violentPerPop)^2)
  result<-rbind(result,c(k,error))
plot(result,xlab="number of variables",ylab="misclassification",type="b")
                                                                                                > result
    130000
                                                                                                       [,1]
                                                                                                            130347.1
                                                                                                          2
                                                                                                            123613.4
                                                                                                 [2,]
    128000
                                                                                                            122348.4
                                                                                                  [3,]
                                                                                                  [4,]
                                                                                                          4 122087.4
Root mean squared error
                                                                                                          5 121563.9
                                                                                                 [6,]
                                                                                                          6 121728.2
    126000
                                                                                                            120987.9
                                                                                                 Γ8.
                                                                                                          8 121512.8
                                                                                                 [9.]
                                                                                                          9 121621.5
                                                                                                         10 120902.8
                                                                                                Γ10,]
    124000
                                                                                                [11.]
                                                                                                         11 121139.1
                                                                                                [12,]
                                                                                                         12 120702.4
                                                                                                [13,]
                                                                                                         13 120907.2
    122000
                                                                                                [14,]
                                                                                                            120660.7
                                                                                                [15,]
                                                                                                         15 121318.3
                                                                                                 [16,]
                                                                                                         16 121479.3
                                                                                                [17,]
                                                                                                         17 121074.1
                                                                                                [18.]
                                                                                                         18 121196.8
                                                                                                [19,]
                                                                                                         19 121460.4
                       5
                                       10
                                                       15
                                                                        20
                                                                                                [20,]
                                                                                                         20 121338.5
                                                                                                [21,]
                                                                                                         21 121580.7
                                                                                                Γ22.1
                                     number of variables
                                                                                                         22 121721.1
```

From the graph above and the predictors' result table, it can be inferred that mtry=14 gives the least test error. The code below with mtry=14 gives RMSE as 120,993 which is far better than the pruned tree.

```
> set.seed(1111)
> rf.model-randomForest(violentPerPop<.,crimeViolenceFinalData1[train,],mtry=14,importance=TRUE,ntree=1501)
> pred.value<-predict(rf.model,crimeViolenceFinalData1[-train,])
> mean((pred.value-crimeViolenceFinalData1[-train,]$violentPerPop)^2)
[1] 120993.3
```

We can get the variable importance using the **varImpPlot()** and the **importance()** function. The importance plots are shown below:

```
> importance(rf.model)
                        %IncMSE IncNodePurity
3.596190 18203135
pctBlack
                      18.596190
pctWhite
                      28.775650
                                       33598239
pct12to29
                       9.937725
                                        5907633
pctUrban
                       9.631237
                                        1885728
                     9.427520
13.553577
asianPerCap
                                        8874904
                                      10690219
otherPerCap
                       2.752074
pctMaleDivorc
                      26.849688
                                      23989813
pctKids2Par
                      47.423263
                                     152828219
pctWorkMom18
                      11.634477
                                        8042306
                     39.749917
                                     122037269
pctKidsBornNevrMarr
pctPopDenseHous
                      35.042508
                                       16782115
pctSmallHousUnits
                     16, 321099
                                      12394226
houseVacant
                      24.321962
pctHous0ccup
                       6.997586
                                        8191062
pctVacantBoarded
                       3.141162
                                        8824431
rentQrange
                     15.467322
                                        8657224
medRentpctHousInc
                       8.751142
                                        6805535
medOwnCostPctWO
                     15.139890
                                        7358574
pctForeignBorn
                      14.988458
                                        8520580
pctBornStateResid
                     16.246287
                                        9170241
pctOfficDrugUnit
                       5.722735
                                        2587255
```



It can be interpreted that pctKids2Par, pctKidsBornNevrMarr, pctPoPDenseHous, pctWhite, pctMaleDivorc, houseVacant, and pctBlack are important variables to be considered when predicting violent crime per population (violentPerPop).

5. Conclusion

The final variables obtained from the lasso regression has 23 variables including the intercept term. Some of the variables are pctUrban (percentage of people living in areas classified as urban), pctBlack (percentage of population that is African American), pctWhite (percentage of population that is Caucasian) pctKidsBornNeverMar (percentage of kids born to never married), pctPersDenseHous (percent of persons in dense housing (more than 1 person per room), pctHousLess3BR (percent of housing units with less than 3 bedrooms), housevacant (number of vacant households), pctHousOccup (percent of housing occupied), and pctOfficDrugUnit (percent of officers assigned to drug units). Based on our everyday life and intuition, with information from news channels and the internet, it can be observed that these variables influence crimes in our cities.

However, lasso regression does not give the significance attached to each variable with respect to the output and the data at hand. This can be evaluated using other regression models such as linear regression or regression trees, which gives a better understanding of how the predictor variables influence the output.

Of the three models we have to choose a model that can predict the violent crimes accurately. The pruned tree has the highest test error among the three models chosen for final model prediction. The pruned tree and the linear regression models are easy to interpret when compared to the random forest. Though both the variables and the model are significant in the multiple linear regression model, the test error rate is really high when compared to the random forest model. This could be because of high variance that is inherent in the linear regression model. Yet, random forests approach has the lowest test error rate. However, this comes at the price of model interpretability.

Overall, the RMSE of regression trees was over 128,000 while RMSE for linear regression was 127,357. The RMSE for backward stepwise selection was 122,106 while random forest had the lowest RMSE of

120,993. Thus this data analysis that violentPerPop (violent crime per population) is most heavily influenced by pctBlack, pctWhite, pct12to29, and pctUrban variables.

6. Project Team Contribution

This is a brief overview of the tasks that each member contributed to the project.

Team name:	Pine				
Title:	"Analyzing Crime Rates in America: Data Analytics Approach				
Last Name	First Name	Tasks performed (briefly summarize what each person did in the project)			
Bhatt	Nipur	Ridge Regression			
Choi	Jongwoon	Backward Selection			
Gonzalez	Karla	Literature Review, Concised & Revised Project Proposal and the Final Paper			
Venkateswaran	Bharadwaj	Lasso Regression			

7. Reference

Chen, H., W. Chung, J.J. Xu, G. Wang, Y. Qin, and M. Chau. "Crime Data Mining: A General Framework and Some Examples." Computer 37.4 (2004): 50-56. Wiley. Web. 20 Apr. 2016.

Levy, Francesca. "America's Safest Cities." Forbes. Forbes Magazine, n.d. Web. 27 Apr. 2016.

McMillen, Daniel P., "Issues in Spatial Data Analysis" Journal of Regional Science, Vol. 50, Issue 1. (2009):119-141.Wiley.Web. 20 Apr. 2016.

Source for the dataset:

Creator: Michael Redmond; Computer Science; La Salle University; Philadelphia, PA, 19141, USA

Culled from 1990 US Census, 1995 US FBI Uniform Crime Report, 1990 US Law Enforcement Management and Administrative Statistics Survey, available from ICPSR at U of Michigan.