

Naïve Bayes

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- Overview

• Learn $f(x)$ $x \rightarrow y$

↳ $P(y|x)$

• Using $P(x|y)$

• Via Bayes $\rightarrow P(x|y)P(y)$

* Bayes classifier: $\hat{y} = \arg \max_y P(Y=y | X=x)$

* Simple framework $\rightarrow Y$ is K classes
all x_p are binary (BOW)

↳ parameters from data: $K(2^P - 1)$

* Assumption:

- Features are independent given the class $Y=y$!

$$P(x_1, \dots, x_P | Y) = \prod_{i=1}^P P(x_i | Y)$$

↳ parameters $K \times P$

Ex

	dog	cat	mouse	class
D_1	1	0	0	pets
D_2	0	0	0	food
\vdots	0	1	1	pets

D_n		0		1		0		pets
		0		0		1		food
				\uparrow				\uparrow
				$\frac{2}{3} \mid Y = \text{pets}$				$P(Y)$
				$\frac{0}{2} \mid Y = \text{food}$				$(\frac{3}{5}, \frac{2}{5})$
								pets, food

Laplacian Smoothing