Social network Graph Link Prediction - Facebook Challenge

Problem statement:

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

Data Overview

Taken data from facebook's recruting challenge on kaggle https://www.kaggle.com/c/FacebookRecruiting data contains two columns source and destination eac edge in graph

- Data columns (total 2 columns):
- source_node int64
- destination_node int64

Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he
 followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on
 these features to predict link.
- · Some reference papers and videos :
 - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
 - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf
 - https://www.youtube.com/watch?v=2M77Hgy17cg

Business objectives and constraints:

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

Performance metric for supervised learning:

from sklearn.cluster import MiniBatchKMeans, KMeans

from sklearn.ensemble import RandomForestClassifier from sklearn.model_selection import RandomizedSearchCV

from scipy.sparse.linalg import svds, eigs

from scipy.stats import randint as sp randint

from scipy.stats import uniform

from sklearn.model_selection import train_test_split, StratifiedKFold

from sklearn.metrics import f1 score, confusion matrix, roc curve, auc

- Both precision and recall is important so F1 score is good choice
- Confusion matrix

import datetime

import xgboost as xgb

#Clustering

import gc

In [1]:

```
# Importing necessary Libraries
import warnings
warnings.filterwarnings('ignore')
import numpy as np
import pandas as pd
from pandas import HDFStore, DataFrame
from pandas import read_hdf
import matplotlib.pyplot as plt
import seaborn as sns
import csv
from matplotlib import rcParams
import math
import pickle
import os
from collections import Counter
import random
from tqdm import tqdm
#Convert to unix time
import time
```

https://networkx.github.io/documentation/stable/tutorial.html import networkx as nx #https://docs.python.org/3/library/pdb.html import pdb # python debugger

In [2]:

```
if not os.path.isfile('lab/data/after_eda/train_woheader.csv'):
    traincsv = pd.read_csv('lab/data/train.csv')
    print(traincsv.isna().any(1)])
    print(traincsv.info())

# duplication check
    print("Number of duplicate entries: ",sum(traincsv.duplicated()))
    traincsv.to_csv('lab/data/after_eda/train_woheader.csv',header=False,index=False)
    print("saved the graph into file")
else:
    # opening the .csv file with "networkx" library and checking its info
# https://networkx.github.io/documentation/networkx-1.9/reference/generated/networkx.readwrite.edgelist.read_edgelist.html
    g= nx.read_edgelist('lab/data/after_eda/train_woheader.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=int)
    print(nx.info(g))
```

Name:

Type: DiGraph

Number of nodes: 1862220 Number of edges: 9437519 Average in degree: 5.0679 Average out degree: 5.0679

Displaying a sub graph

In [3]:

```
if not os.path.isfile('lab/data/after_eda/train_woheader_sample.csv'):
    pd.read_csv('lab/data/train.csv', nrows=50).to_csv('train_woheader_sample.csv', header= False, index= False)

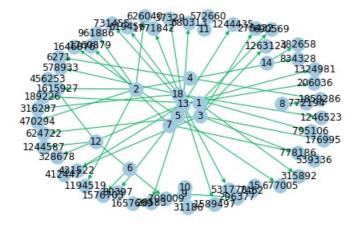
subgraph= nx.read_edgelist('train_woheader_sample.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=int)

# https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with-networkx-and-matplotlib
# https://networkx.github.io/documentation/networkx-1.9/reference/generated/networkx.drawing.layout.spring_layout.html
pos= nx.spring_layout(subgraph)
nx.draw(subgraph, pos, node_color='#A0CBE2', edge_color='#00bb5e', width= 1, edge_cmap= plt.cm.Blues, with_labels= True)
plt.savefig("graph_sample.pdf")

print(nx.info(subgraph))
```

Name:

Type: DiGraph Number of nodes: 66 Number of edges: 50 Average in degree: 0.7576 Average out degree: 0.7576



1. Exploratory Data Analysis

In [4]:

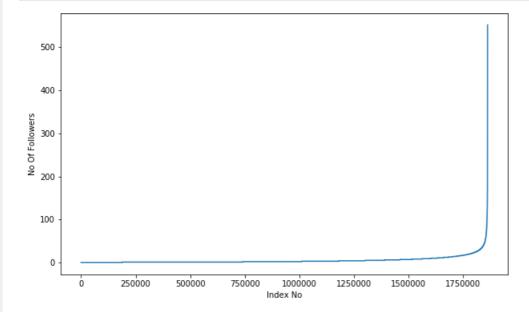
```
# No of Unique persons
print("The number of unique persons",len(g.nodes()))
```

The number of unique persons 1862220

1.1 No of followers for each person

In [5]:

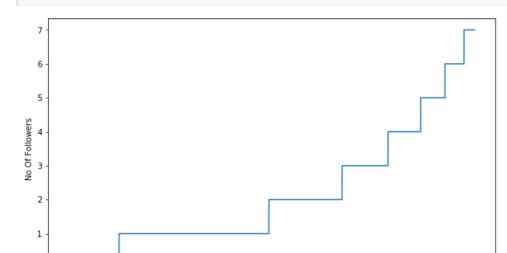
```
# in_degree => incoming edges
# g.in_degree() has tuples of index(node) as key and out_degree as values hence converted to dict,then to list and sorted.
indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(indegree_dist)
plt.valueb('Index No')
plt.ylabel('No Of Followers')
plt.show()
```



In [6]:

```
indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))

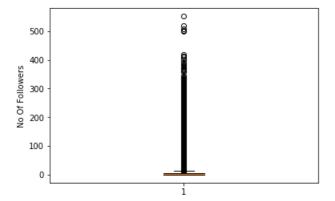
# Zooming upto 1.5M indexes
plt.plot(indegree_dist[0:1500000])
plt.xlabel('Index No upto 1.5M')
plt.ylabel('No Of Followers')
plt.show()
```



```
200000
           400000
                       600000
                                   800000
                                              1000000
                                                          1200000
                                                                      1400000
                           Index No upto 1.5M
```

In [7]:

```
# Checking the outliers
plt.boxplot(indegree_dist)
plt.ylabel('No Of Followers')
plt.show()
```



In [8]:

```
# 90-100 percentile
for i in range(0,11):
  print(90+i,'percentile value is',np.percentile(indegree_dist,90+i))
```

90 percentile value is 12.0

91 percentile value is 13.0

92 percentile value is 14.0

93 percentile value is 15.0 94 percentile value is 17.0

95 percentile value is 19.0

96 percentile value is 21.0

97 percentile value is 24.0

98 percentile value is 29.0

99 percentile value is 40.0

100 percentile value is 552.0

99% of data having only 40 followers.

In [9]:

```
### 99-100 percentile
for i in range(1,11):
   print(99+(i/10), 'percentile value is', np.percentile(indegree_dist, 99+(i/10)))
```

99.1 percentile value is 42.0

99.2 percentile value is 44.0

99.3 percentile value is 47.0 99.4 percentile value is 50.0

99.5 percentile value is 55.0

99.6 percentile value is 61.0

99.7 percentile value is 70.0

99.8 percentile value is 84.0

99.9 percentile value is 112.0

100.0 percentile value is 552.0

99.9 percentile of data having 112 followers and 100 percentile have nearly 552 followers.

1.2 No of people each person is following

In [11]:

sns.set_style('ticks')

plt.show()

plt.xlabel('PDF of Indegree')

sns.distplot(indegree_dist, color='#16A085')

```
# out_degree => out going edges

# g.out_degree() has tuples of index(node) as key and out_degree as values hence converted to dict, then to list and sorted.

outdegree_dist = list(dict(g.out_degree()).values())

outdegree_dist.sort()

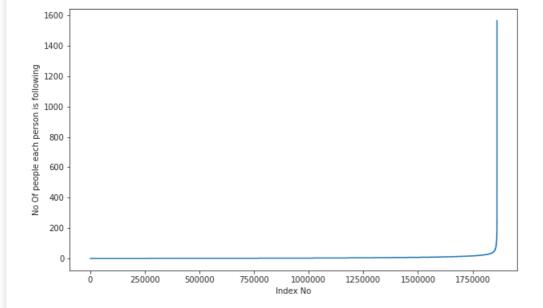
plt.figure(figsize=(10,6))

plt.plot(outdegree_dist)

plt.xlabel('Index No')

plt.ylabel('No Of people each person is following')

plt.show()
```



In [12]:

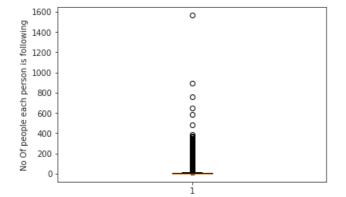
```
# Zooming upto 1.5M indexes
plt.plot(outdegree_dist[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following')
plt.show()
```



```
10 oV
           200000 400000 600000 800000100000012000001400000
                              Index No
```

In [13]:

```
# Checking the outliers
plt.boxplot(outdegree_dist)
plt.ylabel('No Of people each person is following')
plt.show()
```



In [14]:

```
# 90-100 percentile
for i in range(0,11):
  print(90+i,'percentile value is',np.percentile(outdegree_dist,90+i))
```

```
90 percentile value is 12.0
```

91 percentile value is 13.0 92 percentile value is 14.0

93 percentile value is 15.0

94 percentile value is 17.0

95 percentile value is 19.0

96 percentile value is 21.0

97 percentile value is 24.0

98 percentile value is 29.0

99 percentile value is 40.0

100 percentile value is 1566.0

In [15]:

```
### 99-100 percentile
for i in range(1,11,1):
  print(99+(i/10), 'percentile value is',np.percentile(outdegree_dist,99+(i/10)))
```

```
99.1 percentile value is 42.0
```

99.2 percentile value is 45.0

99.3 percentile value is 48.0

99.4 percentile value is 52.0 99.5 percentile value is 56.0

99.6 percentile value is 63.0

99.7 percentile value is 73.0

99.8 percentile value is 90.0

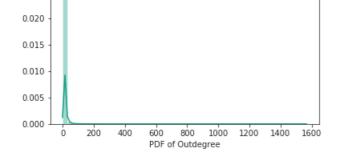
99.9 percentile value is 123.0

100.0 percentile value is 1566.0

In [16]:

```
sns.set_style('ticks')
sns.distplot(outdegree_dist, color='#16A085')
plt.xlabel('PDF of Outdegree')
plt.show()
```

```
0.030
0.025
```



In [17]:

```
print('No of persons those are not following anyone are' ,sum(np.array(outdegree_dist)==0),'and % is', sum(np.array(outdegree_dist)==0)*100/len(outdegree_dist))
```

No of persons those are not following anyone are 274512 and % is 14.741115442858524

In [18]:

```
print('No of persons having zero followers are' ,sum(np.array(indegree_dist)==0),'and % is', sum(np.array(indegree_dist)==0)*100/len(indegree_dist) )
```

No of persons having zero followers are 188043 and % is 10.097786512871734

In [19]:

```
# for each node, if no predecessor and also if no successor then,
count=0
for i in g.nodes():
   if len(list(g.predecessors(i)))==0:
        if len(list(g.successors(i)))==0:
            count+=1
print('No of persons those are not not following anyone and also not having any followers are', count)
```

No of persons those are not not following anyone and also not having any followers are 0

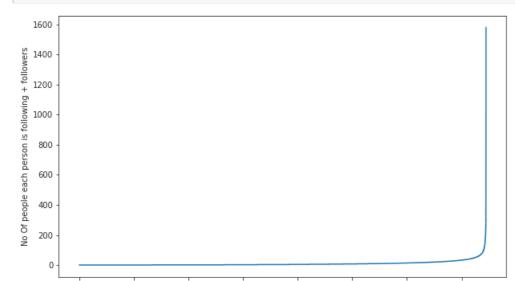
1.3 Both Followers + Following

In [20]:

```
# 'd' contains all the dict of incoming and outgoing nodes.

d = Counter(dict(g.in_degree())) + Counter(dict(g.out_degree()))
in_out_degree = np.array(list(d.values()))

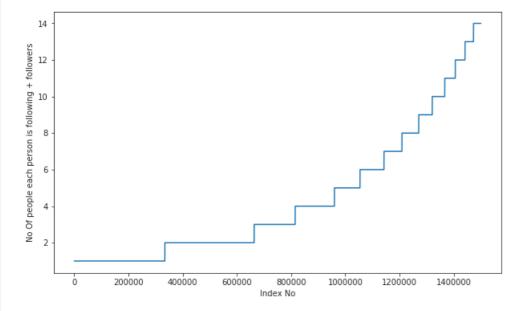
in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort)
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



250000 500000 750000 1000000 1250000 1500000 1750000 Index No

In [21]:

```
in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



In [22]:

```
### 90-100 percentile
for i in range(0,11):
  print(90+i,'percentile value is',np.percentile(in_out_degree_sort,90+i))
```

90 percentile value is 24.0

91 percentile value is 26.0

92 percentile value is 28.0

93 percentile value is 31.0 94 percentile value is 33.0

95 percentile value is 37.0

96 percentile value is 41.0

97 percentile value is 48.0

98 percentile value is 58.0

99 percentile value is 79.0

100 percentile value is 1579.0

In [23]:

```
### 99-100 percentile
for i in range(1,11):
  print(99+(i/10),'percentile value is',np.percentile(in_out_degree_sort,99+(i/10)))
```

```
99.1 percentile value is 83.0
```

99.2 percentile value is 87.0

99.3 percentile value is 93.0

99.4 percentile value is 99.0 99.5 percentile value is 108.0

99.6 percentile value is 120.0

99.7 percentile value is 138.0

99.8 percentile value is 168.0

99.9 percentile value is 221.0

100.0 percentile value is 1579.0

In [24]:

```
print('Min of no of followers + following = ',in_out_degree.min())
print('*'*50)
print('These many ',np.sum(in_out_degree == in_out_degree.min()),'persons are having minimum no of followers + following.')
```

```
Min of no of followers + following = 1
```

These many 334291 persons are having minimum no of followers + following.

In [25]:

```
print('Max of no of followers + following = ',in_out_degree.max())
print('***50)
print('These many',np.sum(in_out_degree == in_out_degree.max()),'persons are having maximum no of followers + following.')
```

Max of no of followers + following = 1579

These many 1 persons are having maximum no of followers + following.

In [26]:

```
print('These many',np.sum(in_out_degree<10),'persons are having followers + following less than 10.')
```

These many 1320326 persons are having followers + following less than 10.

In [27]:

```
print('No of weakly connected components:',len(list(nx.weakly_connected_components(g))))
count=0
for i in list(nx.weakly_connected_components(g)):
    if len(i) == 2:
        count += 1
print('Weakly connected components with 2 nodes:',count)
```

No of weakly connected components: 45558 Weakly connected components with 2 nodes: 32195

2. Posing a problem as classification problem

2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

In [28]:

```
###generating bad edges from given graph
if not os.path.isfile('lab/data/after_eda/missing_edges_final.p'):
  #getting all set of edges
  r = csv.reader(open('lab/data/after_eda/train_woheader.csv','r'))
  # 9.43M edges of tuples in to dict format
  edges = dict()
  for edge in r:
     edges[(edge[0], edge[1])] = 1
  # create a set "missing_edges" which must contain the 0 labels
  missing_edges = set([])
   # must be less than 9.43M to generate in random from whopping '1.86M(1.86M - 1)' nodes to obtain 0 labelled connections
  while (len(missing_edges) < 9437519):
     # random node from 1.86M nodes
     ui= random.randint(1, 1862220)
     uj= random.randint(1, 1862220)
     # check for connection between nodes 'ui', 'uj' & if connection then check shortest path > 2, add them to 0 label.
     tmp = edges.get((ui, uj), -1)
     if tmp == -1 and ui != uj:
       try:
          if nx.shortest_path_length(g, source= ui, target= uj) > 2:
            missing_edges.add((ui, uj))
          else:
            continue
       except:
            missing_edges.add((ui, uj))
  pickle.dump(missing edges,open('lab/data/after eda/missing edges final.p','wb'))
  missing_edges = pickle.load(open('lab/data/after_eda/missing_edges_final.p','rb'))
```

```
Wall time: 4.16 s

In [29]:

len(missing_edges)
```

Out[29]:

9437519

2.2 Training and Test data split:

CPU times: user 2.2 s, sys: 1.22 s, total: 3.42 s

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

In [30]:

```
if (not os.path.isfile('lab/data/after_eda/train_pos_after_eda.csv')) and \
(not os.path.isfile('lab/data/after_eda/test_pos_after_eda.csv')):
   #reading total data df
  df pos = pd.read csv('lab/data/train.csv')
  df_neg = pd.DataFrame(list(missing_edges), columns=['source_node', 'destination_node'])
  print("Number of nodes in the graph with edges", df pos.shape[0])
  print("Number of nodes in the graph without edges", df_neg.shape[0])
   #Trian test split
   #Spiltted data into 80-20
   #positive links and negative links saperatly because we need positive training data only for creating graph
   #and for feature generation
  X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,np.ones(len(df_pos)),
                                              test_size=0.2, random_state=9)
  X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,np.zeros(len(df_neg)),
                                              test_size=0.2, random_state=9)
  print('*'*60)
  print("Number of nodes in the train data graph with edges", X_train_pos.shape[0],"=",y_train_pos.shape[0])
  print("Number of nodes in the train data graph without edges", X_train_neg.shape[0],"=", y_train_neg.shape[0])
  print('='*60)
  print("Number of nodes in the test data graph with edges", X test pos.shape[0],"=",y test pos.shape[0])
  print("Number of nodes in the test data graph without edges", X_test_neg.shape[0],"=",y_test_neg.shape[0])
   #removing header and saving
  X_train_pos.to_csv('lab/data/after_eda/train_pos_after_eda.csv',header=False, index=False)
  X\_test\_pos\_to\_csv('lab/data/after\_eda/test\_pos\_after\_eda.csv', header=\textit{False}, index=\textit{False})
  X train neg.to csv('lab/data/after eda/train neg after eda.csv',header=False, index=False)
  X_test_neg.to_csv('lab/data/after_eda/test_neg_after_eda.csv',header=False, index=False)
else:
  #Graph from Training data only
  del missing_edges
```

In [31]:

```
if (os.path.isfile('lab/data/after_eda/train_pos_after_eda.csv')) and \
(os.path.isfile('lab/data/after_eda/test_pos_after_eda.csv')):
  train_graph=nx.read_edgelist('lab/data/after_eda/train_pos_after_eda.csv', delimiter=',', create_using= nx.DiGraph(),
                     nodetype=int)
  test_graph=nx.read_edgelist('lab/data/after_eda/test_pos_after_eda.csv', delimiter=',', create_using= nx.DiGraph(),
                    nodetype=int)
  print(nx.info(train_graph))
  print(nx.info(test_graph))
   # finding the unique nodes in the both train and test graphs
  train_nodes_pos = set(train_graph.nodes())
  test_nodes_pos = set(test_graph.nodes())
  # intersection gives the common nodes in train and test after split
  print('No of people common in train and test -- ', len(train nodes pos.intersection(test nodes pos)))
  # sets are different hence we obtain people not in test data but in train data
  print('No of people present in train but not present in test -- ', len(train_nodes_pos - test_nodes_pos))
  # sets are different hence we obtain people not in train data but in test data and also in percentage.
  print('No of people present in test but not present in train -- ', len(test_nodes_pos - train_nodes_pos))
```

```
print('No of people not there in Train but exist in Test in total Test data are {} %'.format(
len(test_nodes_pos - train_nodes_pos)/len(test_nodes_pos)*100))
```

Name: Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

Name: Type: DiGraph

Number of nodes: 1144623 Number of edges: 1887504 Average in degree: 1.6490 Average out degree: 1.6490

No of people common in train and test -- 1063125

No of people present in train but not present in test -- 717597 No of people present in test but not present in train -- 81498

No of people not there in Train but exist in Test in total Test data are 7.1200735962845405 %

we have a cold start problem here as the 81498 nodes info is not present in train data which accounts for 7%

In [32]:

```
#final train and test data sets
if (not os.path.isfile('lab/data/after_eda/train_after_eda.csv')) and \
(not os.path.isfile('lab/data/after_eda/test_after_eda.csv')) and \
(not os.path.isfile('lab/data/train_y.csv')) and \
(not os.path.isfile('lab/data/test_y.csv')) and \
(os.path.isfile('lab/data/after_eda/train_pos_after_eda.csv')) and \
(os.path.isfile('lab/data/after_eda/test_pos_after_eda.csv')) and \
(os.path.isfile('lab/data/after eda/train neg after eda.csv')) and \
(os.path.isfile('lab/data/after_eda/test_neg_after_eda.csv')):
  X train pos = pd.read csv('lab/data/after eda/train pos after eda.csv', names=['source node', 'destination node'])
  X test pos = pd.read csv('lab/data/after eda/test pos after eda.csv', names=['source node', 'destination node'])
  X_train_neg = pd.read_csv('lab/data/after_eda/train_neg_after_eda.csv', names=['source_node', 'destination_node'])
  X_test_neg = pd.read_csv('lab/data/after_eda/test_neg_after_eda.csv', names=['source_node', 'destination_node'])
  print("Number of nodes in the train data graph with edges", X_train_pos.shape[0])
  print("Number of nodes in the train data graph without edges", X_train_neg.shape[0])
  print('='*60)
  print("Number of nodes in the test data graph with edges", X_test_pos.shape[0])
  print("Number of nodes in the test data graph without edges", X_test_neg.shape[0])
  X_train = X_train_pos.append(X_train_neg,ignore_index=True)
  y_train = np.concatenate((y_train_pos,y_train_neg))
  X_test = X_test_pos.append(X_test_neg,ignore_index=True)
  y_test = np.concatenate((y_test_pos,y_test_neg))
  X\_train.to\_csv(\mbox{\ensuremath{'}lab/data/after\_eda/train\_after\_eda.csv'}, header=\mbox{\ensuremath{'}header=}\mbox{\ensuremath{'}False})
  X_test.to_csv('lab/data/after_eda/test_after_eda.csv',header=False,index=False)
  pd.DataFrame(y_train.astype(int)).to_csv('lab/data/train_y.csv',header=False,index=False)
  pd.DataFrame(y_test.astype(int)).to_csv('lab/data/test_y.csv',header=False,index=False)
```

Reading Data

In [33]:

```
X_train_pos = pd.read_csv('lab/data/after_eda/train_after_eda.csv')

X_test_pos = pd.read_csv('lab/data/after_eda/test_after_eda.csv')

y_train_pos = pd.read_csv('lab/data/train_y.csv')

y_test_pos = pd.read_csv('lab/data/train_y.csv')

print("Data points in train data", X_train_pos.shape)

print("Data points in test data", X_test_pos.shape)

print("Shape of target variable in train", y_train_pos.shape)

print("Shape of target variable in test", y_test_pos.shape)
```

Data points in train data (15100029, 2) Data points in test data (3775007, 2) Shape of target variable in train (15100029, 1) Shape of target variable in test (3775007, 1)

```
In [34]:
```

```
print(nx.info(train_graph))
```

Name: Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

 $\begin{array}{l} \left(X \right) = \left(X \right) \\ \left(X \right) \\$

In [35]:

In [36]:

```
#one test case
print(jaccard_for_followees(273084,1505602))
```

0.0

In [37]:

```
#node 1635354 not in graph
print(jaccard_for_followees(273084,1505602))
```

0.0

In [38]:

In [39]:

```
print(jaccard_for_followers(273084,470294))
```

0.0

In [40]:

```
#node 1635354 not in graph
print(jaccard_for_followees(669354,1635354))
```

2.2 Cosine distance

 $\beta = \frac{|X \cdot Y|}{|X \cdot Y|}$

```
In [41]:
```

In [42]:

```
print(cosine_for_followees(273084,1505602))
```

0.0

In [43]:

```
print(cosine_for_followees(273084,1635354))
```

0

In [44]:

In [45]:

```
print(cosine_for_followers(2,470294))
```

0.02886751345948129

In [46]:

```
print(cosine_for_followers(669354,1635354))
```

0

3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link analysis.pagerank_alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

```
In [47]:
```

```
if not os.path.isfile('lab/data/fea_sample/page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr, open('lab/data/fea_sample/page_rank.p','wb'))
else:
    pr = pickle.load(open('lab/data/fea_sample/page_rank.p','rb'))
```

In [48]:

```
print('PageRank Min:',pr[min(pr, key=pr.get)])
print('PageRank Max:',pr[max(pr, key=pr.get)])
print('PageRank Mean:',float(sum(pr.values())) / len(pr))
```

PageRank Min: 1.6556497245737814e-07 PageRank Max: 2.7098251341935827e-05 PageRank Mean: 5.615699699365892e-07

In [49]:

```
#for imputing to nodes which are not there in Train data (replacing into the 80k test data with mean value)
mean_pr = float(sum(pr.values())) / len(pr)
print(mean_pr)
```

5.615699699365892e-07

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between two nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

In [50]:

```
#if has direct edge then deleting that edge and calculating shortest path

def compute_shortest_path_length(a,b):
    p= -1
    try:
        if train_graph.has_edge(a,b):
            train_graph.remove_edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
            train_graph.add_edge(a,b)
        else:
            p= nx.shortest_path_length(train_graph,source=a,target=b)
        return p
        except:
            # no connected edges at all between nodes
        return -1
```

In [51]:

```
#testing
compute_shortest_path_length(77697, 826021)
```

Out[51]:

10

In [52]:

```
#testing compute_shortest_path_length(669354,1635354)
```

Out[52]:

4.2 Checking for same community

```
In [53]:
```

```
#getting weakly connected edges from graph (weakly bcoz to check for community like college, school, workplace)
wcc=list(nx.weakly_connected_components(train_graph))
def belongs_to_same_wcc(a,b):
  index = []
  if train_graph.has_edge(b,a):
     return 1
  if train_graph.has_edge(a,b):
       for i in wcc:
          if a in i:
            index= i
            break
       if (b in index):
          train_graph.remove_edge(a,b)
          if compute\_shortest\_path\_length(a,b) == -1:
            train_graph.add_edge(a,b)
            return 0
          else:
            train_graph.add_edge(a,b)
            return 1
       else:
          return 0
  else:
       for i in wcc:
          if a in i:
            index= i
            break
       if(b in index):
          return 1
       else:
          return 0
In [54]:
```

```
belongs_to_same_wcc(861, 1659750)

Out[54]:
0
```

In [55]:

```
belongs_to_same_wcc(669354,1635354)
```

Out[55]:

0

4.3 Adamic/Adar Index:

Adamic / Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices. $A(x,y)=\sum_{u \in N(y)}\frac{1}{\log(|N(u)|)}$

In [56]:

```
# whether the node is celebrity or is just a common school mate/ work / college
def calc_adar_in(a,b):
    sum=0
    try:
        n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors(b))))
    if len(n)!=0:
        for i in n:
            sum=sum+(1/np.log10(len(list(train_graph.predecessors(i))))))
        return sum
    else:
        return 0
    except:
    return 0
```

```
calc_adar_in(1,189226)
Out[57]:
In [58]:
calc_adar_in(669354,1635354)
Out[58]:
4.4 Does a person follows back:
In [59]:
def follows_back(a,b):
  if train_graph.has_edge(b,a):
    return 1
  else:
    return 0
In [60]:
follows_back(1,189226)
Out[60]:
In [61]:
follows_back(669354,1635354)
Out[61]:
0
4.5 Katz Centrality:
https://en.wikipedia.org/wiki/Katz_centrality
https://www.geeksforgeeks.org/katz-centrality-measure/ Katz centrality computes the centrality for a node based on the centrality of its
neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is
x_i = \alpha \sum_{j} A_{ij} x_j + \beta_{ij} x_j
where A is the adjacency matrix of the graph G with eigenvalues $$\lambda$$.
The parameter $$\beta$$ controls the initial centrality and
\ shalpha < \frac{1}{\lambda}.
In [62]:
if not os.path.isfile('lab/data/fea_sample/katz.p'):
  katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
  pickle.dump(katz,open('lab/data/fea_sample/katz.p','wb'))
else:
  katz = pickle.load(open('lab/data/fea_sample/katz.p','rb'))
In [63]:
print('Katz Centrality Min:',katz[min(katz, key=katz.get)])
```

Katz Centrality Min: 0.0007313532484065916 Katz Centrality Max: 0.003394554981699122 Katz Centrality Mean: 0.0007483800935504637

print('Katz Centrality Max:',katz[max(katz, key=katz.get)])
print('Katz Centrality Mean:',float(sum(katz.values())) / len(katz))

In [64]:

```
mean_katz = float(sum(katz.values())) / len(katz)
print(mean_katz)
```

0.0007483800935504637

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm

In [65]:

```
if not os.path.isfile('lab/data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('lab/data/fea_sample/hits.p','wb'))
else:
    hits = pickle.load(open('lab/data/fea_sample/hits.p','rb'))
```

In [66]:

```
print('HITS Score Min:', hits[0][min(hits[0], key=hits[0].get)])
print('HITS Score Max:', hits[0][max(hits[0], key=hits[0].get)])
print('HITS Score Mean:', float(sum(hits[0].values())) / len(hits[0]))
```

HITS Score Min: 0.0

HITS Score Max: 0.004868653378780953 HITS Score Mean: 5.615699699353278e-07

5. Featurization

5. 1 Reading a sample of Data from both train and test

In [67]:

```
# Train data

filename = "lab/data/after_eda/train_after_eda.csv"

if os.path.isfile(filename):

# you uncomment this line, if you dont know the lentgh of the file name

# here we have hardcoded the number of lines as 15100030

# n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)

n_train = 15100028

s = 100000 #desired sample size

skip_train = sorted(random.sample(range(1, n_train + 1), n_train - s))

#https://stackoverflow.com/a/22259008/4084039
```

In [68]:

```
filename = "lab/data/after_eda/test_after_eda.csv"

if os.path.isfile(filename):

# you uncomment this line, if you dont know the lentgh of the file name

# here we have hardcoded the number of lines as 3775008

# n_test = sum(1 for line in open(filename)) #number of records in file (excludes header)

n_test = 3775006

s = 50000 #desired sample size

skip_test = sorted(random.sample(range(1, n_test + 1), n_test - s))

#https://stackoverflow.com/a/22259008/4084039
```

In [69]:

```
print("Number of rows in the train data file:", n_train)
print("Number of rows we are going to elimiate in train data are",len(skip_train))
print("Number of rows in the test data file:", n_test)
print("Number of rows we are going to elimiate in test data are",len(skip_test))
```

Number of rows in the train data file: 15100028

Number of rows we are going to elimiate in train data are 15000028

Number of rows in the test data file: 3775006

Number of rows we are going to elimiate in test data are 3725006

In [70]:

Our train matrix size (100002, 3)

1163878

Out[70]:

source_node destination_node indicator_link 0 273084 1505602 1

1629981

In [71]:

Our test matrix size (50002, 3)

Out[71]:

	source_noue	destination_node	ilidicatoi_ilik
0	848424	784690	1
1	1427585	1224220	1

course node dectination node indicator link

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard_followers
- 2. jaccard_followees
- 3. cosine_followers
- 4. cosine_followees
- 5. num_followers_s6. num_followees_s
- 7. num followers d
- 8. num_followees_d
- 9. inter_followers
- 10. inter_followees

In [72]:

In [73]:

```
def compute_features_stage1(df_final):
   # calculating no of followers and followees for source 's' and destination 'd'
  # calculating intersection of followers and followees for source and destination
  num followers s=[]
  num followees s=[]
  num_followers_d=[]
  num_followees_d=[]
  inter followers=[]
  inter followees=[]
  for i, j in df_final.iterrows():
    try:
       s1= set(train_graph.predecessors(j['source_node']))
       s2= set(train_graph.successors(j['source_node']))
     except:
       s1= set()
       s2 = set()
     try:
       d1= set(train_graph.predecessors(j['destination_node']))
       d2= set(train_graph.successors(j['destination_node']))
     except:
       d1 = set()
       d2 = set()
     num_followers_s.append(len(s1))
     num_followees_s.append(len(s2))
     num_followers_d.append(len(d1))
     num_followees_d.append(len(d2))
     inter_followers.append(len(s1.intersection(d1)))
    inter_followees.append(len(s2.intersection(d2)))
  return num followers s, num followers d, num followees s, num followees d, inter followers, inter followees
```

In [74]:

In [75]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage1.h5'): # file doesn't has 'num_followers_d', hence composing
  \label{lem:continuous} df\_final\_train['num\_followers\_s'], \ df\_final\_train['num\_followers\_d'], \ \\ \\ \\ \\
  df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
  df_final_train['inter_followers'], df_final_train['inter_followees']= compute_features_stage1(df_final_train)
  df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
  df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
  df final test['inter followers'], df final test['inter followees']= compute features stage1(df final test)
  # https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.HDFStore.put.html#pandas.HDFStore.put
   # https://kite.com/python/docs/pandas.HDFStore
  hdf = HDFStore('lab/data/fea_sample/storage_sample_stage1.h5')
  hdf.put('train df',df final train, format='table', data columns=True)
  hdf.put('test df',df final test, format='table', data columns=True)
  hdf.close()
else:
  # https://stackoverflow.com/a/58546205/10219869 (!pip3 install --user tables)
  df_final_train = read_hdf('lab/data/fea_sample/storage_sample_stage1.h5', 'train_df',mode='r')
  df_final_test = read_hdf('lab/data/fea_sample/storage_sample_stage1.h5', 'test_df',mode='r')
```

```
df_final_train.columns
```

Out[75]:

```
Index(['source_node', 'destination_node', 'indicator_link',
    'jaccard_followers', 'jaccard_followees', 'cosine_followers',
    'cosine_followees', 'num_followers_s', 'num_followers_d',
    'num_followees_s', 'num_followees_d', 'inter_followers',
    'inter_followees'],
    dtype='object')
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

In [76]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage2.h5'):
   #mapping adar index on train and test
  df_final_train['adar_index'] = df_final_train.apply(lambda i:
                                   calc_adar_in(i['source_node'], i['destination_node']), axis=1)
  df final test['adar index'] = df final test.apply(lambda i:
                                  calc_adar_in(i['source_node'], i['destination_node']), axis=1)
  #mapping followback or not on train and test
  df_final_train['follows_back'] = df_final_train.apply(lambda i:
                                     follows_back(i['source_node'], i['destination_node']), axis=1)
  df_final_test['follows_back'] = df_final_test.apply(lambda i:
                                   follows_back(i['source_node'], i['destination_node']), axis=1)
   #mapping same component of wcc or not on train and test
  df_final_train['same_comp'] = df_final_train.apply(lambda i:
                                   belongs to same_wcc(i['source_node'], i['destination_node']), axis=1)
  df_final_test['same_comp'] = df_final_test.apply(lambda i:
                                 belongs_to_same_wcc(i['source_node'], i['destination_node']), axis=1)
  #mapping shortest path on train and test
  df_final_train['shortest_path'] = df_final_train.apply(lambda i:
                                     compute_shortest_path_length(i['source_node'],
                                                        i['destination_node']), axis=1)
  df_final_test['shortest_path'] = df_final_test.apply(lambda i:
                                    compute_shortest_path_length(i['source_node'],
                                                      i['destination_node']), axis=1)
  hdf = HDFStore('lab/data/fea\_sample/storage\_sample\_stage2.h5') \\
  hdf.put('train_df',df_final_train, format='table', data_columns=True)
  hdf.put('test_df',df_final_test, format='table', data_columns=True)
  hdf.close()
else:
  df_final_train = read_hdf('lab/data/fea_sample/storage_sample_stage2.h5', 'train_df',mode='r')
  df_final_test = read_hdf('lab/data/fea_sample/storage_sample_stage2.h5', 'test_df',mode='r')
```

In [77]:

df_final_train.columns

Out[77]:

```
Index(['source_node', 'destination_node', 'indicator_link',
    'jaccard_followers', 'jaccard_followees', 'cosine_followers',
    'cosine_followees', 'num_followers_s', 'num_followers_d',
    'num_followees_s', 'num_followees_d', 'inter_followers',
    'inter_followees', 'adar_index', 'follows_back', 'same_comp',
    'shortest_path'],
    dtype='object')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - · weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang \begin{equation} W = \frac{11}{\sqrt{1+|X|}} \end{equation}

it is directed graph so calculated Weighted in and Weighted out differently

In [78]:

```
#weight for source and destination of each link

Weight_in = {}
Weight_out = {}
for i in tqdm(train_graph.nodes()):
    s1=set(train_graph.predecessors(i))
    w_in = 1.0/(np.sqrt(1+len(s1)))
Weight_in[i]=w_in

    s2=set(train_graph.successors(i))
    w_out = 1.0/(np.sqrt(1+len(s2)))
Weight_out[i]=w_out

#for imputing with mean
    mean_weight_in = np.mean(list(Weight_in.values()))
mean_weight_out = np.mean(list(Weight_out.values()))

100%| 1780722/1780722 [00:16<00:00, 110249.47it/s]
```

In [79]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
  #mapping to pandas train and test
  df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x, mean weight in))
  df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out.get(x, mean_weight_out))
  df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x, mean weight in))
  df_final_test['weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out.get(x, mean_weight_out))
  #some features engineerings on the in and out weights on train data
  df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
  df final train['weight f2'] = df final train.weight in * df final train.weight out
  df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_out)
  df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_out)
  #some features engineerings on the in and out weights on test data
  df\_final\_test[\color=black] = df\_final\_test.weight\_in + df\_final\_test.weight\_out
  df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
  df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
  df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)
```

```
if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
     #page rank for source and destination in Train and Test
     #if anything not there in train graph then adding mean page rank
    df final train['page rank s'] = df final train.source node.apply(lambda x: pr.get(x, mean pr))
    df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x: pr.get(x, mean_pr))
    df_final_test['page_rank_s'] = df_final_test.source_node.apply(lambda x: pr.get(x, mean_pr))
    df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x: pr.get(x, mean_pr))
     #Katz centrality score for source and destination in Train and test
     #if anything not there in train graph then adding mean katz score
    df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x, mean katz))
    df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x, mean_katz))
    df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x, mean_katz))
    df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x, mean katz))
     #Hits algorithm score for source and destination in Train and test
     #if anything not there in train graph then adding 0
    df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x, 0))
    df_{inal\_train['hubs\_d']} = df_{inal\_train.destination\_node.apply(lambda x: hits[0].get(x, 0))
    df\_final\_test[\begin{subarray}{c} \label{eq:final_test.source_node.apply} \end{subarray} (\begin{subarray}{c} \label{eq:final_test.source_node.apply} \end{subarray} \end{subarray} (\begin{subarray}{c} \label{eq:final_tes
    df_{inal\_test['hubs\_d']} = df_{inal\_test.destination\_node.apply(lambda x: hits[0].get(x, 0))
     #Hits algorithm score for source and destination in Train and Test
     #if anything not there in train graph then adding 0
    df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x, 0))
    df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x, 0))
    df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hits[1].get(x, 0))
    df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: hits[1].get(x, 0))
    hdf = HDFStore('lab/data/fea sample/storage sample stage3.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df_final_train = read_hdf('lab/data/fea_sample/storage_sample_stage3.h5', 'train_df',mode='r')
    df_final_test = read_hdf('lab/data/fea_sample/storage_sample_stage3.h5', 'test_df',mode='r')
```

In [81]:

df_final_train.columns

Out[81]:

```
Index(['source_node', 'destination_node', 'indicator_link',
    'jaccard_followers', 'jaccard_followees', 'cosine_followers',
    'cosine_followees', 'num_followers_s', 'num_followers_d',
    'num_followees_s', 'num_followees_d', 'inter_followers',
    'inter_followees', 'adar_index', 'follows_back', 'same_comp',
    'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
    'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
    'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d'],
    dtype='object')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

In [82]:

```
def svd(x, S):
    try:
    z = sadj_dict[x]
    return S[z]
    except:
    return [0,0,0,0,0,0]
```

In [83]:

```
sadj_col = sorted(train_graph.nodes())
sadj_dict = { value:index for index, value in enumerate(sadj_col)}
```

In [84]:

https://docs.scipy.org/doc/scipy-0.14.0/reference/generated/scipy.sparse.coo_matrix.asfptype.html
https://networkx.github.io/documentation/networkx-1.9/reference/generated/networkx.linalg.graphmatrix.adjacency_matrix.html
Adj = nx.adjacency_matrix(train_graph, nodelist= sadj_col).asfptype()

In [85]:

```
# https://docs.scipy.org/doc/scipy/reference/generated/scipy.sparse.linalg.svds.html
U, s, V = svds(Adj, k = 6)

print('Adjacency matrix Shape',Adj.shape)
print('U Shape',U.shape)
print('V Shape',V.shape)
print('S Shape',s.shape)
```

Adjacency matrix Shape (1780722, 1780722) U Shape (1780722, 6) V Shape (6, 1780722) s Shape (6,)

In [86]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage4.h5'):
  # Source and destination train for 'U'
  df_final_train.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
  df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
  df\_final\_train.destination\_node.apply(\textbf{lambda}\ x:\ svd(x,\ U)).apply(pd.Series)
  # Source and destination train for 'V'
  df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
  df\_final\_train.destination\_node.apply(\textbf{lambda}\ x:\ svd(x,\ V.T)).apply(pd.Series)
  # Source and destination test for 'U'
  df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
  df_final_test.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
  df final test[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
  df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
  # Source and destination test for 'V'
  df final test[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
  df_final_test.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
  df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6']] = \
  df_final_test.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
  hdf = HDFStore('lab/data/fea_sample/storage_sample_stage4.h5')
  hdf.put('train df',df final train, format= 'table', data columns= True)
  hdf.put('test_df',df_final_test, format= 'table', data_columns= True)
  hdf.close()
```

In [87]:

df_final_train.columns

Out[87]:

```
Index(['source_node', 'destination_node', 'indicator_link', 'jaccard_followers', 'jaccard_followees', 'cosine_followers', 'cosine_followees', 'num_followers_s', 'num_followers_d', 'inter_followers_s', 'num_followees_d', 'inter_followers', 'i
```

```
inter_followees, adar_index, follows_back, same_comp
    'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
    'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
    'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
    'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
    'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
    "svd\_u\_d\_5", "svd\_u\_d\_6", "svd\_v\_s\_1", "svd\_v\_s\_2", "svd\_v\_s\_3", \\
    'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
    'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
    dtype='object')
In [88]:
len(df_final_train.columns)
Out[88]:
55
In [89]:
y train = df final train['indicator link']
y_test = df_final_test['indicator_link']
```

Random Forest

Without Preferential Attachment and SVD

df_final_train.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=**True**) df_final_test.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=**True**)

In [91]:

In [90]:

```
estimators = [10,50,100,250,450]
train_scores = []
test scores = []
for i in estimators:
  clf = RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini', max depth=5, max features='auto',
                    max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None,
                    min_samples_leaf=52, min_samples_split=120, min_weight_fraction_leaf=0.0, n_estimators=i,
                    n_jobs=-1,random_state=25,verbose=0,warm_start=False)
  clf.fit(df_final_train, y_train)
  y_pred_train = clf.predict(df_final_train)
  train\_sc = f1\_score(y\_train, y\_pred\_train)
  y_pred_test = clf.predict(df_final_test)
  test_sc = f1_score(y_test, y_pred_test)
  test_scores.append(test_sc)
  train_scores.append(train_sc)
  print('Estimators:',i,'Train Score:',train_sc,'test Score:',test_sc)
```

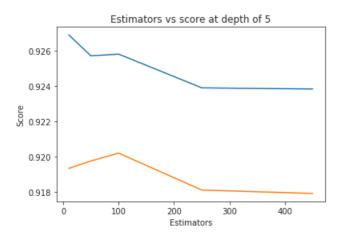
Estimators: 10 Train Score: 0.9269198879081435 test Score: 0.9193365048625437 Estimators: 50 Train Score: 0.9257276540139524 test Score: 0.9197594682983437 Estimators: 100 Train Score: 0.925826028320971 test Score: 0.9202034484941857 Estimators: 250 Train Score: 0.9239105275340362 test Score: 0.9181059903951471 Estimators: 450 Train Score: 0.923845377302936 test Score: 0.91791406134866

In [92]:

```
plt.plot(estimators, train_scores, label='Train Score')
plt.plot(estimators, test_scores, label='Test Score')
plt.xlabel('Estimators')
plt.ylabel('Score')
plt.title('Estimators vs score at depth of 5')
```

Out[92]:

Text(0.5, 1.0, 'Estimators vs score at depth of 5')



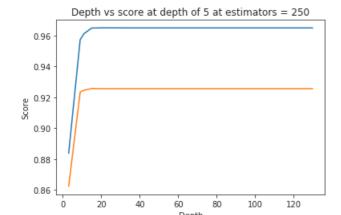
In [93]:

```
depths = [3,9,11,15,20,35,50,70,130]
train_scores = []
test_scores = []
for i in depths:
  clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini', max_depth= i, max_features='auto',
                    max leaf nodes=None, min impurity decrease=0.0, min impurity split=None,
                    min samples leaf=52, min samples split=120, min weight fraction leaf=0.0, n estimators=250,
                    n_jobs=-1, random_state=25, verbose=0, warm_start=False)
  clf.fit(df_final_train, y_train)
  y_pred_train = clf.predict(df_final_train)
  train_sc = f1_score(y_train, y_pred_train)
  y_pred_test = clf.predict(df_final_test)
  test_sc = f1_score(y_test, y_pred_test)
  test_scores.append(test_sc)
  train_scores.append(train_sc)
  print('Depths:',i,'Train Score:',train_sc,'test Score:',test_sc)
```

Depths: 3 Train Score: 0.8837393840610791 test Score: 0.8622905270469742 Depths: 9 Train Score: 0.9572870242303161 test Score: 0.9232974306009316 Depths: 11 Train Score: 0.9611820123228463 test Score: 0.9245350576044146 Depths: 15 Train Score: 0.9647720786104543 test Score: 0.925660178853235 Depths: 20 Train Score: 0.9648965446947304 test Score: 0.925505714947271 Depths: 35 Train Score: 0.9648620271358525 test Score: 0.925508850954556 Depths: 50 Train Score: 0.9648620271358525 test Score: 0.925508850954556 Depths: 70 Train Score: 0.9648620271358525 test Score: 0.925508850954556 Depths: 130 Train Score: 0.9648620271358525 test Score: 0.925508850954556

In [94]:

```
plt.plot(depths, train_scores, label='Train Score')
plt.plot(depths, test_scores, label='Test Score')
plt.xlabel('Depth')
plt.ylabel('Score')
plt.title('Depth vs score at depth of 5 at estimators = 250')
plt.show()
```



```
In [95]:
param_dist = {"n_estimators":sp_randint(105,125),
        "max depth": sp randint(10,15),
         "min_samples_split": sp_randint(110,190),
        "min_samples_leaf": sp_randint(25,65)}
clf = RandomForestClassifier(random_state=25,n_jobs=-1)
skf = StratifiedKFold(n_splits= 5)
rf_random = RandomizedSearchCV(clf, param_distributions=param_dist, n_iter=10, cv= skf, scoring="f1", random_state=25,
                   return_train_score= True)
rf_random.fit(df_final_train,y_train)
print('mean test scores', rf_random.cv_results_['mean_test_score'])
# return train score: boolean, default= False
If False, the cv_results_ attribute will not include training scores. Computing training scores is used to get insights on
how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training
set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization
performance.
print('mean train scores', rf_random.cv_results_['mean_train_score'])
mean test scores [0.96284045 0.96254949 0.95999826 0.9619557 0.96426847 0.96095504
0.96031971 0.96256768 0.96202355 0.95882266]
mean train scores [0.96340597 0.96323411 0.96042792 0.96296677 0.96526832 0.96183264
0.96097563 0.96346565 0.96282375 0.9590613 ]
In [96]:
print(rf_random.best_estimator_)
RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
              max_depth=14, max_features='auto', max_leaf_nodes=None,
              min_impurity_decrease=0.0, min_impurity_split=None,
              min_samples_leaf=28, min_samples_split=111,
              min_weight_fraction_leaf=0.0, n_estimators=121,
              n_jobs=-1, oob_score=False, random_state=25, verbose=0,
              warm_start=False)
In [97]:
clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini', max_depth=14, max_features='auto',
                  max leaf nodes=None, min impurity decrease=0.0, min impurity split=None, min samples leaf=28,
                 min_samples_split=111, min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1,
                 oob score=False, random state=25, verbose=0, warm start=False)
clf.fit(df_final_train,y_train)
```

```
y_train_pred = clf.predict(df_final_train)
y_test_pred = clf.predict(df_final_test)
print('Train f1 score',f1_score(y_train,y_train_pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
```

Train f1 score 0.9662060724899659 Test f1 score 0.926357979116127

In [108]:

```
# Created my own function with slight changes
def confusionmatrix(a, b):
  c_m = confusion_matrix(a, b)
  precision = (c_m / c_m.sum(axis=0))
  recall = (c_m.T / c_m.sum(axis=0)).T
  plt.figure(figsize=(20,4))
  labels = [1,2]
   # representing Confusion Matrix in heatmap format
```

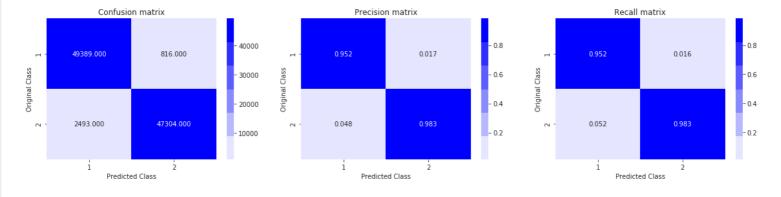
```
cmap=sns.light_palette("blue")
plt.subplot(1, 3, 1)
sns.heatmap(c_m, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Confusion matrix")
# representing Precision Matrix in heatmap format
plt.subplot(1, 3, 2)
sns.heatmap(precision, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Precision matrix")
plt.subplot(1, 3, 3)
# representing Recall Matrix in heatmap format
sns.heatmap(recall, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Recall matrix")
plt.show()
```

In [99]:

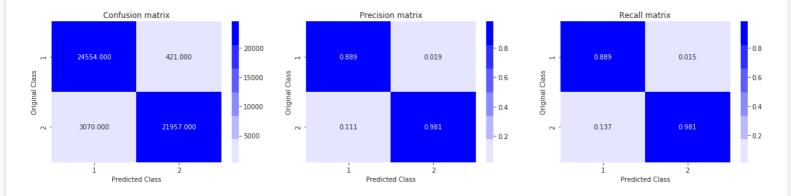
```
print('Train confusion_matrix')
confusionmatrix(y_train, y_train_pred)

print('Test confusion_matrix')
confusionmatrix(y_test, y_test_pred)
```

Train confusion_matrix



Test confusion_matrix

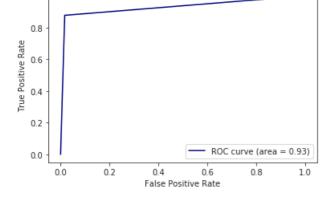


In [100]:

1.0

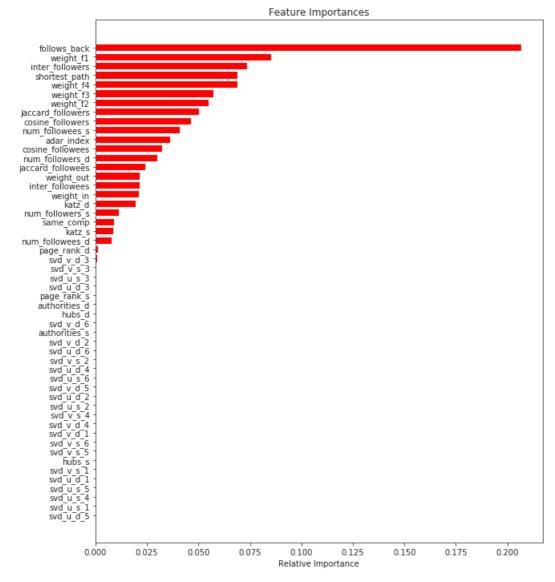
```
fpr, tpr, thresholds = roc_curve(y_test,y_test_pred)
auc_score = auc(fpr, tpr)

plt.plot(fpr, tpr, color='navy', label= 'ROC curve (area = %0.2f)' % auc_score)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver Operating Characteristic Curve with test data')
plt.legend()
plt.show()
```



In [101]:

```
# Feature Importances
importances = clf.feature_importances_
indices = np.argsort(importances)
features = df_final_train.columns
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.xlabel('Relative Importance')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.show()
```



Preferential Attachment feature

Preferential Attachement for followers

```
len(df_final_train.columns)
Out[91]:
52
In [92]:
#for train dataset
preferential_followers=[]
for i in range(len(df_final_train['num_followers_s'])):
           preferential\_followers.append (df\_final\_train['num\_followers\_s'][i] * df\_final\_train['num\_followers\_d'][i]) * df\_final\_train
df_final_train['preferential_Attachment_followers']= preferential_followers
df_final_train.head()
Out[92]:
                jaccard_followers jaccard_followees cosine_followers cosine_followees_num_followers_s num_followers_d in
    0
                                                 0.000000
                                                                                                                                          0.000
                                                                                                                                                                                                    0.000000
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    2
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                                                                                                                                                                                                    0.074032
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                                                 0.466667
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                                                 0.000000
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                                                 0.538462
                                                                                                                                          0.375
                                                                                                                                                                                                    0.212121
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                                                                                                                                                                                                                                                                                                                                                                                                                                                      11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               13
5 rows × 53 columns
In [93]:
#for test dataset
preferential_followers=[]
for i in range(len(df_final_test['num_followers_s'])):
           preferential\_followers.append (df\_final\_test['num\_followers\_s'][i] * df\_final\_test['num\_followers\_d'][i]) * df\_final\_test['num_followers\_d'][i]) * df\_final\_test['num_followers\_d'][i]) * df\_final\_test['num_followers\_d'][i]) * df\_final\_test['num_follow
df_final_test['preferential_Attachment_followers']= preferential_followers
df_final_test.head()
Out[93]:
               jaccard_followers jaccard_followers cosine_followers num_followers_s num_followers_d num_followees_d in
    0
                                                 0.052632
                                                                                                                            0.000000
                                                                                                                                                                                                    0.029161
                                                                                                                                                                                                                                                                           0.000000
                                                                                                                                                                                                                                                                                                                                                                                 6
                                                                                                                                                                                                                                                                                                                                                                                                                                                     14
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                                                 0.166667
                                                                                                                            0.125000
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                                                                                                                                                                                                                                                                                                                                                                             12
                                                                                                                                                                                                                                                                                                                                                                                                                                                     36
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                                                 0.028571
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                                                                                                                                                                                                                                                                                                                                                                                                                                                         3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  8
5 rows × 53 columns
```

In [94]:

#for train dataset

preferential_followees=[]

for i in range(len(df_final_train['num_followees_s'])):

preferential_followees.append(df_final_train['num_followees_s'][i] * df_final_train['num_followees_d'][i])

 $\label{thm:continuity} df_final_train['preferential_Attachment_followees'] = preferential_followees \\ df_final_train.head()$

Out[94]:

	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_followers_d	num_followees_s	num_followees_d in
0	0.000000	0.000	0.000000	0.000000	11	6	15	8
1	0.129032	0.000	0.065600	0.000000	22	13	11	0
2	0.466667	0.420	0.074032	0.601722	80	74	84	58
3	0.000000	0.000	0.000000	0.000000	64	8	73	7
4	0.538462	0.375	0.212121	0.554700	9	11	13	9

 $5 \text{ rows} \times 54 \text{ columns}$

4

In [95]:

#for test dataset

preferential_followees=[]

for i in range(len(df_final_test['num_followees_s'])):

preferential_followees.append(df_final_test['num_followees_s'][i] * df_final_test['num_followees_d'][i])

df_final_test['preferential_Attachment_followees']= preferential_followees df_final_test.head()

Out[95]:

	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_followers_d	num_followees_s	num_followees_d i
0	0.052632	0.000000	0.029161	0.000000	6	14	6	9
1	0.166667	0.125000	0.141421	0.223607	2	5	4	5
2	0.021277	0.020833	0.008019	0.047458	12	36	12	37
3	0.028571	0.000000	0.017010	0.000000	24	12	33	0
4	0.000000	0.000000	0.000000	0.000000	7	3	8	4

5 rows × 54 columns

-1

SVD DOT Feature

Train

```
In [98]:
```

SVD v feature

Train

In [100]:

In [102]:

```
df\_final\_train.head()
```

Out[102]:

	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_followers_d	num_followees_s	num_followees_d	ir
0	0.000000	0.000	0.000000	0.000000	11	6	15	8	
1	0.129032	0.000	0.065600	0.000000	22	13	11	0	
2	0.466667	0.420	0.074032	0.601722	80	74	84	58	
3	0.000000	0.000	0.000000	0.000000	64	8	73	7	
4	0.538462	0.375	0.212121	0.554700	9	11	13	9	

5 rows × 56 columns

SVD u feature

Test

In [99]:

```
df_final_test['svd_u_s_3'][i] * df_final_test['svd_u_d_3'][i] +\
    df_final_test['svd_u_s_4'][i] * df_final_test['svd_u_d_4'][i] +\
    df_final_test['svd_u_s_5'][i] * df_final_test['svd_u_d_5'][i] +\
    df_final_test['svd_u_s_6'][i] * df_final_test['svd_u_d_6'][i]
    )

df_final_test['svd_dot_u']=svd_dot_u_test
```

SVD v feature

Test

```
In [101]:
```

```
      svd_dot_v_test=[]

      for i in range(len(df_final_test['svd_v_s_1'])):

      svd_dot_v_test.append(df_final_test['svd_v_s_1'][i] * df_final_test['svd_v_d_2'][i] +\

      df_final_test['svd_v_s_2'][i] * df_final_test['svd_v_d_3'][i] +\

      df_final_test['svd_v_s_4'][i] * df_final_test['svd_v_d_4'][i] +\

      df_final_test['svd_v_s_5'][i] * df_final_test['svd_v_d_5'][i] +\

      df_final_test['svd_v_s_6'][i] * df_final_test['svd_v_d_6'][i]

      )

      df_final_test['svd_dot_v']=svd_dot_v_test
```

In [103]:

```
df_final_test.head()
```

Out[103]:

	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_followers_d	num_followees_s	num_followees_d ii
0	0.052632	0.000000	0.029161	0.000000	6	14	6	9
1	0.166667	0.125000	0.141421	0.223607	2	5	4	5
2	0.021277	0.020833	0.008019	0.047458	12	36	12	37
3	0.028571	0.000000	0.017010	0.000000	24	12	33	0
4	0.000000	0.000000	0.000000	0.000000	7	3	8	4

5 rows × 56 columns

Random Forest

With Preferential Attachment and SVD features

In [104]:

```
# return_train_score: boolean, default= False
```

If False, the cv_results_ attribute will not include training scores. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.

print('mean train scores', rf_random.cv_results_['mean_train_score'])

mean test scores [0.96233826 0.96225971 0.96007707 0.96189568 0.96379037 0.96108087 0.96090413 0.96241894 0.96172267 0.95968837] mean train scores [0.96361484 0.96301524 0.96100192 0.96315617 0.96499005 0.96171303 0.96154008 0.96316819 0.96279704 0.96034335]

In [105]:

```
print(rf_random.best_estimator_)
```

RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini', max_depth=14, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=28, min_samples_split=111, min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1, oob_score=False, random_state=25, verbose=0, warm_start=False)

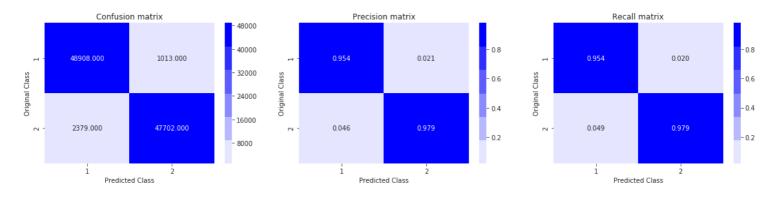
In [106]:

Train f1 score 0.9656666261791976 Test f1 score 0.9210320562939797

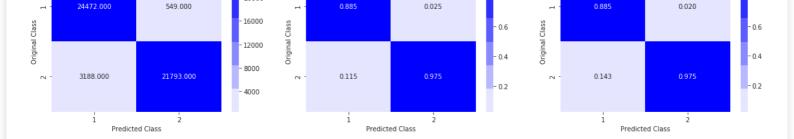
In [109]:

```
print('Train confusion_matrix')
confusionmatrix(y_train, y_train_pred)
print('Test confusion_matrix')
confusionmatrix(y_test, y_test_pred)
```

Train confusion_matrix

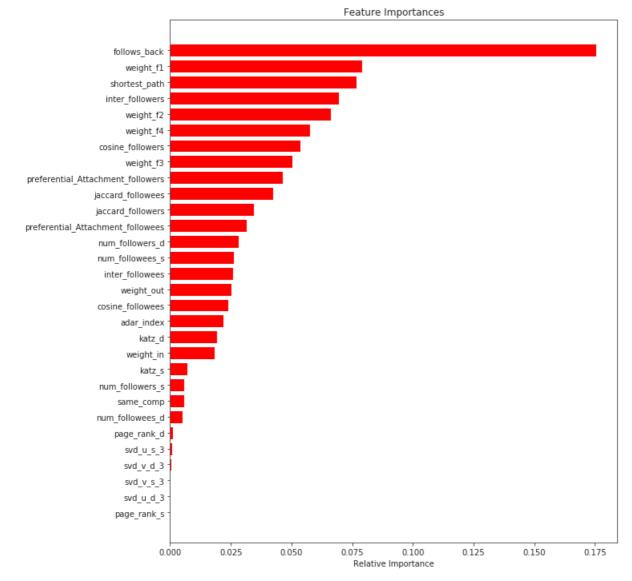


Test confusion_matrix



In [110]:

```
# Feature Importances
importances= clf.feature_importances_
indices = np.argsort(importances)[-30:]
features = df_final_train.columns
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.xlabel('Relative Importance')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.show()
```



XGBOOST

With Preferential Attachment and SVD features

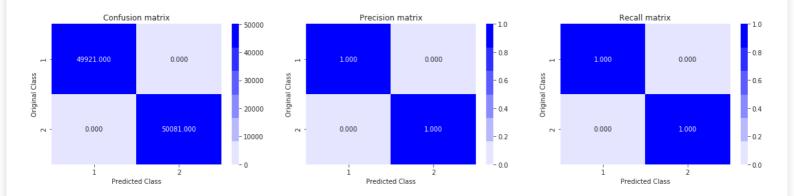
In [111]:

```
from datetime import datetime
start = datetime.now()
parameters = {'n_estimators' : [500, 1000, 2000],
'objective' : ['binary:logistic' | 'binary:hinge', 'reg:squarederror'].
```

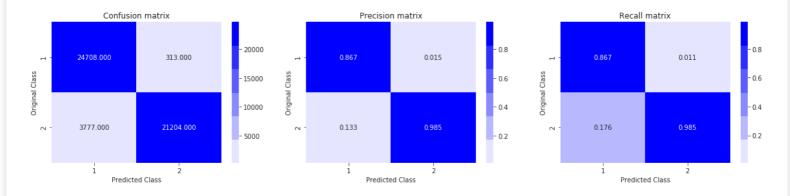
```
'eval_metric' : ['logloss', 'error'],
         'max_depth': [4, 6, 8],
         'eta': [0.001, 0.02, 0.3],
         'gamma': [0, 0.1, 5, 10, 15],
         'min_child_weight': [3, 5, 7],
         'reg_alpha': [0.005, 0.01, 0],
         'reg_lambda': [0.005, 0.01, 1]}
skf = StratifiedKFold(n_splits= 5)
rscv = RandomizedSearchCV(estimator = xgb.XGBClassifier(n_jobs= -1), param_distributions = parameters, n_jobs= -1,
                return_train_score= True, n_iter=10 ,cv= skf, scoring = 'roc_auc')
rscv.fit(df_final_train,y_train)
print('mean test scores', rscv.cv_results_['mean_test_score'])
# return_train_score: boolean, default= False
If False, the cv_results_ attribute will not include training scores. Computing training scores is used to get insights on
how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training
set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization
performance.
print('mean train scores', rscv.cv_results_['mean_train_score'])
print('Time taken to complete train linear data: ', datetime.now()-start)
mean test scores [0.98192473 0.99807957 0.99905358 0.98279969 0.97657257 0.9984245
0.99832342\ 0.97\widetilde{6}85208\ 0.99837079\ 0.99808177]
mean train scores [0.99990265 0.99841775 1.
                                                   0.99445838 0.97798179 0.99894275
0.99977899 0.9784888 0.99889181 0.99846017]
Time taken to complete train linear data: 1:29:33.399636
In [112]:
print(rscv.best estimator )
XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,
        colsample_bynode=1, colsample_bytree=1, eta=0.02,
        eval_metric='error', gamma=0.1, learning_rate=0.1,
        max_delta_step=0, max_depth=8, min_child_weight=7, missing=None,
        n estimators=1000, n jobs=-1, nthread=None,
        objective='binary:logistic', random_state=0, reg_alpha=0.005,
        reg_lambda=0.01, scale_pos_weight=1, seed=None, silent=None,
        subsample=1, verbosity=1)
In [113]:
clf = xgb.XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1, colsample_bynode=1, colsample_bytree=1,
               eta=0.02, eval_metric='error', gamma=0.1, learning_rate=0.1, max_delta_step=0, max_depth=8,
               min_child_weight=7, missing=None, n_estimators=1000, n_jobs=-1, nthread=None, random_state=0,
               objective='binary:logistic', reg_alpha=0.005, reg_lambda=0.01, seed=None, silent=None, subsample=1)
clf.fit(df_final_train,y_train)
y_train_pred = clf.predict(df_final_train)
y_test_pred = clf.predict(df_final_test)
print('Train f1 score',f1_score(y_train,y_train_pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
Train f1 score 1.0
Test f1 score 0.9120392274936556
In [114]:
print('Train confusion_matrix')
confusionmatrix(y_train, y_train_pred)
print('Test confusion_matrix')
```

confusionmatrix(y_test, y_test_pred)

Train confusion matrix



Test confusion_matrix

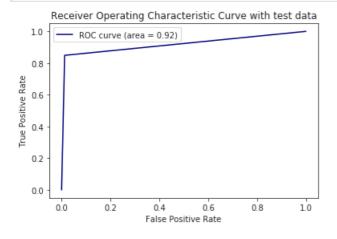


In [115]:

```
# ROC
```

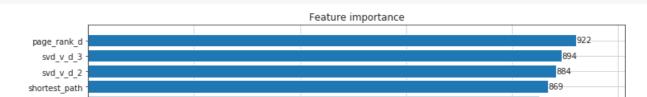
```
fpr, tpr, thresholds = roc_curve(y_test,y_test_pred)
auc_score = auc(fpr, tpr)

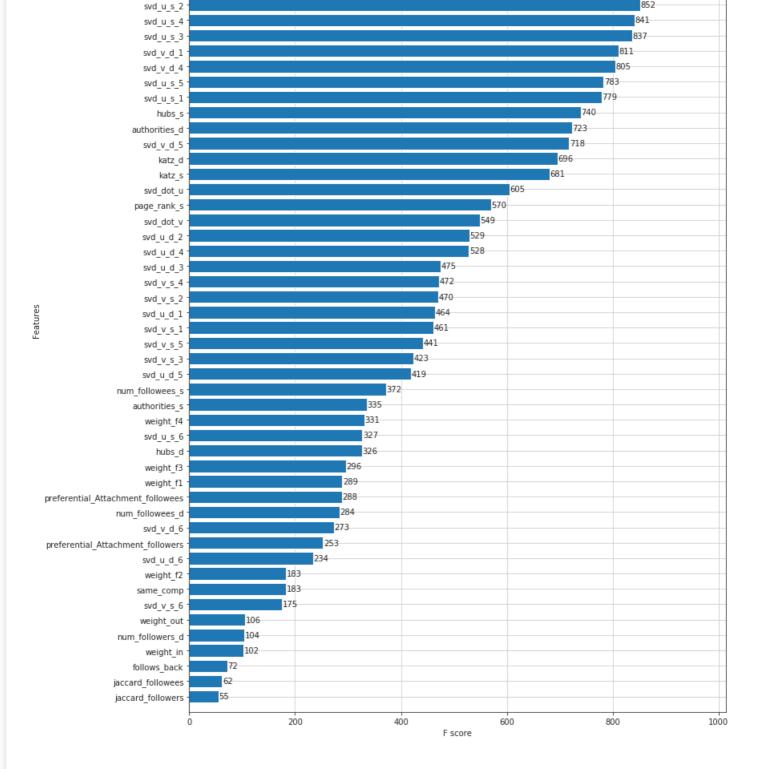
plt.plot(fpr, tpr, color='navy', label= 'ROC curve (area = %0.2f)' % auc_score)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver Operating Characteristic Curve with test data')
plt.legend()
plt.show()
```



In [116]:

```
# Feature Importances
# https://stackoverflow.com/a/44990345/10219869
fig, ax = plt.subplots(figsize=(12,18))
xgb.plot_importance(clf, max_num_features=50, height=0.8, ax=ax)
plt.show()
```





Conclusions

```
In [117]:
```

In []:

