

System Deployment Model | Policy Computation Algorithmic Control Flow

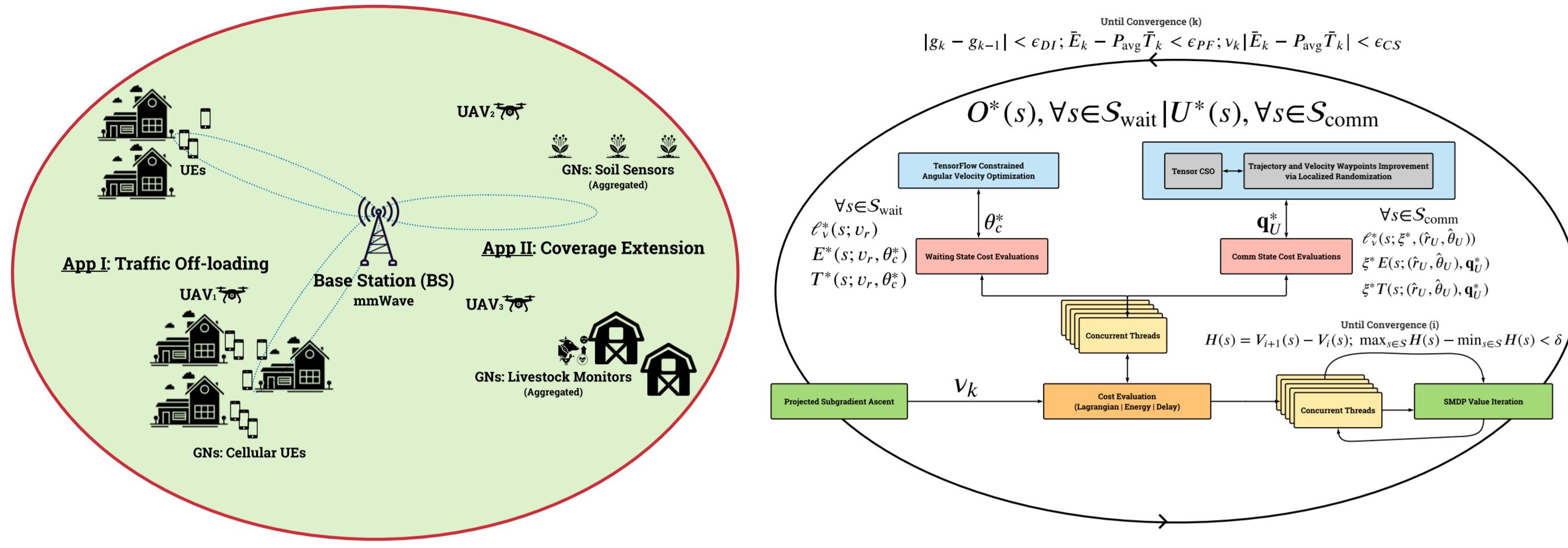


Figure 1. The deployment architecture under analysis: A cellular Base Station (BS) at the center of a circular cell of radius a meters, with multiple UAVs serving as BS relays for traffic off-loading and coverage extension (a); The algorithmic flowchart of our Semi-Markov Decision Process and Hierarchical Competitive Swarm Optimization framework to solve the single-agent two-stage scheduling and trajectory optimization problem (b).

Single-Agent Optimal Policy Computation: Mathematical Construction

- UAV Mobility Power Model: $P_{\text{mob}}(V) = P_1 \left(1 + \frac{3V^2}{U_{\text{tip}}^2} \right) + P_2 \left(\sqrt{1 + \frac{V^4}{4v_0^2} - \frac{V^2}{2v_0^2}} \right)^{1/2} + P_3 V^3$
- A2G Channel Model (with Rate Adaptation):

$$P_{\text{LoS}}(\varphi) = \frac{1}{1 + z_1 \cdot \exp(-z_2 [\varphi - z_1])}, \quad P_{\text{NLoS}}(\varphi) = 1 - P_{\text{LoS}}(\varphi); C(h) = B \cdot \log_2 \left(1 + \frac{|h|^2 P}{\sigma^2 \Gamma} \right)$$

$$P_{\text{out}}(\Upsilon, \beta, K) = 1 - Q_1 \left(\sqrt{2K}, \sqrt{2(K+1)u(\Upsilon, \beta)} \right); u(\Upsilon, \beta) \triangleq \sigma^2 \Gamma (2^{\Upsilon/B} - 1) / (\beta P)$$

$$R(\Upsilon, \beta, K) = \Upsilon \cdot (1 - P_{\text{out}}(\Upsilon, \beta, K)) = \Upsilon \cdot Q_1 \left(\sqrt{2K}, \sqrt{2(K+1)u(\Upsilon, \beta)} \right)$$

With $Z \triangleq \sqrt{\frac{2\beta P}{\sigma^2 \Gamma}} u(\Upsilon, \beta)$, $\Upsilon = B \log_2 \left(1 + \frac{1}{2} Z^2 \right) \triangleq f(Z)$ and $\Upsilon^*(\beta, K) = f(Z^*(\beta, K))$

$$Z^*(\beta, K) \triangleq \arg \min_{Z \geq 0} -\ln f(Z) - \ln Q_1 \left(\sqrt{2K}, \sqrt{\frac{(K+1)\sigma^2 \Gamma}{\beta P}} Z \right) \quad [\text{Bisection Method}]$$

$$\bar{R}(d, \varphi) \triangleq P_{\text{LoS}}(\varphi) \cdot R^*(\beta_{\text{LoS}}(d), K(\varphi)) + P_{\text{NLoS}}(\varphi) \cdot R^*(\beta_{\text{NLoS}}(d), 0)$$

Two-Stage Decision Framework | A Semi-Markov Decision Process (SMDP) formulation

- Waiting states ($s \in \mathcal{S}_{\text{wait}}$):
 - Outer decision | Optimal UAV radial velocity (v_r^*) | SMDP Value Iteration
 - Inner decision | Optimal UAV angular velocity (θ_c^*) | Solve

$$\ell_v^*(s; v_r) = \min_{\theta_c} \nu \left(P_{\text{mob}} \left(\sqrt{v_r^2 + r_U^2 \cdot \theta_c^2} \right) - P_{\text{avg}} \right) \Delta_0 \quad \text{s.t. } \sqrt{v_r^2 + r_U^2 \cdot \theta_c^2} \leq V_{\max}$$
- Communication states ($s \in \mathcal{S}_{\text{comm}}$):
 - Outer decision | Optimal UAV end position $(\hat{r}_U^*, \hat{\theta}_U^*)$ | SMDP Value Iteration
 - Inner decision I | Optimal scheduling strategy (ξ^*) | Pick the minimizing action between

$$\ell_\nu^*(s; r_U, 0) = L/\bar{R}_{GB}(r) \text{ and } \ell_\nu^*(s; \hat{r}_U, 1) = \min_{\Delta, q_U, t_p} (1 - \nu P_{\text{avg}}) \Delta + \nu \int_0^\Delta P_{\text{mob}} \left(\sqrt{r_U'(\eta)^2 + r_U^2(\eta) \cdot \theta_U'(\eta)^2} \right) d\eta$$

s.t. data payload, max velocity, and start & end position constraints
 - Inner decision II | Optimal trajectory | Hierarchical Competitive Swarm Optimization (HCSO)

$$\mathbf{P}^*, \mathbf{v}^* = \underset{\mathbf{p}, \mathbf{v} \in [V_{\text{low}}, V_{\text{max}}]^M}{\operatorname{argmin}} \left(1 - \nu P_{\text{avg}} \right) \sum_{m=0}^{M-1} \frac{\|\mathbf{x}_{m+1} - \mathbf{x}_m\|_2}{v_m} + \nu \sum_{m=0}^{M-1} \frac{\|\mathbf{x}_{m+1} - \mathbf{x}_m\|_2 P_{\text{mob}}(v_m)}{v_m}$$

s.t. data payload, max velocity, and start & end position constraints

Scenario Evaluation: Optimal SMDP-HCSO Policy + Multi-Agent Heuristics

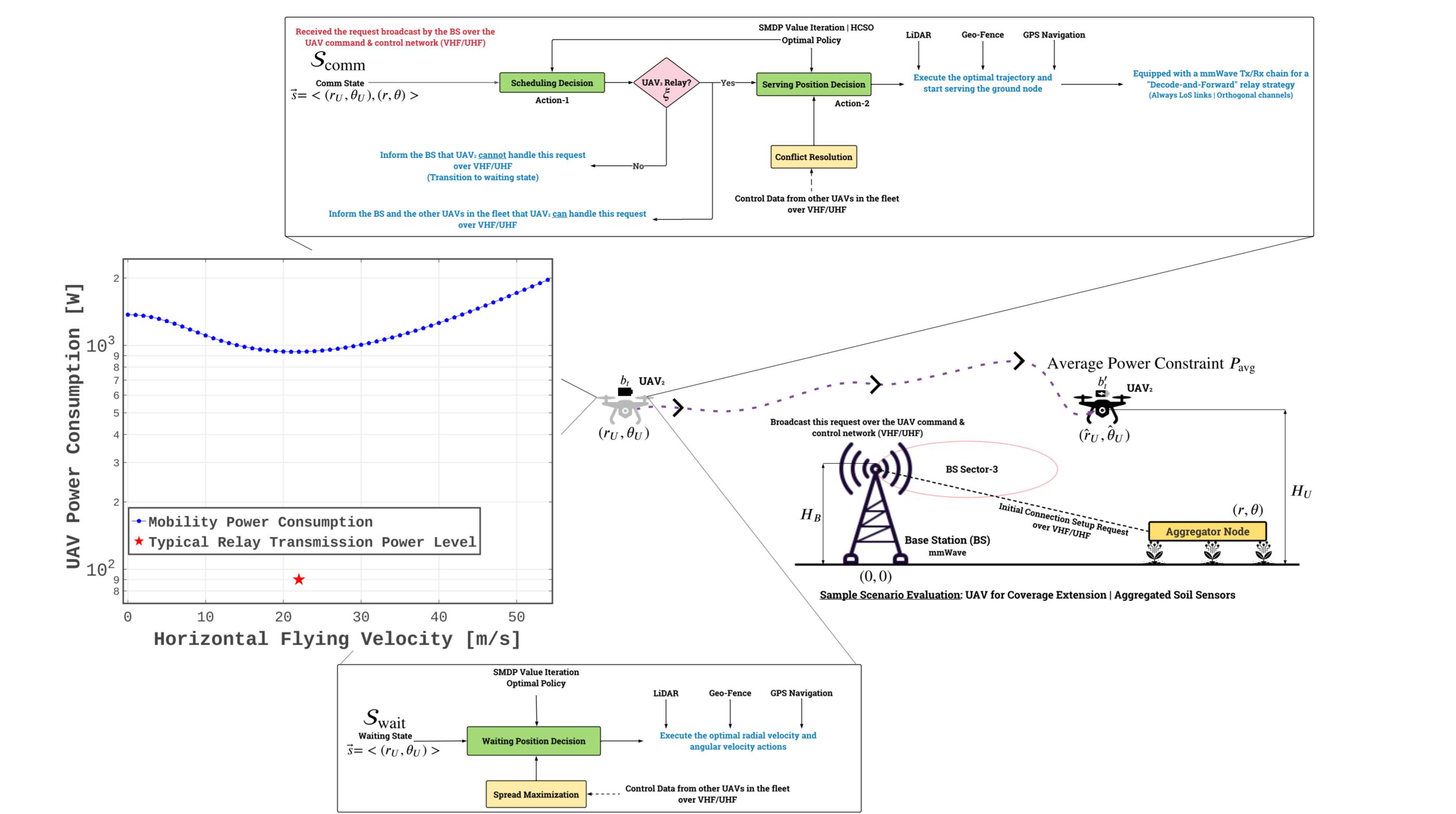


Figure 2. The multi-agent evaluation of optimal policy execution in smart agriculture from the perspective of UAV₂: coverage extension for soil sensors as Ground Nodes (via an aggregator node).

Visualizations: Delay-Power Trade-offs | Optimal Trajectories

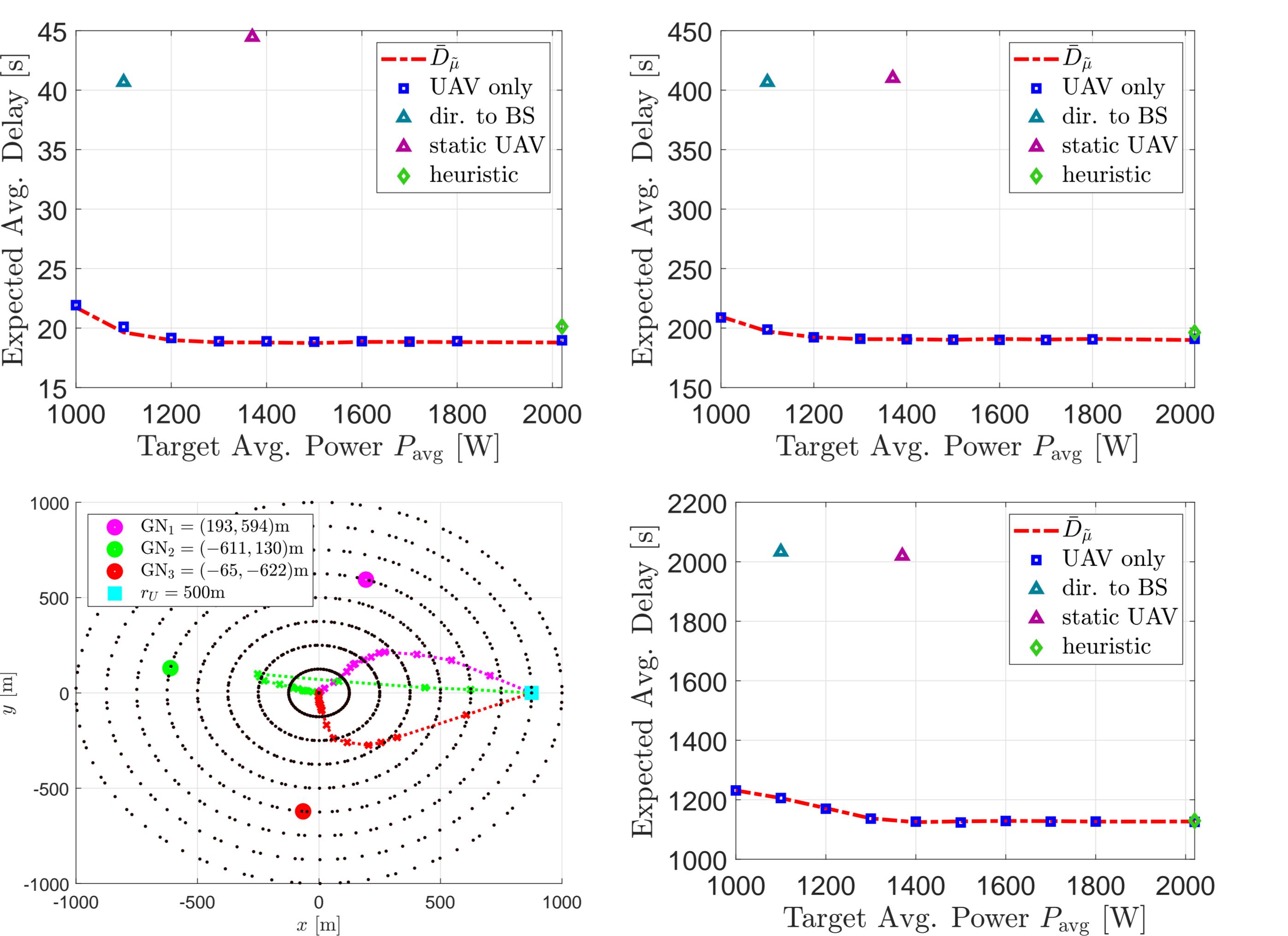


Figure 3. (Clockwise from top-left) The expected service delay versus the target average power constraint for varying packet lengths: 0.1Mb; 1.0Mb; 5.0Mb; The optimal UAV trajectories under 0.1Mb | $P_{\text{avg}}=1.1\text{kW}$. [M. Bliss and N. Michelusi, "Power-Constrained Trajectory Optimization for Wireless UAV Relays with Random Requests," IEEE ICC 2020]

Asynchronous Actor-Critic in a Double Deep-Q Network Framework

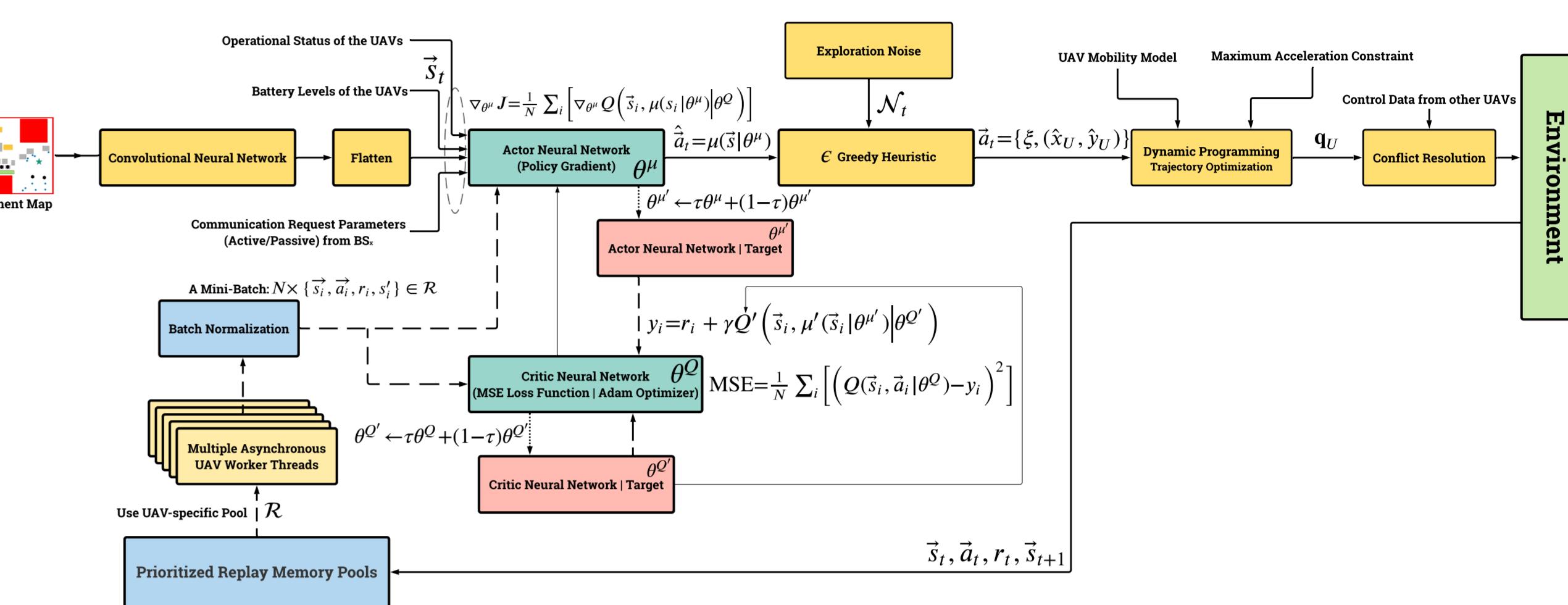


Figure 4. A different approach to UAV fleet automation: an asynchronous Actor-Critic structure with a Deep Deterministic Policy Gradient (DDPG) in the Actor and a Mean Square Error (MSE) driven Adam optimizer in the Critic—coupled with target networks, thread-specific hyper-parameter training, thread-specific prioritized experiential replay memory pools, and exploration noise (via an ϵ -greedy heuristic). Equipped with advanced UAV power & mobility models, additional constraints such as maximum UAV acceleration are imposed in the trajectory optimization paradigm—solved via Dynamic Programming. [T. P. Lillicrap, et al., "Continuous Control with Deep RL," ICLR 2016]

Companion Research: NSF POWDER Millimeter-Wave Propagation Modeling

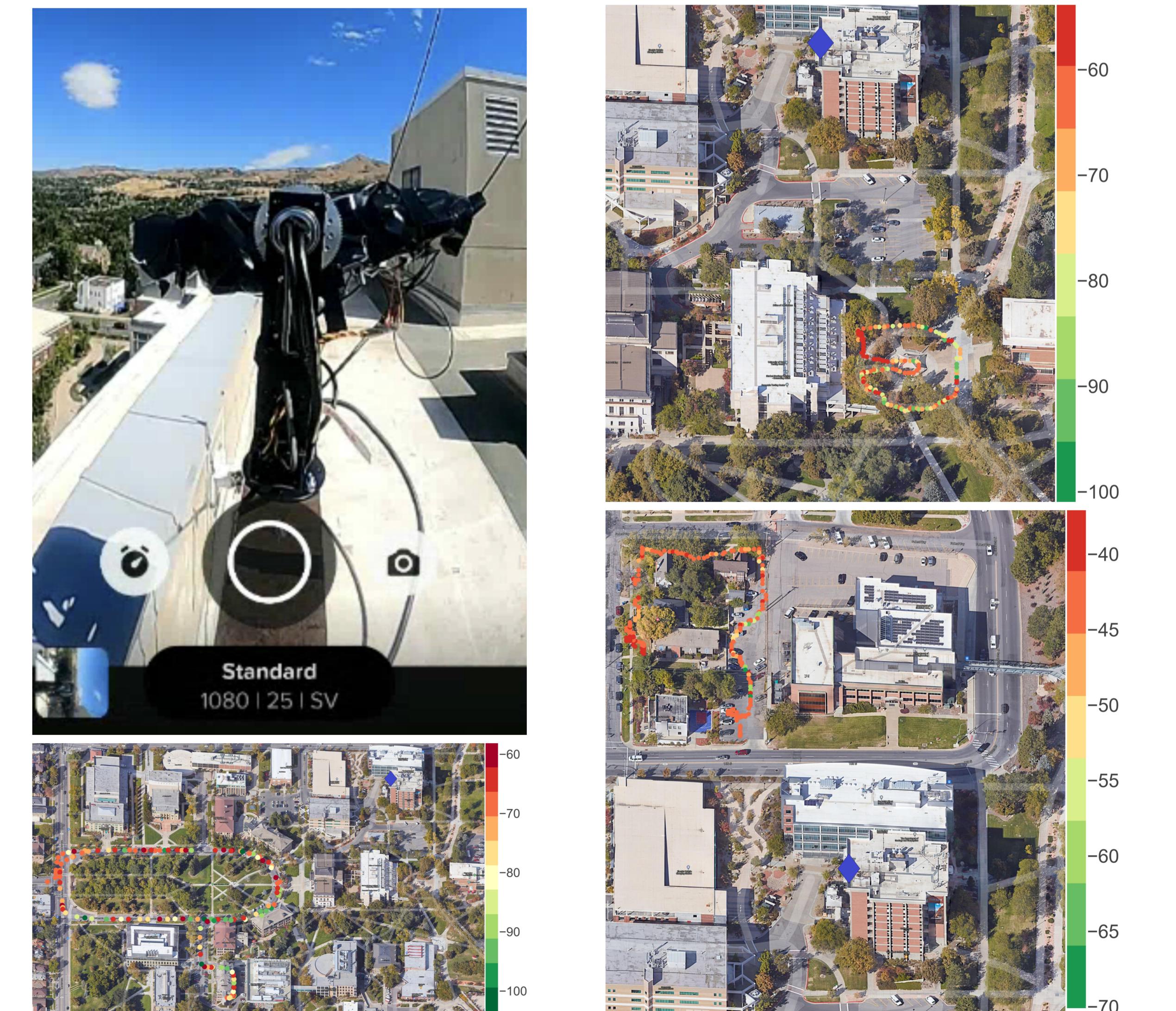


Figure 5. (Clockwise from top-left) Our remote monitoring & troubleshooting interface—via an Android Debug Bridge—exhibiting the deployment of our Tx on the roof-top of the William Browning Building; The illustrations of the received signal power values superimposed on a Google Hybrid map of the sites under analysis. [B. Keshavamurthy, et al., "A Robotic Antenna Alignment and Tracking System for Millimeter Wave Propagation Modeling," USNC-URSI NRSM 2022]