

R PROGRAMMING



ROOT FINDING

For real or complex polynomials, one can use the `polyroot()` function. To solve

$$f(x)=x^2-2x-3=0$$

```
polyroot(c(-3, -2, 1))
```

EIGEN VALUES

```
A<-matrix(c(13, -4, 2, -4, 11, -2, 2, -2, 8), 3, 3, byrow=TRUE)
```

```
A
```

```
print(eigen(A))
```

LINEAR REGRESSION

- The steps to create the relationship is –
 - Carry out the experiment of gathering a sample of observed values of height and corresponding weight.
 - Create a relationship model using the **lm()** functions in R.
 - Find the coefficients from the model created and create the mathematical equation using these
 - Get a summary of the relationship model to know the average error in prediction. Also called **residuals**.
 - To predict the weight of new persons, use the **predict()** function in R.

LINEAR REGRESSION

- `lm()` Function
 - This function creates the relationship model between the predictor and the response variable.
- Syntax
 - The basic syntax for **`lm()`** function in linear regression is –
`lm(formula,data)`
- Following is the description of the parameters used –
 - **formula** is a symbol presenting the relation between x and y.
 - **data** is the vector on which the formula will be applied.

LINEAR REGRESSION

- predict() Function
- Syntax
 - The basic syntax for predict() in linear regression is – predict(object,newdata)
- Following is the description of the parameters used –
 - **object** is the formula which is already created using the lm() function.
 - **newdata** is the vector containing the new value for predictor variable.

LINEAR REGRESSION: GET THE COEFFICIENTS

```
x <- c(15, 17, 18, 16, 12, 13, 19, 10, 15, 11)
```

```
y <- c(63, 81, 56, 91, 47, 57, 76, 72, 62, 48)
```

```
# Apply the lm() function.
```

```
relation<-lm(y~x)
```

```
Print(relation)
```

LINEAR REGRESSION:PREDICTING FOR NEW DATA

```
x <- c(15, 17, 18, 16, 12, 13, 19, 10, 15, 11)
```

```
y <- c(63, 81, 56, 91, 47, 57, 76, 72, 62, 48)
```

```
# Apply the lm() function.
```

```
relation<-lm(y~x)
```

```
print(summary(relation))
```

```
a<-data.frame(x = 170)
```

```
result<-predict(relation,a)
```

```
print(result)
```


SINGULAR VALUES

- Singular values of a $M \times N$ matrix A are the square roots of the eigen values of the $N \times N$ matrix $A(A^T)$.

SINGULAR VALUE DECOMPOSITION (SVD)

- Handy mathematical technique that has application to many problems
- Given any $m \times n$ matrix \mathbf{A} , algorithm to find matrices \mathbf{U} , \mathbf{V} , and \mathbf{W} such that

$$\mathbf{A} = \mathbf{U} \mathbf{W} \mathbf{V}^T$$

\mathbf{U} is $m \times n$ and orthonormal

\mathbf{W} is $n \times n$ and diagonal

\mathbf{V} is $n \times n$ and orthonormal

SVD

- The w_i are called the singular values of \mathbf{A}
- If \mathbf{A} is singular, some of the w_i will be 0
- In general $\text{rank}(\mathbf{A}) = \text{number of nonzero } w_i$
- SVD is mostly unique (up to permutation of singular values, or if some w_i are equal)

SVD

```
A<-matrix(c(13, -4, 2, -4, 11, -2, 2, -2, 8), 3, 3, byrow=TRUE)
```

```
(s <- svd(A))
```

```
D <- diag(s$d)
```

```
print(D)
```

```
s$u %*% D %*% t(s$v) #  $X = U D V'$ 
```

```
t(s$u) %*% A %*% s$v #  $D = U' X V$ 
```