

```
--  
title: "BA Project"  
author: " Bharati Malik"  
output:  
  pdf_document: default  
  word_document: default  
editor_options:  
  chunk_output_type: console  
--  
  
```{r}  
You should generally clear the working space at the start of every R session
rm(list = ls())

Set the directory
setwd("C:/Users/asark/Desktop/Bharati SCU/1st Quarter/OMIS 2392 Econometrics with R (Lecture) Tue
Thurs 7.35pm to 9.10 pm/0 BA projet/BOPS")

install packages
#install.packages("readstata13")

Load libraries
library(stargazer)
library(gdata)
library(ggplot2)
library(psych)
library(ggeffects)
library(QuantPsyc)
library(readstata13)
library(lmtest)
library(usdm)
library(multiwayvcov)
library(sandwich)
library(foreign)
library(AER)
library(aod)
library(Rcpp)
library(mfx)
library(nnet)
library(reshape2)
library(msm)

turn off scientific notation.
options(scipen = 9)
...
...
```

```
#=====

Data Loading

#=====


```{r}  

cust_Level=read.dta13("C:/Users/asark/Desktop/Bharati SCU/1st Quarter/OMIS 2392 Econometrics with R (Lecture) Tue Thurs 7.35pm to 9.10 pm/0 BA projet/BOPS/consumer level data.dta")  

ODS_prodcat=read.dta13("C:/Users/asark/Desktop/Bharati SCU/1st Quarter/OMIS 2392 Econometrics with R (Lecture) Tue Thurs 7.35pm to 9.10 pm/0 BA projet/BOPS/online daily prod_cat sales-returns data.dta")  

ODS_Overall=read.dta13("C:/Users/asark/Desktop/Bharati SCU/1st Quarter/OMIS 2392 Econometrics with R (Lecture) Tue Thurs 7.35pm to 9.10 pm/0 BA projet/BOPS/online daily sales-returns data.dta")  

trans_level=read.dta13("C:/Users/asark/Desktop/Bharati SCU/1st Quarter/OMIS 2392 Econometrics with R (Lecture) Tue Thurs 7.35pm to 9.10 pm/0 BA projet/BOPS/transaction level data.dta")  

head(cust_Level)  

head(ODS_prodcat)  

head(ODS_Overall)  

head(trans_level) # view the first few rows of the data
```

BA Project_BOPS_Final Submitted.Rmd x cust_Level x ODS_Overall x ODS_prodcat x trans_level x

	customer_id	store_number	age_band	est_income_code	homeowner_code	length_of_residence	child	female	bops_in_effect	salesvalue	salesquantity	purchase_time_period	bops_user
1	103465	2	5	7 R		15	Y	0	0	195.30	1	1	0
2	103465	2	5	7 R		15	Y	0	1	179.00	1	1	0
3	106978	2	9	4 O		3	Y	NA	0	72.00	1	1	0
4	106978	2	9	4 O		3	Y	NA	1	90.16	2	4	0
5	107501	2	9	1 O		15	N	0	0	2898.00	2	7	0
6	107501	2	9	1 O		15	N	0	1	1873.01	8	21	0
7	112054	2	0	6 O		2	Y	0	0	169.15	1	1	1
8	112054	2	0	6 O		2	Y	0	1	335.96	4	5	1
9	113914	2	9	7 O		13	Y	1	0	558.41	1	1	0
10	113914	2	9	7 O		13	Y	1	1	143.99	1	1	0
11	113980	2	0	7 O		2	Y	NA	0	89.10	1	1	0

Showing 1 to 12 of 84,420 entries

BA Project_BOPS_Final Submitted.Rmd x cust_Level x ODS_Overall x ODS_prodcat x trans_level x

	store_number	year	month	month_index	month_dummy	bops_in_effect	day	salesvalue	returnvalue	salesquantity	returnquantity	avg.	
1	2	2012	MAR	32	3	1	583	327516.28	54313.5586	1477	168	^	
2	2	2010	AUG	13	8	0	1	1290.03	48.9900	11	1		
3	2	2010	AUG	13	8	0	2	226777.23	33090.8086	1701	214		
4	2	2010	AUG	13	8	0	3	164627.44	25445.7695	1054	118		
5	2	2010	AUG	13	8	0	4	202743.41	45929.0586	1031	155		
6	2	2010	AUG	13	8	0	5	168273.48	26244.8496	988	100		
7	2	2010	AUG	13	8	0	6	161634.70	26731.4492	804	106		
8	2	2010	AUG	13	8	0	7	11058.96	1583.1799	77	11		
9	2	2010	AUG	13	8	0	8	241.69	0.0000	3	0		
10	2	2010	AUG	13	8	0	9	247811.56	36102.4297	1581	205		

Showing 1 to 12 of 2,858 entries

BA Project_BOPS_Final Submitted.Rmd | cust_Level | ODS_Overall | ODS_prodcat | trans_level | Filter | Search

y	salesvalue	returnvalue	salesquantity	returnquantity	avg_female	avg_age	avg_income	avg_homeowner	avg_residency	avg_chldowner
583	327516.28	54313.5586		1477	168	0.5238829	4.363883	5.083560	0.5835598	6.724864
1	1290.03	48.9900		11	1	0.4444444	3.181818	4.545455	0.7272727	8.272727
2	226777.23	33090.8086		1701	214	0.5964794	4.982840	5.563905	0.6390532	7.076331
3	164627.44	25445.7695		1054	118	0.5744456	4.905033	5.462488	0.6201330	6.236467
4	202743.41	45929.0586		1031	155	0.5719063	5.119534	5.565598	0.6209912	7.001944
5	168273.48	26244.8496		988	100	0.5875706	5.084093	5.530902	0.6727457	7.467072
6	161634.70	26731.4492		804	106	0.5497954	5.022444	5.524938	0.6321696	7.008728
7	11058.96	1583.1799		77	11	0.5652174	4.578948	5.644737	0.5263158	6.736842
8	241.69	0.0000		3	0	0.0000000	3.333333	4.333333	0.6666667	4.000000
9	247811.56	36102.4297		1581	205	0.6028268	4.953768	5.620646	0.6846105	7.150728
10	1000.00	1000.00		272	110	0.5500000	5.000000	5.550000	0.6666667	6.000000
11	1000.00	1000.00		272	110	0.5500000	5.000000	5.550000	0.6666667	6.000000

Showing 1 to 12 of 2,858 entries

BA Project_BOPS_Final Submitted.Rmd | cust_Level | ODS_Overall | ODS_prodcat | trans_level | Filter | Search

store_number	year	month	month_index	product_category	month_dummy	bops_in_effect	day	salesvalue	returnvalue	salesquantity
1	2	2012	MAR		32	5	3	583	39173.61	4828.76
2	2	2010	AUG		13	4	8	0	201.18	0.00
3	2	2010	AUG		13	5	8	0	836.58	0.00
4	2	2010	AUG		13	13	8	0	203.28	0.00
5	2	2010	AUG		13	2	8	0	48.99	48.99
6	2	2010	AUG		13	12	8	0	25299.30	2745.30
7	2	2010	AUG		13	2	8	0	23478.47	3603.17
8	2	2010	AUG		13	4	8	0	51394.78	8993.87
9	2	2010	AUG		13	6	8	0	8042.66	2386.88
10	2	2010	AUG		13	21	8	0	19178.07	3335.25
11	2	2010	AUG		13	5	8	0	25100.00	2770.00

Showing 1 to 12 of 30,475 entries

BA Project_BOPS_Final Submitted.Rmd | cust_Level | ODS_Overall | ODS_prodcat | trans_level | Filter | Search

salesvalue	returnvalue	salesquantity	returnquantity	avg_female	avg_age	avg_income	avg_homeowner	avg_residency	avg_chldowner
39173.61	4828.76	300	29	0.5092251	4.993311	5.612794	0.6296296	7.037037	0.36363637
201.18	0.00	1	0	1.0000000	0.0000000	8.000000	1.0000000	4.000000	0.00000000
836.58	0.00	7	0	0.5000000	3.714286	4.428571	0.8571429	8.428572	0.28571430
203.28	0.00	2	0	0.0000000	2.500000	4.500000	0.5000000	10.000000	0.00000000
48.99	48.99	1	1	0.0000000	4.000000	2.000000	0.0000000	8.000000	1.00000000
25299.30	2745.30	367	34	0.6012461	5.046448	5.691257	0.6229508	7.628415	0.39071038
23478.47	3603.17	178	25	0.6894410	5.393259	4.966292	0.5842696	5.707865	0.34269664
51394.78	8993.87	236	38	0.4747475	4.474576	5.987288	0.6271186	7.495763	0.34745762
8042.66	2386.88	42	8	0.6842105	5.571429	5.047619	0.5714286	5.309524	0.28571430
19178.07	3335.25	246	43	0.6574074	4.630705	5.634855	0.6970955	7.419087	0.33195022
25100.00	2770.00	272	27	0.5500000	5.550000	5.550000	0.6666667	6.000000	0.00000000

Showing 1 to 12 of 30,475 entries

BA Project_BOPS_Final Submitted.Rmd cust_Level ODS_Overall ODS_prodcat trans_level

	customer_id	purchase_date	transaction_id	store_number	price	sku	return	age_band	est_income_code	homeowner_code	length_of_residence
1	308421329614	05MAR2012:00:00:00	50002	2	386.55	12987079	0	7	8	O	
2	308421329614	05MAR2012:00:00:00	50002	2	1236.06	14550214	0	7	8	O	
3	12311873	01AUG2010:00:00:00	2038802	2	201.18	18094953	0	0	8	O	
4	822140002460	01AUG2010:00:00:00	2038804	2	199.00	18012591	0	5	3	O	
5	308431622663	01AUG2010:00:00:00	2038806	2	28.98	18095406	0	0	3	O	
6	25133466	01AUG2010:00:00:00	2038808	2	217.15	17812314	0	5	6	O	
7	22604254	01AUG2010:00:00:00	2038811	2	86.27	17581620	0	5	3	O	
8	22604254	01AUG2010:00:00:00	2038811	2	47.21	18095174	0	5	3	O	
9	22604254	01AUG2010:00:00:00	2038811	2	86.28	18072892	0	5	3	O	
10	26196930	01AUG2010:00:00:00	2038818	2	163.84	16928277	0	6	7	O	
11	6001711	01AUG2010:00:00:00	2038801	2	211.00	17580174	0	0	6	O	

Showing 1 to 12 of 1,671,502 entries

BA Project_BOPS_Final Submitted.Rmd cust_Level ODS_Overall ODS_prodcat trans_level

homeowner_code	length_of_residence	child	year	month	month_index	product_category	month_dummy	week_index	bops	female
3 O	2	Y	2012	MAR	32	5	3	84	0	0
3 O	2	Y	2012	MAR	32	5	3	84	0	0
3 O	4	N	2010	AUG	13	4	8	1	NA	1
3 O	4	Y	2010	AUG	13	5	8	1	NA	0
3 O	12	N	2010	AUG	13	5	8	1	NA	1
5 O	14	Y	2010	AUG	13	5	8	1	NA	1
3 O	5	N	2010	AUG	13	5	8	1	NA	0
3 O	5	N	2010	AUG	13	5	8	1	NA	0
3 O	5	N	2010	AUG	13	13	8	1	NA	0
7 O	4	N	2010	AUG	13	5	8	1	NA	1
..	2010	AUG

Showing 1 to 12 of 1,671,502 entries

````

#=====#

**## Question1: What is the impact of implementing BOPS strategy on online channel sales?**

#=====#

``{r}

**#Descriptive Statistics**

stargazer(ODS\_Overall, type="text", median=TRUE, iqr=TRUE,digits=1, title="Descriptive Statistics")

**Descriptive Statistics**

| Statistic      | N     | Mean     | St. Dev.  | Min   | Pctl(25) | Median   | Pctl(75)  | Max         |
|----------------|-------|----------|-----------|-------|----------|----------|-----------|-------------|
| store_number   | 2,858 | 1,635.6  | 2,668.4   | 2     | 2        | 6        | 5,998     | 5,998       |
| year           | 2,858 | 2,011.6  | 0.9       | 2,010 | 2,011    | 2,012    | 2,012     | 2,013       |
| month_index    | 2,858 | 31.0     | 10.2      | 13    | 22       | 31       | 40        | 48          |
| month_dummy    | 2,858 | 6.5      | 3.5       | 1     | 3        | 6        | 10        | 12          |
| bops_in_effect | 2,858 | 0.6      | 0.5       | 0     | 0        | 1        | 1         | 1           |
| day            | 2,858 | 564.6    | 311.0     | 1     | 298.2    | 564      | 837       | 1,096       |
| salesvalue     | 2,858 | 99,619.0 | 180,986.6 | 0.0   | 8,157.6  | 18,157.7 | 152,580.9 | 1,685,114.0 |
| returnvalue    | 2,858 | 15,346.2 | 26,160.0  | 0.0   | 799.0    | 2,646.6  | 24,473.5  | 200,464.5   |
| salesquantity  | 2,858 | 584.9    | 1,146.3   | 1     | 43       | 106      | 784.2     | 11,630      |
| returnquantity | 2,858 | 59.1     | 106.5     | 0     | 4        | 10       | 89.8      | 895         |
| avg_female     | 2,265 | 0.5      | 0.2       | 0.0   | 0.5      | 0.5      | 0.6       | 1.0         |
| avg_age        | 2,345 | 4.9      | 1.7       | 0.0   | 4.5      | 5.0      | 5.5       | 13.0        |
| avg_income     | 2,334 | 5.3      | 0.9       | 1.0   | 5.1      | 5.4      | 5.6       | 9.0         |
| avg_homeowner  | 2,334 | 0.7      | 0.2       | 0.0   | 0.6      | 0.7      | 0.7       | 1.0         |
| avg_residency  | 2,334 | 7.0      | 2.1       | 0.0   | 6.7      | 7.1      | 7.5       | 15.0        |
| avg_childowner | 2,334 | 0.4      | 0.2       | 0.0   | 0.3      | 0.4      | 0.4       | 1.0         |

```
#Filtering data for days before sept.27,2012, when BOPS was implemented only for stores 2&6.
sales1 <- ODS_Overall[(ODS_Overall$day<786),]
```

Showing 1 to 8 of 2,005 entries

Showing 1 to 8 of 2,005 entries

```
#Add a BIE timeline variable dividing the data into two groups, one before Aug.1, 2011 and the other after.
```

```
#Add a grouping variable for stores dividing the data into two groups, one for 2&6 and the other for 5998.
```

```
sales1$BIE_timeline <- ifelse(sales1$day<366,0,1)
sales1$group_store <- ifelse((sales1$store_number==2) | (sales1$store_number==6),1,0)
```

Showing 1 to 8 of 2,005 entries

```
#Assuming mean value for all 'na' values
```

```
sales1$avg_female[is.na(sales1$avg_female)] <- mean(sales1$avg_female, na.rm = TRUE)
```

```

sales1$avg_age[is.na(sales1$avg_age)] <- mean(sales1$avg_age, na.rm = TRUE)
sales1$avg_income[is.na(sales1$avg_income)] <- mean(sales1$avg_income, na.rm = TRUE)
sales1$avg_chldowner[is.na(sales1$avg_chldowner)] <- mean(sales1$avg_chldowner, na.rm = TRUE)
sales1$avg_homeowner[is.na(sales1$avg_homeowner)] <- mean(sales1$avg_homeowner, na.rm = TRUE)

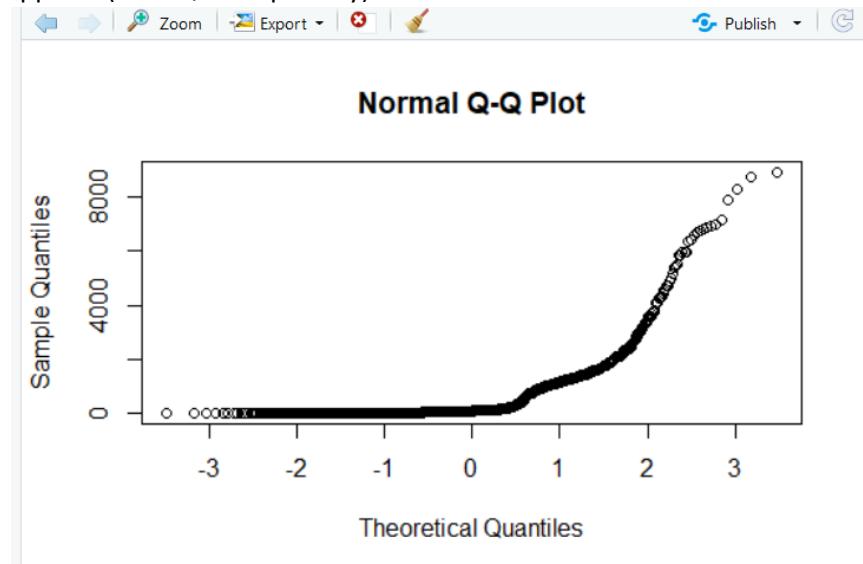
```

```
stargazer(sales1, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

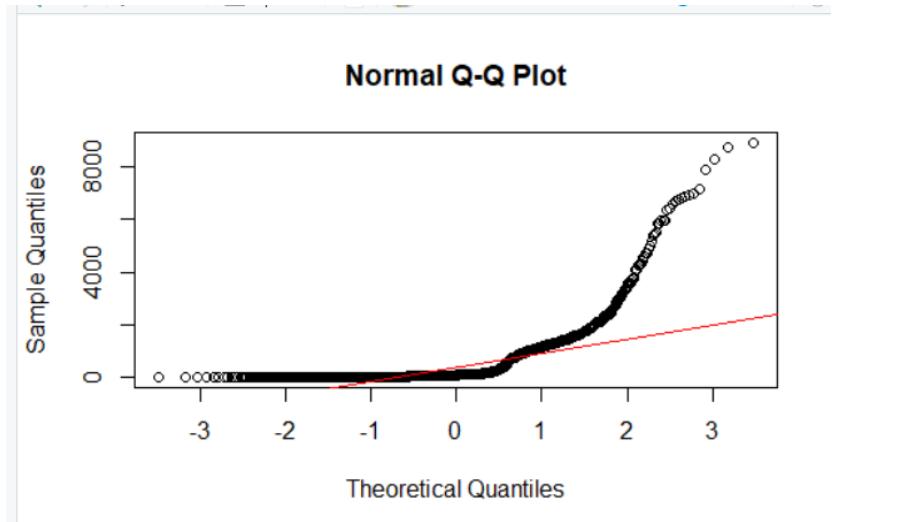
| Descriptive Statistics |       |          |           |       |          |          |           |             |
|------------------------|-------|----------|-----------|-------|----------|----------|-----------|-------------|
| Statistic              | N     | Mean     | St. Dev.  | Min   | Pctl(25) | Median   | Pctl(75)  | Max         |
| store_number           | 2,005 | 1,579.4  | 2,639.1   | 2     | 2        | 6        | 5,998     | 5,998       |
| year                   | 2,005 | 2,011.2  | 0.7       | 2,010 | 2,011    | 2,011    | 2,012     | 2,012       |
| month_index            | 2,005 | 25.8     | 7.3       | 13    | 20       | 26       | 32        | 38          |
| month_dummy            | 2,005 | 6.6      | 3.4       | 1     | 4        | 7        | 9         | 12          |
| bops_in_effect         | 2,005 | 0.4      | 0.5       | 0     | 0        | 0        | 1         | 1           |
| day                    | 2,005 | 404.8    | 221.0     | 1     | 215      | 411      | 593       | 785         |
| salesvalue             | 2,005 | 91,493.4 | 164,109.9 | 0.0   | 7,248.1  | 16,249.7 | 148,777.0 | 1,413,919.0 |
| returnvalue            | 2,005 | 14,406.6 | 24,454.2  | 0.0   | 681.4    | 2,387.7  | 24,014.7  | 192,876.8   |
| salesquantity          | 2,005 | 523.0    | 989.2     | 1     | 38       | 98       | 760       | 8,933       |
| returnquantity         | 2,005 | 55.2     | 97.8      | 0     | 3        | 10       | 88        | 876         |
| avg_female             | 2,005 | 0.5      | 0.2       | 0.0   | 0.5      | 0.5      | 0.6       | 1.0         |
| avg_age                | 2,005 | 5.1      | 1.5       | 0.0   | 4.7      | 5.1      | 5.5       | 13.0        |
| avg_income             | 2,005 | 5.4      | 0.8       | 1.0   | 5.2      | 5.4      | 5.5       | 9.0         |
| avg_homeowner          | 2,005 | 0.7      | 0.2       | 0.0   | 0.6      | 0.7      | 0.7       | 1.0         |
| avg_residency          | 1,633 | 7.1      | 2.1       | 0.0   | 6.7      | 7.0      | 7.5       | 15.0        |
| avg_chldowner          | 2,005 | 0.4      | 0.1       | 0.0   | 0.3      | 0.4      | 0.4       | 1.0         |
| BIE_timeline           | 2,005 | 0.6      | 0.5       | 0     | 0        | 1        | 1         | 1           |
| group_store            | 2,005 | 0.7      | 0.4       | 0     | 0        | 1        | 1         | 1           |

```
#check normalization
```

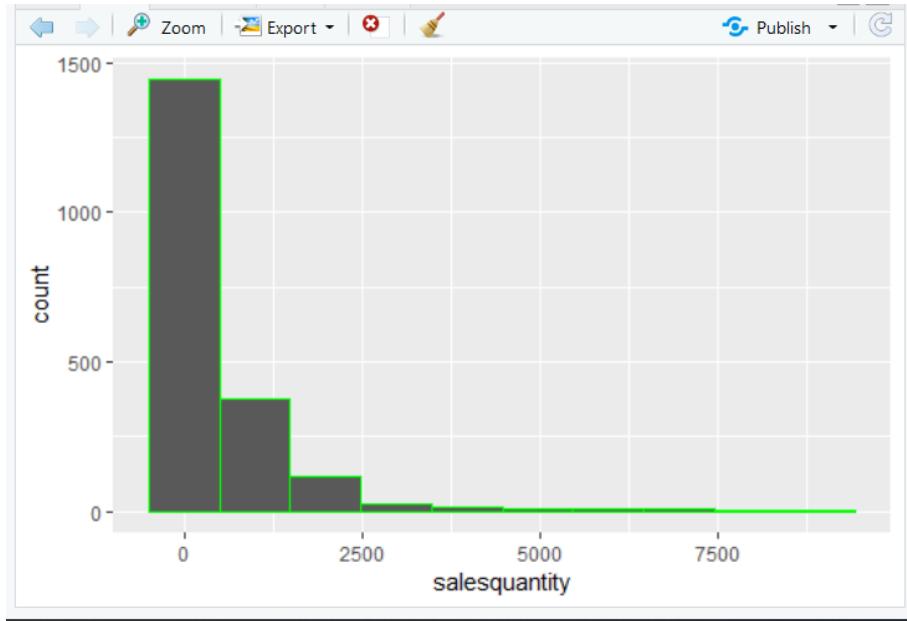
```
qqnorm(sales1$salesquantity)
```



```
qqline(sales1$salesquantity, col=2)
```



```
ggplot(sales1, aes(x=salesquantity)) + geom_histogram(colour="green", bins= 10)
```



#Analysing trend in raw dataset with boxplot for salesquantity.

```
df11 <- data.frame(salesquantity=sales1$salesquantity, BIE_timeline=as.factor(sales1$BIE_timeline))
```

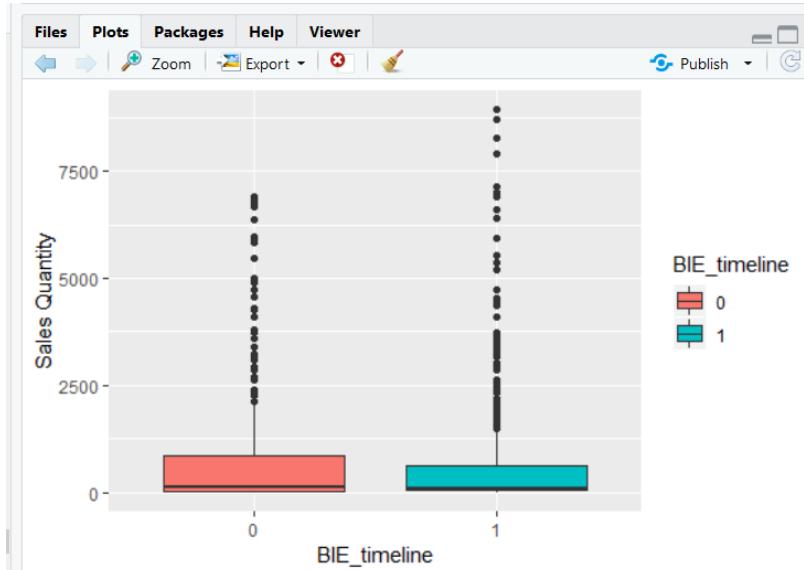
BA Project\_BOPS\_Final Submitted.Rmd\* df11 sales1

Filter

|   | salesquantity | BIE_timeline |
|---|---------------|--------------|
| 1 | 1477          | 1            |
| 2 | 11            | 0            |
| 3 | 1701          | 0            |
| 4 | 1054          | 0            |
| 5 | 1031          | 0            |
| 6 | 988           | 0            |
| 7 | 804           | 0            |
| 8 | 77            | 0            |

Showing 1 to 8 of 2,005 entries

```
ggplot(df11, aes(x=BIE_timeline, y=salesquantity, fill=BIE_timeline)) + geom_boxplot() +
 xlab("BIE_timeline") + ylab("Sales Quantity")
```



# Boxplot indicates that online purchase quantity decreases after BOPS implementation for stores 2&6. However, we can't come to a conclusion basis this interpretation.

```
Checking for multi-collinearity
sales value is 0 for 30 rows is while sales quantity exists (complementary products or service)
```

```
df12=sales1[c("BIE_timeline",
"group_store","month_dummy","avg_female","avg_age","avg_income","avg_homeowner",
"avg_chldowner")]
```

BA Project\_BOPS\_Final Submitted.Rmd\* df12 df11 sales1 cust\_Level ODS\_Overall ODS\_prodcat trans\_l >>

Filter

| BIE_timeline | group_store | month_dummy | avg_female | avg_age   | avg_income | avg_homeowner | avg_childowner |
|--------------|-------------|-------------|------------|-----------|------------|---------------|----------------|
| 1            | 1           | 1           | 3          | 0.5238829 | 4.363883   | 5.083560      | 0.5835598      |
| 2            | 0           | 1           | 8          | 0.4444444 | 3.181818   | 4.545455      | 0.7272727      |
| 3            | 0           | 1           | 8          | 0.5964794 | 4.982840   | 5.563905      | 0.6390532      |
| 4            | 0           | 1           | 8          | 0.5744456 | 4.905033   | 5.462488      | 0.6201330      |
| 5            | 0           | 1           | 8          | 0.5719063 | 5.119534   | 5.565598      | 0.6209912      |
| 6            | 0           | 1           | 8          | 0.5875706 | 5.084093   | 5.530902      | 0.6727457      |
| 7            | 0           | 1           | 8          | 0.5497954 | 5.022444   | 5.524938      | 0.6321696      |
| 8            | 0           | 1           | 8          | 0.5652174 | 4.578948   | 5.644737      | 0.5263158      |

Showing 1 to 8 of 2,005 entries

```
round(cor(df12),3)
> round(cor(df12),3)
 BIE_timeline group_store month_dummy avg_female avg_age avg_income avg_homeowner avg_childowner
BIE_timeline 1.000 -0.084 0.059 -0.047 -0.103 -0.036 0.005 0.013
group_store -0.084 1.000 0.035 0.126 0.106 -0.083 0.091 0.155
month_dummy 0.059 0.035 1.000 -0.031 0.020 0.069 0.079 0.027
avg_female -0.047 0.126 -0.031 1.000 0.042 -0.073 0.039 0.031
avg_age -0.103 0.106 0.020 0.042 1.000 0.114 0.214 0.140
avg_income -0.036 -0.083 0.069 -0.073 0.114 1.000 0.308 0.075
avg_homeowner 0.005 0.091 0.079 0.039 0.214 0.308 1.000 0.300
avg_childowner 0.013 0.155 0.027 0.031 0.140 0.075 0.300 1.000
```

```
vifcor(df12)
> vifcor(df12) # There is no multi-collinearity in the data for the chosen variables.
No variable from the 8 input variables has collinearity problem.
```

The linear correlation coefficients ranges between:  
min correlation ( avg\_homeowner ~ BIE\_timeline ): 0.004773467  
max correlation ( avg\_homeowner ~ avg\_income ): 0.3077424

----- VIFs of the remained variables -----

| Variables        | VIF      |
|------------------|----------|
| 1 BIE_timeline   | 1.026005 |
| 2 group_store    | 1.070168 |
| 3 month_dummy    | 1.014866 |
| 4 avg_female     | 1.026377 |
| 5 avg_age        | 1.077031 |
| 6 avg_income     | 1.136619 |
| 7 avg_homeowner  | 1.251431 |
| 8 avg_childowner | 1.125705 |

> |

# There is no multi-collinearity in the data for the chosen variables.

#####Notes on control variables for the sales value and sales quantity mode==##

#We are not taking avg\_residency as a control behavior, as conceptually, we don't see a relation between buying jewellery online and number of years a person has lived in his/her current residence.  
#We are considering month\_dummy to account for the effect of seasonality.

#####-----IMPACT ON SALES QUANTITY-----#####

#Since sales quantity is a non-negative integer value, we are using count data models to understand how it is impacted by BOPS implementation.

```

poisson11 <-
glm(salesquantity~BIE_timeline*group_store+as.factor(month_dummy)+avg_female+avg_age+avg_inco
me+avg_homeowner+avg_chardown, family="poisson", data=sales1)
stargazer(poisson11,
 title="Poisson Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))

```

| Poisson Results         |                          |                                                |
|-------------------------|--------------------------|------------------------------------------------|
|                         | Dependent variable:      |                                                |
|                         | salesquantity<br>Model-1 |                                                |
| BIE_timeline            | 0.22***<br>(0.01)        | as.factor(month_dummy)8<br>-0.23***<br>(0.01)  |
| group_store             | 3.09***<br>(0.01)        | as.factor(month_dummy)9<br>-0.30***<br>(0.01)  |
| as.factor(month_dummy)2 | 0.40***<br>(0.005)       | as.factor(month_dummy)10<br>-0.15***<br>(0.01) |
| as.factor(month_dummy)3 | -0.23***<br>(0.01)       | as.factor(month_dummy)11<br>0.41***<br>(0.005) |
| as.factor(month_dummy)4 | -0.26***<br>(0.01)       | as.factor(month_dummy)12<br>1.23***<br>(0.004) |
| as.factor(month_dummy)5 | 0.17***<br>(0.01)        | avg_female<br>-0.88***<br>(0.01)               |
| as.factor(month_dummy)6 | -0.32***<br>(0.01)       | avg_age<br>-0.19***<br>(0.001)                 |
| as.factor(month_dummy)7 | -0.44***<br>(0.01)       | avg_income<br>0.29***<br>(0.002)               |
|                         |                          | avg_homeowner<br>-0.62***<br>(0.01)            |
|                         |                          | avg_chardown<br>0.42***<br>(0.01)              |
|                         |                          | BIE_timeline:group_store<br>-0.21***<br>(0.01) |

|          |                   |
|----------|-------------------|
| Constant | 3.42***<br>(0.02) |
|----------|-------------------|

|                   |              |
|-------------------|--------------|
| Observations      | 2,005        |
| Log Likelihood    | -681,213.20  |
| Akaike Inf. Crit. | 1,362,466.00 |

Note: \*p<0.05; \*\*p<0.01; \*\*\*p<0.001

#### ## Model fit assessment - Poisson

```
poisson11a <- glm(salesquantity~1, data=sales1, family="poisson")
```

|              |                                 |
|--------------|---------------------------------|
| ▶ poisson11  | Large glm (30 elements, 1.8 Mb) |
| ▶ poisson11a | Large glm (30 elements, 1.4 Mb) |

#running a comparison with null model.

```
lrtest(poisson11, poisson11a)
```

### Likelihood ratio test

```

Model 1: salesquantity ~ BIE_timeline * group_store + as.factor(month_dummy) +
 avg_female + avg_age + avg_income + avg_homeowner + avg_childowner
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 20 -681213
2 1 -1108920 -19 855414 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> |

```

# We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

##Since Poisson doesn't fit the data, we will check for negative binomial model.

```

negbin11<-
glm.nb(salesquantity~BIE_timeline*group_store+as.factor(month_dummy)+avg_female+avg_age+avg_i
ncome+avg_homeowner+avg_childowner, data = sales1)
stargazer(negbin11,
apply.coef = exp, t.auto=F, p.auto = F,
title="Negative Bionomial Results", type="text",
column.labels=c("IRRs"),
df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))

```

| Negative Bionomial Results |                        |                                                |
|----------------------------|------------------------|------------------------------------------------|
|                            |                        | Dependent variable:                            |
|                            |                        | salesquantity                                  |
|                            |                        | IRRs                                           |
| BIE_timeline               | 1.4176**<br>(0.1162)   | as.factor(month_dummy)10 0.8494<br>(0.1440)    |
| group_store                | 17.0403***<br>(0.1046) | as.factor(month_dummy)11 1.4442**<br>(0.1386)  |
| as.factor(month_dummy)2    | 1.3090<br>(0.1425)     | as.factor(month_dummy)12 3.2493***<br>(0.1389) |
| as.factor(month_dummy)3    | 0.7370*<br>(0.1406)    | avg_female 0.3042***<br>(0.1778)               |
| as.factor(month_dummy)4    | 0.7827<br>(0.1419)     | avg_age 0.8380***<br>(0.0196)                  |
| as.factor(month_dummy)5    | 1.1738<br>(0.1391)     | avg_income 1.3227***<br>(0.0372)               |
| as.factor(month_dummy)6    | 0.7368*<br>(0.1417)    | avg_homeowner 0.4862***<br>(0.1885)            |
| as.factor(month_dummy)7    | 0.6947**<br>(0.1390)   | avg_childowner 0.8962<br>(0.2007)              |
| as.factor(month_dummy)8    | 0.8239<br>(0.1300)     | BIE_timeline:group_store 0.6666**<br>(0.1327)  |
| as.factor(month_dummy)9    | 0.8129<br>(0.1344)     | Constant 59.3098***<br>(0.2675)                |
|                            |                        | -----                                          |
|                            |                        | Observations 2,005                             |
|                            |                        | Log Likelihood -13,277.7000                    |
|                            |                        | theta 0.6365*** (0.0172)                       |
|                            |                        | Akaike Inf. Crit. 26,595.4100                  |
|                            |                        | -----                                          |
| Note:                      |                        | *p<0.05; **p<0.01; ***p<0.001                  |
| >                          |                        |                                                |

```
Model fit assessment - Negative Binomial
```

```
negbin11a <- glm.nb(salesquantity ~ 1, data = sales1)
```

|                                                                                             |                                    |
|---------------------------------------------------------------------------------------------|------------------------------------|
|  negbin11  | Large negbin (30 elements, 1.5 Mb) |
|  negbin11a | Large negbin (28 elements, 1.1 Mb) |

```
lrtest(negbin11, negbin11a)
```

```
Likelihood ratio test
```

```
Model 1: salesquantity ~ BIE_timeline * group_store + as.factor(month_dummy) +
 avg_female + avg_age + avg_income + avg_homeowner + avg_childowner
```

```
Model 2: salesquantity ~ 1
```

```
#Df LogLik Df Chisq Pr(>Chisq)
1 21 -13277
2 2 -13856 -19 1158.9 < 2.2e-16 ***

```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Test results signifies that the model fits the data.
```

```
Check for heteroskedasticity
```

```
gqttest(negbin11) # Goldfeld-Quandt test indicates no heteroskedasticity
```

```
bptest(negbin11) # Breusch-Pagan test indicates heteroskedasticity
```

```
Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
Goldfeld-Quandt test
```

```
data: negbin11
GQ = 0.0040545, df1 = 983, df2 = 982, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2
```

```
> bptest(negbin11) # Breusch-Pagan test indicates heteroskedasticity
```

```
studentized Breusch-Pagan test
```

```
data: negbin11
BP = 350.98, df = 19, p-value < 2.2e-16
```

```
HWrobstdter <- sqrt(diag(vcovHC(negbin11, type="HC1"))) # produces Huber-White robust standard
```

```
errors
```

```
Values
```

|             |                                                    |
|-------------|----------------------------------------------------|
| HWrobstdter | Named num [1:20] 0.256 0.0962 0.0998 0.1337 0.1... |
|-------------|----------------------------------------------------|

```
stargazer(negbin11, negbin11,
```

```
 apply.coef = exp, t.auto=F, p.auto = F,
 se=list(NULL, HWrobstdter),
 title="Negative Binomial Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| Negative Binomial Results           |  |                      |                      |                          |                      |                      |
|-------------------------------------|--|----------------------|----------------------|--------------------------|----------------------|----------------------|
|                                     |  |                      |                      | Dependent variable:      |                      |                      |
|                                     |  |                      |                      | salesquantity            |                      |                      |
|                                     |  | Normal SE<br>(1)     | HW-Robust SE<br>(2)  |                          |                      |                      |
| BIE_timeline                        |  | 1.418**<br>(0.116)   | 1.418**<br>(0.096)   | as.factor(month_dummy)9  | 0.813<br>(0.134)     | 0.813<br>(0.123)     |
| group_store                         |  | 17.040***<br>(0.105) | 17.040***<br>(0.100) | as.factor(month_dummy)10 | 0.849<br>(0.144)     | 0.849<br>(0.135)     |
| as.factor(month_dummy)2             |  | 1.309<br>(0.142)     | 1.309<br>(0.134)     | as.factor(month_dummy)11 | 1.444**<br>(0.139)   | 1.444**<br>(0.132)   |
| as.factor(month_dummy)3             |  | 0.737*<br>(0.141)    | 0.737*<br>(0.124)    | as.factor(month_dummy)12 | 3.249***<br>(0.139)  | 3.249***<br>(0.126)  |
| as.factor(month_dummy)4             |  | 0.783<br>(0.142)     | 0.783<br>(0.125)     | avg_female               | 0.304***<br>(0.178)  | 0.304***<br>(0.182)  |
| as.factor(month_dummy)5             |  | 1.174<br>(0.139)     | 1.174<br>(0.129)     | avg_age                  | 0.838***<br>(0.020)  | 0.838***<br>(0.021)  |
| as.factor(month_dummy)6             |  | 0.737*<br>(0.142)    | 0.737*<br>(0.132)    | avg_income               | 1.323***<br>(0.037)  | 1.323***<br>(0.037)  |
| as.factor(month_dummy)7             |  | 0.695**<br>(0.139)   | 0.695**<br>(0.126)   | avg_homeowner            | 0.486***<br>(0.188)  | 0.486***<br>(0.184)  |
| as.factor(month_dummy)8             |  | 0.824<br>(0.130)     | 0.824<br>(0.123)     | avg_childowner           | 0.896<br>(0.201)     | 0.896<br>(0.228)     |
|                                     |  |                      |                      | BIE_timeline:group_store | 0.667**<br>(0.133)   | 0.667**<br>(0.114)   |
|                                     |  |                      |                      | Constant                 | 59.310***<br>(0.268) | 59.310***<br>(0.256) |
|                                     |  |                      |                      | Observations             | 2,005                | 2,005                |
|                                     |  |                      |                      | Log Likelihood           | -13,277.700          | -13,277.700          |
|                                     |  |                      |                      | theta                    | 0.636*** (0.017)     | 0.636*** (0.017)     |
|                                     |  |                      |                      | Akaike Inf. Crit.        | 26,595.410           | 26,595.410           |
| <hr/>                               |  |                      |                      |                          |                      |                      |
| Note: *p<0.05; **p<0.01; ***p<0.001 |  |                      |                      |                          |                      |                      |

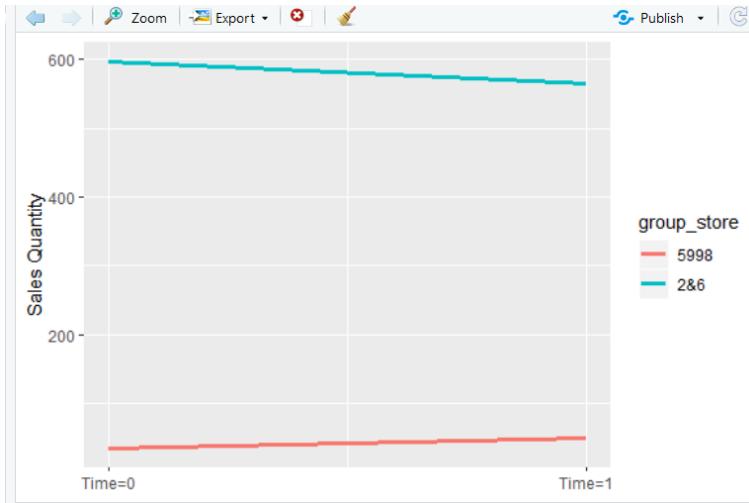
## # Visualize the output

```
meffects11 <- ggpredict(negbin11, terms=c("BIE_timeline", "group_store"))
```

| x | predicted | conf.low  | conf.high | group     |
|---|-----------|-----------|-----------|-----------|
| 1 | 0         | 35.04624  | 27.16446  | 45.21494  |
| 2 | 0         | 597.19679 | 485.06072 | 735.25640 |
| 3 | 1         | 49.68168  | 39.40601  | 62.63688  |
| 4 | 1         | 564.31031 | 459.53045 | 692.98155 |

## # generates a tidy data frame

```
ggplot(meffects11,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Sales Quantity") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998", "2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())
```

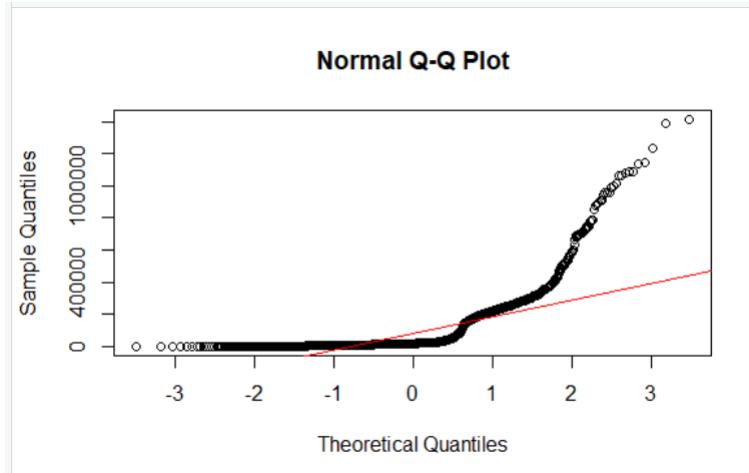


## Interpretation- The interaction coefficient for BIE\_timeline:group\_store is significant with value 0.667. This means that the BOPS implementation is associated with 33.3% decrease in the sales quantity. This doesn't seem intuitive at first. However, a likely reason for this decrease is the knowledge of inventory that is available to a customer after BOPS implementation. When the inventory information for various stores is available while shopping online, a user might be more inclined to actually visit store and check out the product before making a purchase. So, even though the purchase was initiated online, it will actually get closed at the store and would be booked as a brick and mortar sales.

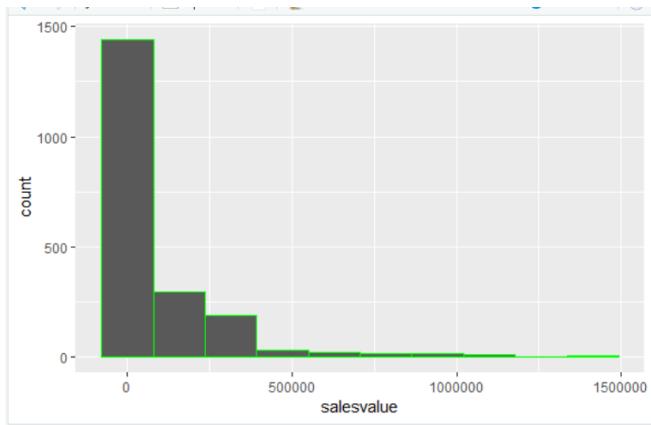
#### ===== IMPACT ON SALES VALUE =====

# We are using OLS model to estimate the impact of BOPS implementation on sales value

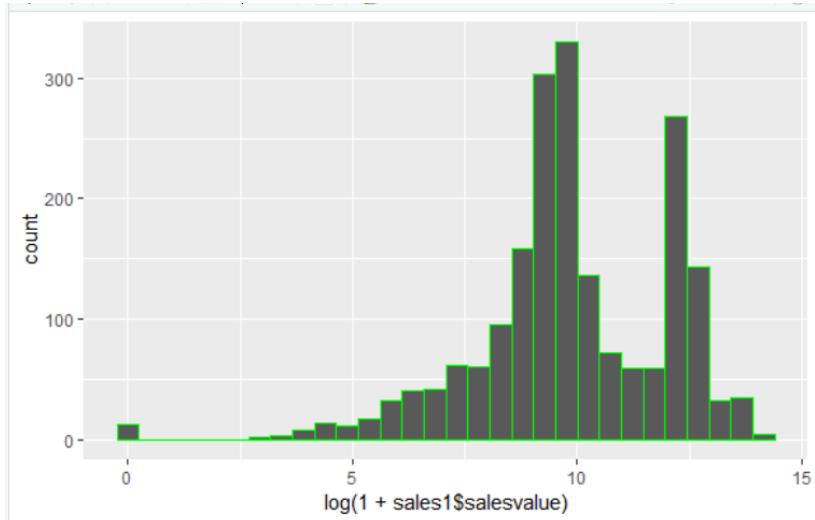
```
#checking normalization
qqnorm(sales1$salesvalue)
qqline(sales1$salesvalue, col=2)
```



```
ggplot(sales1, aes(x=salesvalue)) + geom_histogram(colour="green", bins = 10)
```



```
ggplot(sales1, aes(x=log(1+sales1$salesvalue))) + geom_histogram(colour="green", bins = 30)
```



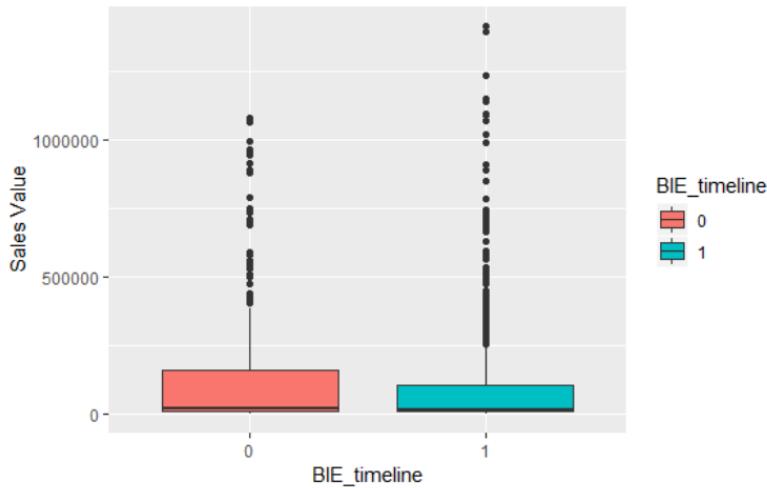
#Analysing trend in raw dataset with boxplot for salesvalue

```
df13 <- data.frame(salesvalue=sales1$salesvalue, BIE_timeline=as.factor(sales1$BIE_timeline))
```

|   | salesvalue | BIE_timeline |
|---|------------|--------------|
| 1 | 327516.28  | 1            |
| 2 | 1290.03    | 0            |
| 3 | 226777.23  | 0            |
| 4 | 164627.44  | 0            |
| 5 | 202743.41  | 0            |
| 6 | 168273.48  | 0            |
| 7 | 161634.70  | 0            |
| 8 | 11058.96   | 0            |

Showing 1 to 8 of 2,005 entries

```
ggplot(df13, aes(x=BIE_timeline, y=salesvalue, fill=BIE_timeline)) + geom_boxplot() +
 xlab("BIE_timeline") + ylab("Sales Value")
```



```
Boxplot indicates that online purchase quantity decreases after BOPS implementation for stores 2&6. However, we can't come to a conclusion basis this interpretation.
```

```
#Since sales value is a dollar value, we will use a linear interaction model with log transformed dependent variable.
```

```
sales1$log_salesvalue <- log(1+sales1$salesvalue)
```

| g_female  | avg_age  | avg_income | avg_homeowner | avg_residency | avg_childowner | BIE_timeline | group_store | log_salesvalue |
|-----------|----------|------------|---------------|---------------|----------------|--------------|-------------|----------------|
| 0.5238829 | 4.363883 | 5.083560   | 0.5835598     | 6.724864      | 0.3559783      | 1            | 1           | 12.699296      |
| 0.4444444 | 3.181818 | 4.545455   | 0.7272727     | 8.272727      | 0.2727273      | 0            | 1           | 7.163196       |
| 0.5964794 | 4.982840 | 5.563905   | 0.6390532     | 7.076331      | 0.3396450      | 0            | 1           | 12.331728      |
| 0.5744456 | 4.905033 | 5.462488   | 0.6201330     | 6.236467      | 0.3789174      | 0            | 1           | 12.011446      |
| 0.5719063 | 5.119534 | 5.565598   | 0.6209912     | 7.001944      | 0.3624879      | 0            | 1           | 12.219701      |
| 0.5875706 | 5.084093 | 5.530902   | 0.6727457     | 7.467072      | 0.3535967      | 0            | 1           | 12.033352      |
| 0.5497954 | 5.022444 | 5.524938   | 0.6321696     | 7.008728      | 0.3678304      | 0            | 1           | 11.993100      |

```
ols11 =
lm(log_salesvalue~BIE_timeline*group_store+as.factor(month_dummy)+avg_female+avg_age+avg_income+avg_homeowner+avg_childowner, data=sales1)
stargazer(ols11,
 title="Regression Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results      |                   |                                     |                    |
|-------------------------|-------------------|-------------------------------------|--------------------|
|                         |                   | Dependent variable:                 |                    |
|                         |                   | log_salesvalue                      |                    |
| Model-1                 |                   |                                     |                    |
| BIE_timeline            | 0.37*             | as.factor(month_dummy)10            | -0.09<br>(0.23)    |
|                         | (0.18)            | as.factor(month_dummy)11            | 0.45*<br>(0.22)    |
| group_store             | 1.95***<br>(0.16) | as.factor(month_dummy)12            | 1.45***<br>(0.22)  |
|                         |                   | avg_female                          | -1.13***<br>(0.28) |
| as.factor(month_dummy)2 | 0.55*<br>(0.22)   | avg_age                             | -0.19***<br>(0.03) |
|                         |                   | avg_income                          | 0.28***<br>(0.06)  |
| as.factor(month_dummy)3 | 0.17<br>(0.22)    | avg_homeowner                       | -0.54<br>(0.29)    |
|                         |                   | avg_childowner                      | 0.76*<br>(0.31)    |
| as.factor(month_dummy)4 | 0.02<br>(0.22)    | BIE_timeline:group_store            | -0.49*<br>(0.21)   |
|                         |                   | Constant                            | 8.37***<br>(0.42)  |
| as.factor(month_dummy)5 | 0.15<br>(0.22)    |                                     |                    |
|                         |                   |                                     |                    |
| as.factor(month_dummy)6 | -0.14<br>(0.22)   | Observations                        |                    |
|                         |                   | R2                                  |                    |
| as.factor(month_dummy)7 | -0.29<br>(0.22)   | Adjusted R2                         |                    |
|                         |                   | Residual Std. Error                 |                    |
| as.factor(month_dummy)8 | -0.04<br>(0.20)   | F Statistic                         |                    |
|                         |                   | 2,005                               |                    |
| as.factor(month_dummy)9 | -0.19<br>(0.21)   | 0.18                                |                    |
|                         |                   | 0.17                                |                    |
|                         |                   | 1.97                                |                    |
|                         |                   | 22.58***                            |                    |
|                         |                   |                                     |                    |
|                         |                   | Note: *p<0.05; **p<0.01; ***p<0.001 |                    |

```
Check for heteroskedasticity
```

```
gqtest(ols11) # Goldfeld-Quandt test indicates no heteroskedasticity
```

```
bptest(ols11) # Breusch-Pagan test indicates heteroskedasticity
```

```
Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
Goldfeld-Quandt test

data: ols11
GQ = 0.61023, df1 = 983, df2 = 982, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2

> bptest(ols11) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

data: ols11
BP = 72.346, df = 19, p-value = 0.00000003732
```

```
HWrobstderr <- sqrt(diag(vcovHC(ols11, type="HC1"))) # produces Huber-White robust standard errors
```

```
values
```

|             |                                                   |
|-------------|---------------------------------------------------|
| HWrobstderr | Named num [1:20] 0.664 0.128 0.13 0.227 0.224 ... |
|-------------|---------------------------------------------------|

```
stargazer(ols11, ols11,
```

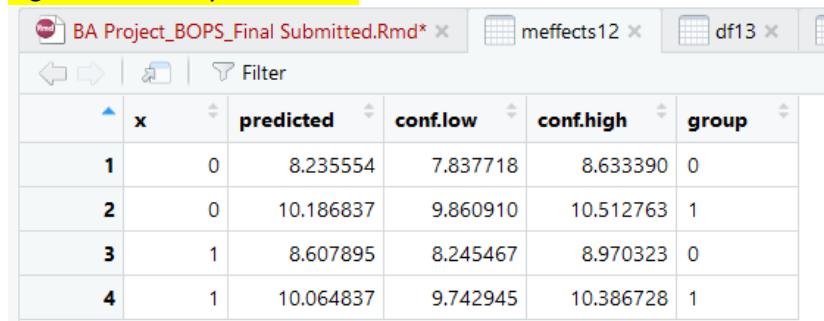
```
se=list(NULL, HWrobstderr),
title="OLS Results", type="text",
column.labels=c("Normal SE", "HW-Robust SE"),
df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| OLS Results             |  |                                       |                        | as.factor(month_dummy)10      | -0.091<br>(0.226)    | -0.091<br>(0.239)    |
|-------------------------|--|---------------------------------------|------------------------|-------------------------------|----------------------|----------------------|
|                         |  | Dependent variable:<br>log_salesvalue |                        | as.factor(month_dummy)11      | 0.453*<br>(0.217)    | 0.453<br>(0.239)     |
|                         |  | Normal<br>SE<br>(1)                   | HW-Robust<br>SE<br>(2) | as.factor(month_dummy)12      | 1.451***<br>(0.218)  | 1.451***<br>(0.225)  |
| BIE_timeline            |  | 0.372*<br>(0.181)                     | 0.372**<br>(0.128)     | avg_female                    | -1.128***<br>(0.278) | -1.128*<br>(0.478)   |
| group_store             |  | 1.951***<br>(0.163)                   | 1.951***<br>(0.130)    | avg_age                       | -0.192***<br>(0.031) | -0.192***<br>(0.047) |
| as.factor(month_dummy)2 |  | 0.552*<br>(0.223)                     | 0.552*<br>(0.227)      | avg_income                    | 0.283***<br>(0.058)  | 0.283**<br>(0.100)   |
| as.factor(month_dummy)3 |  | 0.168<br>(0.220)                      | 0.168<br>(0.224)       | avg_homeowner                 | -0.544<br>(0.295)    | -0.544<br>(0.490)    |
| as.factor(month_dummy)4 |  | 0.017<br>(0.222)                      | 0.017<br>(0.236)       | avg_childowner                | 0.764*<br>(0.314)    | 0.764<br>(0.605)     |
| as.factor(month_dummy)5 |  | 0.150<br>(0.218)                      | 0.150<br>(0.239)       | BIE_timeline:group_store      | -0.494*<br>(0.207)   | -0.494**<br>(0.168)  |
| as.factor(month_dummy)6 |  | -0.139<br>(0.222)                     | -0.139<br>(0.235)      | Constant                      | 8.366***<br>(0.418)  | 8.366***<br>(0.664)  |
| as.factor(month_dummy)7 |  | -0.294<br>(0.218)                     | -0.294<br>(0.246)      | Observations                  | 2,005                | 2,005                |
| as.factor(month_dummy)8 |  | -0.043<br>(0.204)                     | -0.043<br>(0.216)      | R2                            | 0.178                | 0.178                |
| as.factor(month_dummy)9 |  | -0.186<br>(0.211)                     | -0.186<br>(0.233)      | Adjusted R2                   | 0.170                | 0.170                |
|                         |  |                                       |                        | Residual Std. Error           | 1.969                | 1.969                |
|                         |  |                                       |                        | F Statistic                   | 22.580***            | 22.580***            |
|                         |  | Note:                                 |                        | *p<0.05; **p<0.01; ***p<0.001 |                      |                      |

### # Visualize the output

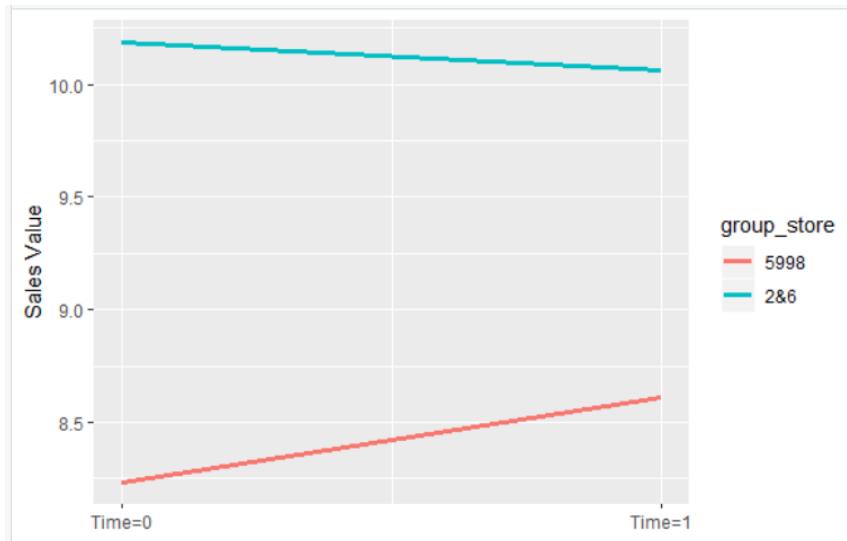
```
meffects12 <- ggpredict(ols11, terms=c("BIE_timeline", "group_store"))
```

```
generates a tidy data frame
```



|   | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 8.235554  | 7.837718 | 8.633390  | 0     |
| 2 | 0 | 10.186837 | 9.860910 | 10.512763 | 1     |
| 3 | 1 | 8.607895  | 8.245467 | 8.970323  | 0     |
| 4 | 1 | 10.064837 | 9.742945 | 10.386728 | 1     |

```
ggplot(meffects12,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Sales Value") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())
```



```
Interpretation -The interaction coefficient for BIE_timeline:group_store is significant with value -0.494. This means that the BOPS implementation is associated with 49.4% decrease in the sales value. Like quantity, sales value is also decreasing after BOPS implementation. The percentage reduction in sales value is more than the reduction in sales quantity. This implies that sales in general is reducing for relatively high priced items.
```

```
````
```

```
#=====#
## Question2: What is the impact of implementing BOPS strategy on online channel returns?
```

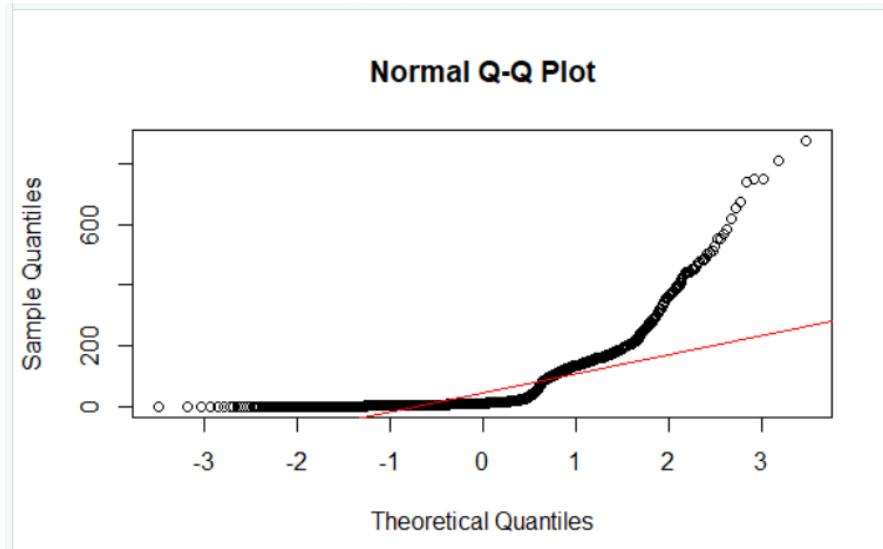
```
#=====#
```

```
```{r}
```

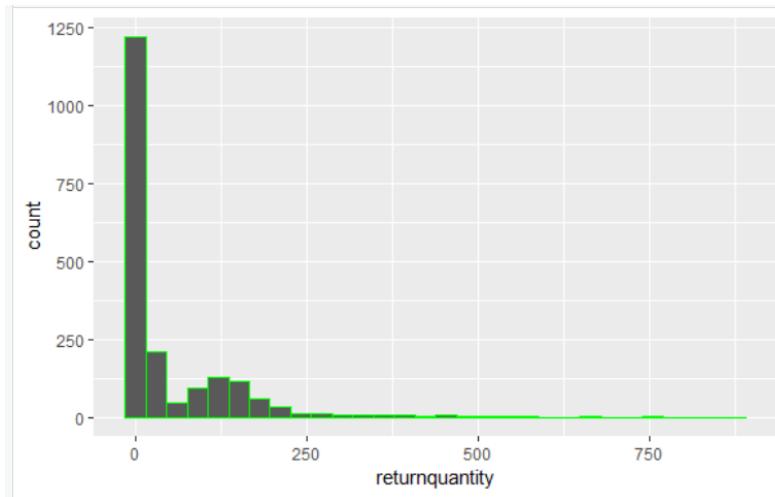
```
#check normalization
```

```
qqnorm(sales1$returnquantity)
```

```
qqline(sales1$returnquantity, col=2)
```



```
ggplot(sales1, aes(x{returnquantity})) + geom_histogram(colour="green", bins= 30)
```



#Analysing trend in raw dataset with boxplot for returnquantity

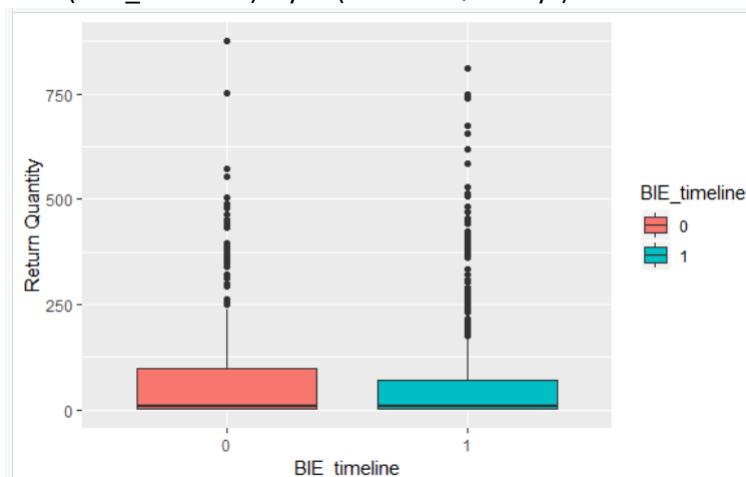
```
df21 <- data.frame(returnquantity=sales1$returnquantity, BIE_timeline=as.factor(sales1$BIE_timeline))
```

BA Project\_BOPS\_Final Submitted.Rmd\* df21

	returnquantity	BIE_timeline
1	168	1
2	1	0
3	214	0
4	118	0
5	155	0

Showing 1 to 5 of 2,005 entries

```
ggplot(df21, aes(x=BIE_timeline, y=returnquantity, fill=BIE_timeline)) + geom_boxplot() +
 xlab("BIE_timeline") + ylab("Return Quantity")
```



# Boxplot indicates that return quantity should decrease after BOPS implementation for stores 2&6. However, we can't come to a conclusion basis this interpretation.

# Checking for multi-collinearity

```
sales value is 0 for 30 rows is while sales quantity exists (complementary products or service)
```

```
df22=sales1[c("BIE_timeline", "group_store","salesquantity",
"month_dummy","avg_female","avg_age","avg_income", "avg_childowner")]
```

	BIE_timeline	group_store	salesquantity	month_dummy	avg_female	avg_age	avg_income	avg_childowner
1	1	1	1477	3	0.5238829	4.363883	5.083560	0.3559783
2	0	1	11	8	0.4444444	3.181818	4.545455	0.2727273
3	0	1	1701	8	0.5964794	4.982840	5.563905	0.3396450
4	0	1	1054	8	0.5744456	4.905033	5.462488	0.3789174
5	0	1	1031	8	0.5719063	5.119534	5.565598	0.3624879
6	0	1	988	8	0.5875706	5.084093	5.530902	0.3535967

Showing 1 to 6 of 2,005 entries

```
round(cor(df22),3)
```

```
> round(cor(df22),3)
 BIE_timeline group_store salesquantity month_dummy avg_female avg_age avg_income avg_childowner
BIE_timeline 1.000 -0.084 -0.018 0.059 -0.047 -0.103 -0.036 0.013
group_store -0.084 1.000 0.283 0.035 0.126 0.106 -0.083 0.155
salesquantity -0.018 0.283 1.000 0.147 -0.102 -0.020 0.049 0.043
month_dummy 0.059 0.035 0.147 1.000 -0.031 0.020 0.069 0.027
avg_female -0.047 0.126 -0.102 -0.031 1.000 0.042 -0.073 0.031
avg_age -0.103 0.106 -0.020 0.020 0.042 1.000 0.114 0.140
avg_income -0.036 -0.083 0.049 0.069 -0.073 0.114 1.000 0.075
avg_childowner 0.013 0.155 0.043 0.027 0.031 0.140 0.075 1.000
```

```
vifcor(df22)
```

```
> vifcor(df22)
No variable from the 8 input variables has collinearity problem.
```

```
The linear correlation coefficients ranges between:
min correlation (avg_childowner ~ BIE_timeline): 0.01283863
max correlation (salesquantity ~ group_store): 0.2830485
```

```
----- VIFs of the remained variables -----
```

	Variables	VIF
1	BIE_timeline	1.024987
2	group_store	1.172569
3	salesquantity	1.140331
4	month_dummy	1.031143
5	avg_female	1.043402
6	avg_age	1.055700
7	avg_income	1.043918
8	avg_childowner	1.049147

```
####=Notes on control variables for the return value and return quantity model==##
```

```
#We are not taking AVG_RESIDENCY as a control behavior, as conceptually, we don't see a relation
between returning jewellery and number of years a person has lived in his/her current residence.
#Also, we don't think that having a CHILD or being a HOMEOWNER affects jewellery returns.
```

```
#####=====IMPACT ON RETURN QUANTITY =====###
```

```
sales1$log_salesquantity <- log(sales1$salesquantity)
```

	avg_female	avg_age	avg_income	avg_homeowner	avg_residency	avg_childowner	BIE_timeline	group_store	log_salesvalue	log_salesquantity
3	0.5238829	4.363883	5.083560	0.5835598	6.724864	0.3559783	1	1	12.699296	7.297768
1	0.4444444	3.181818	4.545455	0.7272727	8.272727	0.2727273	0	1	7.163196	2.397895
4	0.5964794	4.982840	5.563905	0.6390532	7.076331	0.3396450	0	1	12.331728	7.438972
3	0.5744456	4.905033	5.462488	0.6201330	6.236467	0.3789174	0	1	12.011446	6.960348
5	0.5719063	5.119534	5.565598	0.6209912	7.001944	0.3624879	0	1	12.219701	6.938284

```

poisson21 <-
glm(returnquantity~BIE_timeline*group_store+log_salesquantity+as.factor(month_dummy)+avg_age+a
vg_income+avg_female, family="poisson", data=sales1)
stargazer(poisson21,
 title="Poisson Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))

```

Poisson Results			
Dependent variable:			
returnquantity Model-1			
BIE_timeline	0.18*** (0.05)	as.factor(month_dummy)9	-0.32*** (0.02)
group_store	0.59*** (0.04)	as.factor(month_dummy)10	-0.19*** (0.02)
log_salesquantity	0.95*** (0.004)	as.factor(month_dummy)11	-0.20*** (0.01)
as.factor(month_dummy)2	-0.31*** (0.01)	as.factor(month_dummy)12	-0.33*** (0.01)
as.factor(month_dummy)3	-0.14*** (0.02)	avg_age	-0.09*** (0.01)
as.factor(month_dummy)4	-0.22*** (0.02)	avg_income	-0.02 (0.01)
as.factor(month_dummy)5	-0.34*** (0.02)	avg_female	-0.03 (0.05)
as.factor(month_dummy)6	-0.06*** (0.02)	BIE_timeline:group_store	-0.19*** (0.05)
as.factor(month_dummy)7	-0.02 (0.02)	Constant	-1.63*** (0.08)
as.factor(month_dummy)8	-0.24*** (0.01)		
as.factor(month_dummy)9	-0.32*** (0.02)	Observations	2,005
		Log Likelihood	-9,646.01
		Akaike Inf. Crit.	19,330.02
		Note:	*p<0.05; **p<0.01; ***p<0.001

### ## Model fit assessment

```
poisson21a <- glm(returnquantity~1, data=sales1, family="poisson")
```

poisson21	Large glm (30 elements, 1.8 Mb)
poisson21a	Large glm (30 elements, 1.4 Mb)

```
running a comparison with null model.
lrtest(poisson21, poisson21a)
Likelihood ratio test

Model 1: returnquantity ~ BIE_timeline * group_store + log_salesquantity +
 as.factor(month_dummy) + avg_age + avg_income + avg_female
Model 2: returnquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 19 -9646
2 1 -118715 -18 218138 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

# We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

```
Since Poisson doesn't fit the data, we will check for negative binomial model.
negbin21 <-
glm.nb(returnquantity~BIE_timeline*group_store+log_salesquantity+as.factor(month_dummy)+avg_ag
e+avg_income+avg_female, data = sales1)
stargazer(negbin21,
apply.coef = exp, t.auto=F, p.auto = F,
title="Negative Binomial Results", type="text",
column.labels=c("IRRs"),
df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

Negative Binomial Results			
Dependent variable:			
	returnquantity	IRRs	
BIE_timeline	1.2021** (0.0568)	as.factor(month_dummy)9 as.factor(month_dummy)10 as.factor(month_dummy)11 as.factor(month_dummy)12	0.7186*** (0.0441) 0.8076*** (0.0469) 0.7447*** (0.0445) 0.6885*** (0.0432)
group_store	1.4453*** (0.0538)	avg_age	0.9698*** (0.0092)
log_salesquantity	2.7196*** (0.0075)	avg_income	0.9880 (0.0170)
as.factor(month_dummy)2	0.7380*** (0.0455)	avg_female	0.9523 (0.0843)
as.factor(month_dummy)3	0.8648** (0.0468)	BIE_timeline:group_store	0.8279** (0.0599)
as.factor(month_dummy)4	0.8151*** (0.0474)	Constant	0.1233*** (0.1273)
as.factor(month_dummy)5	0.7114*** (0.0458)		
as.factor(month_dummy)6	0.8845* (0.0479)	Observations	2,005
as.factor(month_dummy)7	0.9661 (0.0466)	Log Likelihood	-6,345.6270
as.factor(month_dummy)8	0.7659*** (0.0427)	theta	11.7966*** (0.6434)
		Akaike Inf. Crit.	12,729.2500
		Note:	*p<0.05; **p<0.01; ***p<0.001

```

Model fit assessment - Negative Binomial
negbin21a <- glm.nb(salesquantity ~ 1, data = sales1)

| | | |
|-------------|------------------------------------|---|
| ● negbin21 | Large negbin (30 elements, 1.5 Mb) | C |
| ● negbin21a | Large negbin (28 elements, 1.1 Mb) | C |

lrtest(negbin21, negbin21a)
Likelihood ratio test

Model 1: returnquantity ~ BIE_timeline * group_store + log_salesquantity +
 as.factor(month_dummy) + avg_age + avg_income + avg_female
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 20 -6344.6
2 2 -13856.2 -18 15023 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Check for heteroskedasticity
gqtest(negbin21) # Goldfeld-Quandt test indicates no heteroskedasticity
bpptest(negbin21) # Breusch-Pagan test indicates heteroskedasticity

| |
|---|
| Goldfeld-Quandt test |
| data: negbin21
GQ = 0.0050659, df1 = 984, df2 = 983, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2 |
| > bpptest(negbin21) # Breusch-Pagan test indicates heteroskedasticity |
| studentized Breusch-Pagan test |
| data: negbin21
BP = 157.95, df = 18, p-value < 2.2e-16 |

Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
HWrobstd <- sqrt(diag(vcovHC(negbin21, type="HC1")))
produces Huber-White robust standard errors

| | |
|----------|--|
| Values | |
| HWrobstd | Named num [1:19] 0.13518 0.06045 0.05... |

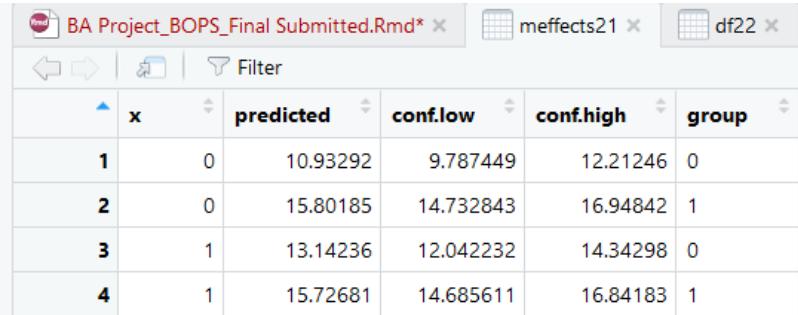
stargazer(negbin21, negbin21,
 apply.coef = exp, t.auto=F, p.auto = F,
 se=list(NULL, HWrobstd),
 title="Negative Binomial Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))

```

Negative Binomial Results					
			Dependent variable:		
			returnquantity		
			Normal SE	HW-Robust SE	
			(1)	(2)	
BIE_timeline			1.202** (0.057)	1.202** (0.060)	as.factor(month_dummy)8 0.766*** (0.043)
group_store			1.445*** (0.054)	1.445*** (0.059)	0.766*** (0.041)
log_salesquantity			2.720*** (0.007)	2.720*** (0.008)	0.719*** (0.044)
as.factor(month_dummy)2			0.738*** (0.046)	0.738*** (0.042)	0.719*** (0.040)
as.factor(month_dummy)3			0.865** (0.047)	0.865** (0.042)	0.745*** (0.045)
as.factor(month_dummy)4			0.815*** (0.047)	0.815*** (0.042)	0.745*** (0.037)
as.factor(month_dummy)5			0.711*** (0.046)	0.711*** (0.040)	0.688*** (0.043)
as.factor(month_dummy)6			0.884* (0.048)	0.884* (0.085)	0.970*** (0.009)
as.factor(month_dummy)7			0.966 (0.047)	0.966 (0.095)	0.970*** (0.009)
			avg_age		
			avg_income		
			avg_female		
			BIE_timeline:group_store		
			Constant		
			0.123*** (0.127)		
			-----		
			Observations		
			2,005		
			Log Likelihood		
			-6,345.627		
			theta		
			11.797*** (0.643)		
			Akaika Inf. Crit.		
			12,729.250		
			12,729.250		
			=====		
			Note: *p<0.05; **p<0.01; ***p<0.001		

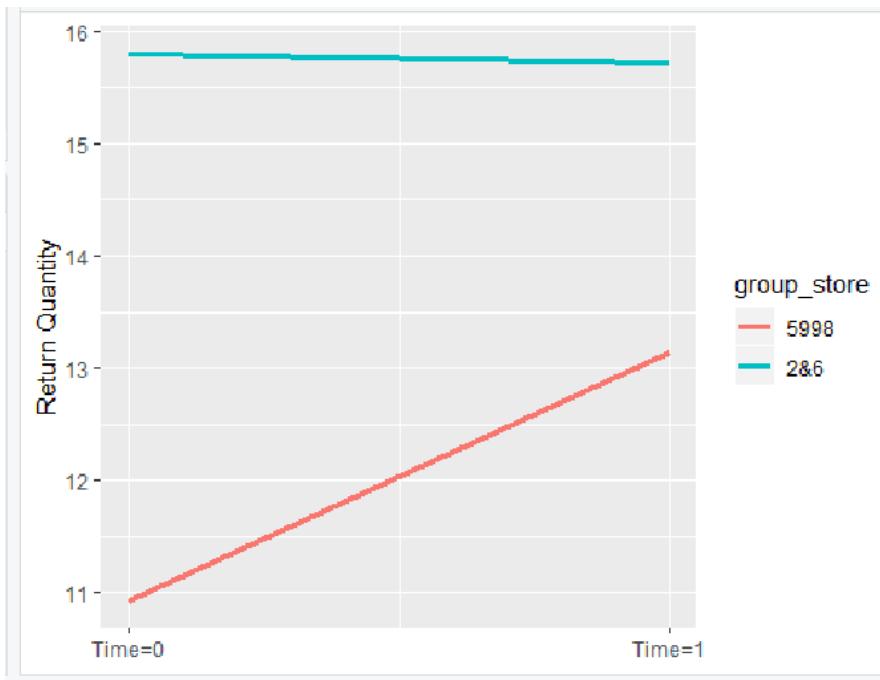
# Visualize the output

```
meffects21 <- ggpredict(negbin21, terms=c("BIE_timeline", "group_store"))
```



# generates a tidy data frame at two different values of BIE\_timeline - before and after BOPS implementation.

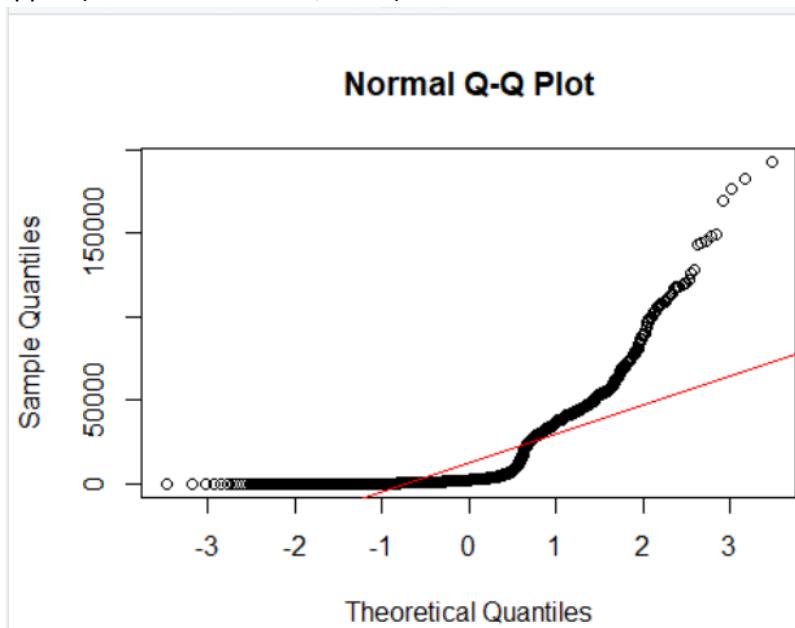
```
ggplot(meffects21,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Return Quantity") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())
```



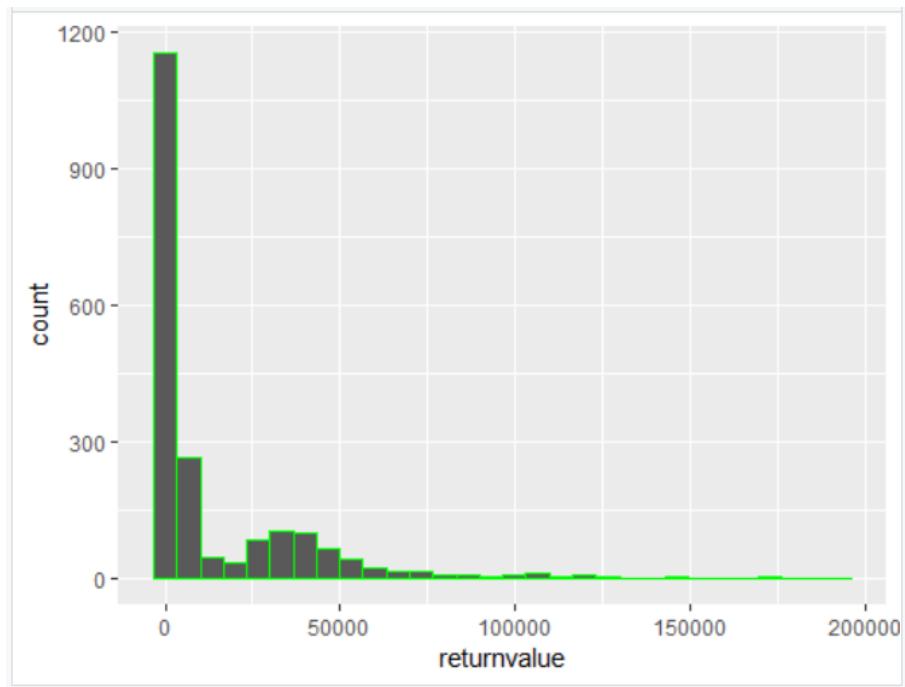
```
Interpretation - The interaction coefficient for BIE_timeline:group_store is significant with value 0.828. This means that the BOPS implementation is associated with 17.2% decrease in the return quantity.
```

#### ##### IMPACT ON RETURN VALUE #####

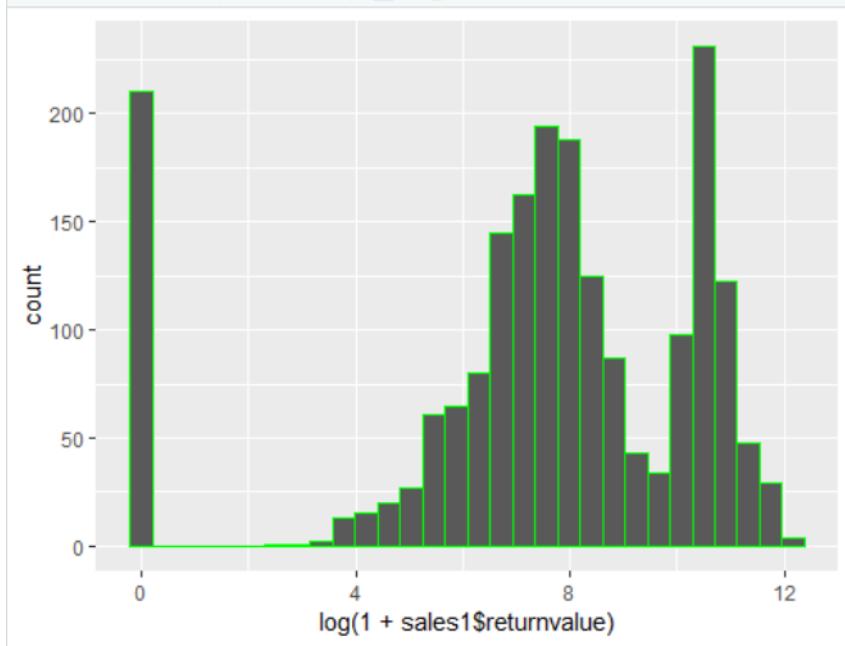
```
qqnorm(sales1$returnvalue)
qline(sales1$returnvalue, col=2)
```



```
ggplot(sales1, aes(x{returnvalue})) + geom_histogram(colour="green", bins = 30)
```



```
ggplot(sales1, aes(x=log(1+sales1$returnvalue))) + geom_histogram(colour="green", bins = 30)
```



```
#Analysing trend in raw dataset with boxplot for returnvalue
```

```
df23 <- data.frame(returnvalue=sales1$returnvalue, BIE_timeline=as.factor(sales1$BIE_timeline))
```

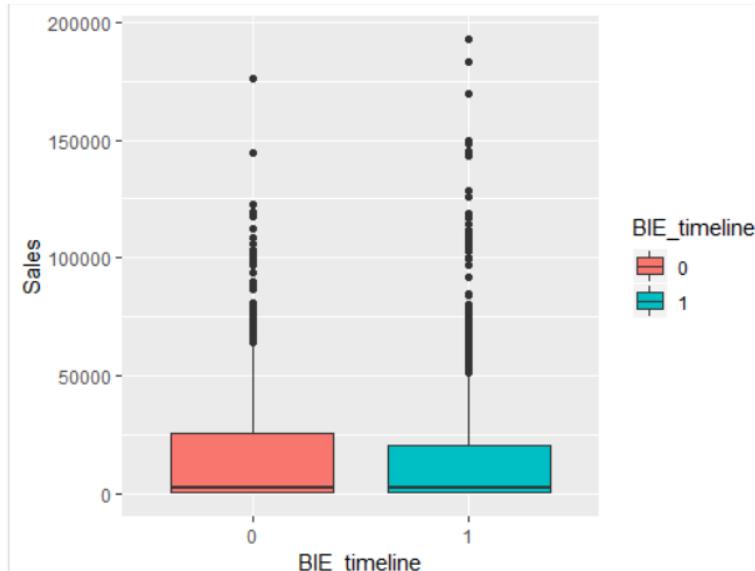
BA Project\_BOPS\_Final Submitted.Rmd\* df23

Filter

	returnvalue	BIE_timeline
1	54313.56	1
2	48.99	0
3	33090.81	0
4	25445.77	0

Showing 1 to 5 of 2,005 entries

```
ggplot(df23, aes(x=BIE_timeline, y=returnvalue, fill=BIE_timeline)) + geom_boxplot() +
 xlab("BIE_timeline") + ylab("Sales")
```



# Boxplot indicates that return value decreases after BOPS implementation for stores 2&6. However, we can't come to a conclusion basis this interpretation.

#Since return value is a dollar value, we will use a linear interaction model with log transformed dependent variable.

```
sales1$log_returnvalue <- log(1+sales1$returnvalue)
```

df23 meffects21 df22 df21 meffects12 df13 meffects11 df12 df11 sales1 cust\_Level

Filter

avg_income	avg_homeowner	avg_residency	avg_childowner	BIE_timeline	group_store	log_salesvalue	log_salesquantity	log_returnvalue
5.083560	0.5835598	6.724864	0.3559783	1	1	12.699296	7.297768	10.902548
4.545455	0.7272727	8.272727	0.2727273	0	1	7.163196	2.397895	3.911823
5.563905	0.6390532	7.076331	0.3396450	0	1	12.331728	7.438972	10.407041
5.462488	0.6201330	6.236467	0.3789174	0	1	12.011446	6.960348	10.144344
5.565598	0.6209912	7.001944	0.3624879	0	1	12.219701	6.938284	10.734875
5.530902	0.6727457	7.467072	0.3535967	0	1	12.033352	6.895683	10.175263
5.524938	0.6321696	7.008728	0.3678304	0	1	11.993100	6.689599	10.193633
5.644737	0.5263158	6.736842	0.4210526	0	1	9.311087	4.343805	7.367822
4.333333	0.6666667	4.000000	0.0000000	0	1	5.491785	1.098612	0.000000
5.600000	0.6000000	7.150720	0.3617070	1	1	10.400100	7.055010	10.101110

Showing 1 to 11 of 2,005 entries

```

ols21 =
lm(log_returnvalue~BIE_timeline*group_store+log_salesvalue+as.factor(month_dummy)+avg_age+avg_
income+avg_female, data=sales1)
stargazer(ols21,
 title="Regression Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))

```

Regression Results		
	Dependent variable:	
	log_returnvalue Model-1	
BIE_timeline	0.64*** (0.13)	as.factor(month_dummy)9 -0.34* (0.15)
group_store	0.85*** (0.12)	as.factor(month_dummy)10 -0.52** (0.16)
log_salesvalue	1.24*** (0.02)	as.factor(month_dummy)11 -0.59*** (0.16)
as.factor(month_dummy)2	-0.47** (0.16)	as.factor(month_dummy)12 -0.64*** (0.16)
as.factor(month_dummy)3	-0.60*** (0.16)	avg_age -0.02 (0.02)
as.factor(month_dummy)4	-0.56*** (0.16)	avg_income 0.04 (0.04)
as.factor(month_dummy)5	-0.53*** (0.16)	avg_female 0.56** (0.20)
as.factor(month_dummy)6	-0.51** (0.16)	BIE_timeline:group_store -0.66*** (0.15)
as.factor(month_dummy)7	-0.44** (0.16)	Constant -5.51*** (0.33)
as.factor(month_dummy)8	-0.59*** (0.15)	
Observations		
R2		
Adjusted R2		
Residual Std. Error		
F Statistic		
Note: *p<0.05; **p<0.01; ***p<0.001		

# Check for heteroskedasticity

gqtest(ols21) # Goldfeld-Quandt test indicates no heteroskedasticity

bptest(ols21) # Breusch-Pagan test indicates heteroskedasticity

# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.

Goldfeld-Quandt test

```

data: ols21
GQ = 2.3074, df1 = 984, df2 = 983, p-value < 2.2e-16
alternative hypothesis: variance increases from segment 1 to 2

```

> bptest(ols21) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

```

data: ols21
BP = 442.85, df = 18, p-value < 2.2e-16

```

```
HWrobstdter <- sqrt(diag(vcovHC(ols21, type="HC1"))) # produces Huber-White robust standard errors
```

Values	
HWrobstdter	Named num [1:19] 0.4854 0.1892 0.183 0.027...

```
stargazer(ols21, ols21,
 se=list(NULL, HWrobstdter),
 title="Regression Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

Regression Results		as.factor(month_dummy)8	-0.589*** (0.148)	-0.589*** (0.145)
	Dependent variable:			
	log_returnvalue			
	Normal SE	HW-Robust SE		
	(1)	(2)		
BIE_timeline	0.637*** (0.131)	0.637*** (0.189)	as.factor(month_dummy)9	-0.342* (0.153)
group_store	0.849*** (0.122)	0.849*** (0.183)	as.factor(month_dummy)10	-0.519** (0.164)
log_salesvalue	1.243*** (0.016)	1.243*** (0.028)	as.factor(month_dummy)11	-0.591*** (0.158)
as.factor(month_dummy)2	-0.465** (0.162)	-0.465** (0.153)	as.factor(month_dummy)12	-0.644*** (0.159)
as.factor(month_dummy)3	-0.600*** (0.160)	-0.600*** (0.156)	avg_age	-0.016 (0.022)
as.factor(month_dummy)4	-0.563*** (0.161)	-0.563** (0.177)	avg_income	0.044 (0.040)
as.factor(month_dummy)5	-0.533*** (0.158)	-0.533*** (0.154)	avg_female	0.561** (0.202)
as.factor(month_dummy)6	-0.511** (0.161)	-0.511** (0.169)	BIE_timeline:group_store	-0.660*** (0.150)
as.factor(month_dummy)7	-0.443** (0.158)	-0.443* (0.174)	Constant	-5.514*** (0.329)
			Observations	2,005
			R2	0.789
			Adjusted R2	0.787
			Residual Std. Error	1.428
			F Statistic	413.297***
				413.297***
			Note:	*p<0.05; **p<0.01; ***p<0.001

```
meffects22 <- ggpredict(ols21, terms=c("BIE_timeline", "group_store")) # generates a tidy data frame
```

BA Project\_BOPS\_Final Submitted.Rmd\* meffects22

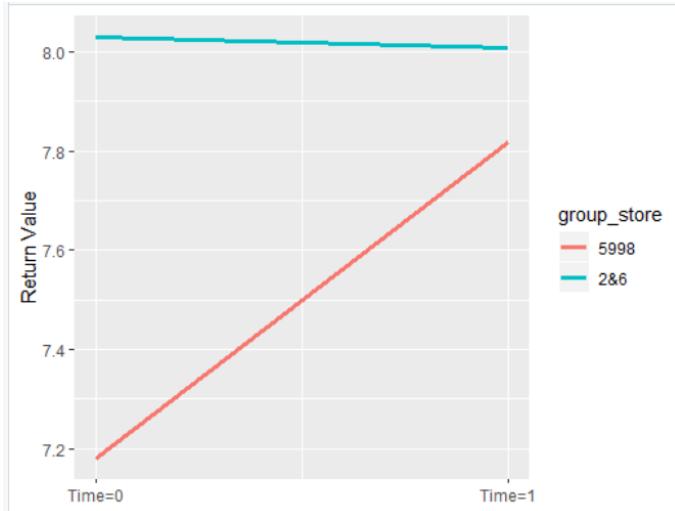
x	predicted	conf.low	conf.high	group
1	0	7.181039	6.888460	7.473619 0
2	0	8.029902	7.793377	8.266427 1
3	1	7.818156	7.553395	8.082917 0
4	1	8.006848	7.773493	8.240204 1

```
ggplot(meffects22,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
```

```

xlab("BOPS Timeline") + ylab("Return Value") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())

```



## Interpretation - The interaction coefficient for BIE\_timeline:group\_store is significant with value (-0.660). This means that the BOPS implementation is associated with ~66% decrease in the return value.  
```

```

#=====
## Question3: What is the impact of using the BOPS service on online customer purchase behavior?
#=====

``{r}
#To answer question 3 we are using consumer data. Following variables in consumer data have missing
values:
# 1.Female"-(~12%) values are missing
# 2.Age_band"
# 3.Est_income_code
# 4.Homeowner_code
# 5.Child

#Since female variable has a lot of missing entries, we used following two approaches to handle this
variable in the model:
#1. Keeping Female as control variable and removing rows where female, homeonwer and child are
missing.
#2. Removing Female as control variable, removing rows where homeonwer and child are missing.
#In both the approaches missing values in age_band and est_income_code are replaced with the
median values of these variables.

#Creating dummy variable from factor variables ## this is done to ensure that these variables get
included in descriptive stats and multi-collinearity test

cust_Level$childn = ifelse(cust_Level$child=="Y",1,ifelse(cust_Level$child=="N",0,cust_Level$child))
cust_Level$homeowner_coden =
ifelse(cust_Level$homeowner_code=="O",1,ifelse(cust_Level$homeowner_code=="R",0,cust_Level$ho
meowner_code))
cust_Level$childn <- as.numeric(cust_Level$childn)

```

```
cust_Level$homeowner_coden <- as.numeric(cust_Level$homeowner_coden)
```

Showing 1 to 9 of 84,420 entries

```
#####=====APPROACH 1=====#####
```

```
##--Keeping Female as control variable and removing rows where female, homeonwer and child are missing--##
```

```
#Descriptive Statistics
```

```
stargazer(cust_Level, type="text", median=TRUE, iqr=TRUE, digits=2, title="Descriptive Statistics")
```

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|----------------------|--------|-------------------|--------------------|---------|------------|------------|------------|-----------------|
| <hr/> | | | | | | | | |
| customer_id | 84,420 | 60,707,965,648.00 | 198,215,133,553.00 | 103,465 | 18,418,146 | 26,079,925 | 27,885,126 | 919,600,001,722 |
| store_number | 84,420 | 208.31 | 1,092.20 | 2 | 2 | 2 | 2 | 5,998 |
| age_band | 81,454 | 4.88 | 3.93 | 0.00 | 0.00 | 5.00 | 8.00 | 13.00 |
| est_income_code | 81,434 | 5.46 | 2.22 | 1.00 | 4.00 | 6.00 | 7.00 | 9.00 |
| length_of_residence | 81,434 | 7.32 | 5.42 | 0.00 | 2.00 | 6.00 | 13.00 | 15.00 |
| female | 74,518 | 0.43 | 0.49 | 0.00 | 0.00 | 0.00 | 1.00 | 1.00 |
| bops_in_effect | 84,420 | 0.50 | 0.50 | 0 | 0 | 0.5 | 1 | 1 |
| salesvalue | 84,420 | 392.67 | 930.65 | 0.00 | 98.99 | 197.99 | 388.93 | 82,226.24 |
| salesquantity | 84,420 | 2.52 | 7.64 | 1 | 1 | 1 | 3 | 1,474 |
| purchase_time_period | 84,420 | 2.89 | 4.25 | 1 | 1 | 1 | 2 | 24 |
| bops_user | 84,420 | 0.19 | 0.39 | 0 | 0 | 0 | 0 | 1 |
| childn | 81,434 | 0.39 | 0.49 | 0.00 | 0.00 | 0.00 | 1.00 | 1.00 |
| homeowner_coden | 81,434 | 0.68 | 0.47 | 0.00 | 0.00 | 1.00 | 1.00 | 1.00 |

```
#There are missing values in each of the following columns - "length_of_residence""", "female""", "est_income_code""", "age_band". Since female is a dummy variable, we are not replacing it with its mean. Instead, we are removing the rows where "female" variable has missing values. For other variables, we will replace the NA's with median values.
```

```
#We are creating sales2 data set to remove rows where "female", "child", "homeowner_code" have NA's
```

```
sales2 <- cust_Level[which((cust_Level$female==1 | cust_Level$female==0) & (cust_Level$child == "Y" | cust_Level$child == "N"),(cust_Level$homeowner_code=="R" | cust_Level$homeowner_code=="O"))],
```

BA Project_BOPS_Final Submitted.Rmd* sales2 cust_Level

Showing 1 to 9 of 74,504 entries

```
#stargazer(sales2, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

| Descriptive Statistics | | | | | | | | |
|------------------------|--------|------------------|-------------------|---------|------------|--------------|------------|-----------------|
| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
| customer_id | 74,504 | 64,766,358,970.0 | 203,798,610,698.0 | 103,465 | 18,362,271 | 25,989,831.0 | 27,748,712 | 919,600,001,722 |
| store_number | 74,504 | 4.1 | 105.3 | 2 | 2 | 2 | 2 | 5,998 |
| age_band | 74,492 | 5.2 | 3.9 | 0.0 | 0.0 | 5.0 | 8.0 | 13.0 |
| est_income_code | 74,504 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| length_of_residence | 74,504 | 7.5 | 5.4 | 0 | 2 | 6 | 14 | 15 |
| female | 74,504 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| bops_in_effect | 74,504 | 0.5 | 0.5 | 0 | 0 | 0.5 | 1 | 1 |
| salesvalue | 74,504 | 382.5 | 756.2 | 0.0 | 98.7 | 194.6 | 384.1 | 47,648.4 |
| salesquantity | 74,504 | 2.4 | 4.1 | 1 | 1 | 1 | 2 | 369 |
| purchase_time_period | 74,504 | 2.9 | 4.3 | 1 | 1 | 1 | 2 | 24 |
| bops_user | 74,504 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| childn | 74,504 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| homeowner_coden | 74,504 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |

Replacing NA's with mean values for other variables.

```
sales2$age_band[is.na(sales2$age_band)] = median(sales2$age_band, na.rm = TRUE)
```

BA Project_BOPS_Final Submitted.Rmd* sales2 cust_Level

Showing 1 to 10 of 74,504 entries

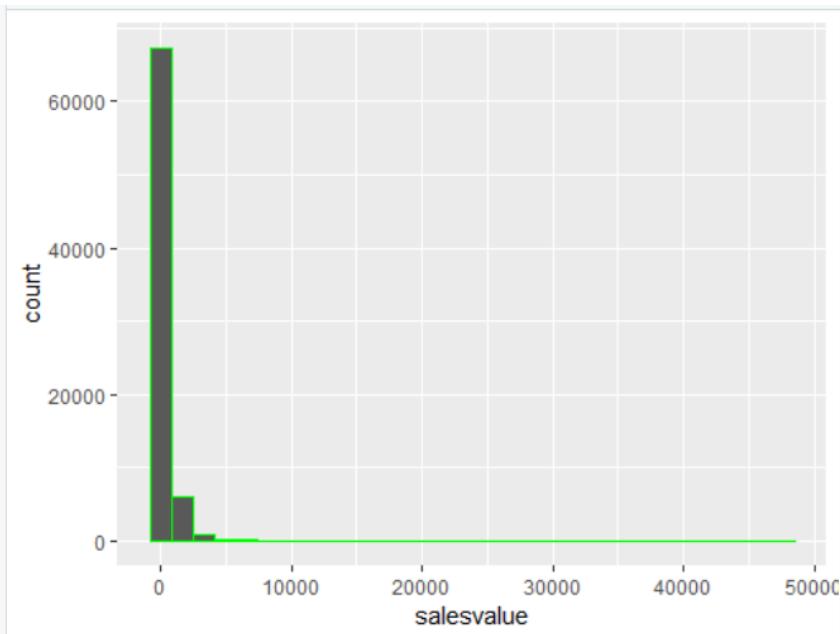
#Summary stats after replacing NA's with median and removing rows where "female", "homeowner_code" & "child" are NA.

```
stargazer(sales2, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|----------------------|--------|------------------|-------------------|---------|------------|--------------|------------|-----------------|
| <hr/> | | | | | | | | |
| customer_id | 74,504 | 64,766,358,970.0 | 203,798,610,698.0 | 103,465 | 18,362,271 | 25,989,831.0 | 27,748,712 | 919,600,001,722 |
| store_number | 74,504 | 4.1 | 105.3 | 2 | 2 | 2 | 2 | 5,998 |
| age_band | 74,504 | 5.2 | 3.9 | 0 | 0 | 5 | 8 | 13 |
| est_income_code | 74,504 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| length_of_residence | 74,504 | 7.5 | 5.4 | 0 | 2 | 6 | 14 | 15 |
| female | 74,504 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| bops_in_effect | 74,504 | 0.5 | 0.5 | 0 | 0 | 0.5 | 1 | 1 |
| salesvalue | 74,504 | 382.5 | 756.2 | 0.0 | 98.7 | 194.6 | 384.1 | 47,648.4 |
| salesquantity | 74,504 | 2.4 | 4.1 | 1 | 1 | 1 | 2 | 369 |
| purchase_time_period | 74,504 | 2.9 | 4.3 | 1 | 1 | 1 | 2 | 24 |
| bops_user | 74,504 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| childn | 74,504 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| homeowner_coden | 74,504 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |

#Check Normality

```
ggplot(sales2, aes(x=salesvalue)) + geom_histogram(colour="green", bins =30)
```

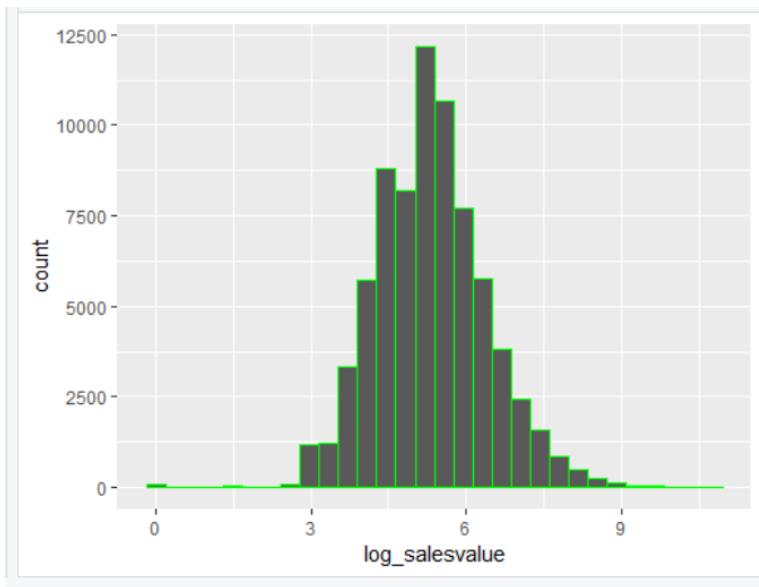


##salesvale doesn't seem to follow normal dist, so will use log of salesvalue as dependent variable.

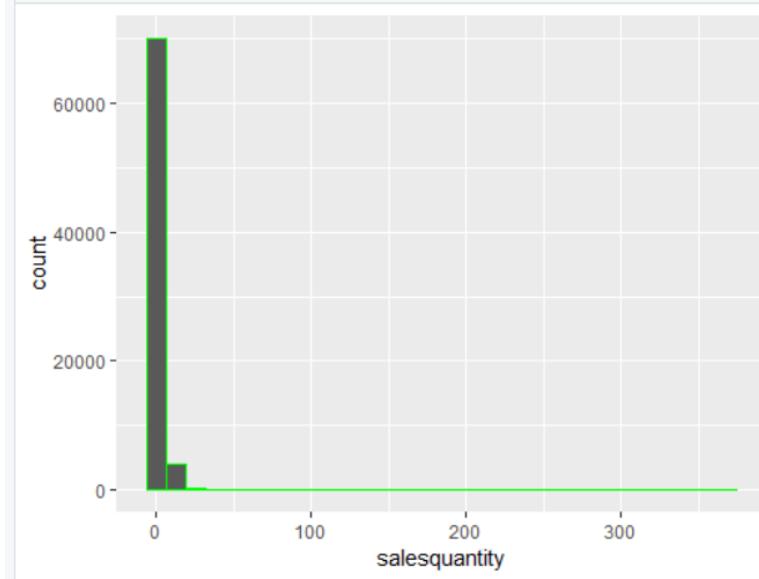
```
sales2$log_salesvalue <- log(1+sales2$salesvalue)
#since salesvalue is 0 at some places, we are taking log of (1+salesvalue)
```

| child | female | bops_in_effect | salesvalue | salesquantity | purchase_time_period | bops_user | chldn | homeowner_coden | log_salesvalue |
|-------|--------|----------------|------------|---------------|----------------------|-----------|-------|-----------------|----------------|
| Y | 0 | 0 | 195.30 | 1 | | 1 | 0 | 1 | 5.279644 |
| Y | 0 | 1 | 179.00 | 1 | | 1 | 0 | 1 | 5.192957 |
| N | 0 | 0 | 2898.00 | 2 | | 7 | 0 | 0 | 7.972121 |
| N | 0 | 1 | 1873.01 | 8 | | 21 | 0 | 0 | 7.535836 |
| Y | 0 | 0 | 169.15 | 1 | | 1 | 1 | 1 | 5.136680 |
| Y | 0 | 1 | 335.96 | 4 | | 5 | 1 | 1 | 5.819964 |

```
ggplot(sales2, aes(x=log_salesvalue)) + geom_histogram(colour="green", bins =30)
```



```
ggplot(sales2, aes(x=salesquantity)) + geom_histogram(colour="green" , bins = 30)
```



```
## Check Multicollinearity
```

```
df3 =
sales2[c("homeowner_coden","purchase_time_period","length_of_residence","est_income_code","age_band", "bops_in_effect", "bops_user", "childn","female","store_number")]
```

| | homeowner_coden | purchase_time_period | length_of_residence | est_income_code | age_band | bops_in_effect | bops_user | childn | female | store_number |
|---|-----------------|----------------------|---------------------|-----------------|----------|----------------|-----------|--------|--------|--------------|
| 1 | 0 | 1 | 15 | 7 | 5 | 0 | 0 | 1 | 0 | 2 |
| 2 | 0 | 1 | 15 | 7 | 5 | 1 | 0 | 1 | 0 | 2 |
| 5 | 1 | 7 | 15 | 1 | 9 | 0 | 0 | 0 | 0 | 2 |
| 6 | 1 | 21 | 15 | 1 | 9 | 1 | 0 | 0 | 0 | 2 |
| 7 | 1 | 1 | 2 | 6 | 0 | 0 | 1 | 1 | 0 | 2 |

Showing 1 to 5 of 74,504 entries

```
round(cor(df3),3)
```

```
> round(cor(df3),3)
   homeowner_coden purchase_time_period length_of_residence est_income_code age_band bops_in_effect bops_user childn female store_number
homeowner_coden          1.000           0.029        0.278       0.315     0.176      0.000    -0.015    0.208     0.008     -0.002
purchase_time_period       0.029          1.000        0.026       0.009    -0.008      0.233     0.060    0.012     0.051     -0.006
length_of_residence        0.278          0.026        1.000       0.133     0.130      0.000    -0.025    -0.032    0.029     -0.005
est_income_code            0.315          0.009        0.133       1.000     0.112      0.000    -0.011    0.083    -0.022     0.003
age_band                   0.176         -0.008        0.130       0.112     1.000      0.000    -0.038    -0.002    0.077     -0.002
bops_in_effect             0.000          0.233        0.000       0.000     0.000      1.000     0.000    0.000     0.000     -0.004
bops_user                  -0.015         0.060        -0.025     -0.011    -0.038      0.000     1.000    0.016     0.071     -0.005
childn                     0.208          0.012        -0.032      0.083    -0.002      0.000     0.016    1.000     0.040     -0.003
female                      0.008          0.051        0.029      -0.022    0.077      0.000     0.071    0.040     1.000     -0.002
store_number                -0.002         -0.006        -0.005      0.003    -0.002      -0.004    -0.005   -0.003    -0.002     1.000
` |
```

vifcor(df3)

```
> vifcor(df3)
```

No variable from the 10 input variables has collinearity problem.

The linear correlation coefficients ranges between:

min correlation (est_income_code ~ purchase_time_period): -0.00009741116

max correlation (est_income_code ~ homeowner_coden): 0.3239835

----- VIFs of the remained variables -----

| | Variables | VIF |
|----|----------------------|----------|
| 1 | homeowner_coden | 1.276555 |
| 2 | purchase_time_period | 1.070553 |
| 3 | length_of_residence | 1.098384 |
| 4 | est_income_code | 1.125427 |
| 5 | age_band | 1.060988 |
| 6 | bops_in_effect | 1.063050 |
| 7 | bops_user | 1.006026 |
| 8 | childn | 1.067158 |
| 9 | female | 1.021652 |
| 10 | store_number | 1.001598 |

#####=====IMPACT ON SALES QUANTITY=====#####

```
poisson31 <- glm(salesquantity~ bops_in_effect*bops_user + purchase_time_period + est_income_code
+ age_band + female + factor(store_number) + homeowner_coden +childn, family="poisson",
data=sales2)
```

```
stargazer(poisson31,
title="Poisson Results", type="text",
column.labels=c("Model-1"),
df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Poisson Results | | (0.02) |
|---|---------------------|--|
| =====
Dependent variable:
salesquantity
Model-1
===== | | |
| bops_in_effect | -0.25***
(0.01) | childn
0.002
(0.005) |
| bops_user | 0.01
(0.01) | bops_in_effect:bops_user
-0.02
(0.01) |
| purchase_time_period | 0.10***
(0.0004) | Constant
0.36***
(0.01) |
| est_income_code | 0.01***
(0.001) | =====
Observations
74,504
Log Likelihood
-147,007.20
Akaike Inf. Crit.
294,038.50
===== |
| age_band | -0.0003
(0.001) | Note: *p<0.05; **p<0.01; ***p<0.001 |
| female | 0.31***
(0.005) | > |
| factor(store_number)6 | 0.01
(0.01) | |
| factor(store_number)5998 | -0.44*
(0.19) | |
| homeowner_coden | 0.03***
(0.01) | |

Model fit assessment

```
poisson31a <- glm(salesquantity~1, data=sales2, family="poisson")
```

```
▶ poisson31 Large glm (30 elements, 57.2 Mb)
▶ poisson31a Large glm (30 elements, 46.4 Mb)
```

##running a comparison with null model.

```
lrtest(poisson31, poisson31a)
```

```
##' ... omitted ...
Likelihood ratio test

Model 1: salesquantity ~ bops_in_effect * bops_user + purchase_time_period +
  est_income_code + age_band + female + factor(store_number) +
  homeowner_coden + childn
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1  12 -147007
2   1 -181001 -11 67988 < 2.2e-16 ***
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> |
```

We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

##Since Poisson doesn't fit the data, we will check for negative binomial model.

##This model has child as control variable

```

negbin31 <- glm.nb(salesquantity ~ bops_in_effect * bops_user + purchase_time_period +
est_income_code + age_band + female + factor(store_number) + homeowner_coden + childn, data =
sales2)

stargazer(negbin31,
apply.coef = exp, t.auto=F, p.auto = F,
title="Negative Binomial Results", type="text",
column.labels=c("IRRs negbin31"),
df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))

```

| Negative Binomial Results | | |
|---------------------------|-----------------------|---|
| Dependent variable: | | |
| | salesquantity | IRR negbin31 |
| bops_in_effect | 0.8274***
(0.0071) | homeowner_coden
1.0268***
(0.0072) |
| bops_user | 1.0052
(0.0111) | childn
1.0061
(0.0063) |
| purchase_time_period | 1.1150***
(0.0006) | bops_in_effect:bops_user
0.9671*
(0.0154) |
| est_income_code | 1.0077***
(0.0015) | Constant
1.3895***
(0.0105) |
| age_band | 1.0019*
(0.0008) | |
| female | 1.3330***
(0.0061) | |
| factor(store_number)6 | 1.0162
(0.0118) | Observations
74,504 |
| factor(store_number)5998 | 0.6717
(0.2109) | Log Likelihood
-132,795.6000 |
| | | theta
4.5130*** (0.0504) |
| | | Akaike Inf. Crit.
265,615.2000 |
| | | Note: *p<0.05; **p<0.01; ***p<0.001 |

Model fit assessment - Negative Binomial

```
negbin31a <- glm.nb(salesquantity ~ 1, data = sales2)
```

| | | |
|-------------|-------------------------------------|---|
| ⌚ negbin31 | Large negbin (30 elements, 48.7 Mb) | 🔍 |
| ⌚ negbin31a | Large negbin (28 elements, 37.8 Mb) | 🔍 |

```
lrtest(negbin31, negbin31a)
```

Likelihood ratio test

```

Model 1: salesquantity ~ bops_in_effect * bops_user + purchase_time_period +
est_income_code + age_band + female + factor(store_number) +
homeowner_coden + childn
Model 2: salesquantity ~ 1
#DF LogLik Df Chisq Pr(>Chisq)
1 13 -132795
2 2 -149589 -11 33588 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```
# Check for heteroskedasticity
gqtest(negbin31) # Goldfeld-Quandt test indicates no heteroskedasticity
bptest(negbin31) # Breusch-Pagan test indicates heteroskedasticity

  Goldfeld-Quandt test

  data: negbin31
  GQ = 0.3098, df1 = 37240, df2 = 37240, p-value = 1
  alternative hypothesis: variance increases from segment 1 to 2

  > bptest(negbin31) # Breusch-Pagan test indicates heteroskedasticity

  studentized Breusch-Pagan test

  data: negbin31
  BP = 226.51, df = 11, p-value < 2.2e-16
```

Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.

```
HWrobstdter <- sqrt(diag(vcovHC(negbin31, type="HC1")))
```

Values

| HWrobstdter | Named num [1:12] | 0.0149 | 0.01043 | 0.02024 | ... |
|-------------|------------------|--------|---------|---------|-----|
|-------------|------------------|--------|---------|---------|-----|

produces Huber-White robust standard errors

```
stargazer(negbin31, negbin31,
           se=list(NULL, HWrobstdter),
           apply.coef = exp, t.auto=F, p.auto = F,
           title="Negative Binomial Results", type="text",
           column.labels=c("Normal SE", "HW-Robust SE"),
           df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

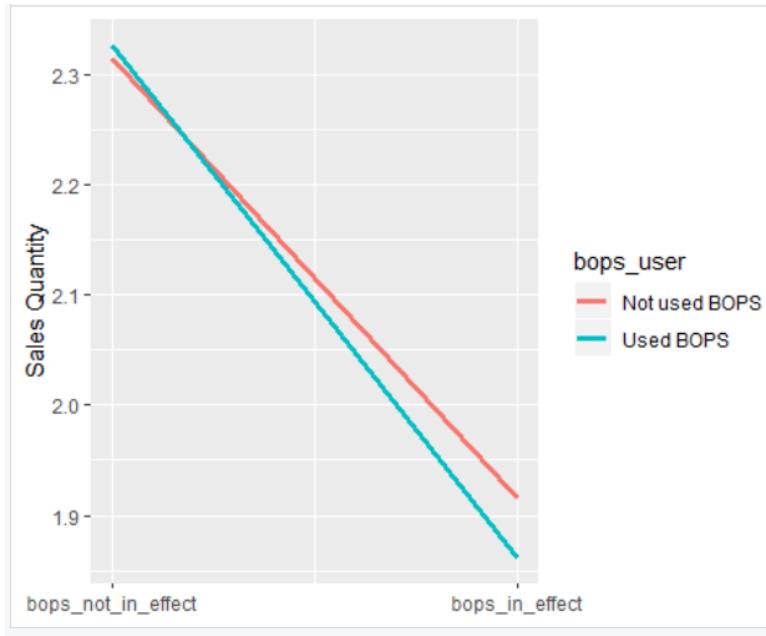
| Negative Binomial Results | | | | | |
|--|---------------------|---------------------|--------------------------|---------------------|---------------------|
| | | Dependent variable: | | | |
| | | salesquantity | | | |
| | | Normal SE | HW-Robust SE | | |
| | | (1) | (2) | | |
| bops_in_effect | 0.827***
(0.007) | 0.827***
(0.010) | homeowner_coden | 1.027***
(0.007) | 1.027***
(0.010) |
| bops_user | 1.005
(0.011) | 1.005
(0.020) | childn | 1.006
(0.006) | 1.006
(0.009) |
| purchase_time_period | 1.115***
(0.001) | 1.115***
(0.001) | bops_in_effect:bops_user | 0.967*
(0.015) | 0.967*
(0.025) |
| est_income_code | 1.008***
(0.001) | 1.008***
(0.002) | Constant | 1.389***
(0.010) | 1.389***
(0.015) |
| age_band | 1.002*
(0.001) | 1.002*
(0.001) | Observations | 74,504 | 74,504 |
| female | 1.333***
(0.006) | 1.333***
(0.009) | Log Likelihood | -132,795.600 | -132,795.600 |
| factor(store_number)6 | 1.016
(0.012) | 1.016
(0.014) | theta | 4.513*** (0.050) | 4.513*** (0.050) |
| factor(store_number)5998 | 0.672
(0.211) | 0.672
(0.080) | Akaike Inf. Crit. | 265,615.200 | 265,615.200 |
| Note: *p<0.05; **p<0.01; ***p<0.001
> | | | | | |

Visualize the output- generated a data frame at two different values of bops_in_effect for two groups - who used BOPS and who didn't after BOPS implementation.

```
meffects31 <- ggpredict(negbin31, terms=c("bops_in_effect","bops_user"))
```

| | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 2.314271 | 2.292138 | 2.336617 | 0 |
| 2 | 0 | 2.326389 | 2.281006 | 2.372674 | 1 |
| 3 | 1 | 1.914841 | 1.895670 | 1.934206 | 0 |
| 4 | 1 | 1.861633 | 1.825557 | 1.898422 | 1 |

```
ggplot(meffects31,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
  xlab("bops_in_effect") + ylab("Sales Quantity") +
  labs(colour="bops_user") +
  scale_colour_discrete(labels=c("Not used BOPS","Used BOPS")) +
  scale_x_continuous(breaks=c(0,1), labels=c("bops_not_in_effect", "bops_in_effect")) +
  theme(axis.title.x=element_blank())
```



#Interpretation - The interaction coefficient for bops_in_effect:bops_user is significant with value (0.967). This means that the usage of BOPS service is associated with ~3.3% decrease in sales quantity.
#####===== IMPACT ON SALES VALUE=====#####

```
ols32 = lm(log_salesvalue~ bops_in_effect*bops_user + purchase_time_period + est_income_code +
age_band + factor(store_number) + female + homeowner_coden + chldn, data=sales2)
stargazer(ols32,
  title="Regression Results", type="text",
  column.labels=c("Model-OLS32","Model-OLS31"),
  df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | |
|--------------------------|-------------------------------|--|
| ===== | | |
| | Dependent variable: | |
| | log_salesvalue | |
| | Model-OLS32 | |
| bops_in_effect | -0.15***
(0.01) | |
| bops_user | -0.22***
(0.01) | |
| purchase_time_period | 0.10***
(0.001) | |
| est_income_code | 0.01***
(0.002) | |
| age_band | 0.01***
(0.001) | |
| factor(store_number)6 | -0.08***
(0.01) | |
| factor(store_number)5998 | 0.20
(0.20) | |
| female | -0.15***
(0.01) | |
| homeowner_coden | -0.001
(0.01) | |
| childn | -0.04***
(0.01) | |
| childn | -0.04***
(0.01) | |
| bops_in_effect:bops_user | -0.04
(0.02) | |
| Constant | 5.15***
(0.01) | |
| ===== | | |
| Observations | 74,504 | |
| R2 | 0.17 | |
| Adjusted R2 | 0.17 | |
| Residual Std. Error | 0.97 | |
| F Statistic | 1,418.85*** | |
| ===== | | |
| Note: | *p<0.05; **p<0.01; ***p<0.001 | |
| > | | |

```
# Check for heteroskedasticity
```

```
gqttest(ols32) # Goldfeld-Quandt test indicates no heteroskedasticity
```

```
bptest(ols32) # Breusch-Pagan test indicates heteroskedasticity
```

```
Goldfeld-Quandt test
```

```
data: ols32
GQ = 0.92642, df1 = 37240, df2 = 37240, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2
```

```
> bptest(ols32) # Breusch-Pagan test indicates heteroskedasticity
```

```
studentized Breusch-Pagan test
```

```
data: ols32
BP = 191.48, df = 11, p-value < 2.2e-16
```

```
# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
HWrobstderr <- sqrt(diag(vcovHC(ols32, type="HC1"))) # produces Huber-White robust standard errors
```

| Values |
|--------|
|--------|

| | |
|-------------|---|
| HWrobstderr | Named num [1:12] 0.01192 0.00798 0.01321... |
|-------------|---|

```
stargazer(ols32, ols32,
          se=list(NULL, HWrobstderr),
          title="Regression Results", type="text",
```

```
column.labels=c("Normal SE", "HW-Robust SE"),
df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | | | female | -0.153***
(0.007) | -0.153***
(0.007) |
|--------------------------|--|----------------------|----------------------|--------------------------|-------------------------------|----------------------|
| | | Dependent variable: | | homeowner_coden | -0.001
(0.008) | -0.001
(0.008) |
| | | log_salesvalue | | childn | -0.042***
(0.007) | -0.042***
(0.007) |
| | | Normal SE | HW-Robust SE | bops_in_effect:bops_user | -0.035
(0.018) | -0.035
(0.019) |
| | | (1) | (2) | Constant | 5.145***
(0.012) | 5.145***
(0.012) |
| bops_in_effect | | -0.146***
(0.008) | -0.146***
(0.008) | | | |
| bops_user | | -0.216***
(0.013) | -0.216***
(0.013) | | | |
| purchase_time_period | | 0.105***
(0.001) | 0.105***
(0.001) | | | |
| est_income_code | | 0.006***
(0.002) | 0.006***
(0.002) | | | |
| age_band | | 0.007***
(0.001) | 0.007***
(0.001) | | | |
| factor(store_number)6 | | -0.079***
(0.014) | -0.079***
(0.014) | | | |
| factor(store_number)5998 | | 0.201
(0.202) | 0.201
(0.146) | | | |
| | | | | Observations | 74,504 | 74,504 |
| | | | | R2 | 0.173 | 0.173 |
| | | | | Adjusted R2 | 0.173 | 0.173 |
| | | | | Residual Std. Error | 0.969 | 0.969 |
| | | | | F Statistic | 1,418.846*** | 1,418.846*** |
| | | | | Note: | *p<0.05; **p<0.01; ***p<0.001 | |
| | | | | | | |

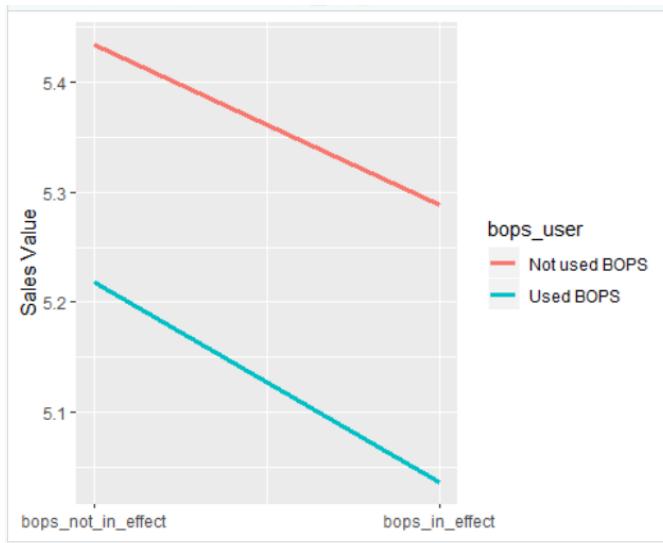
Visualize the output

```
meffects32 <- ggpredict(ols32, terms=c("bops_in_effect", "bops_user"))
```

| | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 5.434436 | 5.423210 | 5.445663 | 0 |
| 2 | 0 | 5.218199 | 5.195117 | 5.241281 | 1 |
| 3 | 1 | 5.288045 | 5.276878 | 5.299211 | 0 |
| 4 | 1 | 5.036537 | 5.013288 | 5.059787 | 1 |

#generates a tidy data frame at two different values of bops_in_effect for two groups - who used BOPS and who didn't after BOPS implementation.

```
ggplot(meffects32, aes(x, predicted, colour=group)) + geom_line(size=1.3) +
  xlab("bops_in_effect") + ylab("Sales Value") +
  labs(colour="bops_user") +
  scale_colour_discrete(labels=c("Not used BOPS", "Used BOPS")) +
  scale_x_continuous(breaks=c(0,1), labels=c("bops_not_in_effect", "bops_in_effect")) +
  theme(axis.title.x=element_blank())
```



#Interpretation - The interaction coefficient for bops_in_effect:bops_user is insignificant. Thus, we cannot comment about the impact of BOPS usage on sales quantity.

#####=APPROACH 2=====#####

##Removing Female as control variable, removing rows where homeowner and child are missing.

#Here we are removing data where "child" and "homeowner_code" have NA's.

```
sales21 <- cust_Level[which((cust_Level$child == "Y" | cust_Level$child == "N"),(cust_Level$homeowner_code == "R" | cust_Level$homeowner_code == "O"))]
```

#Dropping female as control behavior

```
sales21$female <- NULL
```

```
stargazer(sales21, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

Descriptive Statistics

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|----------------------|--------|------------------|-------------------|---------|------------|------------|------------|-----------------|
| customer_id | 81,434 | 62,707,033,354.0 | 201,169,744,468.0 | 103,465 | 18,356,040 | 25,988,667 | 27,748,316 | 919,600,001,722 |
| store_number | 81,434 | 4.4 | 113.1 | 2 | 2 | 2 | 2 | 5,998 |
| age_band | 81,418 | 4.9 | 3.9 | 0.0 | 0.0 | 5.0 | 8.0 | 13.0 |
| est_income_code | 81,434 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| length_of_residence | 81,434 | 7.3 | 5.4 | 0 | 2 | 6 | 13 | 15 |
| bops_in_effect | 81,434 | 0.5 | 0.5 | 0 | 0 | 0.5 | 1 | 1 |
| salesvalue | 81,434 | 391.3 | 940.1 | 0.0 | 98.7 | 194.6 | 386.5 | 82,226.2 |
| salesquantity | 81,434 | 2.5 | 7.8 | 1 | 1 | 1 | 3 | 1,474 |
| purchase_time_period | 81,434 | 2.9 | 4.3 | 1 | 1 | 1 | 2 | 24 |
| bops_user | 81,434 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| childn | 81,434 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| homeowner_coden | 81,434 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |

Replacing NA's with mean values for other variables.

```
sales21$age_band[is.na(sales21$age_band)] = median(sales21$age_band, na.rm = TRUE)
sales21$est_income_code[is.na(sales21$est_income_code)] <- median(sales21$est_income_code,
na.rm = TRUE)
sales21$length_of_residence[is.na(sales21$length_of_residence)] <-
median(sales21$length_of_residence, na.rm = TRUE)
```

```
stargazer(sales21, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|----------------------|--------|------------------|-------------------|---------|------------|------------|------------|-----------------|
| customer_id | 81,434 | 62,707,033,354.0 | 201,169,744,468.0 | 103,465 | 18,356,040 | 25,988,667 | 27,748,316 | 919,600,001,722 |
| store_number | 81,434 | 4.4 | 113.1 | 2 | 2 | 2 | 2 | 5,998 |
| age_band | 81,434 | 4.9 | 3.9 | 0 | 0 | 5 | 8 | 13 |
| est_income_code | 81,434 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| length_of_residence | 81,434 | 7.3 | 5.4 | 0 | 2 | 6 | 13 | 15 |
| bops_in_effect | 81,434 | 0.5 | 0.5 | 0 | 0 | 0.5 | 1 | 1 |
| salesvalue | 81,434 | 391.3 | 940.1 | 0.0 | 98.7 | 194.6 | 386.5 | 82,226.2 |
| salesquantity | 81,434 | 2.5 | 7.8 | 1 | 1 | 1 | 3 | 1,474 |
| purchase_time_period | 81,434 | 2.9 | 4.3 | 1 | 1 | 1 | 2 | 24 |
| bops_user | 81,434 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| childn | 81,434 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| homeowner_coden | 81,434 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |

#####=====IMPACT ON SALES QUANTITY=====#####

```
poisson32 <- glm(salesquantity~ bops_in_effect*bops_user + purchase_time_period + est_income_code + age_band + factor(store_number) + homeowner_coden + childn, family="poisson", data=sales21)
```

```
stargazer(poisson32,
  title="Poisson Results", type="text",
  column.labels=c("Model-1"),
  df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Poisson Results | | | |
|--------------------------|---------------------|--------------------------|-------------------------------|
| | | Dependent variable: | |
| | | salesquantity
Model-1 | |
| bops_in_effect | -0.30***
(0.01) | homeowner_coden | -0.01*
(0.01) |
| bops_user | 0.04***
(0.01) | childn | -0.01*
(0.005) |
| purchase_time_period | 0.11***
(0.0004) | bops_in_effect:bops_user | -0.02*
(0.01) |
| est_income_code | 0.02***
(0.001) | Constant | 0.54***
(0.01) |
| age_band | -0.01***
(0.001) | Observations | 81,434 |
| factor(store_number)6 | 0.01
(0.01) | Log Likelihood | -181,090.90 |
| factor(store_number)5998 | -0.25
(0.14) | Akaike Inf. Crit. | 362,203.80 |
| | | Note: | *p<0.05; **p<0.01; ***p<0.001 |

Model fit assessment

```
poisson32a <- glm(salesquantity~1, data=sales21, family="poisson")
```

| | |
|--------------|---|
| ① poisson32 | Large <code>glm</code> (30 elements, 61 Mb) |
| ① poisson32a | Large <code>glm</code> (30 elements, 50.1 Mb) |

##running a comparison with null model.

```
lrtest(poisson32, poisson32a)
```

Likelihood ratio test

```

Model 1: salesquantity ~ bops_in_effect * bops_user + purchase_time_period +
  est_income_code + age_band + factor(store_number) + homeowner_coden +
  childn
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 11 -181091
2 1 -222022 -10 81863 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
>

```

We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

##Since Poisson doesn't fit the data, we will check for negative binomial model.

```
negbin32 <- glm.nb(salesquantity~ bops_in_effect*bops_user + purchase_time_period +
est_income_code + age_band + factor(store_number) + homeowner_coden + childn, data = sales21)
```

```

stargazer(negbin32,
  apply.coef = exp, t.auto=F, p.auto = F,
  title="Negative Binomial Results", type="text",
  column.labels=c("IRRs negbin31"),
  df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))

```

| Negative Binomial Results | | | |
|---------------------------|-----------------------|--------------------------|-----------------------|
| | | Dependent variable: | |
| | | salesquantity | |
| | | IRRs negbin31 | |
| bops_in_effect | 0.8115***
(0.0070) | childn | 1.0023
(0.0063) |
| bops_user | 1.0308**
(0.0109) | bops_in_effect:bops_user | 0.9586**
(0.0153) |
| purchase_time_period | 1.1250***
(0.0006) | Constant | 1.5909***
(0.0098) |
| est_income_code | 1.0128***
(0.0014) | ----- | |
| age_band | 0.9990
(0.0008) | Observations | 81,434 |
| factor(store_number)6 | 1.0238*
(0.0119) | Log Likelihood | -149,141.0000 |
| factor(store_number)5998 | 0.7535
(0.1800) | theta | 3.5620*** (0.0328) |
| homeowner_coden | 0.9964
(0.0071) | Akaike Inf. Crit. | 298,304.0000 |

Note: *p<0.05; **p<0.01; ***p<0.001

Model fit assessment - Negative Binomial

```
negbin32a <- glm.nb(salesquantity ~ 1, data = sales21)
```

| | | |
|--|------------------------|-------------------------------------|
| | <code>negbin32</code> | Large negbin (30 elements, 52.3 Mb) |
| | <code>negbin32a</code> | Large negbin (28 elements, 41.4 Mb) |

```

lrttest(negbin32, negbin32a)
Likelihood ratio test

Model 1: salesquantity ~ bops_in_effect * bops_user + purchase_time_period +
          est_income_code + age_band + factor(store_number) + homeowner_coden +
          childn
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1   12 -149140
2     2 -167228 -10 36177 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> |

```

```

# Check for heteroskedasticity
gqttest(negbin32) # Goldfeld-Quandt test indicates no heteroskedasticity
bptest(negbin32) # Breusch-Pagan test indicates heteroskedasticity

```

```

Goldfeld-Quandt test

data: negbin32
GQ = 0.13122, df1 = 40706, df2 = 40706, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2

> bptest(negbin32) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

data: negbin32
BP = 34.768, df = 10, p-value = 0.0001368

```

```
# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
HWrobstdter <- sqrt(diag(vcovHC(negbin32, type="HC1")))
```

```
# produces Huber-White robust standard errors
```

| Values | |
|-------------|---|
| HWrobstdter | Named num [1:11] 0.01883 0.02196 0.02345... |

```

stargazer(negbin32, negbin32,
           se=list(NULL, HWrobstdter),
           apply.coef = exp, t.auto=F, p.auto = F,
           title="Negative Binomial Results", type="text",
           column.labels=c("Normal SE", "HW-Robust SE"),
           df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))

```

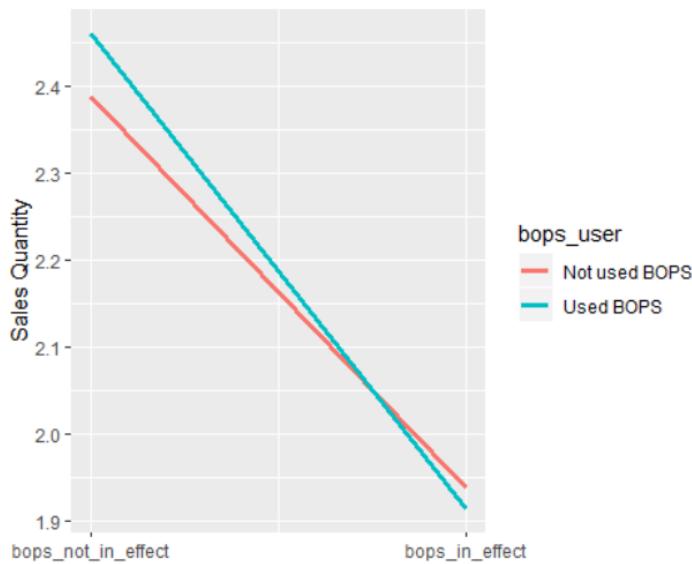
| Negative Binomial Results | | |
|-------------------------------------|---------------------|---------------------|
| Dependent variable: salesquantity | | |
| | Normal SE | HW-Robust SE |
| | (1) | (2) |
| bops_in_effect | 0.811***
(0.007) | 0.811***
(0.022) |
| bops_user | 1.031**
(0.011) | 1.031**
(0.023) |
| purchase_time_period | 1.125***
(0.001) | 1.125***
(0.002) |
| est_income_code | 1.013***
(0.001) | 1.013***
(0.004) |
| age_band | 0.999
(0.001) | 0.999
(0.002) |
| factor(store_number)6 | 1.024*
(0.012) | 1.024*
(0.014) |
| factor(store_number)5998 | 0.753
(0.180) | 0.753
(0.122) |
| homeowner_coden | 0.996
(0.007) | 0.996
(0.022) |
| homeowner_coden | 0.996
(0.007) | 0.996
(0.022) |
| childn | 1.002
(0.006) | 1.002
(0.012) |
| bops_in_effect:bops_user | 0.959**
(0.015) | 0.959**
(0.031) |
| Constant | 1.591***
(0.010) | 1.591***
(0.019) |
| Observations | | |
| Log Likelihood | | |
| theta | | |
| Akaike Inf. Crit. | | |
| 298,304.000 | | |
| ==== | | |
| Note: *p<0.05; **p<0.01; ***p<0.001 | | |
| > | | |

Visualize the output- generated a data frame at two different values of bops_in_effect for two groups - who used BOPS and who didn't after BOPS implementation.

```
meffects33 <- ggpredict(negbin32, terms=c("bops_in_effect", "bops_user"))
```

| | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 2.386680 | 2.364058 | 2.409517 | 0 |
| 2 | 0 | 2.460138 | 2.413039 | 2.508157 | 1 |
| 3 | 1 | 1.936744 | 1.917495 | 1.956187 | 0 |
| 4 | 1 | 1.913799 | 1.877051 | 1.951265 | 1 |

```
ggplot(meffects33, aes(x, predicted, colour=group)) + geom_line(size=1.3) +
  xlab("bops_in_effect") + ylab("Sales Quantity") +
  labs(colour="bops_user") +
  scale_colour_discrete(labels=c("Not used BOPS", "Used BOPS")) +
  scale_x_continuous(breaks=c(0,1), labels=c("bops_not_in_effect", "bops_in_effect")) +
  theme(axis.title.x=element_blank())
```



#Interpretation of approach 2 - The interaction coefficient for bops_in_effect:bops_user is significant with value (0.959). This means that the usage of BOPS service is associated with ~4.1% decrease in sales quantity.

#####=====IMPACT ON SALES VALUE=====#####

```
sales21$log_salesvalue <- log(1+sales21$salesvalue)
```

| BA Project_BOPS_Final Submitted.Rmd | | | | | | | | | | | sales21 | |
|-------------------------------------|-------|----------------|------------|---------------|----------------------|-----------|--------|-----------------|----------------|--|---------|--|
| | | | | | | | | | | | | |
| | | | | | | | | | | | | |
| _of_residence | child | bops_in_effect | salesvalue | salesquantity | purchase_time_period | bops_user | childn | homeowner_coden | log_salesvalue | | | |
| 15 | Y | 0 | 195.30 | 1 | | 1 | 0 | 1 | 5.279644 | | | |
| 15 | Y | 1 | 179.00 | 1 | | 1 | 0 | 1 | 5.192957 | | | |
| 3 | Y | 0 | 72.00 | 1 | | 1 | 0 | 1 | 4.290459 | | | |
| 3 | Y | 1 | 90.16 | 2 | | 4 | 0 | 1 | 4.512616 | | | |
| 15 | N | 0 | 2898.00 | 2 | | 7 | 0 | 0 | 7.972121 | | | |
| 15 | N | 1 | 1873.01 | 8 | | 21 | 0 | 0 | 7.535836 | | | |

Showing 1 to 7 of 81,434 entries

#since salesvalue is 0 at some places, we are taking log of (1+salesvalue)

```
ols33 = lm(log_salesvalue ~ bops_in_effect * bops_user + purchase_time_period + est_income_code +
age_band + factor(store_number) + homeowner_coden + childn, data=sales21)
stargazer(ols33,
  title="Regression Results", type="text",
  column.labels=c("Model-OLS33","Model-OLS31"),
  df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | |
|--------------------------|-------------------------------|--|
| | Dependent variable: | |
| | log_salesvalue | |
| | Model-OLS33 | |
| bops_in_effect | -0.14***
(0.01) | |
| bops_user | -0.22***
(0.01) | |
| purchase_time_period | 0.11***
(0.001) | |
| est_income_code | 0.01***
(0.002) | |
| age_band | 0.01***
(0.001) | |
| factor(store_number)6 | -0.10***
(0.01) | |
| factor(store_number)5998 | 0.34
(0.18) | |
| homeowner_coden | -0.004
(0.01) | |
| childn | -0.05***
(0.01) | |
| bops_in_effect:bops_user | -0.04*
(0.02) | |
| Constant | 5.08***
(0.01) | |
| Observations | 81,434 | |
| R2 | 0.17 | |
| Adjusted R2 | 0.17 | |
| Residual Std. Error | 0.98 | |
| F Statistic | 1,689.92*** | |
| Note: | *p<0.05; **p<0.01; ***p<0.001 | |
| > | | |

```
# Check for heteroskedasticity
```

```
gqtest(ols33) # Goldfeld-Quandt test indicates no heteroskedasticity
```

```
bptest(ols33) # Breusch-Pagan test indicates heteroskedasticity
```

```
> gqtest(ols33) # Goldfeld-Quandt test indicates no heteroskedasticity
```

Goldfeld-Quandt test

```
data: ols33
```

```
GQ = 0.92765, df1 = 40706, df2 = 40706, p-value = 1
```

```
alternative hypothesis: variance increases from segment 1 to 2
```

```
> bptest(ols33) # Breusch-Pagan test indicates heteroskedasticity
```

studentized Breusch-Pagan test

```
data: ols33
```

```
BP = 54.836, df = 10, p-value = 0.00000003389
```

```
# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
HWrobstderr <- sqrt(diag(vcovHC(ols33, type="HC1"))) # produces Huber-White robust standard errors
```

Values

| HWrobstderr | Named num [1:11] 0.010905 0.00769 0.0127... |
|-------------|---|
|-------------|---|

```
stargazer(ols33, ols33,
          se=list(NULL, HWrobstderr),
          title="Regression Results", type="text",
          column.labels=c("Normal SE", "HW-Robust SE"),
          df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | | |
|--------------------------|----------------------|----------------------|--------------|
| | | Dependent variable: | |
| | | log_salesvalue | |
| | | Normal SE | HW-Robust SE |
| | | (1) | (2) |
| bops_in_effect | -0.144***
(0.008) | -0.144***
(0.008) | |
| bops_user | -0.222***
(0.012) | -0.222***
(0.013) | |
| purchase_time_period | 0.106***
(0.001) | 0.106***
(0.001) | |
| est_income_code | 0.008***
(0.002) | 0.008***
(0.002) | |
| age_band | 0.005***
(0.001) | 0.005***
(0.001) | |
| factor(store_number)6 | -0.098***
(0.014) | -0.098***
(0.013) | |
| factor(store_number)5998 | 0.341
(0.181) | 0.341**
(0.128) | |
| homeowner_coden | -0.004
(0.008) | -0.004
(0.008) | |
| childn | -0.045***
(0.007) | -0.045***
(0.007) | |
| bops_in_effect:bops_user | -0.044*
(0.018) | -0.044*
(0.018) | |
| Constant | 5.083***
(0.011) | 5.083***
(0.011) | |
| Observations | 81,434 | 81,434 | |
| R2 | 0.172 | 0.172 | |
| Adjusted R2 | 0.172 | 0.172 | |
| Residual Std. Error | 0.977 | 0.977 | |
| F Statistic | 1,689.924*** | 1,689.924*** | |

Note: *p<0.05; **p<0.01; ***p<0.001

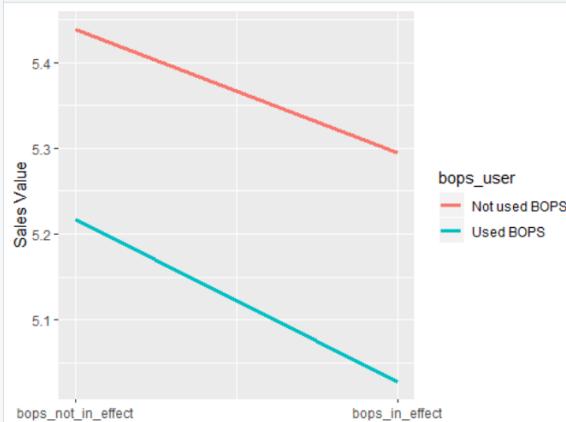
```
# Visualize the output
```

```
meffects34 <- ggpredict(ols33, terms=c("bops_in_effect","bops_user"))
```

| | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 5.438957 | 5.428127 | 5.449787 | 0 |
| 2 | 0 | 5.216780 | 5.194715 | 5.238845 | 1 |
| 3 | 1 | 5.294682 | 5.283919 | 5.305445 | 0 |
| 4 | 1 | 5.028070 | 5.005819 | 5.050321 | 1 |

```
#generates a tidy data frame at two different values of bops_in_effect for two groups - who used BOPS and who didn't after BOPS implementation.
```

```
ggplot(meffects34,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
  xlab("bops_in_effect") + ylab("Sales Value") +
  labs(colour="bops_user") +
  scale_colour_discrete(labels=c("Not used BOPS","Used BOPS")) +
  scale_x_continuous(breaks=c(0,1), labels=c("bops_not_in_effect", "bops_in_effect")) +
  theme(axis.title.x=element_blank())
```



#Interpretation of approach 2 - The interaction coefficient for bops_in_effect:bops_user is significant with value (-0.044). This means that the usage of BOPS service is associated with ~4.4% decrease in sales value.

#We got different results with Approach-1 (removing rows where female is NA) and Approach-2 (dropping female as control variable). Impact on sales value of BOPS usage was insignificant with Approach-1. However, it came out significant with Approach-2.

...

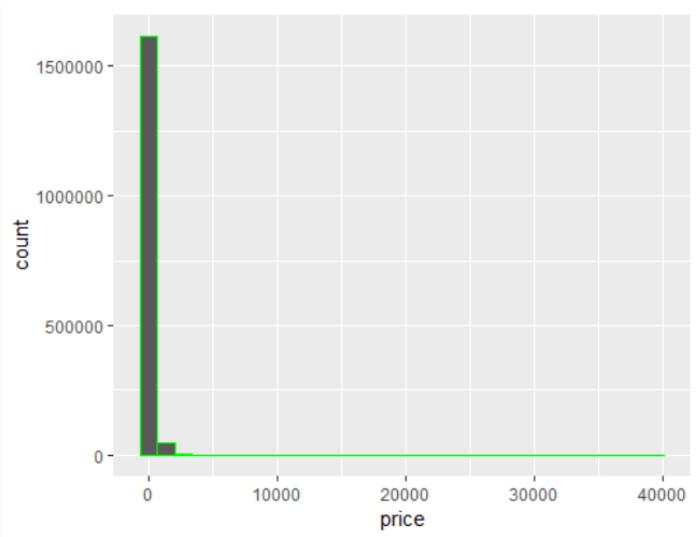
```
#=====#
## Question4: What is the impact of using the BOPS service on online customer return behavior?
#=====#
``{r}
```

#Descriptive Statistics

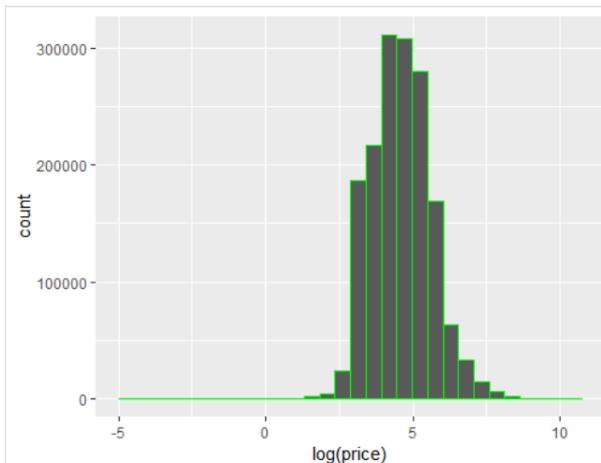
```
stargazer(trans_level, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|---------------------|-----------|------------------|-------------------|------------|------------|------------|-------------|-----------------|
| customer_id | 1,671,502 | 29,441,376,672.0 | 141,529,202,622.0 | 100,348 | 25,694,206 | 30,152,198 | 34,992,529 | 919,650,001,519 |
| transaction_id | 1,671,502 | 3,338,930.0 | 817,965.5 | 7,198 | 2,649,367 | 3,355,444 | 4,030,256.0 | 4,702,552 |
| store_number | 1,671,502 | 229.5 | 1,145.0 | 2 | 2 | 2 | 2 | 5,998 |
| price | 1,671,502 | 170.3 | 319.5 | 0.0 | 45.1 | 90.0 | 189.0 | 39,422.0 |
| sku | 1,671,502 | 18,300,993.0 | 1,587,131.0 | 10,033,405 | 17,859,869 | 18,126,698 | 18,584,417 | 80,006,100 |
| return | 1,671,502 | 0.1 | 0.3 | 0 | 0 | 0 | 0 | 1 |
| age_band | 1,599,464 | 5.0 | 3.9 | 0.0 | 0.0 | 5.0 | 8.0 | 13.0 |
| est_income_code | 1,602,838 | 5.4 | 2.3 | 1.0 | 4.0 | 6.0 | 7.0 | 9.0 |
| length_of_residence | 1,602,838 | 7.1 | 5.4 | 0.0 | 2.0 | 6.0 | 13.0 | 15.0 |
| year | 1,671,502 | 2,011.6 | 1.0 | 2,010 | 2,011 | 2,012 | 2,012 | 2,013 |
| month_index | 1,671,502 | 31.5 | 10.4 | 13 | 22 | 31 | 41 | 48 |
| product_category | 1,671,498 | 10.1 | 6.5 | 1.0 | 5.0 | 9.0 | 12.0 | 21.0 |
| month_dummy | 1,671,502 | 7.4 | 4.0 | 1 | 4 | 8 | 12 | 12 |
| week_index | 1,671,502 | 83.0 | 45.0 | 1 | 41 | 81 | 124 | 157 |
| bops | 1,170,568 | 0.2 | 0.4 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 |
| female | 1,413,233 | 0.5 | 0.5 | 0.0 | 0.0 | 0.0 | 1.0 | 1.0 |

```
ggplot(trans_level, aes(x=price)) + geom_histogram(colour="green", bins = 30)
```



```
ggplot(trans_level, aes(x=log(price))) + geom_histogram(colour="green", bins = 30)
```



#Histogram plot shows that log-transformed price look more like a normal. Therefore, we will use log-transformed price, instead of the raw price.

```
trans_level$logprice <- log(1+trans_level$price)
```

| | length_of_residence | child | year | month | month_index | product_category | month_dummy | week_index | bops | female | logprice |
|--|---------------------|-------|------|-------|-------------|------------------|-------------|------------|------|--------|----------|
| | 2 | Y | 2012 | MAR | 32 | 5 | 3 | 84 | 0 | 0 | 5.959845 |
| | 2 | Y | 2012 | MAR | 32 | 5 | 3 | 84 | 0 | 0 | 7.120493 |
| | 4 | N | 2010 | AUG | 13 | 4 | 8 | 1 | NA | 1 | 5.309158 |
| | 4 | Y | 2010 | AUG | 13 | 5 | 8 | 1 | NA | 0 | 5.298317 |
| | 12 | N | 2010 | AUG | 13 | 5 | 8 | 1 | NA | 1 | 3.400530 |
| | 14 | Y | 2010 | AUG | 13 | 5 | 8 | 1 | NA | 1 | 5.385183 |
| | 5 | N | 2010 | AUG | 13 | 5 | 8 | 1 | NA | 0 | 4.469007 |
| | 5 | N | 2010 | AUG | 13 | 5 | 8 | 1 | NA | 0 | 3.875566 |

Showing 1 to 9 of 1,671,502 entries

To take care about the negative values, scaling doesn't have any impact

Creating a subset to analyze the impact of using BOPS service when BOPS was in effect

```
trans_level1 <- subset(trans_level, trans_level$bops == 1 | trans_level$bops == 0)
```

```
# Converting child variable to a dummy variable.
trans_level1$child = ifelse(trans_level1$child=="Y",1,0)

# Converting homeowner_code to a dummy variable.
trans_level1$homeowner_code = ifelse(trans_level1$homeowner_code=="O",1,0)
```

```
# 183466 records (~15.6% of trans_level1) of female variable have NA values
table(trans_level1$female == 'NA')
```

```
FALSE
987102
```

```
# To replace NA values of est_income_code, age band and length of residence with their median values
trans_level1$est_income_code[is.na(trans_level1$est_income_code)] <-
median(trans_level1$est_income_code, na.rm = TRUE)
trans_level1$age_band[is.na(trans_level1$age_band)] <- median(trans_level1$age_band, na.rm = TRUE)
trans_level1$length_of_residence[is.na(trans_level1$length_of_residence)] <-
median(trans_level1$length_of_residence, na.rm = TRUE)
```

```
stargazer(trans_level1, type="text", median=TRUE, iqr=TRUE, digits=2, title="Descriptive Statistics")
Descriptive Statistics
```

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|---------------------|-----------|-------------------|--------------------|------------|-------------|------------|-------------|-----------------|
| customer_id | 1,170,568 | 23,247,802,315.00 | 125,423,860,663.00 | 100,348 | 28,454,419 | 31,964,480 | 35,423,835 | 919,650,001,519 |
| transaction_id | 1,170,568 | 3,751,126.00 | 561,621.20 | 50,002 | 3,262,163.0 | 3,787,321 | 4,236,822.0 | 4,702,552 |
| store_number | 1,170,568 | 180.36 | 1,017.89 | 2 | 2 | 2 | 2 | 5,998 |
| price | 1,170,568 | 170.16 | 323.39 | 0.00 | 44.24 | 89.99 | 186.99 | 39,422.00 |
| sku | 1,170,568 | 18,424,852.00 | 1,380,845.00 | 11,373,024 | 17,951,286 | 18,214,460 | 18,697,427 | 80,006,100 |
| return | 1,170,568 | 0.10 | 0.30 | 0 | 0 | 0 | 0 | 1 |
| age_band | 1,170,568 | 4.84 | 3.89 | 0 | 0 | 5 | 8 | 13 |
| est_income_code | 1,170,568 | 5.41 | 2.23 | 1 | 4 | 6 | 7 | 9 |
| homeowner_code | 1,170,568 | 0.64 | 0.48 | 0 | 0 | 1 | 1 | 1 |
| length_of_residence | 1,170,568 | 7.14 | 5.34 | 0 | 2 | 6 | 13 | 15 |
| child | 1,170,568 | 0.39 | 0.49 | 0 | 0 | 0 | 1 | 1 |
| year | 1,170,568 | 2,012.05 | 0.71 | 2,011 | 2,012 | 2,012 | 2,013 | 2,013 |
| month_index | 1,170,568 | 37.03 | 6.62 | 25 | 30 | 39 | 42 | 48 |
| product_category | 1,170,564 | 10.10 | 6.47 | 1.00 | 5.00 | 9.00 | 12.00 | 21.00 |
| month_dummy | 1,170,568 | 7.39 | 4.04 | 1 | 4 | 8 | 12 | 12 |
| week_index | 1,170,568 | 107.13 | 28.66 | 53 | 78 | 117 | 129 | 157 |
| bops | 1,170,568 | 0.24 | 0.43 | 0 | 0 | 0 | 0 | 1 |
| female | 987,102 | 0.49 | 0.50 | 0.00 | 0.00 | 0.00 | 1.00 | 1.00 |
| logprice | 1,170,568 | 4.47 | 1.25 | 0.00 | 3.81 | 4.51 | 5.24 | 10.58 |

```
# Checking for multi-collinearity
```

```
df41=trans_level1[c("bops","month_dummy","product_category","female","logprice","year",
"age_band", "est_income_code")]
```

| | bops | month_dummy | product_category | female | logprice | year | age_band | est_income_code |
|--------|------|-------------|------------------|--------|----------|------|----------|-----------------|
| 434241 | 0 | 8 | 4 | 0 | 7.067448 | 2011 | 11 | 6 |
| 434242 | 0 | 8 | 12 | 1 | 3.044046 | 2011 | 8 | 9 |
| 434243 | 0 | 8 | 12 | 0 | 3.753027 | 2011 | 0 | 5 |
| 434244 | 0 | 8 | 6 | NA | 5.525413 | 2011 | 0 | 5 |
| 434245 | 0 | 8 | 21 | 1 | 4.930004 | 2011 | 10 | 6 |
| 434246 | 0 | 8 | 4 | 0 | 5.268116 | 2011 | 4 | 2 |

Showing 56 to 62 of 1,170,568 entries

```
round(cor(df41),3)
> round(cor(df41),3)
      bops month_dummy product_category female logprice year age_band est_income_code
bops    1.000   -0.006          NA   NA  -0.021  0.086  -0.027   -0.013
month_dummy -0.006    1.000          NA   NA   0.026 -0.656   0.057    0.051
product_category  NA       NA          1   NA     NA   NA     NA     NA
female        NA       NA          1   NA     NA   NA     NA     NA
logprice      -0.021   0.026          NA   NA   1.000 -0.065  -0.009   -0.003
year          0.086  -0.656          NA   NA  -0.065  1.000  -0.046   -0.038
age_band     -0.027   0.057          NA   NA  -0.009 -0.046   1.000   0.169
est_income_code -0.013   0.051          NA   NA  -0.003 -0.038   0.169   1.000
```

vifcor(df41)

```
> vifcor(df41)
No variable from the 8 input variables has collinearity problem.
```

```
The linear correlation coefficients ranges between:
min correlation ( age_band ~ product_category ):  0.0007822897
max correlation ( year ~ month_dummy ):  -0.6539523
```

```
----- VIFs of the remained variables -----
Variables      VIF
1      bops 1.017853
2      month_dummy 1.765473
3 product_category 1.009632
4      female 1.029113
5      logprice 1.033008
6      year 1.778289
7      age_band 1.017496
8 est_income_code 1.015664
```

#To remove NA value from female

```
trans_level2 <- subset(trans_level1, trans_level1$female != 'NA')
stargazer(trans_level2, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

| Descriptive Statistics | | | | | | | | |
|------------------------|---------|------------------|-------------------|------------|--------------|--------------|--------------|-----------------|
| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
| customer_id | 987,102 | 25,917,443,507.0 | 132,002,375,089.0 | 100,348 | 27,948,575.0 | 31,773,151.0 | 35,404,273.0 | 919,650,001,519 |
| transaction_id | 987,102 | 3,721,998.0 | 560,640.4 | 50,002 | 3,223,963.0 | 3,746,786 | 4,200,095.0 | 4,702,383 |
| store_number | 987,102 | 3.4 | 82.1 | 2 | 2 | 2 | 2 | 5,998 |
| price | 987,102 | 170.1 | 327.4 | 0.0 | 44.1 | 90.0 | 186.1 | 39,422.0 |
| sku | 987,102 | 18,417,145.0 | 1,402,656.0 | 11,373,024 | 17,945,767 | 18,209,999 | 18,688,697 | 80,006,100 |
| return | 987,102 | 0.1 | 0.3 | 0 | 0 | 0 | 0 | 1 |
| age_band | 987,102 | 5.4 | 3.8 | 0 | 3 | 5 | 8 | 13 |
| est_income_code | 987,102 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| homeowner_code | 987,102 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |
| length_of_residence | 987,102 | 7.5 | 5.4 | 0 | 2 | 6 | 14 | 15 |
| child | 987,102 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| year | 987,102 | 2,012.0 | 0.7 | 2,011 | 2,012 | 2,012 | 2,013 | 2,013 |
| month_index | 987,102 | 36.7 | 6.6 | 25 | 30 | 39 | 42 | 48 |
| product_category | 987,099 | 10.1 | 6.5 | 1.0 | 5.0 | 9.0 | 12.0 | 21.0 |
| month_dummy | 987,102 | 7.5 | 4.0 | 1 | 4 | 8 | 12 | 12 |
| week_index | 987,102 | 105.6 | 28.7 | 53 | 75 | 114 | 128 | 157 |
| bops | 987,102 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| female | 987,102 | 0.5 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| logprice | 987,102 | 4.5 | 1.2 | 0.0 | 3.8 | 4.5 | 5.2 | 10.6 |

To remove 3 blank records of product category as the number of records are less and we cannot replace the missing values by its mean or median

```
trans_level2 <- na.omit(trans_level2)
stargazer(trans_level2, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

Descriptive statistics

| Statistic | N | Mean | St. Dev. | Min | Pctl(25) | Median | Pctl(75) | Max |
|---------------------|---------|------------------|-------------------|------------|--------------|------------|--------------|-----------------|
| customer_id | 987,099 | 25,917,522,176.0 | 132,002,567,967.0 | 100,348 | 27,948,555.0 | 31,773,150 | 35,404,274.0 | 919,650,001,519 |
| transaction_id | 987,099 | 3,721,998.0 | 560,639.4 | 50,002 | 3,223,963 | 3,746,785 | 4,200,093.0 | 4,702,383 |
| store_number | 987,099 | 3.4 | 82.1 | 2 | 2 | 2 | 2 | 5,998 |
| price | 987,099 | 170.1 | 327.4 | 0.0 | 44.1 | 90.0 | 186.1 | 39,422.0 |
| sku | 987,099 | 18,417,080.0 | 1,401,287.0 | 11,373,024 | 17,945,767 | 18,209,999 | 18,688,697 | 40,005,720 |
| return | 987,099 | 0.1 | 0.3 | 0 | 0 | 0 | 0 | 1 |
| age_band | 987,099 | 5.4 | 3.8 | 0 | 3 | 5 | 8 | 13 |
| est_income_code | 987,099 | 5.5 | 2.2 | 1 | 4 | 6 | 7 | 9 |
| homeowner_code | 987,099 | 0.7 | 0.5 | 0 | 0 | 1 | 1 | 1 |
| length_of_residence | 987,099 | 7.5 | 5.4 | 0 | 2 | 6 | 14 | 15 |
| child | 987,099 | 0.4 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| year | 987,099 | 2,012.0 | 0.7 | 2,011 | 2,012 | 2,012 | 2,013 | 2,013 |
| month_index | 987,099 | 36.7 | 6.6 | 25 | 30 | 39 | 42 | 48 |
| product_category | 987,099 | 10.1 | 6.5 | 1 | 5 | 9 | 12 | 21 |
| month_dummy | 987,099 | 7.5 | 4.0 | 1 | 4 | 8 | 12 | 12 |
| week_index | 987,099 | 105.6 | 28.7 | 53 | 75 | 114 | 128 | 157 |
| bops | 987,099 | 0.2 | 0.4 | 0 | 0 | 0 | 0 | 1 |
| female | 987,099 | 0.5 | 0.5 | 0 | 0 | 0 | 1 | 1 |
| logprice | 987,099 | 4.5 | 1.2 | 0.0 | 3.8 | 4.5 | 5.2 | 10.6 |

Total number of records are same after cleansing the data

Checking multi collinearity

```
df42=trans_level2[c("bops","month_dummy","product_category","female","logprice","year",
"age_band", "est_income_code")]
```

| | bops | month_dummy | product_category | female | logprice | year | age_band | est_income_code |
|--------|------|-------------|------------------|--------|----------|------|----------|-----------------|
| 1 | 0 | 3 | 5 | 0 | 5.959845 | 2012 | 7 | 8 |
| 2 | 0 | 3 | 5 | 0 | 7.120493 | 2012 | 7 | 8 |
| 434187 | 0 | 8 | 12 | 1 | 3.693867 | 2011 | 9 | 5 |
| 434188 | 0 | 8 | 12 | 1 | 3.753027 | 2011 | 9 | 5 |
| 434189 | 0 | 8 | 5 | 1 | 4.117898 | 2011 | 5 | 6 |
| 434190 | 0 | 8 | 17 | 1 | 6.917616 | 2011 | 4 | 4 |

Showing 1 to 7 of 987,099 entries

```
round(cor(df42),3)
```

```
> round(cor(df42),3)
          bops month_dummy product_category female logprice year age_band est_income_code
bops      1.000   -0.006       0.003  0.041   -0.021  0.079   -0.032    -0.019
month_dummy -0.006    1.000       0.020  -0.040    0.024  -0.653    0.048     0.049
product_category 0.003    0.020       1.000  0.027   -0.082  -0.031    0.005     0.014
female      0.041   -0.040       0.027  1.000   -0.142   0.035    0.068    -0.024
logprice     -0.021    0.024       -0.082  -0.142    1.000  -0.071   -0.011    -0.001
year        0.079   -0.653       -0.031  0.035   -0.071   1.000   -0.022    -0.033
age_band    -0.032    0.048       0.005  0.068   -0.011  -0.022    1.000     0.137
est_income_code -0.019    0.049       0.014  -0.024   -0.001  -0.033    0.137    1.000
```

```
vifcor(df42)
```

```
> vifcor(df42)
No variable from the 8 input variables has collinearity problem.

The linear correlation coefficients ranges between:
min correlation ( logprice ~ bops ): -0.001422741
max correlation ( year ~ month_dummy ): -0.6560216

----- VIFs of the remained variables -----
Variables      VIF
1             bops 1.016310
2           month_dummy 1.772950
3 product_category 1.008077
4           female 1.030778
5          logprice 1.025189
6            year 1.785112
7         age_band 1.037572
8 est_income_code 1.027502
```

Creating factor variables of store number, year and month_dummy if we have to use the factor variable

```
trans_level2$f_store <- as.factor(trans_level2$store_number)
trans_level2$f_year <- as.factor(trans_level2$year)
trans_level2$f_month <- as.factor(trans_level2$month_dummy)
```

| month | month_index | product_category | month_dummy | week_index | bops | female | logprice | f_store | f_year | f_month | |
|-------|-------------|------------------|-------------|------------|------|--------|----------|----------|--------|---------|---|
| 12 | MAR | 32 | 5 | 3 | 84 | 0 | 0 | 5.959845 | 2 | 2012 | 3 |
| 12 | MAR | 32 | 5 | 3 | 84 | 0 | 0 | 7.120493 | 2 | 2012 | 3 |
| 11 | AUG | 25 | 12 | 8 | 53 | 0 | 1 | 3.693867 | 2 | 2011 | 8 |
| 11 | AUG | 25 | 12 | 8 | 53 | 0 | 1 | 3.753027 | 2 | 2011 | 8 |
| 11 | AUG | 25 | 5 | 8 | 53 | 0 | 1 | 4.117898 | 2 | 2011 | 8 |

Showing 1 to 7 of 987,099 entries

#####===== OLS MODEL =====#####

```
lpm41<-
lm(return~bops+logprice+product_category+f_store+est_income_code+female+age_band+f_month+f_y
ear, data=trans_level2)

stargazer(lpm41,
  title="Regression Results", type="text",
  column.labels=c("Model-1"),
  df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | f_month4 | -0.0170***
(0.0016) |
|---------------------|--|-------------------------------|------------------------|
| | | f_month5 | -0.0374***
(0.0015) |
| | | f_month6 | -0.0220***
(0.0018) |
| | | f_month7 | -0.0282***
(0.0018) |
| | | f_month8 | -0.0241***
(0.0019) |
| | | f_month9 | -0.0262***
(0.0019) |
| | | f_month10 | -0.0218***
(0.0018) |
| | | f_month11 | -0.0341***
(0.0015) |
| | | f_month12 | -0.0440***
(0.0014) |
| | | f_year2012 | -0.0086***
(0.0008) |
| | | f_year2013 | -0.0106***
(0.0012) |
| | | Constant | -0.0333***
(0.0021) |
| <hr/> | | | |
| Observations | | 987,099 | |
| R2 | | 0.0245 | |
| Adjusted R2 | | 0.0244 | |
| Residual Std. Error | | 0.2973 | |
| F Statistic | | 1,178.2720*** | |
| <hr/> | | | |
| Note: | | *p<0.05; **p<0.01; ***p<0.001 | |
| > | | | |

Usage of BOPS service is associated with 1.51 percentage points increase in return probability. This means that a BOPS user is 1.51 percentage points more likely to return a jewellery item.

You can also use heteroscedastic-robust standard errors for 2SLS

```
gqttest(lpm41) # Significant Goldfeld-Quandt test indicates heteroskedasticity
bptest(lpm41) # Significant Breusch-Pagan test indicates heteroskedasticity
> gqttest(lpm41) # Significant Goldfeld-Quandt test indicates heteroskedasticity

      Goldfeld-Quandt test

data: lpm41
GQ = 0.88408, df1 = 493530, df2 = 493530, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2

> bptest(lpm41) # Significant Breusch-Pagan test indicates heteroskedasticity

      studentized Breusch-Pagan test

data: lpm41
BP = 24752, df = 21, p-value < 2.2e-16
```

```
consstderr_lpm41 <- sqrt(diag(vcovHC(lpm41, type="const"))) # produces normal standard errors
HWrobstderr_lpm41 <- sqrt(diag(vcovHC(lpm41, type="HC1"))) # produces Huber-White robust standard errors
```

| values | |
|------------------|---|
| consstderr_lpm41 | Named num [1:22] 0.0021194 0.0007191 0.0002477... |
| HWrobstderr | Named num [1:11] 0.010905 0.00769 0.012733 0.0... |

```
stargazer(lpm41, lpm41,
          se=list(consstderr_lpm41, HWrobstderr_lpm41),
          title="Regression Results", type="text",
          column.labels=c("Normal SE", "HW-Robust SE"),
          df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | f_month4 | -0.0170***
(0.0016) | -0.0170***
(0.0016) |
|--------------------|-------------------------|------------|------------------------|------------------------|
| | | f_month5 | -0.0374***
(0.0015) | -0.0374***
(0.0015) |
| | | f_month6 | -0.0220***
(0.0018) | -0.0220***
(0.0020) |
| bops | 0.0151***
(0.0007) | f_month7 | -0.0282***
(0.0018) | -0.0282***
(0.0019) |
| logprice | 0.0354***
(0.0002) | f_month8 | -0.0241***
(0.0019) | -0.0241***
(0.0020) |
| product_category | -0.0007***
(0.00005) | f_month9 | -0.0262***
(0.0019) | -0.0262***
(0.0020) |
| f_store6 | -0.0063***
(0.0012) | f_month10 | -0.0218***
(0.0018) | -0.0218***
(0.0018) |
| f_store5998 | -0.0834***
(0.0219) | f_month11 | -0.0341***
(0.0015) | -0.0341***
(0.0016) |
| est_income_code | 0.0014***
(0.0001) | f_month12 | -0.0440***
(0.0014) | -0.0440***
(0.0014) |
| female | 0.0301***
(0.0006) | f_year2012 | -0.0086***
(0.0008) | -0.0086***
(0.0008) |
| age_band | -0.0011***
(0.0001) | f_year2013 | -0.0106***
(0.0012) | -0.0106***
(0.0012) |
| f_month2 | -0.0317***
(0.0014) | Constant | -0.0333***
(0.0021) | -0.0333***
(0.0020) |
| f_month3 | -0.0146***
(0.0017) | | | |

| | | |
|---------------------|-------------------------------|---------------|
| Observations | 987,099 | 987,099 |
| R2 | 0.0245 | 0.0245 |
| Adjusted R2 | 0.0244 | 0.0244 |
| Residual Std. Error | 0.2973 | 0.2973 |
| F Statistic | 1,178.2720*** | 1,178.2720*** |
| Note: | *p<0.05; **p<0.01; ***p<0.001 | |

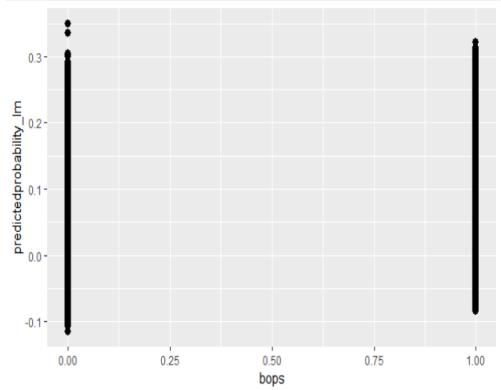
displays normal and HW robust standard errors. # we observe that with robust standard errors.

```
trans_level2$predictedprobability_lm<-predict(lpm41) # let's look at the predicted probability of return  
for each observation in the data
```

| category | month_dummy | week_index | bops | female | logprice | f_store | f_year | f_month | predictedprobability_lm |
|----------|-------------|------------|------|--------|----------|----------|--------|---------|-------------------------|
| 5 | | 3 | 84 | 0 | 0 | 5.959845 | 2 | 2012 | 3 |
| 5 | | 3 | 84 | 0 | 0 | 7.120493 | 2 | 2012 | 3 |
| 12 | | 8 | 53 | 0 | 1 | 3.693867 | 2 | 2011 | 8 |
| 12 | | 8 | 53 | 0 | 1 | 3.753027 | 2 | 2011 | 8 |
| 5 | | 8 | 53 | 0 | 1 | 4.117898 | 2 | 2011 | 8 |
| 17 | | 8 | 53 | 0 | 1 | 6.917616 | 2 | 2011 | 8 |

Showing 1 to 7 of 987,099 entries

```
ggplot(trans_level2, aes(y=predictedprobability_lm, x=bops)) + geom_point(size=2.5)
```



```
range(trans_level2$predictedprobability_lm)
```

```
[1] -0.1153405 0.3497532
```

```
# Range of the predicted probability tells us there are "negative" probabilities of return for some  
observations!!! This cannot be possible. Therefore, linear probability model is not the right model
```

```
confint(lpm41,"bops") # Generating confidence interval for variable BOPS
```

```
2.5 % 97.5 %  
bops 0.01369205 0.01651074
```

```
#####===== LOGIT MODEL =====####
```

```
sum(trans_level2$return==0)
```

```
sum(trans_level2$return==1)
```

```
> sum(trans_level2$return==0)  
[1] 887623  
> sum(trans_level2$return==1)  
[1] 99476
```

```
# We have 99476 observations with Return=1 and 887623 observations with Return=0. Considering that  
we will estimate 21 parameters, we satisfy the minimum 10:1 ratio requirement
```

```
logit42<-
glm(return~bops+logprice+product_category+f_store+f_month+f_year+est_income_code+female+age_
band, data=trans_level2, family="binomial")
stargazer(logit42,
  apply.coef = exp, t.auto=F, p.auto = F,
  title="Regression Results", type="text",
  column.labels=c("OddsRatios"),
  df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | f_month7 | 0.7847***
(0.0192) |
|--------------------|-------------------------------|-----------------|-----------------------|
| <hr/> | | | |
| | Dependent variable: | | |
| | return
oddsRatios | | |
| <hr/> | | | |
| bops | 1.2068***
(0.0079) | f_month8 | 0.8046***
(0.0201) |
| logprice | 1.5831***
(0.0033) | f_month9 | 0.7790***
(0.0206) |
| product_category | 0.9987*
(0.0005) | f_month10 | 0.7931***
(0.0194) |
| f_store6 | 0.9276***
(0.0142) | f_month11 | 0.7305***
(0.0164) |
| f_store5998 | 0.2983***
(0.3633) | f_month12 | 0.6598***
(0.0150) |
| f_month2 | 0.7640***
(0.0153) | f_year2012 | 0.9073***
(0.0096) |
| f_month3 | 0.8900***
(0.0178) | f_year2013 | 0.8578***
(0.0137) |
| f_month4 | 0.7978***
(0.0180) | est_income_code | 1.0163***
(0.0015) |
| f_month5 | 0.7082***
(0.0164) | female | 1.4522***
(0.0070) |
| f_month6 | 0.8345***
(0.0192) | age_band | 0.9873***
(0.0009) |
| | | Constant | 0.0146***
(0.0265) |
| <hr/> | | | |
| Observations | 987,099 | | |
| Log Likelihood | -309,446.1000 | | |
| Akaike Inf. Crit. | 618,936.2000 | | |
| <hr/> | | | |
| Note: | *p<0.05; **p<0.01; ***p<0.001 | | |

The odds of being returned (versus not being returned) increase by a factor of 1.2068 when a customer is a BOPS user.

Model fit assessment

```
logit42a <- glm(return~1, data=trans_level2, family="binomial") # This is the command to run a logit on
null model
```

| | |
|------------|-----------------------------------|
| ➊ logit42 | Large glm (30 elements, 836.2 Mb) |
| ➋ logit42a | Large glm (30 elements, 632.8 Mb) |

```
lrtest(logit42, logit42a)
```

Likelihood ratio test

```

Model 1: return ~ bops + logprice + product_category + f_store + f_month +
          f_year + est_income_code + female + age_band
Model 2: return ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 22 -309446
2  1 -322569 -21 26246 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

#We compare the null model to our model to determine the model fit. The chi-square of 26246 with 21 degrees of freedom and an associated p-value of less than 0.001 tells us that our model as a whole fits significantly better than the null model.

Obtain marginal effects

```

a42 <- logitmfx(formula=return~bops+logprice+product_category+f_store+f_month+f_year+est_income_code
+female+age_band, data=trans_level2) # We can generate the marginal effects with this command.

```

```
marginaleffects42 <- a42$mfxfest[,1]
```

```
marg.std.err42 <- a42$mfxfest[,2]
```

| | |
|------------------|---|
| marg.std.err42 | Named num [1:21] 0.0007031 0.0002453 0.0... |
| marginaleffect.. | Named num [1:21] 0.016027 0.037552 -0.00... |

```

stargazer(logit42,
  omit=c("Constant"),
  coef = list(marginaleffects42), se = list(marg.std.err42),
  title="Regression Results", type="text",
  column.labels=c("Marginal Effects"),
  df=FALSE, digits=5, star.cutoffs = c(0.05,0.01,0.001))

```

| Regression Results | | f_month8 | -0.01639***
(0.00139) |
|--------------------|--------------------------|-------------------|-------------------------------|
| | | f_month9 | -0.01860***
(0.00139) |
| | | f_month10 | -0.01743***
(0.00134) |
| bops | 0.01603***
(0.00070) | f_month11 | -0.02328***
(0.00110) |
| logprice | 0.03755***
(0.00025) | f_month12 | -0.03147***
(0.00105) |
| product_category | -0.00011*
(0.00004) | f_year2012 | -0.00795***
(0.00078) |
| f_store6 | -0.00598***
(0.00110) | f_year2013 | -0.01218***
(0.00105) |
| f_store5998 | -0.06123***
(0.01009) | est_income_code | 0.00132***
(0.00013) |
| f_month2 | -0.02021***
(0.00105) | female | 0.03070***
(0.00057) |
| f_month3 | -0.00913***
(0.00134) | age_band | -0.00104***
(0.00007) |
| f_month4 | -0.01703***
(0.00125) | <hr/> | |
| f_month5 | -0.02513***
(0.00106) | Observations | 987,099 |
| f_month6 | -0.01382***
(0.00137) | Log Likelihood | -309,446.10000 |
| f_month7 | -0.01811***
(0.00131) | Akaike Inf. Crit. | 618,936.20000 |
| <hr/> | | Note: | *p<0.05; **p<0.01; ***p<0.001 |

Usage of BOPS service increases the probability of return by 0.01603, holding other variables at their means.

```
b42 <-  
logitmfx(formula=return~bops+logprice+product_category+f_store+f_month+f_year+est_income_code  
+female+age_band, data=trans_level2, robust=TRUE) # We can obtain the marginal effects from a logit  
that uses robust standard errors. Note that marginal effects do not change, however, std. errors, and  
therefore, p-values change.  
rob.std.err42 <- b42$mfxest[,2]
```

```
stargazer(logit42, logit42,  
se=list(marg.std.err42, rob.std.err42),  
omit=c("Constant"),  
coef = list(marginaleffects42,marginaleffects42),  
title="Regression Results", type="text",  
column.labels=c("Marginal Effects","Marg.Eff.w/RobStdEr" ),  
df=FALSE, digits=5, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results | | f_month7 | -0.01811***
(0.00131) | -0.01811***
(0.00131) |
|--------------------|--------------------------|-------------------|--------------------------|--------------------------|
| | | f_month8 | -0.01639***
(0.00139) | -0.01639***
(0.00139) |
| | | f_month9 | -0.01860***
(0.00139) | -0.01860***
(0.00140) |
| | | f_month10 | -0.01743***
(0.00134) | -0.01743***
(0.00134) |
| | | f_month11 | -0.02328***
(0.00110) | -0.02328***
(0.00111) |
| | | f_month12 | -0.03147***
(0.00105) | -0.03147***
(0.00106) |
| | | f_year2012 | -0.00795***
(0.00078) | -0.00795***
(0.00079) |
| | | f_year2013 | -0.01218***
(0.00105) | -0.01218***
(0.00105) |
| | | est_income_code | 0.00132***
(0.00013) | 0.00132***
(0.00013) |
| | | female | 0.03070***
(0.00057) | 0.03070***
(0.00058) |
| | | age_band | -0.00104***
(0.00007) | -0.00104***
(0.00007) |
| bops | 0.01603***
(0.00070) | f_month7 | -0.01811***
(0.00131) | -0.01811***
(0.00131) |
| logprice | 0.03755***
(0.00025) | f_month8 | -0.01639***
(0.00139) | -0.01639***
(0.00139) |
| product_category | -0.00011*
(0.00004) | f_month9 | -0.01860***
(0.00139) | -0.01860***
(0.00140) |
| f_store6 | -0.00598***
(0.00110) | f_month10 | -0.01743***
(0.00134) | -0.01743***
(0.00134) |
| f_store5998 | -0.06123***
(0.01009) | f_month11 | -0.02328***
(0.00110) | -0.02328***
(0.00111) |
| f_month2 | -0.02021***
(0.00105) | f_month12 | -0.03147***
(0.00105) | -0.03147***
(0.00106) |
| f_month3 | -0.00913***
(0.00134) | f_year2012 | -0.00795***
(0.00078) | -0.00795***
(0.00079) |
| f_month4 | -0.01703***
(0.00125) | f_year2013 | -0.01218***
(0.00105) | -0.01218***
(0.00105) |
| f_month5 | -0.02513***
(0.00106) | est_income_code | 0.00132***
(0.00013) | 0.00132***
(0.00013) |
| f_month6 | -0.01382***
(0.00137) | female | 0.03070***
(0.00057) | 0.03070***
(0.00058) |
| | | age_band | -0.00104***
(0.00007) | -0.00104***
(0.00007) |
| | | Observations | 987,099 | 987,099 |
| | | Log Likelihood | -309,446.10000 | -309,446.10000 |
| | | Akaike Inf. Crit. | 618,936.20000 | 618,936.20000 |

Note: *p<0.05; **p<0.01; ***p<0.001

Usage of BOPS service increases the probability of return by 0.01603, holding other variables at their means.

```
pred42 = predict(logit42, data=trans_level2, type="response")
return_prediction42 <- ifelse(pred42 >= 0.5, 1, 0)
misClasificError42 <- mean(return_prediction42 != trans_level2$return)

misClasificErr... 0.10079840016047
pred42 Large numeric (987099 elements, 67.8 Mb)
return_predict... Large numeric (987099 elements, 67.8 Mb)
rob.std.err42 Named num [1:21] 0.0007046 0.0002353 0.0...
```

```
print(paste('Accuracy', 1-misClasificError42))
[1] "Accuracy 0.89920159983953"
# the correct classification rate increased to 89.92%
```

```
table(trans_level2$return, pred42>=0.5)
```

| | FALSE | TRUE |
|---|--------|------|
| 0 | 887590 | 33 |
| 1 | 99465 | 11 |

The coefficient of BOPS from linear probability model is 0.0151 with confidence intervals (0.01369205, 0.01651074) and the coefficient of LOGIT model is 0.01603. Since coefficient of LOGIT model lies in the confidence interval of coefficient of linear probability model, we can say that these models return similar results.

#####===== TEST FOR ENDOGENEITY USING OLS=====#####

Since using BOPS is a customer's decision , we suspect that key independent variable is endogenous.
Child and length of residence are potential instrument variables. Proximity to store is our omitted variable.

Conceptually, these 2 variables do not explain any variation on return of jewellery items. For a customer with a child, using BOPS service would create a hassle for the customer to go back to store and thus child variable is negatively correlated with BOPS.

Length of residence is the number of years a customer has lived on his/her current residence. The higher the number of years the customer has lived in his residence, the more familiar he is with the stores around and is more likely to use BOPS

With length of residence, child as instrument variables

endo41<-

ivreg(return~bops+logprice+product_category+f_store+f_month+f_year+est_income_code+female+age_band|length_of_residence+child+logprice+product_category+f_store+f_month+f_year+est_income_code+female+age_band, data=trans_level2)

The significant test statistics indicates that endogeneity exists and OLS results model will generate biased effects. Both relevance and exogeneity assumption has passed. Sargan statistic is not significant, meaning the instruments are exogenous. Weak instrument statistic is the F-statistic from the first stage. Since it is 121.89>10, it indicates the instruments are relevant. The significant durbin-wu-hausman test statistics indicates that endogeneity exists and OLS results model will generate biased effects.

summary(endo41,diagnostics = TRUE)

```
Call:
ivreg(formula = return ~ bops + logprice + product_category +
  f_store + f_month + f_year + est_income_code + female + age_band |
  length_of_residence + child + logprice + product_category +
  f_store + f_month + f_year + est_income_code + female +
  age_band, data = trans_level2)
```

Residuals:

| | Min | 1Q | Median | 3Q | Max |
|--|----------|----------|----------|---------|---------|
| | -0.62735 | -0.09321 | -0.02713 | 0.02258 | 1.17781 |

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) |
|------------------|-------------|------------|---------|--------------|
| (Intercept) | -0.07635747 | 0.00665133 | -11.480 | < 2e-16 *** |
| bops | 0.36904126 | 0.05107061 | 7.226 | 4.97e-13 *** |
| logprice | 0.03706413 | 0.00036192 | 102.409 | < 2e-16 *** |
| product_category | -0.00075432 | 0.00005311 | -14.204 | < 2e-16 *** |
| f_store6 | 0.02890149 | 0.00524564 | 5.510 | 3.60e-08 *** |
| f_store5998 | -0.14716693 | 0.02607943 | -5.643 | 1.67e-08 *** |
| f_month2 | -0.04043300 | 0.00200233 | -20.193 | < 2e-16 *** |
| f_month3 | -0.02814154 | 0.00274077 | -10.268 | < 2e-16 *** |
| f_month4 | -0.02016118 | 0.00185282 | -10.881 | < 2e-16 *** |
| f_month5 | -0.04500864 | 0.00196522 | -22.903 | < 2e-16 *** |
| f_month6 | -0.03397232 | 0.00267187 | -12.715 | < 2e-16 *** |
| f_month7 | -0.04315030 | 0.00294558 | -14.649 | < 2e-16 *** |
| f_month8 | -0.02105389 | 0.00212501 | -9.908 | < 2e-16 *** |
| f_month9 | -0.04828603 | 0.00383782 | -12.582 | < 2e-16 *** |
| f_month10 | -0.04478738 | 0.00385257 | -11.625 | < 2e-16 *** |
| f_month11 | -0.06218424 | 0.00439275 | -14.156 | < 2e-16 *** |
| f_month12 | -0.07446752 | 0.00465185 | -16.008 | < 2e-16 *** |
| f_year2012 | -0.05514420 | 0.00678403 | -8.129 | 4.35e-16 *** |
| f_year2013 | -0.06034666 | 0.00730686 | -8.259 | < 2e-16 *** |
| est_income_code | 0.00232129 | 0.00020260 | 11.457 | < 2e-16 *** |
| female | 0.01746318 | 0.00194665 | 8.971 | < 2e-16 *** |
| age_band | 0.00020169 | 0.00020437 | 0.987 | 0.324 |

```

Diagnostic tests:
df1      df2 statistic p-value
Weak instruments   2 987076    121.89 < 2e-16 ***
Wu-Hausman        1 987076     59.84 1.03e-14 ***
Sargan            1     NA      1.95    0.163
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3318 on 987077 degrees of freedom
Multiple R-Squared: -0.215,    Adjusted R-squared: -0.215
Wald test: 931.7 on 21 and 987077 DF, p-value: < 2.2e-16

```

```

stargazer(endo41,
           title="Regression Results", type="text",
           column.labels=c("Endo442"),
           df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))

```

| Regression Results | |
|---------------------|-----------------------|
| | Dependent variable: |
| | return
Endo442 |
| bops | 0.369***
(0.051) |
| logprice | 0.037***
(0.0004) |
| product_category | -0.001***
(0.0001) |
| f_store6 | 0.029***
(0.005) |
| f_store5998 | -0.147***
(0.026) |
| f_month2 | -0.040***
(0.002) |
| f_month3 | -0.028***
(0.003) |
| f_month4 | -0.020***
(0.002) |
| f_month5 | -0.045***
(0.002) |
| f_month6 | -0.034***
(0.003) |
| f_month7 | -0.043***
(0.003) |
| f_month8 | -0.021***
(0.002) |
| f_month9 | -0.048***
(0.004) |
| f_month10 | -0.045***
(0.004) |
| f_month11 | -0.062***
(0.004) |
| f_month12 | -0.074***
(0.005) |
| f_year2012 | -0.055***
(0.007) |
| f_year2013 | -0.060***
(0.007) |
| est_income_code | 0.002***
(0.0002) |
| female | 0.017***
(0.002) |
| age_band | 0.0002
(0.0002) |
| Constant | -0.076***
(0.007) |
| Observations | 987,099 |
| R2 | -0.215 |
| Adjusted R2 | -0.215 |
| Residual Std. Error | 0.332 |

Note: *p<0.05; **p<0.01; ***p<0.001

Interpretations: After treating endogeneity in our model, the coefficient for BOPS in 2SLS model is 0.369. This means that a BOPS user is 36.9 percentage points more likely to return a jewellery item.

Since the results from our OLS and Logit models were similar, we are proceeding with 2SLS results.

``

```

#=====
## Question5: What is the impact of implementing BOPS strategy on product-level sales and returns?
#=====
```

```{r}

#Descriptive Statistics

```
stargazer(ODS_prodcat, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

#### Descriptive Statistics

| Statistic        | N      | Mean    | St. Dev. | Min   | Pctl(25) | Median  | Pctl(75) | Max       |
|------------------|--------|---------|----------|-------|----------|---------|----------|-----------|
| store_number     | 30,475 | 1,398.8 | 2,533.2  | 2     | 2        | 6       | 6        | 5,998     |
| year             | 30,475 | 2,011.6 | 0.9      | 2,010 | 2,011    | 2,012   | 2,012    | 2,013     |
| month_index      | 30,475 | 31.1    | 10.3     | 13    | 22       | 31      | 40       | 48        |
| product_category | 30,475 | 9.3     | 6.3      | 1     | 4        | 7       | 13       | 21        |
| month_dummy      | 30,475 | 6.5     | 3.6      | 1     | 3        | 6       | 10       | 12        |
| bops_in_effect   | 30,475 | 0.6     | 0.5      | 0     | 0        | 1       | 1        | 1         |
| day              | 30,475 | 566.6   | 313.4    | 1     | 292      | 569     | 846      | 1,096     |
| salesvalue       | 30,475 | 9,342.4 | 20,865.0 | 0.0   | 546.3    | 1,950.7 | 8,952.2  | 424,294.6 |
| returnvalue      | 30,475 | 1,439.1 | 3,166.5  | 0.0   | 0.0      | 199.0   | 1,398.9  | 52,508.2  |
| salesquantity    | 30,475 | 54.8    | 162.8    | 1     | 3        | 9       | 34       | 5,111     |
| returnquantity   | 30,475 | 5.5     | 13.5     | 0     | 0        | 1       | 5        | 380       |
| avg_female       | 23,277 | 0.5     | 0.3      | 0.0   | 0.3      | 0.5     | 0.7      | 1.0       |
| avg_age          | 23,795 | 4.9     | 2.1      | 0.0   | 4.0      | 4.9     | 5.9      | 13.0      |
| avg_income       | 23,763 | 5.3     | 1.2      | 1.0   | 4.8      | 5.3     | 5.8      | 9.0       |
| avg_homeowner    | 23,763 | 0.6     | 0.3      | 0.0   | 0.5      | 0.7     | 0.8      | 1.0       |
| avg_residency    | 23,763 | 6.9     | 2.8      | 0.0   | 5.6      | 6.9     | 8.0      | 15.0      |
| avg_childowner   | 23,763 | 0.4     | 0.2      | 0.0   | 0.2      | 0.4     | 0.5      | 1.0       |

#Filtering data for days before sept.27,2012

```
sales5 <- ODS_prodcat[((ODS_prodcat$day<788) | (ODS_prodcat$day==788)),]
```

```
stargazer(sales5, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

#### Descriptive Statistics

| Statistic        | N      | Mean    | St. Dev. | Min   | Pctl(25) | Median  | Pctl(75) | Max       |
|------------------|--------|---------|----------|-------|----------|---------|----------|-----------|
| store_number     | 21,115 | 1,286.5 | 2,458.6  | 2     | 2        | 6       | 6        | 5,998     |
| year             | 21,115 | 2,011.2 | 0.7      | 2,010 | 2,011    | 2,011   | 2,012    | 2,012     |
| month_index      | 21,115 | 25.7    | 7.3      | 13    | 19       | 26      | 32       | 38        |
| product_category | 21,115 | 9.4     | 6.3      | 1     | 4        | 7       | 13       | 21        |
| month_dummy      | 21,115 | 6.7     | 3.5      | 1     | 4        | 7       | 9        | 12        |
| bops_in_effect   | 21,115 | 0.4     | 0.5      | 0     | 0        | 0       | 1        | 1         |
| day              | 21,115 | 401.8   | 223.4    | 1     | 205      | 409     | 591      | 788       |
| salesvalue       | 21,115 | 8,722.2 | 19,132.2 | 0.0   | 508.7    | 1,856.6 | 8,526.0  | 402,473.4 |
| returnvalue      | 21,115 | 1,373.6 | 2,992.2  | 0.0   | 0.0      | 193.8   | 1,376.5  | 51,973.1  |
| salesquantity    | 21,115 | 49.9    | 139.6    | 1     | 2        | 9       | 32       | 4,474     |
| returnquantity   | 21,115 | 5.3     | 12.5     | 0     | 0        | 1       | 5        | 380       |
| avg_female       | 16,489 | 0.5     | 0.3      | 0.0   | 0.3      | 0.5     | 0.7      | 1.0       |
| avg_age          | 16,839 | 5.0     | 2.1      | 0.0   | 4.1      | 5.0     | 6.0      | 13.0      |
| avg_income       | 16,827 | 5.3     | 1.2      | 1.0   | 4.8      | 5.4     | 5.8      | 9.0       |
| avg_homeowner    | 16,827 | 0.6     | 0.3      | 0.0   | 0.5      | 0.7     | 0.8      | 1.0       |
| avg_residency    | 16,827 | 6.9     | 2.8      | 0.0   | 5.5      | 6.8     | 7.9      | 15.0      |
| avg_childowner   | 16,827 | 0.4     | 0.2      | 0.0   | 0.2      | 0.3     | 0.5      | 1.0       |

#Add a BIE timeline variable dividing the data into two groups, one before Aug.1, 2011 and the other after.

```
sales5$BIE_timeline_PC <- ifelse(sales5$day<366,0,1)
```

#Add a grouping variable for stores dividing the data into two groups, one for 2 and 6 and the other for 5998.

```
sales5$group_store_PC <- ifelse((sales5$store_number==2) | (sales5$store_number==6),1,0)
```

#Convert product category and month to factor variables

```
sales5$factor_PC <- as.factor(sales5$product_category)
```

```
sales5$factor_Month <- as.factor(sales5$month_dummy)
```

BA Project\_BOPS\_Final Submitted.Rmd sales5

Showing 1 to 7 of 21,115 entries

#Assuming mean value for all 'na' values

```
sales5$avg_female[is.na(sales5$avg_female)] <- mean(sales5$avg_female, na.rm = TRUE)
sales5$avg_age[is.na(sales5$avg_age)] <- mean(sales5$avg_age, na.rm = TRUE)
sales5$avg_income[is.na(sales5$avg_income)] <- mean(sales5$avg_income, na.rm = TRUE)
sales5$avg_homeowner[is.na(sales5$avg_homeowner)] <- mean(sales5$avg_homeowner, na.rm = TRUE)
sales5$avg_residency[is.na(sales5$avg_residency)] <- mean(sales5$avg_residency, na.rm = TRUE)
sales5$avg_chldowner[is.na(sales5$avg_chldowner)] <- mean(sales5$avg_chldowner, na.rm = TRUE)
```

#Descriptive Statistics after placing mean values for all 'na' values

```
stargazer(sales5, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

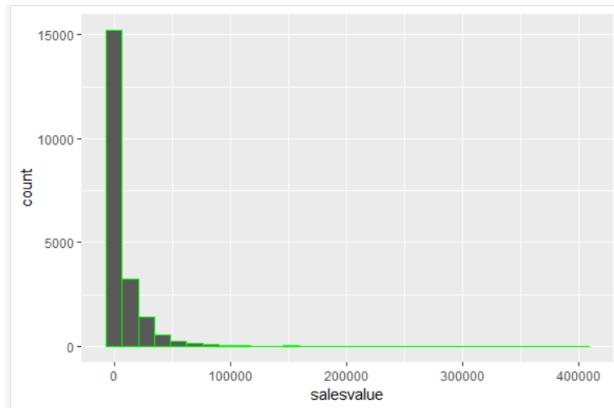
Descriptive Statistics

---

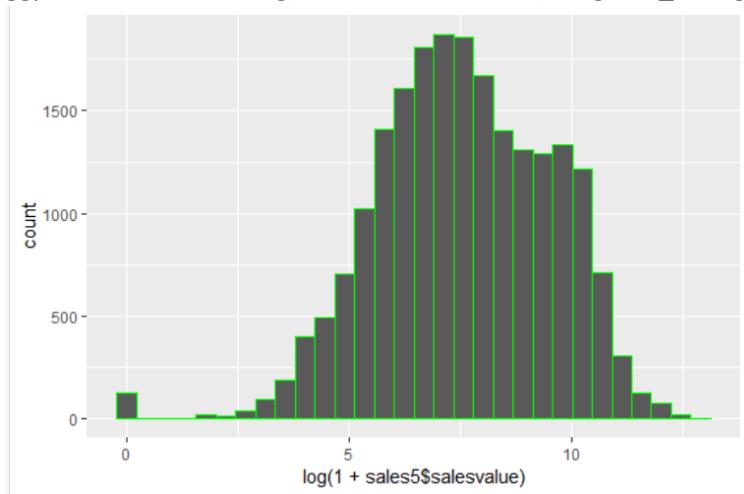
| Statistic        | N      | Mean    | St. Dev. | Min   | Pctl(25) | Median  | Pctl(75) | Max       |
|------------------|--------|---------|----------|-------|----------|---------|----------|-----------|
| store_number     | 21,115 | 1,286.5 | 2,458.6  | 2     | 2        | 6       | 6        | 5,998     |
| year             | 21,115 | 2,011.2 | 0.7      | 2,010 | 2,011    | 2,011   | 2,012    | 2,012     |
| month_index      | 21,115 | 25.7    | 7.3      | 13    | 19       | 26      | 32       | 38        |
| product_category | 21,115 | 9.4     | 6.3      | 1     | 4        | 7       | 13       | 21        |
| month_dummy      | 21,115 | 6.7     | 3.5      | 1     | 4        | 7       | 9        | 12        |
| bops_in_effect   | 21,115 | 0.4     | 0.5      | 0     | 0        | 0       | 1        | 1         |
| day              | 21,115 | 401.8   | 223.4    | 1     | 205      | 409     | 591      | 788       |
| salesvalue       | 21,115 | 8,722.2 | 19,132.2 | 0.0   | 508.7    | 1,856.6 | 8,526.0  | 402,473.4 |
| returnvalue      | 21,115 | 1,373.6 | 2,992.2  | 0.0   | 0.0      | 193.8   | 1,376.5  | 51,973.1  |
| salesquantity    | 21,115 | 49.9    | 139.6    | 1     | 2        | 9       | 32       | 4,474     |
| returnquantity   | 21,115 | 5.3     | 12.5     | 0     | 0        | 1       | 5        | 380       |
| avg_female       | 21,115 | 0.5     | 0.3      | 0.0   | 0.4      | 0.5     | 0.6      | 1.0       |
| avg_age          | 21,115 | 5.0     | 1.9      | 0.0   | 4.4      | 5.0     | 5.7      | 13.0      |
| avg_income       | 21,115 | 5.3     | 1.1      | 1.0   | 5.0      | 5.3     | 5.7      | 9.0       |
| avg_homeowner    | 21,115 | 0.6     | 0.2      | 0.0   | 0.6      | 0.6     | 0.7      | 1.0       |
| avg_residency    | 21,115 | 6.9     | 2.5      | 0.0   | 6.0      | 6.9     | 7.5      | 15.0      |
| avg_chldowner    | 21,115 | 0.4     | 0.2      | 0.0   | 0.3      | 0.4     | 0.4      | 1.0       |
| BIE_timeline_PC  | 21,115 | 0.6     | 0.5      | 0     | 0        | 1       | 1        | 1         |
| group_store_PC   | 21,115 | 0.8     | 0.4      | 0     | 1        | 1       | 1        | 1         |

#Generate plot for Sales Value

```
ggplot(sales5, aes(x=salesvalue)) + geom_histogram(colour="green", bins =30)
```

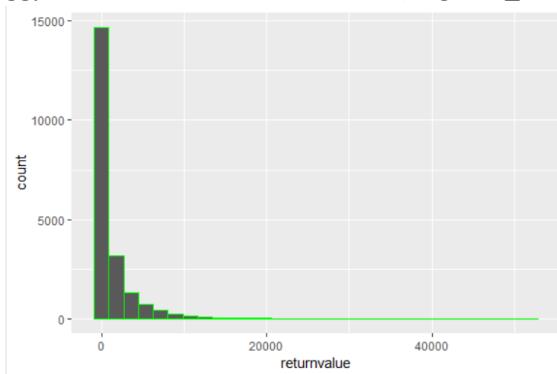


```
ggplot(sales5, aes(x=log(1+sales5$salesvalue))) + geom_histogram(colour="green", bins =30)
```

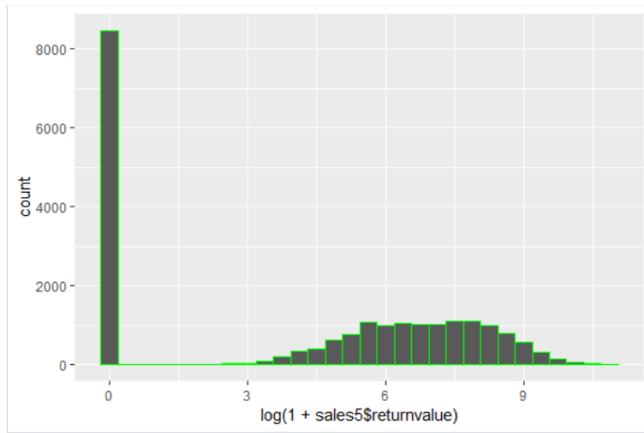


#Generate plot for Return Value

```
ggplot(sales5, aes(x=returnvalue)) + geom_histogram(colour="green", bins =30)
```



```
ggplot(sales5, aes(x=log(1+sales5$returnvalue))) + geom_histogram(colour="green", bins =30)
```



#####=====IMPACT ON SALES QUANTITY=====#####

```
#Count Data model approach for sales quantity
```

```
#Poisson Model
```

```
poisson5 <-
glm(salesquantity~BIE_timeline_PC*group_store_PC+factor_PC+avg_female+avg_age+avg_income+avg
_homeowner+avg_childdowner+factor_Month, family="poisson", data=sales5)
stargazer(poisson5,
 title="Poisson Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Poisson Results |                          |                                   |
|-----------------|--------------------------|-----------------------------------|
|                 | Dependent variable:      |                                   |
|                 | -----                    |                                   |
|                 | salesquantity<br>Model-1 |                                   |
| BIE_timeline_PC | 0.40***<br>(0.01)        | factor_PC10<br>-2.63***<br>(0.07) |
| group_store_PC  | 2.75***<br>(0.01)        | factor_PC11<br>0.38***<br>(0.01)  |
| factor_PC2      | 0.84***<br>(0.01)        | factor_PC12<br>2.29***<br>(0.01)  |
| factor_PC3      | -0.20***<br>(0.01)       | factor_PC13<br>0.23***<br>(0.01)  |
| factor_PC4      | 1.78***<br>(0.01)        | factor_PC14<br>0.05***<br>(0.01)  |
| factor_PC5      | 2.13***<br>(0.01)        | factor_PC15<br>-3.19***<br>(0.18) |
| factor_PC6      | 0.23***<br>(0.01)        | factor_PC17<br>-1.30***<br>(0.02) |
| factor_PC7      | 1.05***<br>(0.01)        | factor_PC20<br>-0.02*<br>(0.01)   |
| factor_PC8      | -1.95***<br>(0.03)       | factor_PC21<br>2.12***<br>(0.01)  |
| factor_PC9      | 0.90***<br>(0.01)        | avg_female<br>-0.37***<br>(0.005) |
|                 |                          | avg_age<br>-0.09***<br>(0.001)    |
|                 |                          | avg_income<br>0.14***<br>(0.001)  |

|                |                    |                                |                               |
|----------------|--------------------|--------------------------------|-------------------------------|
| avg_homeowner  | -0.27***<br>(0.01) | factor_Month9                  | -0.12***<br>(0.01)            |
| avg_childowner | 0.001<br>(0.01)    | factor_Month10                 | -0.10***<br>(0.01)            |
| factor_Month2  | 0.44***<br>(0.005) | factor_Month11                 | 0.44***<br>(0.005)            |
| factor_Month3  | -0.22***<br>(0.01) | factor_Month12                 | 1.20***<br>(0.004)            |
| factor_Month4  | -0.18***<br>(0.01) | BIE_timeline_PC:group_store_PC | -0.38***<br>(0.01)            |
| factor_Month5  | 0.21***<br>(0.01)  | Constant                       | -0.02<br>(0.01)               |
| factor_Month6  | -0.26***<br>(0.01) | <hr/>                          |                               |
| factor_Month7  | -0.30***<br>(0.01) | Observations                   | 21,115                        |
| factor_Month8  | -0.16***<br>(0.01) | Log Likelihood                 | -804,460.10                   |
|                |                    | Akaike Inf. Crit.              | 1,608,994.00                  |
|                |                    | Note:                          | *p<0.05; **p<0.01; ***p<0.001 |
|                |                    | >                              |                               |

### #Model fit assessment

```
poisson5a <- glm(salesquantity~1, data=sales5, family="poisson") #running a comparison with null model.
```

lrtest(poisson5, poisson5a) # We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

#### Likelihood ratio test

```
Model 1: salesquantity ~ BIE_timeline_PC * group_store_PC + factor_PC +
 avg_female + avg_age + avg_income + avg_homeowner + avg_childowner +
 factor_Month
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 37 -804460
2 1 -1524545 -36 1440171 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#Since Poisson doesn't fit the data, we will check for negative binomial model.

#### #Negative Binomial Model

```
negbin5 <-
glm.nb(salesquantity~BIE_timeline_PC*group_store_PC+factor_PC+avg_female+avg_age+avg_income+
avg_homeowner+avg_childowner+factor_Month, data = sales5)
```

```
stargazer(negbin5,
 apply.coef = exp, t.auto=F, p.auto = F,
 title="Negative Binomial Results", type="text",
 column.labels=c("IRRs"),
 df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

| Negative Binomial Results |                        |                                   |
|---------------------------|------------------------|-----------------------------------|
|                           |                        | Dependent variable:               |
|                           |                        | salesquantity<br>IRRs             |
| BIE_timeline_PC           | 1.3906***<br>(0.0403)  | factor_PC10 0.0883***<br>(0.1301) |
| group_store_PC            | 12.4154***<br>(0.0354) | factor_PC11 1.3540***<br>(0.0460) |
| factor_PC2                | 2.0824***<br>(0.0457)  | factor_PC12 7.4624***<br>(0.0435) |
| factor_PC3                | 0.8369***<br>(0.0468)  | factor_PC13 1.1304**<br>(0.0464)  |
| factor_PC4                | 4.8313***<br>(0.0429)  | factor_PC14 1.0746<br>(0.0502)    |
| factor_PC5                | 6.7282***<br>(0.0432)  | factor_PC15 0.0578***<br>(0.3028) |
| factor_PC6                | 1.1427**<br>(0.0460)   | factor_PC17 0.2922***<br>(0.0650) |
| factor_PC7                | 2.9223***<br>(0.0482)  | factor_PC20 1.0459<br>(0.0465)    |
| factor_PC8                | 0.1696***<br>(0.0808)  | factor_PC21 6.3250***<br>(0.0433) |
| factor_PC9                | 3.5301***<br>(0.0621)  | avg_female 0.8112***<br>(0.0354)  |
|                           |                        | avg_age 0.8760***<br>(0.0047)     |
|                           |                        | avg_income 1.2317***<br>(0.0085)  |

|                |                       |                                                      |
|----------------|-----------------------|------------------------------------------------------|
| avg_homeowner  | 0.6094***<br>(0.0413) | factor_Month9 0.9153*<br>(0.0396)                    |
| avg_childowner | 1.0441<br>(0.0386)    | factor_Month10 0.9519<br>(0.0429)                    |
| factor_Month2  | 1.5271***<br>(0.0411) | factor_Month11 1.5923***<br>(0.0409)                 |
| factor_Month3  | 0.8808**<br>(0.0420)  | factor_Month12 2.9406***<br>(0.0393)                 |
| factor_Month4  | 0.8882**<br>(0.0424)  | BIE_timeline_PC:group_store_PC 0.6834***<br>(0.0441) |
| factor_Month5  | 1.2753***<br>(0.0411) | Constant 1.2416**<br>(0.0701)                        |
| factor_Month6  | 0.8487***<br>(0.0427) | -----                                                |
| factor_Month7  | 0.8195***<br>(0.0422) | Observations 21,115                                  |
| factor_Month8  | 0.9268*<br>(0.0386)   | Log Likelihood -87,498.7200                          |
|                |                       | theta 0.7400*** (0.0066)                             |
|                |                       | Akaike Inf. Crit. 175,071.4000                       |
|                |                       | =====                                                |
|                |                       | Note: *p<0.05; **p<0.01; ***p<0.001                  |
|                |                       | >                                                    |

### #Model fit assessment

```
negbin5a <- glm.nb(salesquantity~1, data=sales5) #running a comparison with null model.
```

```
lrtest(negbin5, negbin5a) # We conclude that the model fit because the goodness-of-fit chi-squared test
is statistically significant.
```

### Likelihood ratio test

```

Model 1: salesquantity ~ BIE_timeline_PC * group_store_PC + factor_PC +
 avg_female + avg_age + avg_income + avg_homeowner + avg_childowner +
 factor_Month
Model 2: salesquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 38 -87498
2 2 -96093 -36 17190 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

### # Check for heteroskedasticity

```

gqtest(negbin5) # Goldfeld-Quandt test indicates no heteroskedasticity
bptest(negbin5) # Breusch-Pagan test indicates heteroskedasticity

```

```

> gqtest(negbin5) # Goldfeld-Quandt test indicates no heteroskedasticity
 Goldfeld-Quandt test
 data: negbin5
 GQ = 0.0083442, df1 = 10521, df2 = 10520, p-value = 1
 alternative hypothesis: variance increases from segment 1 to 2
> bptest(negbin5) # Breusch-Pagan test indicates heteroskedasticity
 studentized Breusch-Pagan test
 data: negbin5
 BP = 650.41, df = 36, p-value < 2.2e-16

```

### # Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.

```

HWrobstdter <- sqrt(diag(vcovHC(negbin5, type="HC1"))) # produces Huber-White robust standard
errors

```

#### Values

|  | HWrobstdter | Named num [1:37] 0.0733 0.0364 0.0344 0.044 0.0392... |
|--|-------------|-------------------------------------------------------|
|--|-------------|-------------------------------------------------------|

```

stargazer(negbin5, negbin5,
 apply.coef = exp, t.auto=F, p.auto = F,
 se=list(NULL, HWrobstdter),
 title="Negative Binomial Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))

```

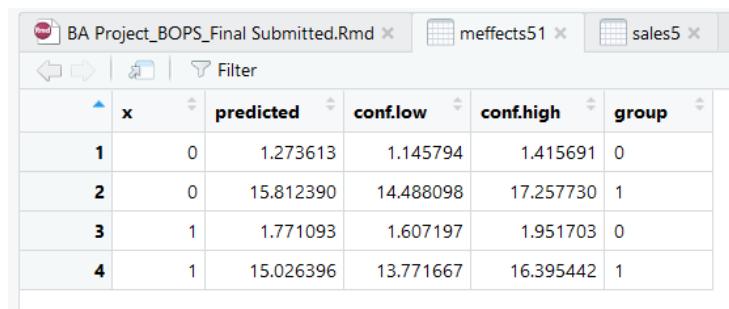
| Negative Binomial Results |  |                      |                      | factor_PC10                    | 0.088***<br>(0.130)           | 0.088***<br>(0.089) |
|---------------------------|--|----------------------|----------------------|--------------------------------|-------------------------------|---------------------|
|                           |  | Dependent variable:  |                      | factor_PC11                    | 1.354***<br>(0.046)           | 1.354***<br>(0.048) |
|                           |  | salesquantity        |                      | factor_PC12                    | 7.462***<br>(0.043)           | 7.462***<br>(0.042) |
|                           |  | Normal SE<br>(1)     | HW-Robust SE<br>(2)  | factor_PC13                    | 1.130**<br>(0.046)            | 1.130**<br>(0.044)  |
| BIE_timeline_PC           |  | 1.391***<br>(0.040)  | 1.391***<br>(0.036)  | factor_PC14                    | 1.075<br>(0.050)              | 1.075<br>(0.049)    |
| group_store_PC            |  | 12.415***<br>(0.035) | 12.415***<br>(0.034) | factor_PC15                    | 0.058***<br>(0.303)           | 0.058***<br>(0.173) |
| factor_PC2                |  | 2.082***<br>(0.046)  | 2.082***<br>(0.044)  | factor_PC17                    | 0.292***<br>(0.065)           | 0.292***<br>(0.045) |
| factor_PC3                |  | 0.837***<br>(0.047)  | 0.837***<br>(0.039)  | factor_PC20                    | 1.046<br>(0.047)              | 1.046<br>(0.040)    |
| factor_PC4                |  | 4.831***<br>(0.043)  | 4.831***<br>(0.041)  | factor_PC21                    | 6.325***<br>(0.043)           | 6.325***<br>(0.041) |
| factor_PC5                |  | 6.728***<br>(0.043)  | 6.728***<br>(0.043)  | avg_female                     | 0.811***<br>(0.035)           | 0.811***<br>(0.034) |
| factor_PC6                |  | 1.143**<br>(0.046)   | 1.143**<br>(0.041)   | avg_age                        | 0.876***<br>(0.005)           | 0.876***<br>(0.004) |
| factor_PC7                |  | 2.922***<br>(0.048)  | 2.922***<br>(0.103)  | avg_income                     | 1.232***<br>(0.008)           | 1.232***<br>(0.008) |
| factor_PC8                |  | 0.170***<br>(0.081)  | 0.170***<br>(0.060)  | avg_homeowner                  | 0.609***<br>(0.041)           | 0.609***<br>(0.033) |
| factor_PC9                |  | 3.530***<br>(0.062)  | 3.530***<br>(0.077)  |                                |                               |                     |
| avg_childowner            |  | 1.044<br>(0.039)     | 1.044<br>(0.031)     | factor_Month8                  | 0.927*<br>(0.039)             | 0.927*<br>(0.048)   |
| factor_Month2             |  | 1.527***<br>(0.041)  | 1.527***<br>(0.049)  | factor_Month9                  | 0.915*<br>(0.040)             | 0.915*<br>(0.040)   |
| factor_Month3             |  | 0.881**<br>(0.042)   | 0.881**<br>(0.043)   | factor_Month10                 | 0.952<br>(0.043)              | 0.952<br>(0.047)    |
| factor_Month4             |  | 0.888**<br>(0.042)   | 0.888**<br>(0.046)   | factor_Month11                 | 1.592***<br>(0.041)           | 1.592***<br>(0.047) |
| factor_Month5             |  | 1.275***<br>(0.041)  | 1.275***<br>(0.047)  | factor_Month12                 | 2.941***<br>(0.039)           | 2.941***<br>(0.048) |
| factor_Month6             |  | 0.849***<br>(0.043)  | 0.849***<br>(0.042)  | BIE_timeline_PC:group_store_PC | 0.683***<br>(0.044)           | 0.683***<br>(0.043) |
| factor_Month7             |  | 0.820***<br>(0.042)  | 0.820***<br>(0.041)  | Constant                       | 1.242**<br>(0.070)            | 1.242**<br>(0.073)  |
|                           |  |                      |                      | Observations                   | 21,115                        | 21,115              |
|                           |  |                      |                      | Log Likelihood                 | -87,498.720                   | -87,498.720         |
|                           |  |                      |                      | theta                          | 0.740***<br>(0.007)           | 0.740***<br>(0.007) |
|                           |  |                      |                      | Akaike Inf. Crit.              | 175,071.400                   | 175,071.400         |
|                           |  |                      |                      | Note:                          | *p<0.05; **p<0.01; ***p<0.001 |                     |

## # Visualize the output

meffects51 &lt;- ggpredict(negbin5, terms=c("BIE\_timeline\_PC", "group\_store\_PC"))

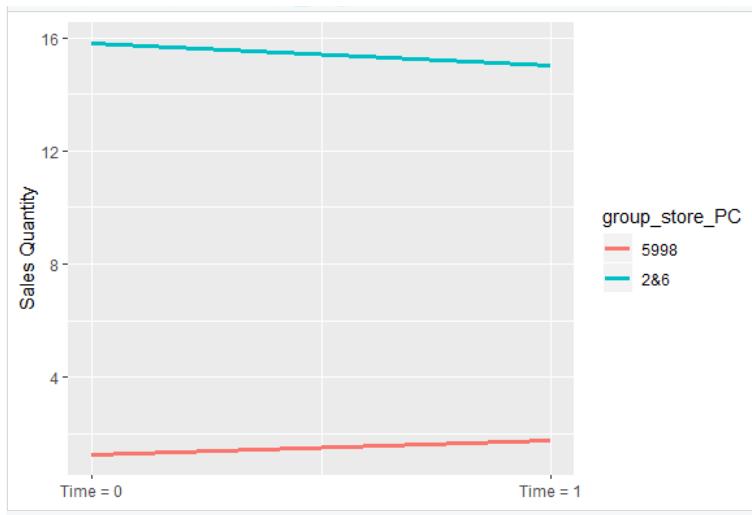
# generates a tidy data frame at two different values of BIE\_timeline - before and after BOPS

implementation.



```
ggplot(meffects51,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline_PC") + ylab("Sales Quantity") +
 labs(colour="group_store_PC") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time = 0", "Time = 1")) +
 theme(axis.title.x=element_blank())
```

## The interaction coefficient of BIE\_timeline\_PC:group\_store\_PC is significant with IRR value 0.6834.  
This means that BOPS implementation is associated with 31.66% decrease in product-level sales quantity.



#### #####=====IMPACT ON SALES VALUE=====#####

#Since sales value is a dollar value, we will use a linear interaction model with log transformed dependent variable.

```
sales5$log_salesvalue <- log(1+sales5$salesvalue)
```

|    | avg_homeowner | avg_residency | avg_childdowner | BIE_timeline_PC | group_store_PC | factor_PC | factor_Month | log_salesvalue |
|----|---------------|---------------|-----------------|-----------------|----------------|-----------|--------------|----------------|
| 94 | 0.6296296     | 7.037037      | 0.36363637      | 1               | 1              | 5         | 3            | 10.575784      |
| 00 | 1.0000000     | 4.000000      | 0.00000000      | 0               | 1              | 4         | 8            | 5.309158       |
| 71 | 0.8571429     | 8.428572      | 0.28571430      | 0               | 1              | 5         | 8            | 6.730517       |
| 00 | 0.5000000     | 10.000000     | 0.00000000      | 0               | 1              | 13        | 8            | 5.319492       |
| 00 | 0.0000000     | 8.000000      | 1.00000000      | 0               | 1              | 2         | 8            | 3.911823       |

Showing 1 to 6 of 21,115 entries

#OLS model approach for sales quantity

```
ols51 =
lm(log_salesvalue~BIE_timeline_PC*group_store_PC+factor_PC+avg_female+avg_age+avg_income+avg_homeowner+avg_childdowner+factor_Month, data=sales5)
stargazer(ols51,
```

```
title="Regression Results", type="text",
column.labels=c("Model-1"),
df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

```
Check for heteroskedasticity
gqtest(ols51) # Goldfeld-Quandt test indicates no heteroskedasticity
bpptest(ols51) # Breusch-Pagan test indicates heteroskedasticity
```

```
Goldfeld-Quandt test

data: ols51
GQ = 0.44738, df1 = 10521, df2 = 10520, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2

> bpptest(ols51) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

data: ols51
BP = 1022.8, df = 36, p-value < 2.2e-16
```

# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.

```
HWrobstdter <- sqrt(diag(vcovHC(ols51, type="HC1"))) # produces Huber-White robust standard errors
```

| Values | HWrobstdter | Named num [1:37] | 0.103 | 0.033 | 0.0321 | 0.0612 | 0.059 | ... | v |
|--------|-------------|------------------|-------|-------|--------|--------|-------|-----|---|
|        |             |                  |       |       |        |        |       |     |   |

```
stargazer(ols51, ols51,
se=list(NULL, HWrobstdter),
title="Negative Binomial Results", type="text",
column.labels=c("Normal SE", "HW-Robust SE"),
df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| Negative Binomial Results |                      |                      |              |             |                      |                      |
|---------------------------|----------------------|----------------------|--------------|-------------|----------------------|----------------------|
|                           |                      | Dependent variable:  |              |             |                      |                      |
|                           |                      | log_salesvalue       |              |             |                      |                      |
|                           |                      | Normal SE            | HW-Robust SE |             |                      |                      |
|                           |                      | (1)                  | (2)          |             |                      |                      |
| BIE_timeline_PC           | 0.265***<br>(0.051)  | 0.265***<br>(0.033)  |              | factor_PC9  | -2.755***<br>(0.084) | -2.755***<br>(0.098) |
| group_store_PC            | 1.565***<br>(0.045)  | 1.565***<br>(0.032)  |              | factor_PC10 | -2.897***<br>(0.151) | -2.897***<br>(0.122) |
| factor_PC2                | -1.197***<br>(0.061) | -1.197***<br>(0.061) |              | factor_PC11 | -0.829***<br>(0.061) | -0.829***<br>(0.061) |
| factor_PC3                | -0.231***<br>(0.062) | -0.231***<br>(0.059) |              | factor_PC12 | -0.309***<br>(0.058) | -0.309***<br>(0.060) |
| factor_PC4                | 0.132*<br>(0.057)    | 0.132*<br>(0.058)    |              | factor_PC13 | -1.240***<br>(0.061) | -1.240***<br>(0.058) |
| factor_PC5                | -0.332***<br>(0.058) | -0.332***<br>(0.059) |              | factor_PC14 | -2.542***<br>(0.067) | -2.542***<br>(0.074) |
| factor_PC6                | -1.126***<br>(0.061) | -1.126***<br>(0.059) |              | factor_PC15 | -3.576***<br>(0.325) | -3.576***<br>(0.321) |
| factor_PC7                | -2.832***<br>(0.064) | -2.832***<br>(0.062) |              | factor_PC17 | 0.267**<br>(0.085)   | 0.267***<br>(0.065)  |
| factor_PC8                | -2.090***<br>(0.100) | -2.090***<br>(0.088) |              | factor_PC20 | -0.693***<br>(0.061) | -0.693***<br>(0.058) |
|                           |                      |                      |              | factor_PC21 | -0.602***<br>(0.058) | -0.602***<br>(0.059) |
|                           |                      |                      |              | avg_female  | -0.364***<br>(0.047) | -0.364***<br>(0.062) |
|                           |                      |                      |              | avg_age     | -0.061***<br>(0.006) | -0.061***<br>(0.008) |

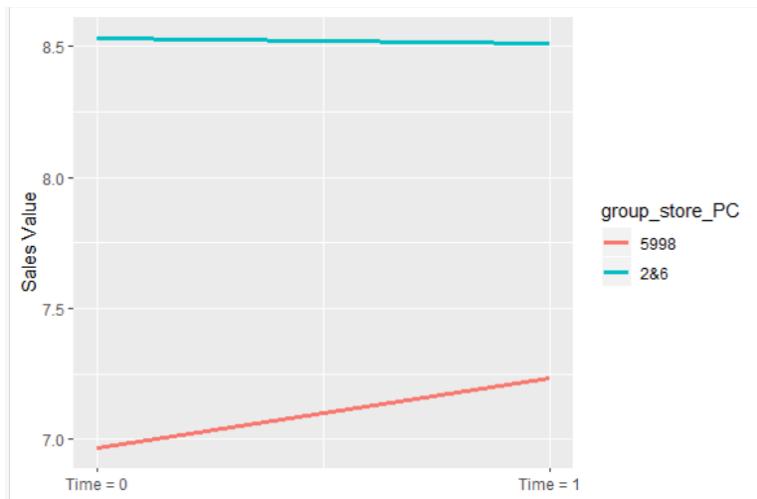
|                |                      |                     |                                |                               |                      |
|----------------|----------------------|---------------------|--------------------------------|-------------------------------|----------------------|
| avg_income     | 0.107***<br>(0.011)  | 0.107***<br>(0.015) | factor_Month11                 | 0.413***<br>(0.055)           | 0.413***<br>(0.058)  |
| avg_homeowner  | -0.200***<br>(0.055) | -0.200**<br>(0.076) | factor_Month12                 | 1.003***<br>(0.053)           | 1.003***<br>(0.056)  |
| avg_childowner | 0.076<br>(0.052)     | 0.076<br>(0.071)    | BIE_timeline_PC:group_store_PC | -0.288***<br>(0.056)          | -0.288***<br>(0.042) |
| factor_Month2  | 0.415***<br>(0.055)  | 0.415***<br>(0.058) | Constant                       | 6.996***<br>(0.092)           | 6.996***<br>(0.103)  |
| factor_Month3  | 0.045<br>(0.056)     | 0.045<br>(0.060)    | Observations                   | 21,115                        | 21,115               |
| factor_Month4  | 0.012<br>(0.057)     | 0.012<br>(0.059)    | R2                             | 0.323                         | 0.323                |
| factor_Month5  | 0.230***<br>(0.055)  | 0.230***<br>(0.059) | Adjusted R2                    | 0.322                         | 0.322                |
| factor_Month6  | -0.0001<br>(0.057)   | -0.0001<br>(0.057)  | Residual Std. Error            | 1.607                         | 1.607                |
| factor_Month7  | -0.003<br>(0.056)    | -0.003<br>(0.058)   | F Statistic                    | 279.284***                    | 279.284***           |
| factor_Month8  | 0.008<br>(0.052)     | 0.008<br>(0.054)    | Note:                          | =====                         |                      |
| factor_Month9  | 0.068<br>(0.053)     | 0.068<br>(0.055)    | >                              | *p<0.05; **p<0.01; ***p<0.001 |                      |
| factor_Month10 | 0.006<br>(0.057)     | 0.006<br>(0.061)    |                                |                               |                      |

```
meffects52 <- ggpredict(ols51, terms=c("BIE_timeline_PC", "group_store_PC"))
generates a tidy data frame
```

|   | x | predicted | conf.low | conf.high | group |
|---|---|-----------|----------|-----------|-------|
| 1 | 0 | 6.967346  | 6.830327 | 7.104365  | 0     |
| 2 | 0 | 8.532798  | 8.416403 | 8.649192  | 1     |
| 3 | 1 | 7.232166  | 7.104944 | 7.359389  | 0     |
| 4 | 1 | 8.509448  | 8.393477 | 8.625419  | 1     |

# Visualize the output

```
ggplot(meffects52,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline_PC") + ylab("Sales Value") +
 labs(colour="group_store_PC") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time = 0", "Time = 1")) +
 theme(axis.title.x=element_blank())
```



## The interaction coefficient of BIE\_timeline\_PC:group\_store\_PC is significant with value -0.288 . This means that BOPS implementation is associated with 28.8% decrease in product-level sales value.

#### #####=====IMPACT ON RETURN QUANTITY=====#####

```
#Count Data model approach for return quantity
#Poisson Model
poisson52 <-
glm(returnquantity~BIE_timeline_PC*group_store_PC+factor_PC+salesquantity+avg_female+avg_age+a
vg_income+factor_Month, family="poisson", data=sales5)
stargazer(poisson52,
 title="Poisson Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

| Poisson Results |                    |                                |                               |
|-----------------|--------------------|--------------------------------|-------------------------------|
|                 |                    | Dependent variable:            |                               |
|                 |                    | returnquantity<br>Model-1      |                               |
| BIE_timeline_PC | 0.52***<br>(0.05)  | factor_PC10                    | -2.25***<br>(0.14)            |
| group_store_PC  | 2.68***<br>(0.04)  | factor_PC11                    | -0.12***<br>(0.02)            |
| factor_PC2      | 0.65***<br>(0.02)  | factor_PC12                    | 0.94***<br>(0.02)             |
| factor_PC3      | -0.26***<br>(0.02) | factor_PC13                    | -0.40***<br>(0.02)            |
| factor_PC4      | 1.07***<br>(0.02)  | factor_PC14                    | -0.52***<br>(0.03)            |
| factor_PC5      | 0.93***<br>(0.02)  | factor_PC15                    | -3.03***<br>(0.50)            |
| factor_PC6      | -0.02<br>(0.02)    | factor_PC17                    | -1.23***<br>(0.05)            |
| factor_PC7      | -2.30***<br>(0.04) | factor_PC20                    | 0.06**<br>(0.02)              |
| factor_PC8      | -1.63***<br>(0.07) | factor_PC21                    | 0.82***<br>(0.02)             |
| factor_PC9      | -0.36***<br>(0.03) | salesquantity                  | 0.002***<br>(0.0000)          |
| avg_income      | 0.09***<br>(0.004) | avg_female                     | -0.17***<br>(0.02)            |
| factor_Month2   | 0.04**<br>(0.01)   | avg_age                        | -0.09***<br>(0.002)           |
| factor_Month3   | -0.27***<br>(0.02) | factor_Month9                  | -0.38***<br>(0.02)            |
| factor_Month4   | -0.33***<br>(0.02) | factor_Month10                 | -0.25***<br>(0.02)            |
| factor_Month5   | -0.15***<br>(0.02) | factor_Month11                 | 0.07***<br>(0.01)             |
| factor_Month6   | -0.23***<br>(0.02) | factor_Month12                 | -0.03*<br>(0.01)              |
| factor_Month7   | -0.20***<br>(0.02) | BIE_timeline_PC:group_store_PC | -0.53***<br>(0.05)            |
| factor_Month8   | -0.34***<br>(0.01) | Constant                       | -1.24***<br>(0.05)            |
|                 |                    | Observations                   | 21,115                        |
|                 |                    | Log Likelihood                 | -81,838.35                    |
|                 |                    | Akaike Inf. Crit.              | 163,748.70                    |
|                 |                    | Note:                          | *p<0.05; **p<0.01; ***p<0.001 |
|                 |                    | >                              |                               |

## ## Model fit assessment

```
poisson52a <- glm(returnquantity~1, data=sales5, family="poisson") # running a comparison with null model.
```

`lrtest(poisson52, poisson52a)` # We conclude that the model does not fit because the goodness-of-fit chi-squared test is statistically significant. If the test had not been statistically significant, it would indicate that the data fit the model well.

## Likelihood ratio test

```

Model 1: returnquantity ~ BIE_timeline_PC * group_store_PC + factor_PC +
 salesquantity + avg_female + avg_age + avg_income + factor_Month
Model 2: returnquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 36 -81838
2 1 -165851 -35 168025 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

##Since Poisson doesn't fit the data, we will check for negative binomial model.

### #Negative Binomial Model

```

negbin53<-
glm.nb(returnquantity~BIE_timeline_PC*group_store_PC+factor_PC+salesquantity+avg_female+avg_ag
e+avg_income+factor_Month, data = sales5)
stargazer(negbin53,
apply.coef = exp, t.auto=F, p.auto = F,
title="Negative Binomial Results", type="text",
column.labels=c("IRRs"),
df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))

```

| Negative Binomial Results |                        |
|---------------------------|------------------------|
|                           | Dependent variable:    |
|                           | returnquantity<br>IRRs |
| BIE_timeline_PC           | 1.5183***<br>(0.0583)  |
| group_store_PC            | 6.0839***<br>(0.0511)  |
| factor_PC2                | 1.2790***<br>(0.0470)  |
| factor_PC3                | 0.8321***<br>(0.0491)  |
| factor_PC4                | 1.2268***<br>(0.0446)  |
| factor_PC5                | 0.8908*<br>(0.0460)    |
| factor_PC6                | 0.8770**<br>(0.0483)   |
| factor_PC7                | 0.1834***<br>(0.0657)  |
| factor_PC8                | 0.2515***<br>(0.0968)  |
| factor_PC9                | 0.4081***<br>(0.0736)  |
| factor_PC10               | 0.1385***<br>(0.1713)  |
| factor_PC11               | 0.6914***<br>(0.0495)  |
| factor_PC12               | 0.9064*<br>(0.0465)    |
| factor_PC13               | 0.5762***<br>(0.0507)  |
| factor_PC14               | 0.5587***<br>(0.0547)  |
| factor_PC15               | 0.0575***<br>(0.5610)  |
| factor_PC17               | 0.3962***<br>(0.0728)  |
| factor_PC20               | 1.0473<br>(0.0483)     |
| factor_PC21               | 0.8070***<br>(0.0462)  |
| salesquantity             | 1.0085***<br>(0.0001)  |
| avg_female                | 1.0975*<br>(0.0393)    |

|               |                       |                                |                               |
|---------------|-----------------------|--------------------------------|-------------------------------|
| avg_age       | 0.9169***<br>(0.0052) | factor_Month9                  | 0.7815***<br>(0.0430)         |
| avg_income    | 1.0863***<br>(0.0090) | factor_Month10                 | 0.8517***<br>(0.0460)         |
| factor_Month2 | 0.9092*<br>(0.0446)   | factor_Month11                 | 0.9205<br>(0.0444)            |
| factor_Month3 | 0.8832**<br>(0.0454)  | factor_Month12                 | 1.0723<br>(0.0429)            |
| factor_Month4 | 0.7917***<br>(0.0463) | BIE_timeline_PC:group_store_PC | 0.6151***<br>(0.0612)         |
| factor_Month5 | 0.8488***<br>(0.0449) | Constant                       | 0.4683***<br>(0.0824)         |
| factor_Month6 | 0.8388***<br>(0.0466) | <hr/>                          |                               |
| factor_Month7 | 0.9131*<br>(0.0456)   | Observations                   | 21,115                        |
| factor_Month8 | 0.8219***<br>(0.0417) | Log Likelihood                 | -43,322.6100                  |
|               |                       | theta                          | 0.9046*** (0.0139)            |
|               |                       | Akaike Inf. Crit.              | 86,717.2200                   |
|               |                       | Note:                          | *p<0.05; **p<0.01; ***p<0.001 |
|               |                       |                                |                               |

```
negbin53a <- glm.nb(returnquantity~1, data=sales5)
#running a comparison with null model.
```

lrtest(negbin53, negbin53a) # We conclude that the model fits well.

Likelihood ratio test

```
Model 1: returnquantity ~ BIE_timeline_PC * group_store_PC + factor_PC +
salesquantity + avg_female + avg_age + avg_income + factor_Month
Model 2: returnquantity ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 37 -43322
2 2 -51169 -35 15694 < 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

# Check for heteroskedasticity

gqttest(negbin53) # Goldfeld-Quandt test indicates no heteroskedasticity

bptest(negbin53) # Breusch-Pagan test indicates heteroskedasticity

> gqttest(negbin53) # Goldfeld-Quandt test indicates no heteroskedasticity

Goldfeld-Quandt test

```
data: negbin53
GQ = 0.021027, df1 = 10522, df2 = 10521, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2
```

> bptest(negbin53) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

```
data: negbin53
BP = 807.5, df = 35, p-value < 2.2e-16
```

# Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.

```
HWrobstdер <- sqrt(diag(vcovHC(negbin53, type="HC1"))) # produces Huber-White robust standard errors
```

### Values

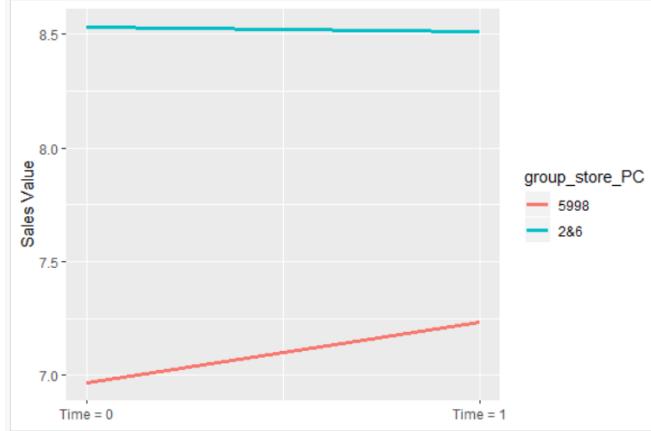
|            |                                                       |
|------------|-------------------------------------------------------|
| HWrobstdер | Named num [1:36] 0.074 0.059 0.0496 0.0418 0.0437 ... |
|------------|-------------------------------------------------------|

```
stargazer(negbin53, negbin53,
 apply.coef = exp, t.auto=F, p.auto = F,
 se=list(NULL, HWrobstdер),
 title="Negative Binomial Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

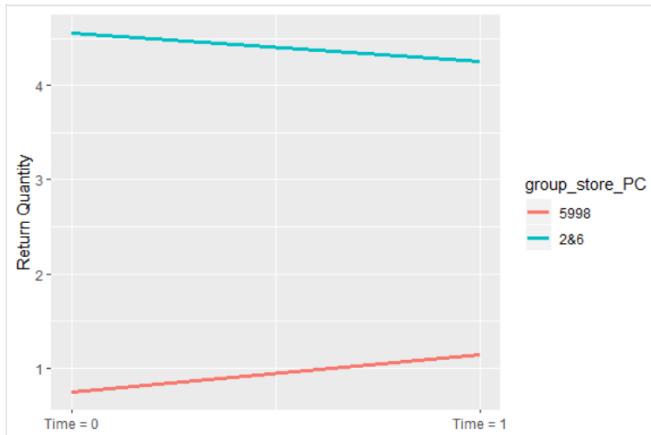
| Negative Binomial Results |                     |                     |                     | factor_PC9                     | 0.408***<br>(0.074)           | 0.408***<br>(0.098)  |
|---------------------------|---------------------|---------------------|---------------------|--------------------------------|-------------------------------|----------------------|
|                           |                     | Dependent variable: |                     | factor_PC10                    | 0.139***<br>(0.171)           | 0.139***<br>(0.151)  |
|                           |                     | returnquantity      |                     | factor_PC11                    | 0.691***<br>(0.049)           | 0.691***<br>(0.045)  |
|                           |                     | Normal SE<br>(1)    | HW-Robust SE<br>(2) | factor_PC12                    | 0.906*<br>(0.046)             | 0.906*<br>(0.041)    |
| BIE_timeline_PC           | 1.518***<br>(0.058) | 1.518***<br>(0.059) |                     | factor_PC13                    | 0.576***<br>(0.051)           | 0.576***<br>(0.045)  |
| group_store_PC            | 6.084***<br>(0.051) | 6.084***<br>(0.050) |                     | factor_PC14                    | 0.559***<br>(0.055)           | 0.559***<br>(0.054)  |
| factor_PC2                | 1.279***<br>(0.047) | 1.279***<br>(0.042) |                     | factor_PC15                    | 0.057***<br>(0.561)           | 0.057***<br>(0.431)  |
| factor_PC3                | 0.832***<br>(0.049) | 0.832***<br>(0.044) |                     | factor_PC17                    | 0.396***<br>(0.073)           | 0.396***<br>(0.060)  |
| factor_PC4                | 1.227***<br>(0.045) | 1.227***<br>(0.039) |                     | factor_PC20                    | 1.047<br>(0.048)              | 1.047<br>(0.044)     |
| factor_PC5                | 0.891*<br>(0.046)   | 0.891*<br>(0.042)   |                     | factor_PC21                    | 0.807***<br>(0.046)           | 0.807***<br>(0.042)  |
| factor_PC6                | 0.877**<br>(0.048)  | 0.877**<br>(0.044)  |                     | salesquantity                  | 1.009***<br>(0.0001)          | 1.009***<br>(0.0001) |
| factor_PC7                | 0.183***<br>(0.066) | 0.183***<br>(0.074) |                     | avg_female                     | 1.098*<br>(0.039)             | 1.098*<br>(0.031)    |
| factor_PC8                | 0.251***<br>(0.097) | 0.251***<br>(0.083) |                     |                                |                               |                      |
| avg_age                   | 0.917***<br>(0.005) | 0.917***<br>(0.004) |                     | factor_Month9                  | 0.782***<br>(0.043)           | 0.782***<br>(0.037)  |
| avg_income                | 1.086***<br>(0.009) | 1.086***<br>(0.007) |                     | factor_Month10                 | 0.852***<br>(0.046)           | 0.852***<br>(0.040)  |
| factor_Month2             | 0.909*<br>(0.045)   | 0.909*<br>(0.039)   |                     | factor_Month11                 | 0.921<br>(0.044)              | 0.921<br>(0.039)     |
| factor_Month3             | 0.883**<br>(0.045)  | 0.883**<br>(0.040)  |                     | factor_Month12                 | 1.072<br>(0.043)              | 1.072<br>(0.039)     |
| factor_Month4             | 0.792***<br>(0.046) | 0.792***<br>(0.040) |                     | BIE_timeline_PC:group_store_PC | 0.615***<br>(0.061)           | 0.615***<br>(0.062)  |
| factor_Month5             | 0.849***<br>(0.045) | 0.849***<br>(0.040) |                     | Constant                       | 0.468***<br>(0.082)           | 0.468***<br>(0.074)  |
| factor_Month6             | 0.839***<br>(0.047) | 0.839***<br>(0.047) |                     |                                |                               |                      |
| factor_Month7             | 0.913*<br>(0.046)   | 0.913*<br>(0.048)   |                     | Observations                   | 21,115                        | 21,115               |
| factor_Month8             | 0.822***<br>(0.042) | 0.822***<br>(0.038) |                     | Log Likelihood                 | -43,322.610                   | -43,322.610          |
|                           |                     |                     |                     | theta                          | 0.905***<br>(0.014)           | 0.905***<br>(0.014)  |
|                           |                     |                     |                     | Akaike Inf. crit.              | 86,717.220                    | 86,717.220           |
|                           |                     |                     |                     | Note:                          | *p<0.05; **p<0.01; ***p<0.001 |                      |

```
Visualize the output
```

```
meffects53 <- ggpredict(negbin53, terms=c("BIE_timeline_PC", "group_store_PC")) # generates a tidy
data frame at two different values of BIE_timeline - before and after BOPS implementation.
```



```
ggplot(meffects53,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline_PC") + ylab("Return Quantity") +
 labs(colour="group_store_PC") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time = 0", "Time = 1")) +
 theme(axis.title.x=element_blank())
```



## The interaction coefficient of BIE\_timeline\_PC:group\_store\_PC is significant with IRR value 0.615. This means that BOPS implementation is associated with 38.5% decrease in product-level return quantity.

#### #####=====IMPACT ON RETURN VALUE=====#####

#Since return value is a dollar value, we will use a linear interaction model with log transformed dependent variable.

```
sales5$log_returnvalue <- log(1+sales5$returnvalue)
```

|     | avg_residency | avg_childowner | BIE_timeline_PC | group_store_PC | factor_PC | factor_Month | log_salesvalue | log_returnvalue |
|-----|---------------|----------------|-----------------|----------------|-----------|--------------|----------------|-----------------|
| 296 | 7.037037      | 0.36363637     |                 | 1              | 1         | 5            | 3              | 10.575784       |
| 000 | 4.000000      | 0.00000000     |                 | 0              | 1         | 4            | 8              | 5.309158        |
| 429 | 8.428572      | 0.28571430     |                 | 0              | 1         | 5            | 8              | 6.730517        |
| 000 | 10.000000     | 0.00000000     |                 | 0              | 1         | 13           | 8              | 5.319492        |
| 000 | 8.000000      | 1.00000000     |                 | 0              | 1         | 2            | 8              | 3.911823        |
| 508 | 7.628415      | 0.39071038     |                 | 0              | 1         | 12           | 8              | 10.138572       |

Showing 1 to 7 of 21,115 entries

```
ols54 =
lm(log_returnvalue~BIE_timeline_PC*group_store_PC+log_salesvalue+factor_PC+avg_female+avg_age+
avg_income+factor_Month, data = sales5)
stargazer(ols54,
 title="Regression Results", type="text",
 column.labels=c("Model-1"),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

```
Check for heteroskedasticity
qqttest(ols54) # Goldfeld-Quandt test indicates no heteroskedasticity
bpptest(ols54) # Breusch-Pagan test indicates heteroskedasticity
> # Check for heteroskedasticity
> qqttest(ols54) # Goldfeld-Quandt test indicates no heteroskedasticity

Goldfeld-Quandt test

data: ols54
GQ = 1.6498, df1 = 10522, df2 = 10521, p-value < 2.2e-16
alternative hypothesis: variance increases from segment 1 to 2

> bpptest(ols54) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

data: ols54
BP = 3378.7, df = 35, p-value < 2.2e-16
```

```
Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
HWrobstderr <- sqrt(diag(vcovHC(ols54, type="HC1"))) # produces Huber-White robust standard errors
```

| Values      |                                                       |
|-------------|-------------------------------------------------------|
| HWrobstderr | Named num [1:36] 0.1636 0.0768 0.0698 0.0115 0.091... |

```
stargazer(ols54, ols54,
 se=list(NULL, HWrobstderr),
 title="Regression Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))
```

| Regression Results             |                      |                      |                      |
|--------------------------------|----------------------|----------------------|----------------------|
|                                |                      | Dependent variable:  |                      |
|                                |                      | log_returnvalue      |                      |
|                                |                      | Normal SE            | HW-Robust SE         |
|                                |                      | (1)                  | (2)                  |
| BIE_timeline_PC                | 0.236***<br>(0.070)  | 0.236**<br>(0.077)   |                      |
| group_store_PC                 | 1.271***<br>(0.064)  | 1.271***<br>(0.070)  |                      |
| log_salesvalue                 | 1.349***<br>(0.010)  | 1.349***<br>(0.011)  |                      |
| factor_PC2                     | 1.129***<br>(0.085)  | 1.129***<br>(0.091)  |                      |
| factor_PC3                     | 0.041<br>(0.085)     | 0.041<br>(0.103)     |                      |
| factor_PC4                     | 0.675***<br>(0.079)  | 0.675***<br>(0.088)  |                      |
| factor_PC5                     | 0.584***<br>(0.080)  | 0.584***<br>(0.087)  |                      |
| factor_PC6                     | 0.659***<br>(0.085)  | 0.659***<br>(0.095)  |                      |
| factor_PC7                     | 0.591***<br>(0.093)  | 0.591***<br>(0.099)  |                      |
| avg_female                     | 0.381***<br>(0.065)  | 0.381***<br>(0.075)  |                      |
| avg_age                        | -0.059***<br>(0.008) | -0.059***<br>(0.010) |                      |
| avg_income                     | 0.042**<br>(0.015)   | 0.042*<br>(0.017)    |                      |
| factor_Month2                  | -0.456***<br>(0.076) | -0.456***<br>(0.076) |                      |
| factor_Month3                  | -0.427***<br>(0.077) | -0.427***<br>(0.079) |                      |
| factor_Month4                  | -0.492***<br>(0.078) | -0.492***<br>(0.078) |                      |
| factor_Month5                  | -0.501***<br>(0.076) | -0.501***<br>(0.077) |                      |
| factor_Month6                  | -0.535***<br>(0.078) | -0.535***<br>(0.078) |                      |
| factor_Month7                  | -0.425***<br>(0.077) | -0.425***<br>(0.078) |                      |
| factor_Month8                  | -0.497***<br>(0.071) | -0.497***<br>(0.071) |                      |
| factor_PC8                     |                      | 0.428**<br>(0.140)   | 0.428*<br>(0.172)    |
| factor_PC9                     |                      | 0.608***<br>(0.118)  | 0.608***<br>(0.123)  |
| factor_PC10                    |                      | 0.371<br>(0.210)     | 0.371<br>(0.257)     |
| factor_PC11                    |                      | 0.184*<br>(0.084)    | 0.184<br>(0.097)     |
| factor_PC12                    |                      | 0.705***<br>(0.080)  | 0.705***<br>(0.086)  |
| factor_PC13                    |                      | 0.295***<br>(0.085)  | 0.295**<br>(0.096)   |
| factor_PC14                    |                      | 1.184***<br>(0.095)  | 1.184***<br>(0.101)  |
| factor_PC15                    |                      | 0.163<br>(0.450)     | 0.163<br>(0.489)     |
| factor_PC17                    |                      | -1.063***<br>(0.117) | -1.063***<br>(0.176) |
| factor_PC20                    |                      | 0.633***<br>(0.085)  | 0.633***<br>(0.096)  |
| factor_PC21                    |                      | 0.567***<br>(0.080)  | 0.567***<br>(0.087)  |
| factor_Month9                  |                      | -0.533***<br>(0.073) | -0.533***<br>(0.073) |
| factor_Month10                 |                      | -0.399***<br>(0.079) | -0.399***<br>(0.079) |
| factor_Month11                 |                      | -0.391***<br>(0.076) | -0.391***<br>(0.074) |
| factor_Month12                 |                      | -0.546***<br>(0.074) | -0.546***<br>(0.073) |
| BIE_timeline_PC:group_store_PC |                      | -0.333***<br>(0.078) | -0.333***<br>(0.083) |
| Constant                       |                      | -7.316***<br>(0.142) | -7.316***<br>(0.164) |
| Observations                   |                      | 21,115               | 21,115               |
| R2                             |                      | 0.604                | 0.604                |
| Adjusted R2                    |                      | 0.603                | 0.603                |
| Residual Std. Error            |                      | 2.218                | 2.218                |
| F Statistic                    |                      | 918.503***           | 918.503***           |

Note: \*p<0.05; \*\*p<0.01; \*\*\*p<0.001

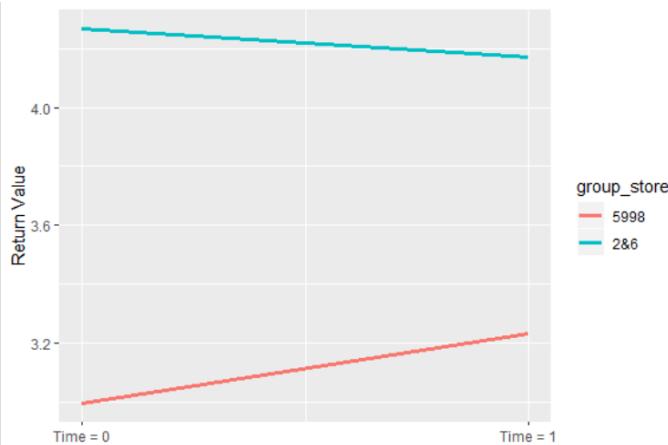
>

```
meffects56 <- ggpredict(ols54, terms=c("BIE_timeline_PC", "group_store_PC"))
```

| x   | predicted | conf.low | conf.high | group |
|-----|-----------|----------|-----------|-------|
| 1 0 | 2.996820  | 2.807414 | 3.186226  | 0     |
| 2 0 | 4.267977  | 4.106324 | 4.429630  | 1     |
| 3 1 | 3.232636  | 3.056981 | 3.408291  | 0     |
| 4 1 | 4.170777  | 4.009743 | 4.331812  | 1     |

```
ggplot(meffects56,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Return Value") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
```

```
scale_x_continuous(breaks=c(0,1), labels=c("Time = 0", "Time = 1")) +
theme(axis.title.x=element_blank())
```



```
The interaction coefficient of BIE_timeline_PC:group_store_PC is significant with value -0.333. This means that BOPS implementation is associated with 33.3% decrease in product-level return value.
```

...

```
#=====
Question6: How does the impact of implementing BOPS strategy vary across product categories?
#=====
``{r}
```

### #Descriptive statistics

```
stargazer(ODS_prodcat, type="text", median=TRUE, iqr=TRUE, digits=3, title="Descriptive Statistics")
```

| Statistic        | N      | Mean      | St. Dev.   | Min   | Pctl(25) | Median    | Pctl(75)  | Max         |
|------------------|--------|-----------|------------|-------|----------|-----------|-----------|-------------|
| store_number     | 30,475 | 1,398.810 | 2,533.160  | 2     | 2        | 6         | 6         | 5,998       |
| year             | 30,475 | 2,011.630 | 0.949      | 2,010 | 2,011    | 2,012     | 2,012     | 2,013       |
| month_index      | 30,475 | 31.096    | 10.292     | 13    | 22       | 31        | 40        | 48          |
| product_category | 30,475 | 9.335     | 6.316      | 1     | 4        | 7         | 13        | 21          |
| month_dummy      | 30,475 | 6.541     | 3.554      | 1     | 3        | 6         | 10        | 12          |
| bops_in_effect   | 30,475 | 0.595     | 0.491      | 0     | 0        | 1         | 1         | 1           |
| day              | 30,475 | 566.639   | 313.415    | 1     | 292      | 569       | 846       | 1,096       |
| salesvalue       | 30,475 | 9,342.367 | 20,865.000 | 0.000 | 546.295  | 1,950.680 | 8,952.230 | 424,294.600 |
| returnvalue      | 30,475 | 1,439.134 | 3,166.514  | 0.000 | 0.000    | 199.000   | 1,398.860 | 52,508.210  |
| salesquantity    | 30,475 | 54.848    | 162.805    | 1     | 3        | 9         | 34        | 5,111       |
| returnquantity   | 30,475 | 5.540     | 13.509     | 0     | 0        | 1         | 5         | 380         |
| avg_female       | 23,277 | 0.501     | 0.285      | 0.000 | 0.333    | 0.500     | 0.667     | 1.000       |
| avg_age          | 23,795 | 4.935     | 2.115      | 0.000 | 4.000    | 4.907     | 5.913     | 13.000      |
| avg_income       | 23,763 | 5.255     | 1.194      | 1.000 | 4.808    | 5.333     | 5.800     | 9.000       |
| avg_homeowner    | 23,763 | 0.645     | 0.251      | 0.000 | 0.534    | 0.667     | 0.778     | 1.000       |
| avg_residency    | 23,763 | 6.893     | 2.815      | 0.000 | 5.615    | 6.910     | 7.958     | 15.000      |
| avg_chldowner    | 23,763 | 0.377     | 0.250      | 0.000 | 0.250    | 0.368     | 0.481     | 1.000       |

```
describeBy(ODS_prodcat, ODS_prodcat$product_category)
```

| Descriptive statistics by group |      |      |          |          |         |          |         |      |           |           |       |          |        |  |
|---------------------------------|------|------|----------|----------|---------|----------|---------|------|-----------|-----------|-------|----------|--------|--|
| group: 1                        | vars | n    | mean     | sd       | median  | trimmed  | mad     | min  | max       | range     | skew  | kurtosis | se     |  |
| store_number                    | 1    | 2059 | 1150.74  | 2358.54  | 6.00    | 690.95   | 5.93    | 2    | 5998.00   | 5996.00   | 1.57  | 0.46     | 51.98  |  |
| year                            | 2    | 2059 | 2011.67  | 0.95     | 2012.00 | 2011.71  | 1.48    | 2010 | 2013.00   | 3.00      | -0.15 | -0.92    | 0.02   |  |
| month_index                     | 3    | 2059 | NaN      | NA       | NA      | NaN      | NA      | Inf  | -Inf      | -Inf      | NA    | NA       | NA     |  |
| product_category                | 5    | 2059 | 1.00     | 0.00     | 1.00    | 1.00     | 0.00    | 1    | 1.00      | 0.00      | NaN   | NaN      | 0.00   |  |
| month_dummy                     | 6    | 2059 | 6.59     | 3.56     | 7.00    | 6.59     | 4.45    | 1    | 12.00     | 11.00     | 0.01  | -1.27    | 0.08   |  |
| bops_in_effect                  | 7    | 2059 | 0.63     | 0.48     | 1.00    | 0.67     | 0.00    | 0    | 1.00      | 1.00      | -0.56 | -1.69    | 0.01   |  |
| day                             | 8    | 2059 | 582.14   | 313.31   | 594.00  | 587.64   | 401.78  | 2    | 1096.00   | 1094.00   | -0.13 | -1.19    | 6.90   |  |
| salesvalue                      | 9    | 2059 | 16232.94 | 22216.16 | 4458.22 | 11848.96 | 5669.52 | 0    | 188843.50 | 188843.50 | 2.20  | 7.11     | 489.60 |  |
| returnvalue                     | 10   | 2059 | 3406.79  | 5082.82  | 869.98  | 2307.84  | 1289.83 | 0    | 31211.98  | 31211.98  | 2.00  | 4.22     | 112.02 |  |
| salesquantity                   | 11   | 2059 | 17.54    | 24.44    | 4.00    | 12.58    | 4.45    | 1    | 203.00    | 202.00    | 2.28  | 7.51     | 0.54   |  |
| returnquantity                  | 12   | 2059 | 3.32     | 4.76     | 1.00    | 2.34     | 1.48    | 0    | 31.00     | 31.00     | 2.00  | 4.67     | 0.10   |  |
| avg_female                      | 13   | 1626 | 0.35     | 0.27     | 0.33    | 0.32     | 0.22    | 0    | 1.00      | 1.00      | 0.79  | 0.42     | 0.01   |  |
| avg_age                         | 14   | 1671 | 4.54     | 2.12     | 4.39    | 4.47     | 1.32    | 0    | 13.00     | 13.00     | 0.54  | 1.91     | 0.05   |  |
| avg_income                      | 15   | 1668 | 4.81     | 1.26     | 4.87    | 4.85     | 0.83    | 1    | 9.00      | 8.00      | -0.33 | 2.06     | 0.03   |  |
| avg_homeowner                   | 16   | 1668 | 0.59     | 0.27     | 0.60    | 0.61     | 0.18    | 0    | 1.00      | 1.00      | -0.40 | 0.03     | 0.01   |  |
| avg_residency                   | 17   | 1668 | 6.60     | 3.04     | 6.50    | 6.45     | 1.88    | 0    | 15.00     | 15.00     | 0.59  | 1.28     | 0.07   |  |
| avg_childowner                  | 18   | 1668 | 0.36     | 0.27     | 0.34    | 0.33     | 0.18    | 0    | 1.00      | 1.00      | 0.77  | 0.55     | 0.01   |  |

#Similarly group 2 to group 20 results are also displayed

# creating groups of store with BOPS implementation

```
sales6 <- ODS_prodcat[(ODS_prodcat$day<786),]
```

#Add a BIE timeline variable dividing the data into two groups, one before Aug.1, 2011 and the other after.

#Add a grouping variable for stores dividing the data into two groups, one for 2&6 and the other for 5998.

```
sales6$BIE_timeline <- ifelse(sales6$day<366,0,1)
```

```
sales6$group_store <- ifelse((sales6$store_number==2) | (sales6$store_number==6),1,0)
```

#Assuming mean value for all 'na' values

```
sales6$avg_female[is.na(sales6$avg_female)] <- mean(sales6$avg_female, na.rm = TRUE)
```

```
sales6$avg_age[is.na(sales6$avg_age)] <- mean(sales6$avg_age, na.rm = TRUE)
```

```
sales6$avg_income[is.na(sales6$avg_income)] <- mean(sales6$avg_income, na.rm = TRUE)
```

```
sales6$avg_homeowner[is.na(sales6$avg_homeowner)] <- mean(sales6$avg_homeowner, na.rm = TRUE)
```

```
sales6$avg_residency[is.na(sales6$avg_residency)] <- mean(sales6$avg_residency, na.rm = TRUE)
```

```
sales6$avg_childowner[is.na(sales6$avg_childowner)] <- mean(sales6$avg_childowner, na.rm = TRUE)
```

|   | returnquantity | avg_female | avg_age   | avg_income | avg_homeowner | avg_residency | avg_childowner | BIE_timeline | group_store |
|---|----------------|------------|-----------|------------|---------------|---------------|----------------|--------------|-------------|
| 0 | 29             | 0.5092251  | 4.993311  | 5.612794   | 0.6296296     | 7.037037      | 0.36363637     | 1            | 1           |
| 1 | 0              | 1.0000000  | 0.0000000 | 8.000000   | 1.0000000     | 4.000000      | 0.00000000     | 0            | 1           |
| 7 | 0              | 0.5000000  | 3.714286  | 4.428571   | 0.8571429     | 8.428572      | 0.28571430     | 0            | 1           |
| 2 | 0              | 0.0000000  | 2.500000  | 4.500000   | 0.5000000     | 10.000000     | 0.00000000     | 0            | 1           |
| 1 | 1              | 0.0000000  | 4.000000  | 2.000000   | 0.0000000     | 8.000000      | 1.00000000     | 0            | 1           |
| 7 | 34             | 0.6012461  | 5.046448  | 5.691257   | 0.6229508     | 7.628415      | 0.39071038     | 0            | 1           |
| 8 | 25             | 0.6894410  | 5.393259  | 4.966292   | 0.5842696     | 5.707865      | 0.34269664     | 0            | 1           |

```
stargazer(sales6, type="text", median=TRUE, iqr=TRUE,digits=1, title="Descriptive Statistics")
```

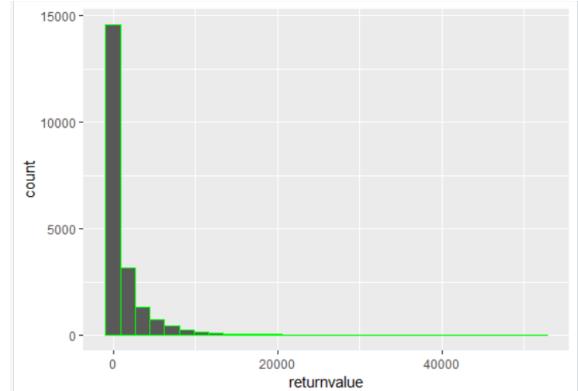
**Descriptive Statistics**

| Statistic        | N      | Mean    | St. Dev. | Min   | Pctl(25) | Median  | Pctl(75) | Max       |
|------------------|--------|---------|----------|-------|----------|---------|----------|-----------|
| store_number     | 21,003 | 1,283.7 | 2,456.6  | 2     | 2        | 6       | 6        | 5,998     |
| year             | 21,003 | 2,011.2 | 0.7      | 2,010 | 2,011    | 2,011   | 2,012    | 2,012     |
| month_index      | 21,003 | 25.6    | 7.3      | 13    | 19       | 26      | 32       | 38        |
| product_category | 21,003 | 9.4     | 6.3      | 1     | 4        | 7       | 13       | 21        |
| month_dummy      | 21,003 | 6.7     | 3.5      | 1     | 4        | 7       | 10       | 12        |
| bops_in_effect   | 21,003 | 0.4     | 0.5      | 0     | 0        | 0       | 1        | 1         |
| day              | 21,003 | 399.7   | 222.2    | 1     | 204      | 408     | 587      | 785       |
| salesvalue       | 21,003 | 8,734.2 | 19,168.4 | 0.0   | 507.9    | 1,857.3 | 8,538.8  | 402,473.4 |
| returnvalue      | 21,003 | 1,375.3 | 2,997.0  | 0.0   | 0.0      | 194.5   | 1,376.5  | 51,973.1  |
| salesquantity    | 21,003 | 49.9    | 139.9    | 1     | 2        | 9       | 32       | 4,474     |
| returnquantity   | 21,003 | 5.3     | 12.6     | 0     | 0        | 1       | 5        | 380       |
| avg_female       | 21,003 | 0.5     | 0.3      | 0.0   | 0.4      | 0.5     | 0.6      | 1.0       |
| avg_age          | 21,003 | 5.0     | 1.9      | 0.0   | 4.4      | 5.0     | 5.7      | 13.0      |
| avg_income       | 21,003 | 5.3     | 1.1      | 1.0   | 5.0      | 5.3     | 5.7      | 9.0       |
| avg_homeowner    | 21,003 | 0.6     | 0.2      | 0.0   | 0.6      | 0.6     | 0.7      | 1.0       |
| avg_residency    | 21,003 | 6.9     | 2.5      | 0.0   | 6.0      | 6.9     | 7.5      | 15.0      |
| avg_childowner   | 21,003 | 0.4     | 0.2      | 0.0   | 0.3      | 0.4     | 0.4      | 1.0       |
| BIE_timeline     | 21,003 | 0.5     | 0.5      | 0     | 0        | 1       | 1        | 1         |
| group_store      | 21,003 | 0.8     | 0.4      | 0     | 1        | 1       | 1        | 1         |

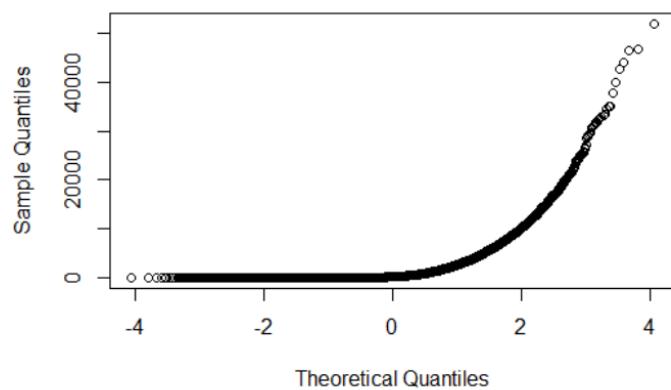
**====IMPACT ON RETURN VALUE=====####**

#check normalization

ggplot(sales6, aes(x=returnvalue)) + geom\_histogram(colour="green", bins = 30)

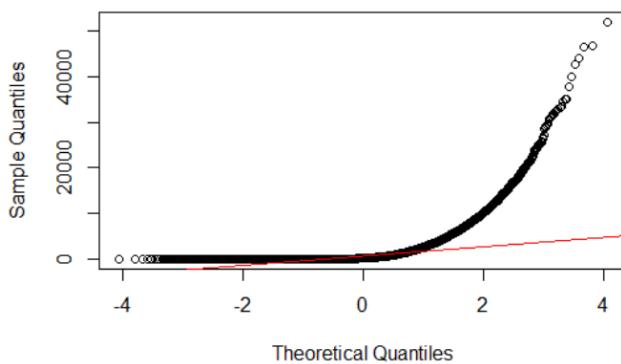


qqnorm(sales6\$returnvalue)

**Normal Q-Q Plot**

qqline(sales6\$returnvalue, col=2) #distribution is not normal

### Normal Q-Q Plot



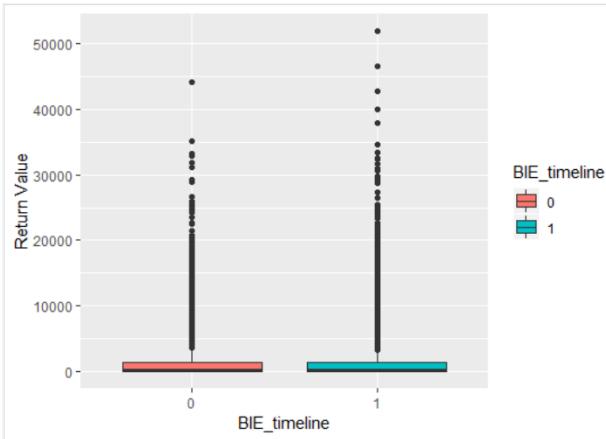
```
#analyzing general trend between key independent and dependent variable using box plot
df61 <- data.frame(returnvalue=sales6$returnvalue, BIE_timeline=as.factor(sales6$BIE_timeline))
```

BA Project\_BOPS\_Final Submitted.Rmd

|   | returnvalue | BIE_timeline |
|---|-------------|--------------|
| 1 | 4828.76     | 1            |
| 2 | 0.00        | 0            |
| 3 | 0.00        | 0            |
| 4 | 0.00        | 0            |
| 5 | 48.99       | 0            |

Showing 1 to 6 of 21,003 entries

```
ggplot(df61, aes(x=BIE_timeline, y=returnvalue, fill=BIE_timeline)) + geom_boxplot() +
 xlab("BIE_timeline") + ylab("Return Value")
```



```
test for multicollinearity
df62=sales6[c("BIE_timeline","group_store","month_dummy","product_category","salesvalue",
"avg_female","avg_age","avg_income")]
```

BA Project\_BOPS\_Final Submitted.Rmd df62 df61 sales6 meffects56 meffects52 meffects51 sales5

Showing 1 to 6 of 21,003 entries

```
stargazer(df62, type="text", median=TRUE, iqr=TRUE, digits=1, title="Descriptive Statistics")
```

#### Descriptive Statistics

| Statistic        | N      | Mean    | St. Dev. | Min | Pctl(25) | Median  | Pctl(75) | Max       |
|------------------|--------|---------|----------|-----|----------|---------|----------|-----------|
| BIE_timeline     | 21,003 | 0.5     | 0.5      | 0   | 0        | 1       | 1        | 1         |
| group_store      | 21,003 | 0.8     | 0.4      | 0   | 1        | 1       | 1        | 1         |
| month_dummy      | 21,003 | 6.7     | 3.5      | 1   | 4        | 7       | 10       | 12        |
| product_category | 21,003 | 9.4     | 6.3      | 1   | 4        | 7       | 13       | 21        |
| salesvalue       | 21,003 | 8,734.2 | 19,168.4 | 0.0 | 507.9    | 1,857.3 | 8,538.8  | 402,473.4 |
| avg_female       | 21,003 | 0.5     | 0.3      | 0.0 | 0.4      | 0.5     | 0.6      | 1.0       |
| avg_age          | 21,003 | 5.0     | 1.9      | 0.0 | 4.4      | 5.0     | 5.7      | 13.0      |
| avg_income       | 21,003 | 5.3     | 1.1      | 1.0 | 5.0      | 5.3     | 5.7      | 9.0       |

```
round(cor(df62),3)
```

```
> round(cor(df62),3)
 BIE_timeline group_store month_dummy product_category salesvalue avg_female avg_age avg_income
BIE_timeline 1.000 -0.096 0.039 -0.007 0.007 -0.018 -0.085 -0.032
group_store -0.096 1.000 0.021 -0.007 0.200 0.012 0.012 -0.012
month_dummy 0.039 0.021 1.000 -0.001 0.091 -0.030 0.050 0.043
product_category -0.007 -0.007 -0.001 1.000 -0.073 0.066 0.070 0.093
salesvalue 0.007 0.200 0.091 -0.073 1.000 -0.129 -0.047 0.031
avg_female -0.018 0.012 -0.030 0.066 -0.129 1.000 0.077 -0.011
avg_age -0.085 0.012 0.050 0.070 -0.047 0.077 1.000 0.172
avg_income -0.032 -0.012 0.043 0.093 0.031 -0.011 0.172 1.000
```

```
vifcor(df62) # No variable from the 9 input variables has collinearity problem.
```

```
No variable from the 8 input variables has collinearity problem.
```

```
The linear correlation coefficients ranges between:
```

```
min correlation (avg_female ~ group_store): 0.004545106
max correlation (salesvalue ~ group_store): 0.2054456
```

```
----- VIFs of the remained variables -----
```

|   | Variables        | VIF      |
|---|------------------|----------|
| 1 | BIE_timeline     | 1.019542 |
| 2 | group_store      | 1.057619 |
| 3 | month_dummy      | 1.012736 |
| 4 | product_category | 1.021246 |
| 5 | salesvalue       | 1.086274 |
| 6 | avg_female       | 1.039312 |
| 7 | avg_age          | 1.059098 |
| 8 | avg_income       | 1.039270 |

```
#converting into factor variables
```

```
sales6$BIE_timeline<- as.factor(sales6$BIE_timeline)
```

```
sales6$month_dummy<- as.factor(sales6$month_dummy)
```

```
sales6$product_category<- as.factor(sales6$product_category)
```

```
#Since sales value is a dollar value, we will use a linear interaction model with log transformed dependent variable.
```

```
sales6$log_salesvalue <- log(1+sales6$salesvalue)
sales6$log_returnvalue <- log(1+sales6$returnvalue)
```

| id | avg_female | avg_age   | avg_income | avg_homeowner | avg_residency | avg_chldowner | BIE_timeline | group_store | log_salesvalue | log_returnvalue |
|----|------------|-----------|------------|---------------|---------------|---------------|--------------|-------------|----------------|-----------------|
| 29 | 0.5092251  | 4.993311  | 5.612794   | 0.6296296     | 7.037037      | 0.36363637    | 1            | 1           | 10.575784      | 8.482552        |
| 0  | 1.0000000  | 0.0000000 | 8.000000   | 1.0000000     | 4.000000      | 0.00000000    | 0            | 1           | 5.309158       | 0.000000        |
| 0  | 0.5000000  | 3.714286  | 4.428571   | 0.8571429     | 8.428572      | 0.28571430    | 0            | 1           | 6.730517       | 0.000000        |
| 0  | 0.0000000  | 2.500000  | 4.500000   | 0.5000000     | 10.000000     | 0.00000000    | 0            | 1           | 5.319492       | 0.000000        |
| 1  | 0.0000000  | 4.000000  | 2.000000   | 0.0000000     | 8.000000      | 1.00000000    | 0            | 1           | 3.911823       | 3.911823        |

Showing 1 to 6 of 21,003 entries

# we want to analyse the impact of BOPS implementation across all the product category, so we will use triple interaction

```
ols61 = lm(log_returnvalue~BIE_timeline*group_store*product_category+log_salesvalue+
month_dummy+ avg_female+avg_age+avg_income, data = sales6)
stargazer(ols61,
 title="Regression Results", type="text",
 column.labels=c("Model-Return value "),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

# Check for heteroskedasticity

```
gqttest(ols61) # Goldfeld-Quandt test indicates heteroskedasticity
bpptest(ols61) # Breusch-Pagan test indicates heteroskedasticity
```

```
Goldfeld-Quandt test

data: ols61
GQ = 1.6404, df1 = 10415, df2 = 10414, p-value < 2.2e-16
alternative hypothesis: variance increases from segment 1 to 2

> bpptest(ols61) # Breusch-Pagan test indicates heteroskedasticity

studentized Breusch-Pagan test

data: ols61
BP = 3471.4, df = 78, p-value < 2.2e-16
```

# Since there is heteroskedasticity in the data, we will replace SEs with clustered robust SEs.

```
HWrobstdter <- sqrt(diag(vcovHC(ols61, type="HC1"))) # produces Huber-White robust standard errors
clusrobstdter <- sqrt(diag(cluster.vcov(ols61, sales6$store_number))) # produces clustered robust standard errors using store_number as clustering variable
```

Values

|               |                                           |
|---------------|-------------------------------------------|
| clusrobstdter | Named num [1:79] 0.37116 0.02824 0.570... |
| HWrobstdter   | Named num [1:79] 0.334 0.385 0.323 0.3... |

```
stargazer(ols61, ols61, ols61,
 se=list(NULL, HWrobstdter, clusrobstdter),
 title="Regression Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE", "Clustered SE"),
```

df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001))

| Regression Results               |                                     |                      |                      |                                  |                      |                      |                      |                     |                     |                     |
|----------------------------------|-------------------------------------|----------------------|----------------------|----------------------------------|----------------------|----------------------|----------------------|---------------------|---------------------|---------------------|
|                                  | Dependent variable: log_returnvalue |                      |                      |                                  |                      |                      |                      |                     |                     |                     |
|                                  | Normal SE                           | HW-Robust SE         | Clustered SE         | (1)                              | (2)                  | (3)                  | product_category9    | 3.278***<br>(0.717) | 3.278***<br>(0.504) | 3.278***<br>(0.154) |
| BIE_timeline1                    | 0.450<br>(0.319)                    | 0.450<br>(0.385)     | 0.450***<br>(0.028)  |                                  | product_category10   | 0.425<br>(0.240)     | 0.425<br>(0.296)     | 0.425<br>(0.664)    |                     |                     |
| group_store                      | 2.853***<br>(0.282)                 | 2.853***<br>(0.323)  | 2.853***<br>(0.570)  |                                  | product_category11   | 1.841***<br>(0.328)  | 1.841***<br>(0.378)  | 1.841***<br>(0.019) |                     |                     |
| product_category2                | 2.503***<br>(0.362)                 | 2.503***<br>(0.395)  | 2.503***<br>(0.078)  |                                  | product_category12   | 2.336***<br>(0.312)  | 2.336***<br>(0.347)  | 2.336***<br>(0.036) |                     |                     |
| product_category3                | 1.293***<br>(0.355)                 | 1.293**<br>(0.443)   | 1.293***<br>(0.004)  |                                  | product_category13   | 0.992**<br>(0.335)   | 0.992**<br>(0.381)   | 0.992***<br>(0.028) |                     |                     |
| product_category4                | 1.659***<br>(0.315)                 | 1.659***<br>(0.367)  | 1.659***<br>(0.008)  |                                  | product_category14   | 3.367***<br>(0.388)  | 3.367***<br>(0.341)  | 3.367***<br>(0.150) |                     |                     |
| product_category5                | 2.131***<br>(0.311)                 | 2.131***<br>(0.353)  | 2.131***<br>(0.028)  |                                  | product_category15   | 0.158<br>(0.493)     | 0.158<br>(0.570)     | 0.158<br>(0.589)    |                     |                     |
| product_category6                | 1.771***<br>(0.347)                 | 1.771***<br>(0.372)  | 1.771***<br>(0.057)  |                                  | product_category17   | -1.180***<br>(0.172) | -1.180***<br>(0.253) | -1.180*<br>(0.487)  |                     |                     |
| product_category7                | 2.562***<br>(0.319)                 | 2.562***<br>(0.330)  | 2.562***<br>(0.114)  |                                  | product_category20   | 1.564***<br>(0.334)  | 1.564***<br>(0.374)  | 1.564***<br>(0.032) |                     |                     |
| product_category8                | 0.406*<br>(0.175)                   | 0.406<br>(0.217)     | 0.406<br>(0.580)     |                                  | product_category21   | 2.065***<br>(0.314)  | 2.065***<br>(0.345)  | 2.065***<br>(0.051) |                     |                     |
| month_dummy2                     |                                     |                      |                      | log_salesvalue                   | 1.348***<br>(0.010)  | 1.348***<br>(0.012)  | 1.348***<br>(0.053)  |                     |                     |                     |
| month_dummy3                     | -0.423***<br>(0.077)                | -0.423***<br>(0.078) | -0.423***<br>(0.116) | month_dummy2                     | -0.449***<br>(0.076) | -0.449***<br>(0.075) | -0.449***<br>(0.036) |                     |                     |                     |
| month_dummy4                     | -0.492***<br>(0.078)                | -0.492***<br>(0.077) | -0.492***<br>(0.116) | avg_income                       | 0.049**<br>(0.015)   | 0.049**<br>(0.017)   | 0.049*<br>(0.020)    |                     |                     |                     |
| month_dummy5                     | -0.494***<br>(0.076)                | -0.494***<br>(0.076) | -0.494***<br>(0.094) | BIE_timeline1:group_store        | -0.519<br>(0.344)    | -0.519<br>(0.415)    | -0.519***<br>(0.047) |                     |                     |                     |
| month_dummy6                     | -0.534***<br>(0.078)                | -0.534***<br>(0.078) | -0.534***<br>(0.081) | BIE_timeline1:product_category2  | -0.306<br>(0.438)    | -0.306<br>(0.498)    | -0.306***<br>(0.006) |                     |                     |                     |
| month_dummy7                     | -0.431***<br>(0.077)                | -0.431***<br>(0.077) | -0.431***<br>(0.055) | BIE_timeline1:product_category3  | -0.348<br>(0.427)    | -0.348<br>(0.550)    | -0.348***<br>(0.015) |                     |                     |                     |
| month_dummy8                     | -0.497***<br>(0.071)                | -0.497***<br>(0.071) | -0.497***<br>(0.145) | BIE_timeline1:product_category4  | 0.499<br>(0.383)     | 0.499<br>(0.464)     | 0.499***<br>(0.010)  |                     |                     |                     |
| month_dummy9                     | -0.529***<br>(0.074)                | -0.529***<br>(0.074) | -0.529***<br>(0.054) | BIE_timeline1:product_category5  | -0.522<br>(0.382)    | -0.522<br>(0.452)    | -0.522***<br>(0.013) |                     |                     |                     |
| month_dummy10                    | -0.400***<br>(0.079)                | -0.400***<br>(0.079) | -0.400***<br>(0.103) | BIE_timeline1:product_category6  | -0.404<br>(0.429)    | -0.404<br>(0.480)    | -0.404***<br>(0.016) |                     |                     |                     |
| month_dummy11                    | -0.380***<br>(0.075)                | -0.380***<br>(0.074) | -0.380***<br>(0.062) | BIE_timeline1:product_category7  | -0.380<br>(0.394)    | -0.380<br>(0.419)    | -0.380***<br>(0.017) |                     |                     |                     |
| month_dummy12                    | -0.524***<br>(0.073)                | -0.524***<br>(0.073) | -0.524***<br>(0.064) | BIE_timeline1:product_category8  | -0.784*<br>(0.305)   | -0.784*<br>(0.355)   | -0.784***<br>(0.141) |                     |                     |                     |
| avg_female                       | 0.441***<br>(0.066)                 | 0.441***<br>(0.077)  | 0.441<br>(0.274)     | BIE_timeline1:product_category9  | -1.386<br>(0.766)    | -1.386*<br>(0.592)   | -1.386***<br>(0.045) |                     |                     |                     |
| avg_age                          | -0.056***<br>(0.008)                | -0.056***<br>(0.010) | -0.056***<br>(0.016) | BIE_timeline1:product_category10 | -1.621**<br>(0.526)  | -1.621**<br>(0.542)  | -1.621***<br>(0.039) |                     |                     |                     |
|                                  |                                     |                      |                      | BIE_timeline1:product_category11 | -0.868*<br>(0.401)   | -0.868*<br>(0.478)   | -0.868***<br>(0.028) |                     |                     |                     |
| BIE_timeline1:product_category12 | -0.195<br>(0.382)                   | -0.195<br>(0.444)    | -0.195***<br>(0.011) | group_store:product_category7    | -2.511***<br>(0.353) | -2.511***<br>(0.364) | -2.511***<br>(0.695) |                     |                     |                     |
| BIE_timeline1:product_category13 | 0.415<br>(0.412)                    | 0.415<br>(0.481)     | 0.415***<br>(0.038)  | group_store:product_category8    |                      |                      |                      |                     |                     |                     |
| BIE_timeline1:product_category14 | -0.796<br>(0.509)                   | -0.796<br>(0.455)    | -0.796***<br>(0.003) | group_store:product_category9    | -2.564***<br>(0.750) | -2.564***<br>(0.537) | -2.564***<br>(0.694) |                     |                     |                     |
| BIE_timeline1:product_category15 | -1.509<br>(1.213)                   | -1.509*<br>(0.626)   | -1.509***<br>(0.109) | group_store:product_category10   |                      |                      |                      |                     |                     |                     |
| BIE_timeline1:product_category17 | -0.223<br>(0.238)                   | -0.223<br>(0.357)    | -0.223***<br>(0.033) | group_store:product_category11   | -1.884***<br>(0.356) | -1.884***<br>(0.408) | -1.884***<br>(0.050) |                     |                     |                     |
| BIE_timeline1:product_category20 | 0.293<br>(0.410)                    | 0.293<br>(0.486)     | 0.293***<br>(0.015)  | group_store:product_category12   | -1.988***<br>(0.338) | -1.988***<br>(0.371) | -1.988***<br>(0.664) |                     |                     |                     |
| BIE_timeline1:product_category21 | -0.141<br>(0.384)                   | -0.141<br>(0.444)    | -0.141***<br>(0.007) | group_store:product_category13   | -0.951**<br>(0.362)  | -0.951*<br>(0.409)   | -0.951***<br>(0.162) |                     |                     |                     |
| group_store:product_category2    | -1.769***<br>(0.385)                | -1.769***<br>(0.418) | -1.769***<br>(0.216) | group_store:product_category14   | -2.324***<br>(0.412) | -2.324***<br>(0.366) | -2.324***<br>(0.489) |                     |                     |                     |
| group_store:product_category3    | -1.426***<br>(0.381)                | -1.426**<br>(0.470)  | -1.426***<br>(0.041) | group_store:product_category15   |                      |                      |                      |                     |                     |                     |
| group_store:product_category4    | -1.287***<br>(0.340)                | -1.287***<br>(0.390) | -1.287*<br>(0.518)   | group_store:product_category17   |                      |                      |                      |                     |                     |                     |
| group_store:product_category5    | -1.806***<br>(0.338)                | -1.806***<br>(0.377) | -1.806***<br>(0.477) | group_store:product_category20   | -1.130**<br>(0.362)  | -1.130**<br>(0.402)  | -1.130***<br>(0.203) |                     |                     |                     |
| group_store:product_category6    | -1.320***<br>(0.372)                | -1.320***<br>(0.399) | -1.320***<br>(0.156) | group_store:product_category21   | -1.734***<br>(0.340) | -1.734***<br>(0.369) | -1.734***<br>(0.462) |                     |                     |                     |

|                                              |                   |                   |                      |                                              |                               |                      |                      |
|----------------------------------------------|-------------------|-------------------|----------------------|----------------------------------------------|-------------------------------|----------------------|----------------------|
| BIE_timeline1:group_store:product_category2  | 0.611<br>(0.474)  | 0.611<br>(0.531)  | 0.611***<br>(0.033)  | BIE_timeline1:group_store:product_category14 | 0.433<br>(0.544)              | 0.433<br>(0.497)     | 0.433***<br>(0.121)  |
| BIE_timeline1:group_store:product_category3  | 0.338<br>(0.467)  | 0.338<br>(0.592)  | 0.338<br>(0.264)     | BIE_timeline1:group_store:product_category15 |                               |                      |                      |
| BIE_timeline1:group_store:product_category4  | -0.448<br>(0.422) | -0.448<br>(0.499) | -0.448*<br>(0.175)   | BIE_timeline1:group_store:product_category17 |                               |                      |                      |
| BIE_timeline1:group_store:product_category5  | 0.540<br>(0.421)  | 0.540<br>(0.486)  | 0.540***<br>(0.054)  | BIE_timeline1:group_store:product_category20 | -0.315<br>(0.451)             | -0.315<br>(0.527)    | -0.315***<br>(0.028) |
| BIE_timeline1:group_store:product_category6  | 0.465<br>(0.465)  | 0.465<br>(0.519)  | 0.465***<br>(0.064)  | BIE_timeline1:group_store:product_category21 | 0.007<br>(0.422)              | 0.007<br>(0.479)     | 0.007<br>(0.174)     |
| BIE_timeline1:group_store:product_category7  | 0.465<br>(0.444)  | 0.465<br>(0.470)  | 0.465*<br>(0.188)    | Constant                                     | -8.745***<br>(0.292)          | -8.745***<br>(0.334) | -8.745***<br>(0.371) |
| BIE_timeline1:group_store:product_category8  |                   |                   |                      | Observations                                 | 21,003                        | 21,003               | 21,003               |
| BIE_timeline1:group_store:product_category9  | 0.715<br>(0.813)  | 0.715<br>(0.643)  | 0.715<br>(0.602)     | R2                                           | 0.608                         | 0.608                | 0.608                |
| BIE_timeline1:group_store:product_category10 |                   |                   |                      | Adjusted R2                                  | 0.607                         | 0.607                | 0.607                |
| BIE_timeline1:group_store:product_category11 | 0.911*<br>(0.442) | 0.911<br>(0.522)  | 0.911***<br>(0.078)  | Residual Std. Error                          | 2.208                         | 2.208                | 2.208                |
| BIE_timeline1:group_store:product_category12 | 0.216<br>(0.421)  | 0.216<br>(0.477)  | 0.216<br>(0.128)     | F Statistic                                  | 416.729***                    | 416.729***           | 416.729***           |
| BIE_timeline1:group_store:product_category13 | -0.267<br>(0.452) | -0.267<br>(0.521) | -0.267***<br>(0.026) | Note:                                        | *p<0.05; **p<0.01; ***p<0.001 |                      |                      |

# displays normal/HW robust/clustered robust standard errors.

### ###-----Marginal Effects -----###

```
meffects61 <- ggpredict(ols61, terms=c("BIE_timeline", "group_store","product_category"))
```

| BA Project_BOPS_Final Submitted.Rmd |   | meffects61 |            |           |       |       |
|-------------------------------------|---|------------|------------|-----------|-------|-------|
|                                     | x | predicted  | conf.low   | conf.high | group | facet |
| 1                                   | 0 | 1.6393230  | 1.11125151 | 2.167395  | 0     | 1     |
| 2                                   | 0 | 4.1420814  | 3.64492469 | 4.639238  | 0     | 2     |
| 3                                   | 0 | 2.9322202  | 2.45686513 | 3.407575  | 0     | 3     |
| 4                                   | 0 | 3.2982594  | 2.94806578 | 3.648453  | 0     | 4     |
| 5                                   | 0 | 3.7701993  | 3.43128916 | 4.109109  | 0     | 5     |
| 6                                   | 0 | 3.4102912  | 2.95623243 | 3.864350  | 0     | 6     |

Showing 1 to 6 of 72 entries

# Replacing by actual variable names for convenience

```
meffects61_colnames <- meffects61[c("x","predicted","group", "facet")]
```

| BA Project_BOPS_Final Submitted.Rmd |   | meffects61_colnames |       |       |
|-------------------------------------|---|---------------------|-------|-------|
|                                     | x | predicted           | group | facet |
| 1                                   | 0 | 1.6393230           | 0     | 1     |
| 2                                   | 0 | 4.1420814           | 0     | 2     |
| 3                                   | 0 | 2.9322202           | 0     | 3     |
| 4                                   | 0 | 3.2982594           | 0     | 4     |
| 5                                   | 0 | 3.7701993           | 0     | 5     |
| 6                                   | 0 | 3.4102912           | 0     | 6     |
| 7                                   | 0 | 4.2015701           | 0     | 7     |
| 8                                   | 0 | 2.0454564           | 0     | 8     |

Showing 1 to 9 of 72 entries

```
colnames(meffects61_colnames) <- c("BIE_timeline", "predicted_return_value","group_store", "product_category")
```

BA Project\_BOPS\_Final Submitted.Rmd × meffects61\_colnames × Filter

|   | BIE_timeline | predicted_return_value | group_store | product_category |
|---|--------------|------------------------|-------------|------------------|
| 1 | 0            | 1.6393230              | 0           | 1                |
| 2 | 0            | 4.1420814              | 0           | 2                |
| 3 | 0            | 2.9322202              | 0           | 3                |
| 4 | 0            | 3.2982594              | 0           | 4                |
| 5 | 0            | 3.7701993              | 0           | 5                |
| 6 | 0            | 3.4102912              | 0           | 6                |
| 7 | 0            | 4.2015701              | 0           | 7                |
| 8 | 0            | 2.0454564              | 0           | 8                |

Showing 1 to 9 of 72 entries

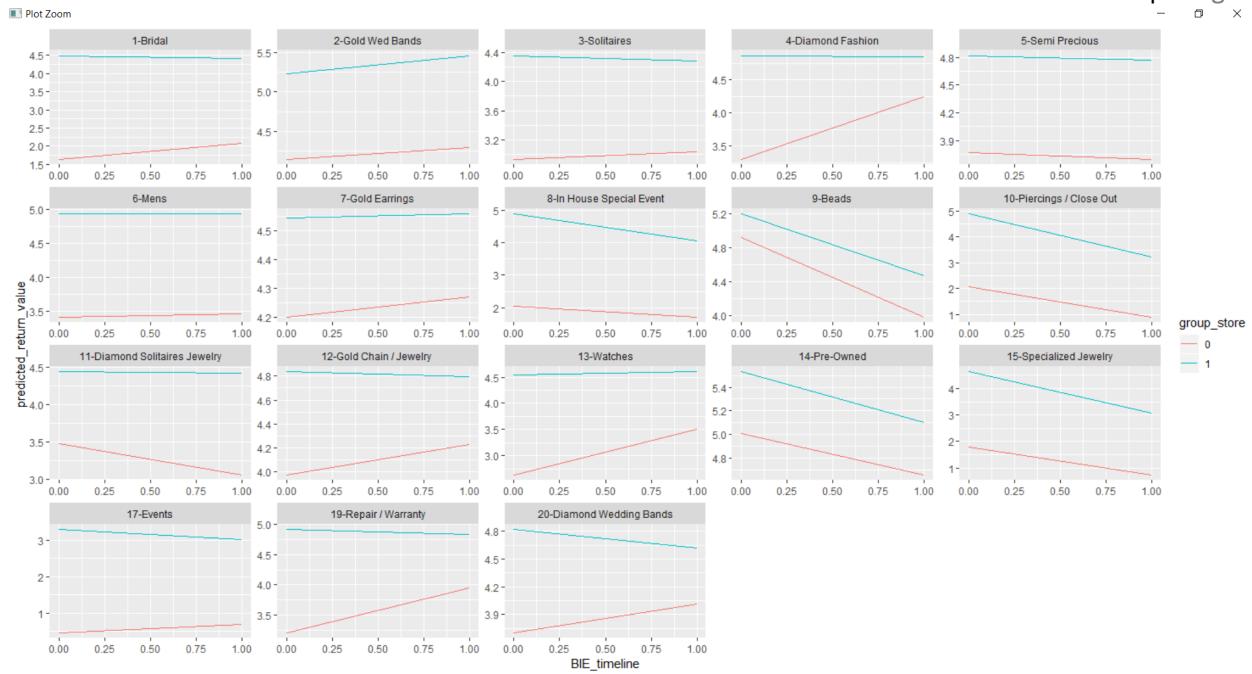
```
levels(meffects61_colnames$product_category) <- c('1-Bridal', '2-Gold Wed Bands', '3-Solitaires', '4-Diamond Fashion', '5-Semi Precious', '6-Mens', '7-Gold Earrings', '8-In House Special Event', '9-Beads', '10-Piercings / Close Out', '11-Diamond Solitaires Jewelry', '12-Gold Chain / Jewelry', '13-Watches', '14-Pre-Owned', '15-Specialized Jewelry', '17-Events', '19-Repair / Warranty', '20-Diamond Wedding Bands', '21-Sterling Silver')
```

BA Project\_BOPS\_Final Submitted.Rmd × meffects61\_colnames × Filter

|   | BIE_timeline | predicted_return_value | group_store | product_category         |
|---|--------------|------------------------|-------------|--------------------------|
| 1 | 0            | 1.6393230              | 0           | 1-Bridal                 |
| 2 | 0            | 4.1420814              | 0           | 2-Gold Wed Bands         |
| 3 | 0            | 2.9322202              | 0           | 3-Solitaires             |
| 4 | 0            | 3.2982594              | 0           | 4-Diamond Fashion        |
| 5 | 0            | 3.7701993              | 0           | 5-Semi Precious          |
| 6 | 0            | 3.4102912              | 0           | 6-Mens                   |
| 7 | 0            | 4.2015701              | 0           | 7-Gold Earrings          |
| 8 | 0            | 2.0454564              | 0           | 8-In House Special Event |

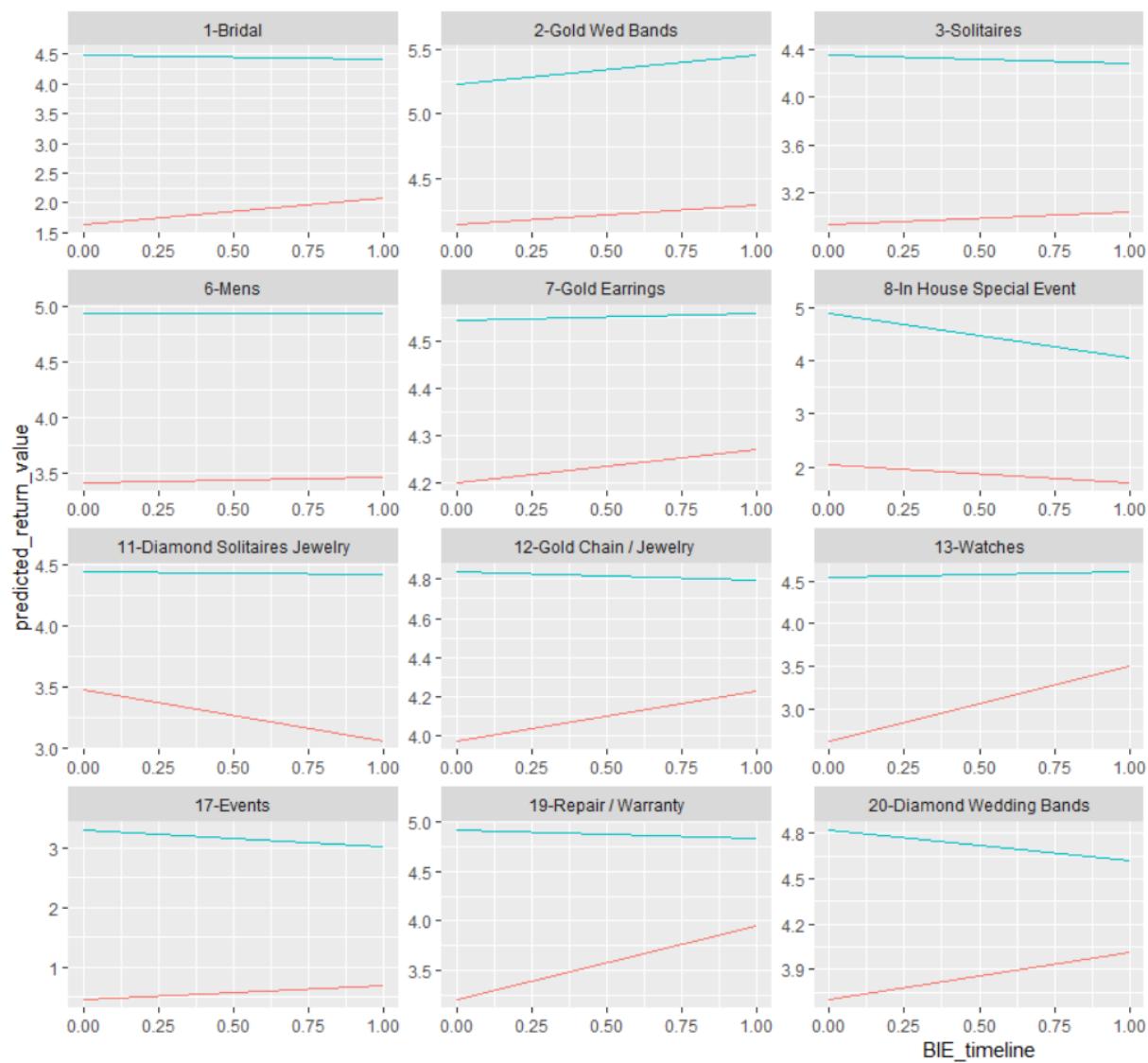
Showing 1 to 9 of 72 entries

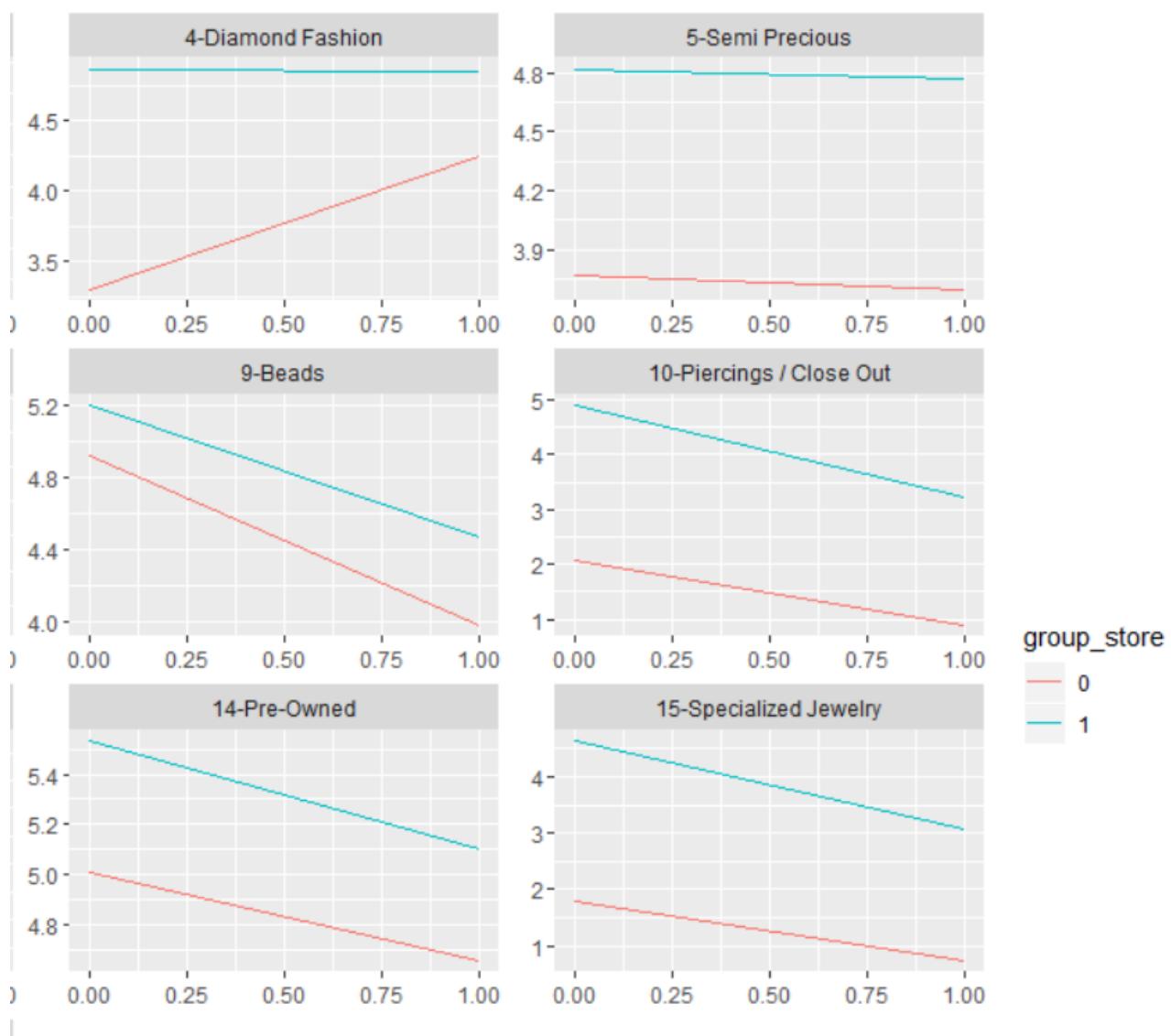
```
ggplot(meffects61_colnames, aes(BIE_timeline,
y= predicted_return_value, colour =group_store)) +
geom_line() +
facet_wrap(product_category ~ ., scales="free")
```



Zoomed version:

Plot Zoom





####-----Subsetting data based on product categories-----####

#Checking predicted values for all the product categories and analyzing impact of BOPS implementation for both storegroups(group 0 = 5998 and group 1 = 2 and 6)

#Change product\_category epeating the code for all

```
df_pc1<- subset(sales6, product_category==1)
```

|      | store_number | year | month | month_index | product_category | month_dummy | bops_in_effect | day | salesvalue | returnvalue | salesquantity | returnquantity | avg_female |
|------|--------------|------|-------|-------------|------------------|-------------|----------------|-----|------------|-------------|---------------|----------------|------------|
| 13   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 2   | 12253.53   | 1478.82     | 13            | 2              | 0.454 ^    |
| 33   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 3   | 7989.74    | 1287.40     | 22            | 3              | 0.55E      |
| 45   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 4   | 26309.46   | 10614.14    | 26            | 5              | 0.44C      |
| 61   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 5   | 6399.69    | 771.66      | 12            | 1              | 0.50C      |
| 76   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 6   | 14782.14   | 3143.39     | 11            | 4              | 0.36E      |
| 92   | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 9   | 19136.12   | 1360.78     | 19            | 3              | 0.53E      |
| 116  | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 10  | 10068.10   | 2699.42     | 21            | 6              | 0.47E      |
| < 17 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 11  | 10067.86   | 2699.42     | 21            | 6              | 0.47E      |

BA Project\_BOPS\_Final Submitted.Rmd df\_pc1 meffects61\_colnames

| isquantity | returnquantity | avg_female | avg_age  | avg_income | avg_homeowner | avg_residency | avg_childowner | BIE_timeline | group_store | log_salesvalue | log_returnvalue |
|------------|----------------|------------|----------|------------|---------------|---------------|----------------|--------------|-------------|----------------|-----------------|
| 13         | 2              | 0.4545455  | 4.615385 | 5.769231   | 0.3076923     | 6.846154      | 0.07692308     | 0            | 1           | 9.413651       | 7.299676        |
| 22         | 3              | 0.5555556  | 3.727273 | 4.590909   | 0.4090909     | 4.863636      | 0.27272728     | 0            | 1           | 8.986039       | 7.161156        |
| 26         | 5              | 0.4400000  | 5.461538 | 5.115385   | 0.5769231     | 6.000000      | 0.42307693     | 0            | 1           | 10.177722      | 9.270037        |
| 12         | 1              | 0.5000000  | 7.250000 | 3.750000   | 0.5833333     | 7.333333      | 0.25000000     | 0            | 1           | 8.764161       | 6.649839        |
| 11         | 4              | 0.3636364  | 6.272727 | 3.727273   | 0.5454546     | 5.727273      | 0.18181819     | 0            | 1           | 9.601243       | 8.053375        |
| 19         | 3              | 0.5333334  | 3.473684 | 4.736842   | 0.6315789     | 4.473684      | 0.31578946     | 0            | 1           | 9.859385       | 7.216548        |
| 21         | 6              | 0.4761905  | 4.142857 | 6.333333   | 0.8095238     | 6.142857      | 0.42857143     | 0            | 1           | 9.217227       | 7.901163        |
| 17         | 4              | 0.5000000  | 4.000000 | 4.000000   | 0.7500000     | 4.166667      | 0.50000000     | 0            | 1           | 9.776157       | 7.494246        |

```
ols_pc1=lm(log_returnvalue~BIE_timeline*group_store+log_salesvalue+ month_dummy+
avg_female+avg_age+avg_income, data = df_pc1)
```

```
stargazer(ols_pc1,
 title="Regression Results", type="text",
 column.labels=c("ME-PC1"),
 df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))
```

```
Check for heteroskedasticity
gqttest(ols_pc1) # Goldfeld-Quandt test indicates heteroskedasticity
bptest(ols_pc1) # Breusch-Pagan test indicates heteroskedasticity
```

#### Goldfeld-Quandt test

```
data: ols_pc1
GQ = 2.3917, df1 = 672, df2 = 671, p-value < 2.2e-16
alternative hypothesis: variance increases from segment 1 to 2
```

```
> bptest(ols_pc1) # Breusch-Pagan test indicates heteroskedasticity
```

#### studentized Breusch-Pagan test

```
data: ols_pc1
BP = 178.49, df = 18, p-value < 2.2e-16
```

```
Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
```

```
HWrobstd \leftarrow sqrt(diag(vcovHC(ols_pc1, type="HC1"))) # produces Huber-White robust standard errors
clusrobstd \leftarrow sqrt(diag(cluster.vcov(ols_pc1, sales6$store_number))) # produces clustered robust
standard errors
```

#### Values

|            |                                        |
|------------|----------------------------------------|
| clusrobstd | Named num [1:79] 0.37116 0.02824 0...  |
| HWrobstd   | Named num [1:19] 0.69 0.4 0.361 0.0... |

```
stargazer(ols_pc1, ols_pc1, ols_pc1,
 se=list(NULL, HWrobstd, clusrobstd),
 title="REgression Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE", "Clustered SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001)) # displays normal/HW robust/clustered robust
standard errors. With clustered robust standard errors
```

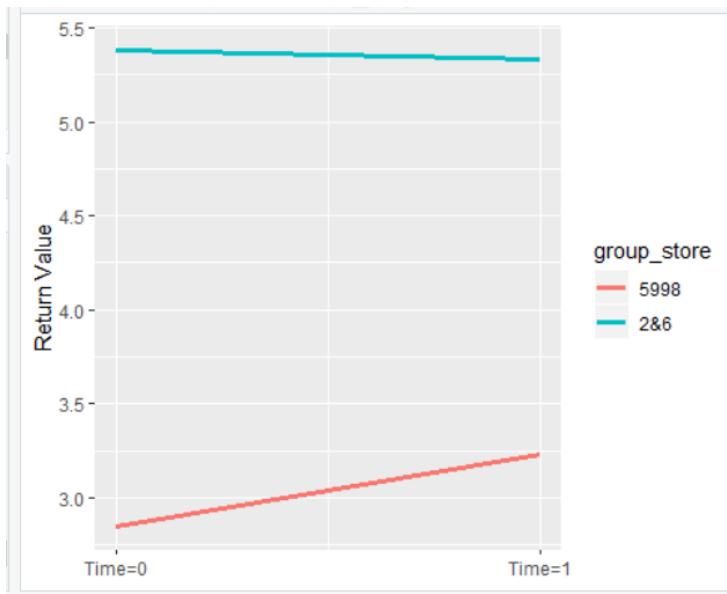
| Regression Results                  |                     |                     |                      |                               |                       |                       |
|-------------------------------------|---------------------|---------------------|----------------------|-------------------------------|-----------------------|-----------------------|
| Dependent variable: log_returnvalue |                     |                     |                      |                               |                       |                       |
|                                     | Normal SE           | HW-Robust SE        | Clustered SE         | (1)                           | (2)                   | (3)                   |
| BIE_timeline1                       | 0.378<br>(0.378)    | 0.378<br>(0.400)    | 0.378***<br>(0.028)  |                               |                       |                       |
| group_store                         | 2.535***<br>(0.343) | 2.535***<br>(0.361) | 2.535***<br>(0.570)  |                               |                       |                       |
| log_salesvalue                      | 1.666**<br>(0.044)  | 1.666***<br>(0.057) | 1.666***<br>(0.053)  |                               |                       |                       |
| month_dummy2                        | -0.325<br>(0.356)   | -0.325<br>(0.350)   | -0.325***<br>(0.036) |                               |                       |                       |
| month_dummy3                        | -0.121<br>(0.360)   | -0.121<br>(0.369)   | -0.121<br>(0.116)    |                               |                       |                       |
| month_dummy4                        | -0.230<br>(0.365)   | -0.230<br>(0.360)   | -0.230*<br>(0.116)   |                               |                       |                       |
| month_dummy5                        | -0.171<br>(0.359)   | -0.171<br>(0.363)   | -0.171<br>(0.094)    |                               |                       |                       |
| month_dummy6                        | -0.046<br>(0.362)   | -0.046<br>(0.363)   | -0.046<br>(0.081)    |                               |                       |                       |
| month_dummy7                        | -0.105<br>(0.356)   | -0.105<br>(0.349)   | -0.105<br>(0.055)    |                               |                       |                       |
| month_dummy8                        | -0.289<br>(0.336)   | -0.289<br>(0.347)   | -0.289*<br>(0.145)   |                               |                       |                       |
| month_dummy9                        |                     |                     |                      | -0.500<br>(0.348)             | -0.500<br>(0.337)     | -0.500***<br>(0.054)  |
| month_dummy10                       |                     |                     |                      | 0.489<br>(0.371)              | 0.489<br>(0.383)      | 0.489***<br>(0.103)   |
| month_dummy11                       |                     |                     |                      | 0.266<br>(0.352)              | 0.266<br>(0.347)      | 0.266***<br>(0.062)   |
| month_dummy12                       |                     |                     |                      | -0.150<br>(0.341)             | -0.150<br>(0.346)     | -0.150*<br>(0.064)    |
| avg_female                          |                     |                     |                      | 1.271***<br>(0.282)           | 1.271***<br>(0.337)   | 1.271***<br>(0.274)   |
| avg_age                             |                     |                     |                      | -0.094**<br>(0.036)           | -0.094*<br>(0.043)    | -0.094***<br>(0.016)  |
| avg_income                          |                     |                     |                      | 0.084<br>(0.060)              | 0.084<br>(0.071)      | 0.084***<br>(0.020)   |
| BIE_timeline1:group_store           |                     |                     |                      | -0.429<br>(0.406)             | -0.429<br>(0.425)     | -0.429***<br>(0.047)  |
| Constant                            |                     |                     |                      | -11.822***<br>(0.627)         | -11.822***<br>(0.690) | -11.822***<br>(0.371) |
| Observations                        |                     |                     |                      | 1,381                         | 1,381                 | 1,381                 |
| R2                                  |                     |                     |                      | 0.591                         | 0.591                 | 0.591                 |
| Adjusted R2                         |                     |                     |                      | 0.586                         | 0.586                 | 0.586                 |
| Residual Std. Error                 |                     |                     |                      | 2.589                         | 2.589                 | 2.589                 |
| F Statistic                         |                     |                     |                      | 109.308***                    | 109.308***            | 109.308***            |
| Note:                               |                     |                     |                      | *p<0.05; **p<0.01; ***p<0.001 |                       |                       |

```
meffects_pc1 <- ggpredict(ols_pc1, terms=c("BIE_timeline", "group_store")) # generates a tidy data frame
```

BA Project\_BOPS\_Final Submitted.Rmd x meffects\_pc1 x df\_pc1 x

| x | predicted | conf.low | conf.high | group |
|---|-----------|----------|-----------|-------|
| 1 | 0         | 2.041666 | 3.655719  | 0     |
| 2 | 0         | 4.848068 | 5.918823  | 1     |
| 3 | 1         | 2.575525 | 3.878003  | 0     |
| 4 | 1         | 4.803626 | 5.861786  | 1     |

```
ggplot(meffects_pc1,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Return Value") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())
```



##Interaction coefficients are insignificant for following categories- 5,6,7.

##Data available only for one store\_group:8,10,15,17.

### Interaction coefficient is significant for categories - 1,2,3,4,9,11,12,13,14,20,21.

## Therefore, BOPS implementation for these categories is associated with:

- # Product Category 1: 42.9% decrease in return value
- # Product Category 3: 93.9% decrease in return value
- # Product Category 4: 95.0% decrease in return value
- # Product Category 9: 49.3% decrease in return value
- # Product Category 12: 34.6% decrease in return value
- # Product Category 13: 81.3% decrease in return value
- # Product Category 14: 41.4% decrease in return value
- # Product Category 20: 92.7% decrease in return value
- # Product Category 21: 54.0% decrease in return value

# Product Category 2: 19.1% increase in return value

# Product Category 11: 37.4% increase in return value

### In order to further access the impact of BOPS implementation on return value, we divided these in three broad groups:

# No Impact: 5,6,7

# Low Impact(Decrease<50%): 1,9,12,14,

# High Impact (Decrease>50%): cat. 3,4,13,20,21.

# Also, we see an increase in return value for categories 2 and 11.

=====IMPACT ON SALES VALUE=====####

```
ols62 = lm(log_salesvalue~BIE_timeline*group_store*product_category+ month_dummy+
avg_female+avg_age+avg_income + avg_homeowner + avg_childowner, data = sales6)
```

```
stargazer(ols62,
 title="Regression Results", type="text",
 column.labels=c("Model-sales value "),
 df=FALSE, digits=2, star.cutoffs = c(0.05,0.01,0.001))
```

# Check for heteroskedasticity

```
gqttest(ols62) # Goldfeld-Quandt test indicates heteroskedasticity
```

```
bptest(ols62) # Breusch-Pagan test indicates heteroskedasticity
```

Goldfeld-Quandt test

```
data: ols62
GQ = 0.44219, df1 = 10414, df2 = 10413, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2
```

```
> bptest(ols62) # Breusch-Pagan test indicates heteroskedasticity
```

studentized Breusch-Pagan test

```
data: ols62
BP = 1104.4, df = 79, p-value < 2.2e-16
```

# Since there is heteroskedasticity in the data, we will replace SEs with clustered robust SEs.

```
HWrobstdr <- sqrt(diag(vcovHC(ols62, type="HC1"))) # produces Huber-White robust standard errors
```

```
clusrobstdr <- sqrt(diag(cluster.vcov(ols62, sales6$store_number))) # produces clustered robust
standard errors using store_number as clustering variable
```

| Values      |       |     |        |         |         |               |
|-------------|-------|-----|--------|---------|---------|---------------|
| clusrobstdr | Named | num | [1:80] | 0.05942 | 0.01047 | 0.9756...     |
| HWrobstdr   | Named | num | [1:80] | 0.141   | 0.119   | 0.123 0.13... |

```
stargazer(ols62, ols62, ols62,
```

```
 se=list(NULL, HWrobstdr, clusrobstdr),
```

```
 title="Regression Results", type="text",
```

```
 column.labels=c("Normal SE", "HW-Robust SE", "Clustered SE"),
```

```
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001)) # displays normal/HW robust/clustered robust
```

standard errors.

| Regression Results                 |           |              |                         |
|------------------------------------|-----------|--------------|-------------------------|
| Dependent variable: log_salesvalue |           |              |                         |
|                                    | Normal SE | HW-Robust SE | Clustered SE            |
| (1)                                | (2)       | (3)          |                         |
| BIE_timeline1                      | 0.493*    | 0.493***     | 0.493***                |
|                                    | (0.230)   | (0.119)      | (0.010)                 |
| group_store                        | 1.533***  | 1.533***     | 1.533                   |
|                                    | (0.203)   | (0.123)      | (0.976)                 |
| product_category2                  | -1.268*** | -1.268***    | -1.268***               |
|                                    | (0.261)   | (0.135)      | (0.003)                 |
| product_category3                  | 0.037     | 0.037        | 0.037***                |
|                                    | (0.256)   | (0.136)      | (0.006)                 |
| product_category4                  | -0.084    | -0.084       | -0.084***               |
|                                    | (0.227)   | (0.126)      | (0.008)                 |
| product_category5                  | -0.421    | -0.421***    | -0.421***               |
|                                    | (0.224)   | (0.121)      | (0.008)                 |
| product_category6                  | -1.076*** | -1.076***    | -1.076***               |
|                                    | (0.250)   | (0.129)      | (0.004)                 |
| product_category7                  | -2.098*** | -2.098***    | -2.098***               |
|                                    | (0.230)   | (0.126)      | (0.011)                 |
| product_category8                  | -1.650*** | -1.650***    | -1.650                  |
|                                    | (0.126)   | (0.106)      | (0.915)                 |
| product_category9                  | -2.800*** | -2.800***    | -2.800***               |
|                                    | (0.517)   | (0.368)      | (0.015)                 |
| month_dummy5                       | 0.216***  | 0.216***     | 0.216***                |
|                                    | (0.054)   | (0.059)      | (0.060)                 |
| month_dummy6                       | 0.005     | 0.005        | 0.005                   |
|                                    | (0.056)   | (0.057)      | (0.143)                 |
| month_dummy7                       | -0.005    | -0.005       | -0.005                  |
|                                    | (0.056)   | (0.057)      | (0.050)                 |
| month_dummy8                       | 0.012     | 0.012        | 0.012                   |
|                                    | (0.051)   | (0.054)      | (0.107)                 |
| month_dummy9                       | 0.056     | 0.056        | 0.056                   |
|                                    | (0.053)   | (0.055)      | (0.049)                 |
| month_dummy10                      | 0.004     | 0.004        | 0.004                   |
|                                    | (0.057)   | (0.060)      | (0.059)                 |
| month_dummy11                      | 0.410***  | 0.410***     | 0.410***                |
|                                    | (0.054)   | (0.057)      | (0.057)                 |
| month_dummy12                      | 1.014***  | 1.014***     | 1.014***                |
|                                    | (0.052)   | (0.055)      | (0.090)                 |
| avg_female                         | -0.394*** | -0.394***    | -0.394***               |
|                                    | (0.048)   | (0.064)      | (0.087)                 |
| avg_age                            | -0.064*** | -0.064***    | -0.064***               |
|                                    | (0.006)   | (0.008)      | (0.008)                 |
| avg_income                         | 0.104***  | 0.104***     | 0.104***                |
|                                    | (0.011)   | (0.015)      | (0.008)                 |
| avg_homeowner                      | -0.194*** | -0.194*      | -0.194***               |
|                                    | (0.055)   | (0.077)      | (0.042)                 |
| BIE_timeline1:product_category12   | -0.318    | -0.318*      | -0.318***               |
|                                    | (0.275)   | (0.158)      | (0.008)                 |
| BIE_timeline1:product_category13   | -0.831**  | -0.831***    | -0.831***               |
|                                    | (0.297)   | (0.163)      | (0.002)                 |
| BIE_timeline1:product_category14   | 0.067     | 0.067        | 0.067***                |
|                                    | (0.367)   | (0.183)      | (0.014)                 |
| BIE_timeline1:product_category15   | 1.304     | 1.304**      | 1.304***                |
|                                    | (0.874)   | (0.478)      | (0.001)                 |
| BIE_timeline1:product_category17   | -0.397*   | -0.397**     | -0.397***               |
|                                    | (0.172)   | (0.135)      | (0.028)                 |
| BIE_timeline1:product_category20   | -0.214    | -0.214       | -0.214***               |
|                                    | (0.295)   | (0.151)      | (0.006)                 |
| BIE_timeline1:product_category21   | -0.055    | -0.055       | -0.055***               |
|                                    | (0.277)   | (0.151)      | (0.001)                 |
| group_store:product_category2      | 0.286     | 0.286        | 0.286***                |
|                                    | (0.278)   | (0.166)      | (0.021)                 |
| group_store:product_category3      | -0.204    | -0.204       | -0.204***               |
|                                    | (0.274)   | (0.168)      | (0.027)                 |
| group_store:product_category4      | 0.320     | 0.320*       | 0.320***                |
|                                    | (0.245)   | (0.159)      | (0.036)                 |
| group_store:product_category5      | 0.302     | 0.302        | 0.302**                 |
|                                    | (0.243)   | (0.157)      | (0.110)                 |
| group_store:product_category6      | -0.017    | -0.017       | -0.017                  |
|                                    | (0.268)   | (0.163)      | (0.047)                 |
| product_category10                 |           |              | -2.814***               |
|                                    |           |              | (0.172) (0.146) (0.946) |
| product_category11                 |           |              | -0.400                  |
|                                    |           |              | (0.237) (0.135) (0.014) |
| product_category12                 |           |              | -0.573*                 |
|                                    |           |              | (0.225) (0.127) (0.011) |
| product_category13                 |           |              | -0.550*                 |
|                                    |           |              | (0.241) (0.131) (0.004) |
| product_category14                 |           |              | -2.772***               |
|                                    |           |              | (0.279) (0.130) (0.004) |
| product_category15                 |           |              | -3.708***               |
|                                    |           |              | (0.355) (0.361) (0.975) |
| product_category17                 |           |              | 0.492***                |
|                                    |           |              | (0.124) (0.093) (0.973) |
| product_category20                 |           |              | -0.636*                 |
|                                    |           |              | (0.241) (0.125) (0.008) |
| product_category21                 |           |              | -0.894***               |
|                                    |           |              | (0.226) (0.121) (0.007) |
| month_dummy2                       |           |              | 0.413***                |
|                                    |           |              | (0.055) (0.057) (0.113) |
| month_dummy3                       |           |              | 0.034                   |
|                                    |           |              | (0.055) (0.059) (0.062) |
| month_dummy4                       |           |              | -0.001                  |
|                                    |           |              | (0.056) (0.058) (0.109) |
| avg_childowner                     |           |              | 0.062                   |
|                                    |           |              | (0.051) (0.071) (0.114) |
| BIE_timeline1:group_store          |           |              | -0.377*                 |
|                                    |           |              | (0.248) (0.155) (0.019) |
| BIE_timeline1:product_category2    |           |              | -0.212                  |
|                                    |           |              | (0.316) (0.171) (0.005) |
| BIE_timeline1:product_category3    |           |              | -0.407                  |
|                                    |           |              | (0.308) (0.167) (0.004) |
| BIE_timeline1:product_category4    |           |              | 0.089                   |
|                                    |           |              | (0.276) (0.157) (0.003) |
| BIE_timeline1:product_category5    |           |              | -0.387                  |
|                                    |           |              | (0.275) (0.152) (0.005) |
| BIE_timeline1:product_category6    |           |              | -0.316                  |
|                                    |           |              | (0.309) (0.156) (0.002) |
| BIE_timeline1:product_category7    |           |              | -0.403                  |
|                                    |           |              | (0.284) (0.156) (0.007) |
| BIE_timeline1:product_category8    |           |              | -1.349***               |
|                                    |           |              | (0.220) (0.194) (0.109) |
| BIE_timeline1:product_category9    |           |              | 0.821                   |
|                                    |           |              | (0.552) (0.388) (0.013) |
| BIE_timeline1:product_category10   |           |              | -0.016                  |
|                                    |           |              | (0.380) (0.298) (0.008) |
| BIE_timeline1:product_category11   |           |              | -0.430**                |
|                                    |           |              | (0.289) (0.163) (0.011) |
| group_store:product_category7      |           |              | -0.896***               |
|                                    |           |              | (0.255) (0.166) (0.557) |
| group_store:product_category8      |           |              |                         |
| group_store:product_category9      |           |              | -1.501**                |
|                                    |           |              | (0.541) (0.393) (0.872) |
| group_store:product_category10     |           |              |                         |
| group_store:product_category11     |           |              | -0.383*                 |
|                                    |           |              | (0.257) (0.170) (0.056) |
| group_store:product_category12     |           |              | 0.520*                  |
|                                    |           |              | (0.244) (0.164) (0.197) |
| group_store:product_category13     |           |              | -0.554*                 |
|                                    |           |              | (0.261) (0.161) (0.139) |
| group_store:product_category14     |           |              | 0.651*                  |
|                                    |           |              | (0.297) (0.182) (0.584) |
| group_store:product_category15     |           |              |                         |
| group_store:product_category17     |           |              |                         |
| group_store:product_category20     |           |              | -0.070                  |
|                                    |           |              | (0.261) (0.157) (0.081) |
| group_store:product_category21     |           |              | 0.403                   |
|                                    |           |              | (0.245) (0.156) (0.033) |

|                                              |                   |                   |                     |                                              |                    |                     |                    |
|----------------------------------------------|-------------------|-------------------|---------------------|----------------------------------------------|--------------------|---------------------|--------------------|
| BIE_timeline1:group_store:product_category2  | -0.083<br>(0.342) | -0.083<br>(0.220) | -0.083<br>(0.044)   | BIE_timeline1:group_store:product_category14 | -0.790*<br>(0.393) | -0.790**<br>(0.245) | -0.790<br>(0.782)  |
| BIE_timeline1:group_store:product_category3  | 0.296<br>(0.337)  | 0.296<br>(0.218)  | 0.296***<br>(0.003) | BIE_timeline1:group_store:product_category15 |                    |                     |                    |
| BIE_timeline1:group_store:product_category4  | -0.183<br>(0.304) | -0.183<br>(0.210) | -0.183<br>(0.121)   | BIE_timeline1:group_store:product_category17 |                    |                     |                    |
| BIE_timeline1:group_store:product_category5  | 0.201<br>(0.303)  | 0.201<br>(0.206)  | 0.201***<br>(0.007) | BIE_timeline1:group_store:product_category20 | 0.286<br>(0.325)   | 0.286<br>(0.204)    | 0.286**<br>(0.104) |
| BIE_timeline1:group_store:product_category6  | 0.343<br>(0.335)  | 0.343<br>(0.207)  | 0.343***<br>(0.041) | BIE_timeline1:group_store:product_category21 | 0.062<br>(0.304)   | 0.062<br>(0.205)    | 0.062<br>(0.088)   |
| BIE_timeline1:group_store:product_category7  | 0.220<br>(0.320)  | 0.220<br>(0.220)  | 0.220<br>(0.206)    | Constant                                     |                    | 6.970**<br>(0.205)  | 6.970**<br>(0.141) |
| BIE_timeline1:group_store:product_category8  |                   |                   |                     |                                              |                    | 6.970**<br>(0.141)  | 6.970**<br>(0.059) |
| BIE_timeline1:group_store:product_category9  | 1.032<br>(0.586)  | 1.032*<br>(0.437) | 1.032***<br>(0.205) | Observations                                 | 21,003             | 21,003              | 21,003             |
| BIE_timeline1:group_store:product_category10 |                   |                   |                     | R2                                           | 0.338              | 0.338               | 0.338              |
| BIE_timeline1:group_store:product_category11 | 0.238<br>(0.319)  | 0.238<br>(0.219)  | 0.238***<br>(0.030) | Adjusted R2                                  | 0.335              | 0.335               | 0.335              |
| BIE_timeline1:group_store:product_category12 | 0.153<br>(0.303)  | 0.153<br>(0.213)  | 0.153***<br>(0.022) | Residual Std. Error                          | 1.592              | 1.592               | 1.592              |
| BIE_timeline1:group_store:product_category13 | 0.509<br>(0.326)  | 0.509*<br>(0.211) | 0.509***<br>(0.041) | F Statistic                                  | 135.036***         | 135.036***          | 135.036***         |

### Since we cannot interpret the results of a triple interaction model, we will analyse the impact of BOPS implementation on individual categories by subsetting the data further. This will help us understand how sales value is changing for each category w.r.t store groups(group 0 = 5998 and group 1 = 2&6).

###-----Marginal Effects -----###

```
meffects62 <- ggpredict(ols62, terms=c("BIE_timeline", "group_store", "product_category"))
```

|   | x | predicted | conf.low | conf.high | group | facet |
|---|---|-----------|----------|-----------|-------|-------|
| 1 | 0 | 6.899337  | 6.518658 | 7.280016  | 0     | 1     |
| 2 | 0 | 5.631111  | 5.273560 | 5.988662  | 0     | 2     |
| 3 | 0 | 6.936172  | 6.593506 | 7.278839  | 0     | 3     |
| 4 | 0 | 6.815450  | 6.563122 | 7.067778  | 0     | 4     |
| 5 | 0 | 6.478612  | 6.234665 | 6.722559  | 0     | 5     |

Showing 1 to 6 of 72 entries

# Replacing by actual variable names for convenience

```
meffects62_colnames <- meffects62[c("x", "predicted", "group", "facet")]
```

BA Project\_BOPS\_Final Submitted.Rmd x meffects62\_colnames x meffects62 x

|   | x | predicted | group | facet |
|---|---|-----------|-------|-------|
| 1 | 0 | 6.899337  | 0     | 1     |
| 2 | 0 | 5.631111  | 0     | 2     |
| 3 | 0 | 6.936172  | 0     | 3     |
| 4 | 0 | 6.815450  | 0     | 4     |
| 5 | 0 | 6.478612  | 0     | 5     |

Showing 1 to 6 of 72 entries

```
colnames(meffects62_colnames) <- c("BIE_timeline", "predicted_sales_value", "group_store", "product_category")
```

BA Project\_BOPS\_Final Submitted.Rmd x meffects62\_colnames x meffects62 x

|   | BIE_timeline | predicted_sales_value | group_store | product_category |
|---|--------------|-----------------------|-------------|------------------|
| 1 | 0            | 6.899337              | 0           | 1                |
| 2 | 0            | 5.631111              | 0           | 2                |
| 3 | 0            | 6.936172              | 0           | 3                |
| 4 | 0            | 6.815450              | 0           | 4                |
| 5 | 0            | 6.478612              | 0           | 5                |

Showing 1 to 6 of 72 entries

```
levels(meffects62_colnames$product_category) <- c('1-Bridal', '2-Gold Wed Bands', '3-Solitaires', '4-Diamond Fashion', '5-Semi Precious', '6-Mens', '7-Gold Earrings', '8-In House Special Event', '9-Beads', '10-Piercings / Close Out', '11-Diamond Solitaires Jewelry', '12-Gold Chain / Jewelry', '13-Watches', '14-Pre-Owned', '15-Specialized Jewelry', '17-Events', '19-Repair / Warranty', '20-Diamond Wedding Bands', '21-Sterling Silver')
```

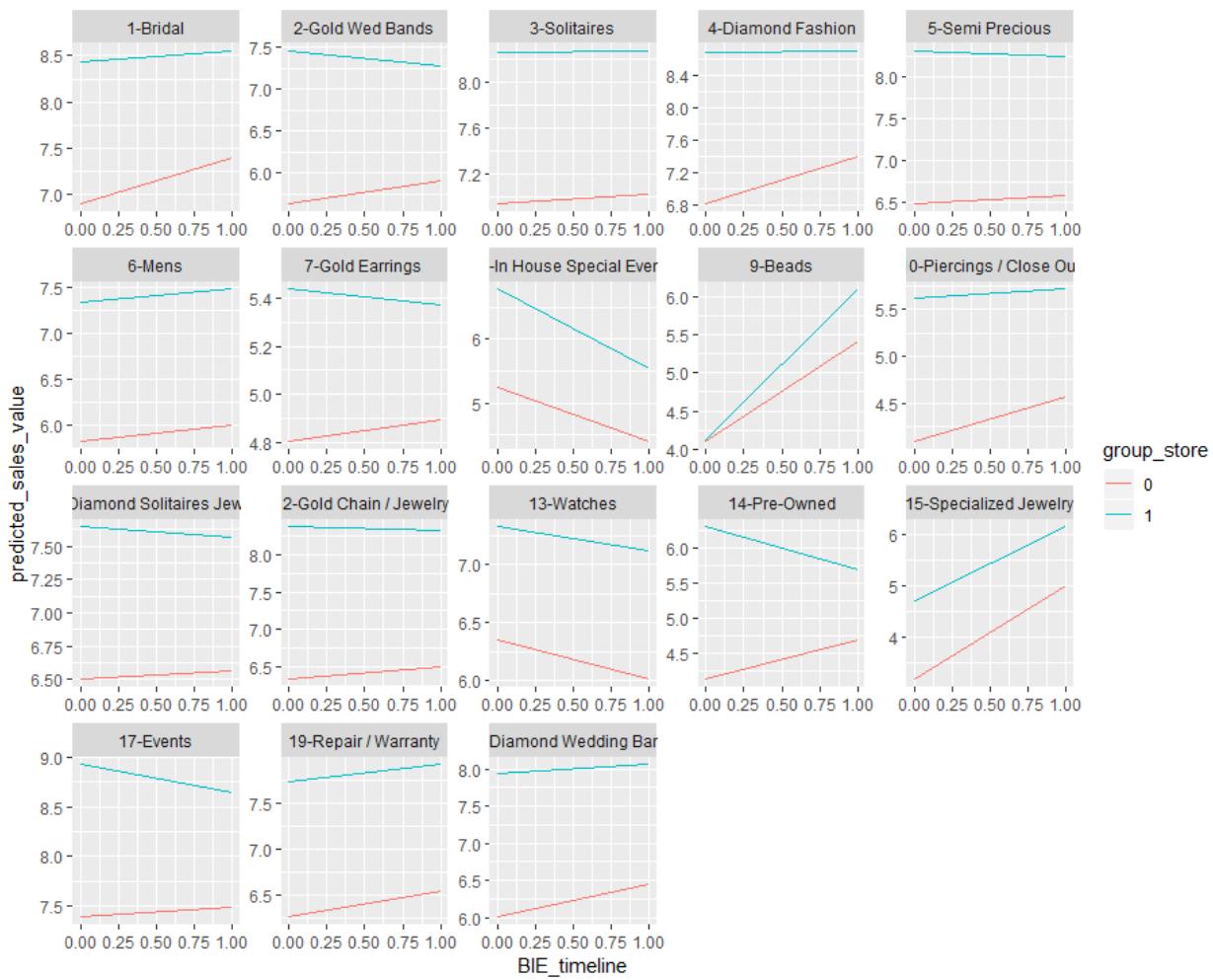
BA Project\_BOPS\_Final Submitted.Rmd x meffects62\_colnames x meffects62 x

|   | BIE_timeline | predicted_sales_value | group_store | product_category  |
|---|--------------|-----------------------|-------------|-------------------|
| 1 | 0            | 6.899337              | 0           | 1-Bridal          |
| 2 | 0            | 5.631111              | 0           | 2-Gold Wed Bands  |
| 3 | 0            | 6.936172              | 0           | 3-Solitaires      |
| 4 | 0            | 6.815450              | 0           | 4-Diamond Fashion |
| 5 | 0            | 6.478612              | 0           | 5-Semi Precious   |

Showing 1 to 6 of 72 entries

```
ggplot(meffects62_colnames, aes(BIE_timeline, y= predicted_sales_value, colour =group_store)) +
 geom_line() +
 facet_wrap(product_category ~ ., scales="free")
```

Plot Zoom



### Checking predicted values for all the product categories (from 1 to 21) and analyzing impact of BOPS implementation for both storegroups(group 0 = 5998 and group 1 = 2 and 6).

```
df2_pc1<-subset(sales6, product_category==1)
```

|    | store_number | year | month | month_index | product_category | month_dummy | bops_in_effect | day | salesvalue | returnvalue | salesquantity | returnquantity | avg_fem |
|----|--------------|------|-------|-------------|------------------|-------------|----------------|-----|------------|-------------|---------------|----------------|---------|
| 13 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 2   | 12253.53   | 1478.82     | 13            | 2              | 8       |
| 33 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 3   | 7989.74    | 1287.40     | 22            | 3              | 8       |
| 45 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 4   | 26309.46   | 10614.14    | 26            | 5              | 8       |
| 61 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 5   | 6399.69    | 771.66      | 12            | 1              | 8       |
| 75 | 2            | 2010 | AUG   | 13          | 1                | 8           | 0              | 6   | 14792.14   | 2142.20     | 14            | 4              | 8       |

Showing 1 to 6 of 1,381 entries

|    | returnquantity | avg_female | avg_age  | avg_income | avg_homeowner | avg_residency | avg_childowner | BIE_timeline | group_store | log_salesvalue | log_returnvalue |
|----|----------------|------------|----------|------------|---------------|---------------|----------------|--------------|-------------|----------------|-----------------|
| 13 | 2              | 0.4545455  | 4.615385 | 5.769231   | 0.3076923     | 6.846154      | 0.07692308     | 0            | 1           | 9.413651       | 7.299676        |
| 22 | 3              | 0.5555556  | 3.727273 | 4.590909   | 0.4090909     | 4.863636      | 0.27272728     | 0            | 1           | 8.986039       | 7.161156        |
| 26 | 5              | 0.4400000  | 5.461538 | 5.115385   | 0.5769231     | 6.000000      | 0.42307693     | 0            | 1           | 10.177722      | 9.270037        |
| 12 | 1              | 0.5000000  | 7.250000 | 3.750000   | 0.5833333     | 7.333333      | 0.25000000     | 0            | 1           | 8.764161       | 6.649839        |
| 11 | 4              | 0.2626264  | 6.777777 | 3.777777   | 0.5858585     | 6.777777      | 0.18181818     | 0            | 1           | 8.601312       | 6.653375        |

Showing 1 to 6 of 1,381 entries

```

ols2_pc1= lm(log_salesvalue~BIE_timeline*group_store+ month_dummy+
avg_female+avg_age+avg_income+ avg_homeowner + avg_chldowner, data = df2_pc1)

stargazer(ols2_pc1,
 title="Regression Results", type="text",
 column.labels=c("ME-pc1"),
 df=FALSE, digits=4, star.cutoffs = c(0.05,0.01,0.001))

Check for heteroskedasticity
gqtest(ols2_pc1) # Goldfeld-Quandt test indicates no heteroskedasticity
bptest(ols2_pc1) # Breusch-Pagan test indicates heteroskedasticity

> gqtest(ols2_pc1) # Goldfeld-Quandt test indicates no heteroskedasticity

 Goldfeld-Quandt test

data: ols2_pc1
GQ = 0.44456, df1 = 671, df2 = 670, p-value = 1
alternative hypothesis: variance increases from segment 1 to 2

> bptest(ols2_pc1) # Breusch-Pagan test indicates heteroskedasticity

 studentized Breusch-Pagan test

data: ols2_pc1
BP = 95.957, df = 19, p-value = 0.000000000000287

```

```

Since there is heteroskedasticity in the data, we will replace SEs with robust SEs.
HWrobstdter <- sqrt(diag(vcovHC(ols2_pc1, type="HC1"))) # produces Huber-White robust standard
errors
clusrobstdter <- sqrt(diag(cluster.vcov(ols2_pc1, sales6$store_number))) # produces clustered robust
standard errors

```

| Values        |                                                       |
|---------------|-------------------------------------------------------|
| clusrobstdter | Named num [1:80] 0.05942 0.01047 0.97567 0.00339 0... |
| HWrobstdter   | Named num [1:20] 0.343 0.118 0.127 0.205 0.242 ...    |

```

stargazer(ols2_pc1, ols2_pc1, ols2_pc1,
 se=list(NULL, HWrobstdter, clusrobstdter),
 title=" Regression Results", type="text",
 column.labels=c("Normal SE", "HW-Robust SE", "Clustered SE"),
 df=FALSE, digits=3, star.cutoffs = c(0.05,0.01,0.001)) # displays normal/HW robust/clustered robust
standard errors. With clustered robust standard errors

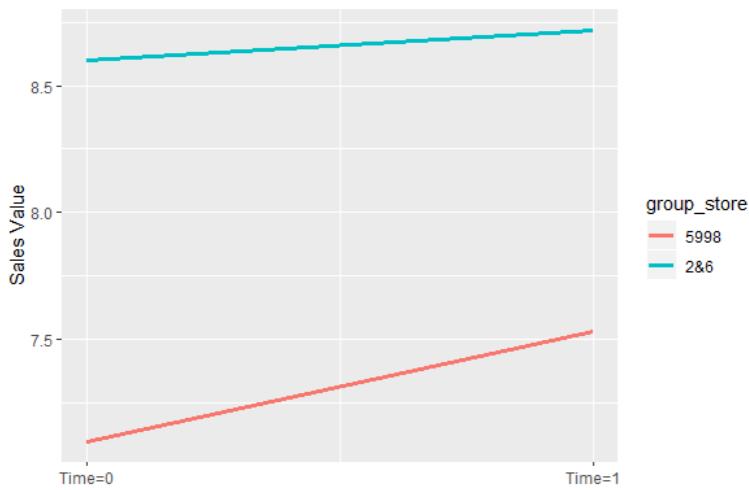
```

| Regression Results         |  |  |  | month_dummy9                  | 0.100<br>(0.213)    | 0.100<br>(0.206)    | 0.100*<br>(0.049)    |
|----------------------------|--|--|--|-------------------------------|---------------------|---------------------|----------------------|
|                            |  |  |  | month_dummy10                 | -0.011<br>(0.227)   | -0.011<br>(0.217)   | -0.011<br>(0.059)    |
|                            |  |  |  | month_dummy11                 | 0.121<br>(0.215)    | 0.121<br>(0.209)    | 0.121*<br>(0.057)    |
|                            |  |  |  | month_dummy12                 | 0.552**<br>(0.208)  | 0.552**<br>(0.200)  | 0.552***<br>(0.090)  |
|                            |  |  |  | avg_female                    | -0.086<br>(0.172)   | -0.086<br>(0.211)   | -0.086<br>(0.087)    |
|                            |  |  |  | avg_age                       | -0.054*<br>(0.023)  | -0.054<br>(0.028)   | -0.054***<br>(0.008) |
|                            |  |  |  | avg_income                    | 0.108**<br>(0.039)  | 0.108*<br>(0.053)   | 0.108***<br>(0.008)  |
|                            |  |  |  | avg_homeowner                 | -0.222<br>(0.188)   | -0.222<br>(0.259)   | -0.222***<br>(0.042) |
|                            |  |  |  | avg_childdowner               | 0.075<br>(0.181)    | 0.075<br>(0.256)    | 0.075<br>(0.114)     |
|                            |  |  |  | BIE_timeline1:group_store     | -0.313<br>(0.248)   | -0.313*<br>(0.154)  | -0.313***<br>(0.019) |
|                            |  |  |  | Constant                      | 6.960***<br>(0.334) | 6.960***<br>(0.343) | 6.960***<br>(0.059)  |
|                            |  |  |  | Observations                  | 1,381               | 1,381               | 1,381                |
|                            |  |  |  | R2                            | 0.104               | 0.104               | 0.104                |
| <b>Observations</b>        |  |  |  | <b>1,381</b>                  | <b>1,381</b>        | <b>1,381</b>        |                      |
| <b>R2</b>                  |  |  |  | <b>0.104</b>                  | <b>0.104</b>        | <b>0.104</b>        |                      |
| <b>Adjusted R2</b>         |  |  |  | <b>0.091</b>                  | <b>0.091</b>        | <b>0.091</b>        |                      |
| <b>Residual Std. Error</b> |  |  |  | <b>1.581</b>                  | <b>1.581</b>        | <b>1.581</b>        |                      |
| <b>F Statistic</b>         |  |  |  | <b>8.289***</b>               | <b>8.289***</b>     | <b>8.289***</b>     |                      |
| <hr/>                      |  |  |  |                               |                     |                     |                      |
| <b>Note:</b>               |  |  |  | *p<0.05; **p<0.01; ***p<0.001 |                     |                     |                      |
| <hr/>                      |  |  |  |                               |                     |                     |                      |

```
meffects2_pc1 <- ggpredict(ols2_pc1, terms=c("BIE_timeline", "group_store")) # generates a tidy data frame
```

|   |           | BA Project_BOPS_Final Submitted.Rmd | meffects2_pc1 | df2_pc1    |
|---|-----------|-------------------------------------|---------------|------------|
|   |           | Filter                              |               |            |
| x | predicted | conf.low                            | conf.high     | group      |
| 1 | 0         | 7.097919                            | 6.610979      | 7.584860 0 |
| 2 | 0         | 8.598620                            | 8.270955      | 8.926285 1 |
| 3 | 1         | 7.532005                            | 7.137703      | 7.926307 0 |
| 4 | 1         | 8.719334                            | 8.396289      | 9.042378 1 |

```
ggplot(meffects2_pc1,aes(x, predicted, colour=group)) + geom_line(size=1.3) +
 xlab("BOPS Timeline") + ylab("Sales Value") +
 labs(colour="group_store") +
 scale_colour_discrete(labels=c("5998","2&6")) +
 scale_x_continuous(breaks=c(0,1), labels=c("Time=0", "Time=1")) +
 theme(axis.title.x=element_blank())
```



### Interaction coefficient is insignificant for categories - 6,7

### However, there was no coefficient displayed for categories - 8,10,15,17, because data is available for only one store group. So, we cannot analyse these categories.

### Interaction coefficient is significant for categories - 1,2,3,4,5,9,11,12,13,14,20,21

## Therefore, BOPS implementation for these categories is associated with:

- # Product Category 1: 31.3% decrease in sales value
- # Product Category 2: 38.8% decrease in sales value
- # Product Category 3: 6.4% decrease in sales value
- # Product Category 4: 62% decrease in sales value
- # Product Category 5: 27.2% decrease in sales value
- # Product Category 11: 16.9% decrease in sales value
- # Product Category 12: 31.7% decrease in sales value
- # Product Category 14: 114% decrease in sales value
- # Product Category 20: 5.7% decrease in sales value
- # Product Category 21: 39.3% decrease in sales value

# Product Category 9: 35% increase in sales value

# Product Category 13: 12.2% increase in sales value

### In order to further access the impact of BOPS implementation on sales value, we divided these in three broad groups:

- # No Impact(insignificant): cat. 6,7
- # Low Impact(Decrease<30%): cat. 3,5, 11,20
- # High Impact (Decrease>50%): cat. 1,2,12,21,4,14

# Also, we see an increase in sales value for categories 9 and 13.

...