



Presented By:
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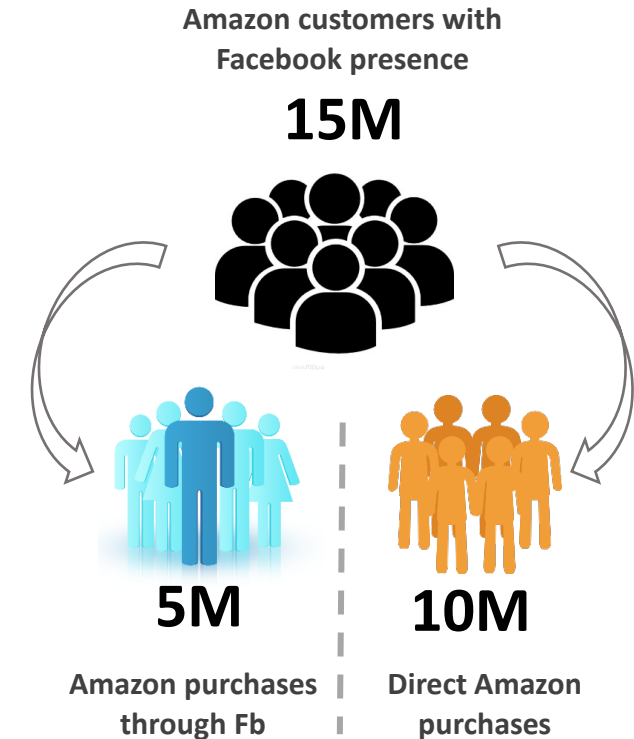
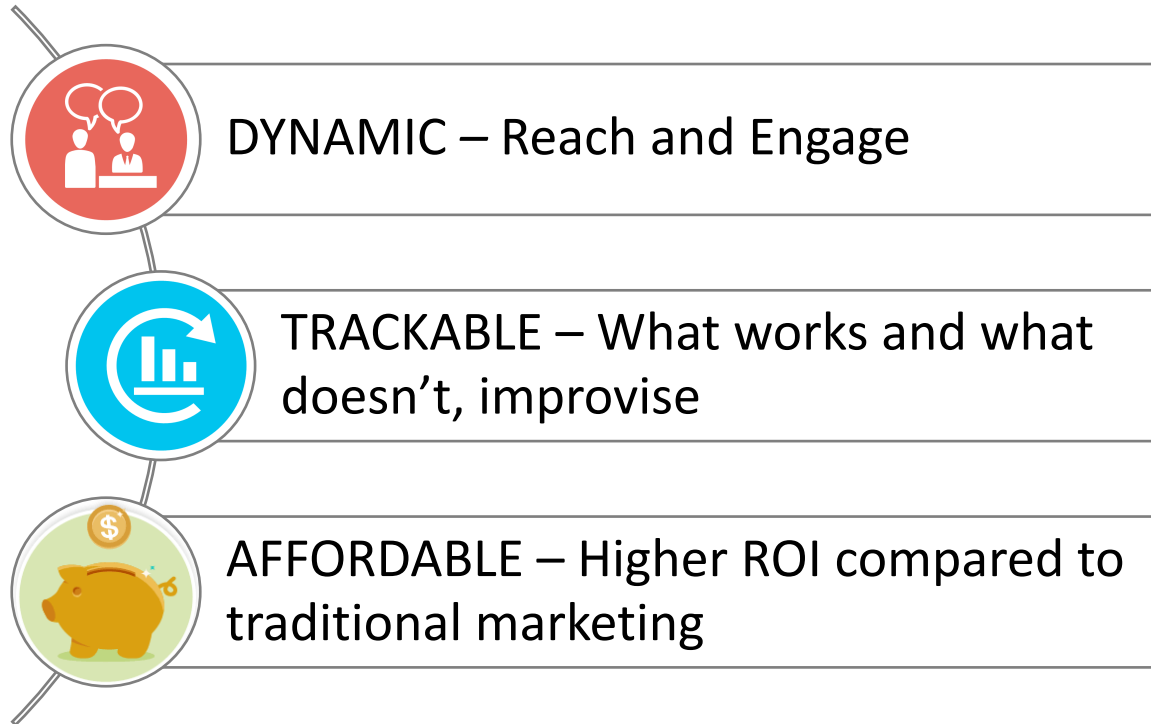
Agenda

- Business Context
- Research Question
- Data Overview
- Analysis
- Insights
- Recommendations
- Limitations



Business Context

Amazon relies heavily on digital marketing:



Facebook gets the biggest share with an annual spend of **\$100M!!**

Research Question

What is the impact of Facebook advertising on Amazon's revenue?

Is it **4X** the advertising cost?

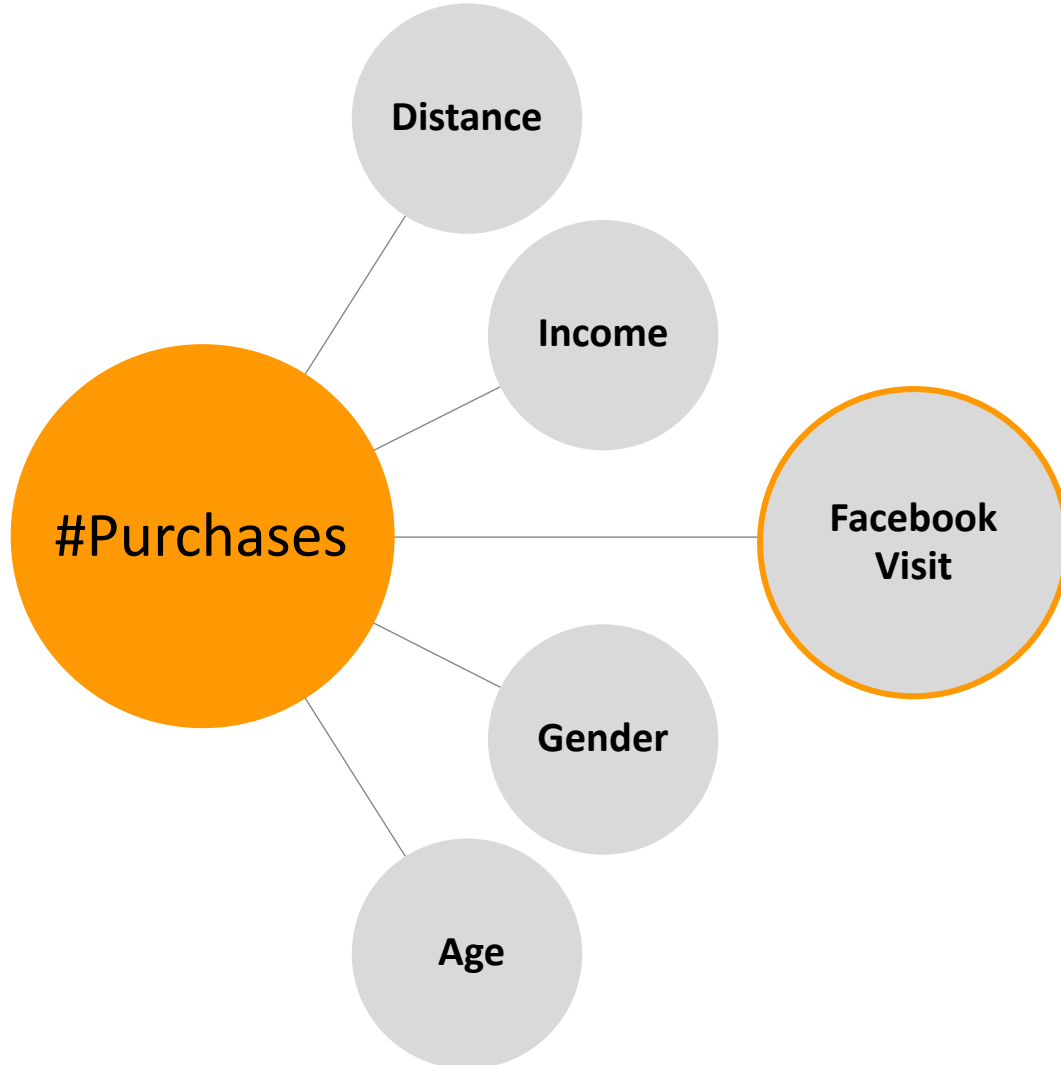


100M



400M

Data Overview



Facebook visit

All the purchases after Facebook visit

All the purchases directly through Amazon



1225



2422

Sample data available for customers from Northern California (3677)



Analysis

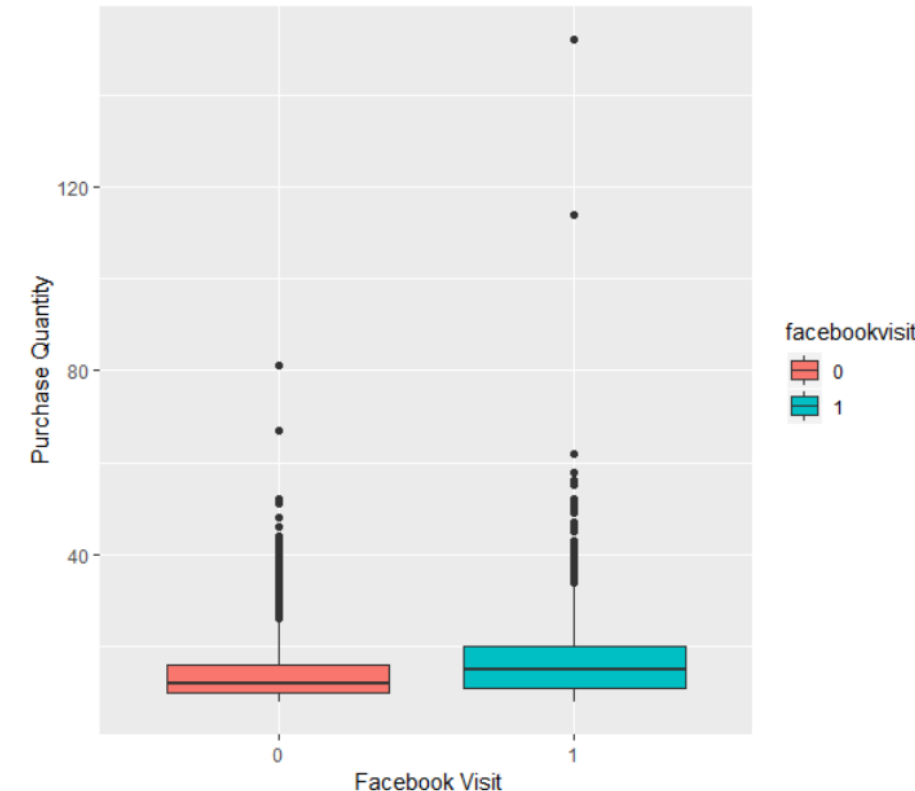
Descriptive statistics by group

group: 0 (Purchase directly through Amazon)

	vars	n	mean	sd	median	trimmed	mad	min	max	range
distance	1	2452	1.50	1.18	1	1.41	1.48	0	6	6
purchase	2	2452	13.83	6.09	12	12.87	4.45	8	81	73
income	3	2452	11.69	3.69	12	12.05	2.97	0	17	17
gender	4	2452	0.10	0.31	0	0.01	0.00	0	1	1
facebookvisit	5	2452	0.00	0.00	0	0.00	0.00	0	0	0
cust_age	6	2452	33.25	5.99	32	32.87	7.41	25	50	25

group: 1 (Purchase after Facebook visit)

	vars	n	mean	sd	median	trimmed	mad	min	max	range
distance	1	1225	2.54	1.40	2	2.48	1.48	0	8	8
purchase	2	1225	16.80	9.17	15	15.46	5.93	8	152	144
income	3	1225	10.16	3.90	11	10.37	2.97	0	17	17
gender	4	1225	0.29	0.45	0	0.24	0.00	0	1	1
facebookvisit	5	1225	1.00	0.00	1	1.00	0.00	1	1	0
cust_age	6	1225	36.24	6.65	36	36.43	8.90	25	50	25



Analysis

Dependent variable:	
purchase	
Negative Binomial Results	
distance	1.1327*** (0.0059)
income	1.0147*** (0.0021)
cust_age	1.0010 (0.0012)
facebookvisit	1.0816*** (0.0188)
gender	1.0176 (0.0256)
Constant	9.2274*** (0.0468)
Observations	3,677
Log Likelihood	-11,331.9500
theta	12.2743*** (0.4867)
Akaike Inf. Crit.	22,675.9000
Note: *p<0.05; **p<0.01; ***p<0.001	

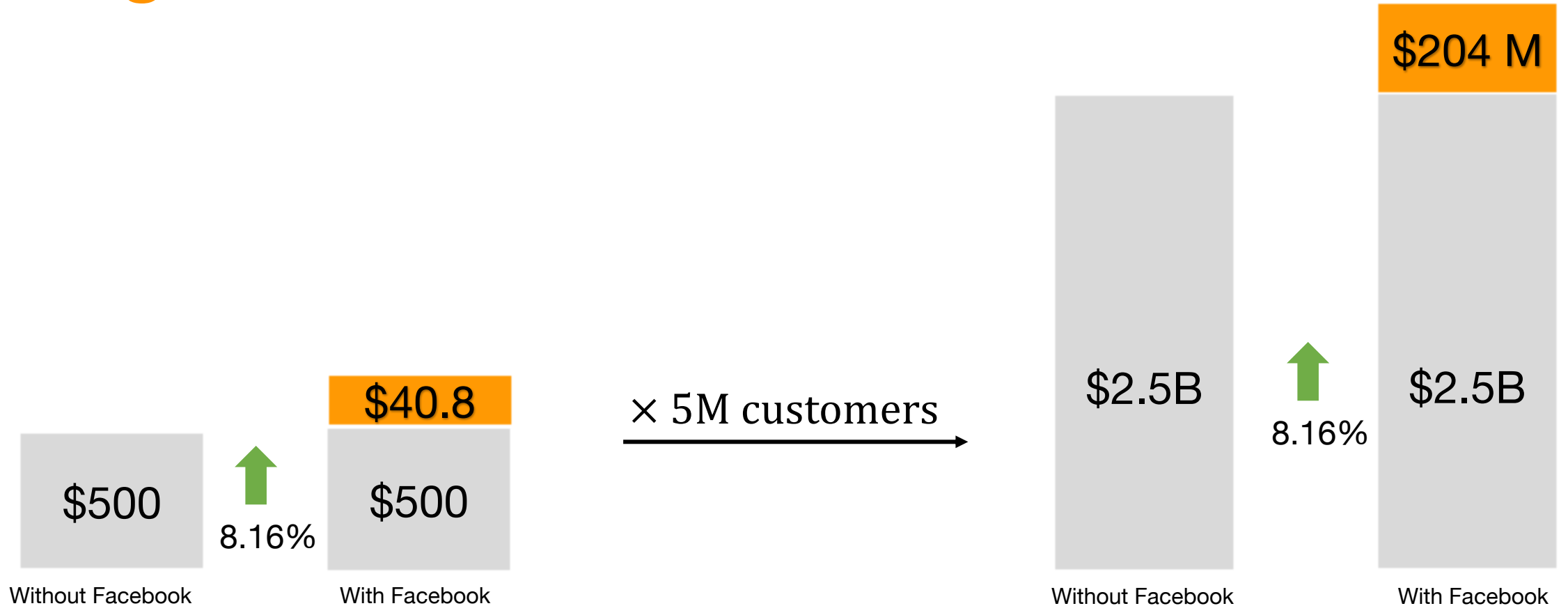
Number of purchases is **8.16%** more when the purchase is made though Facebook vs when it is made directly from Amazon.

Likelihood ratio test

```
Model 1: purchase ~ 1
Model 2: purchase ~ distance + income + cust_age + facebookvisit + gender
#Df LogLik Df Chisq Pr(>Chisq)
1 2 -11742
2 7 -11331 5 821.55 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```



Insights



204M additional revenue from purchases made through Facebook



Recommendations

- Renegotiate with Facebook to reduce Ads spending to \$50M or less.

$$\text{Advertising Cost of Spend (ACoS)} = \frac{\text{Total Ad Spend}}{\text{Total Ad Sales}} = \frac{100}{400} = \$0.25$$

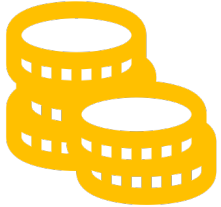
- Collect and analyze more data to better quantify impact of Facebook Ads on revenue. E.g. user might see an Ad on Facebook and later buy directly from Amazon.



Limitations



Data is limited to **Northern California Region**.



Transaction Amount for every customer is unknown.



No data on **Ad Frequency** that led to a direct Amazon purchase post **Facebook Ad Exposure**.



Thank you!



Appendix



Final Model

$$\text{Purchase} = \beta_0 + \beta_1 \text{ facebook visit} + \beta_2 \text{ income} \\ + \beta_3 \text{ gender} + \beta_4 \text{ distance} + \beta_5 \text{ cust_age}$$



Summary Statistics – All variables

Descriptive statistics by group

group: 0

	vars	n	mean	sd	median	trimmed	mad	min	max	range
income	1	2452	11.69	3.69	12	12.05	2.97	0	17	17
gender	2	2452	0.10	0.31	0	0.01	0.00	0	1	1
facebookvisit	3	2452	0.00	0.00	0	0.00	0.00	0	0	0
distance	4	2452	1.50	1.18	1	1.41	1.48	0	6	6
cust_age	5	2452	33.25	5.99	32	32.87	7.41	25	50	25
purchase	6	2452	13.83	6.09	12	12.87	4.45	8	81	73
numoffriends	7	2452	99.07	19.84	99	99.09	19.27	31	165	134
numofposts	8	2452	199.65	34.39	199	199.44	34.10	91	309	218
PublicProfile	9	2452	0.27	0.45	0	0.22	0.00	0	1	1

group: 1

	vars	n	mean	sd	median	trimmed	mad	min	max	range
income	1	1225	10.16	3.90	11	10.37	2.97	0	17	17
gender	2	1225	0.29	0.45	0	0.24	0.00	0	1	1
facebookvisit	3	1225	1.00	0.00	1	1.00	0.00	1	1	0
distance	4	1225	2.54	1.40	2	2.48	1.48	0	8	8
cust_age	5	1225	36.24	6.65	36	36.43	8.90	25	50	25
purchase	6	1225	16.80	9.17	15	15.46	5.93	8	152	144
numoffriends	7	1225	129.19	19.62	129	128.97	19.27	74	206	132
numofposts	8	1225	215.24	35.91	215	215.43	35.58	100	344	244
PublicProfile	9	1225	0.31	0.46	0	0.26	0.00	0	1	1



Multicollinearity - Model Variables

```

      distance income gender facebookvisit cust_age
distance      1.000 -0.068  0.148          0.364   0.098
income        -0.068  1.000 -0.348         -0.188  -0.098
gender         0.148 -0.348  1.000          0.235   0.026
facebookvisit  0.364 -0.188  0.235          1.000   0.221
cust_age       0.098 -0.098  0.026          0.221   1.000

```

No variable from the 5 input variables has collinearity problem.

The linear correlation coefficients ranges between:

min correlation (cust_age ~ gender): 0.02563077

max correlation (facebookvisit ~ distance): 0.3641455

----- VIFs of the remained variables -----

	Variables	VIF
1	distance	1.159531
2	income	1.159732
3	gender	1.186635
4	facebookvisit	1.263052
5	cust_age	1.058062



Endogeneity

Omitted Variable: Technology Friendliness

Endogenous Variable: Facebook Visit

Instrument Variables:

1. Number of posts
2. Number of friends
3. Public Profile

```
ivreg(formula = purchase ~ facebookvisit + distance + income +  
      cust_age + gender | numoffriends + numofposts + PublicProfile +  
      distance + income + cust_age + gender, data = mydata)
```

Residuals:

Min	1Q	Median	3Q	Max
-15.330	-3.829	-1.456	2.161	135.587

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	8.186421	0.761217	10.754	< 2e-16 ***
facebookvisit	1.407317	0.475982	2.957	0.00313 **
distance	1.895852	0.099650	19.025	< 2e-16 ***
income	0.219083	0.031933	6.861	0.000000000000801 ***
cust_age	0.005273	0.018824	0.280	0.77939
gender	0.256071	0.336440	0.761	0.44663

Diagnostic tests:

	df1	df2	statistic	p-value
Weak instruments	3	3669	565.519	<2e-16 ***
Wu-Hausman	1	3670	0.208	0.649
Sargan	2	NA	2.225	0.329

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.807 on 3671 degrees of freedom

Multiple R-Squared: 0.1539. Adjusted R-squared: 0.1528

Wald test: 131.2 on 5 and 3671 DF, p-value: < 2.2e-16



Endogeneity – IV correlation check

	numoffriends	numofposts	PublicProfile	purchase
numoffriends	1.000	0.107	0.006	0.105
numofposts	0.107	1.000	0.012	0.061
PublicProfile	0.006	0.012	1.000	0.025
purchase	0.105	0.061	0.025	1.000

No variable from the 4 input variables has collinearity problem.

The linear correlation coefficients ranges between:

min correlation (PublicProfile ~ numoffriends): 0.006197103

max correlation (numofposts ~ numoffriends): 0.1065741

----- VIFs of the remained variables -----

	Variables	VIF
1	numoffriends	1.021464
2	numofposts	1.014214
3	PublicProfile	1.000753
4	purchase	1.014286



Negative Binomial vs Poisson

```
> lrtest(poisson1, poissonempty) # poisson is not a good fit
Likelihood ratio test
```

```
Model 1: purchase ~ distance + income + cust_age + facebookvisit + gender
```

```
Model 2: purchase ~ 1
```

```
  #Df LogLik Df  Chisq Pr(>Chisq)
1    6 -12416
2    1 -13428 -5 2024.4  < 2.2e-16 ***
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Comparison with negative binomial

```
Likelihood ratio test
```

```
Model 1: purchase ~ distance + income + cust_age + facebookvisit + gender
```

```
Model 2: purchase ~ distance + income + cust_age + facebookvisit + gender
```

```
  #Df LogLik Df  Chisq Pr(>Chisq)
1    6 -12416
2    7 -11331  1 2169.1 < 2.2e-16 ***
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```



Negative Binomial vs Ideal model

Likelihood ratio test

Model 1: purchase ~ 1

Model 2: purchase ~ distance + income + cust_age + facebookvisit + gender

	#Df	LogLik	Df	Chisq	Pr(>Chisq)
1	2	-11742			
2	7	-11331	5	821.55	< 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1



Heteroskedasticity

```
> gqtest(negbin1) # Significant Goldfeld-Quandt test does not indicate heteroscedasticity
```

Goldfeld-Quandt test

```
data: negbin1  
GQ = 0.94104, df1 = 1833, df2 = 1832, p-value = 0.9033  
alternative hypothesis: variance increases from segment 1 to 2
```

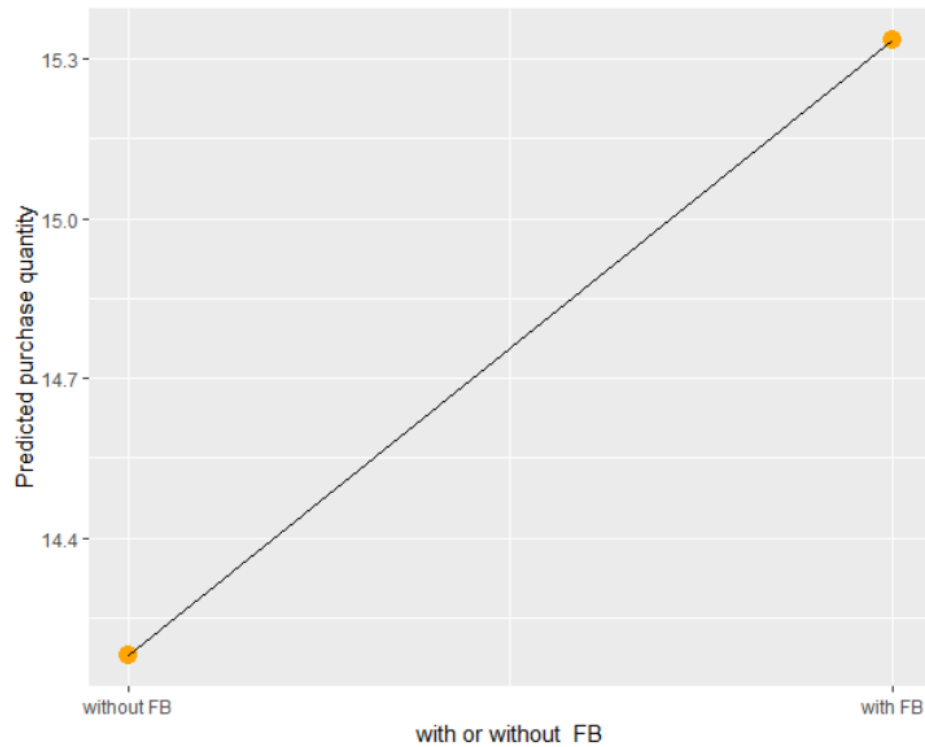
```
> bptest(negbin1) # Significant Breusch-Pagan test indicates heteroscedasticity
```

studentized Breusch-Pagan test

```
data: negbin1  
BP = 30.567, df = 5, p-value = 0.0000114
```



Predicted values



	facebookvisit	cust_age	distance	gender	income	predicted_purchase
1	0	34.24476	1.843351	0.166712	11.18031	14.17957
2	1	34.24476	1.843351	0.166712	11.18031	15.33611



Extras



Descriptive Statistics - combined

Descriptive Statistics

Statistic	N	Mean	St. Dev.	Min	Pctl(25)	Median	Pctl(75)	Max
income	3,677	11.2	3.8	0	9	12	13	17
gender	3,677	0.2	0.4	0	0	0	0	1
facebookvisit	3,677	0.3	0.5	0	0	0	1	1
distance	3,677	1.8	1.4	0	1	2	3	8
cust_age	3,677	34.2	6.4	25	29	34	39	50
purchase	3,677	14.8	7.4	8	10	13	17	152
numoffriends	3,677	109.1	24.3	31	92	108	125	206
numofposts	3,677	204.8	35.7	91	181	204	229	344
PublicProfile	3,677	0.3	0.5	0	0	0	1	1



Negative Binomial – all results

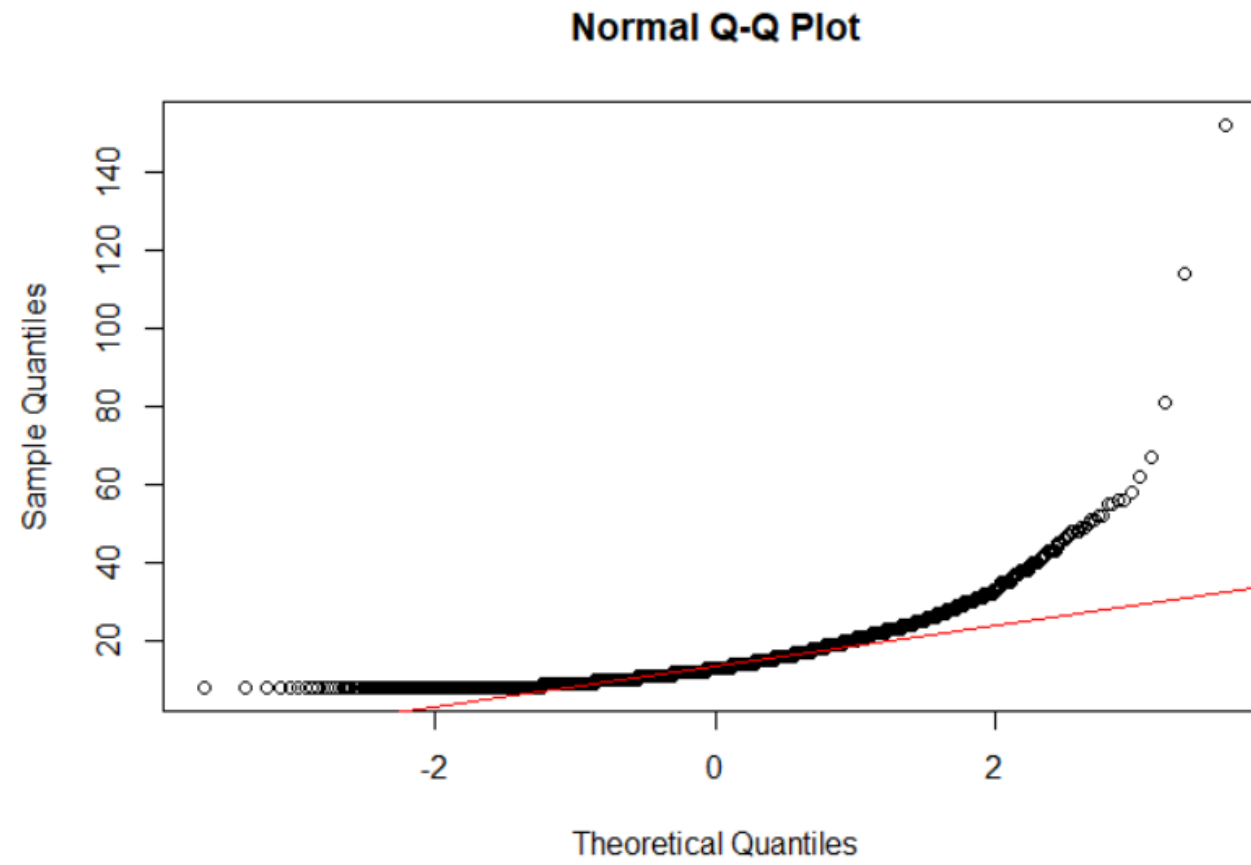
Negative Binomial Results

Dependent variable:									
	negbinempty (1)	negbin1 (2)	negbin2 (3)	negbin3 (4)	purchase negbin4 (5)	negbin5 (6)	(7)	(8)	(9)
distance		0.125*** (0.005)	0.124*** (0.005)	0.125*** (0.005)	0.125*** (0.005)	0.125*** (0.005)	0.125*** (0.005)	0.125*** (0.005)	0.124*** (0.005)
income		0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)	0.015*** (0.002)
cust_age		0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)
facebookvisit1		0.078*** (0.015)	0.072*** (0.018)	0.077*** (0.018)	0.074*** (0.015)	0.078*** (0.015)	0.077*** (0.018)	0.073*** (0.018)	0.074*** (0.015)
gender		0.017 (0.019)	0.018 (0.019)	0.017 (0.019)	0.018 (0.019)	0.017 (0.019)	0.017 (0.019)	0.018 (0.019)	0.018 (0.019)
numoffriends			0.0001 (0.0003)	0.00004 (0.0003)			0.00005 (0.0003)	0.00005 (0.0003)	
numofposts			0.0003 (0.0002)		0.0003 (0.0002)			0.0003 (0.0002)	0.0003 (0.0002)
PublicProfile			0.008 (0.014)			0.008 (0.014)	0.008 (0.014)		0.008 (0.014)
Constant	2.696*** (0.007)	2.222*** (0.043)	2.160*** (0.067)	2.218*** (0.055)	2.168*** (0.057)	2.219*** (0.044)	2.215*** (0.055)	2.163*** (0.066)	2.166*** (0.057)
Observations	3,677	3,677	3,677	3,677	3,677	3,677	3,677	3,677	3,677
Log Likelihood	-11,742.730	-11,331.950	-11,330.690	-11,331.940	-11,330.860	-11,331.790	-11,331.780	-11,330.850	-11,330.700
theta	8.766*** (0.308)	12.274*** (0.487)	12.291*** (0.488)	12.274*** (0.487)	12.288*** (0.487)	12.277*** (0.487)	12.277*** (0.487)	12.288*** (0.487)	12.291*** (0.488)
Akaike Inf. Crit.	23,487.460	22,675.900	22,679.380	22,677.890	22,675.730	22,677.570	22,679.550	22,677.700	22,677.410

Note:

*p<0.05; **p<0.01; ***p<0.001

Normalization



Poisson- all results

```
> lrtest(poisson1, poissonempty) # poisson is not a good fit
Likelihood ratio test

Model 1: purchase ~ distance + income + cust_age + facebookvisit + gender
Model 2: purchase ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 6 -12416
2 1 -13428 -5 2024.4 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> lrtest(poisson2, poissonempty) # poisson is not a good fit
Likelihood ratio test

Model 1: purchase ~ distance + income + cust_age + facebookvisit + gender +
numoffriends + numofposts + PublicProfile
Model 2: purchase ~ 1
#Df LogLik Df Chisq Pr(>Chisq)
1 9 -12412
2 1 -13428 -8 2032.2 < 2.2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> lrtest(poisson1, poisson2)
Likelihood ratio test

Model 1: purchase ~ distance + income + cust_age + facebookvisit + gender
Model 2: purchase ~ distance + income + cust_age + facebookvisit + gender +
numoffriends + numofposts + PublicProfile
#Df LogLik Df Chisq Pr(>Chisq)
1 6 -12416
2 9 -12412 3 7.7724 0.05096 .
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Poisson Results

	Dependent variable:		
	poissonempty (1)	purchase poisson1 (2)	poisson2 (3)
distance		0.123*** (0.003)	0.123*** (0.003)
income		0.015*** (0.001)	0.015*** (0.001)
cust_age		0.001 (0.001)	0.001 (0.001)
facebookvisit1		0.080*** (0.010)	0.075*** (0.012)
gender		0.018 (0.012)	0.018 (0.012)
numoffriends			-0.00000 (0.0002)
numofposts			0.0003* (0.0001)
PublicProfile			0.011 (0.009)
Constant	2.696*** (0.004)	2.227*** (0.029)	2.163*** (0.045)
Observations	3,677	3,677	3,677
Log Likelihood	-13,427.670	-12,415.490	-12,411.600
Akaike Inf. Crit.	26,857.350	24,842.970	24,841.200
Note:	*p<0.05; **p<0.01; ***p<0.001		

Multicollinearity – all variables

	distance	income	gender	facebookvisit	cust_age	numoffriends	numofposts	PublicProfile
distance	1.000	-0.068	0.148	0.364	0.098	0.201	0.080	0.038
income	-0.068	1.000	-0.348	-0.188	-0.098	-0.128	-0.036	-0.014
gender	0.148	-0.348	1.000	0.235	0.026	0.144	0.029	0.012
facebookvisit	0.364	-0.188	0.235	1.000	0.221	0.583	0.206	0.036
cust_age	0.098	-0.098	0.026	0.221	1.000	0.096	0.050	-0.012
numoffriends	0.201	-0.128	0.144	0.583	0.096	1.000	0.107	0.006
numofposts	0.080	-0.036	0.029	0.206	0.050	0.107	1.000	0.012
PublicProfile	0.038	-0.014	0.012	0.036	-0.012	0.006	0.012	1.000

No variable from the 8 input variables has collinearity problem.

The linear correlation coefficients ranges between:

min correlation (PublicProfile ~ numoffriends): 0.006197103

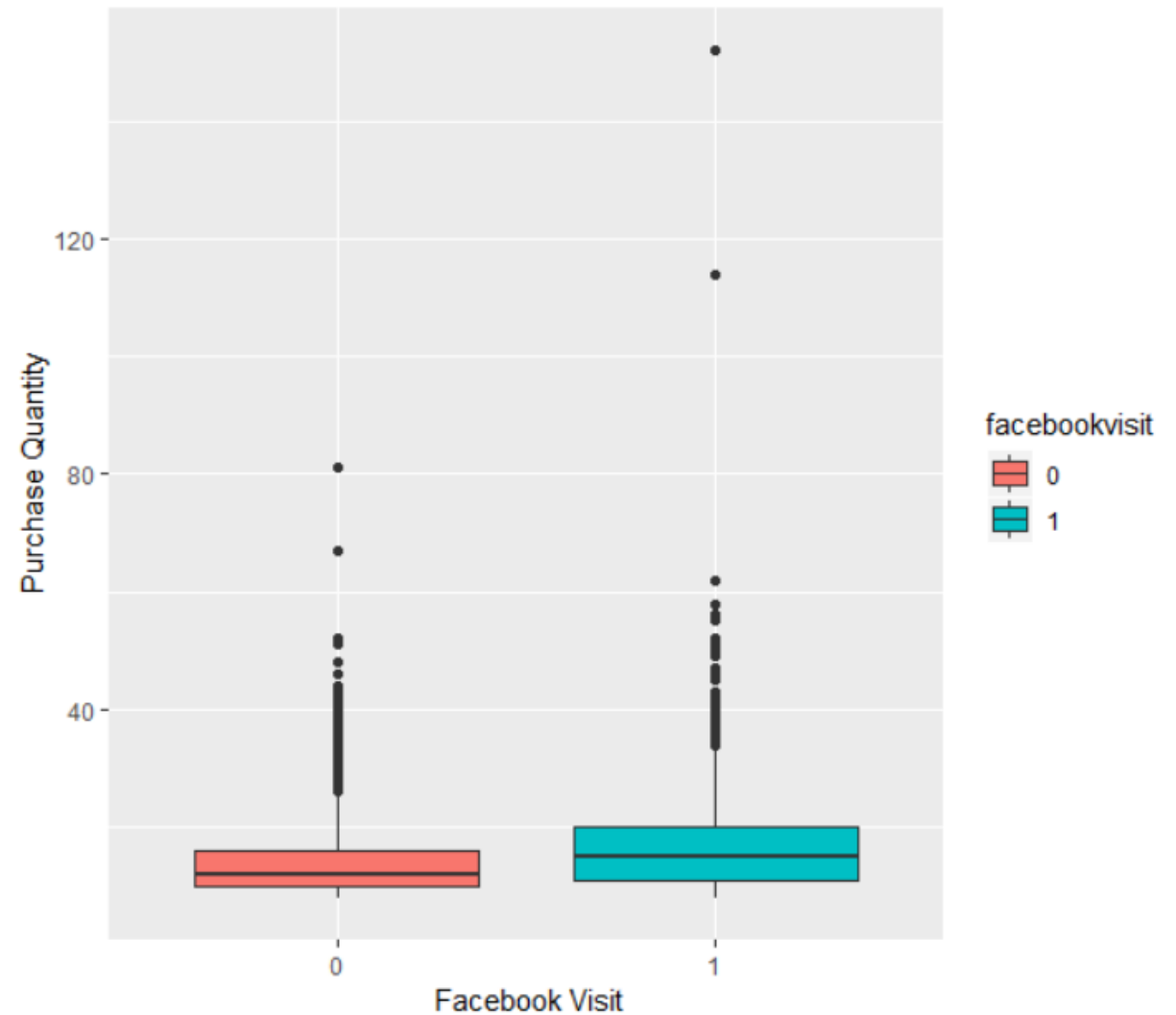
max correlation (numoffriends ~ facebookvisit): 0.5833385

----- VIFs of the remained variables -----

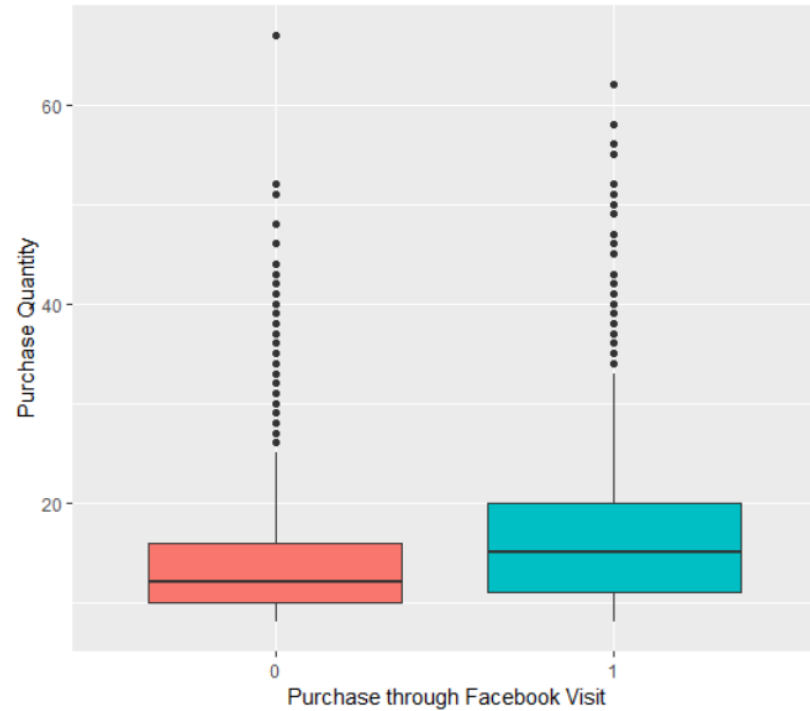
	Variables	VIF
1	distance	1.160624
2	income	1.160494
3	gender	1.187143
4	facebookvisit	1.847091
5	cust_age	1.060565
6	numoffriends	1.520667
7	numofposts	1.045115
8	PublicProfile	1.002961

Outlier Detection

- Outliers present in purchase quantity: 152 and 114
- Both purchases were made after facebook visit



Outlier Detection- Descriptive Statistics



Descriptive statistics by group

group: 0

	vars	n	mean	sd	median	trimmed	mad	min	max	range
income	1	2450	11.69	3.69	12	12.05	2.97	0	17	17
gender	2	2450	0.10	0.31	0	0.01	0.00	0	1	1
facebookvisit	3	2450	0.00	0.00	0	0.00	0.00	0	0	0
distance	4	2450	1.49	1.18	1	1.41	1.48	0	6	6
cust_age	5	2450	33.25	5.99	32	32.87	7.41	25	50	25
purchase	6	2450	13.78	5.84	12	12.86	4.45	8	52	44
numoffriends	7	2450	99.08	19.85	99	99.10	19.27	31	165	134
numofposts	8	2450	199.67	34.40	199	199.45	34.10	91	309	218
PublicProfile	9	2450	0.27	0.45	0	0.22	0.00	0	1	1

group: 1

	vars	n	mean	sd	median	trimmed	mad	min	max	range
income	1	1222	10.16	3.90	11	10.37	2.97	0	17	17
gender	2	1222	0.29	0.45	0	0.24	0.00	0	1	1
facebookvisit	3	1222	1.00	0.00	1	1.00	0.00	1	1	0
distance	4	1222	2.54	1.40	2	2.48	1.48	0	8	8
cust_age	5	1222	36.25	6.65	36	36.45	8.90	25	50	25
purchase	6	1222	16.58	7.74	15	15.43	5.93	8	58	50
numoffriends	7	1222	129.21	19.63	129	129.00	19.27	74	206	132
numofposts	8	1222	215.13	35.89	214	215.32	35.58	100	344	244
PublicProfile	9	1222	0.31	0.46	0	0.26	0.00	0	1	1

Outlier Detection- Model

Negative Binomial Results

Dependent variable:	
	purchase IRRs
distance	1.1291*** (0.0048)
income	1.0136*** (0.0018)
cust_age	1.0016 (0.0010)
facebookvisit	1.0750*** (0.0146)
gender	0.9978 (0.0180)
Constant	9.1937*** (0.0419)

Observations	3,672
Log Likelihood	-11,189.2100
theta	14.1092*** (0.6066)
Akaike Inf. Crit.	22,390.4200
=====	
Note:	*p<0.05; **p<0.01; ***p<0.001

Purchase quantity is **7.5%** more when the purchase is made though Facebook vs when it is made directly from Amazon.