

* Sorting: It is an algorithm that allocates the elements in either ascending or descending order.

1. selection sorting.
2. Bubble sorting
3. insertion sorting.

ex:

1	3	5	4	7	2
---	---	---	---	---	---

 → It is not in sorted order.

1	2	3	4	5	6
---	---	---	---	---	---

 → Inc. order

6	5	4	3	2	1
---	---	---	---	---	---

 → Dec. order.

10 selection sort:

Exo:

R:1

0	1	2	3	4	5
10	1	4	8	5	7

 $i=0$ min 3 4 5

R:2

0	1	2	3	4	5
1	10	4	8	5	7

 $i=1$ min 4 5

R:3

0	1	2	3	4	5
1	4	10	8	5	7

 $i=2$ min 5

R:4

0	1	2	3	4	5
1	4	5	8	10	7

 $i=3$ min 5

R:5

0	1	2	3	4	5
1	4	5	7	10	8

 $i=4$ min

R:6

0	1	2	3	4	5
1	4	5	7	8	10

 $i=5$

Now array is in sorted order.

Ex:2:

R:1

0	1	2	3	4	5
5	4	2	1	7	6

 $i=0$ min 3 4 5

R:2

0	1	2	3	4	5
1	4	2	5	7	6

 $i=1$ min

R:3

0	1	2	3	4	5
1	2	4	5	7	6

 $i=2$ min 4 5

R:4

0	1	2	3	4	5
1	2	4	5	7	6

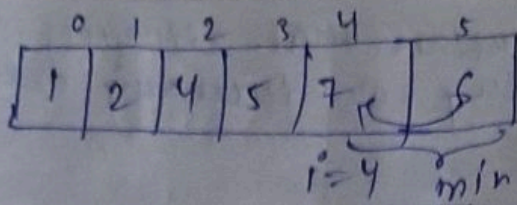
 $i=3$ min 5

R:5

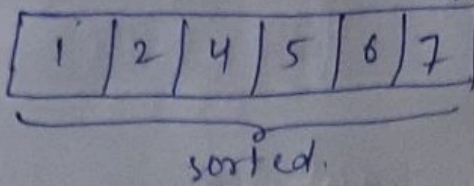
0	1	2	3	4	5
1	2	4	5	7	6

 $i=4$ min

R: 5



R: 6



```

for (int i = 0; i < n-1; i++) { // for every iteration we
    // need to find the
    // minimum (n-1) times
    int minIndex = i; // consider min value in
                       // present at i-th // outer loop
                       // index
    for (j = i+1; j < n; j++) { // to find the minimum value
                                // from i+1 to n.
        if (arr[j] < arr[minIndex]) { // if any value of arr[j]
                                      // is less than
                                      // arr[minIndex]
            minIndex = j;
        }
    }
    swap (arr[i], arr[minIndex]); // swap the current
                                // value with
                                // min value found in
                                // loop.
}
    
```

Time complexity:

for ($i=0 \longrightarrow i < n-1$) { $\longrightarrow 0 \longrightarrow n-1$

for ($j = i+1 \longrightarrow j < n$) { $\longrightarrow 1 \longrightarrow n$

$i=0 \longrightarrow j=1, 2, 3, 4$

$i=1 \longrightarrow j=2, 3, 4$

$i=2 \longrightarrow j=3, 4$

$i=3 \longrightarrow j=4$

$i=0 \longrightarrow n-1$

$j=1 \longrightarrow n$

$n \times (n-1)$ [nested loop]

$\longrightarrow n^2 - n$
 \longrightarrow upper Bound n^2 $O(n^2)$ TC.

Space complexity:

$S.C = O(1)$ as we don't create any extra space inside the function.

*Note: The sc doesn't depends upon the inputs we take in main function.
It depends upon the extra space we created in user defined function.

② Bubble sort: For every ~~iter~~ round the i^{th} ~~element~~ index will be compared with $(i+1)^{th}$ index if i index is greater than $(i+1)^{th}$ index then moves to right

SR:1

0	1	2	3	4	5
1	5	6	3	2	7

$i=0$ $i=1$ $1 > 5$ X NO

SR:2

0	1	2	3	4	5
1	5	6	3	2	7

$i=1$ $i=2$ $5 > 6$ NO.

SR:3

0	1	2	3	4	5
1	5	6	3	2	7

$i=2$ $i=3$ $6 > 3$ Yes

SR:4

0	1	2	3	4	5
1	5	6	3	2	7

$i=3$ $i=4$ $3 > 2$ Yes

SR:5

0	1	2	3	4	5
1	5	6	2	3	7

$i=4$ $i=5$ $3 > 7$ NO

SR: Sub-Round

→ R:1

Now 7 max element is present at last

SR:1

0	1	2	3	4	5
1	5	6	3	2	7

$i=0$ $1 > 5$ NO

SR:2

same

ca fix

$R: 1 \rightarrow 4 \text{ times}$
 $R: 2 \rightarrow 3 \text{ times}$
 $R: 3 \rightarrow 2 \text{ times}$
 $R: 4 \rightarrow 1 \text{ time}$
 $R: 5 \rightarrow 0 \text{ times}$

outer loop inner loop

} loop runs

```

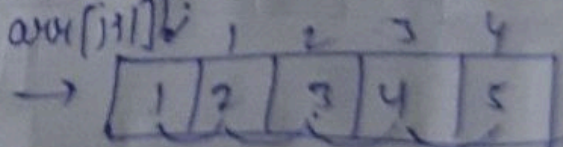
for (int i = 1; i < n; i++) < // outer loop for
                                no. of rounds: 4
                                it will run 3
    for (int j = 0; j <= n - i - 1; j++) <
        if (arr[j] > arr[j+1]) < // inner loop to
                                    check how many
                                    time comparison
                                    done jth index &
                                    (j+1)th index
            swap(arr[j], arr[j+1]);
            swap
    }
    print
  
```

More optimized way:

Best case in sorting: If an array is already sorted, no need to sort.

```

for (int i = 1; i < n; i++) <
    break swap = false;
    for (int j = 0; j <= n - i - 1; j++) <
        if (arr[j] > arr[j+1]) <
            swap = true;
            swap(arr[j], arr[j+1]);
    }
    if (swap == false) <
        // already sorted,
        break;
  
```



R1 [SR:) 1 2 3 4
 4 times

Time complexity:

we their j^{th} value greater than $(j+1)^{\text{th}}$ value means swap done

T.C for () <

$$i=1 \longrightarrow i < n$$
$$j=0 \longrightarrow j < n-i-1$$

for () <

$$n(n-i-1)$$

$$n^2 - ni - n$$

$$n^2 - n(i+1)$$

upper Bound

$$T.C = O(n^2)$$

For Best case when array is sorted

→ for () <
bool swap = false;
for () <

if (arr[j] > arr[j+1]) <

if this loop doesn't come to true

if (swap == false) <
break;

means it run for 4 times
if swap == false break
means already sorted

No need to move to next Round by iterating i.

T.C = $O(n)$ for Best case

S.C = $O(1)$

* worst case: reverse case:

0	1	2	3	4
5	4	3	2	1

4 5

4 3 5

4 3 2 5

4 3 2 1 5

(4)

(3)

(2)

(1)

$$\rightarrow \frac{n(n-1)}{2} O(n^2)$$

- * We use selection sort when we have small array. we select minimum element & place at right place
- * Bubble sort is used when with largest elements needed to be shift in right. (Maximum element to last place)

* Insertion Sort: Inserting the elements means picking the each elements & inserting at right place.

0	1	2	3	4	5
10	1	7	0	14	9

we will use insertion sort when it is partially sorted.

- Step: A: fetch value
 Step: B: Compare with all previous value.
 Step: C: shift the previous value if it is greater.
 Step: D: Copy the ~~present~~ ^{value} to previous value

→ arr[0] will not be considered as first ~~element~~ ^{value} as it will start from arr[i] as first element is considered to be sorted.

```
for (int i = 0; i < n; i++) { // outer loop for seconds
    int value = arr[i]; // to store initial value.
    int j = i - 1;
```

```
    while (j > 0; j--) {
        if (arr[j] > arr[j+1] value) {
```

```
            arr[j+1] = arr[j];
```

```
        }
    } else {
        break;
```

```
    }
    arr[j+1] = value;
```


* The Best case: when the array is already in sorted order.

1	2	3	4	5	6
---	---	---	---	---	---

As we see every previous value is less than current element. then it will check till times

$$T.C = O(n)$$

$$S.C = O(1)$$

* Worst case:

```

for (i=1; i<n; i++) {
    for (; j>=0; j--) {
        j = i-1;
        0
        n
        (n-1)
        (n-2)
    }
}

```

$$T.C = O(n^2)$$

$$S.C = O(1)$$

$$\frac{n(n-1)}{2} = \frac{n^2}{2} - \frac{n}{2}$$

$$O\left(\frac{n^2}{2}\right)$$

$$O(n^2)$$