

Queen's University Management School.

MGT7177 Statistics For Business: Assignment 2

PREDICTING TERM DEPOSIT SUBSCRIPTION USING LOGISTIC REGRESSION

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Contents

1.Introduction	3
2. Methodology and Analysis:	
3. Results and Discussion	
4. Conclusion	
5. Reflective commentary	
6. References	
7. Appendix 1: R Code	20

1.Introduction

Since term deposits are usually an important part of a bank's operations, a robust marketing strategy is imperative. One of the most widely used marketing techniques nowadays is telephone marketing, which consulting firms may find valuable for attracting new clients(Hung, Hanh et al. 2019). Through a marketing campaign that involves calling consumers personally, the bank hopes to choose the best set of customers(Moro, Cortez et al. 2014). A logistic regression model (LR) is used to assess the potential causes to successful deposit subscriptions and anticipate the success rate of bank telemarketing(Jiang 2018). The goal of the marketing campaign was to persuade customers to open a term deposit. The information may be used to understand the factors that affect a customer's choice to subscribe to the term deposit(Miguéis, Camanho et al. 2017).

Related work Literature:

In (Hosseini 2021)work, the logistic regression model is applied. It was primarily concerned with the association between telemarketing success (output variable) and several good characteristics. Furthermore, in (Hosseini 2021) study, the prediction is applied based on the created model to locate some possible consumers who would really subscribe to the deposits.

(Moro, Cortez et al. 2014) set out to predict the success of bank telemarketing. They used a comprehensive data set from 2008 to 2013 and a data collection with 150 characteristics. They examine the logistic regression (LR), decision trees, support vector machines, and neural networks models of data mining (NN). Le & Viviani (2017) carried out research to identify the risk factors for bank failure. They used discriminant analysis and logistic regression, two established statistical techniques, to analyse a sample of 3000 US banks.

Table1: Hypotheses

No of	Variable X	Target Variable	Measures	Description
Relation	(Type)	(Type)	of	
			association	
1	Job(categorical)	Subscribed(binary:	Chi-squared	Bank Client
		'yes','no')	test	Variable
2	marital_status(categorical)	Subscribed(binary:	Chi-squared	Bank Client
		'yes','no')	test	Variable
3	Education(categorical)	Subscribed(binary:	Chi-squared	Bank Client
	_	'yes','no')	test	Variable
4	1	0 1 11 1/1	C1 · 1	771 3.4
4	Month(categorical)	Subscribed(binary:	Chi-squared	The Most
		'yes','no')	test	Recent Contact
				During the
				Marketing
				Campaign
				Variables
5	Poutcome(categorical)	Subscribed(binary:	Chi-squared	Other Variables
		'yes','no')	test	

2. Methodology and Analysis:

The methodology includes filtering and processing of the raw datasets for anomalies like missing data, data standardization, assessing the data and producing summary statistics, evaluating the training and testing datasets, testing multicollinearity among diverse features, and finding a collection of predictor variables to forecast the Term Deposit Subscriptions. The flowchart below depicts the fundamental processes taken (Jiang 2018).

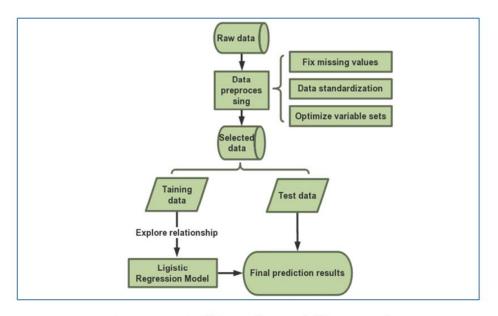


Figure 1: Methodology of LR model(Jiang 2018)

It is used to assess whether closely a sample matches the pattern of a defined population or to look into the relationship between two categorical variables' independence. (Franke, Ho et al. 2012). For visualisations ggplot2 is used. The ggplot2 functions and their outputs can be added to the plot as additional layers. For example, adding a title using ggplot2's labs() method (Ito and Murphy 2013).

To avoid overfitting, we divided the 41153 observations into training data (80%) and test data (20%). Because the answer variable "yes" only accepts a tiny amount of the data, data partitioning via the function createDataPartition is used to provide a balanced response in both training and test data(Lever, Krzywinski et al. 2016).

It is employed for measure of association because the target variable is categorical(goodness of fit). The logistic regression is evaluated using log likelihood, the deviance statistic, pseudo R squared, and the odds ratio (Smith and McKenna 2013). Predictors are evaluated using significance and the odds ratio, and models are compared using the Akaike information criteria (AIC)(Li and Nyholt 2001).

Dataset: Data set includes 41153 clients. Client traits and campaign features, and other social and economic qualities are among the 20 predictor variables.

The client's choice to purchase the long-term deposit, stated as "yes" or "no," is the response variable. The variables education, employment, marital, housing, loan, and default have a 'unknown' level. There are total 40 missing values in the dataset.

Addressing Data Quality Issues:

Age Column: To find outliers in Age data, using the Box Plot function and giving the mean of age to the outliers which are less than 5 and more than 100.

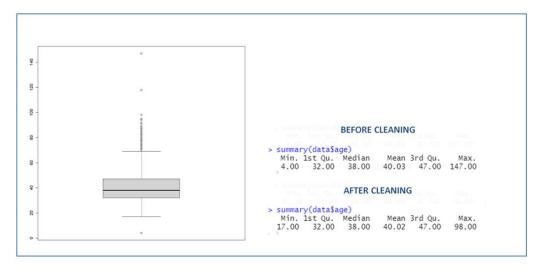


Figure 2: Addressing age column data issue

Default Column: The data quality issue in Default Column has been corrected, the "no" value is misspelt as 'n' per the data dictionary.

```
BEFORE CLEANING

summary(data$default)
n no unknown yes
221 32346 8583 3

AFTER CLEANING

summary(data$default)
n no unknown yes
0 32567 8583 3
```

Figure 3: Addressing Default column data issue

Month Column: The data quality problem in the Month Column has been resolved; the "mar" value is misspelt as "march" according to the data dictionary.

```
BEFORE CLEANING

summary(data$month)
apr aug dec jul jun mar march may nov oct sep
2632 6178 182 7174 5318 501 45 13734 4101 718 570

AFTER CLEANING

summary(data$month)
apr aug dec jul jun mar may nov oct sep
2632 6178 182 7174 5318 546 13734 4101 718 570

Figure 4: Addressing month column data issue
```

Pdays Column: The 999 code indicates that the consumer was not contacted earlier, which might be assigned as 0.

```
BEFORE CLEANING

summary(data$pdays)
Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
0.0 999.0 999.0 962.4 999.0 999.0 40

AFTER CLEANING

summary(data$pdays)
Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
0.0000 0.0000 0.0000 0.2216 0.0000 27.0000 40
```

Figure 5: Addressing Pdays column data issue

3. Results and Discussion Descriptive Statistics:

Descriptive statistics are used to describe data in an ordered manner by explaining the connection between variables within a sample or population. Before conducting inferential statistical comparisons, descriptive statistics should always be calculated as a crucial first step in conducting analysis. (Kaur, Stoltzfus et al. 2018).

> summary(data)						1.6.3.		-
ID	age	job	marital		education	default	housing	loan
	Min. :17.00	admin. :10416	divorced: 4609	university.d		n : 0	no :18604	no :33923
1st Qu.:10289	1st Qu.:32.00	blue-collar: 9244	married :24905	high.school		no :32567	unknown: 990	unknown: 990
Median :20577	Median :38.00	technician : 6739	single :11559	basic.9y	: 6038	unknown: 8583	yes :21559	yes : 6240
Mean :20577	Mean :40.02	services : 3963	unknown: 80	professional	.course: 5240	yes : 3		
3rd Qu.:30865	3rd Qu.:47.00	management : 2920		basic.4y	: 4176	-		
Max. :41153	Max. :98.00	retired : 1719		basic.6v	: 2286			
		(Other) : 6152		(Other)	: 1745			
contact	month		ration ca	mpaign	pdays	previous	poutce	ome
cellular :26144	may :13734				in. : 0.0000	Min. :0.0000		
telephone:15009	jul : 7174				st Qu.: 0.0000	1st Qu.:0.0000		
cerepiionerisous	aug : 6178				ledian : 0.0000	Median :0.0000		1373
	jun : 5318		: 258.2 Mean		lean : 0.2216	Mean :0.1731		13/3
	nov : 4101				rd Qu.: 0.0000	3rd Qu.:0.0000		
			:4918.0 Max.		lax. :27.0000	Max. :7.0000		
	apr : 2632 (Other): 2016		.4910.0 Max.		IA's :40	Max/.0000		
emp.var.rate	cons.price.i		euribor3m	nr.employed	subscribed			
Min. :-3.40000				Min. :4964	no :36513			
1st Qu.:-1.80000				1st Qu.:5099	yes: 4640			
Median : 1.10000				Median :5191				
Mean : 0.08102			Mean :3.620	Mean :5167				
3rd Qu.: 1.40000) 3rd Qu.:93.9	9 3rd Qu.:-36.40	3rd Qu.:4.961	3rd Qu.:5228				
Max. : 1.40000) Max. :94.7	7 Max. :-26.90	Max. :5.045	Max. :5228				

Figure 6: Descriptive Statistics of dataset variables

Relationship between Client Age and Subscribed:

Clients phoned by the bank in its telemarketing efforts range in age from 17 to 98 years old. The average is 40 years old. From the figure below, its shows the majority of clients that called were in their 30s and 40s (32 to 47 years old fall within the 25th to 75th percentiles).

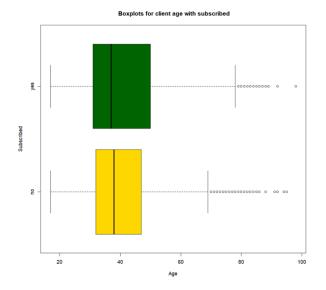


Figure 7: Boxplot of age with Subscription of customers

Relationship between Customer job details and Subscribed:

The chisq.test was used to assess the relationship. Because the p-value is less than 0.05, so ruling out the null hypothesis and concluding that there is a significant relationship.

```
Pearson's Chi-squared test

data: data$job and data$subscribed
X-squared = 960.03, df = 11, p-value < 0.00000000000000022
```

Figure 8: Chi-squared test between job and Subscription of customers

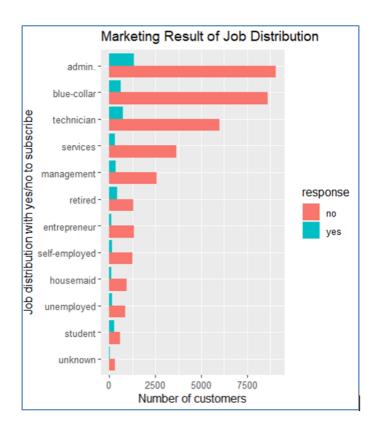


Figure 9: ggplot between relationship of job and Subscription of customers

From the descriptive statistical data (Figure 6), it shows that the majority of consumers work in admin and blue collar jobs. As per the ggplot, students and retired consumers account for more than half of all subscriptions. Blue-collar workers have the lowest conversion rate. Customers in the student, retired, administrative, and jobless groups are more likely to respond positively to the marketing.

Relationship between the marital status and number of customers subscribed:

If the p-value is less than 0.05, a relationship is considered to be significant(Di Leo and Sardanelli 2020).

```
Pearson's Chi-squared test

data: data$marital and data$subscribed

X-squared = 122.58, df = 3, p-value < 0.000000000000000022
```

Figure 10: Chi-squared test between marital status and Subscription of customers

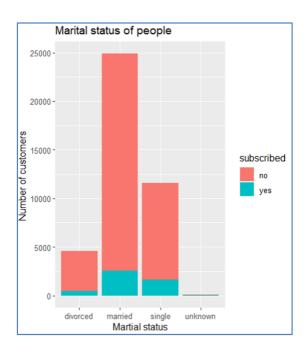


Figure 11: ggplot between marital status and Subscription of customers

Above chart shows that term deposit subscriptions from a "single" client are more likely than those from other groups (divorced and married). Most married customers make up the marketing target and married customers are more likely to respond better than divorced ones.

Relationship between the Education and subscribed clients:

```
Pearson's Chi-squared test

data: data$education and data$subscribed

X-squared = 192.91, df = 7, p-value < 0.0000000000000000022
```

Figure 12: Chi-squared test between Education and Subscription

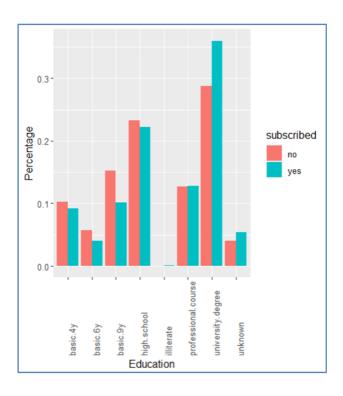


Figure 13: ggplot between Education and Subscription

The chance of enrolling in a term deposit appears to be positively connected with the number of years of education. Those with a university education are the most likely to sign up for a term deposit. High school, professional training, and university degrees should be the three target audiences for bank marketing. Because there are just 18 illiterate clients, the "illiterate" category has the highest subscription rate.

Relationship between the month and subscribed clients:

```
Pearson's Chi-squared test

data: data$month and data$subscribed
X-squared = 3096.6, df = 10, p-value < 0.00000000000000022
```

Figure 14: Chi-squared test between month and Subscription

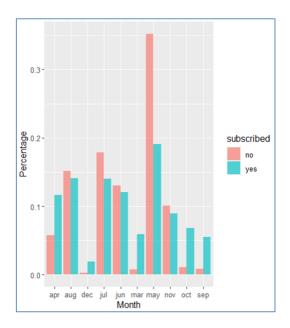


Figure 15: ggplot between month and Subscription

During the months of January and February, no communication was made. Between May and August, the bank contacted the majority of its customers. The largest surge happens in May, yet the ratio of subscribers to people contacted is the poorest. The greatest subscription rate was in March. The months with a low contact frequency (March, September, October, and December) has excellent outcomes.

Relationship between the default and subscribed clients:

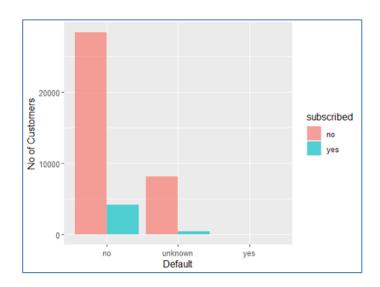


Figure 16: ggplot between default and Subscription

According to the figure above, the majority of the consumers in the marketing campaign had no default history, which is sensible given that defaulters are less likely to have idle funds.

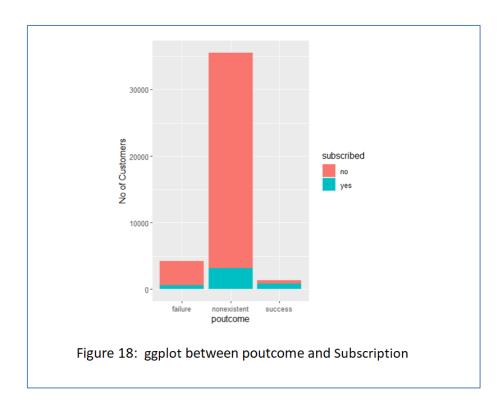
Relationship between the Previous Campaign and subscribed clients:

```
Pearson's Chi-squared test

data: data$poutcome and data$subscribed

X-squared = 4225.7, df = 2, p-value < 0.00000000000000022
```

Figure 17: Chi-squared test between month and Subscription



The plot below shows that the majority of consumers were not contacted previous to this campaign. Customers are less likely to respond positively to a promotion if it has previously failed.

Customers are more likely to respond positively to the advertising if the preceding effort was successful(Brennan and Binney 2010). The outcome is not significant for no previous campaign, however the majority of consumers that offered favourable results were not approached before to this campaign.

The boxplot analysis of categorical characteristics is provided below. The binary values for the column "subscribed" are "yes" and "no" (subscribed to a term deposit).

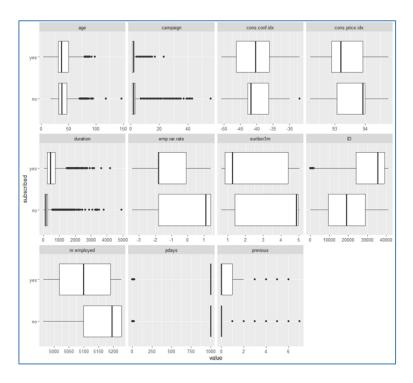


Figure 19: Boxplot of dataset variables and Subscriped customers

Regression Analysis Findings

However, before proceeding to the train-test split, it is necessary to analyse correlation further. A correlation matrix was constructed using continuous variables and discrete variables .

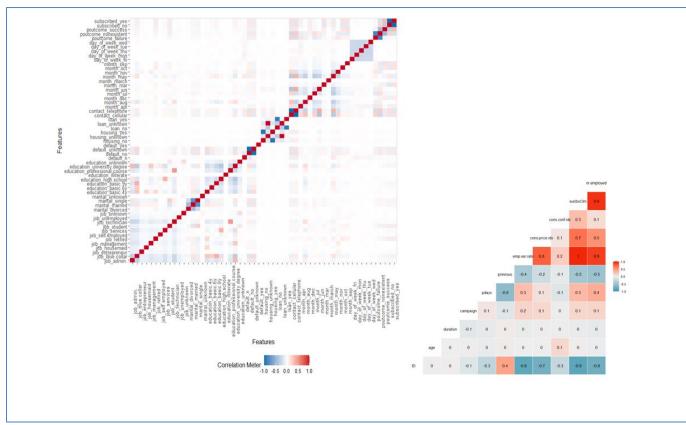


Figure 20: Correlation Matrix

Clearly, subscription of customers to term deposit shows a substantial association with "duration", a moderate link with "previous contacts", and a weak correlation with "month " and "number of campaigns". In the regression models, their effects on campaign outcomes will be studied further.

To obtain an accurate assessment of the model's accuracy, we can divide the data into a training and test set (Refaeilzadeh, Tang et al. 2009) and create the model fit, assess it, and analyse the model coefficients based on the training data. Then, by making predictions on an unidentified test dataset, the model's predictive accuracy can be assessed (Harrell Jr, Lee et al. 1996). Built the model after setting the formula using the predictors (contact + month + poutcome + cons.price.idx + cons.conf.idx + nr.employed). A logistic regression may be created in R using the glm() function (Calcagno and de Mazancourt 2010).

```
Call:
glm(formula = formula4, family = "binomial", data = train)
Deviance Residuals:
                   Median
                                        Мах
   Min
             10
-2.0498 -0.3658 -0.3431 -0.2478
                                     2.7237
Coefficients:
                     Estimate Std. Error z value
                                                              Pr(>|z|)
                                          15.851 < 0.000000000000000000002 ***
                                3.979114
(Intercept)
                    63.073137
                                0.098036
monthaug
                    -0.124650
                                           -1.271
                                                              0.203563
                                0.192691
monthdec
                     0.088125
                                           0.457
                                                              0.647427
monthiul
                    0.173437
                                0.090030
                                           1.926
                                                              0.054050
                    0.227740
                                                              0.010110 *
monthjun
                                0.088545
                                            2.572
                                                   0.0000000034233573 ***
monthmar
                     0.733486
                                0.124112
                                           5.910
                     1.406449
                                                   0.0000492314070458 ***
monthmarch
                                0.346480
                                           4.059
                                0.071340 -10.616 < 0.0000000000000000 ***
monthmay
                    -0.757372
                    -0.346160
                                0.093489
                                           -3.703
                                                              0.000213 ***
monthno∨
monthoct
                    -0.208126
                                0.124337
                                           -1.674
                                                              0.094153
                                          -3.976
monthsep
                    -0.528714
                                0.132967
                                                   0.0000700049348298 ***
                                                   0.000000000000033 ***
                                           7.879
poutcomenonexistent 0.481184
                                0.061070
                     1.786514
                                          20.570 < 0.0000000000000000 ***
poutcomesuccess
                                0.086851
contacttelephone
                    -0.438387
                                0.066619
                                           -6.581
                                                   0.0000000000468803
                    -0.042890
                                0.041764
                                           -1.027
                                                              0.304431
cons.price.idx
                                                   0.0000163440336917
                    0.022112
                                0.005131
                                           4.310
cons.conf.idx
nr.employed
                                0.000323 -36.375 < 0.0000000000000000 ***
                    -0.011749
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
                                    degrees of freedom
    Null deviance: 23192 on 32922
Residual deviance: 18377 on 32906
                                    degrees of freedom
AIC: 18411
Number of Fisher Scoring iterations: 6
```

Figure 21: Summary of Logistic Regression accurate model

To determine if the predictor differs substantially from zero, the z-statistic, which has a normally distributed distribution, is utilised(Krackhardt 1988). The estimated nr. employed is -0.011749, while the z value for emp.var.rate is -36.375. As the number of employees increases, there is a decreasing possibility of subscribing to a term deposit since the value is negative. The marketing effort in March has a higher chance of generating subscriptions. Given that the estimate value is 0.022112 there is a positive correlation between the customer subscribed and the Consumer confidence index. A mathematical test called the Akaike information criterion(AIC) value is 18411, It evaluates the degree to which a model matches the facts it is meant to explain. It penalises models that include more independent variables to prevent over-fitting(Cama, Cristi Nicu et al. 2016).

```
> logisticPseudoR2s(model4)
Pseudo R^2 for logistic regression
Hosmer and Lemeshow R^2 0.208
Cox and Snell R^2 0.136
Nagelkerke R^2 0.269
```

Figure 22: Pseudo R^2 for logistic regression

A adjusted version of Cox and Snell R Squared is Nagelkerke R Squared. Between 0 and 1 is the range of values for Nagelkerke(Krackhardt 1988). The Nagelkerke R^2 value is 0.269 which is more than zero.

> exp(model4\$coefficients) (Intercept) 2467830534239354346406226244.000000 monthjun 1.2557593	monthaug 0.8828057 monthmar 2.0823279	monthdec 1.0921247 monthmarch 4.0814356	monthjul 1.1893863 monthmay 0.4688973
1.2557593 monthnov 0.7073993 poutcomesuccess 5.9686113 nr.employed 0.9883195	2.0823279 monthoct 0.8121050 contacttelephone 0.6450761	4.0814356 monthsep 0.5893624 cons.price.idx 0.9580166	0.4688973 poutcomenonexistent 1.6179891 cons.conf.idx 1.0223583

Figure 23: Odds Ratios

While calculating Odds Ratios, the values of the predictors (poutcome, cons.conf.idx) are more than 1, the odds of the result rises. The likelihood of the remaining variables occurring are fewer than 1, and as the predictor gets bigger, those odds go less(Nick and Campbell 2007).

	GVIF	Df	GVIF^(1/(2*Df))
month	4.725106	10	1.080738
poutcome	1.301824	2	1.068164
contact	1.895528	1	1.376782
cons.price.idx	1.873955	1	1.368925
cons.conf.idx	2.327407	1	1.525584
nr.employed	1.980194	1	1.407194

Figure 24: VIF for LR model

The popular method for identifying multicollinearity is the variance inflation factor (VIF). The GVIF values greater than 10 are not considered in further model (Aheto 2019). There is a no problem with multicollinearity in this situation, which makes it likely that the odd ratio and the coefficient for these variables will be accurate.

When assessing model fit, the standardised residuals are the main area of attention. On average, only 5% should fall outside of 1.96(Tennant and Conaghan 2007). Standardized Residuals(>1.96) add up to 1330, which is less than 5% of 32923. (train data). 295 values (less than 1%) are outside the range of 2.58. Therefore, there is no reason to worry.

```
Reference
Prediction no yes
no 7213 736
yes 89 192

Accuracy: 0.8998
95% CI: (0.8931, 0.9062)
No Information Rate: 0.8872
P-Value [Acc > NIR]: 0.0001429

Kappa: 0.2799

Mcnemar's Test P-Value: < 0.000000000000000022

Sensitivity: 0.9878
Specificity: 0.2069
Pos Pred Value: 0.9074
Neg Pred Value: 0.6833
Prevalence: 0.8872
Detection Rate: 0.8764
Detection Prevalence: 0.9659
Balanced Accuracy: 0.5974

'Positive' Class: no
```

Figure 25: Confusion Matrix and Statistics of the model

There are 197 "yes" entries that were accurately predicted as "yes" and 7213 "no" entries that were correctly forecasted as "no" in the confusion matrix. 89 "no" predictions that were mistakenly made as "yes" and 736 "yes" predictions that were mistakenly made as "no."

Given all the defined customer features, the Logisitic Regression model has an accuracy of 89.9%. indicating a high level of strength in this model's ability to classify the customer response. The comparison of the other LR models is shown in the table below.

Table 2: LR Models

LR Models	Predictors	Residual deviance	AIC	Accuracy
Model 4	month + poutcome+contact	18377	18411	89.9%
	+ cons.price.idx + cons.conf.idx +			
	nr.employed			
Model 3	age+	18350	18390	89.8%
	poutcome+month+			
	emp.var.rate			
	+campaign			
	+previous +			
	euribor3m +			
	cons.conf.idx +			
	nr.employed			
Model 2	nr.employed +	18795	18833	89.8%
	euribor3m +			
	emp.var.rate+			
	cons.price.idx			
	+poutcome + age +			
	job			

Model 1	age + job + marital	19812	19882	89.6%
	+ education +			
	poutcome + month			

4. Conclusion

In this paper, an Logistic Regression classification model was created to evaluate the association between telemarketing effectiveness and other parameters like clients' information, social-economic conditions and so on. The perception of the campaign's investment would have been influenced by higher education. Most of the customers who responded favourably to the campaign were first-time phone callers(Chang and Chen 1998). Clients are more likely to be people in their 20s to 30s, college students, and seniors. The months of March, December, September, and October should be used for the majority of calls (campaigns), according to future planning. Keep the conversation going as long as you can because long phone calls are more effective.

5. Reflective commentary

Because of the principles I've learned and my prior experience applying them practically in the last assignment, I now have a better understanding of the subject. Regarding the information I have learned from the term's classes, I consider my experience as a beginner in statistical analysis to be quite satisfying. My understanding of its practical applications, which are essential to the analytical topics in which I am interested in specialising, is growing.

6. References

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7. Appendix 1: R Code

```
getwd()
setwd ("c:/BHARATGURUNATHANHARIDOSS/Assignment1")\\
dir()
#Load the Library
library(tidyverse)
library(corrplot)
library(psych)
library(dplyr)
library(ggplot2)
library(gtools)
library(caret)
library(readr)
library(readxl)
library(car)
library(GGally)
library(DataExplorer)
library(explore)
library(ltm)
data<-read_excel("banksv.xlsx")
view(data)
summary(data)
describe(data)
#to Check for NA values
anyNA(data)
```

```
sum(is.na(data))
#outputs will be more readablity:
options(scipen = 150)
# converted to factors if it is character
data<- data %>% mutate_if(is.character, as.factor)
#Addressing Data quality issues
#Data quality issue of age
summary(data$age)
boxplot(data$age)
data$age[data$age>100]<- mean(data$age)
data$age[data$age < 5] <- mean(data$age)
boxplot(data$age) # After cleaning data
summary(data$age)
summary(data$job)
summary(data$marital)
#Data quality issue of default
summary(data$default)
data\$default[data\$default == 'n'\ ] <- 'no'
data$default<-as.character(data$default)
data$default<- as.factor(data$default)</pre>
summary(data$default)
summary(data$housing)
summary(data$loan)
summary(data$contact)
```

```
#data quality issue of month
summary(data$month)
data$month[data$month == 'march' ] <- 'mar'</pre>
data$month<-as.character(data$month)</pre>
data$month<- as.factor(data$month)</pre>
summary(data$month)
summary(data$day_of_week)
summary(data$duration)
summary(data$housing)
#data quality issue of pdays
summary(data$pdays)
data$pdays[data$pdays == 999] <- 0 #as 999 means not contacted
boxplot(data$pdays)
summary(data$subscribed)
data$subscribed <- relevel(data$subscribed, "yes")</pre>
#Data Analysis and Data Visualisation
# plot with target variable:
ggplot(data, aes(x = subscribed)) + geom_bar(colour="black", fill="darkblue") +
 ggtitle(" Target variable (subscribed)") +
 xlab("Did consumer subscribed (yes/no)") + ylab("Density")
plot_boxplot(data,by="subscribed")
#Relationship between the age and subscribed
chisq.test(data$age,data$subscribed)
```

```
boxplot(age~subscribed,
     data=data,
     col=(c("gold","darkgreen")),
     main=" Boxplots for client age with subscribed",
     ylab="Subscribed",
     xlab="Age",
     horizontal = TRUE
#Relationship between the job and no of people subscribed
chisq.test(data$job, data$subscribed, correct = FALSE)
#ggplot plot of job of all customers
ggplot(data, aes(x = job)) +
 geom_bar(colour="white", fill="lightblue") +
 ggtitle("Jobs of Overall people") +
 xlab("jobs") + ylab("total number of people")
#ggplot plot of job with only people who subscribed
people_yes <- data %>% group_by(job) %>% filter(subscribed == 'yes')
view(people_yes)
ggplot(people_yes,aes(x= job))+ geom_bar(colour="white", fill="darkblue") +
 ggtitle("Jobs of people that subscribed") +
 xlab("Types of Jobs") + ylab("Number of people") +
 theme(
  plot.title = element_text(color="black", size=15, face="bold")
 )
#ggplot plot of job
job_tab <- data.frame(table(data$job, data$subscribed))</pre>
colnames(job_tab) <- c("job", "response", "count")
ggplot(data=job_y_tab, aes(x=count,y=reorder(job,count), fill=response))+
```

```
geom_bar(stat = 'identity', position = 'dodge')+
 xlab("Number of customers")+ylab("Job distribution with yes/no to subscribe") +
    ggtitle("Marketing Result of Job Distribution")
#Relationship between the marital status and no of people subscribed
chisq.test(data$marital, data$subscribed, correct = FALSE)
#ggplot plot of marital status of all customers
ggplot(data, aes(x = marital)) +
 geom_bar(colour="black", fill="lightblue") +
 ggtitle("Marital status of people") +
 xlab("jobs") + ylab("Number of customers")
#ggplot plot of marital status of all customers and subscribed rate
ggplot(data = data, aes(x = marital, fill = subscribed)) +
 geom_bar() + ggtitle("Marital status of people") +
 xlab("Martial status") + ylab("Number of customers ")
#Relationship between the education and no of people subscribed
chisq.test(data$education, data$subscribed, correct = FALSE)
table(data\( education \)
edutable <- table(data$education, data$subscribed)</pre>
tab <- as.data.frame(prop.table(edutable, 2))
colnames(tab) <- c("education", "subscribed", "perc")</pre>
ggplot(data = tab, aes(x = education, y = perc, fill = subscribed)) +
 geom_bar(stat = 'identity', position = 'dodge') +
 xlab("Education") +
 ylab("Percentage") + theme(axis.text.x=element_text(angle = 90, hjust = 0))
```

```
chisq.test(data$month, data$subscribed, correct = FALSE)
monthtable <- table(data$month, data$subscribed)
tab <- as.data.frame(prop.table(monthtable, 2))
colnames(tab) <- c("month", "subscribed", "perc")</pre>
ggplot(data = tab, aes(x = month, y = perc, fill = subscribed)) +
 geom\_bar(stat = 'identity', position = 'dodge', alpha = 2/3) +
 xlab("Month")+
 ylab("Percentage")
#Relationship between the default and no of people subscribed
chisq.test(data$default, data$subscribed, correct = FALSE)
def_tab <- data.frame(table(data$default,data$subscribed))</pre>
colnames(def_tab) <- c("default", "subscribed", "number_of_customers")</pre>
ggplot(data=def_tab, aes(x=default,y=number_of_customers, fill=subscribed))+
 geom_bar(stat = 'identity', position = 'dodge', alpha = 2/3)+ xlab("Default")+
 ylab("No of Customers")
#Relationship between the poutcome and no of people subscribed
chisq.test(data$poutcome, data$subscribed, correct = FALSE)
ggplot(data=data, aes(x=poutcome, fill=subscribed))+
 geom_bar(position = 'stack')+
 labs(X="Number of customers",
    y="No of Customers")
# Correlation
plot_correlation(data, type = 'continuous')# Graphical representation of correlation for continuous
variables
plot_correlation(data, type = 'discrete') # Graphical representation of correlation for discrete variables
```

#Relationship between the month and no of people subscribed

```
ggcorr(data, label=TRUE)
#Split data into train and test dataset
set.seed(40387258)
index <- createDataPartition(data$subscribed, p= 0.8, list=FALSE)
train <- data[index,]
test <- data[-index,]
#model1
# To produce a logistic regression
formula <- subscribed ~ age + job + marital + education + poutcome + month
model1 <- glm(formula, data = train, family = "binomial")
summary(model1)
logisticPseudoR2s <- function(LogModel) {</pre>
 dev <- LogModel$deviance
 nullDev <- LogModel$null.deviance
 modelN <- length(LogModel$fitted.values)</pre>
 R.l \leftarrow 1 - dev / nullDev
 R.cs <- 1- exp (-(nullDev - dev) / modelN)
 R.n \leftarrow R.cs / (1 - (exp(-(nullDev/modelN))))
 cat("Pseudo R^2 for logistic regression\n")
 cat("Hosmer and Lemeshow R^2 ", round(R.1, 3), "\n")
                             ", round(R.cs, 3), "\n")
 cat("Cox and Snell R^2
 cat("Nagelkerke R^2
                          ", round(R.n, 3), "\n")
}
logisticPseudoR2s(model1)
vif(model1)
predictions<- predict(model1, test, type = "response")</pre>
class_pred <- as.factor(ifelse(predictions > .5, "yes", "no"))
postResample(class_pred, test$subscribed)
```

#Model2

```
formula2 <- subscribed ~ poutcome + age + job + nr.employed + euribor3m + emp.var.rate+
cons.price.idx
model2<- glm(formula2, data = train, family = "binomial"(link="logit"))
summary(model2)
logisticPseudoR2s <- function(LogModel) {</pre>
 dev <- LogModel$deviance
 nullDev <- LogModel$null.deviance
 modelN <- length(LogModel$fitted.values)</pre>
 R.l < -1 - dev / nullDev
 R.cs < \text{-} 1 \text{-} \ exp \ ( \ \text{-} (nullDev \ \text{-} \ dev) \ / \ modelN)
 R.n <- R.cs \, / \, ( \,\, 1 \,\, \text{--} ( \,\, exp \,\, (\text{-(nullDev} \, / \,\, modelN))))
 cat("Pseudo R^2 for logistic regression\n")
 cat("Hosmer and Lemeshow R^2 ", round(R.1, 3), "\n")
 cat("Cox and Snell R^2
                               ", round(R.cs, 3), "\n")
 cat("Nagelkerke R^2
                              ", round(R.n, 3), "\n")
logisticPseudoR2s(model2)
#To get Odds Ratios
exp(model1$coefficients)
#For Confidence intervals
exp(confint(model2))
#Predicted Probabilities
train$predictedProbabilities <- fitted(model2)</pre>
head(data.frame(train$predictedProbabilities, train$subscribed))
#Analysing the Residuals
resid(model2)
```

```
train$standardisedResiduals <- rstandard(model2)</pre>
train$studentisedResiduals <- rstudent(model2)</pre>
sum(train$standardisedResiduals > 1.96)
#Examining Influential Cases
train$cook <- cooks.distance(model2)
sum(train$cook > 1)
#Examining leverage
train$leverage <- hatvalues(model2)</pre>
sum(train\$leverage > 0.0009)
vif(model2)
predictions<- predict(model2, test, type = "response")</pre>
class_pred <- as.factor(ifelse(predictions > .5, "yes", "no"))
postResample(class_pred, test$subscribed)
confusionMatrix(data=class_pred, test$subscribed)
#Model3
formula3 <- subscribed ~ age+ poutcome+month+ emp.var.rate +campaign +previous + euribor3m +
cons.conf.idx + nr.employed
model3 = glm(formula3,data = train,family = "binomial")
summary(model3)
logisticPseudoR2s <- function(LogModel) {</pre>
 dev <- LogModel$deviance
 nullDev <- LogModel$null.deviance
 modelN <- length(LogModel$fitted.values)
 R.l < -1 - dev / nullDev
 R.cs <- 1- exp ( -(nullDev - dev) / modelN)
 R.n <- R.cs / (1 - (exp(-(nullDev/modelN))))
 cat("Pseudo R^2 for logistic regression\n")
 cat("Hosmer and Lemeshow R^2 ", round(R.1, 3), "\n")
                             ", round(R.cs, 3), "\n")
 cat("Cox and Snell R^2
```

```
cat("Nagelkerke R^2
                            ", round(R.n, 3), "\n")
}
logisticPseudoR2s(model3)
#To get Odds Ratios
exp(model3$coefficients)
#For Confidence intervals
exp(confint(model3))
#Predicted Probabilities
train$predictedProbabilities <- fitted(model3)</pre>
head(data.frame(train$predictedProbabilities, train$subscribed))
#Analysing the Residuals
train$standardisedResiduals <- rstandard(model3)</pre>
train$studentisedResiduals <- rstudent(model3)</pre>
sum(train$standardisedResiduals > 1.96)
#Examining Influential Cases
train$cook <- cooks.distance(model3)</pre>
sum(train$cook > 1)
#Examining leverage
train$leverage <- hatvalues(model3)</pre>
sum(train$leverage > 0.0009)
vif(model3)
predictions<- predict(model3, test, type = "response")</pre>
class_pred <- as.factor(ifelse(predictions > .5, "yes", "no"))
postResample(class_pred, test$subscribed)
confusionMatrix(data=class_pred, test$subscribed)
#model4
formula4 <- subscribed ~ month + poutcome+contact + cons.price.idx + cons.conf.idx +
nr.employed
model4 = glm(formula4,data = train,family = "binomial")
```

```
summary(model4)
logisticPseudoR2s <- function(LogModel) {</pre>
 dev <- LogModel$deviance
 nullDev <- LogModel$null.deviance
 modelN <- length(LogModel$fitted.values)</pre>
 R.l < - \ 1 - \ dev \ / \ null Dev
 R.cs <- 1- exp (-(nullDev - dev) / modelN)
 R.n <- R.cs / (1 - (exp(-(nullDev/modelN))))
 cat("Pseudo R^2 for logistic regression\n")
 cat("Hosmer and Lemeshow R^2 ", round(R.1, 3), "\n")
 cat("Cox and Snell R^2
                             ", round(R.cs, 3), "\n")
                            ", round(R.n, 3), "\n")
 cat("Nagelkerke R^2
logisticPseudoR2s(model4)
#To get Odds Ratios
exp(model4$coefficients)
#For Confidence intervals
exp(confint(model4))
#Predicted Probabilities
train$predictedProbabilities <- fitted(model4)</pre>
head(data.frame(train$predictedProbabilities, train$subscribed))
#Analysing the Residuals
resid(model4)
train$standardisedResiduals <- rstandard(model4)</pre>
train$studentisedResiduals <- rstudent(model4)</pre>
sum(train$standardisedResiduals > 1.96)
sum(train\$standardisedResiduals > 2.58)
#Examining Influential Cases
```

```
train$cook <- cooks.distance(model4)
sum(train$cook > 1)
#Examining leverage
train$leverage <- hatvalues(model4)
sum(train$leverage > 0.0009)
# Examining VIF
vif(model4)
predictions<- predict(model4, test, type = "response")
class_pred <- as.factor(ifelse(predictions > .5, "yes", "no"))
postResample(class_pred, test$subscribed)
confusionMatrix(data=class_pred, test$subscribed)
```