

# CS203 - Digital Logic Design

Indian Institute of Technology Ropar

August 31, 2020

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# Chapter 1

## Introduction to CS203

Digital means discrete in nature(values as well as time). For example, our computer handle discrete data only, therefore are digital computers.

Analog means continuous in nature(values as well as time). For example, the atmospheric variables, our senses, etc are analog.

### 1.1 Binary Classification

Classification into **two** groups if called *binary classification*. It is easy. For example, in computers, low voltage is classified as 0 and high voltage is classified as 1.

With N bits(binary digits), we can represent  $2^N$  states.

Some rounding off-

- 10 bits -  $2^{10}$  states = 1024  $\approx 10^3$
- 20 bits -  $2^{20}$  states =  $2^{10} \times 2^{10} \approx 10^6$
- 30 bits -  $2^{30}$  states =  $2^{10} \times 2^{10} \times 2^{10} \approx 10^9$  ~ Population of India

### 1.2 Discretization

The process of discretization of analog signal involves setting discrete levels in values as well as time. Figure 1.1 gives some idea.

We lose some information when discretization occurs. To minimize the loss, we can use **Nyquest Criteria**. Also, simply increasing the number of levels will reduce the error.

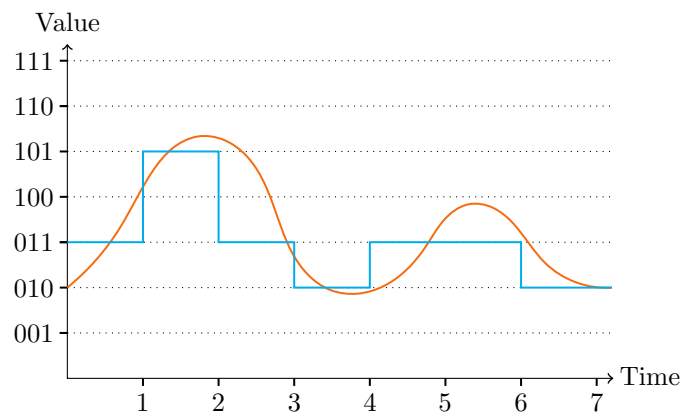


Figure 1.1: Discretization of analog signal

## 1.3 Analog vs Digital System

Our world is analog but our devices are digital. Figure 1.2 shows working of analog and digital systems.

**ADC** - Analog-to-digital converter

**DAC** - Digital-to-analog converter

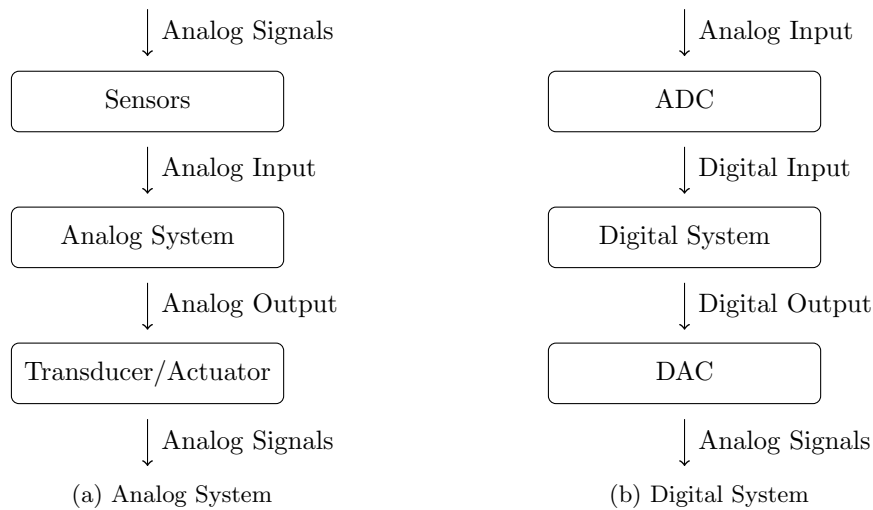


Figure 1.2: Analog and digital systems

### 1.3.1 Advantages of Digital System

- **Precision**
  - Small changes/error in signals does not affect the value. Even if errors occur in digital signal, it is easy to record the error and revert it.
  - Digital signals will produce same output for same input most of the time.
- **Programmability**
  - Each analog system is created for specific use case. But digital systems have generic gates which allow reprogramming.
- **Maintainability**
  - Digital signals are robust to change and can last longer(for years).
- **Design automation**

### 1.3.2 Disadvantages of Digital System

- **Area/Cost**
  - Cost of digital system is more than analog.
- **Power**
- **Performance**
  - Digital signals are slower.
- **Bandwidth**
- **High Frequency Operations**

### 1.3.3 Conclusion

Most systems are going towards digital. But whenever we need very specific solution that required high bandwidth and frequency, analog systems are used. Radio receivers, transmitters, etc. are mostly analog.

## 1.4 Factors pushing the growth story

- **Moore's law**
  - The number of transistors on a unit area of circuit doubles every 18 months.
  - It is not a law but has been pretty accurate till now.
- **Technology**
- **Compute Requirements**
- **Design Automation**

## Chapter 2

# Binary Representation

Historically, different bases(10, 12, 15, 16, 20) have been used. There were two kinds of number system

- **Positional:** Position of a number determines its value. For example, arabic, indic number systems.
- **Non-positional:** Value is largely decided by what symbol is used. For example, roman number system.

Finally, position based decimal system was accepted worldwide because it makes it easy to do calculations.

### 2.1 Positional Number System

Value of symbol depends on its position and radix/base.

$$N = (a_n a_{n-1} \dots a_0)_R = \sum_0^n a_i R^i$$

The definition can be easily extended to fractions.

$$N = (a_n a_{n-1} \dots a_0 a_{-1} \dots a_{-m+1} a_{-m})_R = \sum_0^n a_i R^i$$

Few examples

- $(101101)_2 = 1 \times 2^5 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^0 = 45$
- $(101.101)_2 = 1 \times 2^2 + 1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-3} = 5.625$

#### Decimal to base-R conversion

For converting the number  $N$  in base 10 to a number in base  $R$

1. Divide  $N$  by  $R$ , the remainder is  $a_0$  and quotient is  $Q$
2. Set  $N$  as  $Q$  and repeat the above process to get subsequent digits  $a_1, a_2, \dots$
3. Stop when  $N$  becomes zero

**Example:**  $(24)_{10} = (11000)_2$

$R$	$N$	$Q$	
2	24	12	$a_0 = 0$
2	12	6	$a_1 = 0$
2	6	3	$a_2 = 0$
2	3	1	$a_3 = 1$
2	1	0	$a_4 = 1$
2	0		

For converting fractional part  $F$  to base  $R$

1. Multiply  $F$  with  $R$ , the non-fractional part is  $a_{-1}$  and fractional part is  $F'$
2. Set  $F$  as  $F'$  and repeat the above process to get subsequent digits  $a_{-2}, a_{-3}, \dots$
3. Stop when  $F$  becomes zero

**Example:**  $(0.7)_{10} = (0.1011001100110011 \dots)_2$

$R$	$F$	$F'$	
2	0.7	0.4	$a_{-1} = 1$
2	0.4	0.8	$a_{-2} = 0$
2	0.8	0.6	$a_{-3} = 1$
2	0.6	0.2	$a_{-4} = 1$
2	0.2	0.4	$a_{-5} = 0$
2	0.4	0.8	$a_{-6} = 0$
2	0.8	0.6	$a_{-7} = 1$
2	0.6	0.2	$a_{-8} = 1$
$\vdots$	$\vdots$	$\vdots$	

## 2.2 Hexadecimal Number System

Hexadecimal system requires 16 symbols which are 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F. Hex numbers are generally prefixed by 0x.

### Conversion from binary to hex

To convert a binary number to hex, group the binary number into groups of four (nibbles) from right to left. Then, convert each nibble to hex using a lookup table or simple conversion.

$$(10011110001)_2 \longrightarrow 100 \ 1111 \ 0001 \longrightarrow 0x4F1$$

### Conversion from hex to binary

To convert a hex to binary number, convert each digit to binary and make its length 4 by adding zeros as prefix. Now concatenate these so formed nibbles.

$$0xBAD \longrightarrow 1011 \ 1010 \ 1101 \longrightarrow (101110101101)_2$$

## 2.3 Negative Numbers

### 2.3.1 Sign Magnitude Negative Numbers

We can set one bit to represent the sign. Generally, we choose the most-significant bit as the sign bit.

#### Example

$$\begin{aligned}(1010\ 0011)_2 &= (-35)_{10} \\ (0111\ 1111)_2 &= (127)_{10}\end{aligned}$$

So the range of  $N$ -bit number is  $-(2^{N-1} - 1)$  to  $(2^{N-1} - 1)$ . Also, such representation has two zeros - positive and negative.

#### Addition and subtraction

Addition and subtraction becomes difficult.

- We have to look at the signs and then choose what operation will be performed.
- Two zeros create confusion.
- Either operation may result in addition or subtraction
- Complex hardware implementation
  - Requires both adder and subtractor
  - Requires controller that determine which hardware to use
  - Separate handling of sign

### 2.3.2 1's Complement

For obtaining  $-u$  flip all the bits of  $u$ . Here also,  $N^{th}$  bit represents sign and  $N - 1$  bits represent magnitude.

#### Example

$$\begin{aligned}(+13)_{10} &= (0000\ 1101)_2 & (+69)_{10} &= (0010\ 0101)_2 \\ (-13)_{10} &= (1111\ 0010)_2 & (-69)_{10} &= (1101\ 1010)_2\end{aligned}$$

So the range of  $N$ -bit number is  $-(2^{N-1} - 1)$  to  $(2^{N-1} - 1)$ .

#### Mathematical representation

We know  $2^N - 1 = 111 \dots 1$

$$\therefore -u = \sim |u| = 2^N - 1 - |u|$$

#### Addition and subtraction

Addition and subtraction is difficult.

- In *end-around carry* condition, the wrapped bit must be added to the right-most bit.
- In *end-around borrow* condition, the wrapped bit must be subtracted from the right-most bit.
- There are two representation of zeros.



### 2.3.3 Bias Representation

Let  $F(u)$  be the value of binary representation of  $u$ . In bias represent

$$F(u) = u + bias$$

**Example** (with bias = 127)

$$\begin{aligned}(1)_{10} &= (1000\ 0000)_2 \\ (-127)_{10} &= (0000\ 0000)_2 \\ (128)_{10} &= (1111\ 1111)_2\end{aligned}$$

#### Problems

- Bias should be adjusted while adding two numbers

$$F(u + v) = F(u) + F(v) - bias$$

- Bias should be standardized

### 2.3.4 2's Complement

When  $u \geq 0$

$$F(u) = |u|$$

When  $u < 0$

$$F(u) = 2^N - |u| = \sim |u| + 1$$

#### Properties

- Single zero
- Most-significant bit represents sign(except in case of zero)
- $F(-u) = 2^N - F(u)$
- Range is from  $-2^{N-1}$  to  $(2^{N-1} - 1)$

#### Arithmetic

- Addition

$$F(u + v) = F(u) + F(v)$$

- Subtraction

$$F(u - v) = F(u) + F(-v)$$

- Multiplication (assume no overflow)

$$F(u \times v) = F(u) \times F(v)$$

#### Overflow and Underflow

- If sign of both operands are same and result if of opposite sign or result is 0, overflow/underflow has occurred.
- If sign of both operands are different, overflow cannot occur.

**Converting N-bit number to M-bit number**

To convert to  $N$ -bit number to  $M$ -bit number ( $M \geq N$ ) keep adding the sign bit as prefix until the size becomes  $M$ .

Example (Converting 4-bit number to 8-bit number)

$$\begin{aligned}(3)_{10} &= (\textcolor{red}{1}101)_2 = (\textcolor{red}{1111} \textcolor{red}{1}101)_2 \\ (5)_{10} &= (\textcolor{red}{0}101)_2 = (\textcolor{red}{0000} \textcolor{red}{0}101)_2\end{aligned}$$

**2.3.5 Number Circle**

An efficient way to see different representations in action.

- To add  $x$  to  $u$ , move  $x$  steps in clockwise direction from  $u$ .
- To subtract  $x$  from  $u$ , move  $x$  steps in counter-clockwise direction from  $u$ .
- Crossing dotted lines will result in underflow/overflow.

Visit <https://thesis.laszlokorte.de/demo/number-circle.html> to experiment.

**2.4 Representing Decimal Numbers and Characters**

We have to find a one-to-one mapping between binary combination and corresponding decimal value. *Is there any option better than positional number system?*

**2.4.1 Binary Coded Decimal (BCD) Number System**

In BCD, each decimal digit is mapped to a nibble of its value. These nibbles are concatenated to get the binary representation.

8421 BCD number are numbers where the bits of nibbles have weights 8, 4, 2 and 1. It is the *default* BCD representation. **Example**

$$(5682)_{10} \longrightarrow (0101 \ 01110 \ 1000 \ 0010)_2$$

**Advantages**

- No complex procedure for conversion from decimal representation required.
- BCD numbers are intuitive i.e. one can look at the binary number and grasp the value quickly.

Initial computer (e.g. IBM System/360) used BCD numbers.

**Disadvantages**

- During arithmetic, we have to take care that value of no nibble exceeds 9. In case, when value exceeds 9 (i.e. the value is not a valid BCD number), then add  $(0110)_2$  to the result.

**Why did we add 6?**

[1] Because there are 6 invalid states in BCD numbers. To skip those states, we added 6.

**2.4.2 Excess 3 Code**

It is another BCD representation where value of each digit is 3 more in binary than in decimal.

**Note:** Be careful while adding numbers in *Excess 3 code*.

$$\text{Excess3Add}(u, v) = \text{Excess3}(u) + \text{Excess3}(v) - (0011)_2$$

Decimal	Excess 3 Code
0	0011
1	0100
2	0101
3	0110
$\vdots$	$\vdots$
8	1011
9	1100

Table 2.1: Excess 3 code mapping

**Advantages**

- **Self Complementing**

9's complement can be obtained by inverting all the bits.

$$\text{Excess3}(9 - x) = \sim \text{Excess3}(x)$$

It helps in doing subtraction by addition.

Consider the addition of two digits  $d_1$  and  $d_2$  (digits are represented in excess 3 code).

$$\text{Excess3Subtraction}(d_2, d_1) = \sim \text{Excess3Add}(\sim d_2, d_1)$$

**2.4.3 Two-out-of-five Code**

It is another BCD representation where each decimal digit is mapped to a group of 5 bits. Each digit's binary representation contains **exactly** two 1s.

Decimal	Two-out-of-five Code
0	00011
1	00101
2	00110
3	01001
4	01010
5	01100
6	10001
7	10010
8	10100
9	11000

Table 2.2: Two-out-of-five code mapping

**Advantages**

- **Error Resilient**

If any or several bits flip, there is a high chance that it will not contain 2 ones. In that case, we can know that the value is incorrect and we can redo the computation.

2.4.4 Gray Code

It is another BCD representation. It is a low power code because the trasitions between adjacent numbers is minimum.

Decimal	Gray Code
0	0000
1	0001
2	0011
3	0010
4	0110
5	1110
6	1010
7	1011
8	1001
9	1000

Table 2.3: Gray code mapping

Advantages

- **Low Power Consumption**  
Since the transition between adjacent numbers is minimum, power consumption is minimized.

Gray Code Sequence

To generate Gray code sequence, do the following[2]:

1. Commence with the simplest Gray code possible; that is, for a single bit.
2. Create a mirror image of the existing Gray code below the original values.
3. Prefix the original values with 0s and the mirrored values with 1s.
4. Repeat step 2 and 3 until the desired width is achieved.

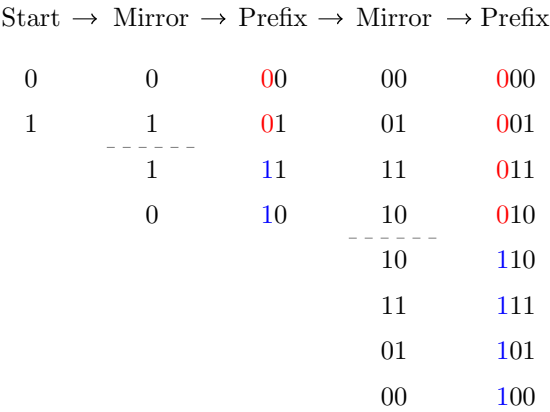


Figure 2.1: Gray code generation upto 3 bits

## 2.5 Representing Characters

- **ASCII**  
Using 8-bit number for each commonly used character
- **UTF-8**
  - Compatible with ASCII
  - Uses 1 to 6 bytes
- **UTF-16**

## 2.6 Real Numbers

How would we represent a decimal point in binary?

### 2.6.1 Fixed Point Numbers

In this kind of numbers, we would fix some bits for only the fractional part.

**Example** (Assuming 4 decimal digits can be represented and decimal point is after 2 digits)

2300 would represent 23.00

123 would represent 1.23

1 would represent 0.01

100 would represent 1.00

### 2.6.2 Floating Point Numbers

To represent very large and very small number, we use scientific notation.

In decimal :  $129 = 1.29 \times 10^2$

In binary :  $1000001 = 1.000001 \times 2^6$

Such numbers have 3 parts:

1. **Significand**( $s$ ): The digit and sign before point  
Can only be +1 or -1
2. **Mantissa**( $m$ ): The fractional part of number  
Can only be positive
3. **Exponent**( $e$ ): The power of 2  
Can be positive or negative

#### Typical representation

- 1 bit is reserved for significand
- Next few bits for exponent
- Remaining bits for mantissa

### 2.6.3 IEEE 754 Single Precision Floating Point Numbers

32-bit number (single precision)

- 1 bit is reserved for sign ( $s$ )
- 8 bits for exponent ( $e$ )
  - Bias representation (with  $bias = 127$ )  
Bias method is sufficient because only addition is need in exponent
  - $(00000000)_2$  and  $(11111111)_2$  are reserved for special purpose
- 23 bits for mantissa ( $m$ )
- $N = (-1)^s \times (1.m) \times 2^e$

[3] Visit <https://www.geeksforgeeks.org/ieee-standard-754-floating-point-numbers/> for more information.

[4] <https://www.h-schmidt.net/FloatConverter/IEEE754.html> is an online converter.

#### Example

Converting 24.25 to IEEE 754 floating point number	
Decimal number	$24.25 = 16 + 8 + 0.25$
Binary number	11000.01
Scientific form	$1.100001 \times 2^4$
Significand	0
Mantissa	100 0010 0000 0000 0000 0000
Exponent	$(127 + 4)_{10} = (1000\ 0011)_2$
Floating Point Number	<span style="color: red;">0</span> <span style="color: blue;">100 0001</span> 1100 0010 0000 0000 0000 0000
In Hex	0x41920000

Converting -0.625 to IEEE 754 floating point number	
Decimal number	$-0.625 = -1 \times (0.5 + 0.125)$
Binary number	-0.101
Scientific form	$-1.01 \times 2^{-1}$
Significand	1
Mantissa	010 0000 0000 0000 0000 0000
Exponent	$(127 + 0)_{10} = (1111\ 1111)_2$
Floating Point Number	<span style="color: red;">1</span> <span style="color: blue;">111 1111</span> 1010 0000 0000 0000 0000 0000
In Hex	0xFFA00000

### 2.6.4 Denormal/subnormal Numbers

In a normal floating-point value, there are no leading zeros in the significand; rather, leading zeros are removed by adjusting the exponent (for example, the number 0.0123 would be written

Converting 0xC2630000 to decimal	
In Hex	0xC2630000
Floating Point Number	1100 0010 0110 0011 0000 0000 0000 0000
Significand	1
Exponent	$(100\ 0010\ 0)_2 = (127 + 5)_{10}$
Mantissa	110 0011 0000 0000 0000 0000
Scientific form	$1.1100011 \times 2^5$
Binary number	111000.11
Decimal number	56.75

as  $1.23 \times 10^{-2}$ ). Denormal numbers are numbers where this representation would result in an exponent that is below the smallest representable exponent (the exponent usually having a limited range). Such numbers are represented using leading zeros in the significand. [5]

### 2.6.5 Special Values

IEEE reserves exponent field values of all 0s and all 1s to denote special values in the floating-point scheme. [6]

#### Denormalized

If the exponent is all 0s, then the value is a *denormalized number* (section 2.6.4), which now has an assumed leading 0 before the binary point. Thus,

$$N = (-1)^s \times 0.m \times 2^{-126}$$

As denormalized numbers get smaller, they lose precision as left bits of the mantissa become zeros.

#### Zero

Zero is a denormalized number, with all bits in exponent and mantissa set to 0. If significand is 1, it represents -0, else +0. Also,

$$+0 = -0$$

#### Infinity

When exponent is all 1s and mantissa is all 0s, it represents *infinity*. If significand is 1, it represents  $-\infty$ , else  $+\infty$ .

#### Not a Number (NaN)

The value *NaN* is used to represent a value that does not represent a real number. NaN's are represented by a bit pattern with exponent of all 1s and a non-zero mantissa. There are two types on NaN's

1. **Quiet NaN (QNaN)**

A QNaN is a NaN with the most-significant mantissa bit set to 1. It represents *indeterminate operations*.

2. **Signalling NaN (SNaN)**

A SNaN is a NaN with the most-significant mantissa bit set to 0. It represents *invalid operations*.

### 2.6.6 IEEE 754 Half Precision Floating Point Numbers

16-bit number (half precision)

- 1 bit is reserved for significand ( $s$ )
- 5 bits for exponent ( $e$ )
  - Bias representation (with  $bias = 15$ )
  - $(00000)_2$  and  $(11111)_2$  are reserved for special purpose
- 10 bits for mantissa ( $m$ )

### 2.6.7 IEEE 754 Double Precision Floating Point Numbers

64-bit number (double precision)

- 1 bit is reserved for significand ( $s$ )
- 11 bits for exponent ( $e$ )
  - Bias representation (with  $bias = 1023$ )
  - $(00000000000)_2$  and  $(11111111111)_2$  are reserved for special purpose
- 52 bits for mantissa ( $m$ )

### 2.6.8 Issues with Floating Point Numbers

- **Quantization Issues**
  - Different rounding can lead to different results
  - Different formats have different precision
  - Accumulation of errors
  - Non-terminating numbers cannot be represented
- **Hardware/Computational Costs**



## Chapter 3

# Boolean Algebra

Boolean algebra is algebra on boolean values - *true* and *false*. These boolean values can be represented by bits - 0 for *false* and 1 for *true*.

A *boolean function* is a function that takes boolean inputs, performs only boolean operations and returns a boolean output. A *truth table* is a table listing outcomes of a function for every combination of input variables.

### 3.1 Basic Operations

There are three basic operations in boolean algebra.

1. **AND**

$A \text{ AND } B$  is *true* iff both  $A$  and  $B$  are *true*.

$A$	$B$	$A \cdot B$
0	0	0
0	1	0
1	0	0
1	1	1

Table 3.1: Truth table for AND

2. **OR**

$A \text{ OR } B$  is *true* iff at least one of  $A$  and  $B$  is *true*.

$A$	$B$	$A \cdot B$
0	0	0
0	1	1
1	0	1
1	1	1

Table 3.2: Truth table for OR

3. **OR**

NOT  $A$  is *true* iff  $A$  is *false*.

$A$	$A'$
0	1
1	0

Table 3.3: Truth table for NOT

## 3.2 Basic Theorems

- **Operation with 0**

$$X + 0 = X$$

$$X \cdot 0 = 0$$

- **Operation with 1**

$$X + 1 = 1$$

$$X \cdot 1 = X$$

- **Idempotent Law**

$$X + X = X$$

$$X \cdot X = X$$

- **Involution Law**

$$(X')' = X$$

- **Law of Complementarity**

$$X + X' = 1$$

$$X \cdot X' = 0$$

- **Commutative Law**

$$X + Y = Y + X$$

$$X \cdot Y = Y \cdot X$$

- **Associative Law**

$$(X + Y) + Z = X + (Y + Z) = X + Y + Z$$

$$(X \cdot Y) \cdot Z = X \cdot (Y \cdot Z) = X \cdot Y \cdot Z$$

- **Distributive Law**

$$X \cdot (Y + Z) = X \cdot Y + X \cdot Z$$

$$X + (Y \cdot Z) = (X + Y) \cdot (X + Z)$$

- DeMorgans's Law

$$(X + Y)' = X' \cdot Y'$$

$$(X \cdot Y)' = X' + Y'$$

### 3.3 Duality Principle

0 is identity for OR. 1 is identity for AND.

Laws of boolean algebra remain same if operators and identity elements are interchanged.

In simple words, if in a boolean equation, all 0s and 1s are exchanged and all OR operators and all AND operators are exchanged with each other, the boolean equation continues to hold its validity.

### 3.4 Simplification Theorems

#### 1. Uniting

$$X \cdot Y + X \cdot Y' = X$$

$$(X + Y) \cdot (X + Y') = X$$

#### 2. Absorption

$$X + X \cdot Y = X$$

$$X \cdot (X + Y) = X$$

#### 3. Elimination

$$X + (X' \cdot Y) = X + Y$$

$$X \cdot (X' + Y) = X \cdot Y$$

#### 4. Consensus

$$X \cdot Y + X' \cdot Z + Y \cdot Z = X \cdot Y + X' \cdot Z$$

$$(X + Y) \cdot (X' + Z) \cdot (Y + Z) = (X + Y) \cdot (X' + Z)$$

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