

# STAT 429 Project: US Housing Market

Kunal Bhardwaj

2024-02-23

```
library(readr)
MSPUS <- read_csv("Data/MSPUS.csv",
                  col_types = cols(Date = col_date(format = "%Y-%m-%d")))

MSACSR <- read_csv("Data/MSACSR.csv",
                  col_types = cols(Date = col_date(format = "%Y-%m-%d")))

HOUST <- read_csv("Data/HOUST.csv",
                  col_types = cols(Date = col_date(format = "%Y-%m-%d"),
                                   HOUST = col_number()))

RHORUSQ156N <- read_csv("Data/RHORUSQ156N.csv",
                       col_types = cols(Date = col_date(format = "%Y-%m-%d")))

MORTGAGE30US <- read_csv("Data/MORTGAGE30US.csv",
                       col_types = cols(Date = col_date(format = "%Y-%m-%d"),
                                         MORTGAGE30US = col_number()))
```

```
library(astsa)
library(ggplot2)
library(ggfortify)
library(fpp2)
library(imputeTS) # For handling missing values by imputation
library(tseries) # To carry out ADF & KPSS Tests
library(lmtest) # To carry out BP-Test

mbspus.ts <- ts(MSPUS$MSPUS[34:244], start = c(1971, 2), frequency = 4, end = c(2023, 4))
msacsr.ts <- ts(MSACSR$MSACSR[34:244], start = c(1971, 2), frequency = 4, end = c(2023, 4))
houst.ts <- ts(HOUST$HOUST[50:261], start = c(1971, 2), frequency = 4, end = c(2023, 4))
rhorusq156n.ts <- ts(RHORUSQ156N$RHORUSQ156N[26:236], start = c(1971, 2), frequency = 4, end = c(2023, 4))

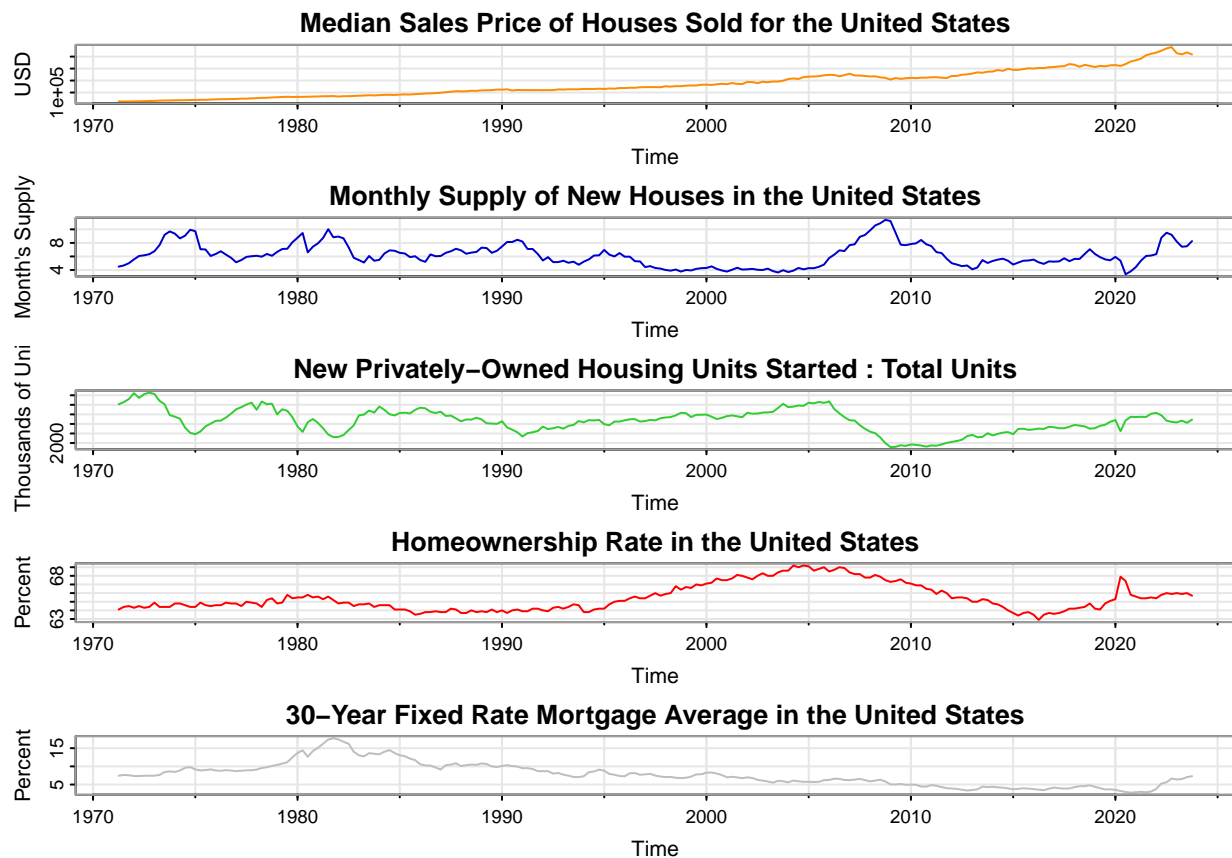
# MORTGAGE30US contains missing values. They are occupied by "."
# They will be imputed by replacing with NA followed by linear interpolation
#MORTGAGE30US$MORTGAGE30US <- ifelse(MORTGAGE30US$MORTGAGE30US == ".",
#                                  NA, MORTGAGE30US$MORTGAGE30US)
#MORTGAGE30US$MORTGAGE30US <- na_interpolation(as.numeric(MORTGAGE30US$MORTGAGE30US))
# Select 2nd column from MORTGAGE30US. The first value on Apr 2 1971 falls on the 14th week
mortgage.ts <- ts(MORTGAGE30US$MORTGAGE30US, start = c(1971, 2), frequency = 4, end = c(2023, 4))

par(mfrow=c(5,1))
tsplot(mbspus.ts, col = "darkorange",
```

```

    main = "Median Sales Price of Houses Sold for the United States",
    ylab = "USD")
tsplot(msacsr.ts, col = "mediumblue",
    main = "Monthly Supply of New Houses in the United States",
    ylab = "Month's Supply")
tsplot(houst.ts, col = "limegreen",
    main = "New Privately-Owned Housing Units Started : Total Units",
    ylab = "Thousands of Units")
tsplot(rhorusq156n.ts, col = "red",
    main = "Homeownership Rate in the United States",
    ylab = "Percent")
tsplot(mortgage.ts, col = "grey",
    main = "30-Year Fixed Rate Mortgage Average in the United States", ylab = "Percent")

```



From the plot of Median Sales Price of Houses Sold, we can see that there exists an obvious trend in the data. Therefore de-trending needs to be carried out to achieve stationarity.

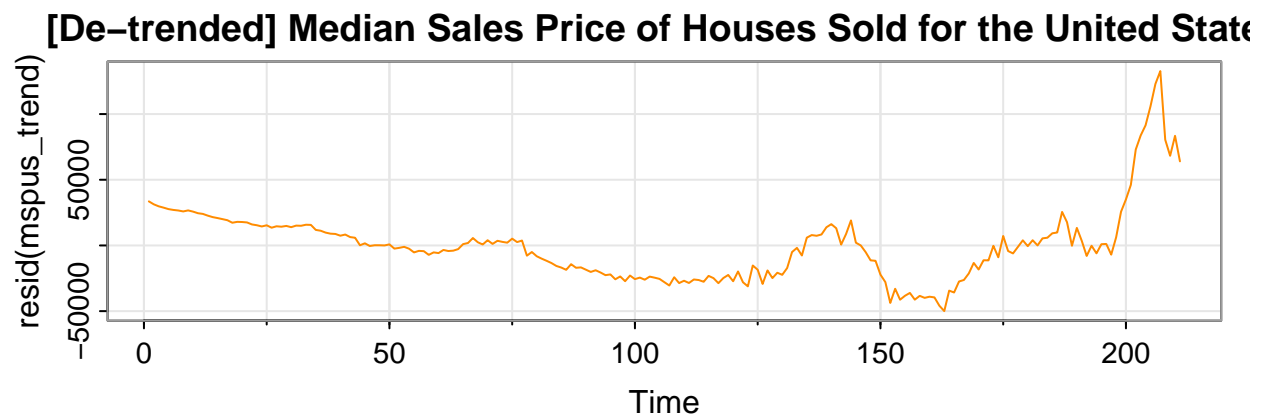
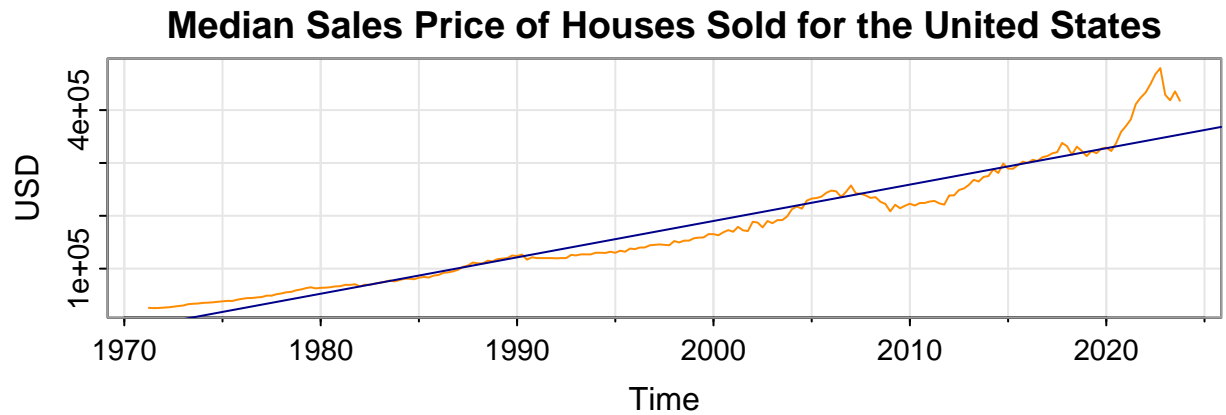
```

# De-trending MSPUS Time Series
mbspus_trend <- lm(mbspus.ts ~ time(mbspus.ts))
#summary(mbspus_trend)

par(mfrow=c(2,1))
tsplot(mbspus.ts, col = "darkorange",
    main = "Median Sales Price of Houses Sold for the United States",
    ylab = "USD")
abline(mbspus_trend, col = "darkblue")

```

```
tsplot(resid(mspus_trend), col = "darkorange",
      main = "[De-trended] Median Sales Price of Houses Sold for the United States")
```



```
# check for Stationarity using (Augmented) Dickey-Fuller Test and KPSS Test
adf.test(resid(mspus_trend))
```

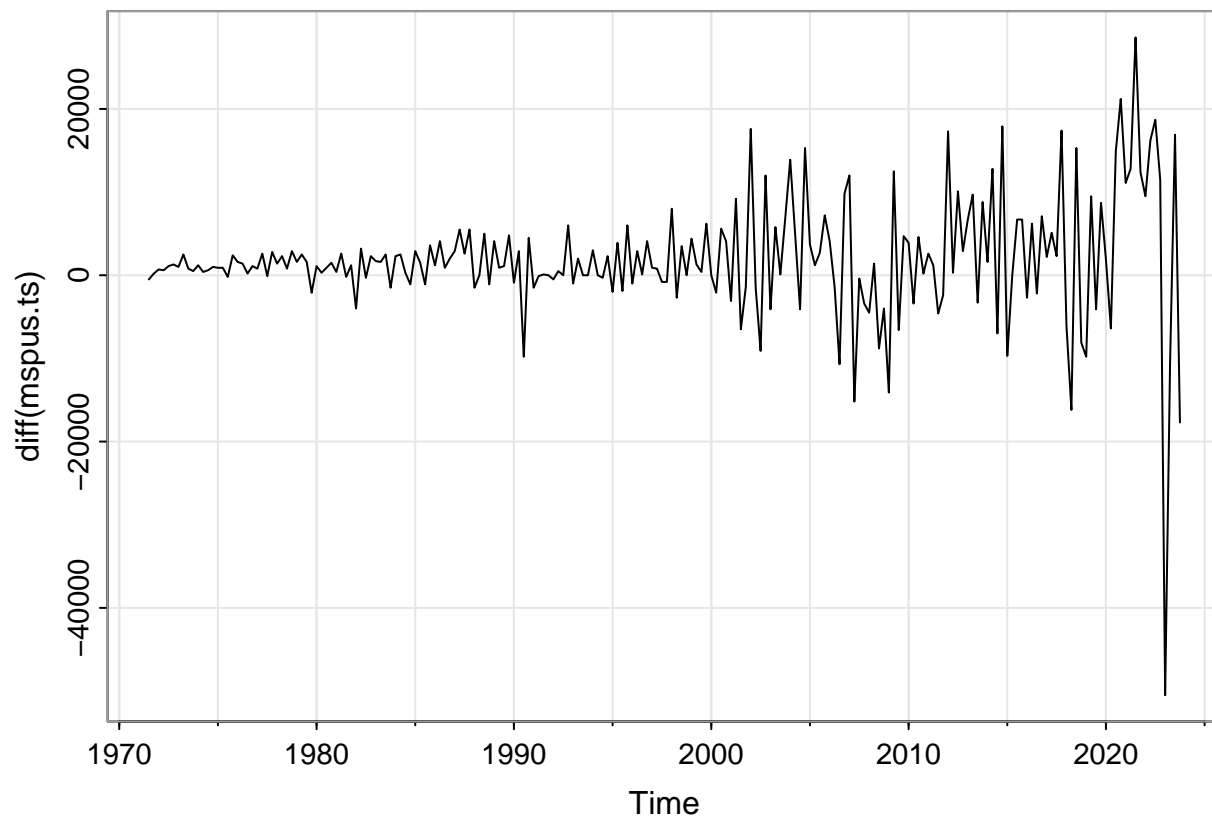
```
##
## Augmented Dickey-Fuller Test
##
## data: resid(mspus_trend)
## Dickey-Fuller = -3.5527, Lag order = 5, p-value = 0.03894
## alternative hypothesis: stationary
```

```
kpss.test(resid(mspus_trend))
```

```
##
## KPSS Test for Level Stationarity
##
## data: resid(mspus_trend)
## KPSS Level = 0.58369, Truncation lag parameter = 4, p-value = 0.02412
```

Both ADF and KPSS tests conclude that the MSPUS de-trended series is non-stationary. We will try differencing to achieve stationarity.

```
# Differencing MSPUS Time Series
tsplot(diff(mspus.ts))
```



```
adf.test(diff(mspus.ts))
```

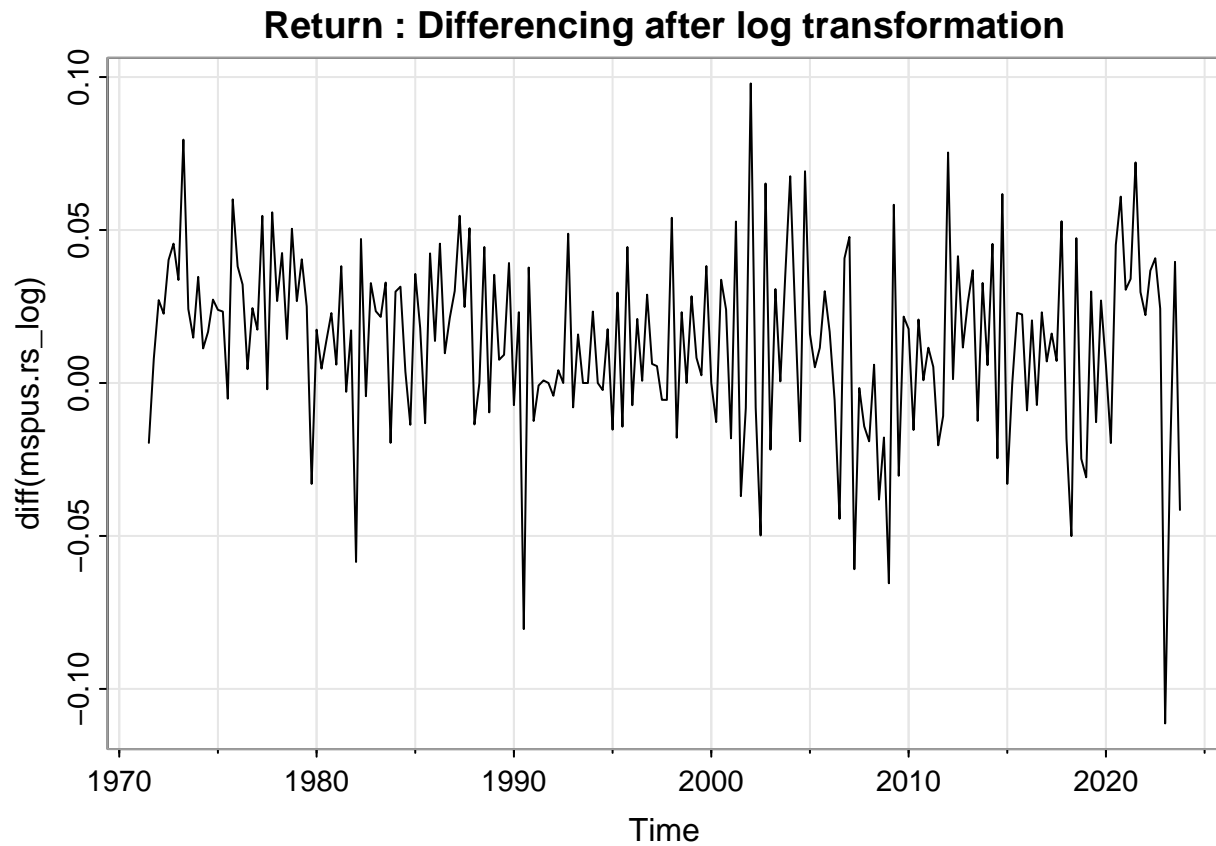
```
##
## Augmented Dickey-Fuller Test
##
## data: diff(mspus.ts)
## Dickey-Fuller = -4.6871, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
```

```
kpss.test(diff(mspus.ts))
```

```
##
## KPSS Test for Level Stationarity
##
## data: diff(mspus.ts)
## KPSS Level = 0.25017, Truncation lag parameter = 4, p-value = 0.1
```

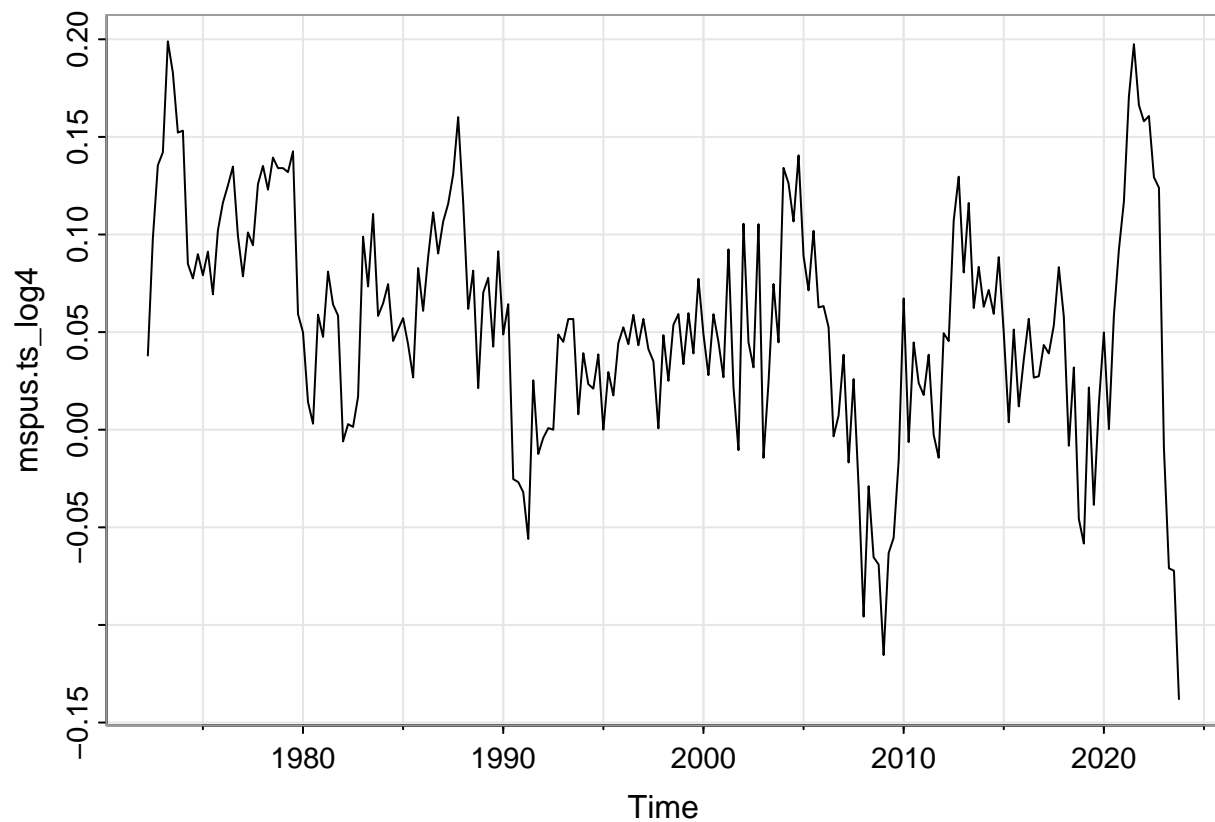
The series passes both these tests of stationarity. But the series exhibits an obvious heteroscedasticity where higher levels are associated with higher variation. A log-transformation is recommended.

```
mspus.rs_log <- log(mspus.ts)
tsplot(diff(mspus.rs_log), main = "Return : Differencing after log transformation") # Return (Differenc
```



The BP Test for homoscedasticity fails for MSPUS,  $\log(\text{MSPUS})$ ,  $\text{diff}(\text{MSPUS})$ ,  $\text{diff}(\text{MSPUS}, \text{lag} = 4)$ ,  $\text{diff}(\log(\text{MSPUS}))$ , and  $\text{diff}(\text{resid}(\text{mspus\_trend}))$ . Will try differencing with a lag of 4 after log transformation.

```
# Differencing with a lag of 4 after taking log
mspus.ts_log4 <- diff(log(mspus.ts), lag = 4)
tsplot(mspus.ts_log4)
```



```
adf.test(mspus.ts_log4)
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: mspus.ts_log4  
## Dickey-Fuller = -4.1169, Lag order = 5, p-value = 0.01  
## alternative hypothesis: stationary
```

```
kpss.test(mspus.ts_log4)
```

```
##  
## KPSS Test for Level Stationarity  
##  
## data: mspus.ts_log4  
## KPSS Level = 0.71681, Truncation lag parameter = 4, p-value = 0.01202
```

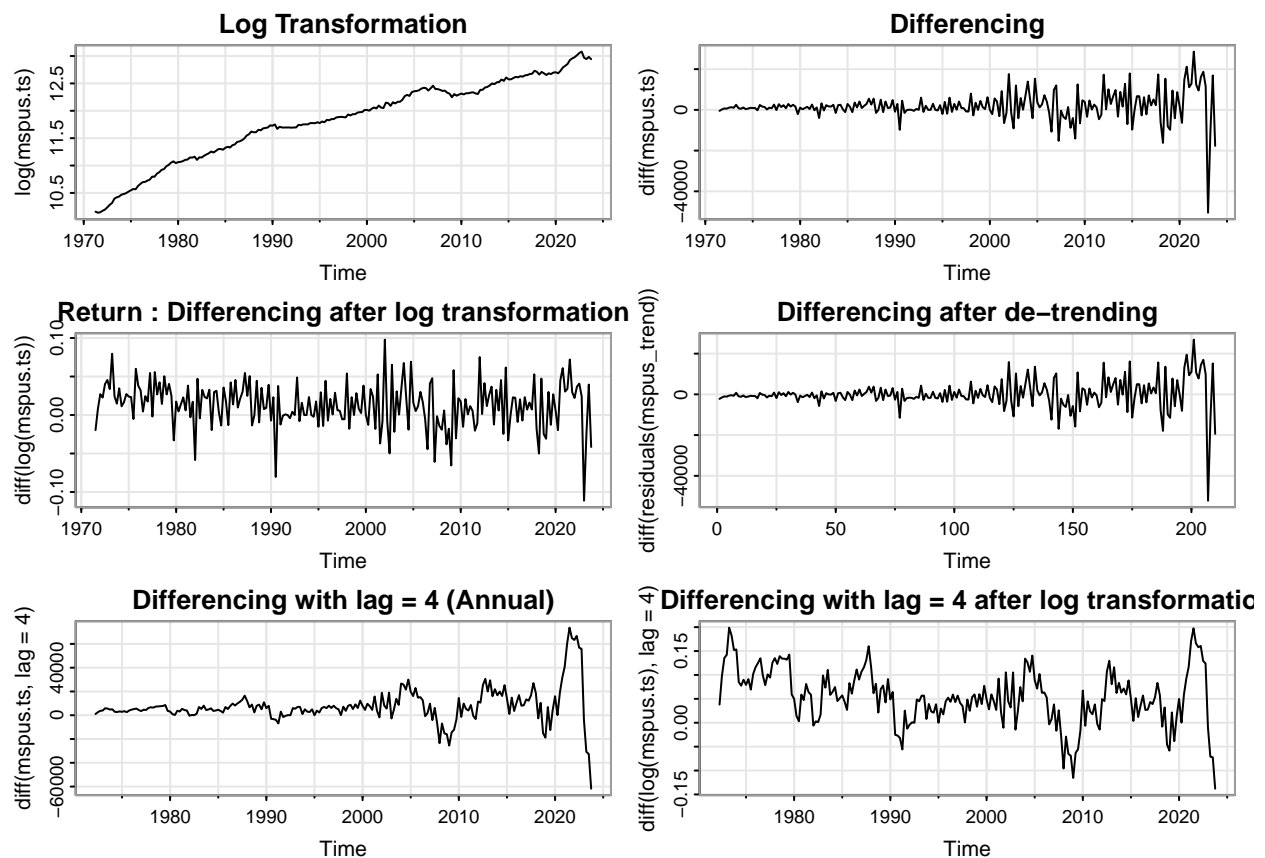
```
bptest(lm(mspus.ts_log4 ~ time(mspus.ts_log4)))
```

```
##  
## studentized Breusch-Pagan test  
##  
## data: lm(mspus.ts_log4 ~ time(mspus.ts_log4))  
## BP = 15.768, df = 1, p-value = 7.162e-05
```

*# Log transformation of the differencing at lag 4 is not carried out because it produces NaNs*

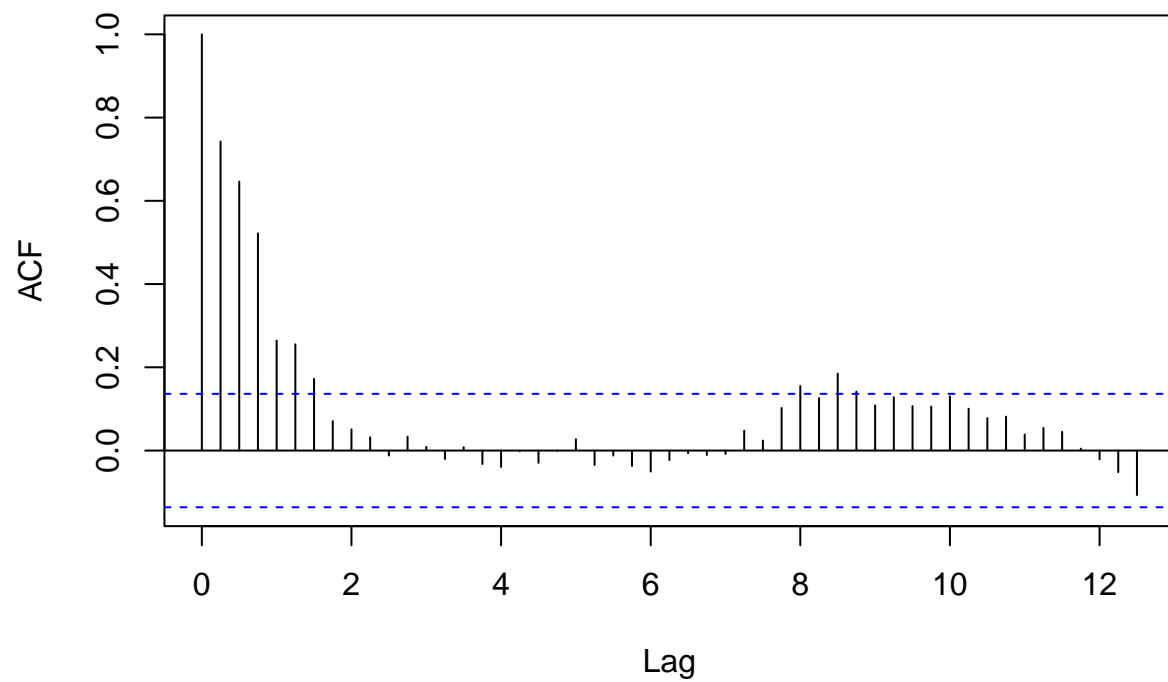
Differencing with a lag of 4 after taking log passes ADF Test & KPSS tests of stationarity and BP-Test for homoscedasticity. Taking lag = 4 insted of the default lag = 1 while differencing seems to have helped in removing the seasonality associated with the MSPUS series.

```
par(mfrow=c(3,2))
tsplot(log(mspus.ts), main = "Log Transformation") # Log Transformation
tsplot(diff(mspus.ts), main = "Differencing") # Differencing
tsplot(diff(log(mspus.ts)), main = "Return : Differencing after log transformation") # Return (Differen
tsplot(diff(residuals(mspus_trend)), main = "Differencing after de-trending") # Differencing after de-t
tsplot(diff(mspus.ts, lag = 4), main = "Differencing with lag = 4 (Annual)") # Differencing with a lag
tsplot(diff(log(mspus.ts), lag = 4), main = "Differencing with lag = 4 after log transformation")
```



```
# ACF of transformed outcome variable
acf(mspus.ts_log4, lag.max = 50)
```

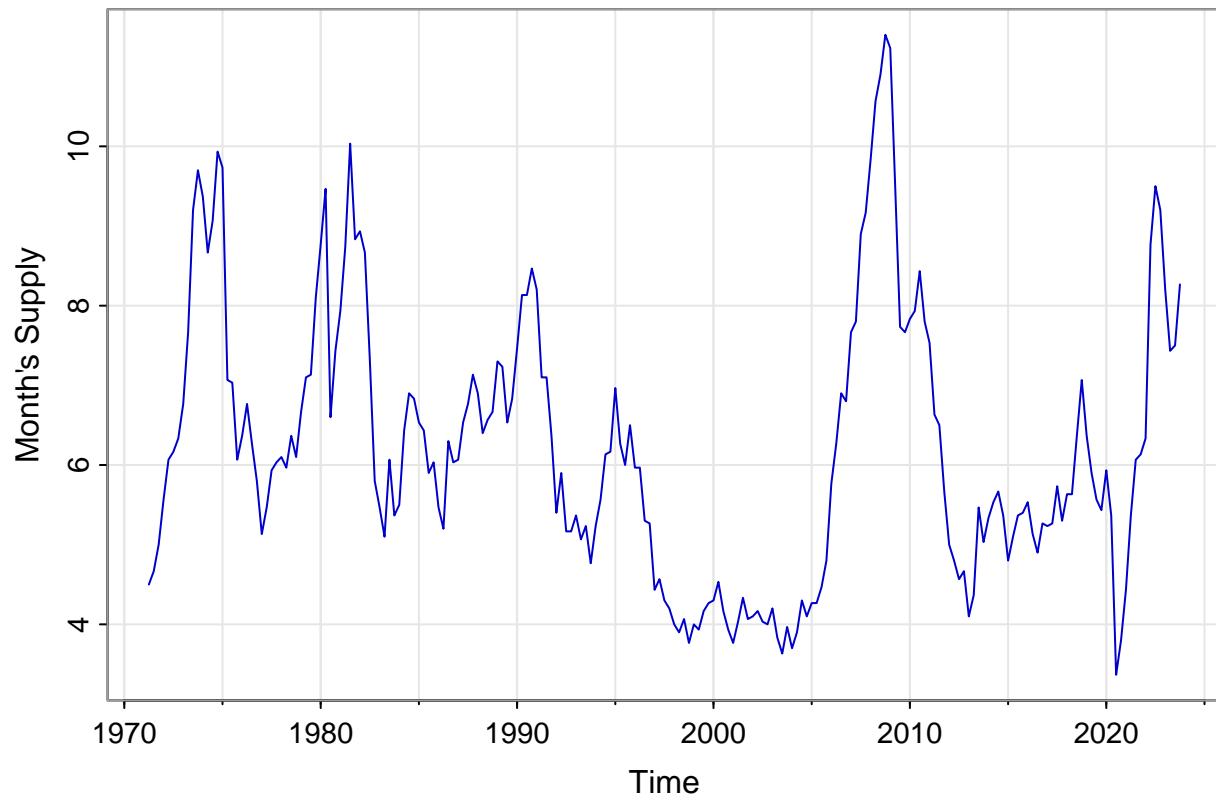
### Series mspus.ts\_log4



```
#msacsr_trend <- lm(msacsr.ts ~ time(msacsr.ts))  
#summary(msacsr_trend)  
tsplot(msacsr.ts, col = "mediumblue",  
       main = "Monthly Supply of New Houses in the United States",  
       ylab = "Month's Supply")
```



## Monthly Supply of New Houses in the United States



```
#abline(msacsr_trend, col = "red")
#tsplot(resid(msacsr_trend), col = "darkblue",
#       main = "[De-trended] Monthly Supply of New Houses in the United States")
adf.test(msacsr.ts)
```

```
##
## Augmented Dickey-Fuller Test
##
## data: msacsr.ts
## Dickey-Fuller = -3.909, Lag order = 5, p-value = 0.01468
## alternative hypothesis: stationary
```

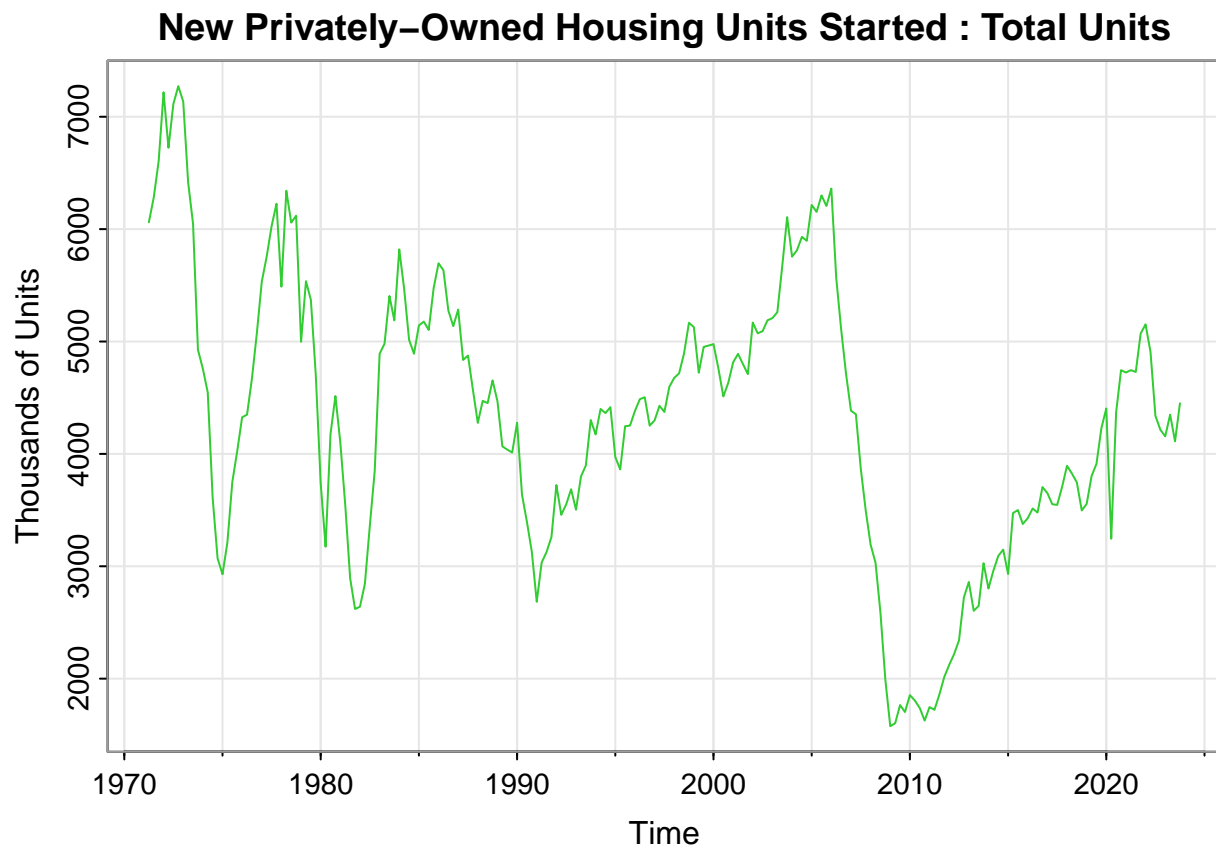
```
kpss.test(msacsr.ts)
```

```
##
## KPSS Test for Level Stationarity
##
## data: msacsr.ts
## KPSS Level = 0.35987, Truncation lag parameter = 4, p-value = 0.09445
```

```
#bptest(lm(msacsr.ts ~ time(msacsr.ts)))
#bptest(lm(log(msacsr.ts) ~ time(msacsr.ts)))
```

Thus the MSACSR series is stationary.

```
tsplot(houst.ts, col = "limegreen",
      main = "New Privately-Owned Housing Units Started : Total Units",
      ylab = "Thousands of Units")
```



```
adf.test(houst.ts)
```

```
## Warning in adf.test(houst.ts): p-value smaller than printed p-value
```

```
##
## Augmented Dickey-Fuller Test
##
## data: houst.ts
## Dickey-Fuller = -4.112, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
```

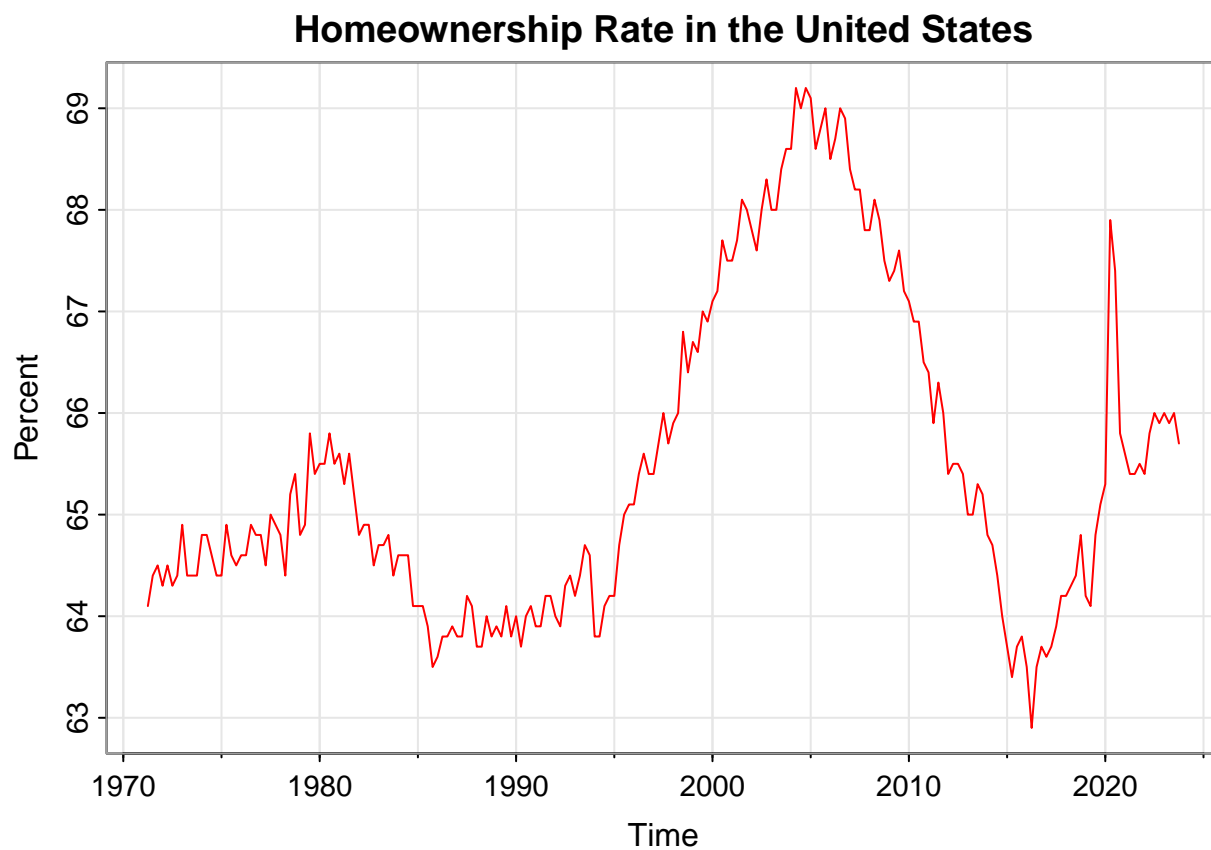
```
kpss.test(houst.ts)
```

```
## Warning in kpss.test(houst.ts): p-value smaller than printed p-value
```

```
##
## KPSS Test for Level Stationarity
##
## data: houst.ts
## KPSS Level = 0.87153, Truncation lag parameter = 4, p-value = 0.01
```

The ADF Test & KPSS tests confirm stationarity of HOUST.

```
tsplot(rhorusq156n.ts, col = "red",  
       main = "Homeownership Rate in the United States",  
       ylab = "Percent")
```



```
adf.test(rhorusq156n.ts)
```

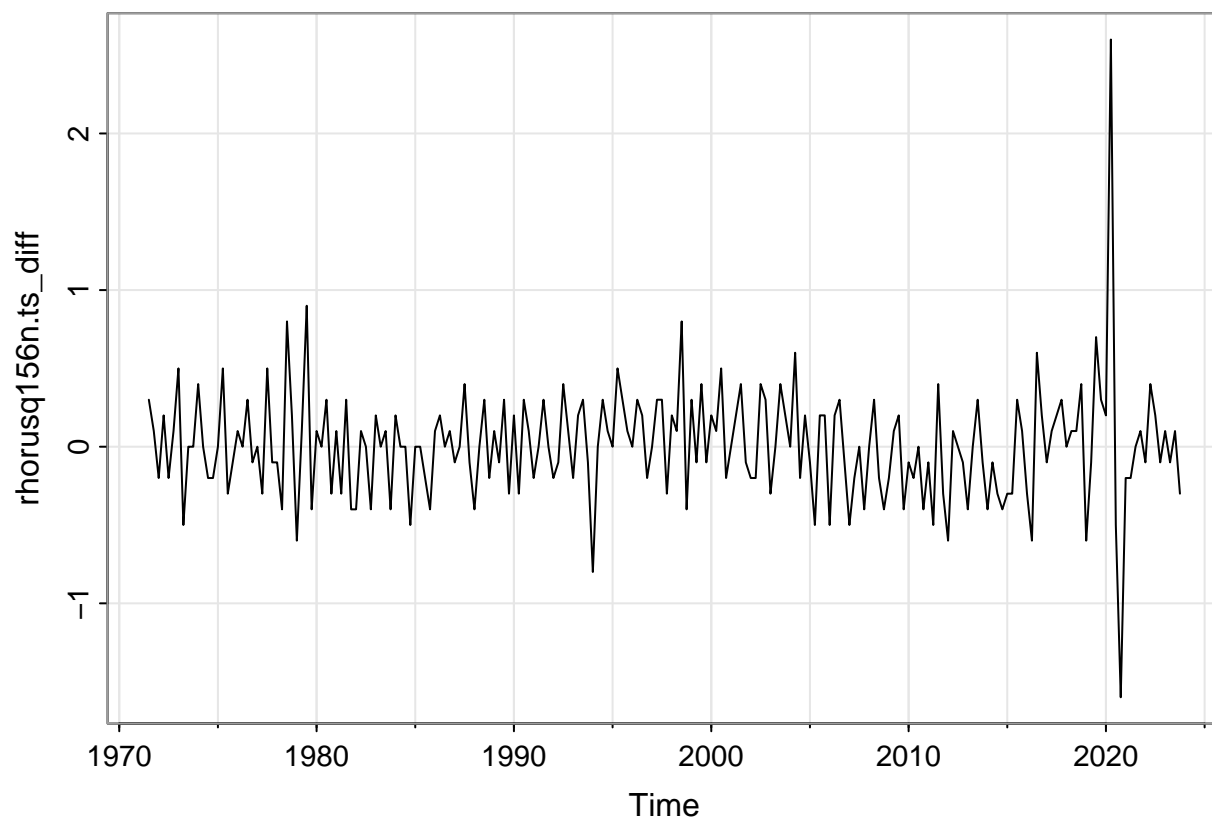
```
##  
## Augmented Dickey-Fuller Test  
##  
## data: rhorusq156n.ts  
## Dickey-Fuller = -1.4017, Lag order = 5, p-value = 0.8269  
## alternative hypothesis: stationary
```

```
kpss.test(rhorusq156n.ts)
```

```
## Warning in kpss.test(rhorusq156n.ts): p-value smaller than printed p-value
```

```
##  
## KPSS Test for Level Stationarity  
##  
## data: rhorusq156n.ts  
## KPSS Level = 0.98637, Truncation lag parameter = 4, p-value = 0.01
```

```
rhorusq156n.ts_diff <- diff(rhorusq156n.ts)
tsplot(rhorusq156n.ts_diff)
```



```
adf.test(rhorusq156n.ts_diff)
```

```
## Warning in adf.test(rhorusq156n.ts_diff): p-value smaller than printed p-value
```

```
##
## Augmented Dickey-Fuller Test
##
## data: rhorusq156n.ts_diff
## Dickey-Fuller = -5.7219, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
```

```
kpss.test(rhorusq156n.ts_diff)
```

```
## Warning in kpss.test(rhorusq156n.ts_diff): p-value greater than printed p-value
```

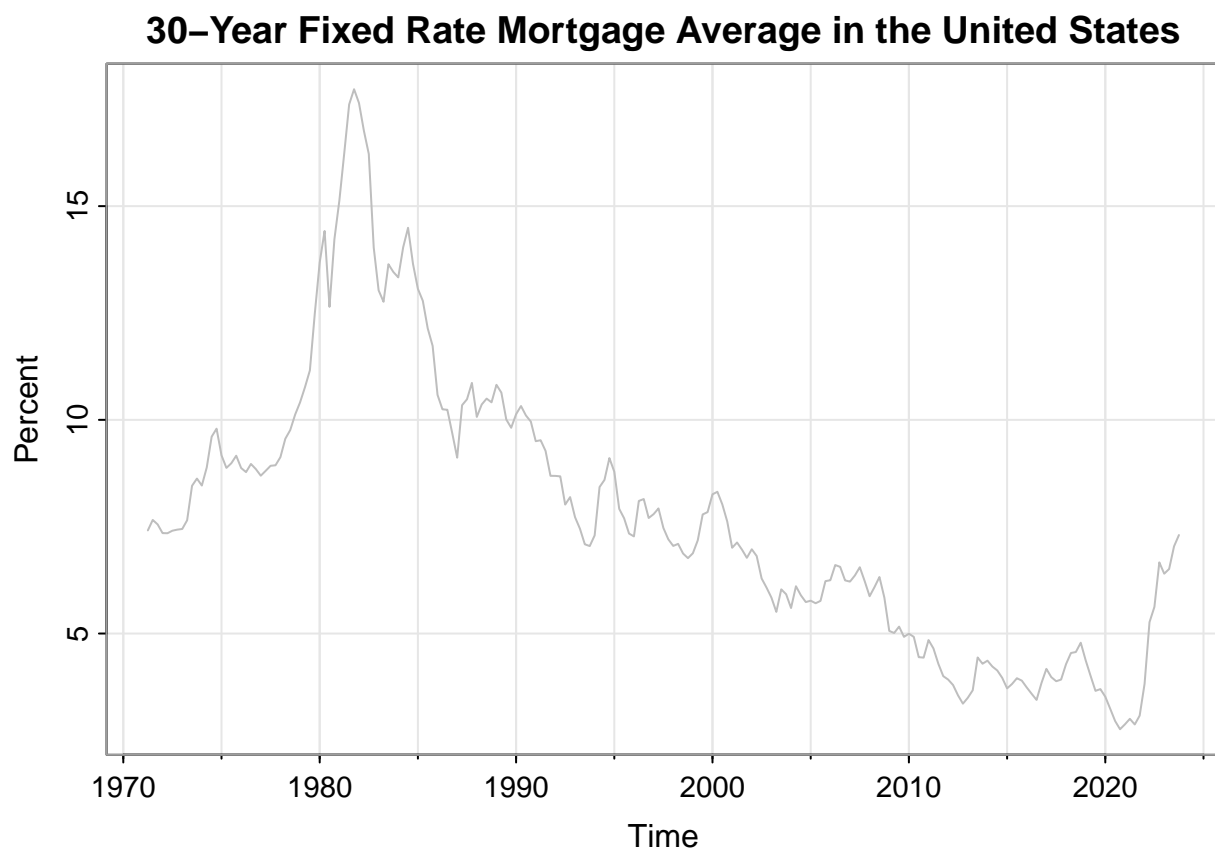
```
##
## KPSS Test for Level Stationarity
##
## data: rhorusq156n.ts_diff
## KPSS Level = 0.1225, Truncation lag parameter = 4, p-value = 0.1
```

```
bptest(lm(rhorusq156n.ts_diff ~ time(rhorusq156n.ts_diff)))
```

```
##  
## studentized Breusch-Pagan test  
##  
## data: lm(rhorusq156n.ts_diff ~ time(rhorusq156n.ts_diff))  
## BP = 3.5926, df = 1, p-value = 0.05804
```

Thus Home Ownership series passes the tests for stationarity and homoscedasticity.

```
tsplot(mortgage.ts, col = "grey",  
       main = "30-Year Fixed Rate Mortgage Average in the United States", ylab = "Percent")
```



```
adf.test(mortgage.ts)
```

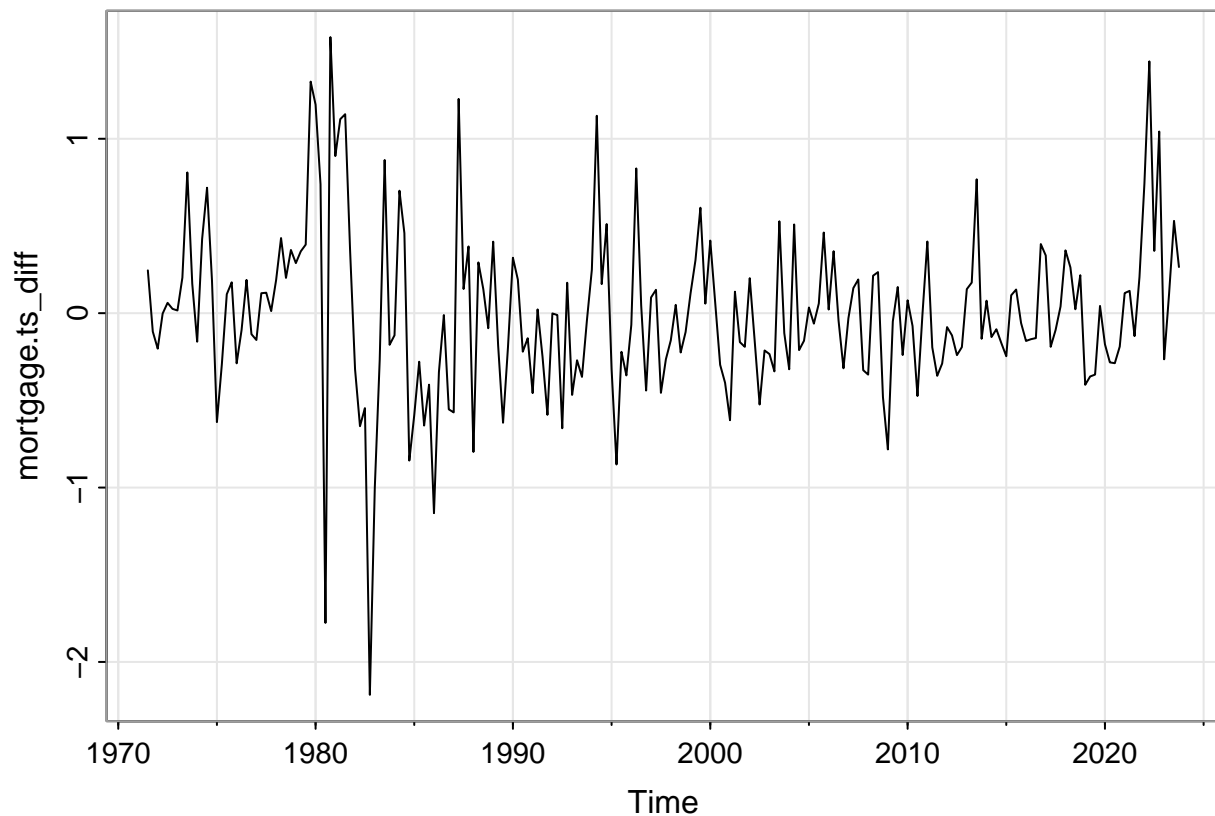
```
##  
## Augmented Dickey-Fuller Test  
##  
## data: mortgage.ts  
## Dickey-Fuller = -2.6749, Lag order = 5, p-value = 0.293  
## alternative hypothesis: stationary
```

```
kpss.test(mortgage.ts)
```

```
## Warning in kpss.test(mortgage.ts): p-value smaller than printed p-value
```

```
##  
## KPSS Test for Level Stationarity  
##  
## data: mortgage.ts  
## KPSS Level = 2.9416, Truncation lag parameter = 4, p-value = 0.01
```

```
mortgage.ts_diff <- diff(mortgage.ts)  
tsplot(mortgage.ts_diff)
```



```
adf.test(mortgage.ts_diff)
```

```
## Warning in adf.test(mortgage.ts_diff): p-value smaller than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: mortgage.ts_diff  
## Dickey-Fuller = -5.5994, Lag order = 5, p-value = 0.01  
## alternative hypothesis: stationary
```

```
kpss.test(mortgage.ts_diff)
```

```
## Warning in kpss.test(mortgage.ts_diff): p-value greater than printed p-value
```

```
##
## KPSS Test for Level Stationarity
##
## data: mortgage.ts_diff
## KPSS Level = 0.13192, Truncation lag parameter = 4, p-value = 0.1
```

```
bptest(lm(mortgage.ts_diff ~ time(mortgage.ts_diff)))
```

```
##
## studentized Breusch-Pagan test
##
## data: lm(mortgage.ts_diff ~ time(mortgage.ts_diff))
## BP = 7.2256, df = 1, p-value = 0.007187
```

```
# Clipping the series to bring them to the same length
msacsr.ts <- ts(MSACSR$MSACSR, start = c(1972, 2), frequency = 4, end = c(2023, 4))
houst.ts <- ts(HOUST$HOUST, start = c(1972, 2), frequency = 4, end = c(2023, 4))
mortgage.ts <- ts(MORTGAGE30US$MORTGAGE30US, start = c(1972, 1), frequency = 4, end = c(2023, 4))
mortgage.ts_diff <- diff(mortgage.ts)
```

```
trend <- time(mspus.ts_log4)
reg_model <- lm(mspus.ts_log4 ~ trend + msacsr.ts + houst.ts + mortgage.ts_diff)
summary(reg_model)
```

```
##
## Call:
## lm(formula = mspus.ts_log4 ~ trend + msacsr.ts + houst.ts + mortgage.ts_diff)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.19579 -0.03126  0.00202  0.03613  0.15346
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2.800e+00  5.056e-01   5.538 9.44e-08 ***
## trend        -1.346e-03  2.519e-04  -5.342 2.47e-07 ***
## msacsr.ts     -3.068e-04  2.437e-03  -0.126  0.89992
## houst.ts      -1.229e-05  3.791e-06  -3.243  0.00138 **
## mortgage.ts_diff -1.579e-02  7.925e-03  -1.993  0.04764 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.05376 on 202 degrees of freedom
## Multiple R-squared:  0.1602, Adjusted R-squared:  0.1436
## F-statistic: 9.636 on 4 and 202 DF, p-value: 3.755e-07
```

```
summary(aov(reg_model))
```

```
##              Df Sum Sq Mean Sq F value    Pr(>F)
## trend          1  0.0702  0.07016   24.279 1.73e-06 ***
## msacsr.ts       1  0.0049  0.00491    1.700  0.19380
## houst.ts        1  0.0248  0.02484    8.596  0.00376 **
## mortgage.ts_diff 1  0.0115  0.01148    3.971  0.04764 *
## Residuals      202  0.5838  0.00289
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```