

## Problem 13

For the given parameters and initial guess, one equilibrium position is given below

```
% Parameters and initial conditions
```

```
rA = [5 0]';  
rB = [-5 0]';  
kA = 50; LA = 10; cA = 0;  
kB = 50; LB = 10; cB = 0;  
m = 1;  
g = 0;  
c = 0;
```

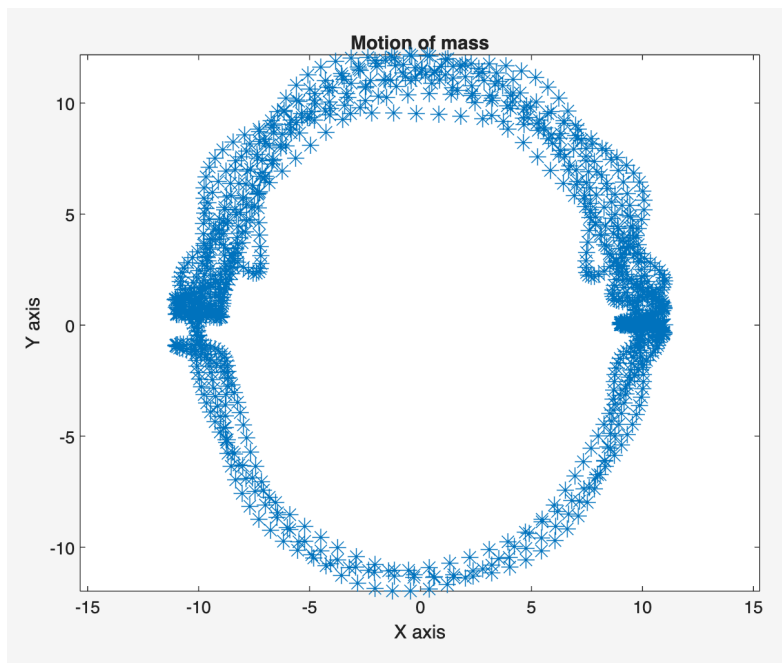
```
% Initial guess
```

```
r0 = [11; 0.001];  
v0 = [0; 0];  
z0 = [r0; v0];
```

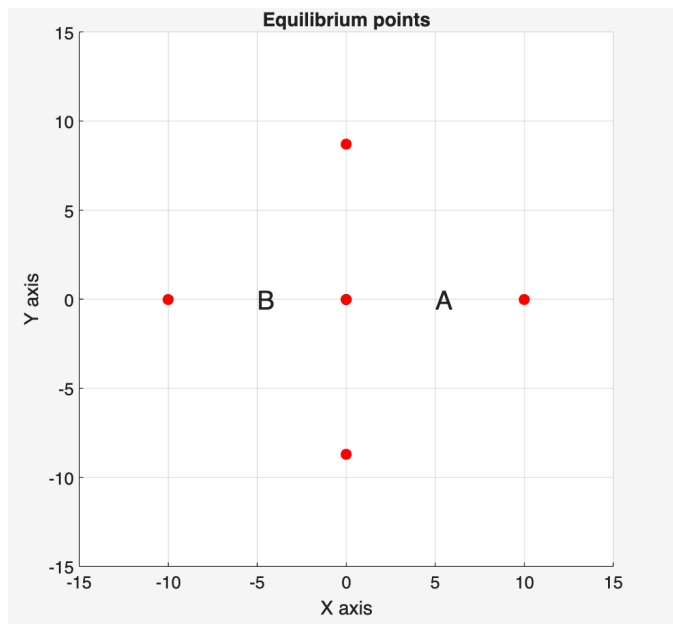
The x and y equilibrium point is

```
10.0000  
0.0000
```

The motion of the system for the given parameters is shown below



## Equilibrium points



Maximum number of equilibrium points found were 5

Number of converged optimisations is 900

The 5 equilibrium points have these [x; y; vx; vy] values

Each row is one root

-10.0000	0	0	0
0	-8.7000	0	0
0	0	0	0
0	8.7000	0	0
10.0000	0	0	0

From the eigenvalues of the Jacobian matrix obtained using finite differences of each state variable, the roots with no positive real eigen values are stable.

Root at location:  $x = -10$   $y = 0$

Eigenvalues:

$0.0000 + 10.0000i$   
 $0.0000 - 10.0000i$   
 $5.7735 + 0.0000i$   
 $-5.7735 + 0.0000i$

Root at location:  $x = 0$   $y = 0$

Eigenvalues:

$0.0000 + 10.0000i$   
 $0.0000 - 10.0000i$   
 $10.0000 + 0.0000i$   
 $-10.0000 + 0.0000i$

Root at location:  $x = 0$   $y = -8.7$

Eigenvalues:

$0.0000 + 5.0087i$   
 $0.0000 - 5.0087i$   
 $0.0000 + 8.6751i$   
 $0.0000 - 8.6751i$

Root at location:  $x = 0$   $y = 8.7$

Eigenvalues:

$0.0000 + 5.0087i$   
 $0.0000 - 5.0087i$   
 $0.0000 + 8.6751i$   
 $0.0000 - 8.6751i$

Root at location:  $x = 10$   $y = 0$

Eigenvalues:

$0.0000 + 10.0000i$

$0.0000 - 10.0000i$

$5.7735 + 0.0000i$

$-5.7735 + 0.0000i$

Thus, the following equilibrium points are stable.

1.  $x = 0$   $y = -8.7$

2.  $x = 0$   $y = 8.7$